

Madrid
09/06/2015

Dark Radiation in Sequestered String Models

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University of Bologna
and INFN



Based on:

- 1) "Sequestered dS String Scenarios: Soft terms", L. Aparicio, M. Cicoli, S. Krippendorff, A. Maharana, FM, F. Quevedo, [1409.1931]
- 2) "General Analysis of DR in Sequestered String Models", M. Cicoli, FM, [to appear]

14th String Pheno 2015

Instituto de Física Teórica UAM-CSIC



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Física
Teórica
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SEQUESTERED STRING MODELS

M. Cicoli's talk
arXiv:1409.1931

(dS vacua, LVS moduli stabilization, visible sector at singularities)

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$$m_0 \simeq B\hat{\mu} \simeq M_a \approx 1 \text{ TeV}$$

SPLIT-SUSY scenario

$$M_a \approx 1 \text{ TeV}$$

$$m_0 \simeq B\hat{\mu} \approx 10^7 \text{ GeV}$$

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➤ Gravitino mass: $m_{3/2} \simeq 10^{10} \text{ GeV}$

$$m_{\text{soft}} \ll m_{3/2}$$

(sequestering)

➤ Lightest modulus: $m_v \simeq 10^7 \text{ GeV}$

$$m_v \gg 50 \text{ TeV}$$

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Q: which kind of cosmology can arise from them?

L. Aparicio's talk
[Aparicio et al., 2015]

Dark Radiation: what is it?

Relativistic particles in the hidden sector

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Relativistic particles in the hidden sector

energy density of relativistic
d.o.f. after e^+e^- annihilation

$$\rho_{\text{rel}} = \rho_\gamma \left(1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} N_{\text{eff}} \right)$$

effective number of neutrino species:

$$N_{\text{eff}} = N_{\text{eff,SM}} + \Delta N_{\text{eff}}$$
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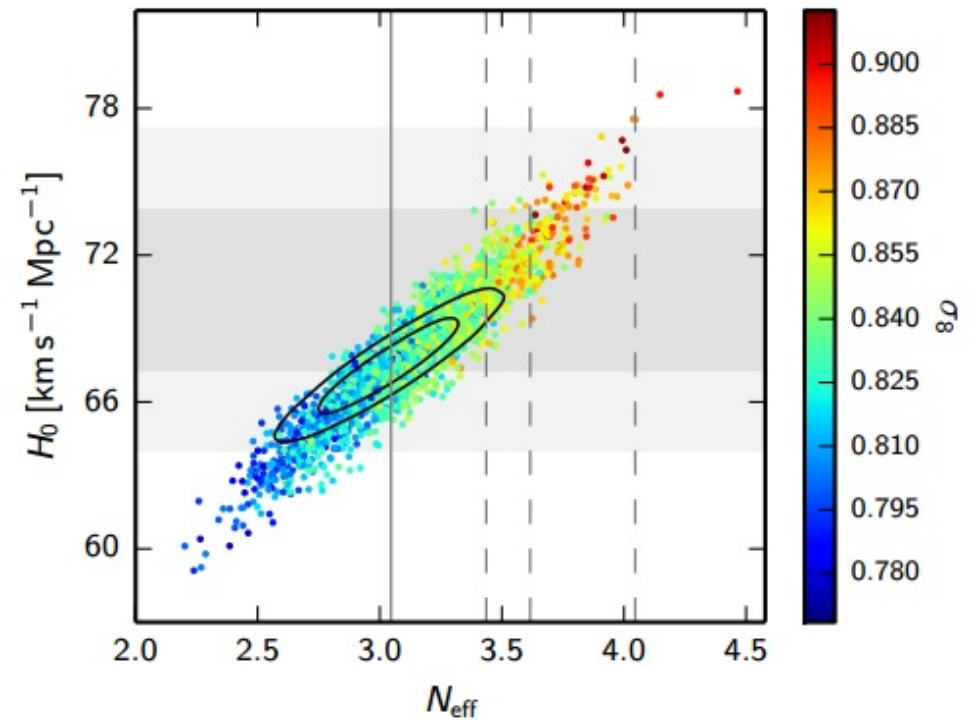
$$\Delta N_{\text{eff}} > 0 \longrightarrow$$

**DARK
RADIATION**

experimental constraints coming from BBN and CMB observations:

larger $\rho_{\text{rel}} \longrightarrow$ larger $H \longrightarrow$ can modify CMB and BBN predictions

Planck 2015: there is no need for dark radiation.

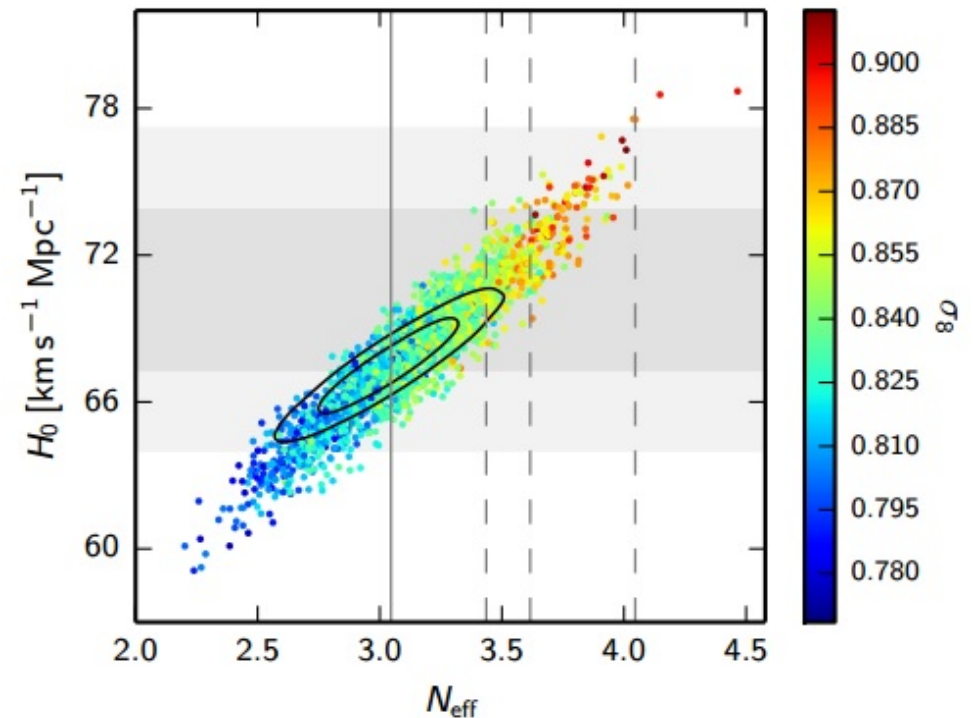


[Planck collaboration 2015, arXiv:1502.01589]

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BUT

- There is a positive correlation between H_0 and ΔN_{eff} .
- The value of H_0 used by Planck is in tension with direct measurements by the HST.
- Example reported by Planck: $\Delta N_{\text{eff}} = 0.39$.

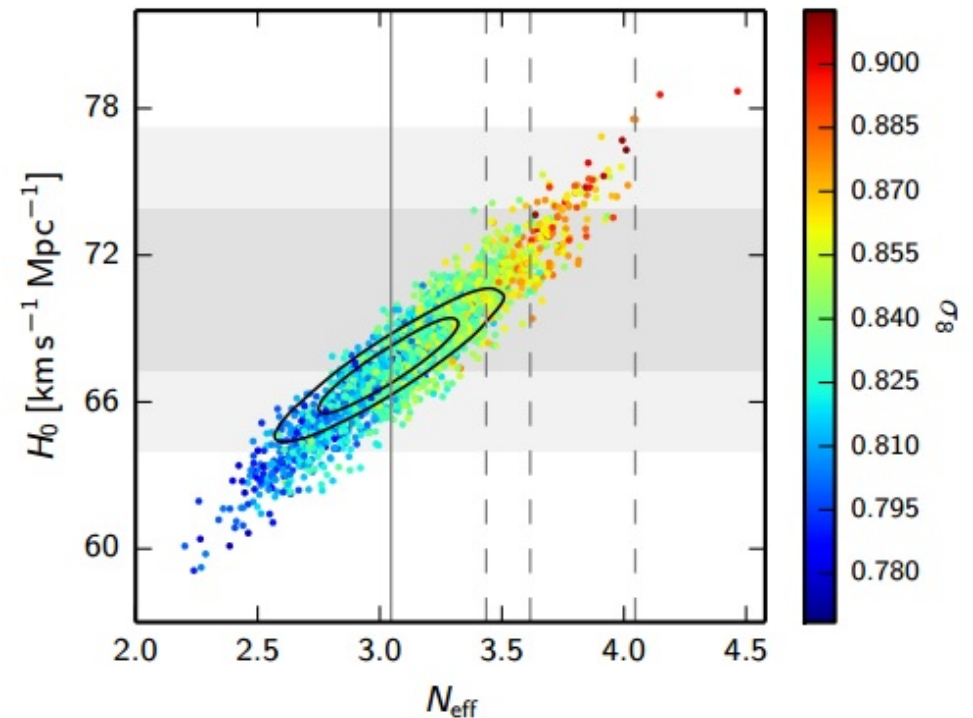


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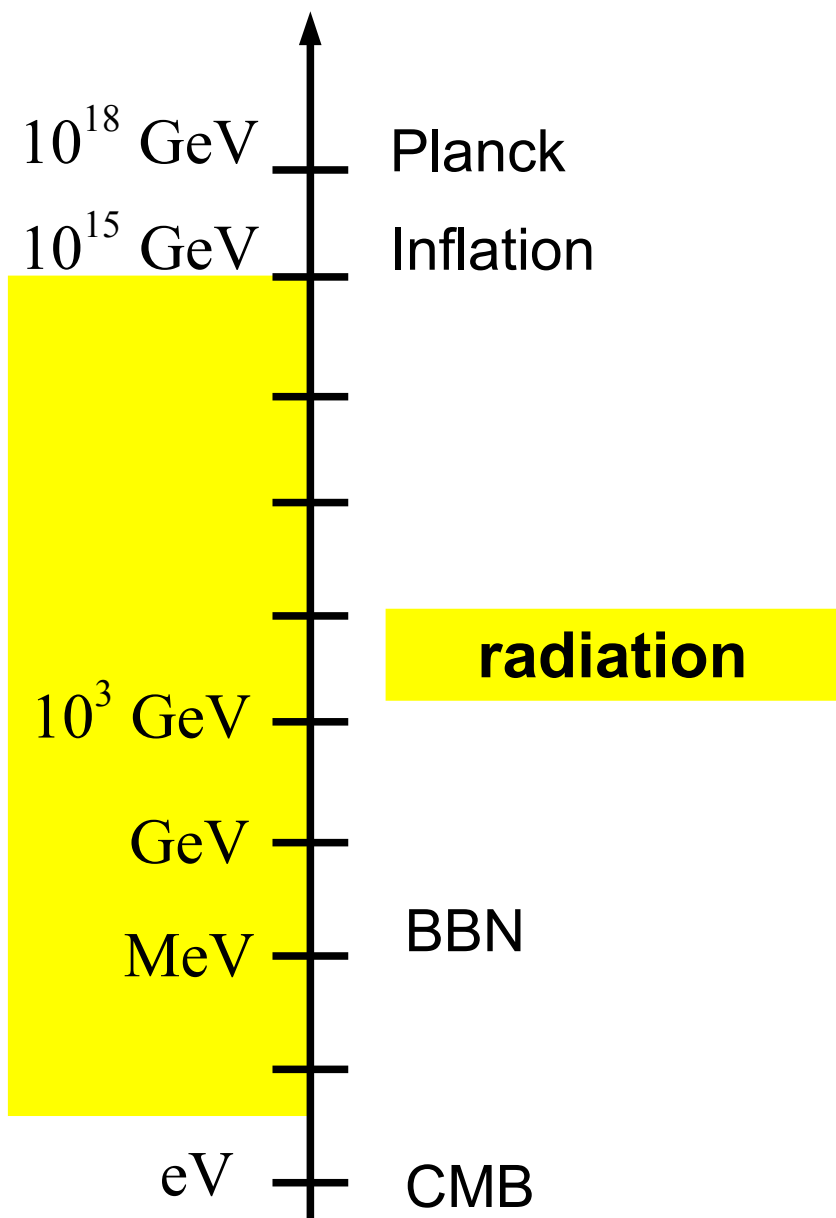
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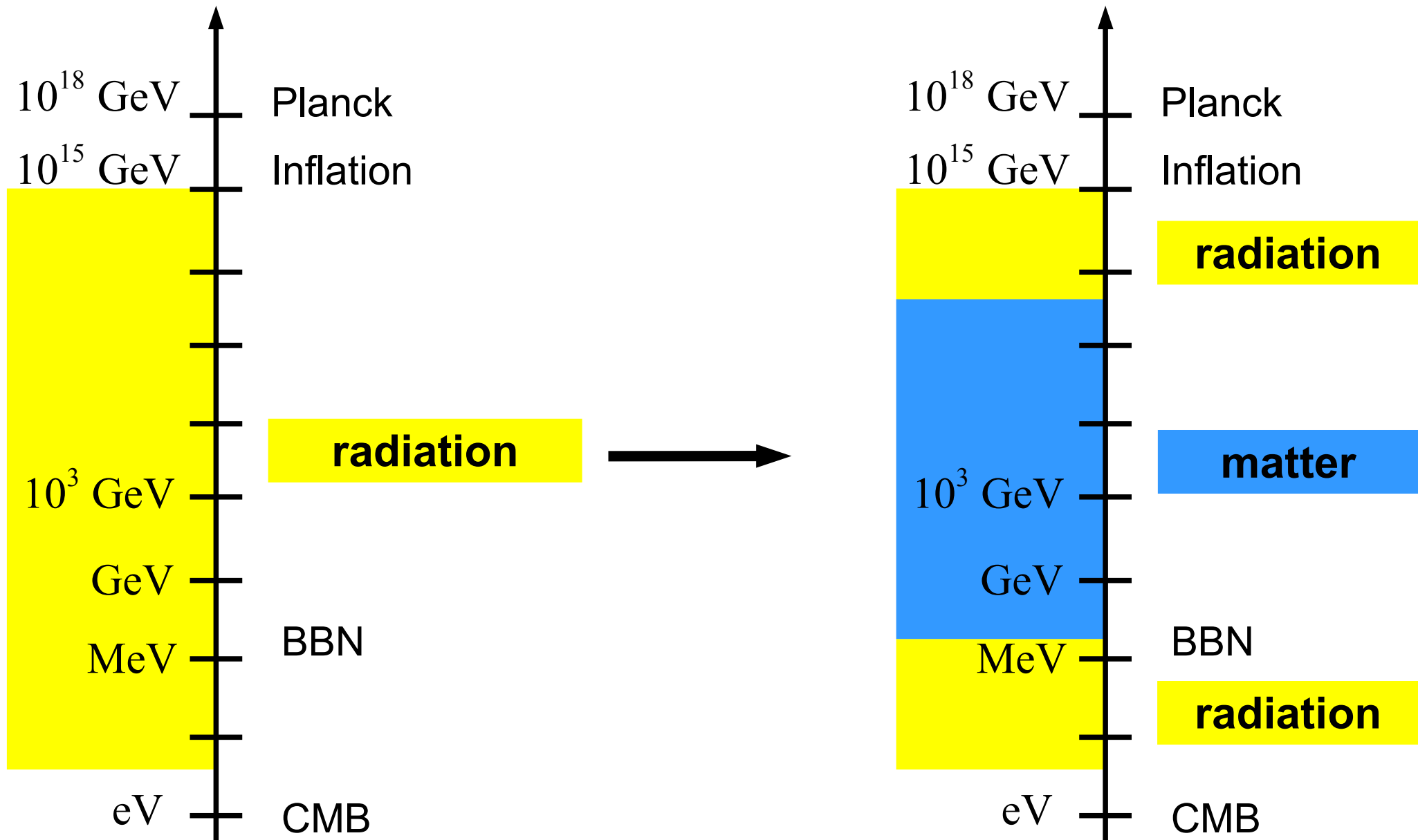
In this talk I will consider $\Delta N_{\text{eff}} \leq 0.5$ as a reference upper bound on ΔN_{eff} .

Thermal History



The presence of moduli can
modify this standard picture

Thermal History

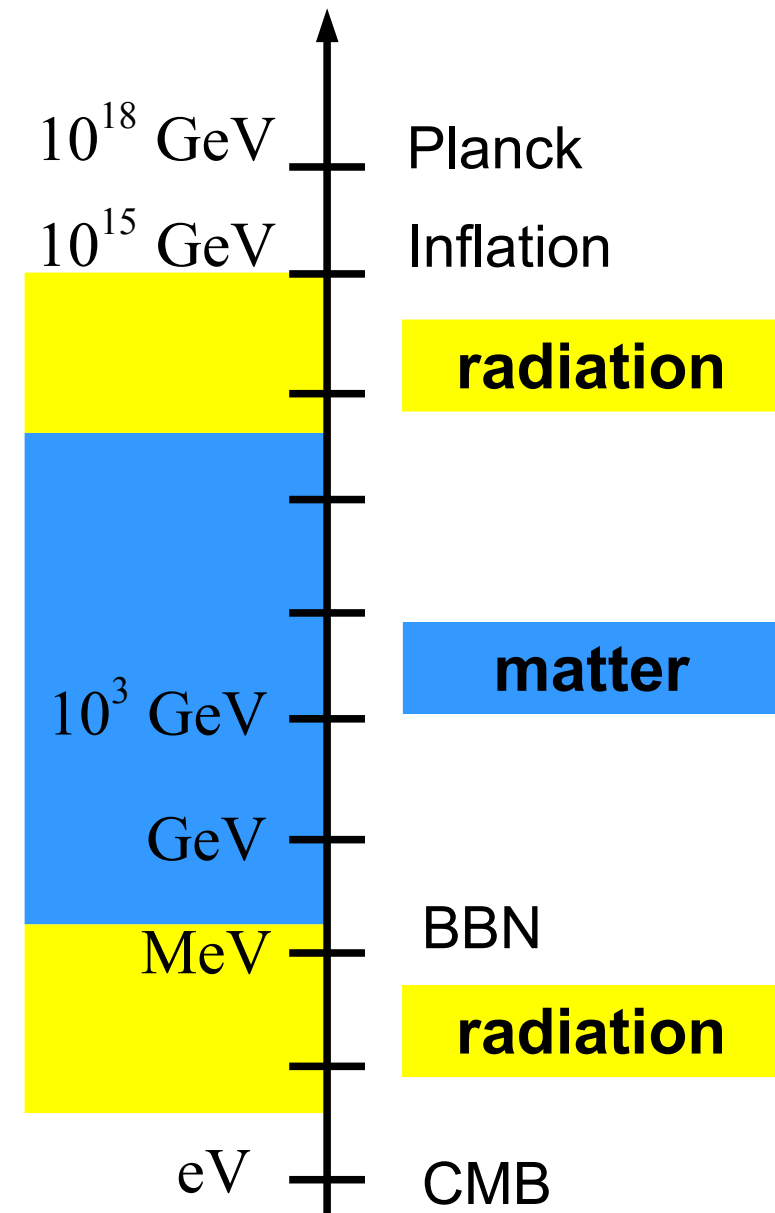


Non-thermal history

- Quantum corrections displace moduli during inflation

$$V = \frac{1}{2} m_\phi^2 \phi^2 + H^2 (\phi - \phi_0)^2 \quad m_\phi \ll H_{\text{inf}}$$

E.o.m. $\ddot{\phi} + 3 H \dot{\phi} + V'(\phi) = 0$



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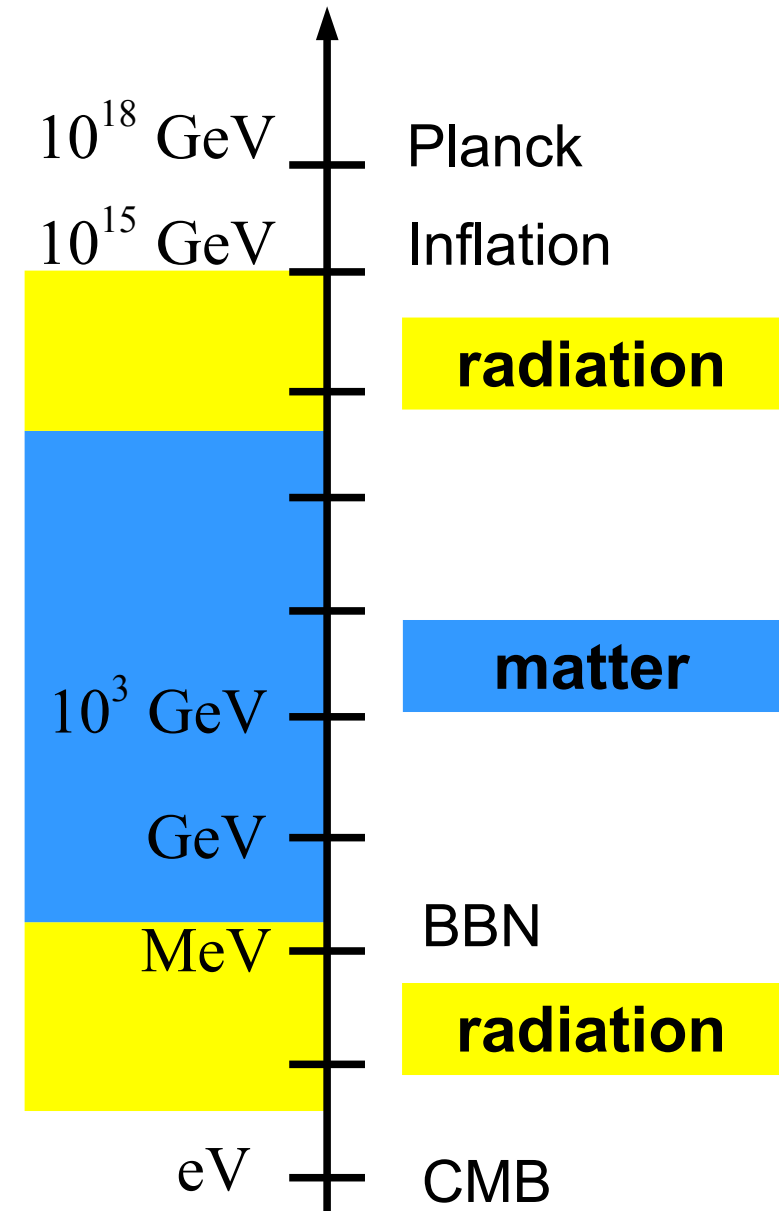
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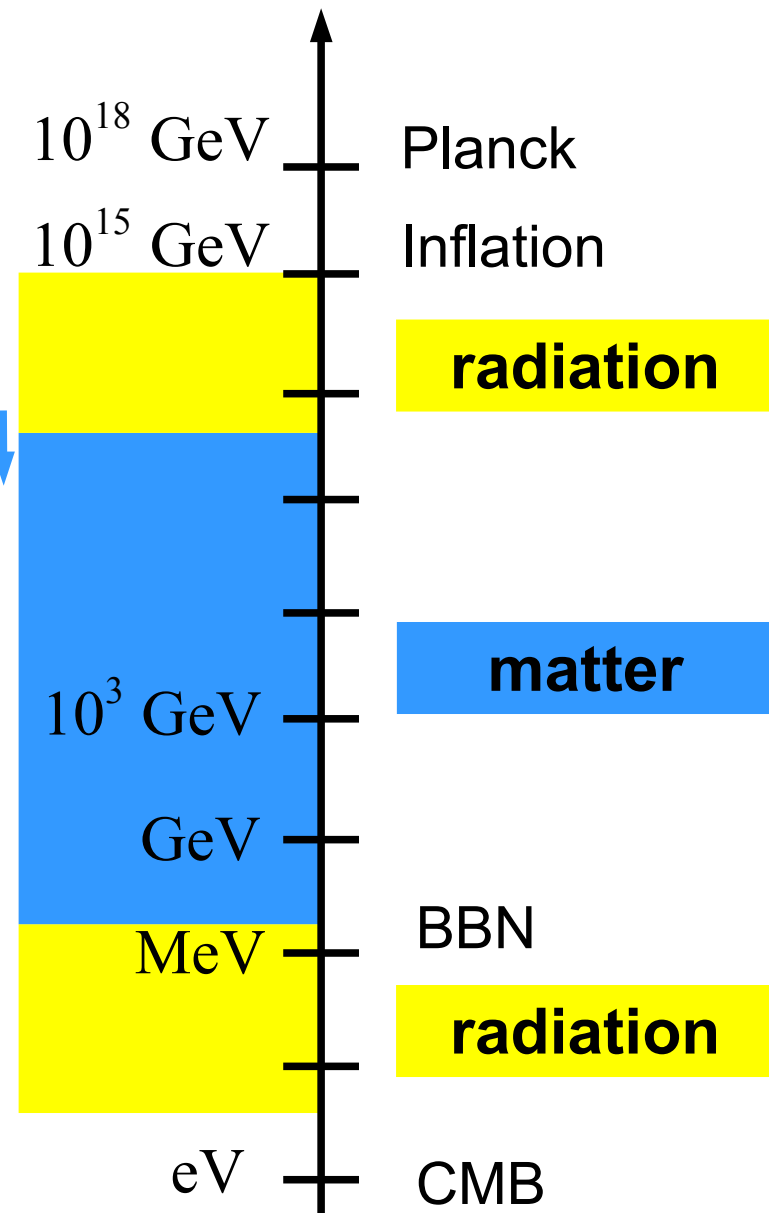
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→ matter domination

OSCILLATIONS ↓



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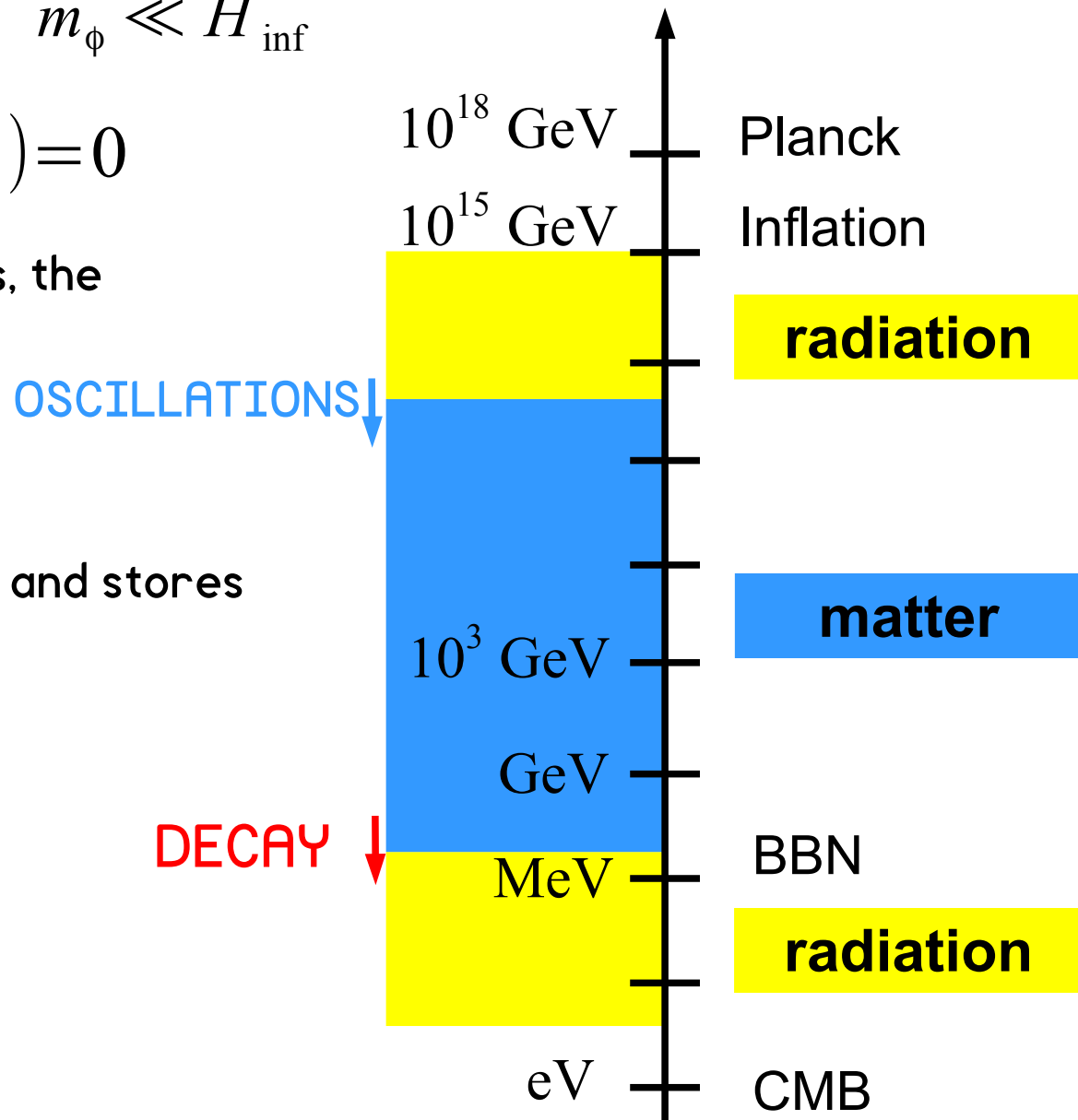
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- Decay when: $H \approx \Gamma \approx \frac{m_\phi^3}{M_p^2}$



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[Allahverdi et al., 2014]

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1) τ_b perturbative:	$m_{\tau_b} \simeq M_p / V^{3/2}$
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$$\mathcal{L}_{\text{int}} \supset -\sqrt{\frac{2}{3}} \delta\Phi \partial_\mu a_b \partial^\mu a_b$$

$$\text{CN: } \Phi = \sqrt{\frac{3}{2}} \log \tau_b \quad a_b = \sqrt{\frac{3}{2}} \frac{\psi_b}{\langle \tau_b \rangle}$$

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→ Decay width $\Phi \rightarrow a_b a_b$:

$$\Gamma = \frac{1}{48 \pi} \frac{m_\Phi^3}{M_p^2} \equiv \Gamma_0$$

Decay channels into the visible sector

- Decay into visible
gauge bosons
 $\Phi \rightarrow A A$

$$\Gamma_{\Phi \rightarrow AA} = \left(\frac{\alpha_{\text{SM}}}{4\pi} \right)^2 \Gamma_0 \ll \Gamma_0$$

always loop
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(mass-terms)

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$$\Gamma_{\Phi \rightarrow HH} \simeq f(Z, m_H, B\hat{\mu}) \Gamma_0$$

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$$\text{Total decay rate: } \Gamma_{\text{tot}} = (1 + c_{\text{vis}}) \Gamma_0$$

Sequestered CMSSM

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➤ DR produced: $\Delta N_{\text{eff}} = \frac{43}{7} \frac{1}{c_{\text{vis}}} \left[\frac{g(T_{\text{dec}})}{g(T_{\text{reheat}})} \right]^{1/3}$

$$g(T_{\text{dec}}) \simeq 10.75$$

$$g(T_{\text{reheat}}) \simeq 86.25$$

$$0.7 \text{ GeV} \leq T_{\text{reheat}} \leq 13 \text{ GeV}$$

$$\xrightarrow{Z=1} 1.63 \leq \Delta N_{\text{eff}} \leq 1.74$$

[Cicoli, Conlon, Quevedo, 2012]

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[Angus, Conlon et al., 2013]

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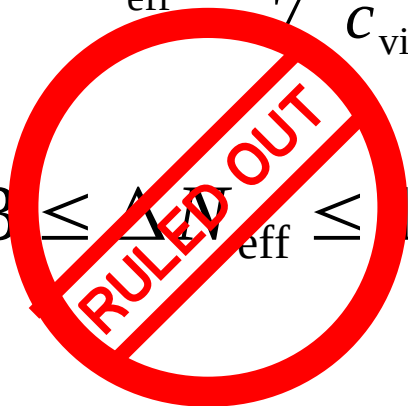
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Decay channels:

$\Phi \rightarrow C \bar{C}$		mass		$\Phi \rightarrow H_u H_d$	GM & $B\hat{\mu}$ -terms
$\Phi \rightarrow H_{u/d} \bar{H}_{u/d}$		terms			

Sketch of the computation:

- Lagrangian depends on Φ : $\mathcal{L}(\Phi) = \mathcal{L}_{\text{kin}}(\Phi) - V(\Phi)$
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- Start from the Kähler potential which determines the kinetic terms:

$$K = -2 \log \mathcal{V} + \frac{2}{T_b + \bar{T}_b} \sum_{\alpha} C^{\alpha} \bar{C}^{\alpha} + \left(\frac{2Z}{T_b + \bar{T}_b} H_u H_d + \text{h.c.} \right) \longrightarrow \mathcal{L}_{\text{kin}}(\Phi)$$

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- The scalar potential takes the form:

$$V = V_{\text{LVS}} + \frac{m_0^2}{2} \sum_{\alpha} \left(\sigma^{\alpha 2} + \chi^{\alpha 2} \right) + \frac{1}{2} \left(\hat{\mu}^2 + m_0^2 \right) \sum_{i=1}^8 h_i^2 + B \hat{\mu} (h_1 h_4 - h_2 h_3 + h_6 h_7 - h_5 h_8)$$

➤ Expand the soft-terms which depend on the volume,

for example:
$$m_0^2(\Phi) = m_0^2 \left(1 - \frac{9}{2} \sqrt{\frac{2}{3}} \delta \Phi \right)$$

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for example:
$$m_0^2(\Phi) = m_0^2 \left(1 - \frac{9}{2} \sqrt{\frac{2}{3}} \delta \Phi \right)$$

- Integrate by parts and use the e.o.m.:

$$\partial^2 \sigma^\alpha = -m_0^2 \sigma^\alpha \quad \partial^2 \chi^\alpha = -m_0^2 \chi^\alpha \quad \partial^2 h_1 = -(\hat{\mu}^2 + m_0^2) h_1 - B \hat{\mu} h_4 \quad \dots$$

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- Interaction lagrangian:
(neglecting the $\hat{\mu}$ -term)
$$\mathcal{L}_{\text{int}} = \frac{7}{2\sqrt{6}} \left[m_0^2 \delta \Phi \sum_{i=1}^8 h_i^2 + m_0^2 \delta \Phi \sum_{\alpha} C^\alpha C^\alpha \right] + \left(\frac{7}{\sqrt{6}} B \hat{\mu} + Z m_\Phi^2 \right) \delta \Phi (h_1 h_4 - h_2 h_3 + h_6 h_7 - h_5 h_8)$$

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- The total decay rate into the visible sector is given by:

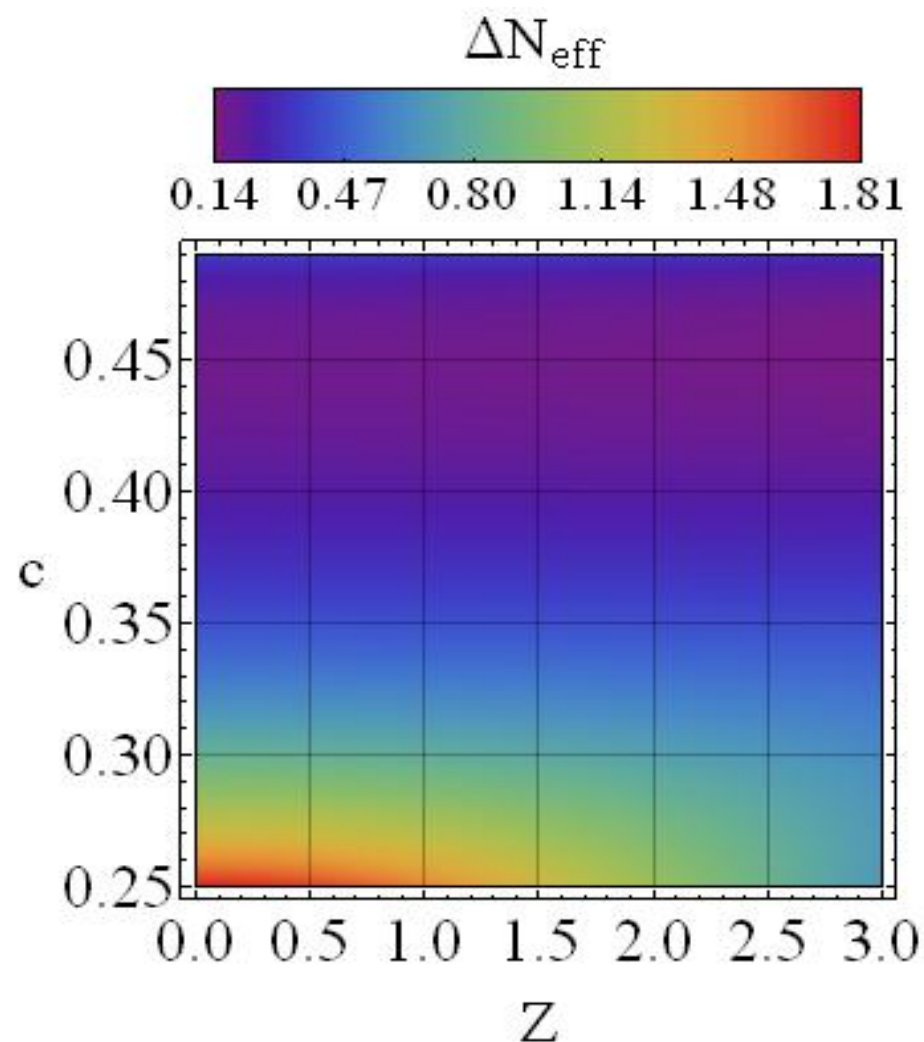
$$B \hat{\mu} = Z m_0^2 \quad c = \frac{m_0}{m_\Phi}$$

$$c_{\text{vis}} = \left[2 Z^2 (7 c^2 - 1)^2 + 49 c^4 \left(1 + \frac{2 N}{4} \right) \right] \sqrt{1 - 4 c^2}$$

$2 N = 90$ squarks and sleptons d.o.f. in the MSSM

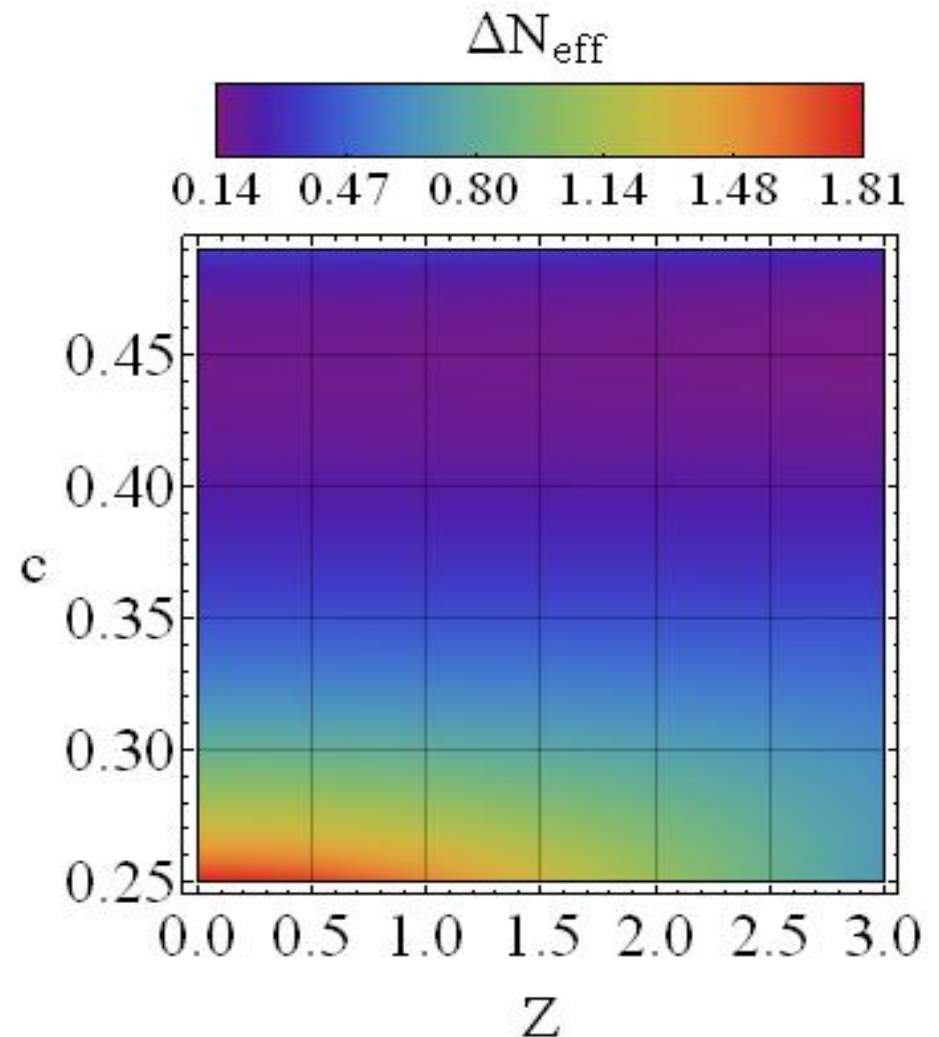
Results

- A large region of the parameter space admits values of $\Delta N_{\text{eff}} \leq 0.5$.
- Most of the suppression is due to the decay into scalars.



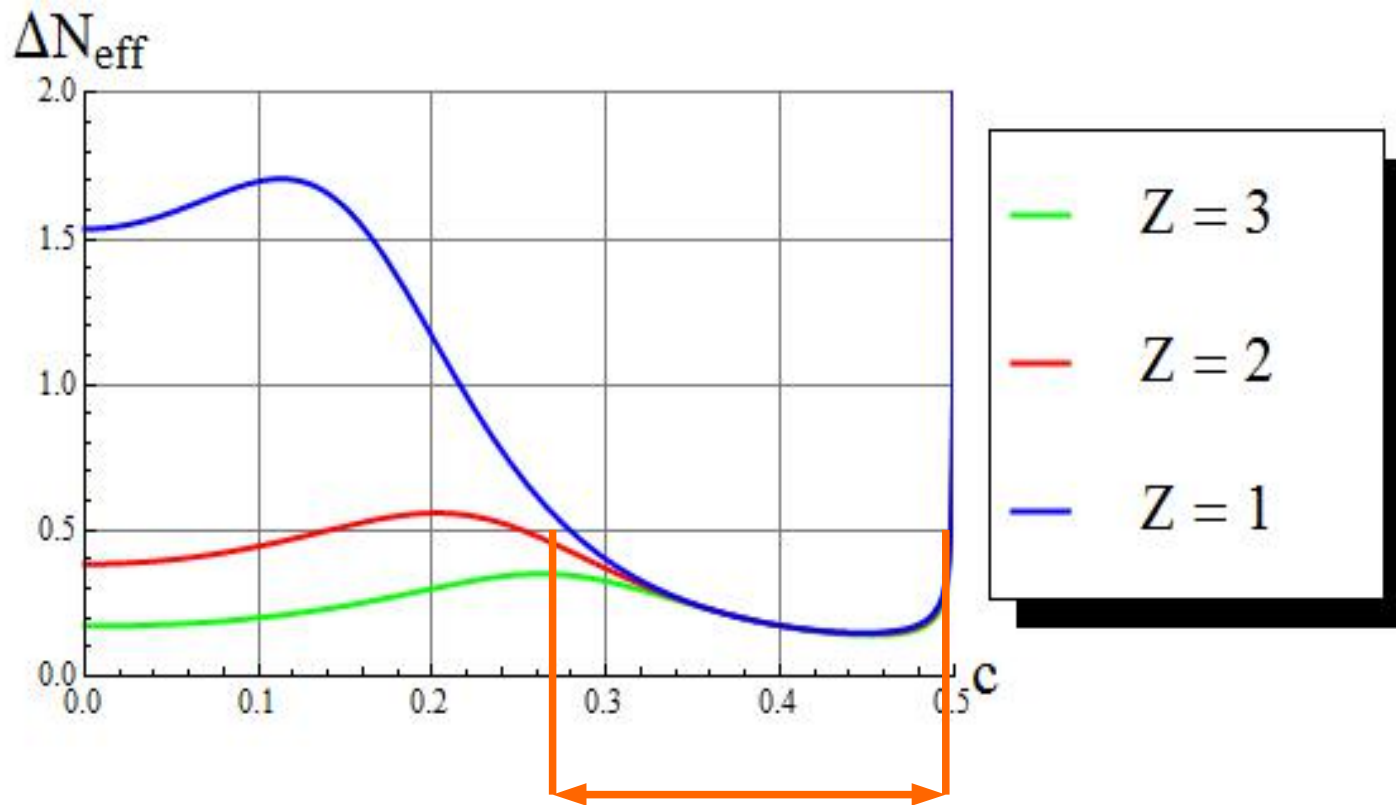
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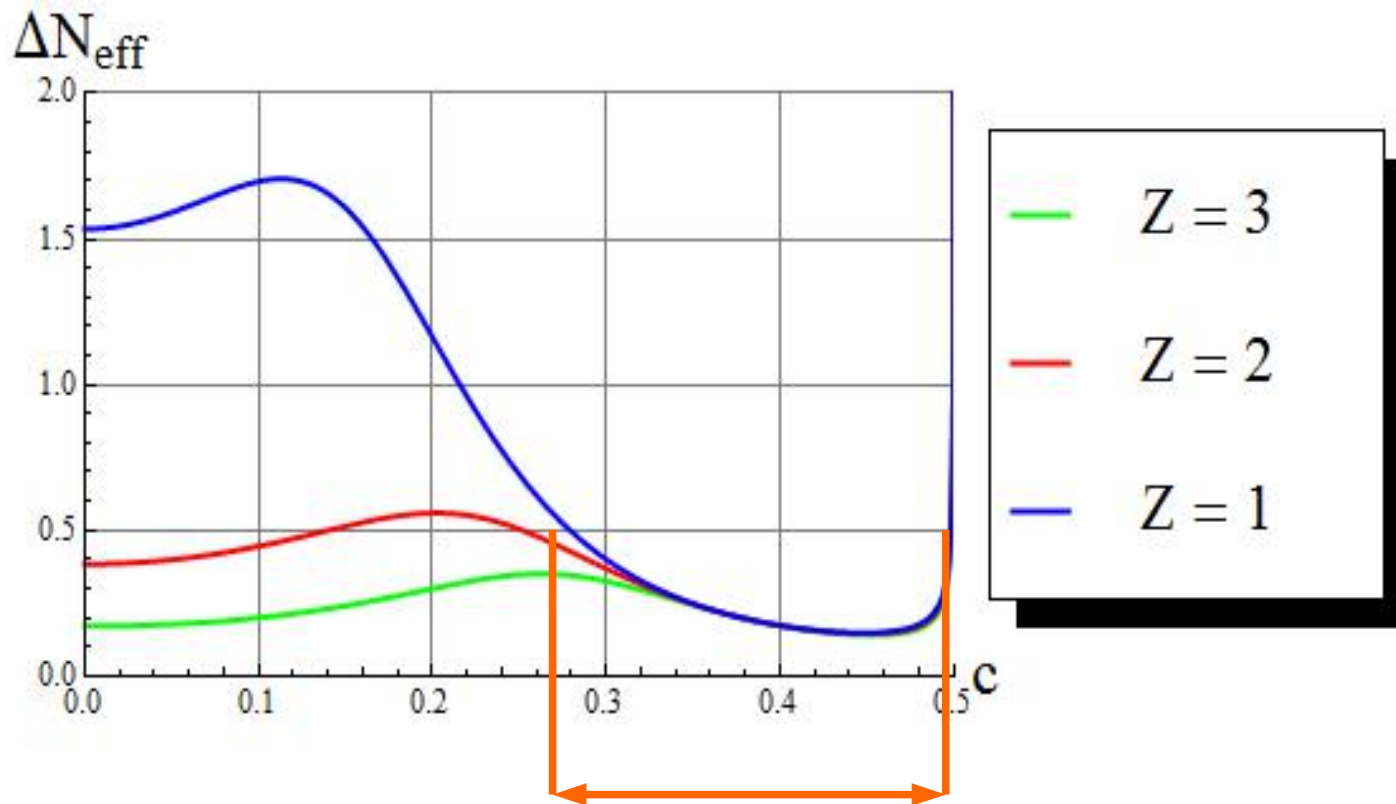
For $Z = 1$, $m_0 = 10^7$ GeV and $c = 0.45$ we get $\Delta N_{\text{eff}} = 0.14$

It is not a fine-tuned result!



For $Z = 1$ all these values of c : $0.28 < c < 0.49$
correspond to $\Delta N_{\text{eff}} \leq 0.5$.

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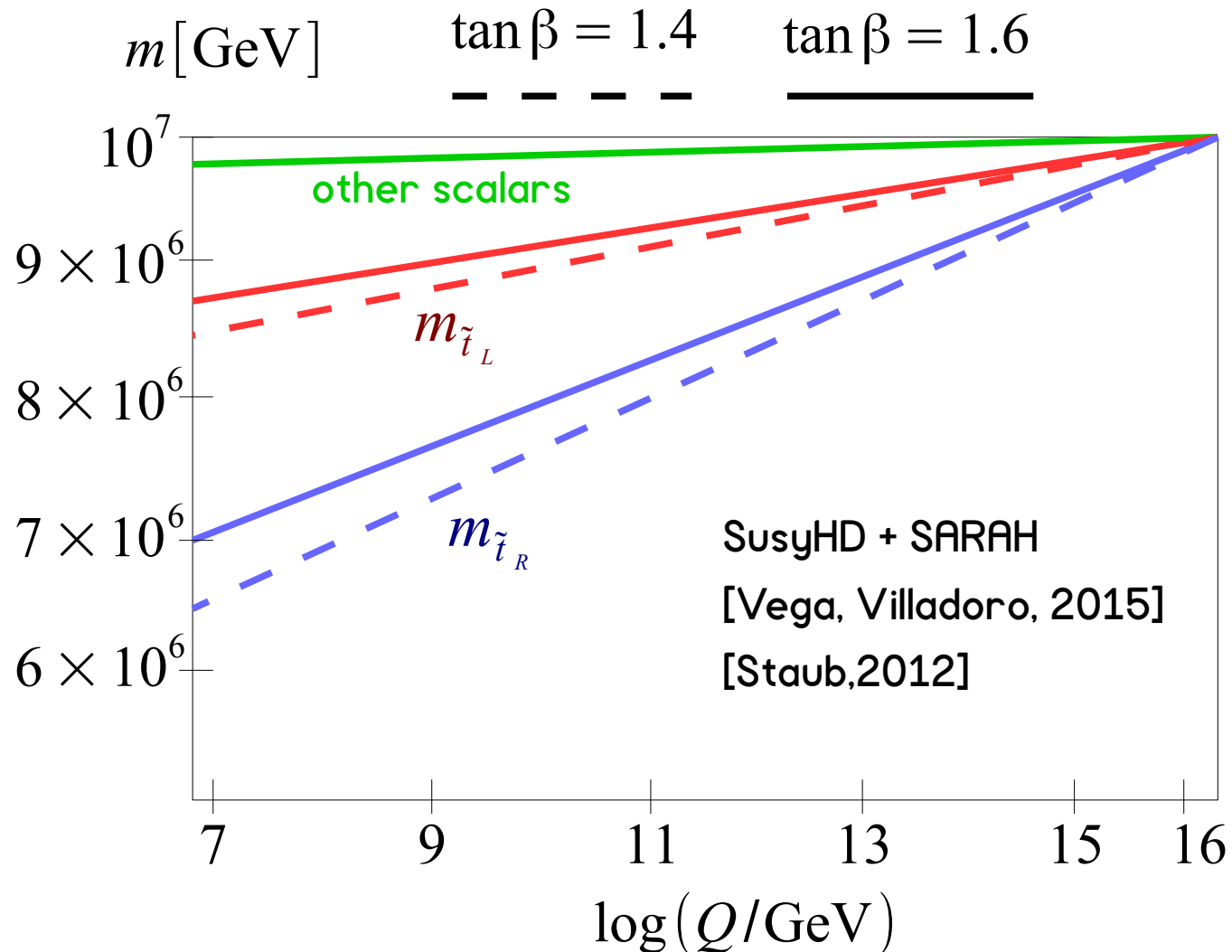


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Q: is the result modified by taking into account the RG flow?

The result is essentially independent of the RG running.

- Scalars don't run, except for $m_{\tilde{t}_L}$ and $m_{\tilde{t}_R}$.
- We take the running of $B\hat{u}$ and Z into account.
- We didn't study the EWSB so far.



For $m_\Phi = 2.2 \times 10^7 \text{ GeV}$ we get $\Delta N_{\text{eff}} \simeq 0.16$

Conclusions and next steps

We have shown that the the amount of DR produced in Split-SUSY, LVS sequestered string models with all moduli stabilized and dS vacua is generically within the current experimental bounds, if the decay into scalar fields is kinematically allowed.

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We have shown that the the amount of DR produced in Split-SUSY, LVS sequestered string models with all moduli stabilized and dS vacua is generically within the current experimental bounds, if the decay into scalar fields is kinematically allowed.

- EWSB has to be analyzed carefully.
- Correlation with DM production.

Thank you!

Yukawas: $\hat{Y}_{\alpha\beta\gamma} = e^{K/2} \frac{Y_{\alpha\beta\gamma}}{\sqrt{\tilde{K}_\alpha \tilde{K}_\beta \tilde{K}_\gamma}}$

Locality of Yukawa couplings requires: $\tilde{K} = e^{K/3}$

We parameterize the Kähler matter metric $\tilde{K} = \frac{f_\alpha}{\mathcal{V}^{2/3}} \left(1 - c_s \frac{\xi s^{3/2}}{\mathcal{V}} \right)$

Scalar masses: $m_0^2 = \frac{15}{2} \left(c_s - \frac{1}{3} \right) \frac{m_{3/2}^2 \tau_s^{3/2}}{\mathcal{V}} \quad c_s \neq \frac{1}{3}$

Volume modulus mass: $m_\Phi^2 = \# \frac{m_{3/2}^2 \tau_s^{1/2}}{\mathcal{V}}$

In LVS: $\tau_s \simeq \log \left(\frac{\mathcal{V}}{W_0} \right) \gg 1 \longrightarrow$ Typically: $\frac{m_0^2}{m_\Phi^2} > \frac{1}{4}$

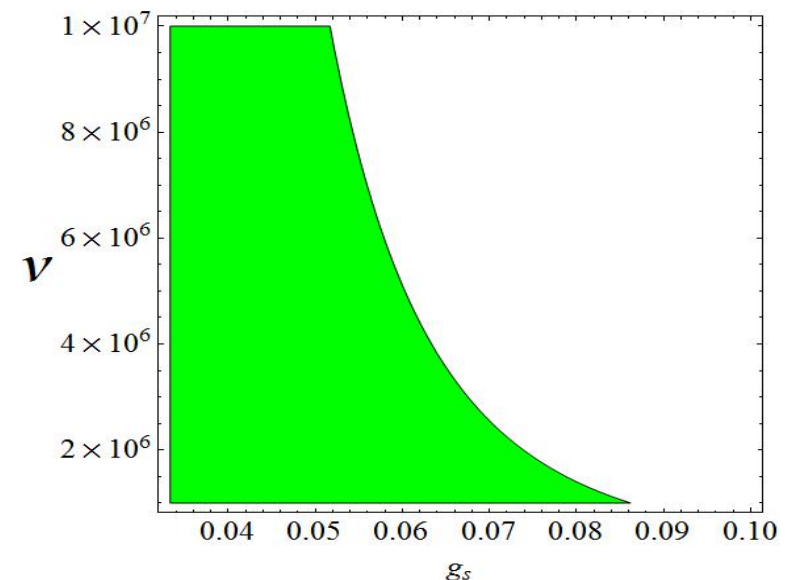
Introduce SL corrections into the Kähler potential: $\delta K_{\text{loop}} = \frac{g_s}{\nu^{2/3}}$

Matter metric gets modified: $\tilde{K} = \frac{1}{\nu^{2/3}} \left(1 - c_s \frac{\xi s^{3/2}}{\nu} - \frac{c_{\text{loop}} g_s}{\nu^{2/3}} \right)$

Scalar masses take the form:

$$m_0^2 = \left(\frac{15}{2} \left(c_s - \frac{1}{3} \right) \frac{\tau_s^{3/2}}{\nu} - \left(c_{\text{loop}} - \frac{1}{3} \right) \frac{2 g_s}{\nu^{2/3}} \right) m_{3/2}^2 \quad \tau_s = \left(\frac{\xi}{2} \right)^{2/3} \frac{1}{g_s}$$

→ Enlarge the region
of the parameter
space where the
decay is possible:
i.e. for $c_s = 1/3$
and $c_{\text{loop}} = 0$



Canonically normalized fields:

$$h_1 = \frac{\Re H_u^+}{\sqrt{\langle \tau_b \rangle}} \quad h_2 = \Re \frac{H_u^0}{\sqrt{\langle \tau_b \rangle}} \quad h_3 = \Re \frac{H_d^0}{\sqrt{\langle \tau_b \rangle}} \quad h_4 = \Re \frac{H_d^-}{\sqrt{\langle \tau_b \rangle}}$$

$$h_5 = \Im \frac{H_u^+}{\sqrt{\langle \tau_b \rangle}} \quad h_6 = \Im \frac{H_u^0}{\sqrt{\langle \tau_b \rangle}} \quad h_7 = \Im \frac{H_d^0}{\sqrt{\langle \tau_b \rangle}} \quad h_8 = \Im \frac{H_d^-}{\sqrt{\langle \tau_b \rangle}}$$

$$\sigma_\alpha = \frac{\Re C^\alpha}{\langle \tau_b \rangle} \quad \chi_\alpha = \frac{\Im C^\alpha}{\sqrt{\langle \tau_b \rangle}}$$