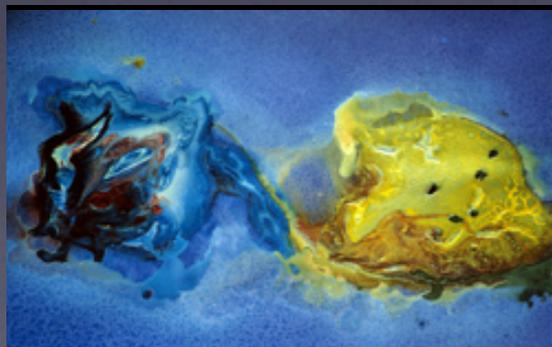


Heavy Quarkonium with Effective Field Theories



NORA BRAMBILLA

- the physics of quarkonium and its relevance to the physics of Standard Model and beyond
- the state of the art theory tools confronted to experimental data
- experimental/theoretical challenges and opportunities

QCD and strongly coupled gauge theories: challenges and perspectives

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We highlight the progress, current status, and open challenges of QCD-driven physics, in theory and in experiment. We discuss how the strong interaction is intimately connected to a broad sweep of physical problems, in settings ranging from astrophysics and cosmology to strongly-coupled, complex systems in particle and condensed-matter physics, as well as to searches for physics beyond the Standard Model. We also discuss how success in describing the strong interaction impacts other fields, and, in turn, how such subjects can impact studies of the strong interaction. In the course of the work we offer a perspective on the many research streams which flow into and out of QCD, as well as a vision for future developments.

1. Overview ¹

1.1. Readers' guide

2. The nature of QCD ²

2.1. Broader themes in QCD

2.2. Experiments addressing QCD

2.3. Theoretical tools for QCD

2.4. Fundamental parameters of QCD

9. Strongly coupled theories and conformal symmetry ⁹

9.1. New exact results in quantum field theory

9.1.1. Integrability of planar $\mathcal{N} = 4$ SYM

9.1.2. Scattering amplitudes

9.1.3. Generalized unitarity and its consequences

9.1.4. Supersymmetric gauge theories

9.1.5. Conformal field theories

9.1.6. 3d CFTs and higher spin symmetry

9.2. Conformal symmetry, strongly coupled theories and new physics

9.2.1. Theory of the conformal window

9.2.2. Lattice, AdS/CFT, and the electroweak symmetry breaking

9.3. Electroweak symmetry breaking

9.3.1. Strongly coupled scenarios for EWSB

9.3.2. Conformal symmetry, the Planck scale, and naturalness

9.4. Methods from high-energy physics for strongly coupled, condensed matter systems

9.4.1. Lattice gauge theory results

9.4.2. Gauge-gravity duality results

9.5. Summary and future prospects

3. Light quarks ³

3.1. Introduction

3.2. Hadron structure

3.2.1. Parton distribution functions in QCD

3.2.2. PDFs in the DGLAP approach

3.2.3. PDFs and nonlinear evolution equations

3.2.4. GPDs and tomography of the nucleon

3.2.5. Hadron form factors

3.2.6. The proton radius puzzle

3.2.7. The pion and other pseudoscalar mesons

3.3. Hadron spectroscopy

3.3.1. Lattice QCD

3.3.2. Continuum methods

6. Deconfinement ⁶

6.1. Mapping the QCD phase diagram

6.1.1. Precision lattice QCD calculations at finite-temperature

6.1.2. A critical point in the QCD phase diagram?

6.1.3. Experimental exploration of the QCD phase diagram

6.2. Near-equilibrium properties of the QGP

6.2.1. Global event characterization

6.2.2. Azimuthal anisotropies

6.2.3. Transport coefficients & spectral functions: theory

6.3. Approach to equilibrium

6.3.1. Thermalization at weak and strong coupling

6.3.2. Multiplicities and entropy production

6.4. Hard processes and medium induced effects

6.4.1. Introduction

6.4.2. Theory of hard probes

Nuclear matter effects in pA collisions
Energy loss theory

Quarkonium interaction at finite temperature and quarkonium suppression

6.4.3. Experimental results on hard probes

High p_T observables

Heavy flavors

6.5. Reference for heavy-ion collisions

6.6. Lattice QCD, AdS/CFT and perturbative QCD

6.6.1. Weakly and strongly coupled (Super) Yang-Mills theories

6.6.2. Holographic breaking of scale invariance and IHQCD

8. Vacuum structure and infrared QCD: confinement and chiral symmetry breaking ⁸

8.1. Confinement

8.2. Functional methods

8.3. Mechanism of chiral symmetry breaking

8.4. Future Directions

5. Searching for new physics with precision measurements and computations ⁵

5.1. Introduction

5.2. QCD for collider-based BSM searches

5.2.1. Theoretical overview: factorization

5.2.2. Outcomes for a few sample processes

5.2.3. LHC results: Higgs and top physics

5.2.4. Uncertainties from nucleon structure and PDFs

5.2.5. Complementarity with low-energy probes

5.3. Low-energy framework for the analysis of BSM effects

5.4. Permanent EDMs

5.4.1. Overview

5.4.2. Experiments, and their interpretation and implications

5.4.3. EFTs for EDMs: the neutron case

5.4.4. Lattice-QCD matrix elements

5.5. Probing non- $(V - A)$ interactions in beta decays

5.5.1. The role of the neutron lifetime

5.6. Broader applications of QCD

5.6.1. Determination of the proton radius

5.6.2. Dark-matter searches

5.6.3. Neutrino physics

5.6.4. Cold nuclear medium effects

5.6.5. Gluonic structure

5.7. Quark flavor physics

5.7.1. Quark masses and charges

5.7.2. Testing the CKM paradigm

5.7.3. New windows on CP and T violation

5.7.4. Rare decays

5.8. Future Directions

4. Heavy quarks ⁴

4.1. Methods

4.1.1. Nonrelativistic effective field theory

4.1.2. The progress on NRQCD factorization

4.1.3. Lattice gauge theory

4.2. Heavy semileptonic decays

4.2.1. Exclusive and inclusive D decays

4.2.2. Exclusive B decays

4.2.3. Inclusive B decays

4.2.4. Rare charm decays

4.3. Spectroscopy

4.3.1. Experimental tools

4.3.2. Heavy quarkonia below open flavor thresholds

Quarkonium **today** is
a golden system to study strong
interactions

many experimental data and opportunities

Quarkonium today is
a golden system to study strong
interactions

new theoretical tools:
Effective Field Theories (EFTs) of QCD
and progress in lattice QCD

In the near past data came from:

B-FACTORIES (Belle, BABAR): Heavy Mesons Factories

CLEO-c BES tau charm factories

CLEO-III bottomonium factory

Fermilab CDF, D0, E835

Hera RHIC (Star, Phenix), NA60

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Discovery of New States, New
Production Mechanisms, Exotics, New
decays and transitions, Precision and
high statistics data

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BESIII at IHEP

CMS ATLAS LHCb

ALICE at CERN

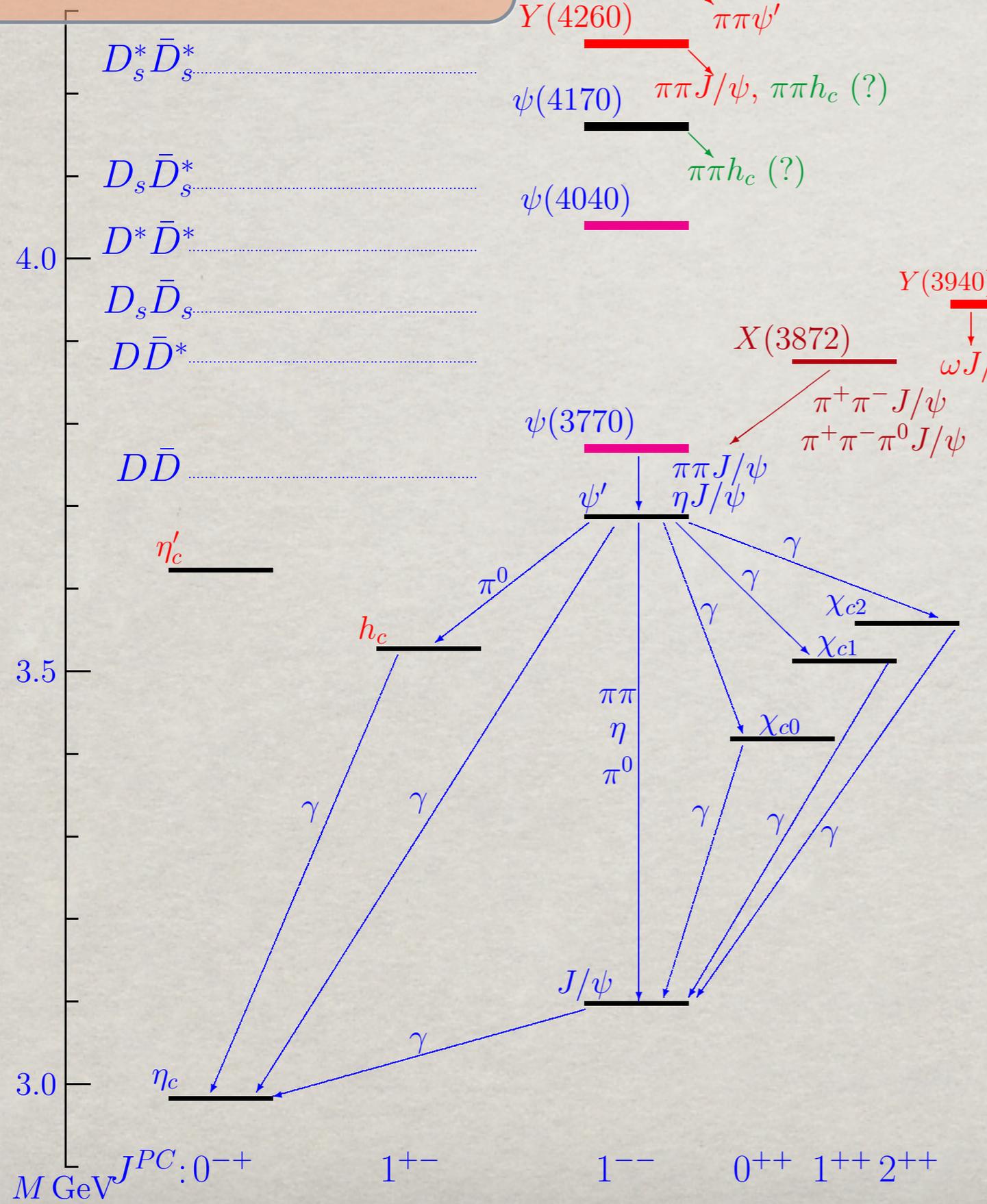
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at FAIR

Charmonium the present revolution

DØ



CLEO



M GeV $J^{PC}: 0^{--} \quad 1^{+-} \quad 1^{--} \quad 0^{++} \quad 1^{++} \quad 2^{++} \quad ?$

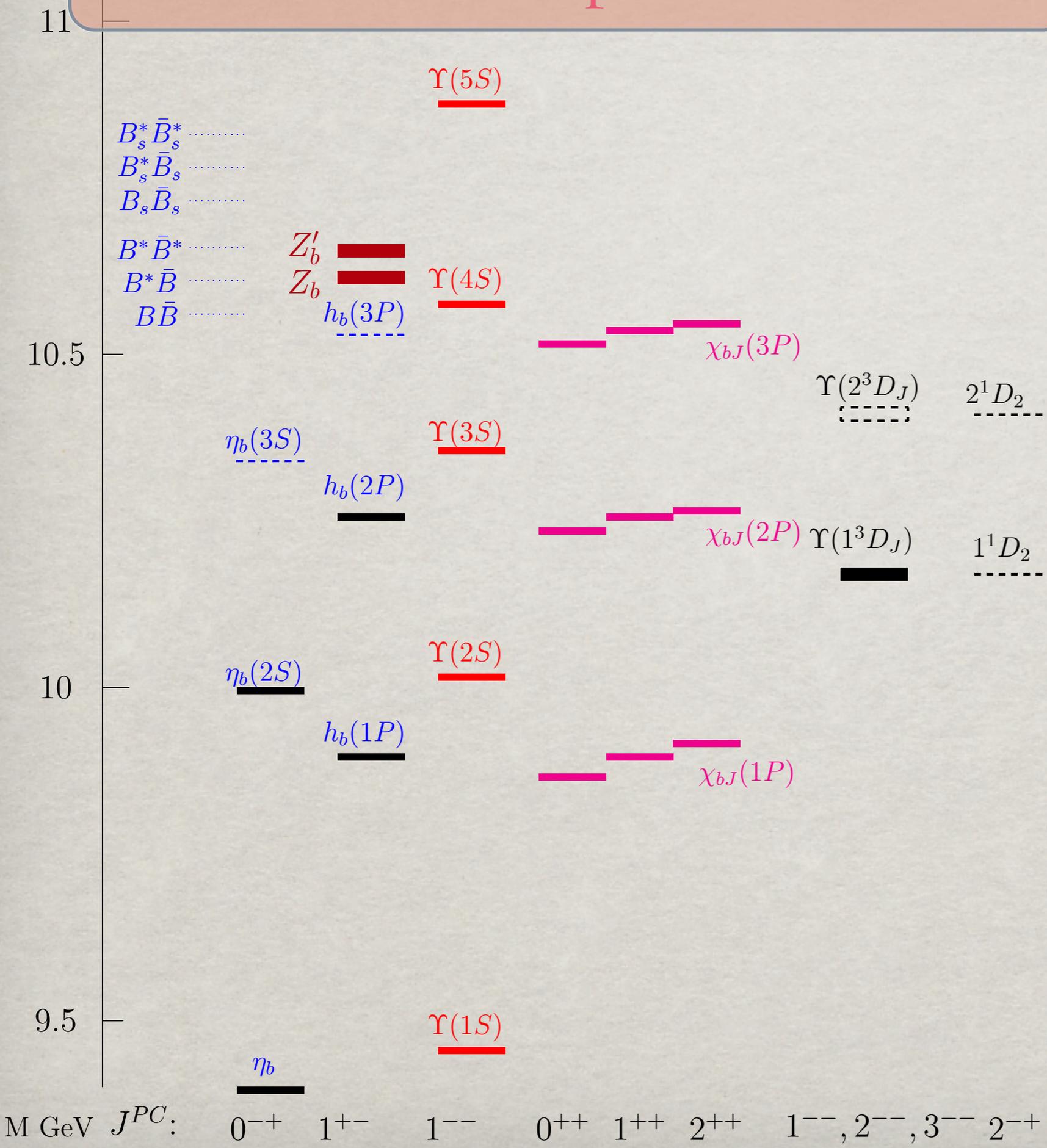
bottomonium: the present revolution



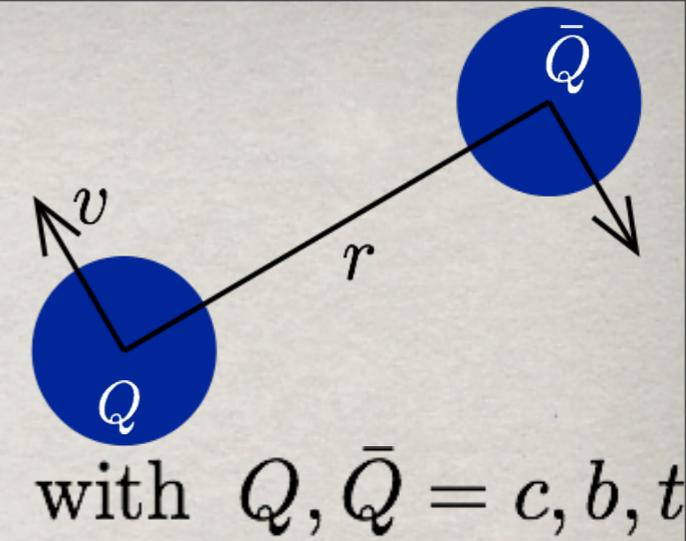
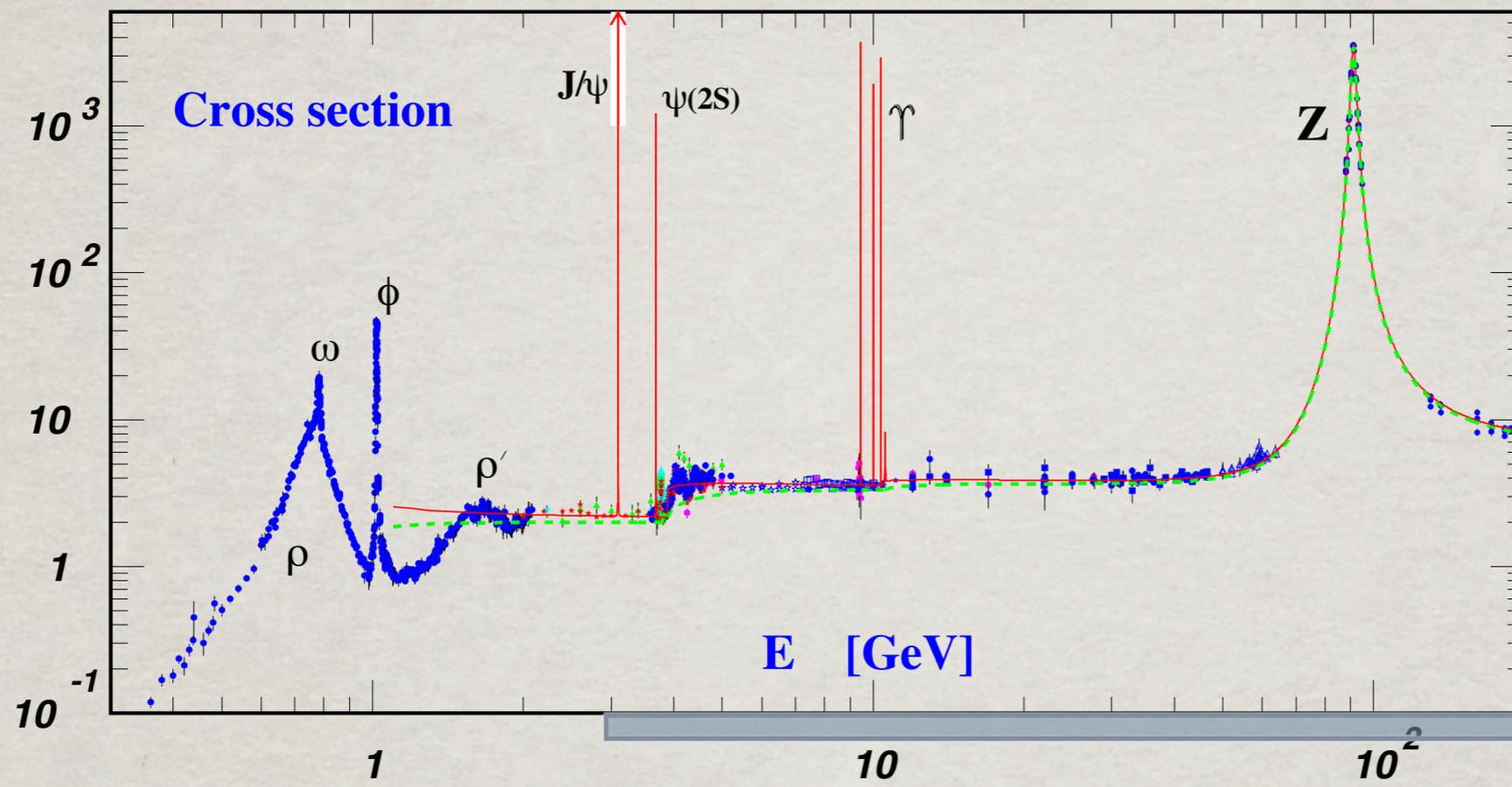
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CLEO

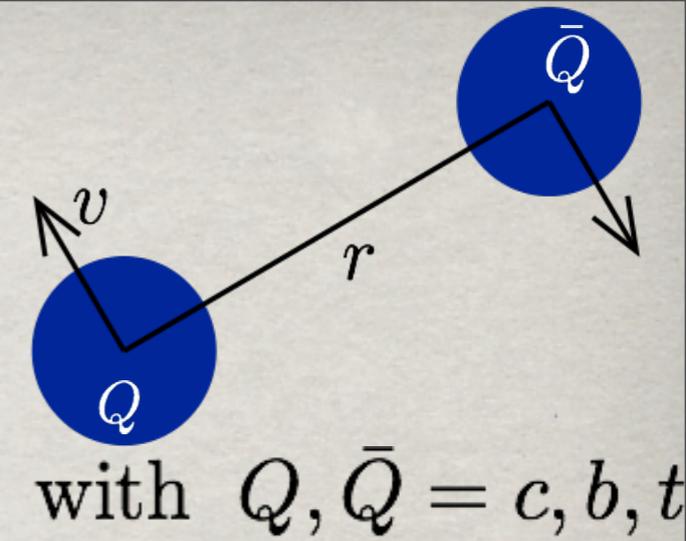
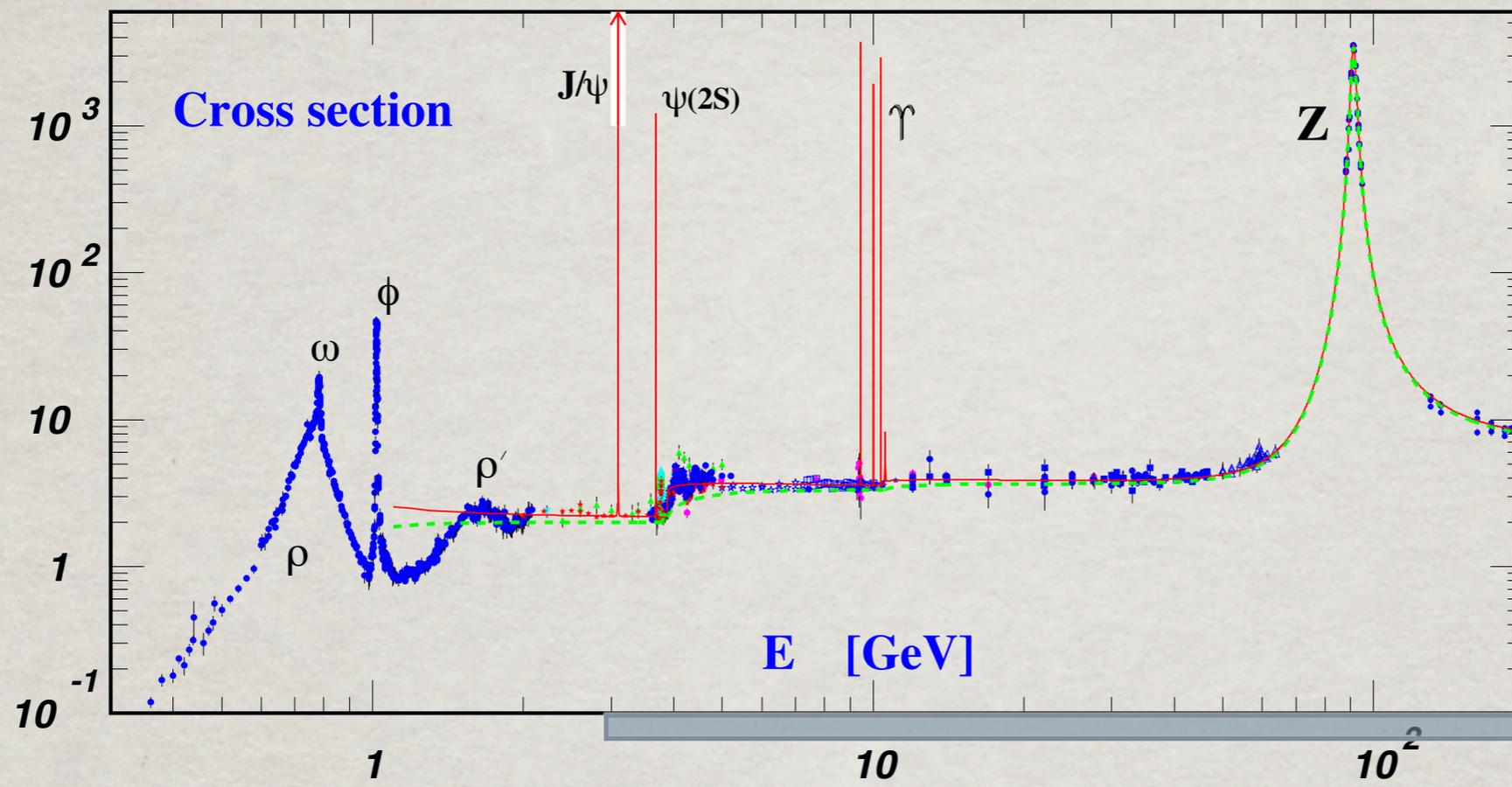


Heavy quarks offer a privileged access



$m_c \sim 1.5\text{GeV}$
 $m_b \sim 5\text{GeV}$
 $m_t \sim 170\text{GeV}$

Heavy quarks offer a privileged access



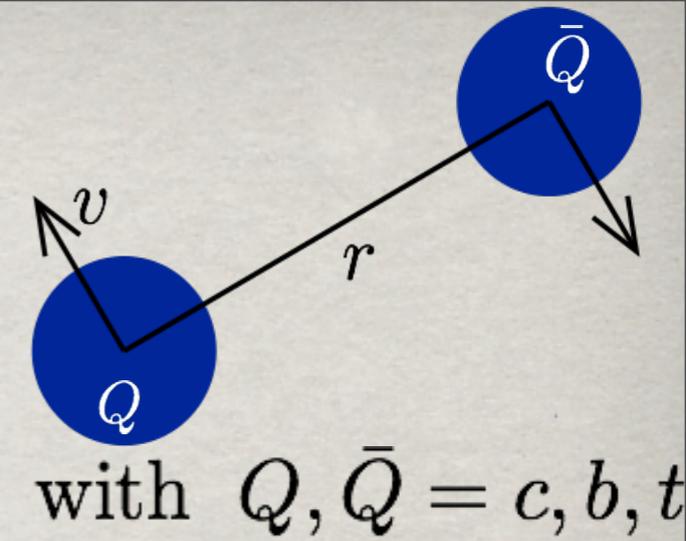
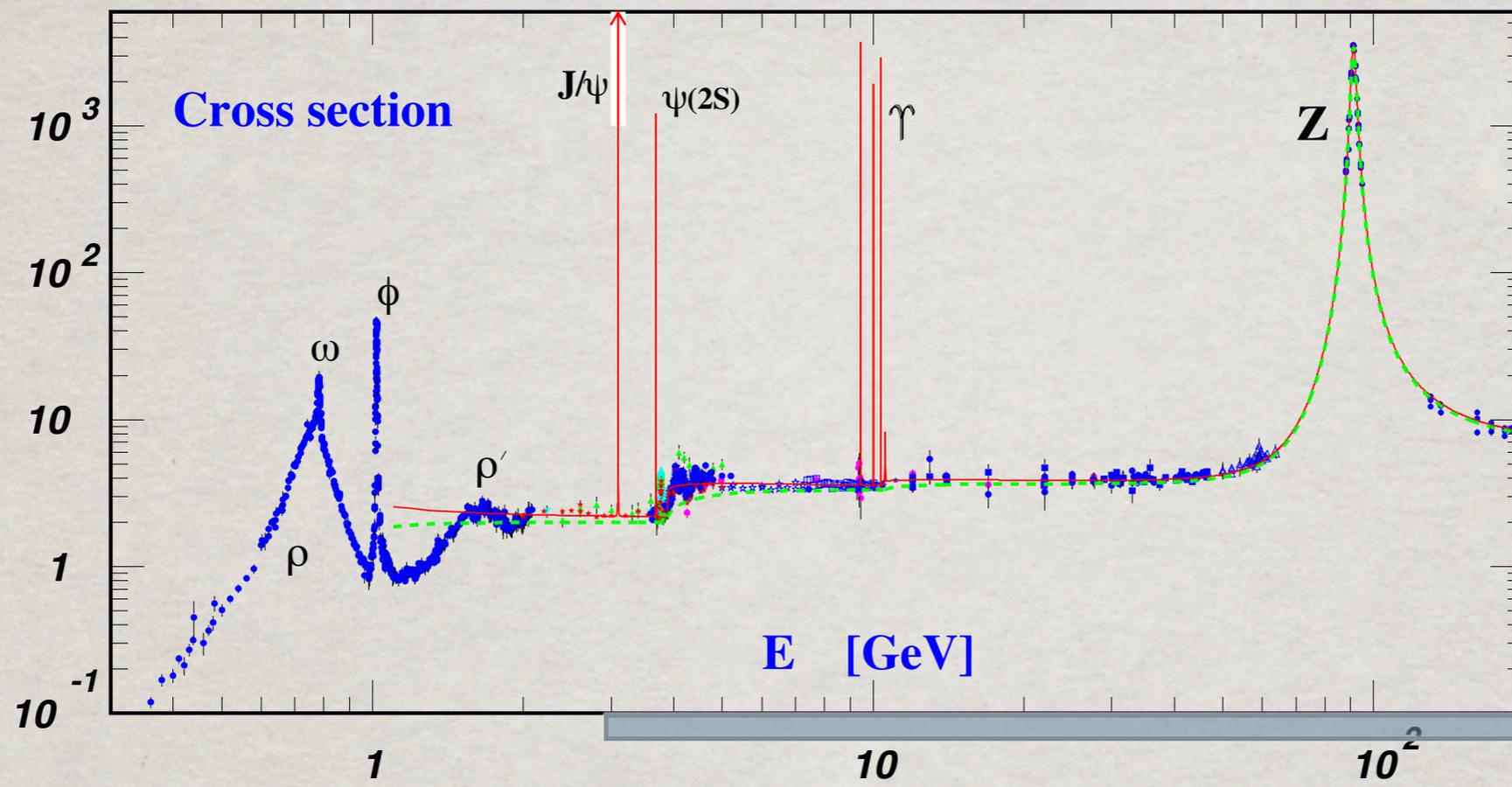
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A large scale

$$m_Q \gg \Lambda_{\text{QCD}}$$

$$\alpha_s(m_Q) \ll 1$$

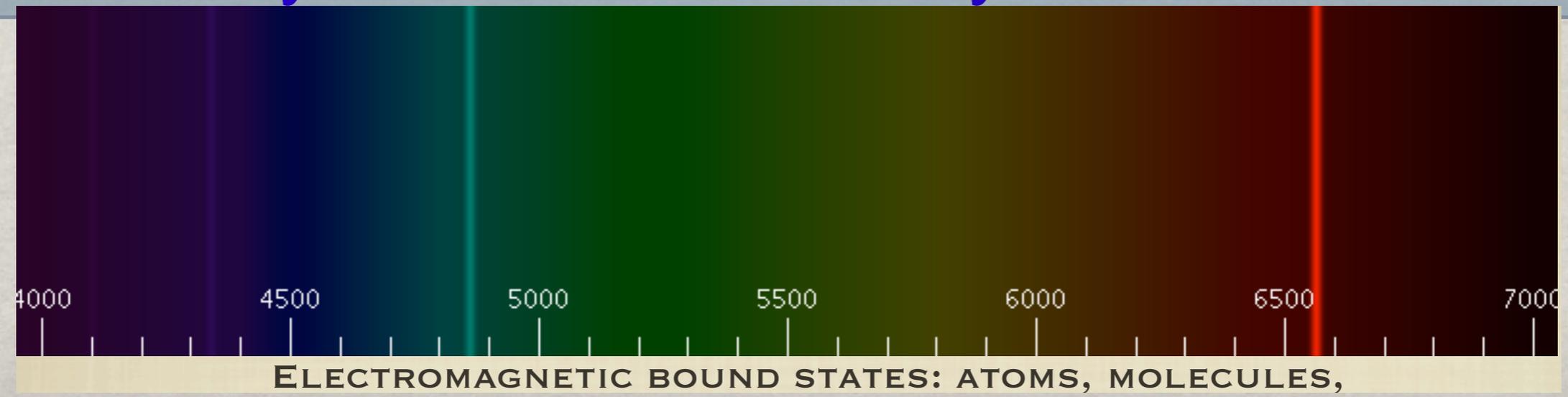
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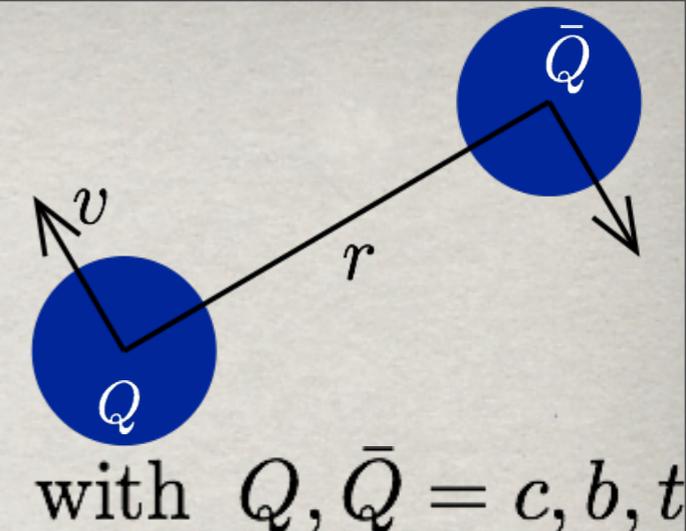
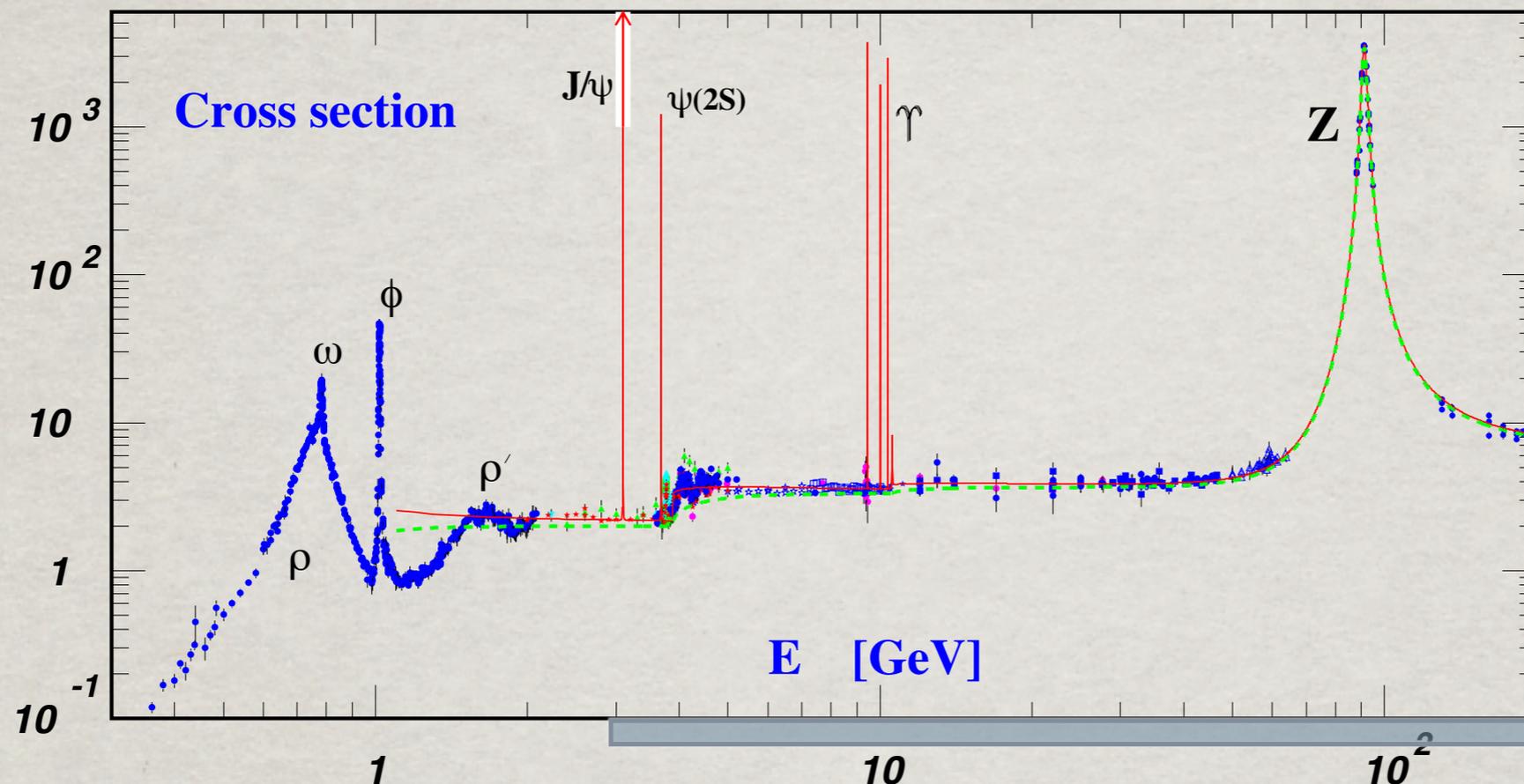
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A large scale $m_Q \gg \Lambda_{\text{QCD}}$ $\alpha_s(m_Q) \ll 1$

Heavy quarkonia are nonrelativistic bound systems: multiscale systems



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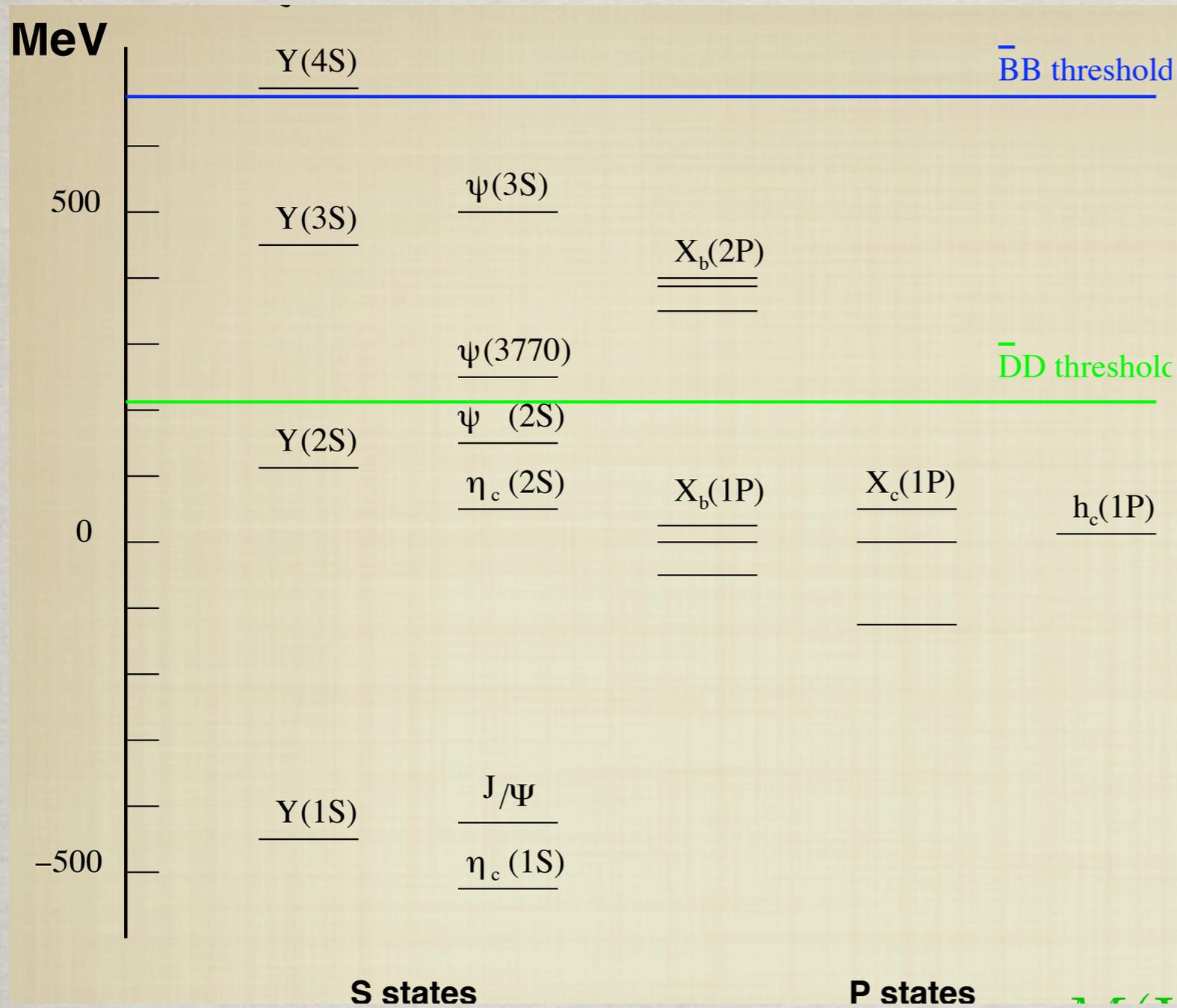
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Heavy quarkonia are nonrelativistic bound systems: multiscale systems

many scales: a challenge and an opportunity

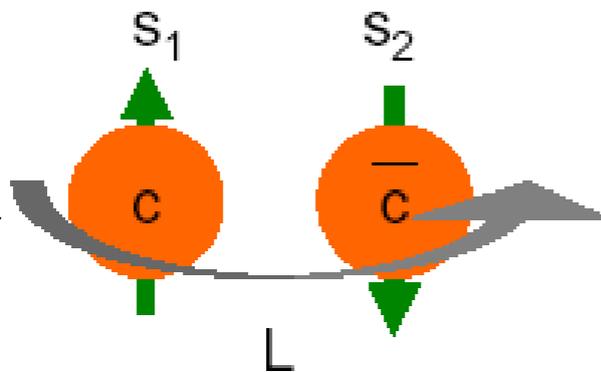


Quarkonium scales



Normalized with respect to $\chi_b(1P)$ and $\chi_c(1P)$

$$2S+1 L_J$$

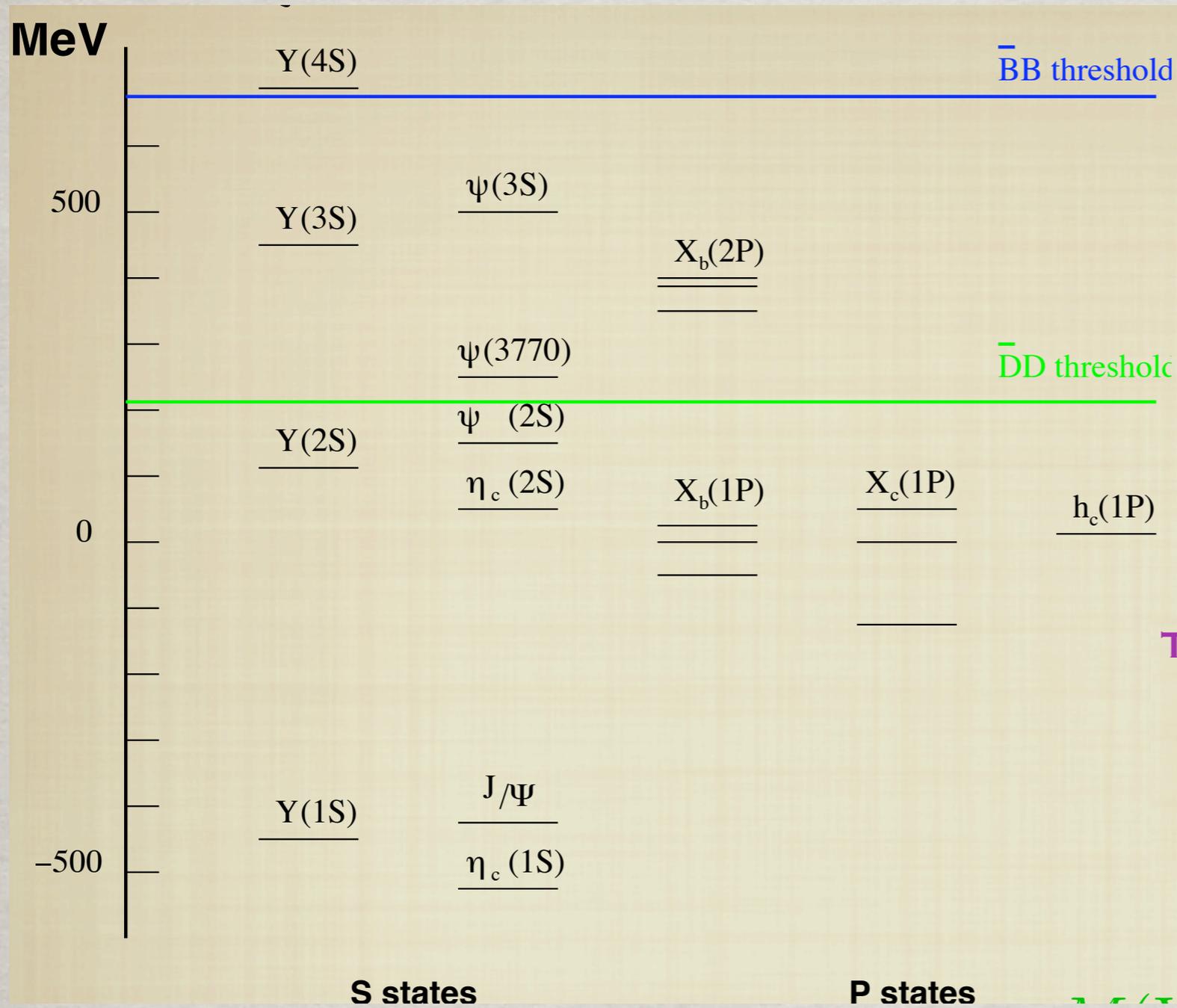


THE MASS SCALE IS PERTURBATIVE

$$m_Q \gg \Lambda_{\text{QCD}}$$

$$m_b \simeq 5 \text{ GeV}; m_c \simeq 1.5 \text{ GeV}$$

Quarkonium scales

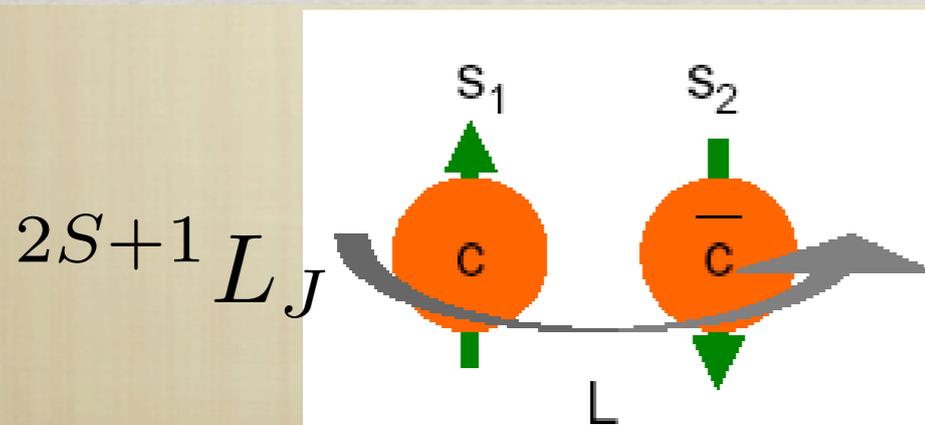


THE SYSTEM IS NONRELATIVISTIC(NR)

$$\Delta E \sim mv^2, \Delta_{fs} E \sim mv^4$$

$$v_b^2 \sim 0.1, v_c^2 \sim 0.3$$

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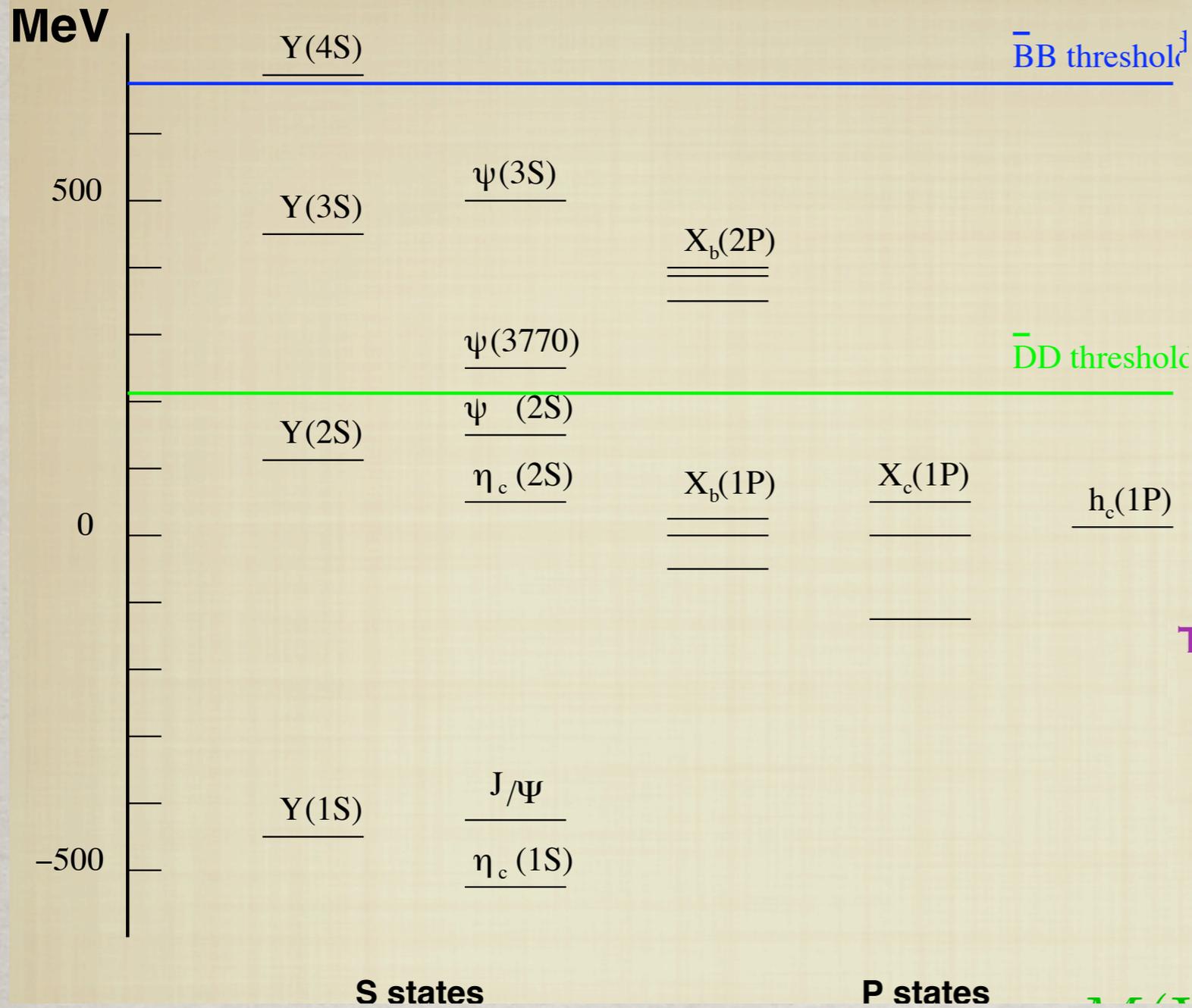


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NR BOUND STATES HAVE AT LEAST 3 SCALES

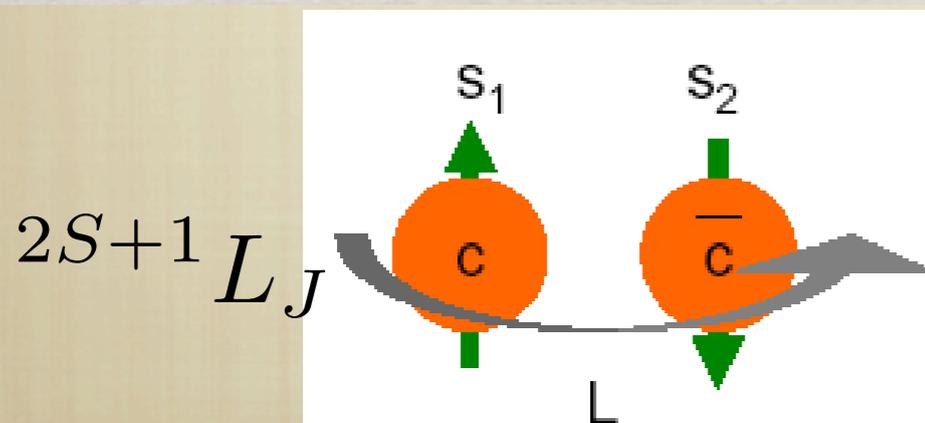
$$m \gg mv \gg mv^2 \quad v \ll 1$$

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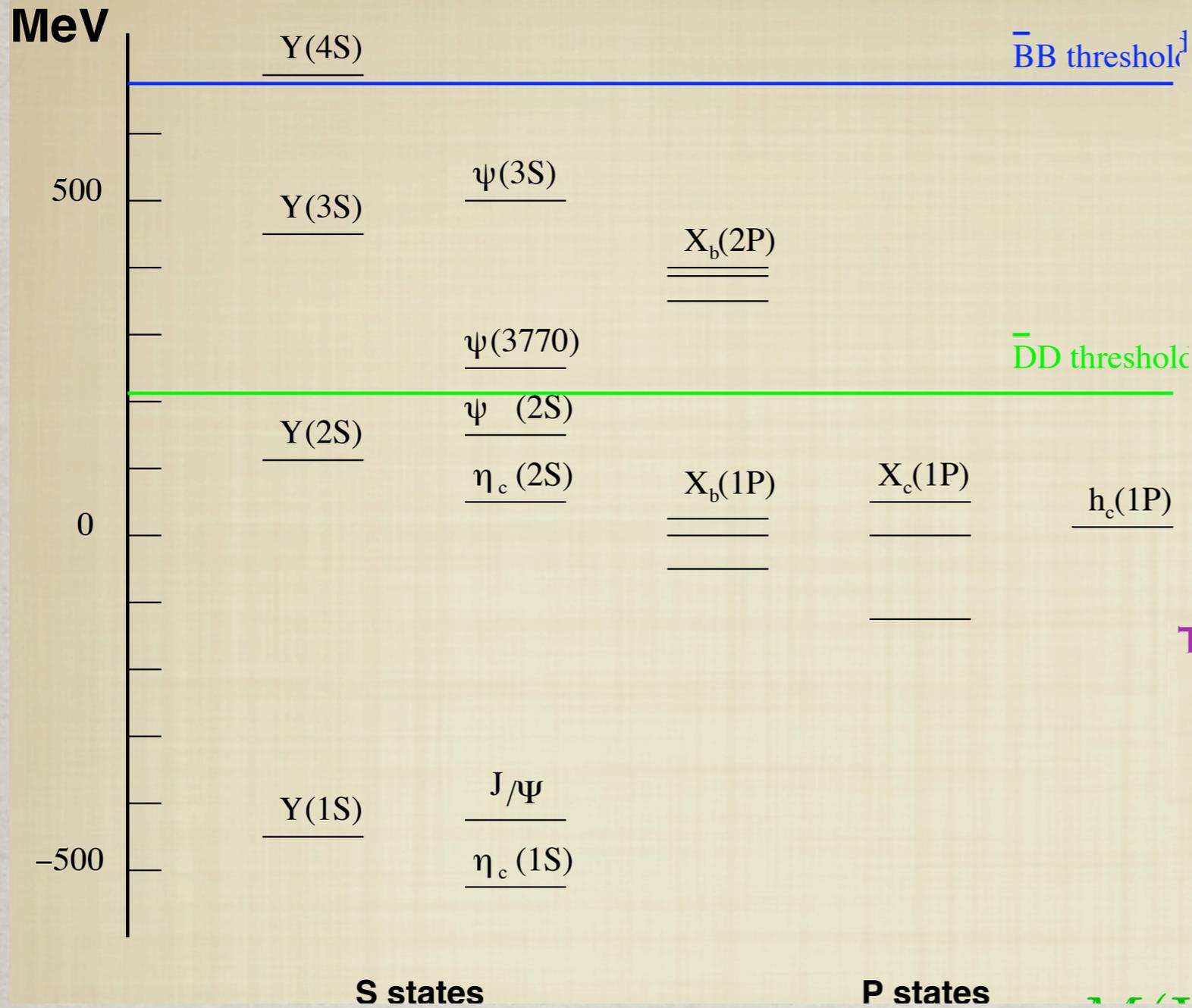


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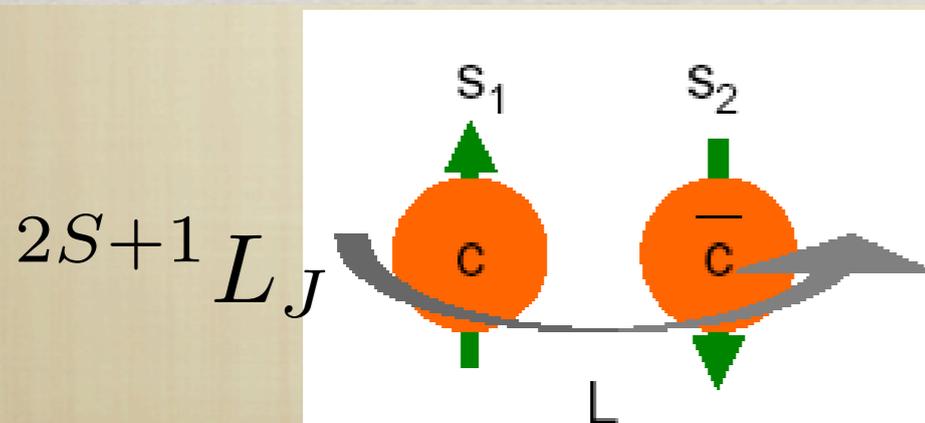
$$mv \sim r^{-1}$$

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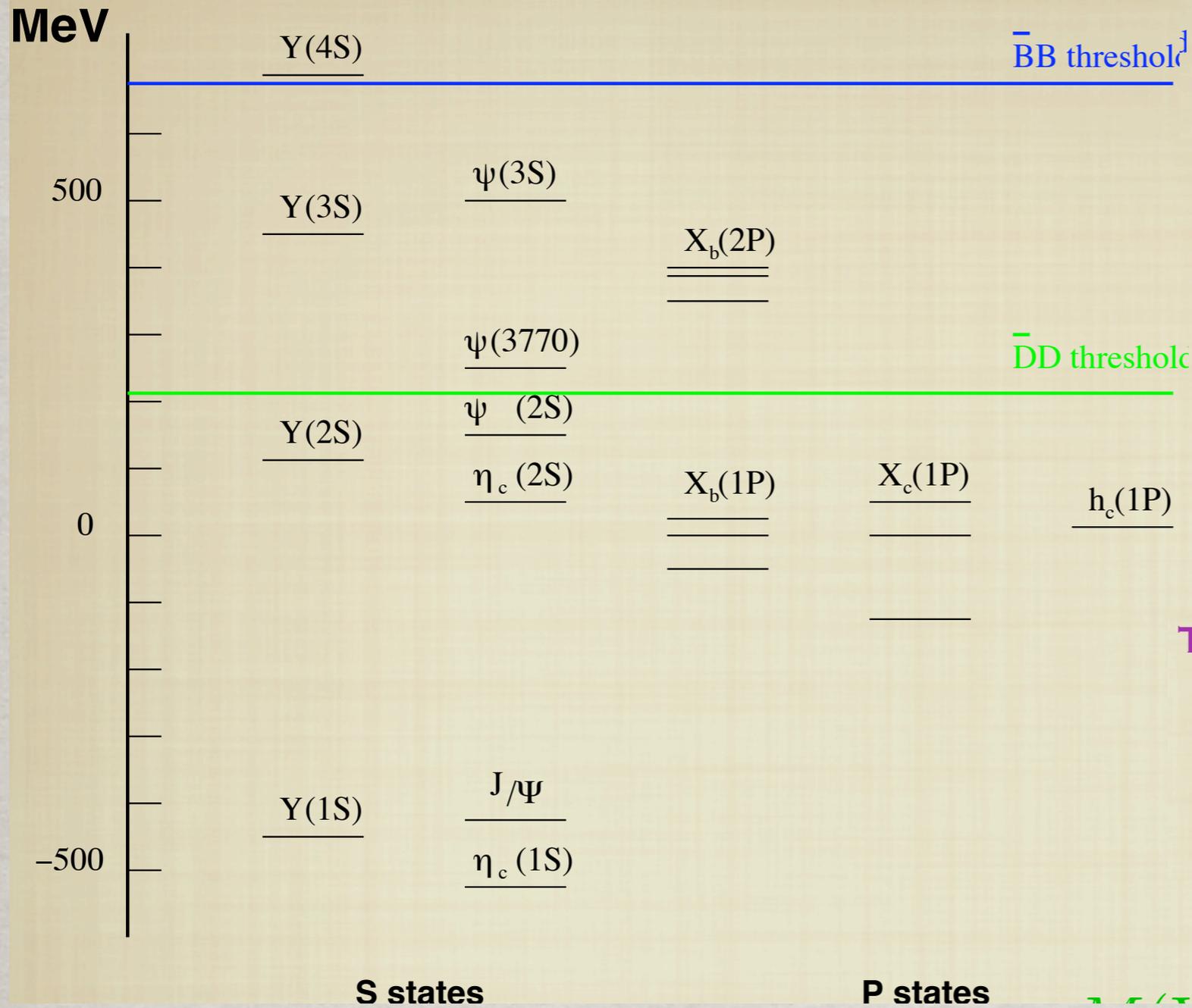


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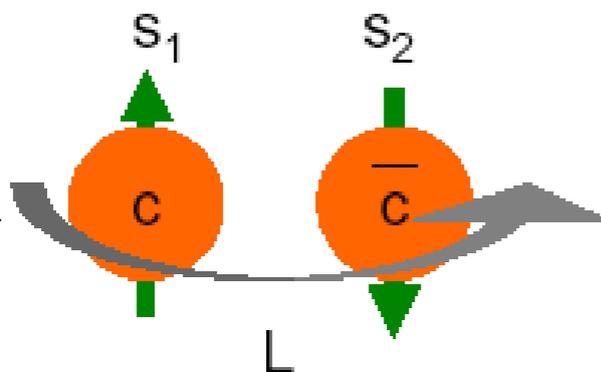
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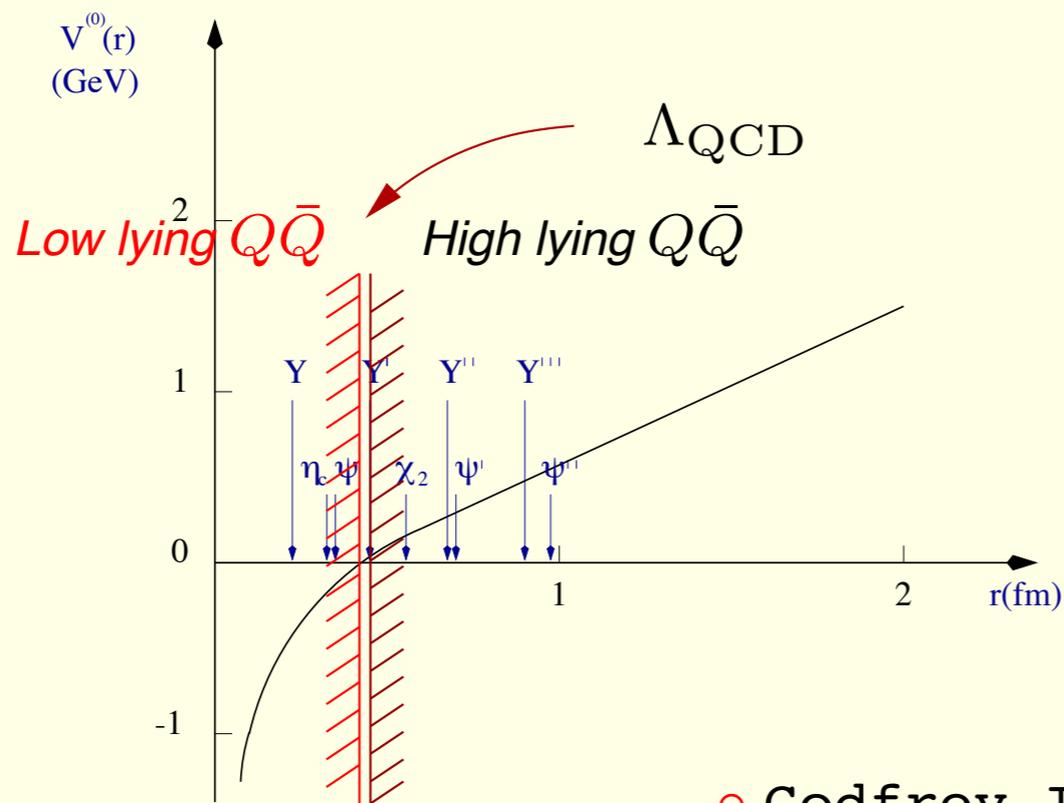
$$m_b \simeq 5 \text{ GeV}; m_c \simeq 1.5 \text{ GeV}$$

Quarkonium as a confinement and deconfinement probe

The rich structure of separated energy scales makes $Q\bar{Q}$ an ideal probe

At zero temperature

- The different quarkonium radii provide different measures of the transition from a Coulombic to a confined bound state.

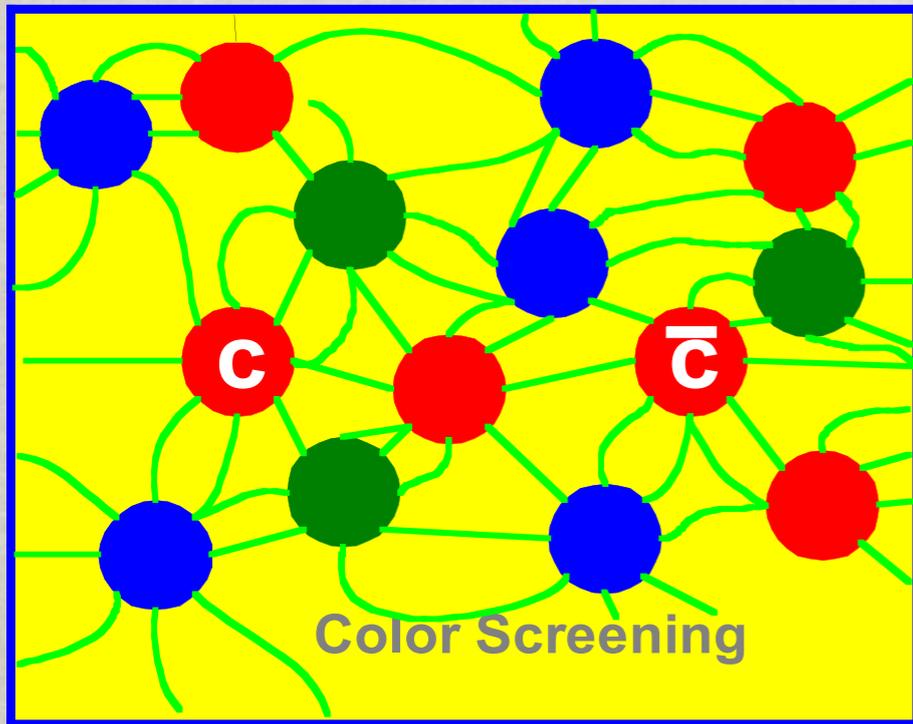


○ Godfrey Isgur PRD 32(85)189

quarkonia probe the perturbative (high energy) and non perturbative region (low energy) as well as the transition region in dependence of their radius r

Quarkonium as a confinement and deconfinement probe

At finite temperature T they are sensitive to the formation of a quark gluon plasma via color screening



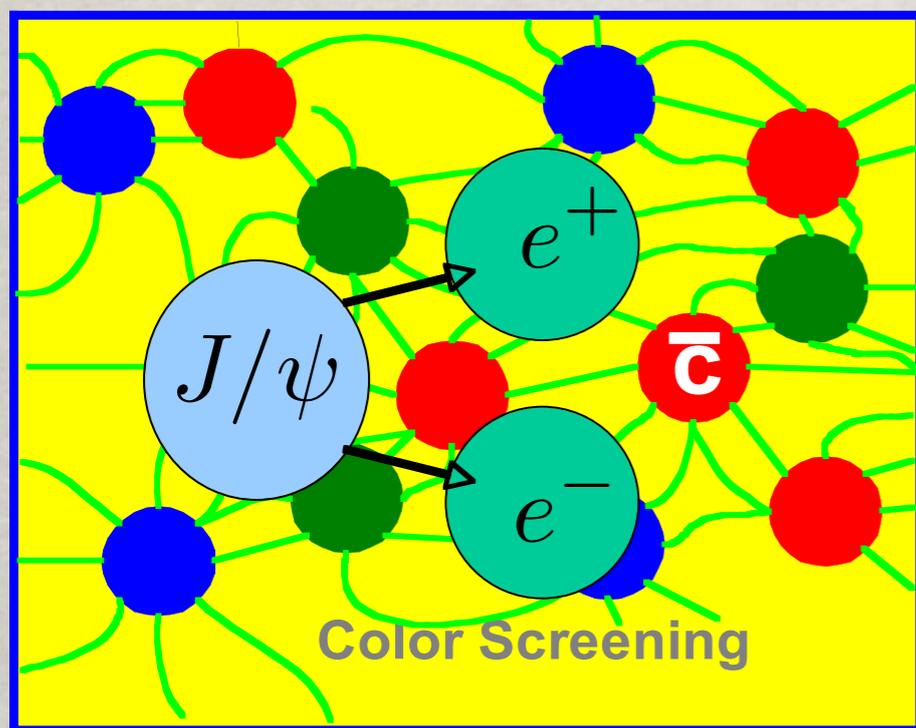
Debye charge screening $m_D \sim gT$

$$V(r) \sim -\alpha_s \frac{e^{-m_D r}}{r}$$

Matsui Satz 1986

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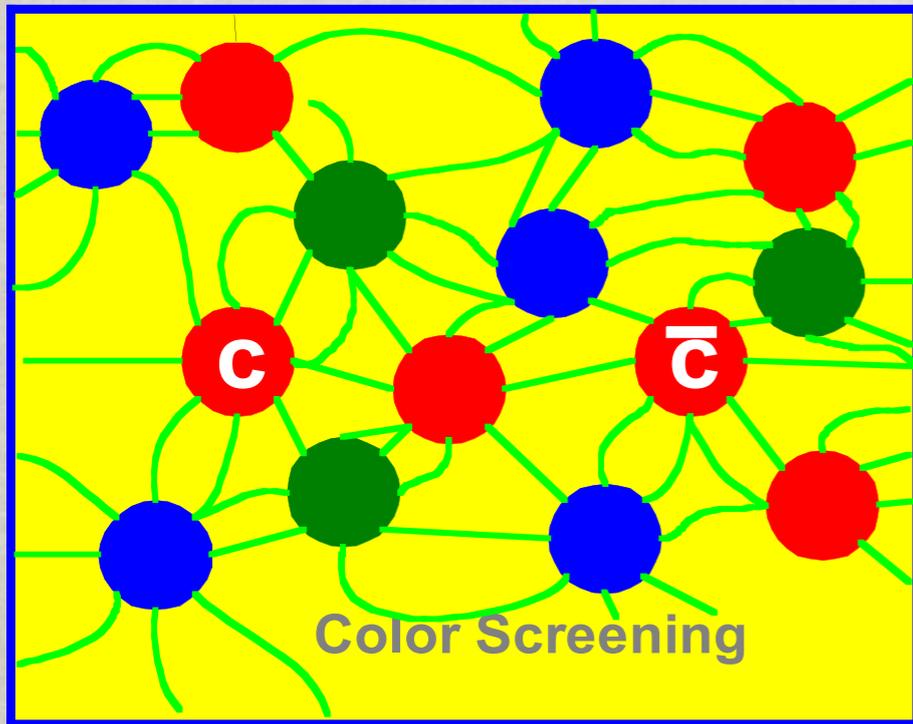
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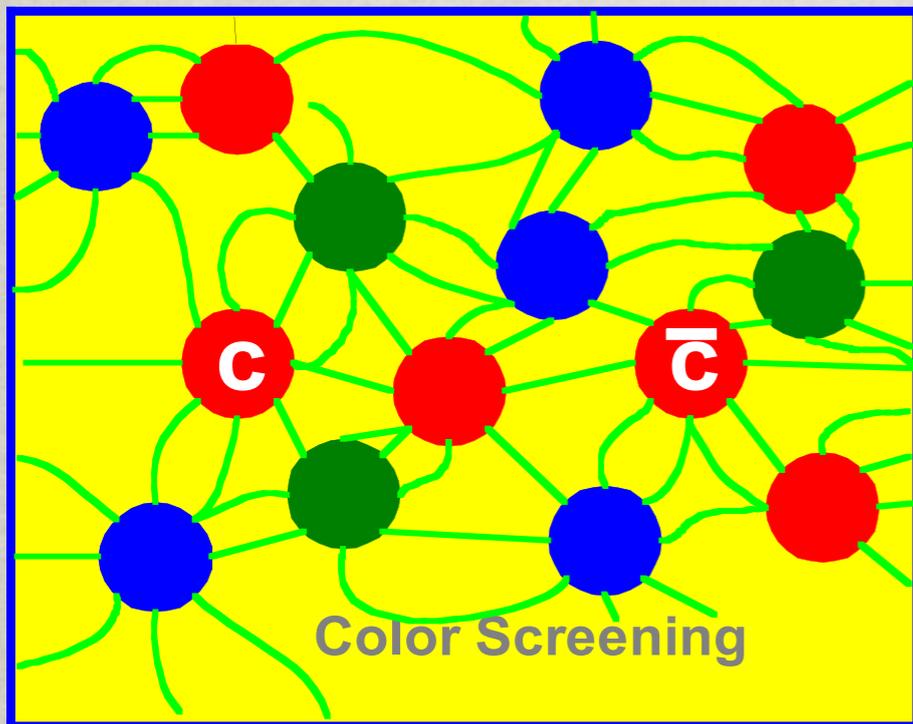
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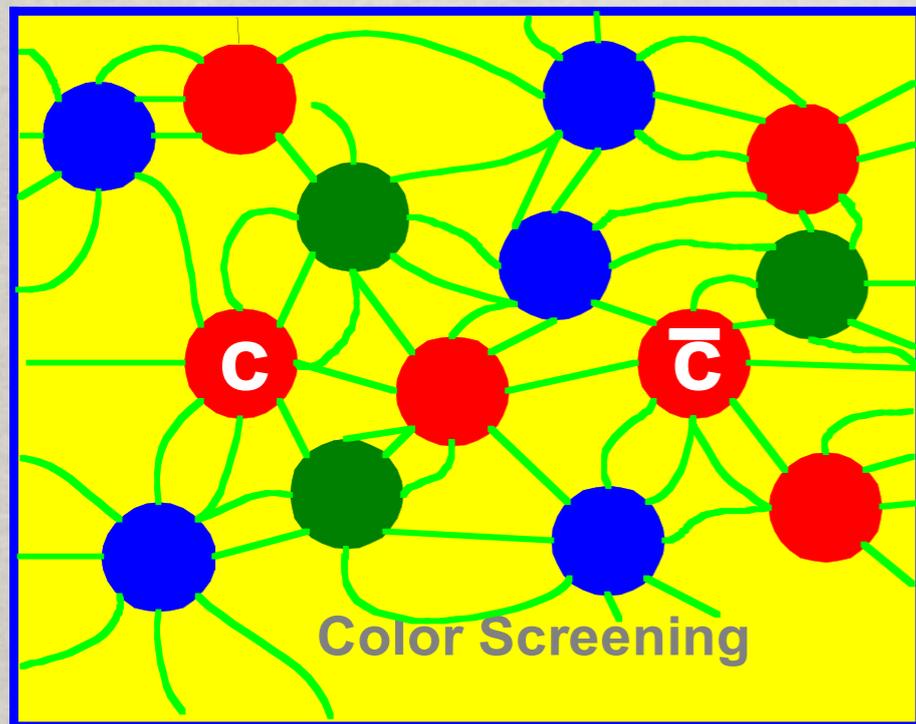
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$$r \sim \frac{1}{m_D} \longrightarrow \text{Bound state dissolves}$$

Matsui Satz 1986

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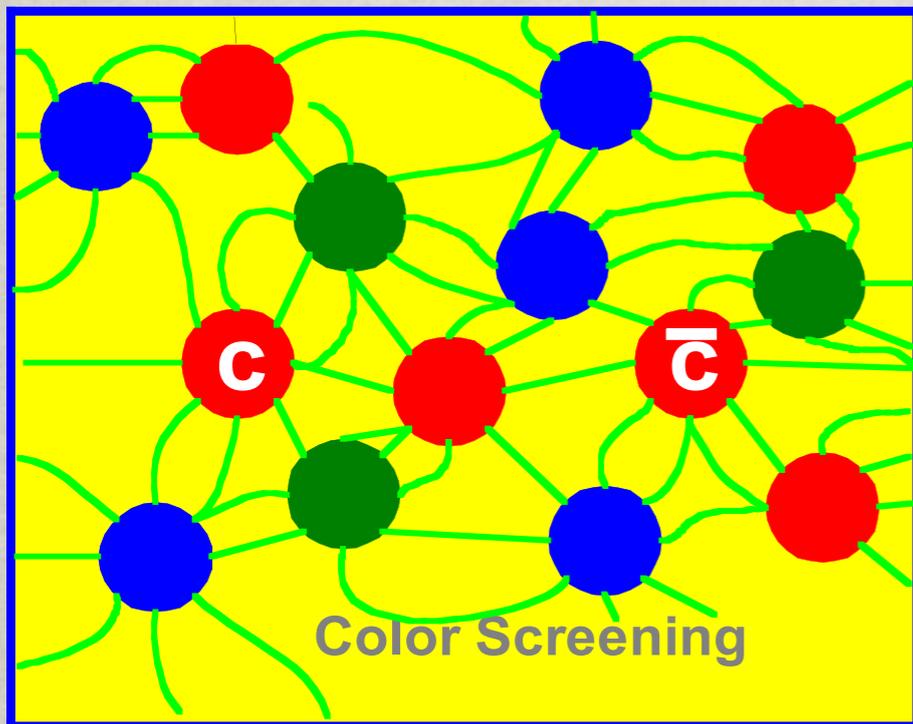
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Matsui Satz 1986

quarkonia dissociate at different temperature in dependence of their radius: they are a Quark Gluon Plasma thermometer

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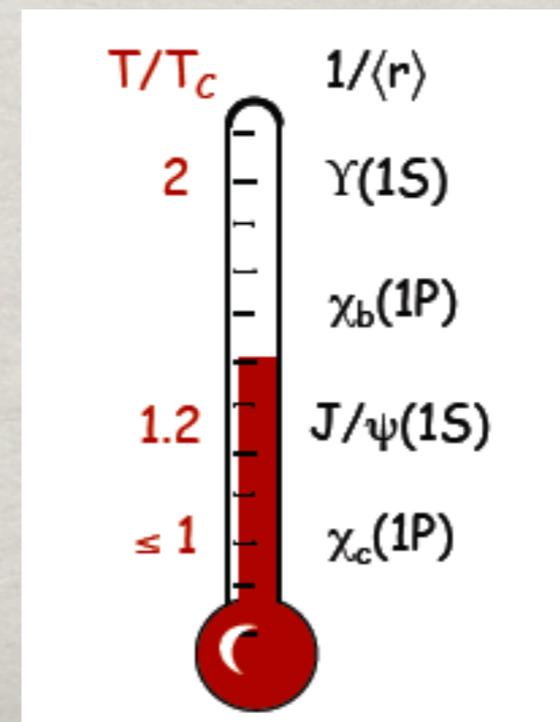
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Quarkonium as an exploration tool of physics of Standard Model and beyond

Quarkonium can serve for the precise extraction of Standard Model parameters: heavy quark masses and strong coupling constant α_s

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The large mass makes quarkonium an ideal probe of new particles

BaBar light-Higgs & dark-photon searches

Mode	Mass range (GeV)	BF upper limit (90% CL)
$\Upsilon(2S, 3S) \rightarrow \gamma A^0, A^0 \rightarrow \mu^+ \mu^-$	$0.21 < m_A < 9.3$	$(0.3 - 8.3) \times 10^{-6}$
$\Upsilon(3S) \rightarrow \gamma A^0, A^0 \rightarrow \tau^+ \tau^-$	$4.0 < m_A < 10.1$	$(1.5 - 16) \times 10^{-5}$
$\Upsilon(2S, 3S) \rightarrow \gamma A^0, A^0 \rightarrow \text{hadrons}$	$0.3 < m_A < 7.0$	$(0.1 - 8) \times 10^{-5}$
$\Upsilon(1S) \rightarrow \gamma A^0, A^0 \rightarrow \chi \bar{\chi}$	$m_\chi < 4.5 \text{ GeV}$	$(0.5 - 24) \times 10^{-5}$
$\Upsilon(1S) \rightarrow \gamma A^0, A^0 \rightarrow \text{invisible}$	$m_A < 9.2 \text{ GeV}$	$(1.9 - 37) \times 10^{-6}$
$\Upsilon(3S) \rightarrow \gamma A^0, A^0 \rightarrow \text{invisible}$	$m_A < 9.2 \text{ GeV}$	$(0.7 - 31) \times 10^{-6}$
$\Upsilon(1S) \rightarrow \gamma A^0, A^0 \rightarrow g \bar{g}$	$m_A < 9.0 \text{ GeV}$	$10^{-6} - 10^{-2}$
$\Upsilon(1S) \rightarrow \gamma A^0, A^0 \rightarrow s \bar{s}$	$m_A < 9.0 \text{ GeV}$	$10^{-5} - 10^{-3}$

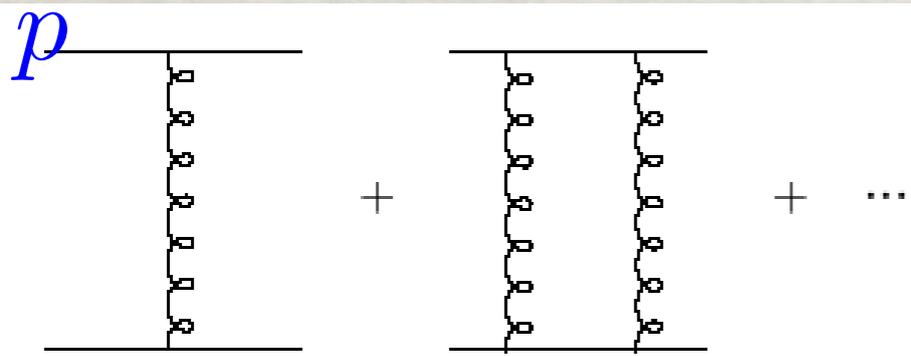
QCD theory of Quarkonium: a very hard problem

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Close to the bound state $\alpha_s \sim v$

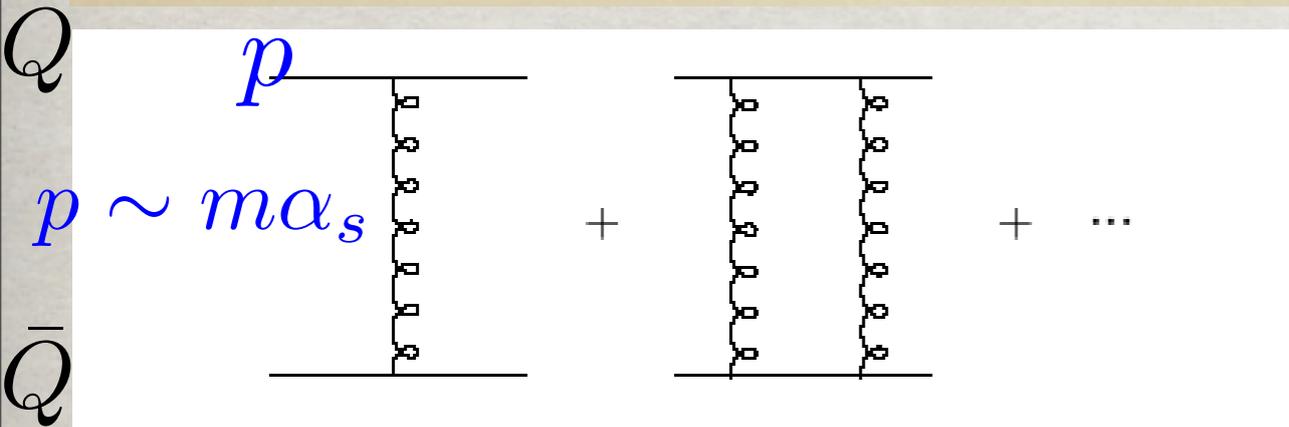
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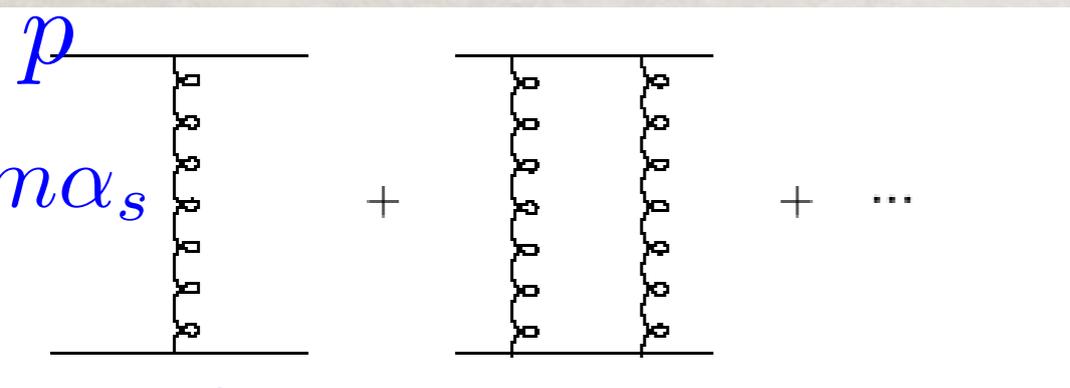


QCD theory of Quarkonium: a very hard problem

Close to the bound state $\alpha_s \sim v$

Q

$p \sim m\alpha_s$

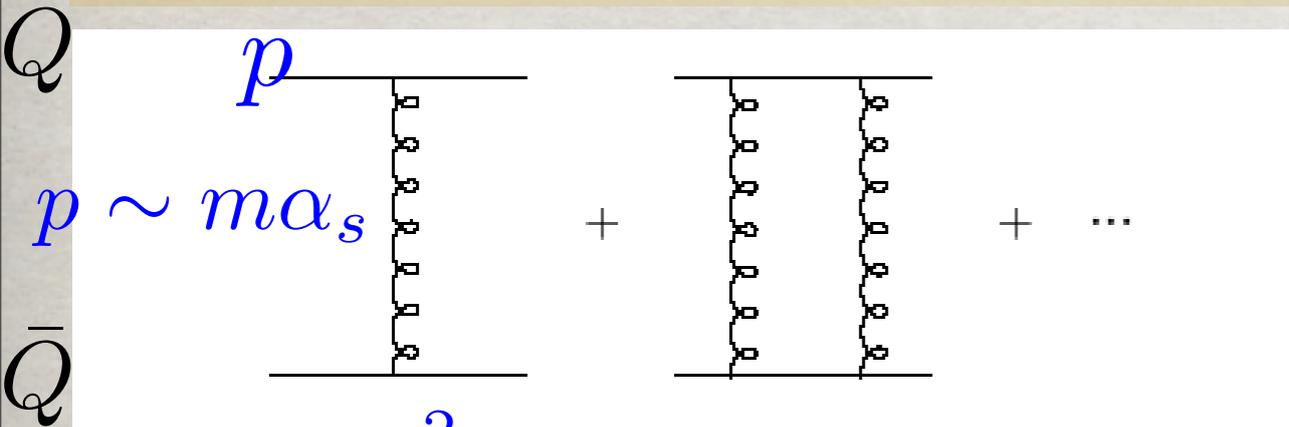


Q

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QCD theory of Quarkonium: a very hard problem

Close to the bound state $\alpha_s \sim v$

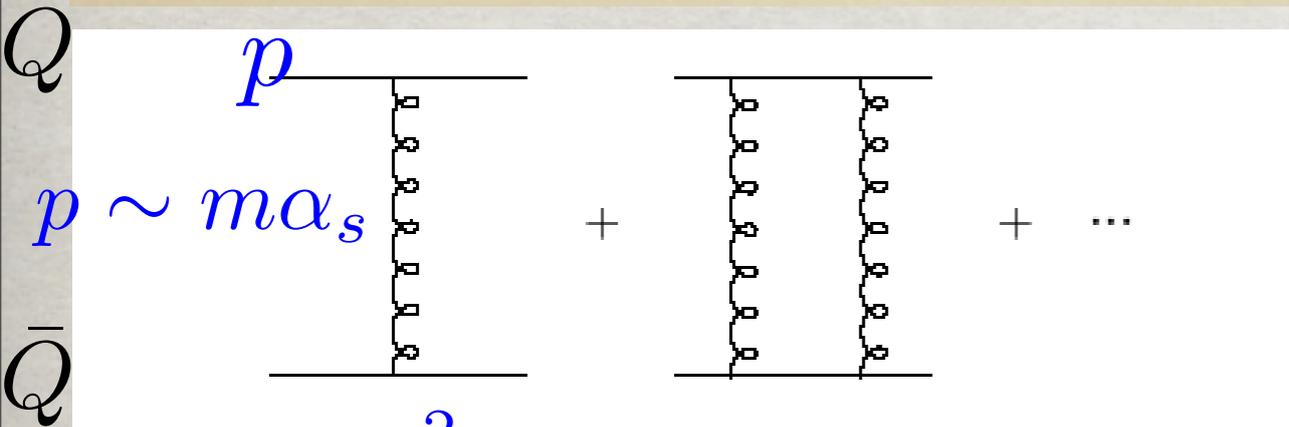


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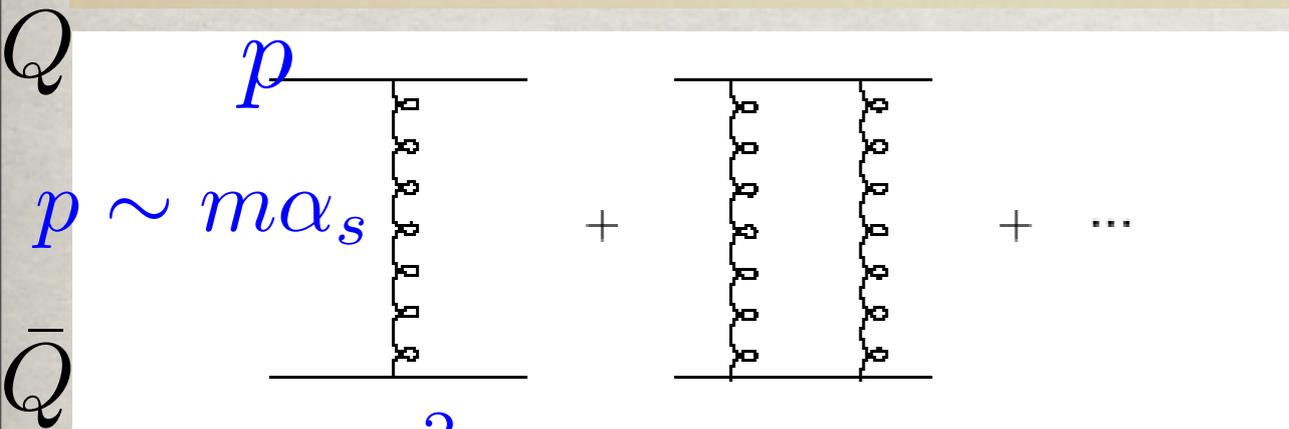
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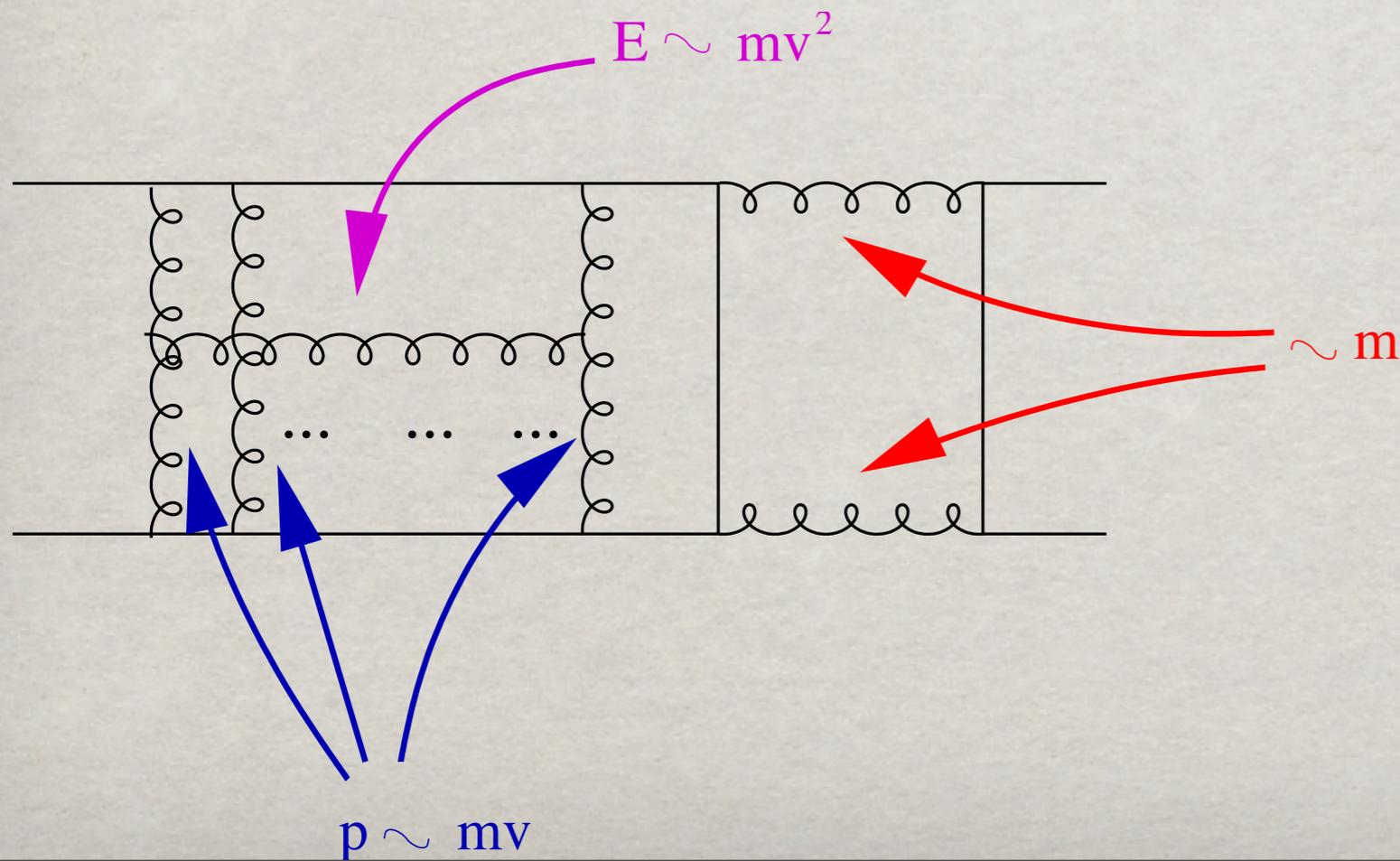
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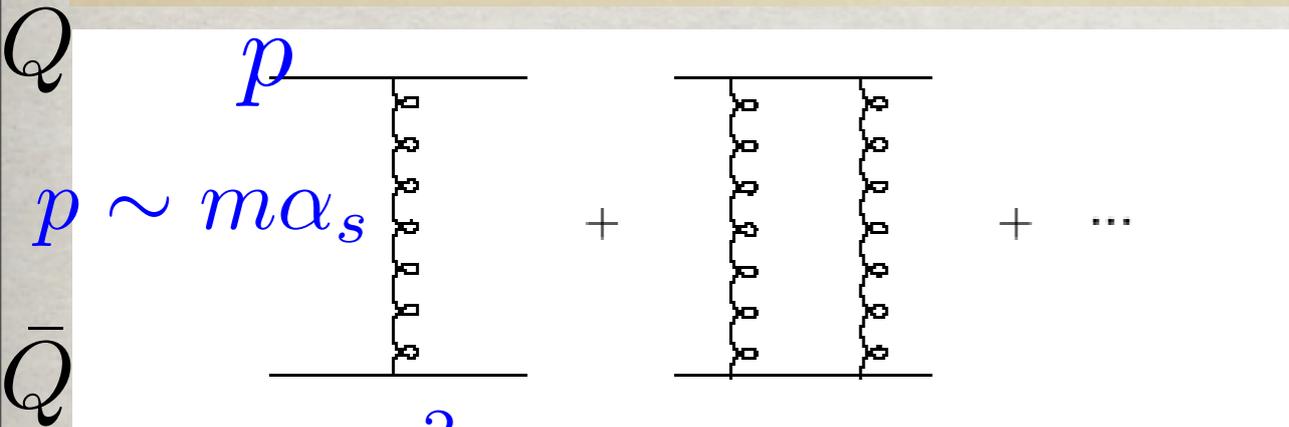
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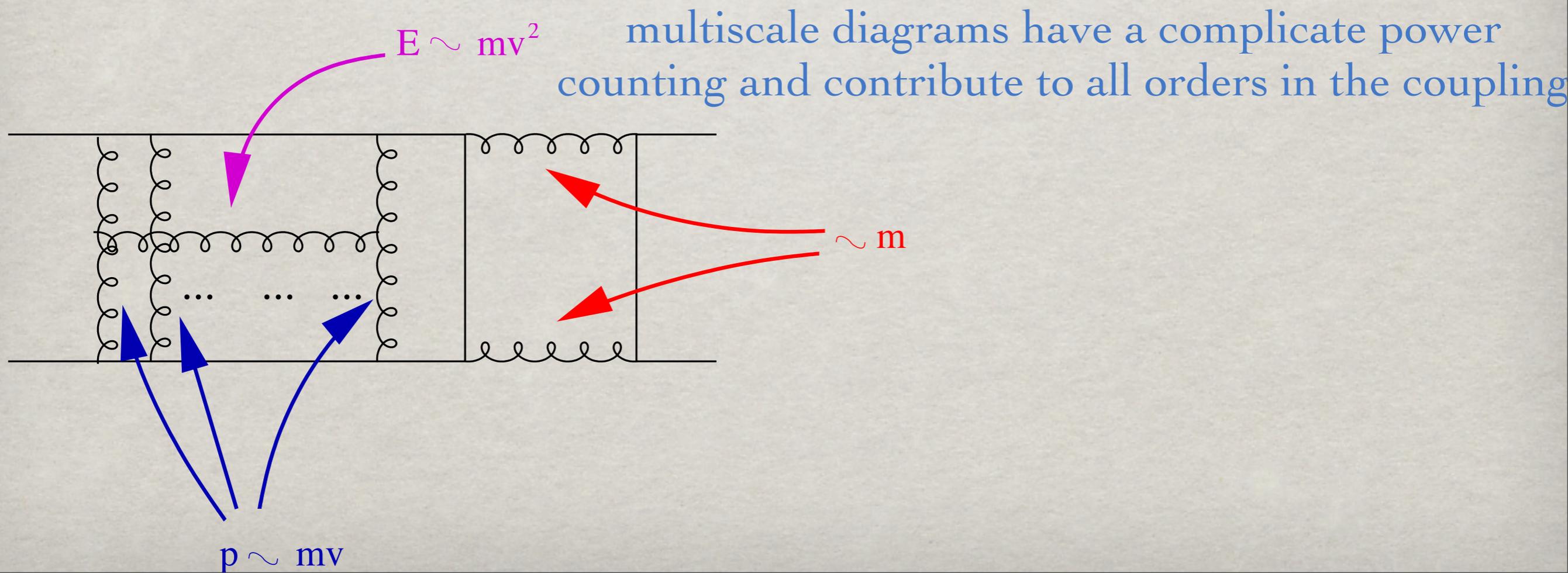
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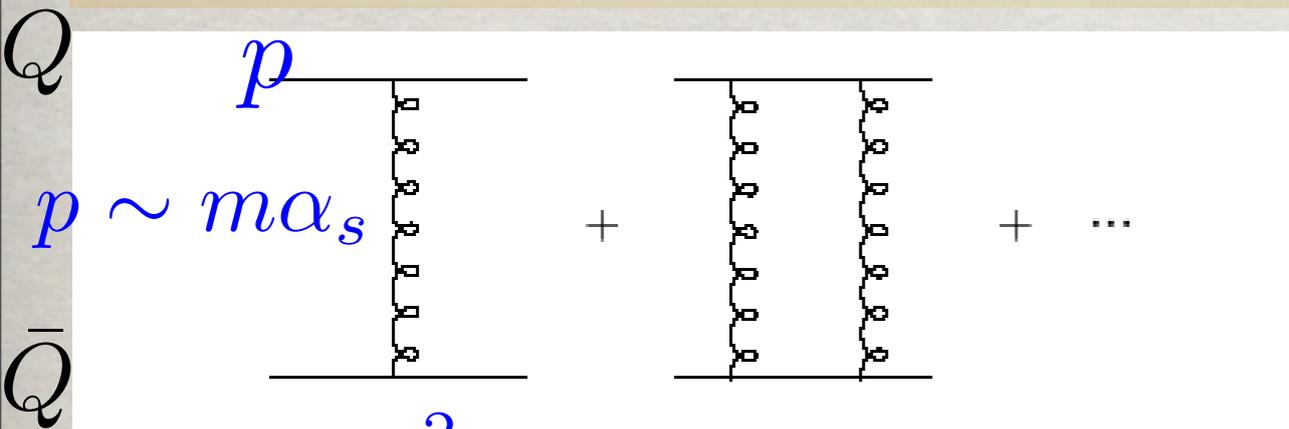
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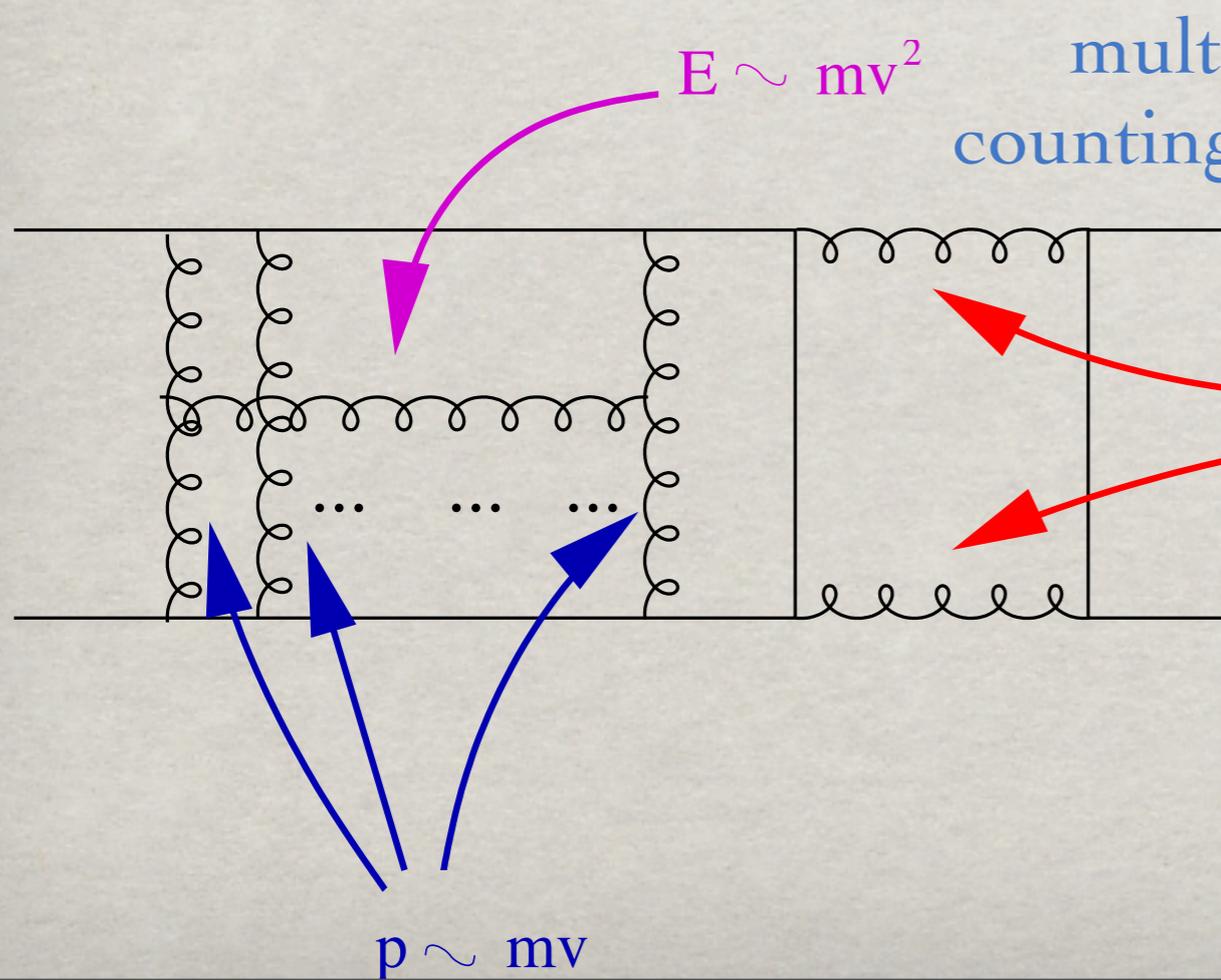
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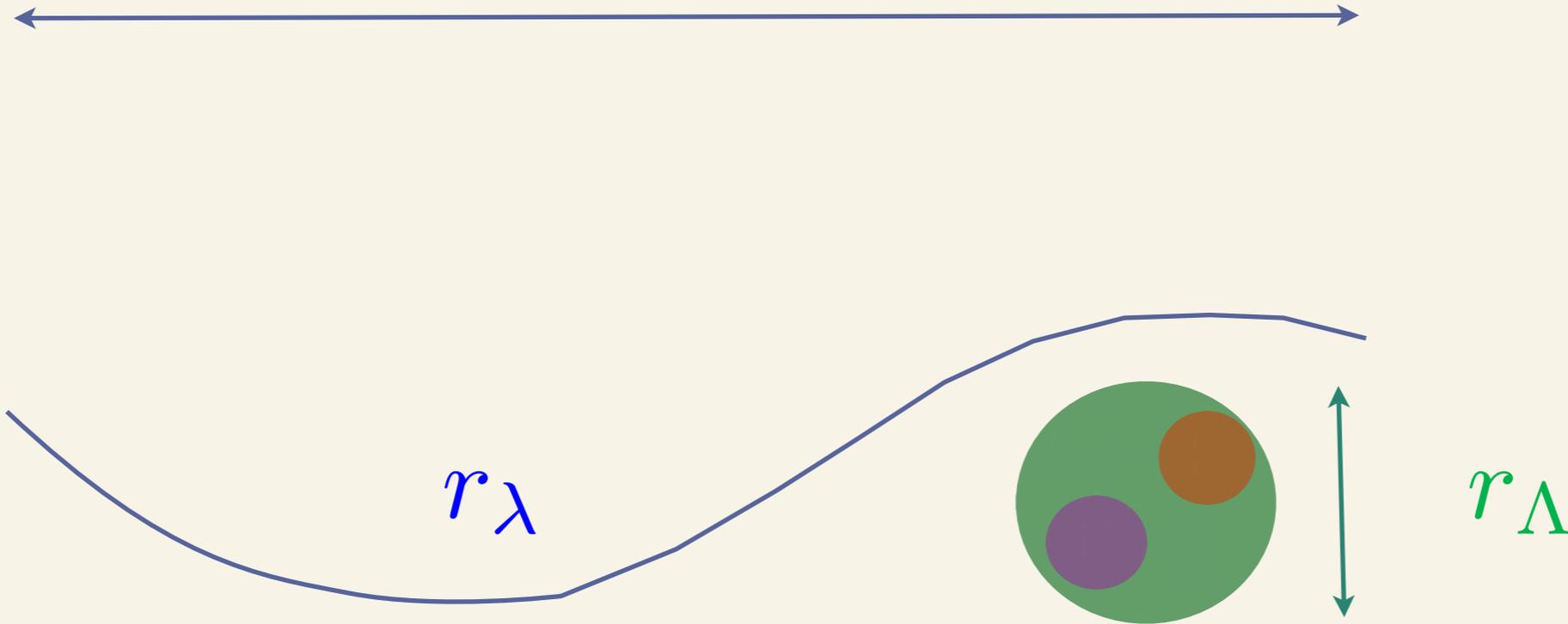


multiscale diagrams have a complicated power counting and contribute to all orders in the coupling

Difficult also for the lattice!

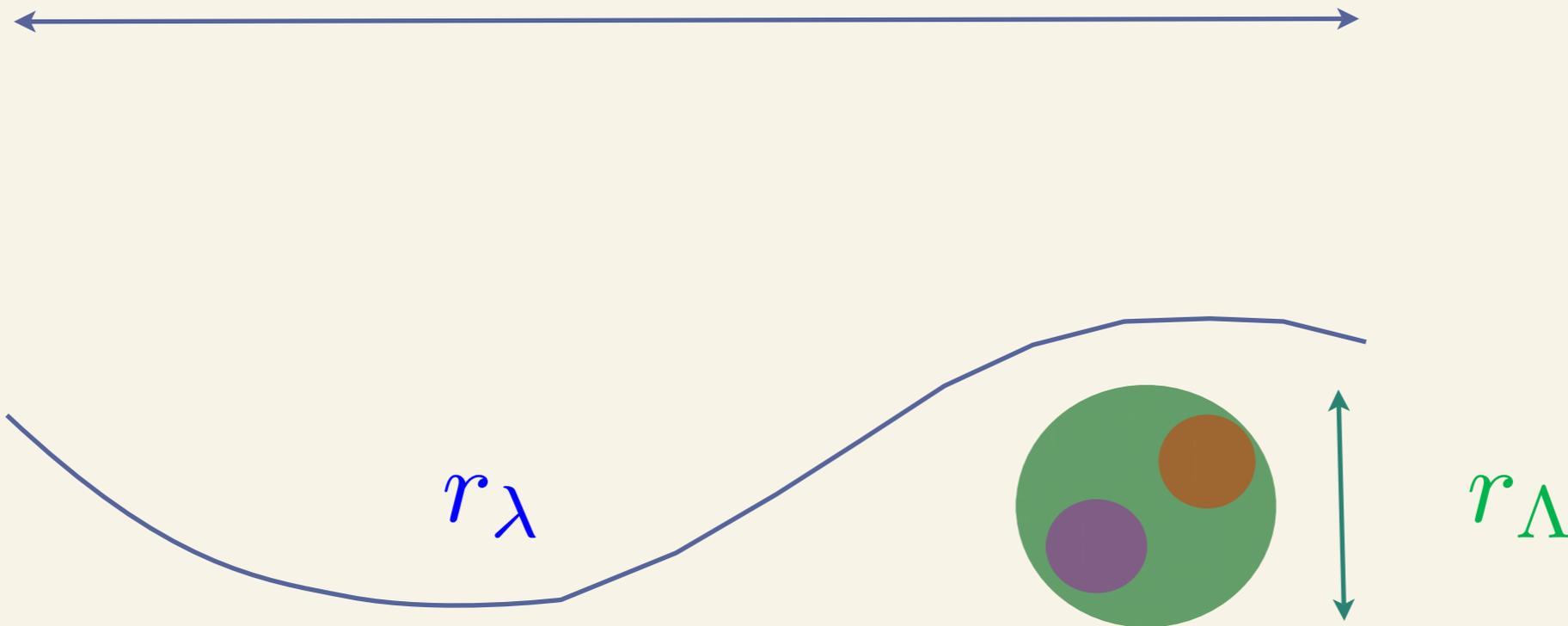
$$L^{-1} \ll \lambda \ll \Lambda \ll a^{-1}$$

a hierarchy of EFTs can be formulated in
correspondence to the hierarchy of scales



An **effective field theory** makes the expansion in λ/Λ explicit at the Lagrangian level.

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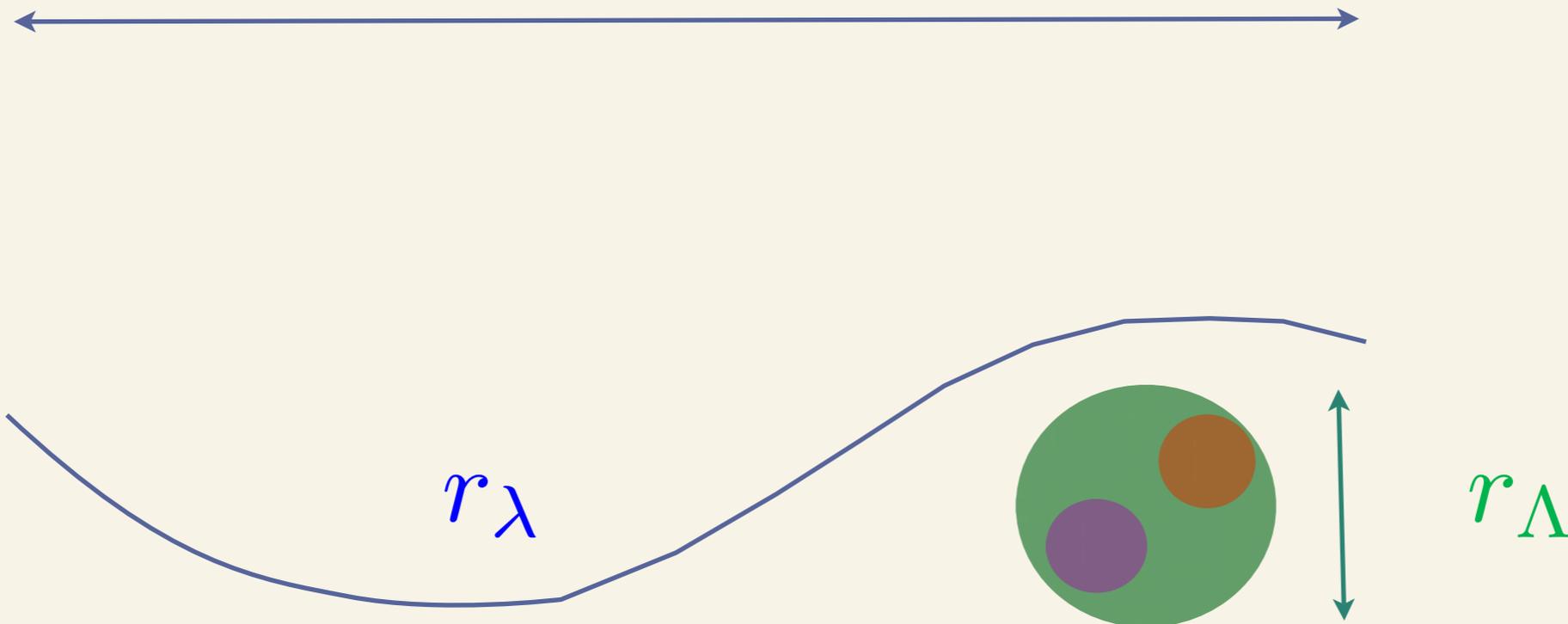
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The EFT Lagrangian, \mathcal{L}_{EFT} , suitable to describe H at scales lower than Λ is defined by

(1) a **cut off** $\Lambda \gg \mu \gg \lambda$;

(2) by some **degrees of freedom** that exist at scales lower than μ

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RANGE OF VALIDITY OF THE EFT: ENERGY $< \mu$

$\Rightarrow \mathcal{L}_{\text{EFT}}$ is made of all operators O_n that may be built from the effective **degrees of freedom** and are consistent with the **symmetries of \mathcal{L}** .

Effective Field Theories

$$\mathcal{L}_{\text{EFT}} = \sum_n c_n(\Lambda, \mu) \frac{O_n(\mu, \lambda)}{\Lambda^n}$$

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Wilson coefficient

low energy operator

large scale

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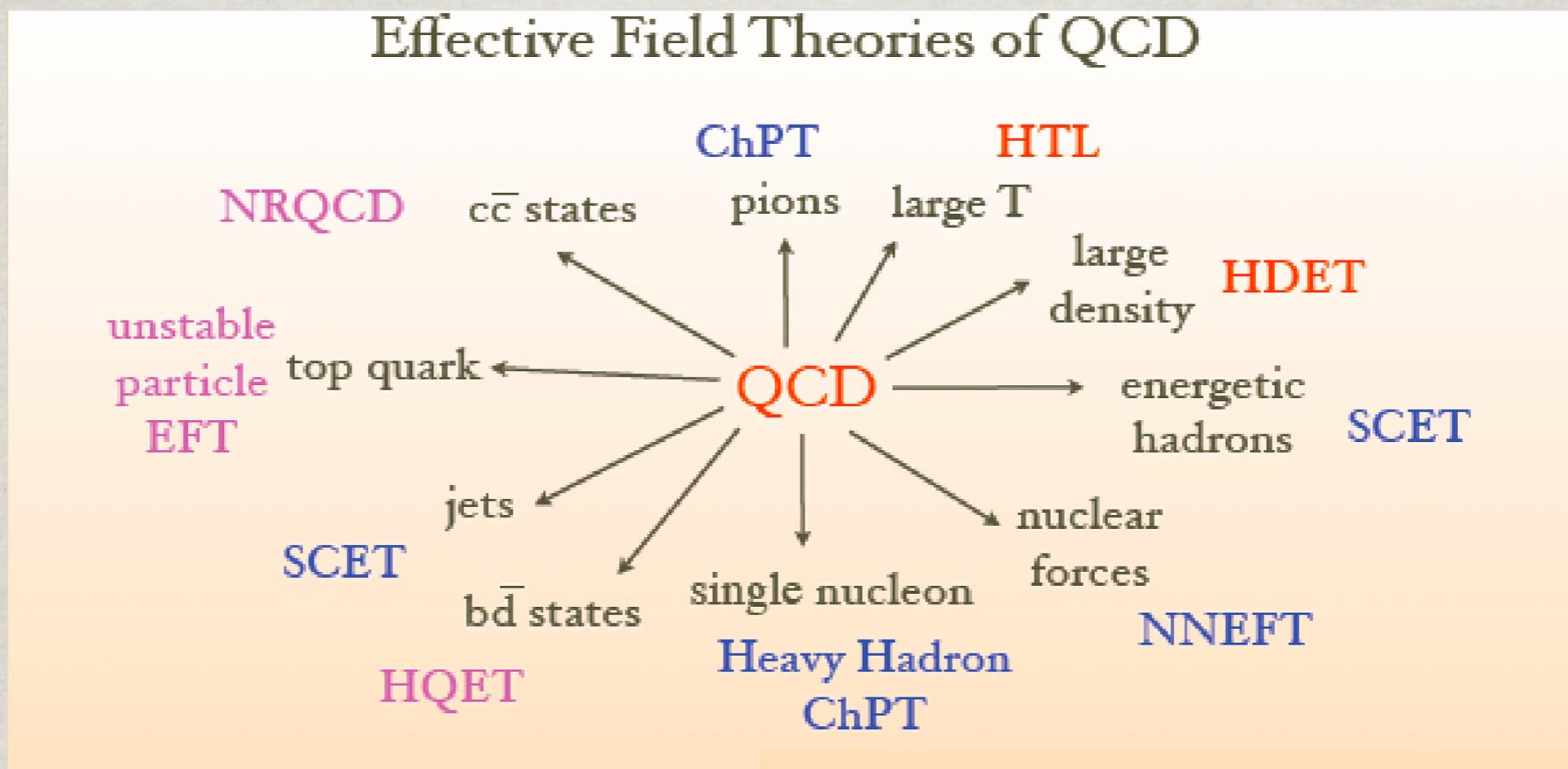
- If $\Lambda \gg \Lambda_{\text{QCD}}$ then $c_n(\Lambda/\mu)$ may be calculated in perturbation theory.

- Symmetries of the system become manifest;

- Large $\log(\Lambda/\lambda)$ can be resummed via RG. (Renormalization group)

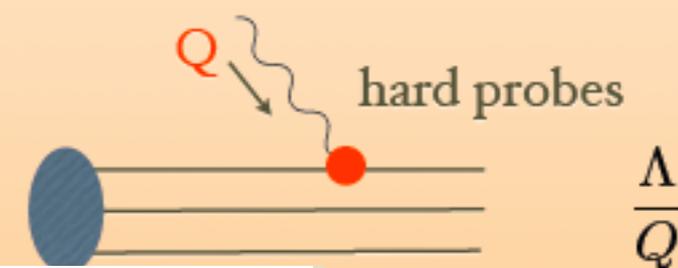
QCD Effective Field Theories

To address the research frontier of strong interactions we need to construct effective field theories

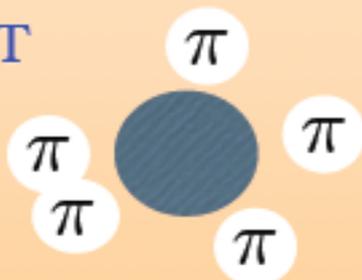


- Heavy quark effective theory (HQET): $\frac{\lambda}{\Lambda} = \frac{\Lambda_{\text{QCD}}}{m}$

Soft-Collinear Effective Theory (SCET)



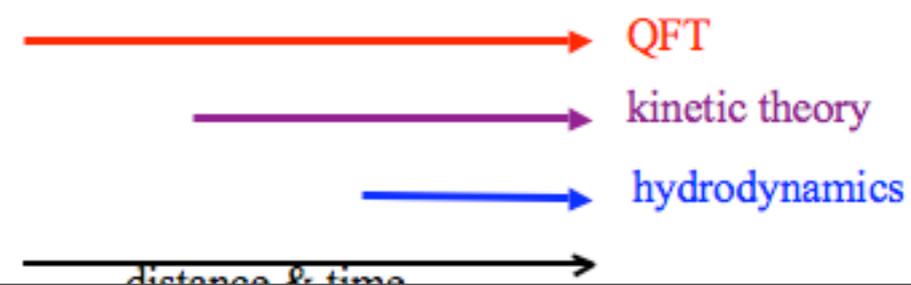
ChPT



$$\frac{m_\pi}{\Lambda} \ll 1$$

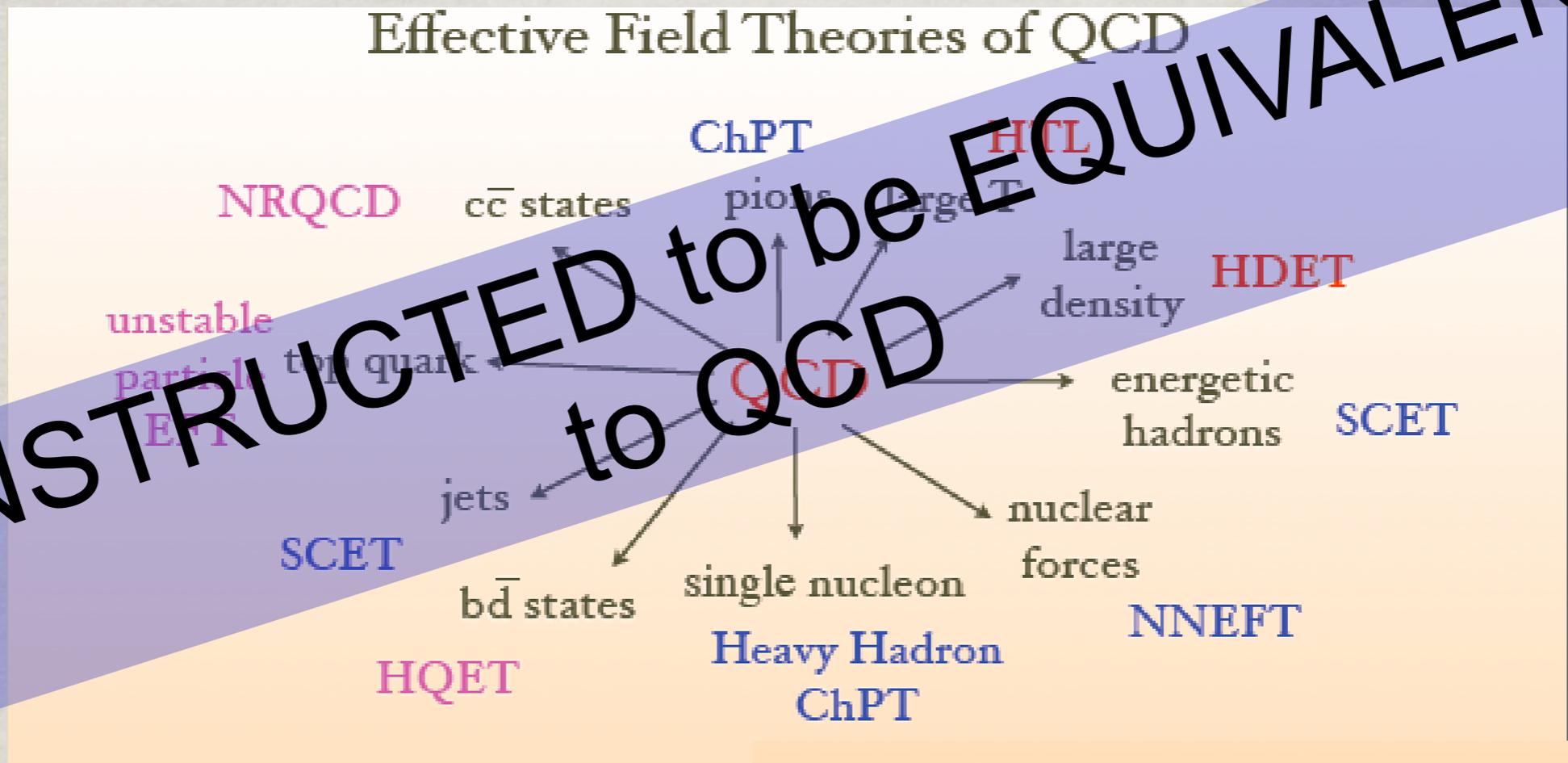
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Lattice QCD \equiv Effective Field Theory ($\Lambda = \pi/a$).



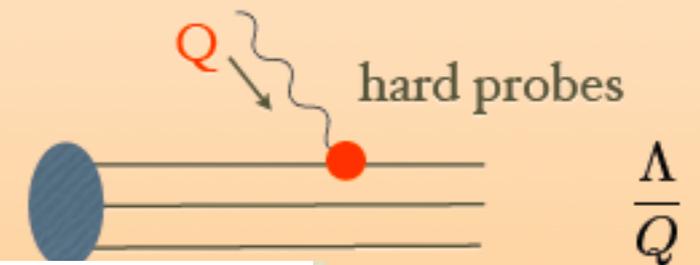
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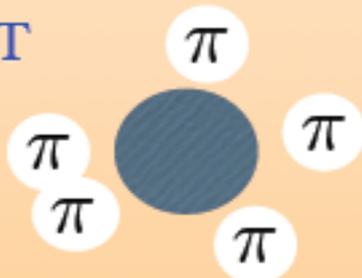


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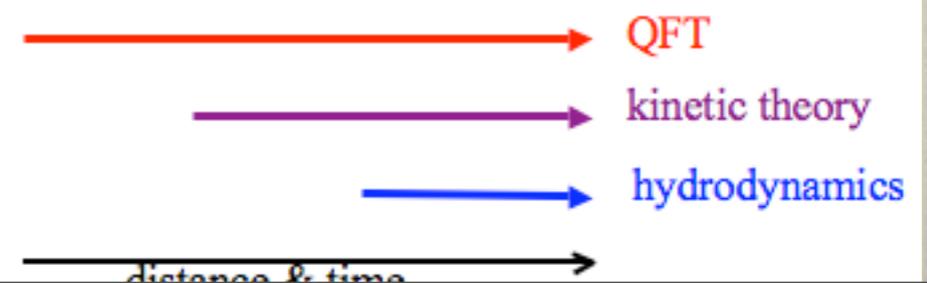
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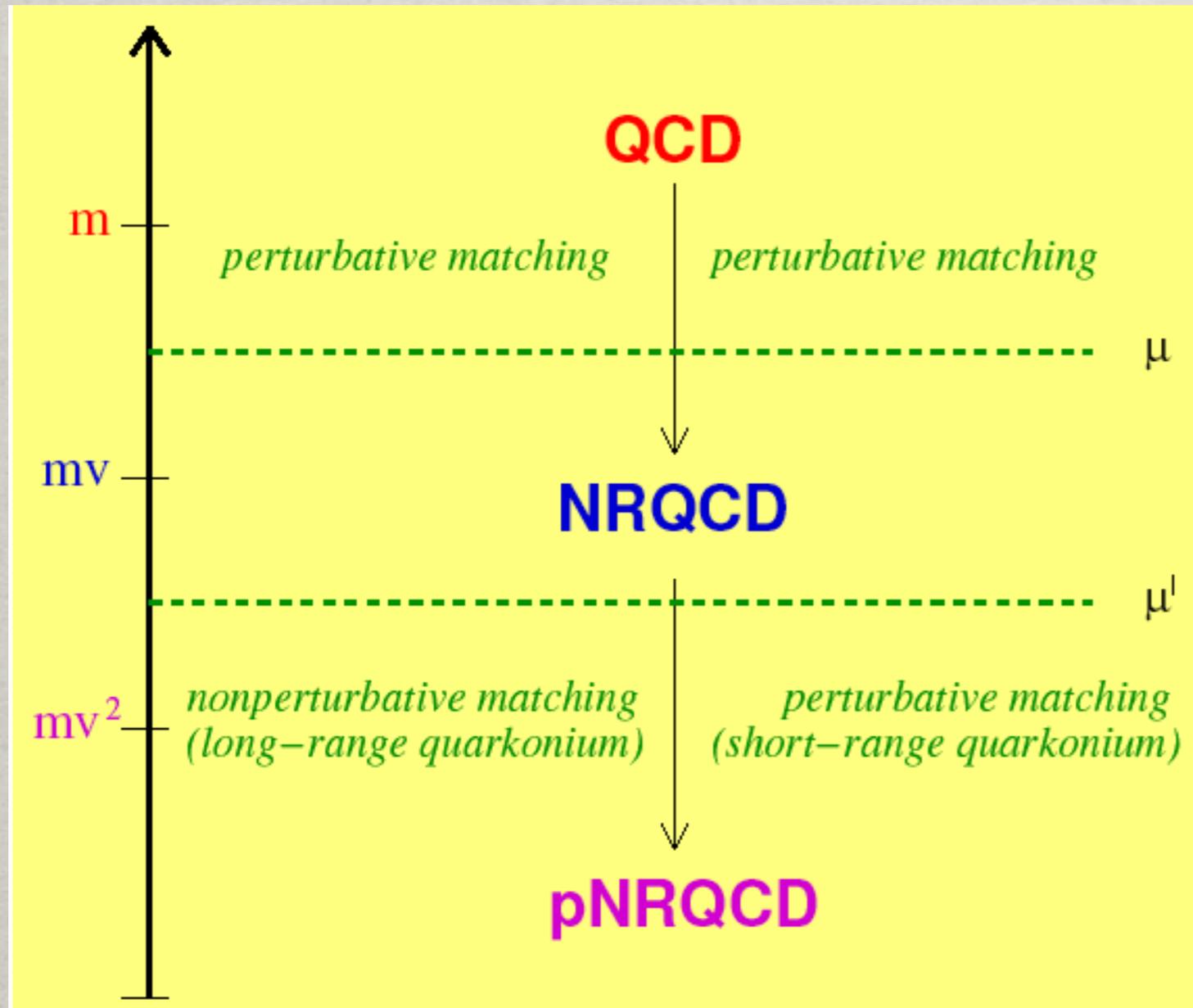
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Quarkonium with NR EFT

Color degrees of freedom
 $3 \times 3 = 1 + 8$
singlet and octet $Q\bar{Q}$



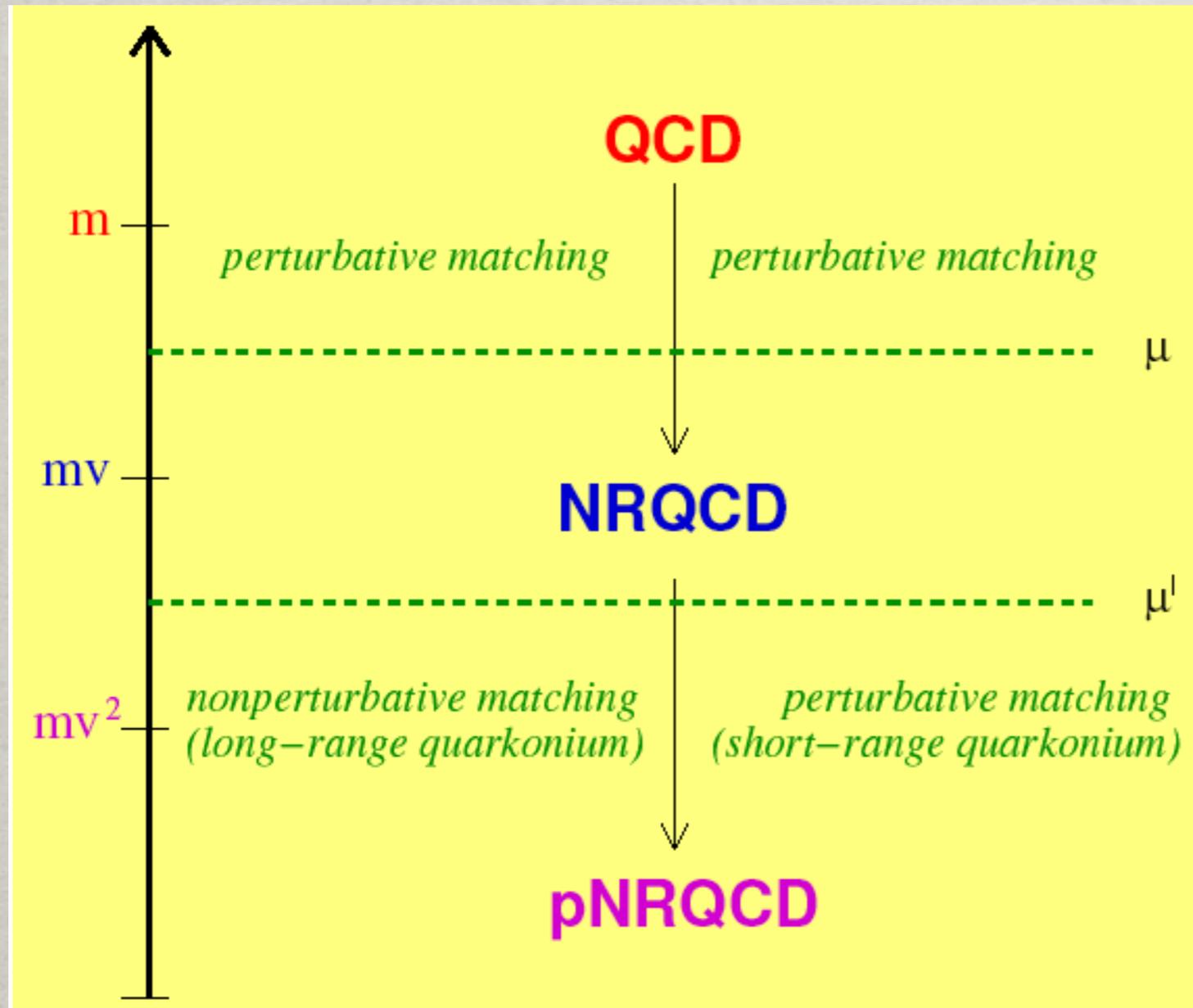
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Soft
(relative
momentum)

Ultrasoft
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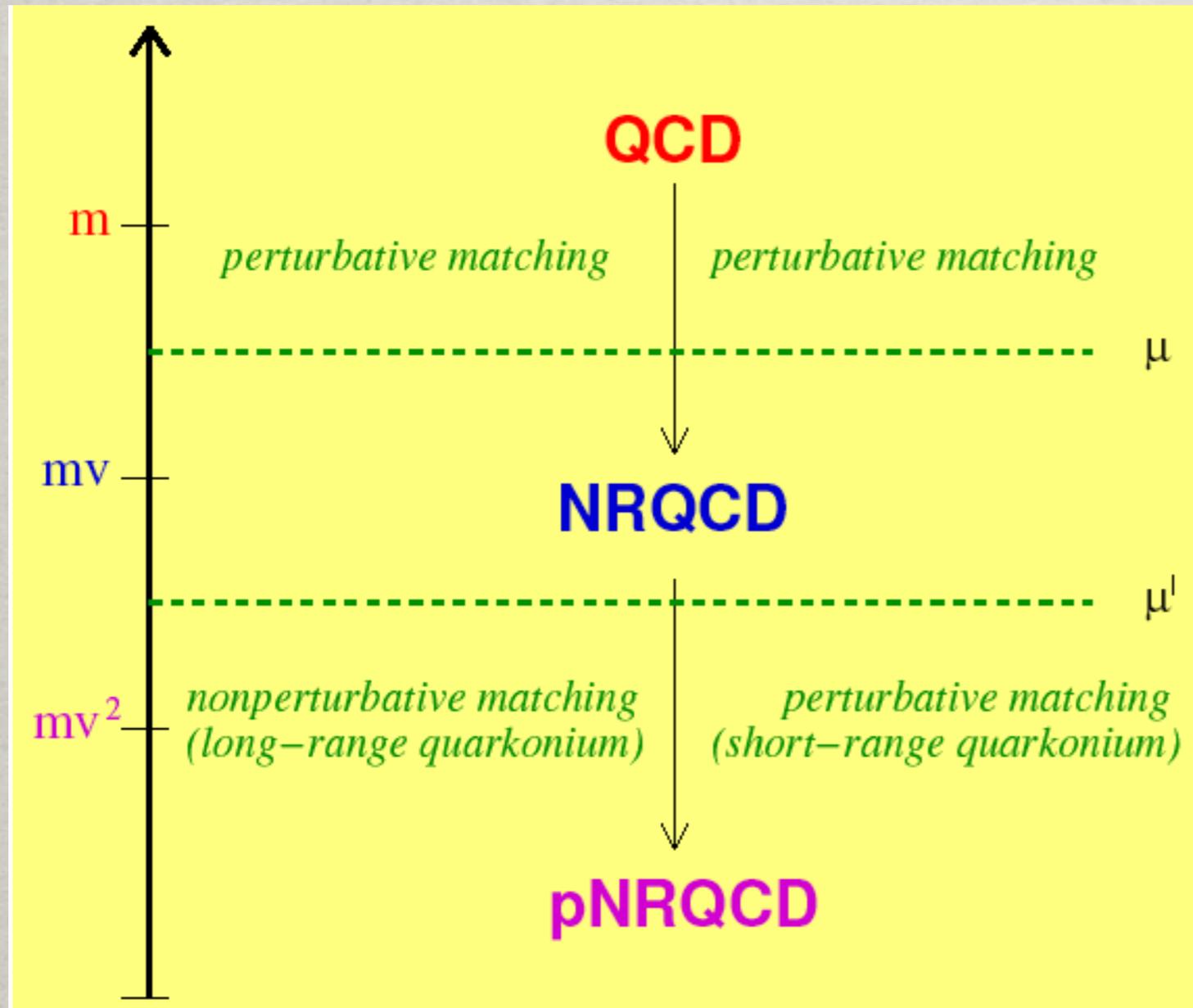
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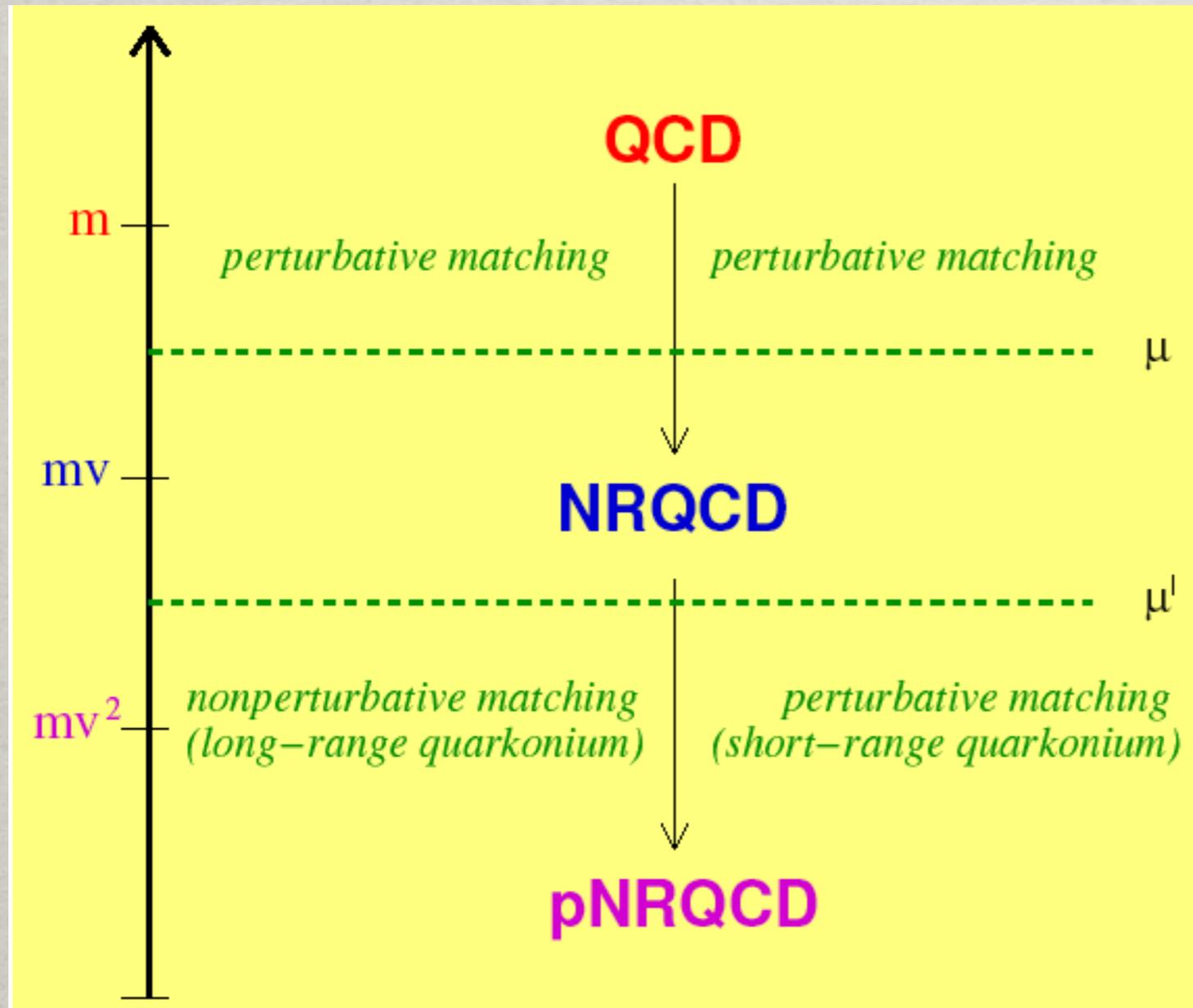
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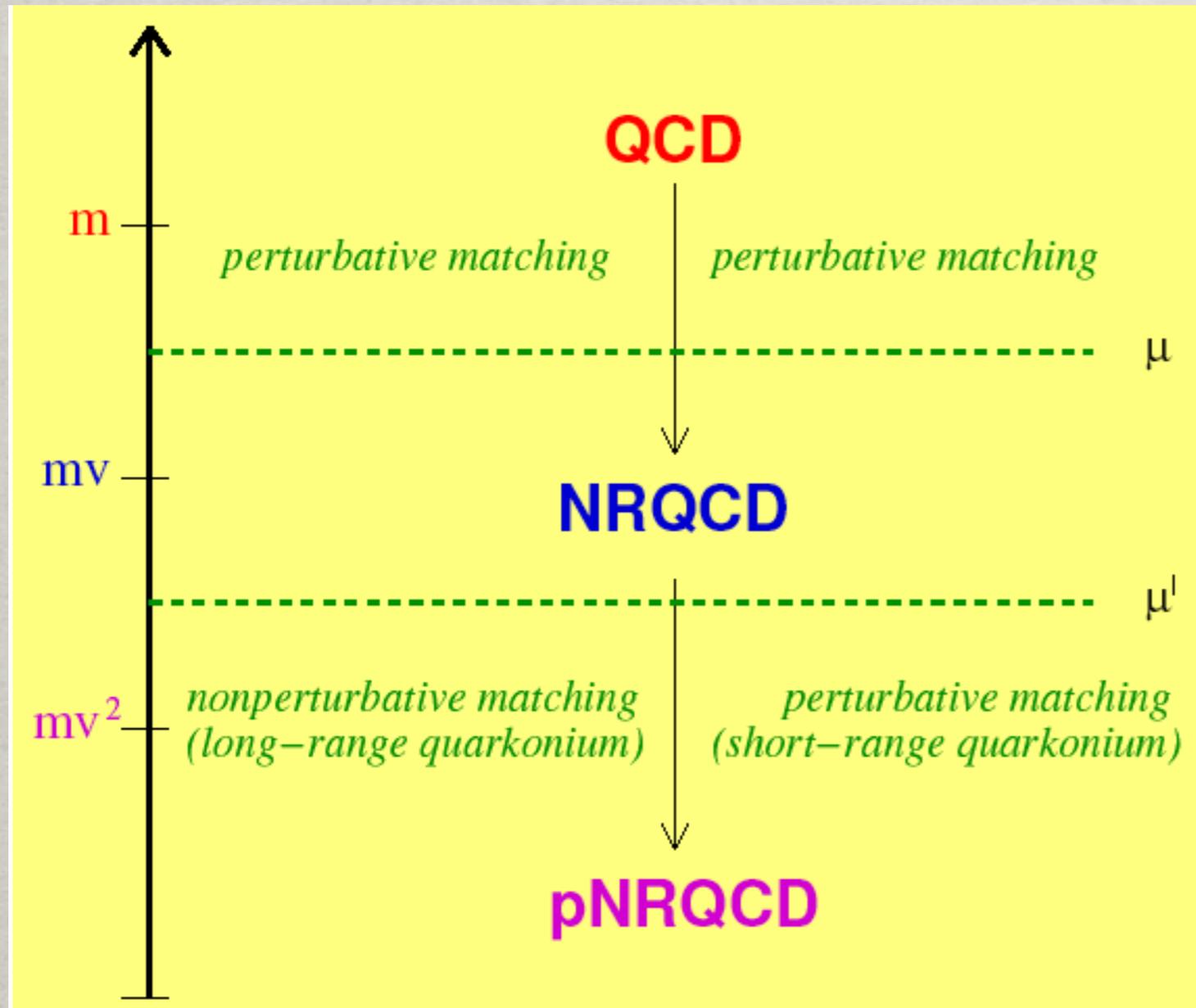
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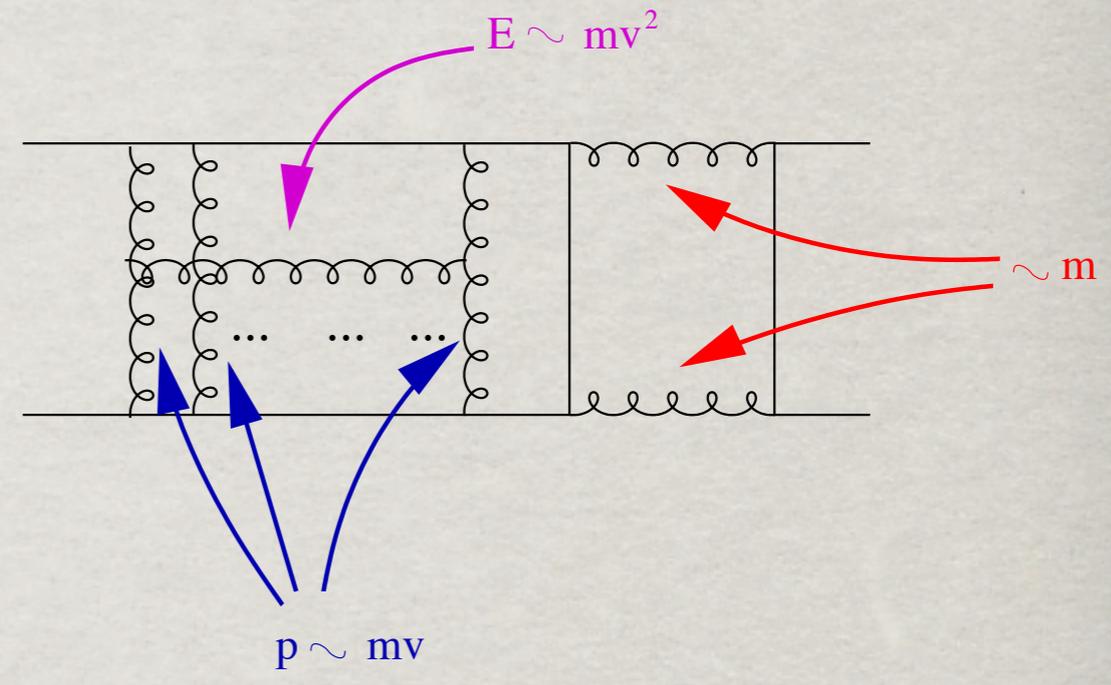
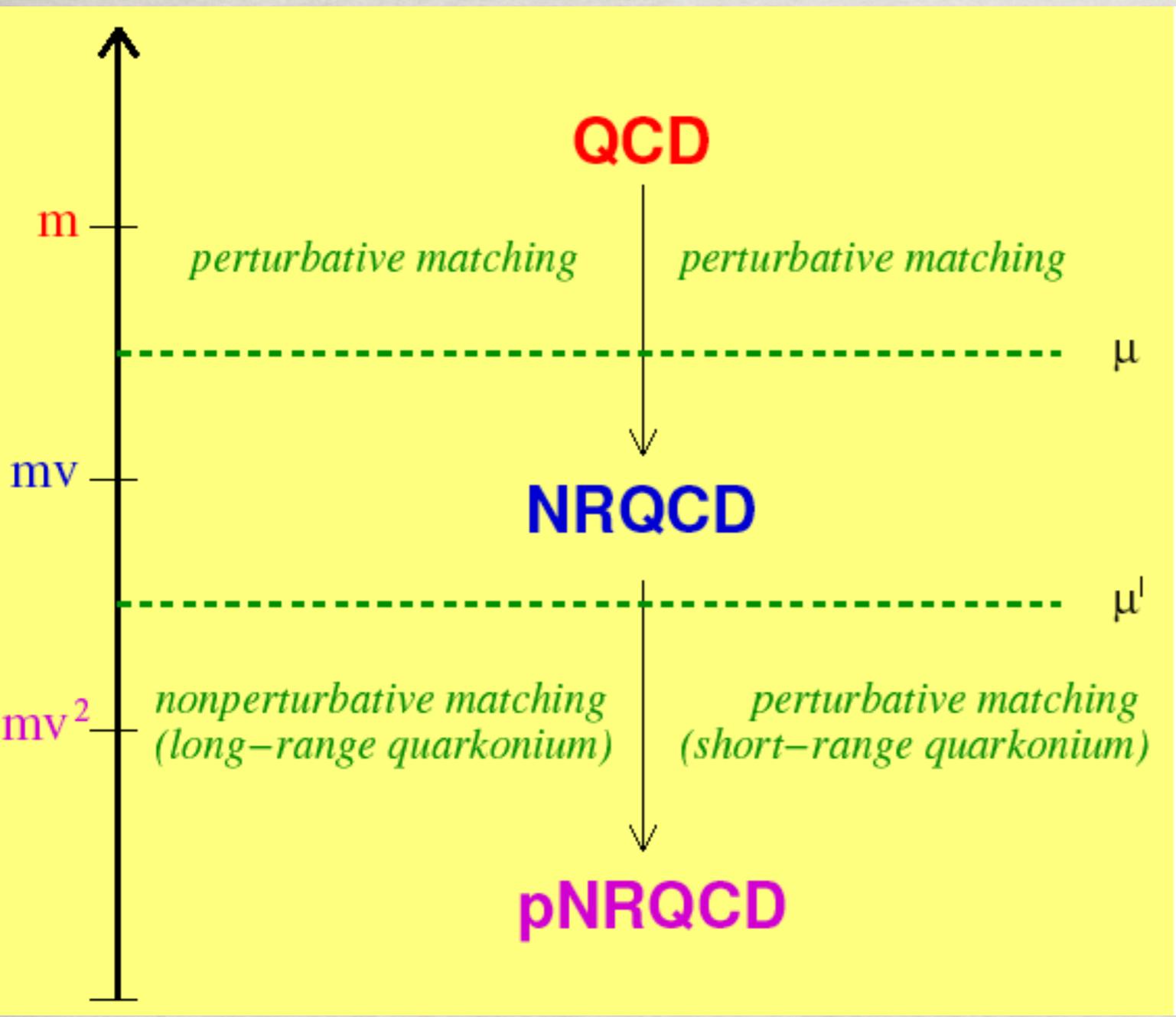
$$\frac{E_\lambda}{E_\Lambda} = \frac{mv^2}{mv}$$

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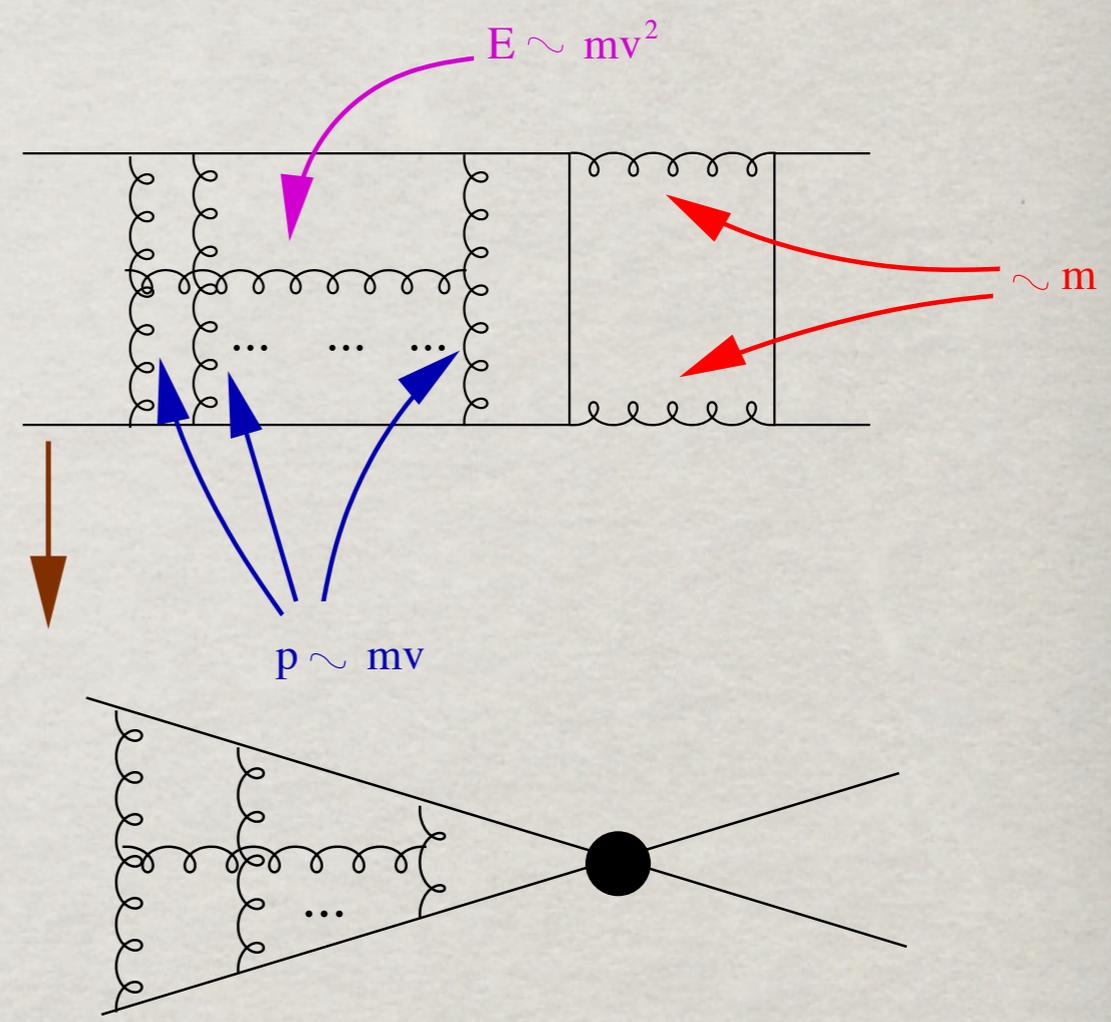
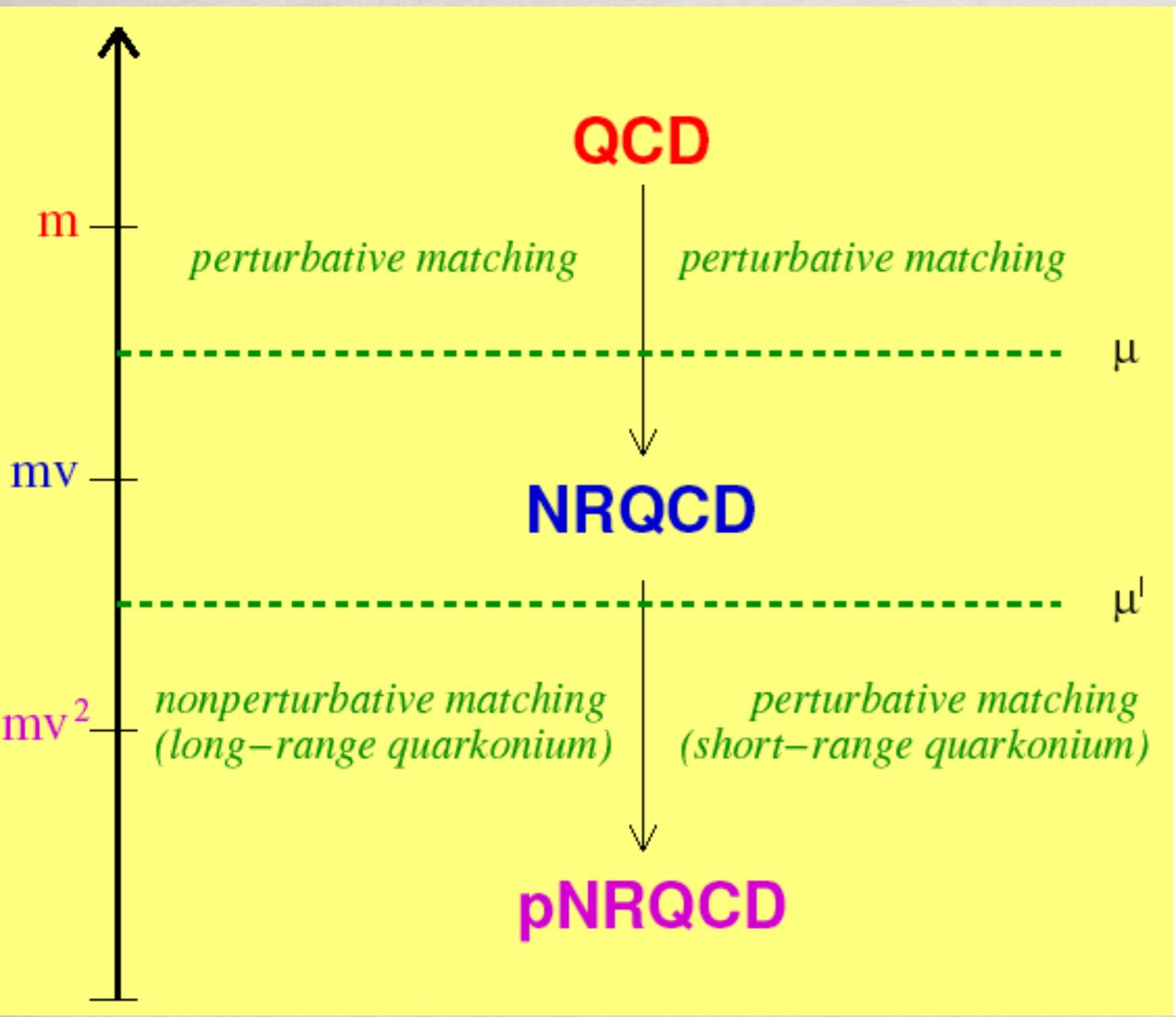
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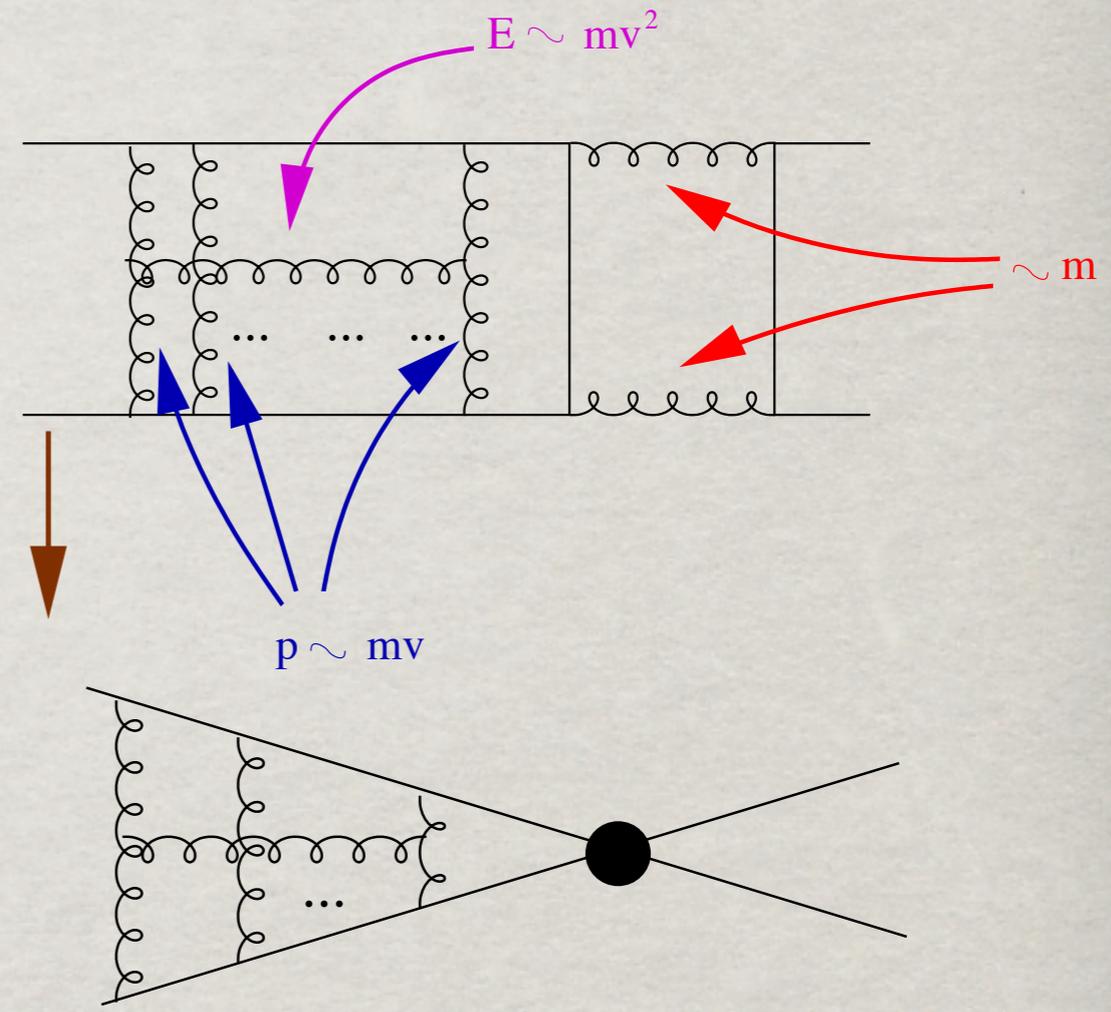
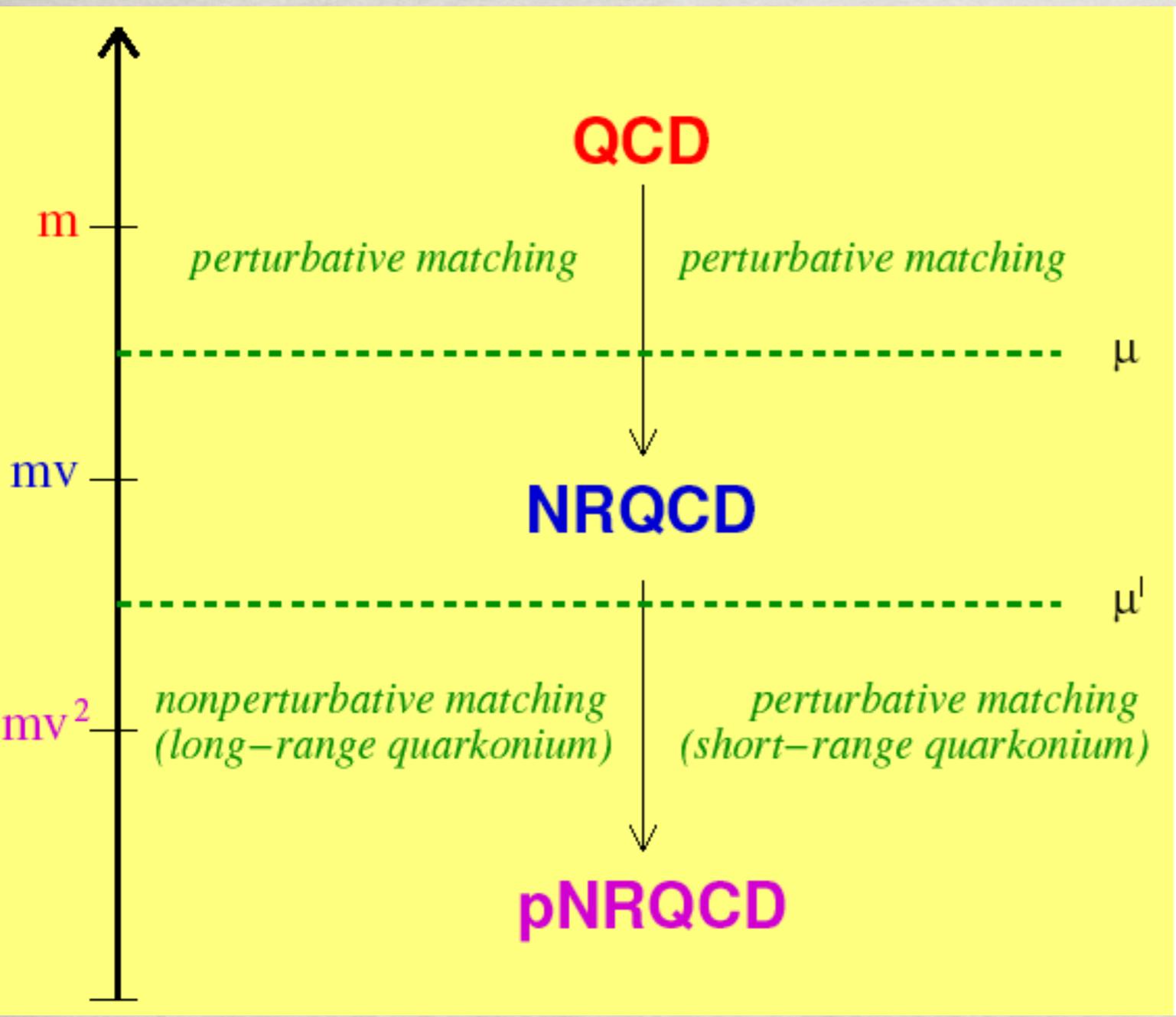
Quarkonium with NR EFT: Non Relativistic QCD (NRQCD)



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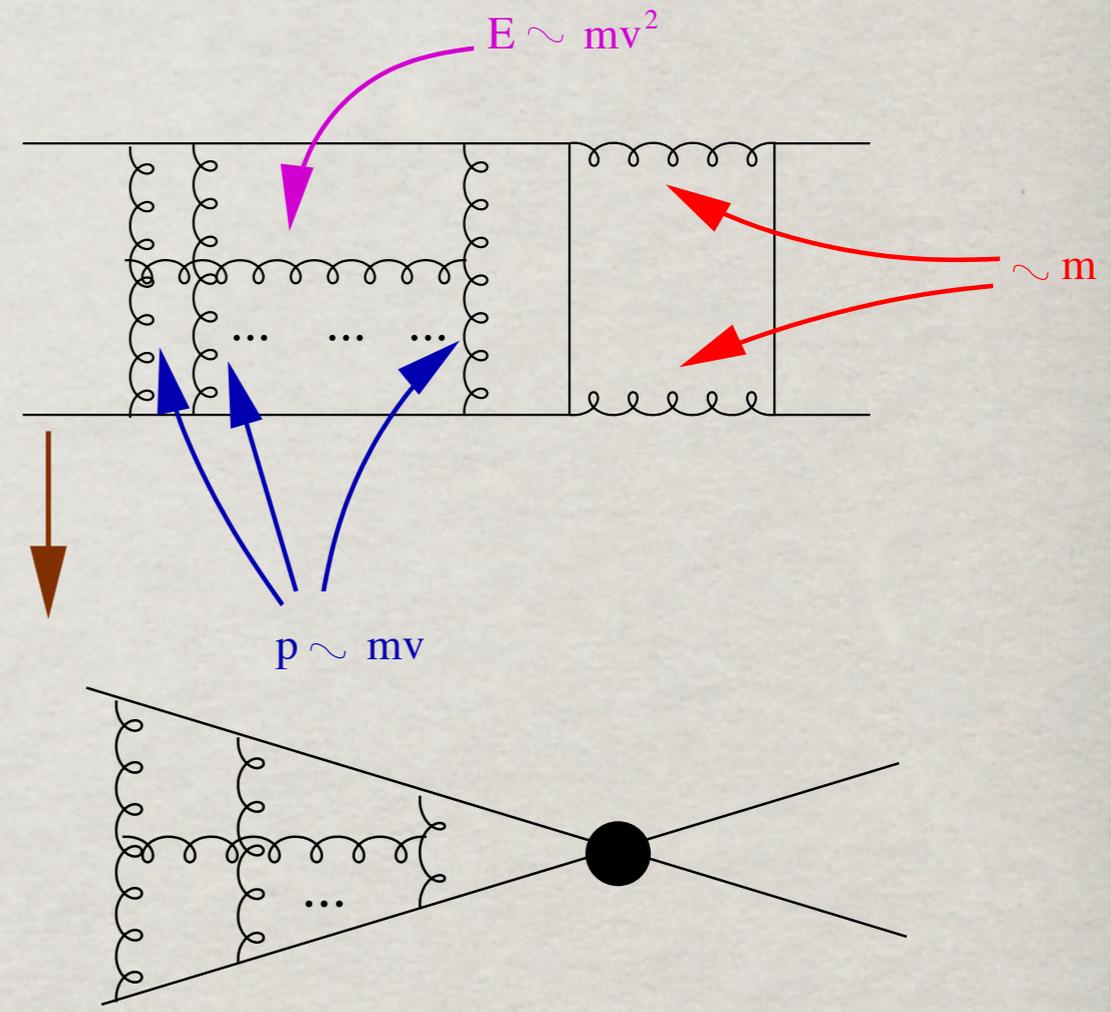
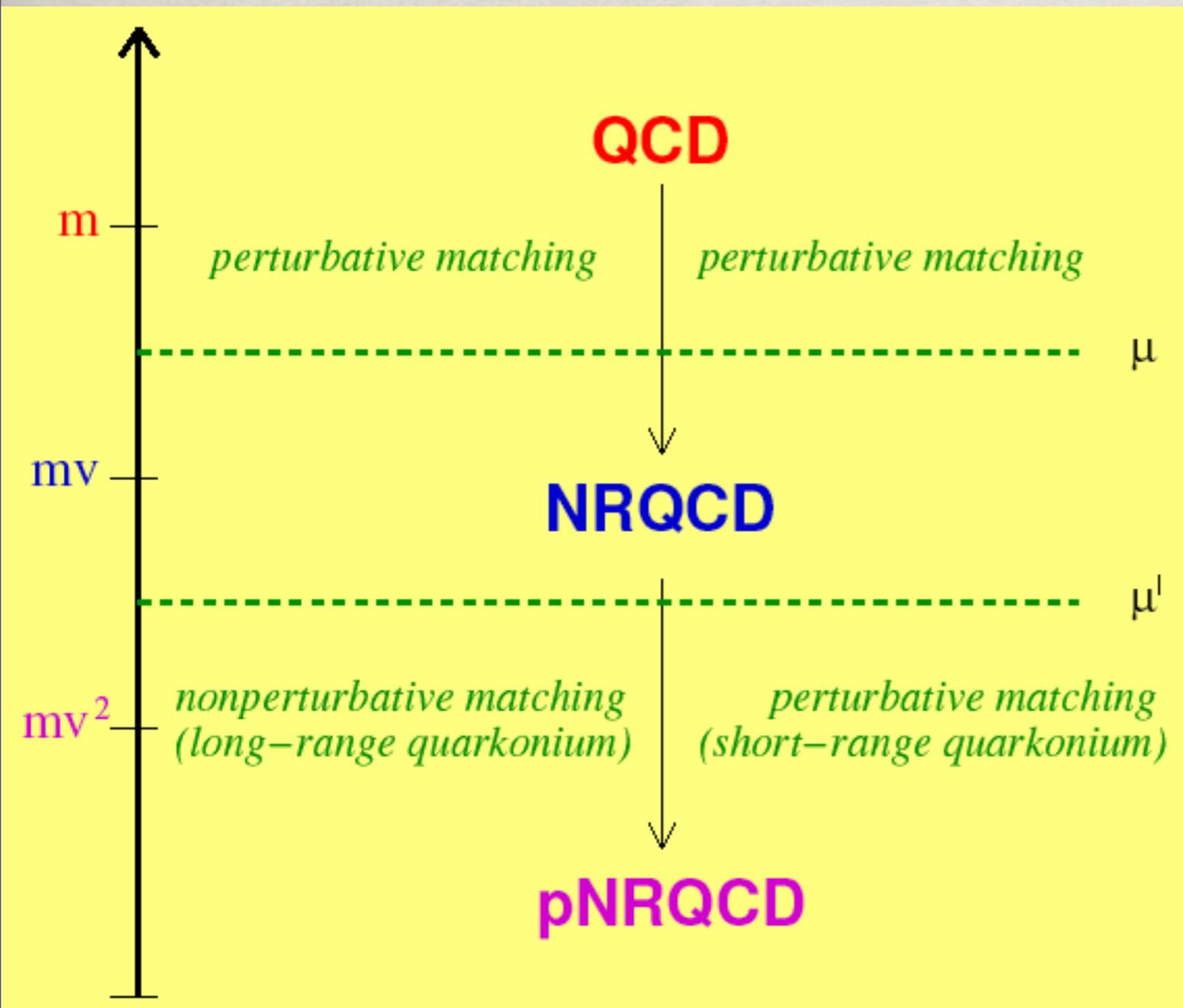


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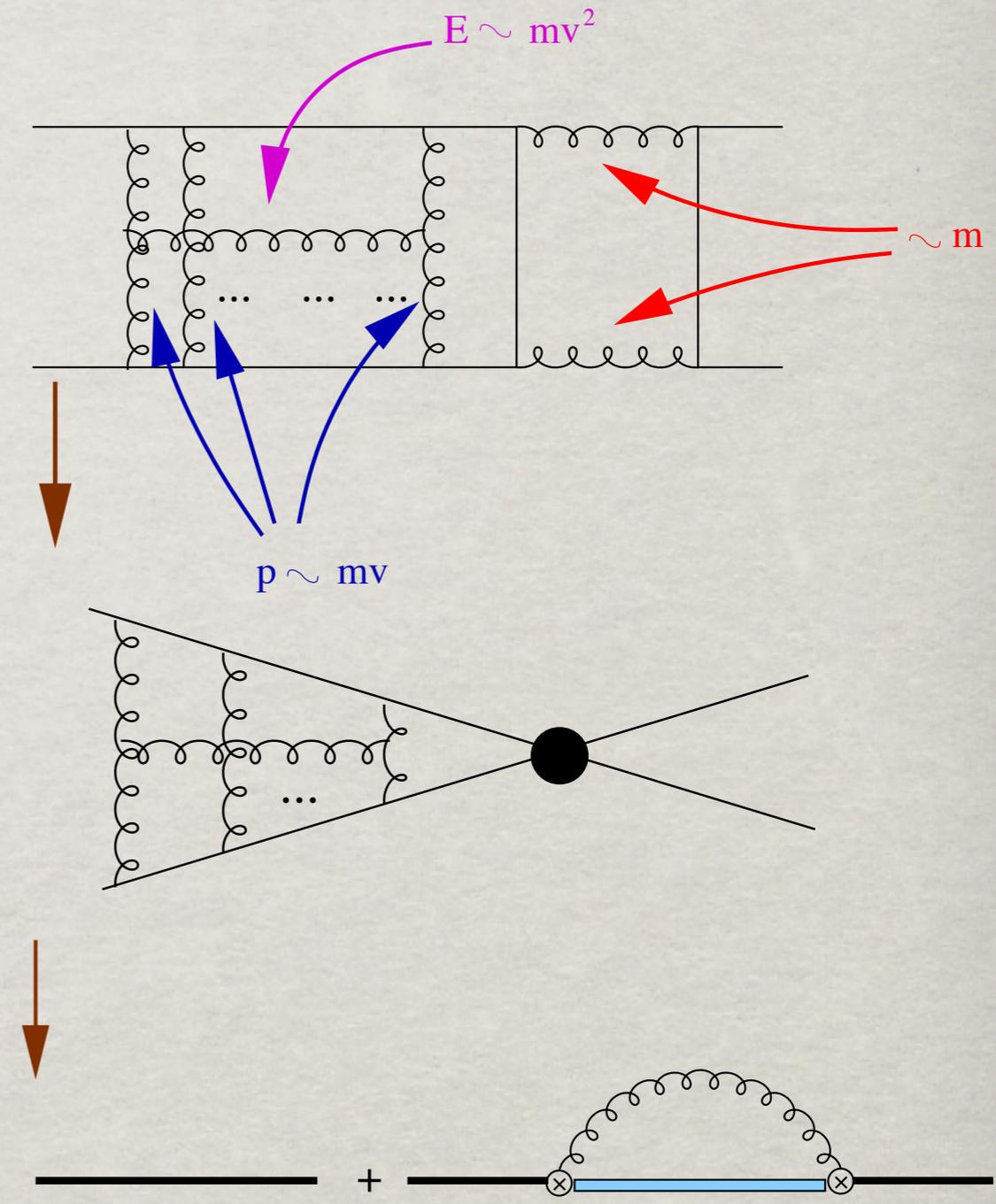
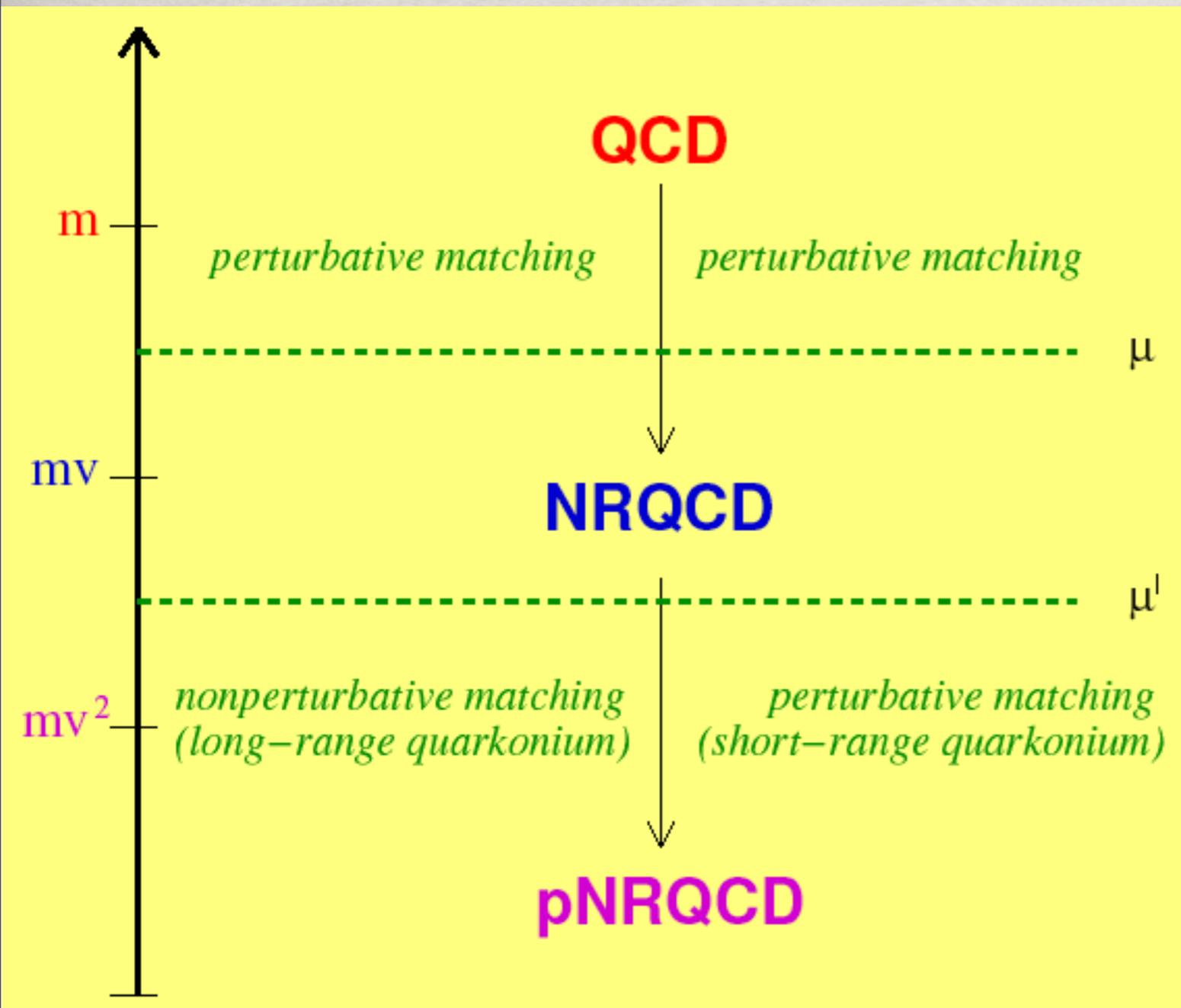


$$\mathcal{L}_{\text{NRQCD}} = \sum_n c(\alpha_s(m/\mu)) \times \frac{O_n(\mu, \lambda)}{m^n}$$

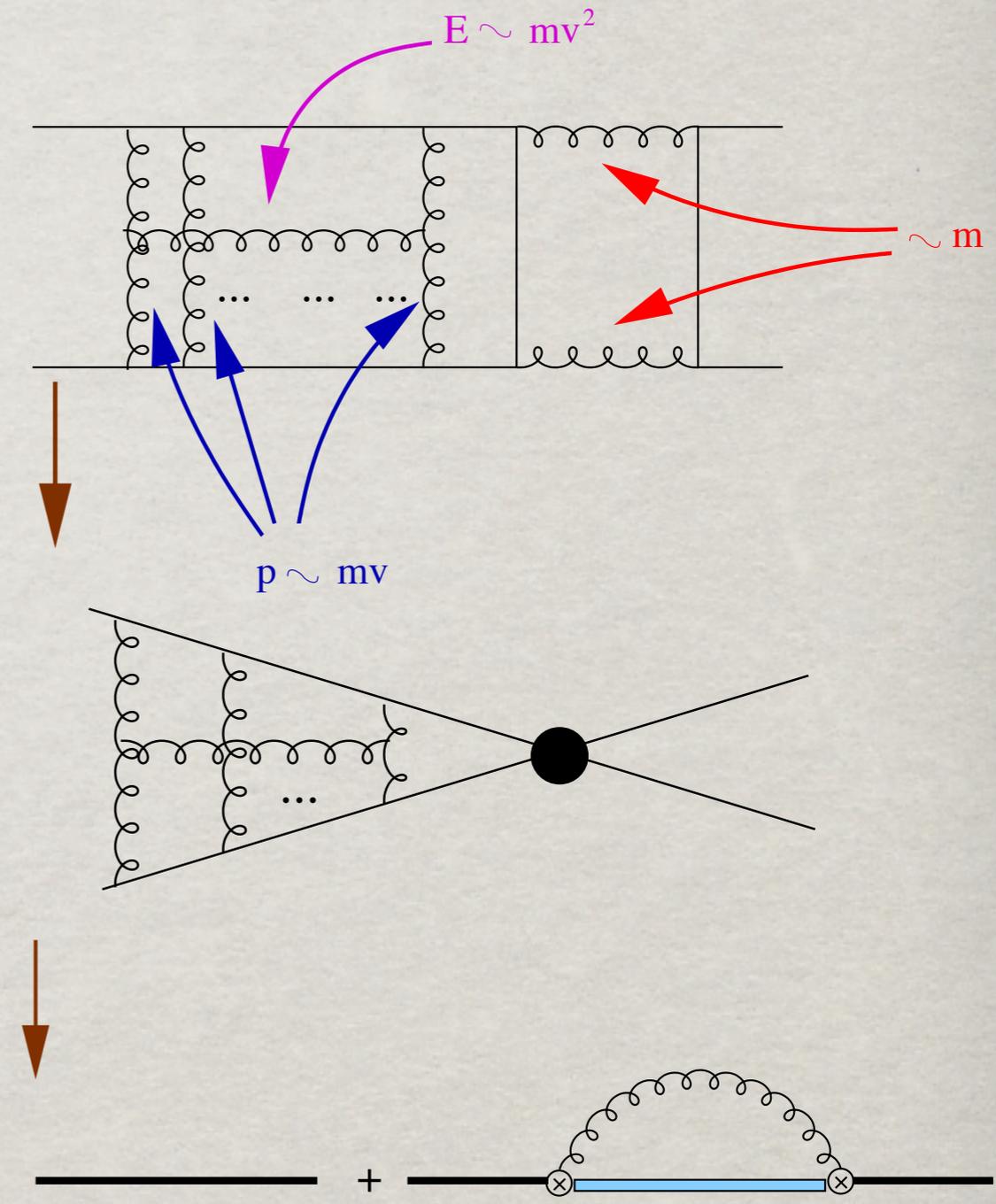
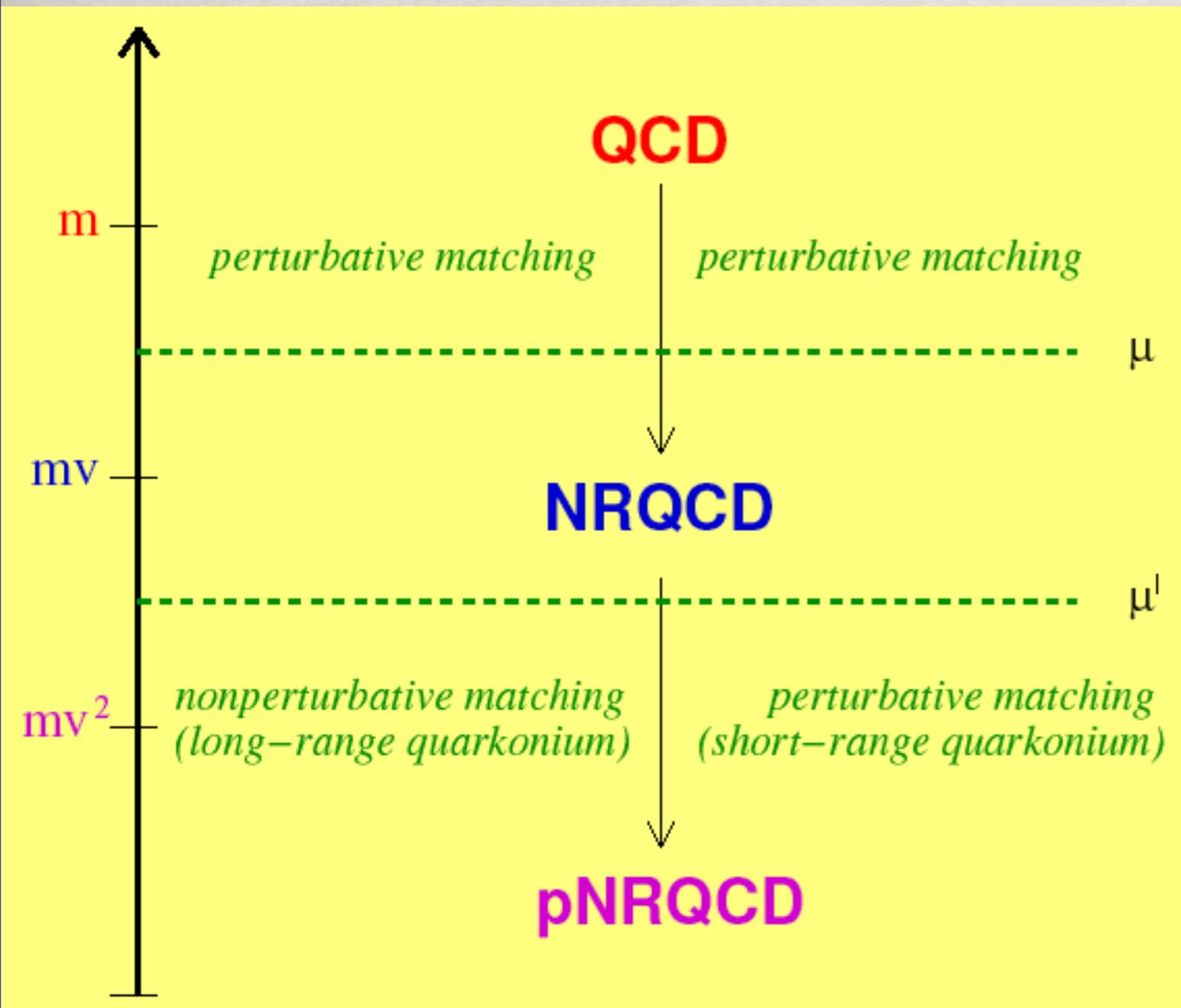
Quarkonium with NR EFT: potential NonRelativistic QCD (pNRQCD)



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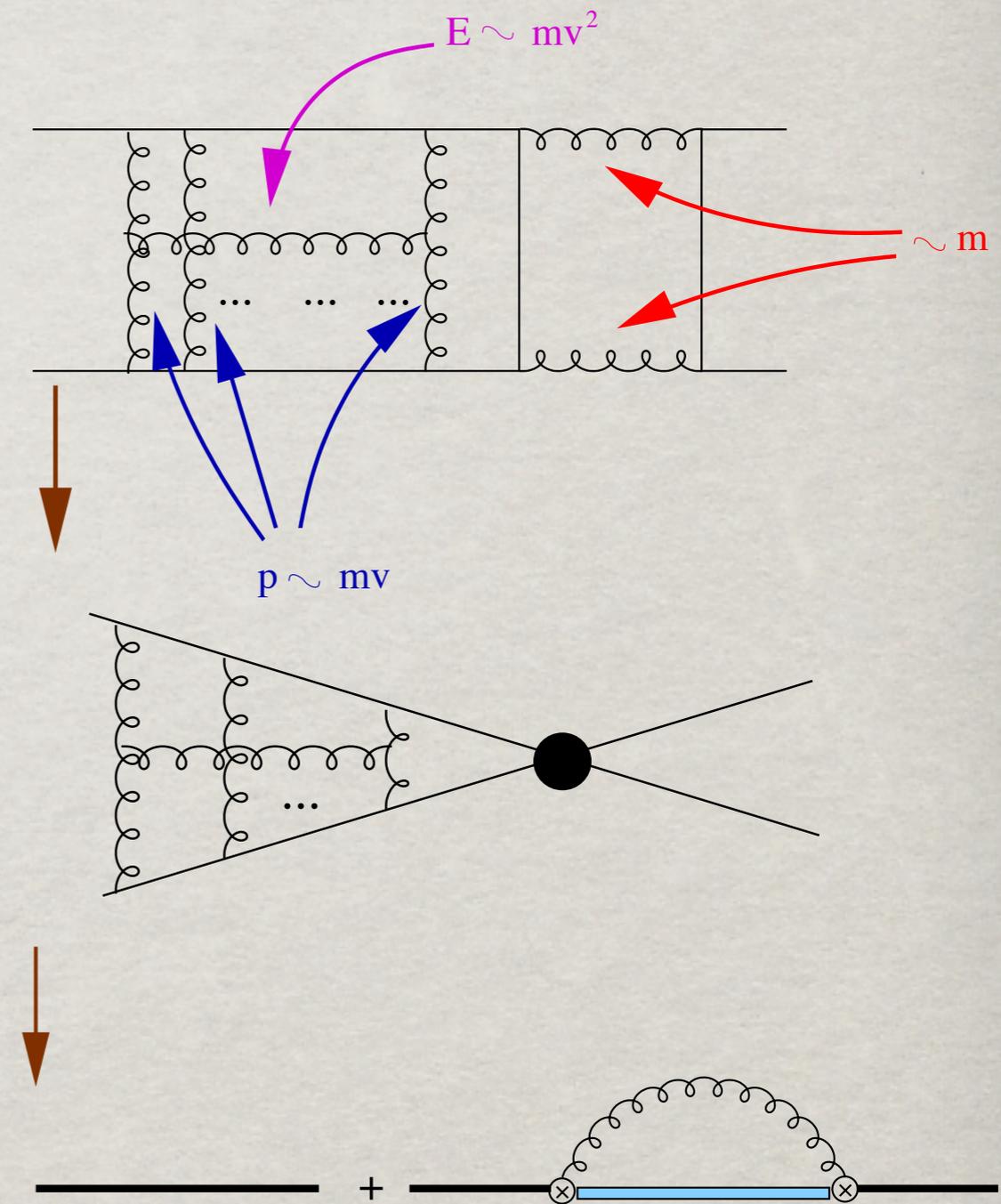
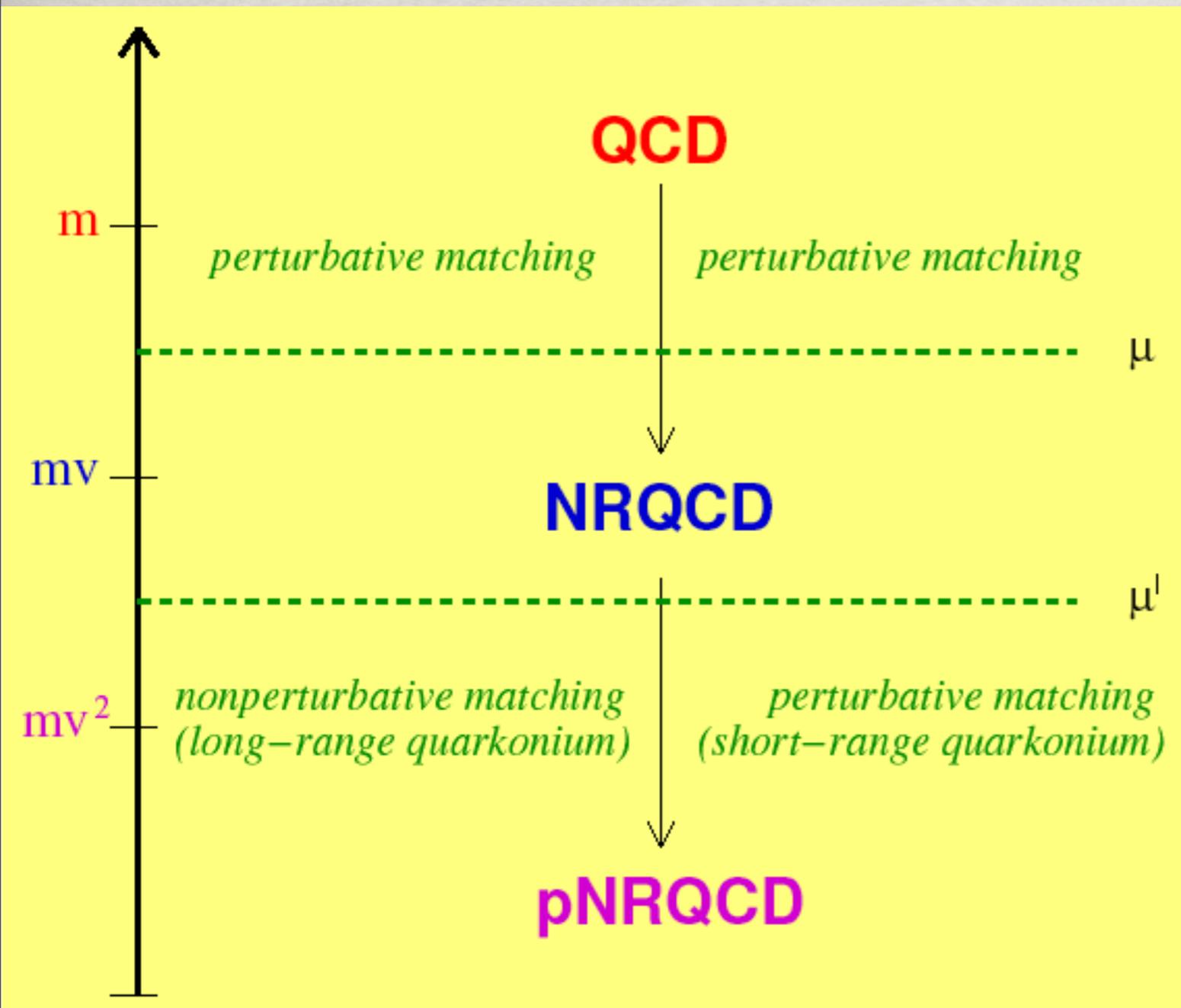


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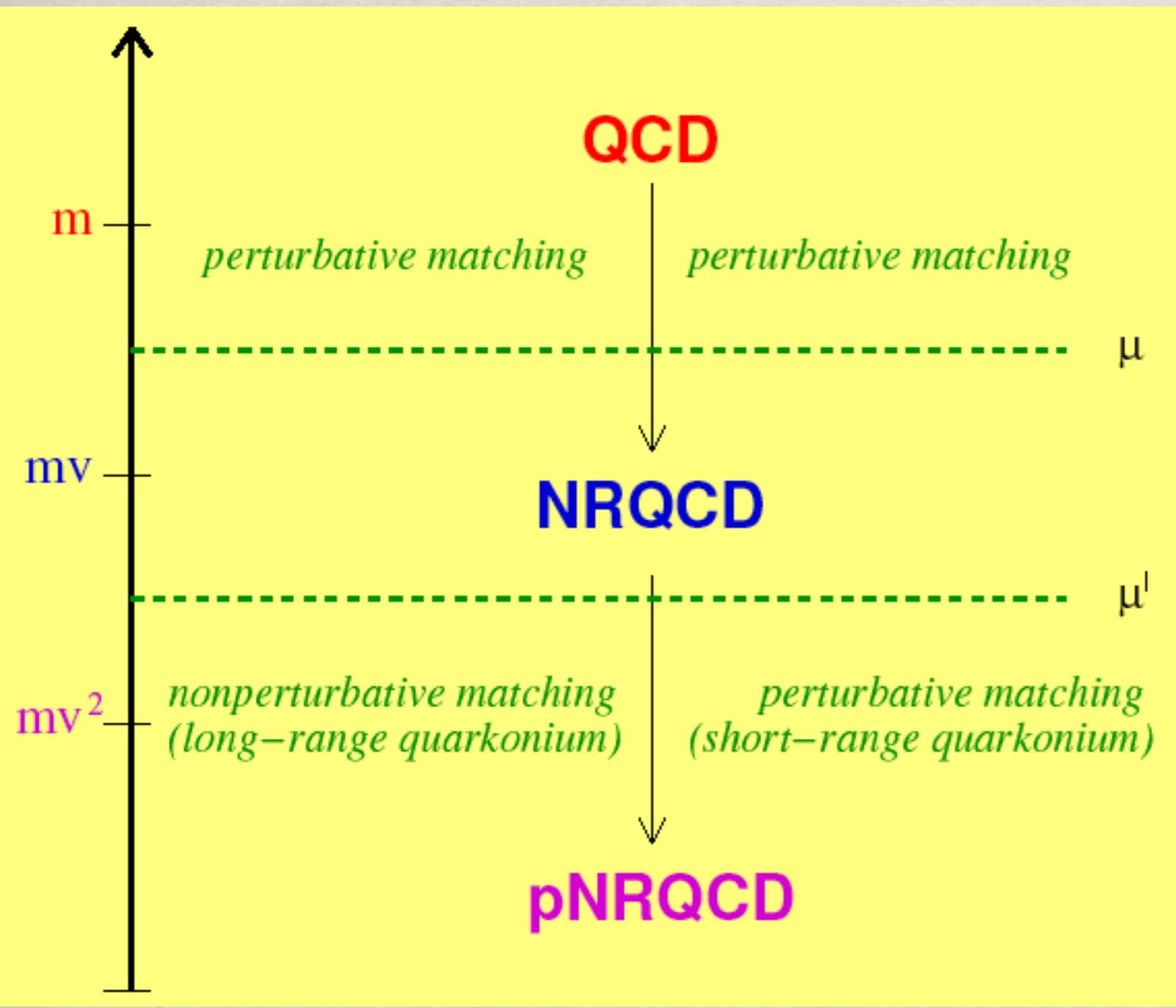
$$\mathcal{L}_{\text{pNRQCD}} = \sum_k \sum_n \frac{1}{m^k} c_k(\alpha_s(m/\mu)) \times V(r\mu', r\mu) \times O_n(\mu', \lambda) r^n$$

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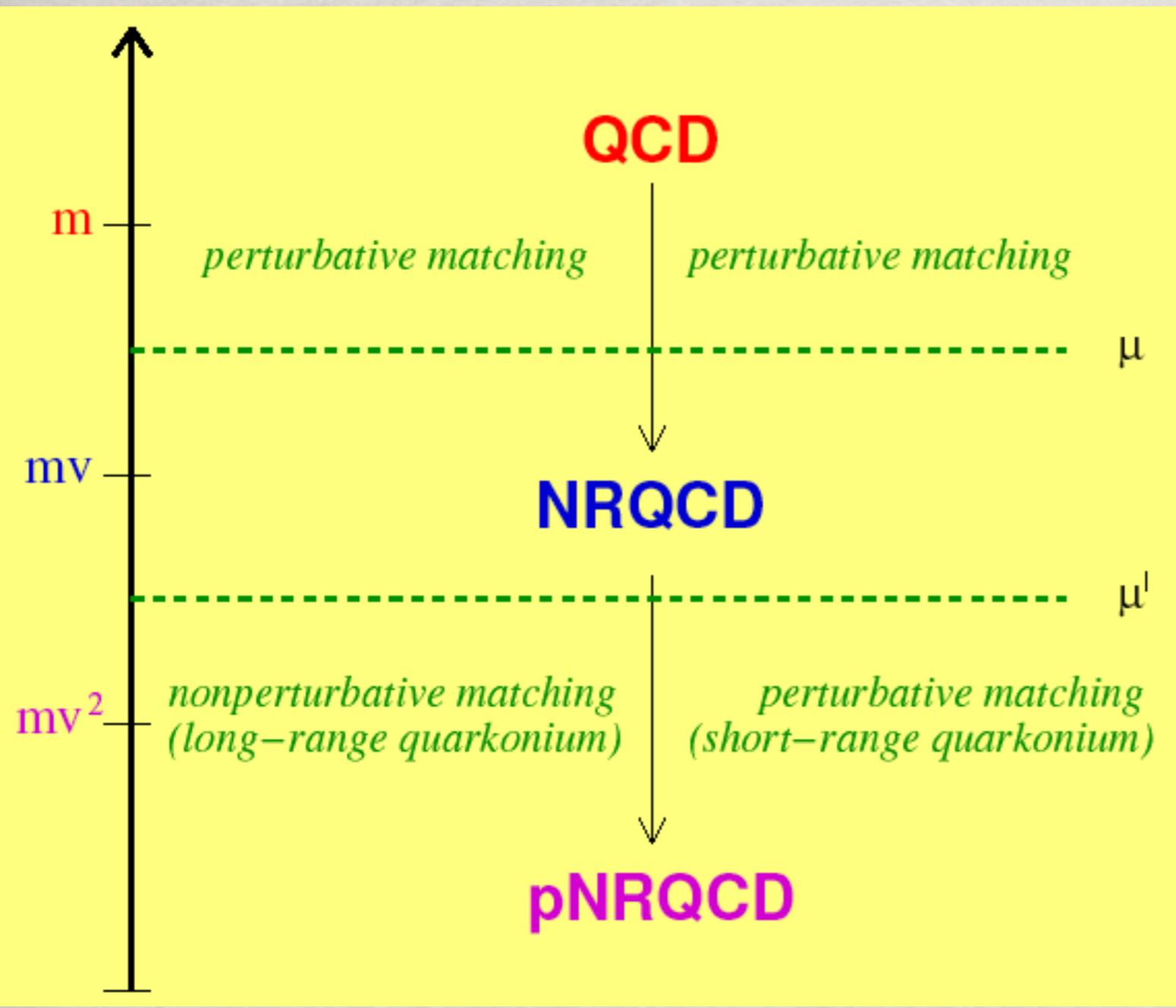


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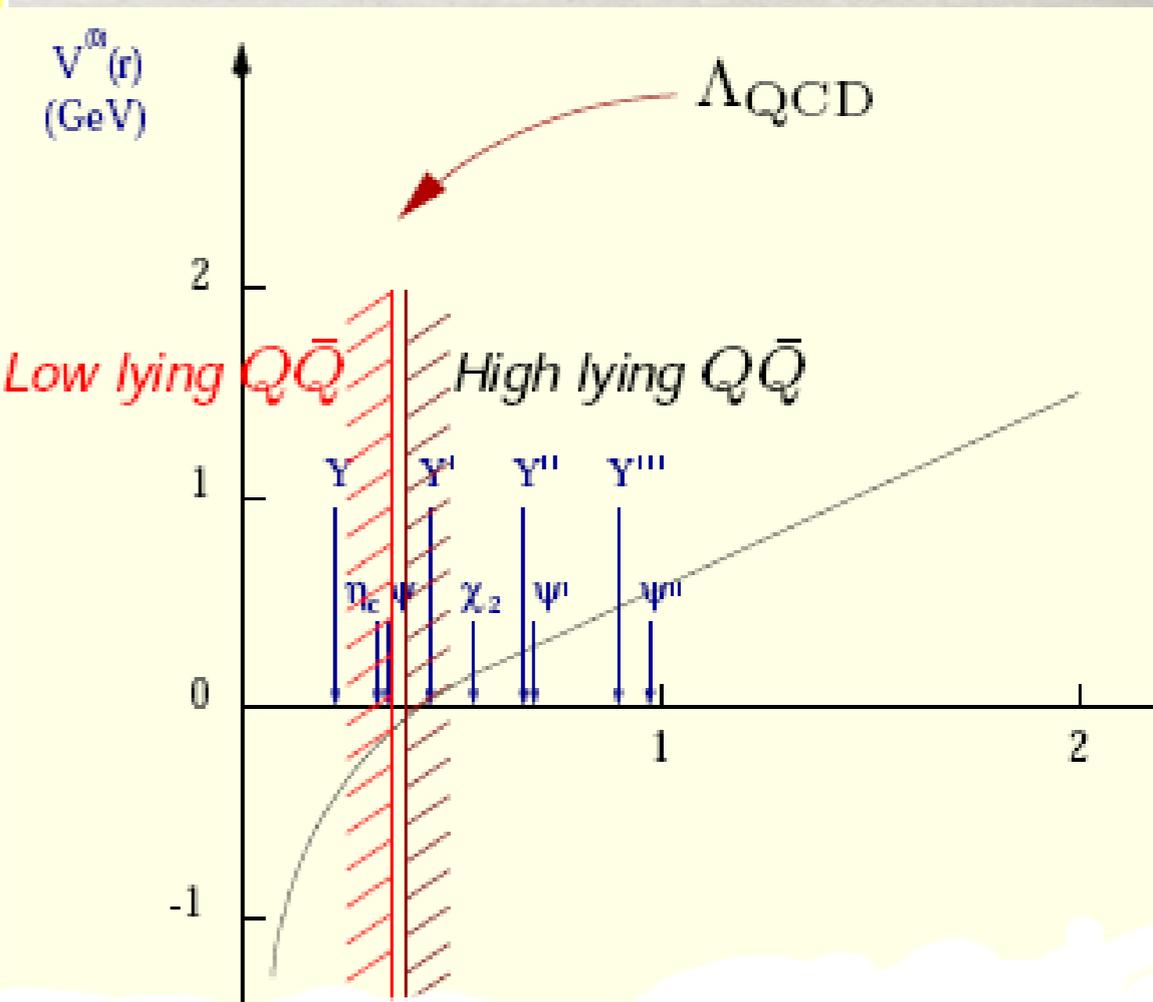
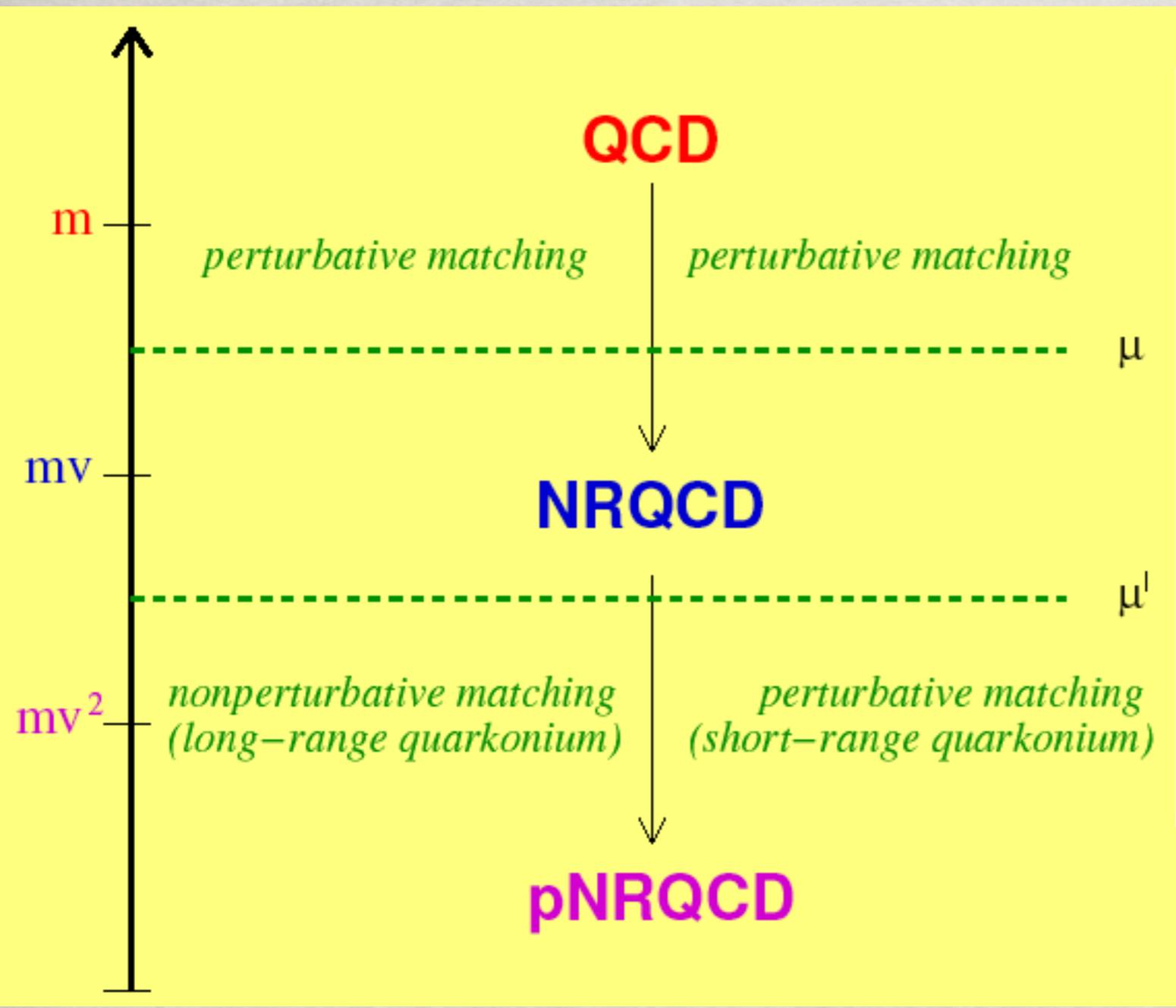
Quarkonium with NR EFT: pNRQCD



In QCD another scale is relevant

$$\Lambda_{\text{QCD}}$$

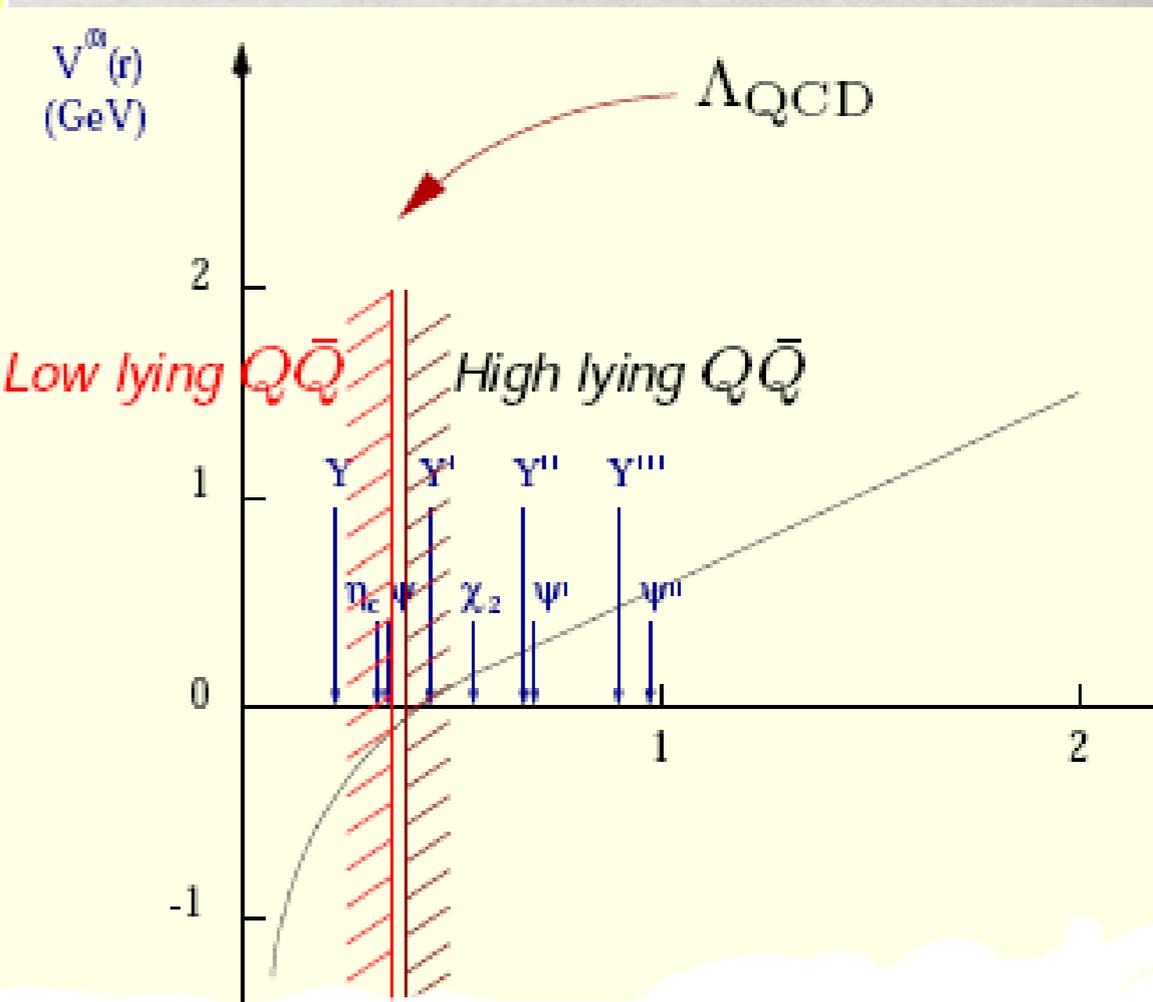
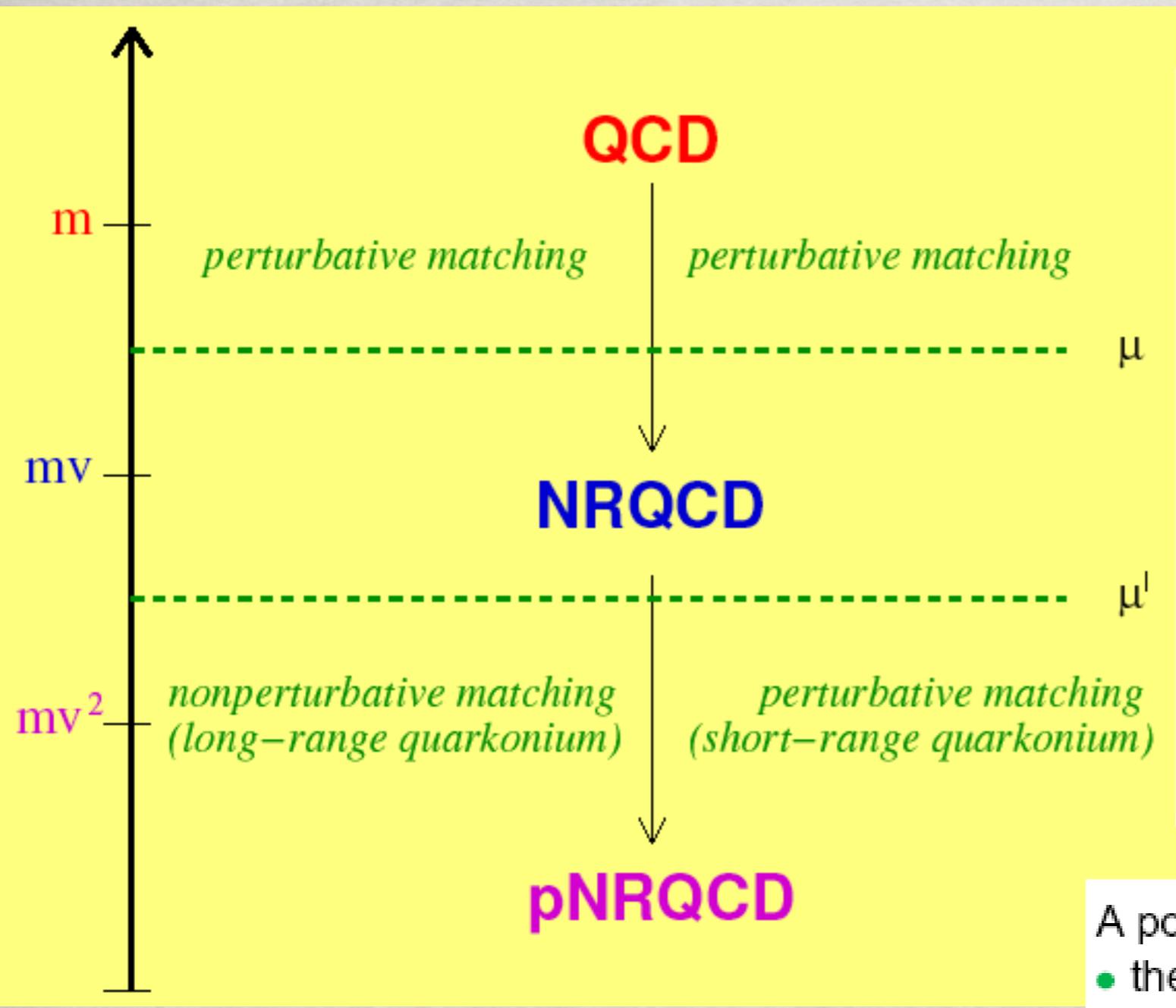
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Quarkonium with NR EFT: pNRQCD



A potential picture arises at the level of pNRQCD:

- the potential is perturbative if $mv \gg \Lambda_{\text{QCD}}$
- the potential is non-perturbative if $mv \sim \Lambda_{\text{QCD}}$

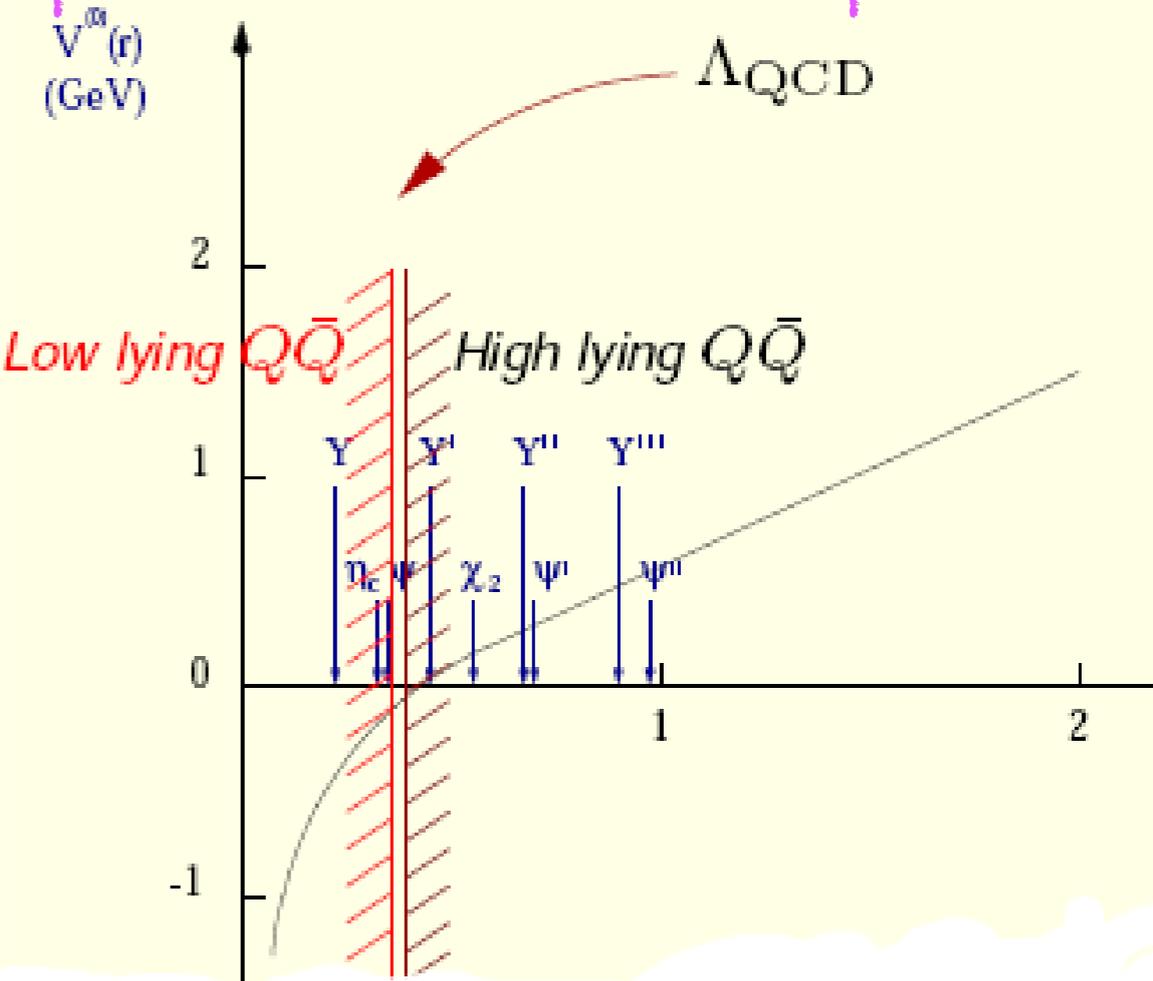
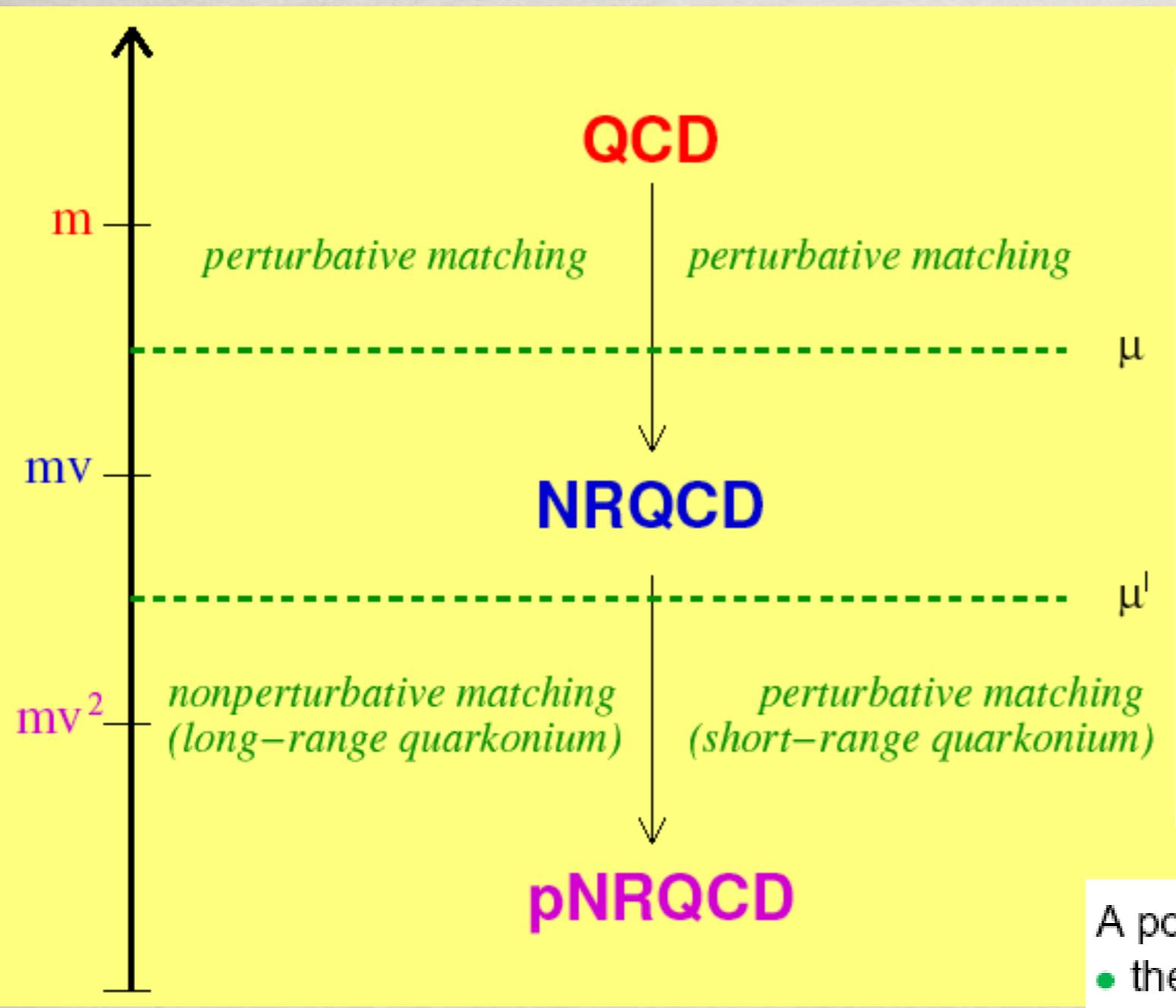
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Quarkonium with NR EFT: pNRQCD

weakly coupled
pNRQCD

strongly coupled
pNRQCD



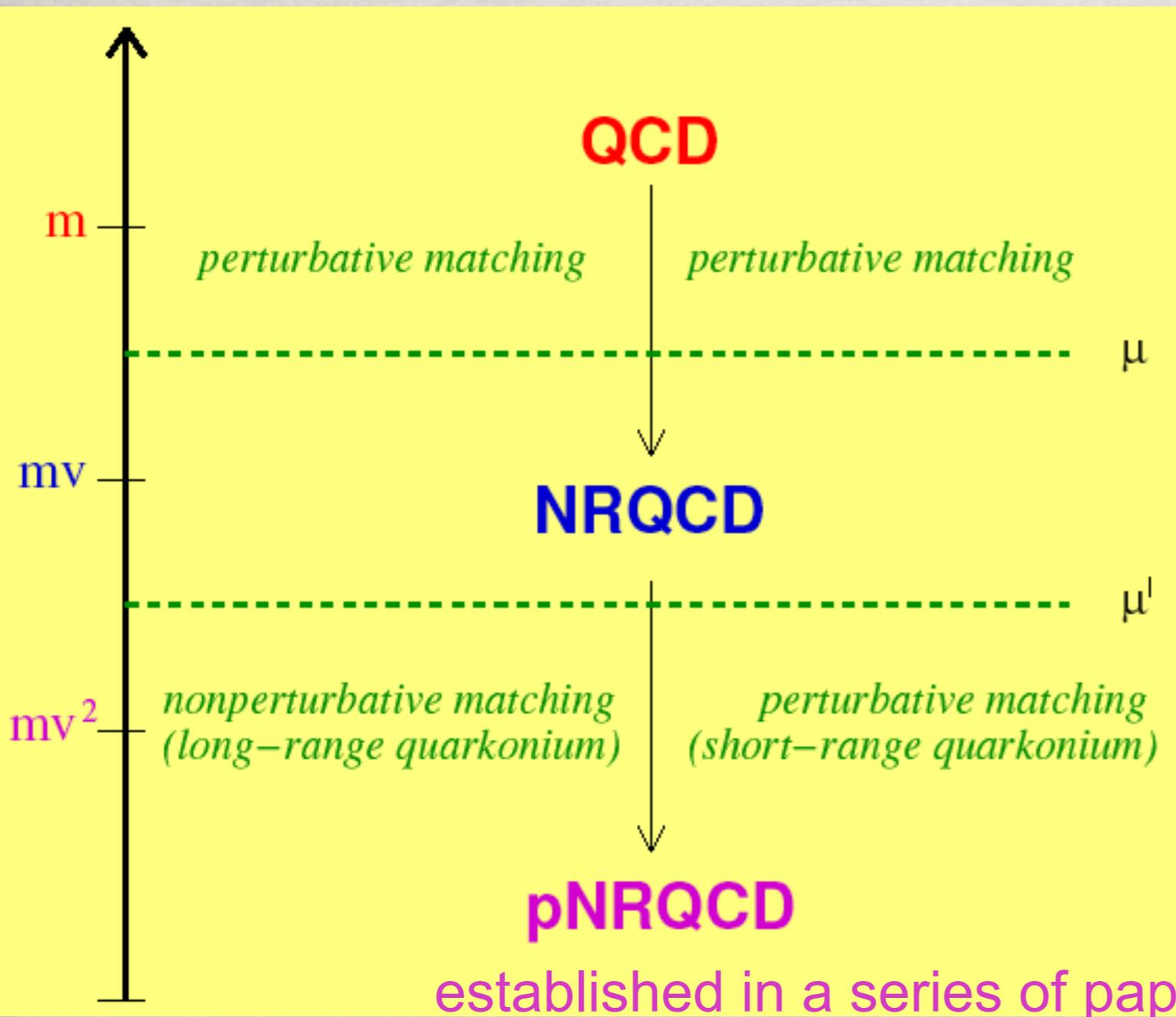
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Quarkonium with EFT



Caswell, Lepage 86,
Lepage, Thacker 88
Bodwin, Braaten, Lepage 95.....

established in a series of papers:

Pineda, Soto, N.B., Pineda, Soto, Vairo 97, 99

N.B. Vairo, Pineda, Soto 00--015

N.B., Pineda, Soto, Vairo Review of Modern Physics 77(2005)

Physics at the scale m : NRQCD
quarkonium production and decays

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quarkonium production and decays

STUDIES of QUARKONIUM
PRODUCTION IN VACUUM
and in a MEDIUM are
PROMINENT at the LARGE
HADRON COLLIDER

Quarkonium production

Bodwin Braaten Lepage 1995

NRQCD factorization formula for quarkonium production
valid for large p_T

$$\sigma(H) = \sum_n F_n \langle 0 | \mathcal{O}_n^H | 0 \rangle.$$

cross section

short distance coefficients

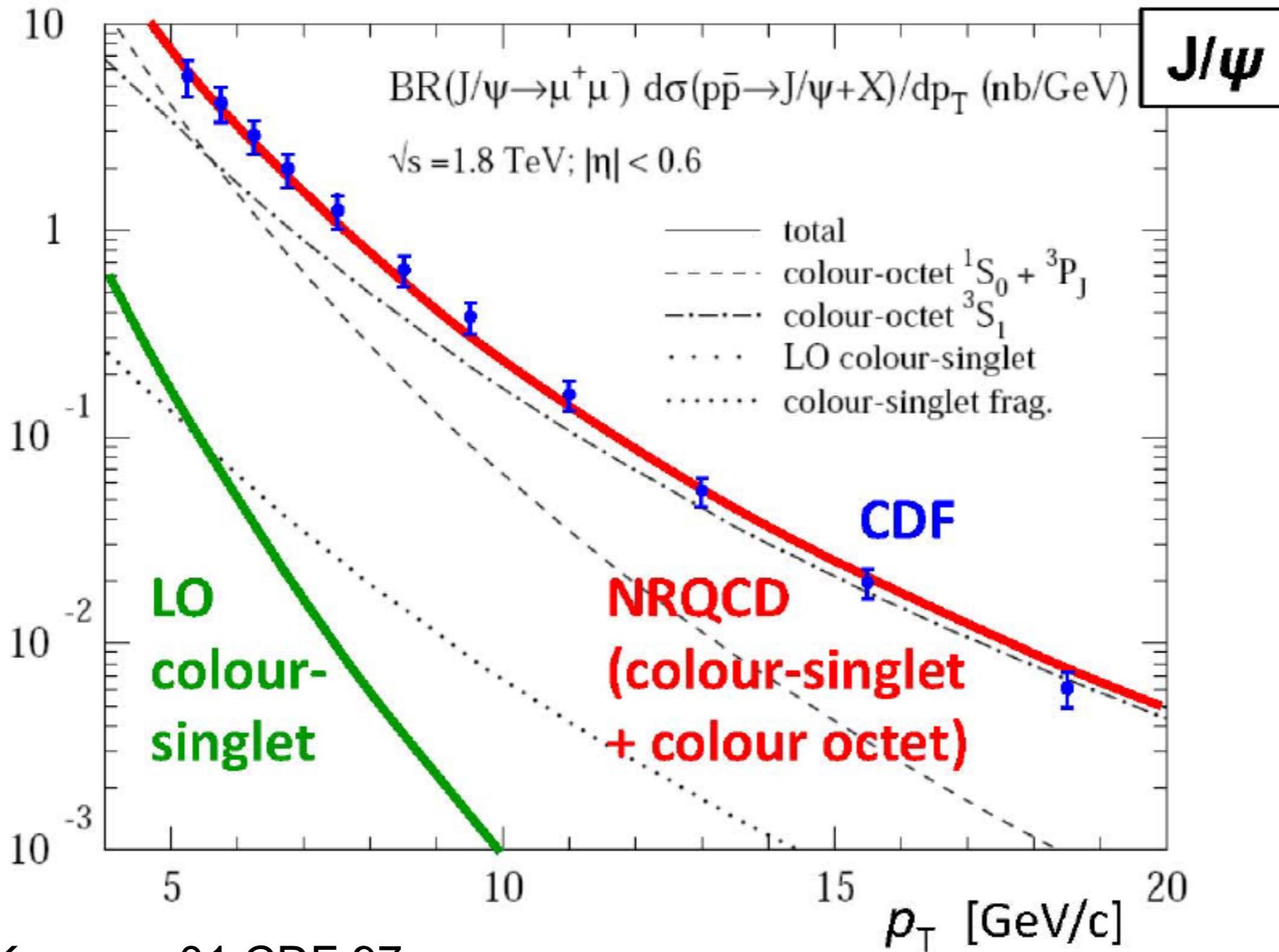
partonic hard scattering cross section
convoluted with parton distribution

long distance matrix elements
give the probability of a qqbar
pair with certain quantum
number to evolve into a final
quarkonium H

they are vacuum expectation
values of four fermion operators
and contain color singlet and
color octet contribution

Quarkonium production

page 1995



M. Kraemer 01 CDF 97

elements
of a qqbar
antum
o a final
+
expectation
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Explained the data at Fermilab on the cross section with the octet contribution (the singlet model failed)

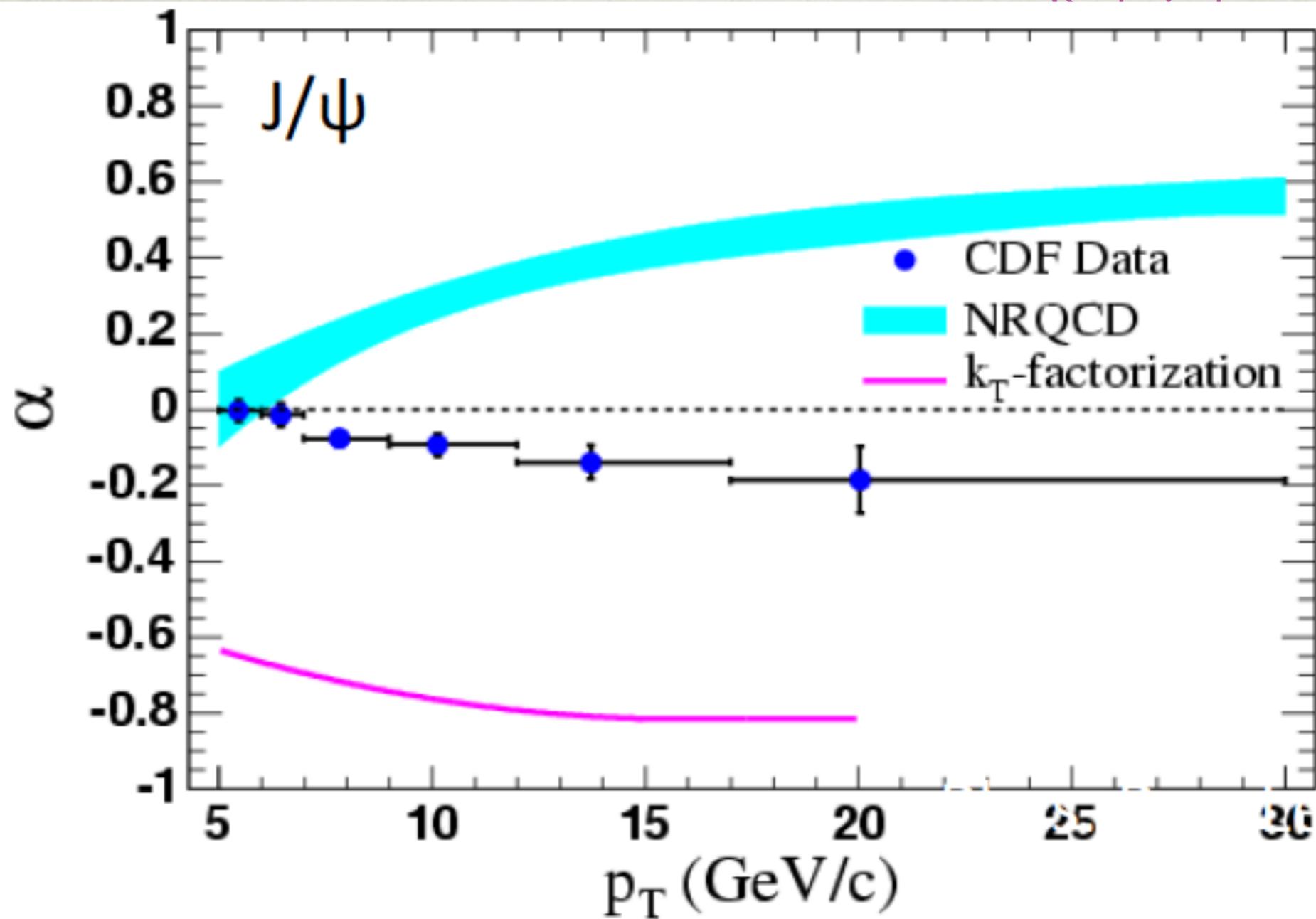
Quarkonium production

1995

NRQCD

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Difficulties in explaining quarkonium polarization at Fermilab

Quarkonium production

Terrific progress in production in the last few years

- Proof of NRQCD factorization at NNLO Qiu, Nayak, Sterman 05-08
- Calculation of the differential singlet cross section at NLO and NNLO* Gong, Wang 08 Artoisenet, Campbell, Lansberg, Maltoni, Tramontano 07
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a coherent picture in NRQCD for quarkonium production at Tevatron, Rhic, Hera is emerging and is being scrutinized at LHC

many more data are produced by LHC : polarizations (J/psi, psi(2s), Y(nS)), ratio of chi states, double quarkonium production, production of new states

NRQCD on the lattice for spectra calculations:
many advances in the calculation of the
matching coefficients in the lattice regularization
and in considering higher order corrections in
 v^2 : applications to bottomonium, hyperfine
separation..... still a challenge the excited states

NRQCD for exclusive decays, implement collinear
degrees of freedom with SCET

Physics at the scale mv and
 mv^2 : pNRQCD
bound state formation

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 mv^2 : pNRQCD
bound state formation

pNRQCD is today the theory used to address
quarkonium bound states properties

pNRQCD and quarkonium Several cases for the physics at hand

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The EFT has been constructed (away from the strong decay threshold)

- *Work at calculating higher order perturbative corrections in v and α_s
- *Resumming the log
- *Calculating/extracting nonperturbatively the low energy quantities
- *Extending the theory (electromagnetic effect, 3 bodies)

pNRQCD and quarkonium Several cases for the physics at hand

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The issue here is precision physics and the study of confinement

- Precise and systematic high order calculations allow the extraction of precise determinations of standard model parameters like the quark masses and α_s
- The EFT has allowed to systematically factorize and to study the low energy nonperturbative contributions

pNRQCD and quarkonium Several cases for the physics at hand

The EFT is constructed (Finite T, small g)

Laine et al, 2007, Escobedo, Soto
2007 N. B., A. Vairo et al. 2008-2015

*Results on the static potential hint at a new physical picture of dissociation

*Mass and width of quarkonium at $m \alpha^5 (Y(1S) \text{ bbar at LHC})$

N. B. Escobedo,
Ghiglieri, Vairo Soto,

*Polyakov loop calculation

N. B., Ghiglieri, Petreczky, Vairo 2010-2015

2010-2014

The eft allows us to discover new, unexpected and important facts:

- The potential is neither the color singlet free energy nor the internal energy
- The quarkonium dissociation is a consequence of the appearance of a thermal decay width rather than being due to the color screening of the real part of the potential

We have now a coherent and systematical setup to calculate masses and width of quarkonium at finite T for small coupling

We have provided inspiration for other approaches: lattice, strings etc that now find imaginary parts in the finite T potential

pNRQCD and quarkonium Several cases for the physics at hand

The EFT has not yet been constructed (Exotics close to threshold)

*Degrees of freedom still to be identified

only in particular cases (X(3872)) a universal treatment is possible

E. Braaten et al

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Important to understand the X, Y, Z puzzles of the dozens of unexpected states showing up at the LHC and other collider experiments

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Important to understand the X, Y, Z puzzles of the dozens of unexpected states showing up at the LHC and other collider experiments

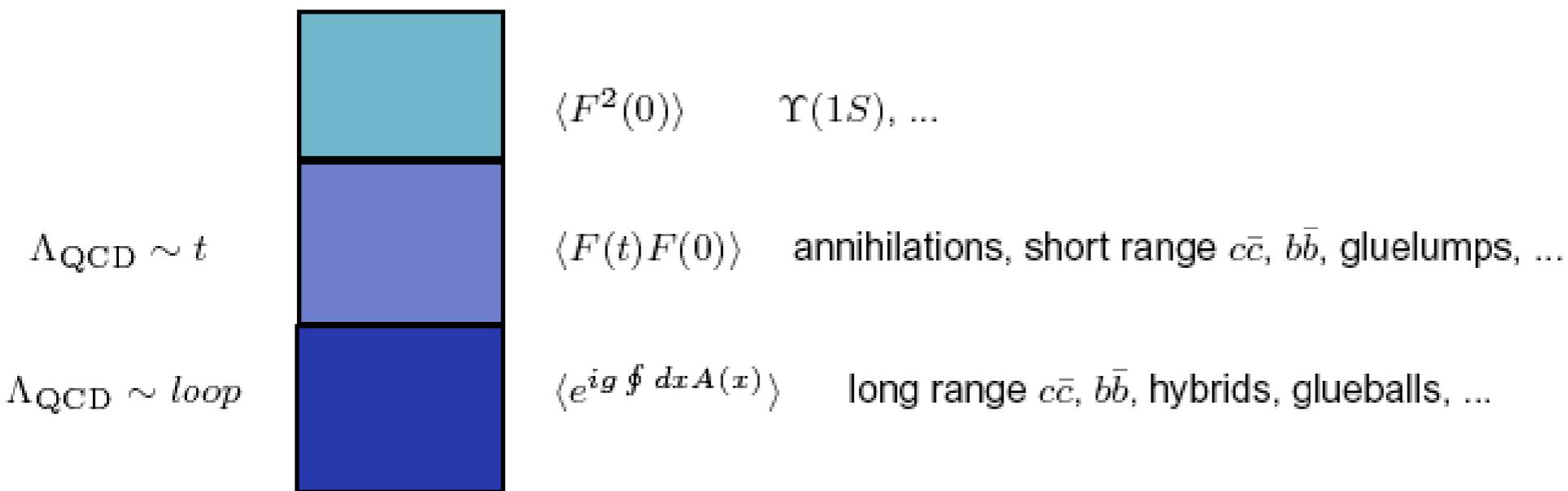
Near threshold heavy-light mesons have to be included and many additional degrees of freedom considered

No systematic treatment is available; lattice calculations are also challenging and in the infancy state in this case

pNRQCD treatment available at the moment for the exotics states made by excited glue: HYBRIDS

Low energy (nonperturbative) factorized effects depend on the size of the physical system

The EFT factorizes the low energy nonperturbative part.
Depending on the physical system:



The more extended the physical object, the more we probe the non-perturbative vacuum.

$$r \ll \frac{1}{\Lambda_{QCD}}$$

lowest

quarkonia states

excited
quarkonia states

$$r \sim \frac{1}{\Lambda_{QCD}}$$

quarkonia
and exotics
close and
above
threshold

$$r \ll \frac{1}{\Lambda_{QCD}}$$

T

quarkonia
in a hot medium

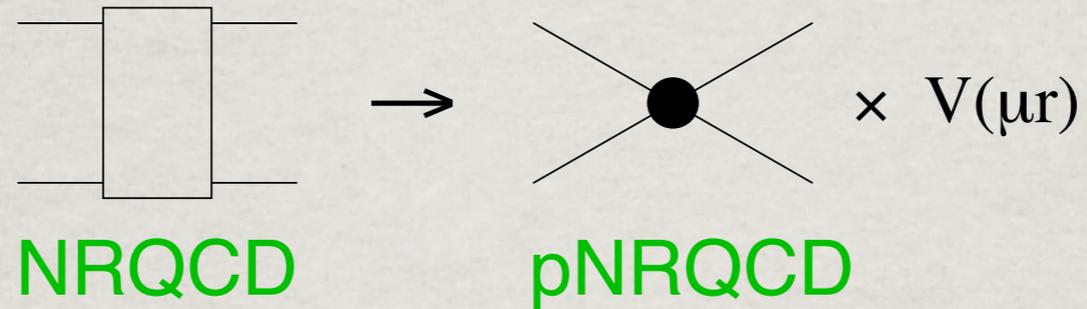
$$r \sim \frac{1}{\Lambda_{QCD}}$$

Quarkonium systems with
small radius $r \ll \Lambda_{\text{QCD}}^{-1}$

pNRQCD for quarkonia with small radius

$$r \ll \Lambda_{\text{QCD}}^{-1}$$

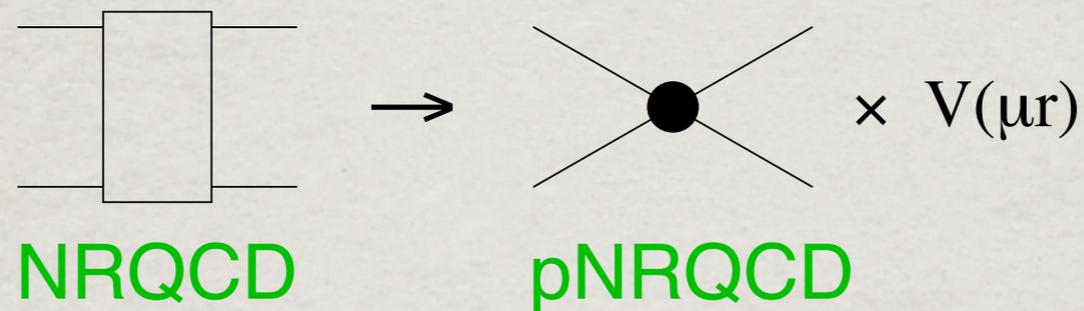
Degrees of freedom that **scale** like mv are integrated out:



pNRQCD for quarkonia with small radius

$$r \ll \Lambda_{\text{QCD}}^{-1}$$

Degrees of freedom that **scale** like mv are integrated out:



- If $mv \gg \Lambda_{\text{QCD}}$, the matching is perturbative

- Degrees of freedom: quarks and gluons

$Q-\bar{Q}$ states, with energy $\sim \Lambda_{\text{QCD}}$, mv^2 and momentum $\lesssim mv$

\Rightarrow (i) singlet S (ii) octet O

Gluons with energy and momentum $\sim \Lambda_{\text{QCD}}$, mv^2

- Definite power counting: $r \sim \frac{1}{mv}$ and $t, R \sim \frac{1}{mv^2}, \frac{1}{\Lambda_{\text{QCD}}}$

The gauge fields are multipole expanded:

$$A(R, r, t) = A(R, t) + \mathbf{r} \cdot \nabla A(R, t) + \dots$$

Non-analytic behaviour in $r \rightarrow$ matching coefficients V

weak pNRQCD

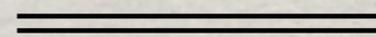
$$r \ll \Lambda_{\text{QCD}}^{-1}$$

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F^{\mu\nu a} + \text{Tr} \left\{ S^\dagger \left(i\partial_0 - \frac{\mathbf{p}^2}{m} - V_s \right) S \right. \\ \left. + O^\dagger \left(iD_0 - \frac{\mathbf{p}^2}{m} - V_o \right) O \right\}$$

LO in r

S singlet field

O octet field



singlet propagator

octet propagator

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LO in r

$$+ V_A \text{Tr} \left\{ \mathbf{O}^\dagger \mathbf{r} \cdot g\mathbf{E} \mathbf{S} + \mathbf{S}^\dagger \mathbf{r} \cdot g\mathbf{E} \mathbf{O} \right\} \\ + \frac{V_B}{2} \text{Tr} \left\{ \mathbf{O}^\dagger \mathbf{r} \cdot g\mathbf{E} \mathbf{O} + \mathbf{O}^\dagger \mathbf{O} \mathbf{r} \cdot g\mathbf{E} \right\} \\ + \dots$$

NLO in r

S singlet field

O octet field



singlet propagator

octet propagator

weak pNRQCD

$$r \ll \Lambda_{\text{QCD}}^{-1}$$

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F^{\mu\nu a} + \text{Tr} \left\{ \mathbf{S}^\dagger \left(i\partial_0 - \frac{\mathbf{p}^2}{m} - V_s \right) \mathbf{S} \right. \\ \left. + \mathbf{O}^\dagger \left(iD_0 - \frac{\mathbf{p}^2}{m} - V_o \right) \mathbf{O} \right\}$$

Singlet static potential

LO in r

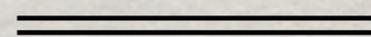
Octet static potential

$$+ V_A \text{Tr} \left\{ \mathbf{O}^\dagger \mathbf{r} \cdot g\mathbf{E} \mathbf{S} + \mathbf{S}^\dagger \mathbf{r} \cdot g\mathbf{E} \mathbf{O} \right\} \\ + \frac{V_B}{2} \text{Tr} \left\{ \mathbf{O}^\dagger \mathbf{r} \cdot g\mathbf{E} \mathbf{O} + \mathbf{O}^\dagger \mathbf{O} \mathbf{r} \cdot g\mathbf{E} \right\} \\ + \dots$$

NLO in r

S singlet field

O octet field



singlet propagator

octet propagator

pNRQCD

- ✱ pNRQCD provides a QM description from field theory: the Schroedinger equation and the potentials appear once all scales above the binding energy have been integrated out
- ✱ The EFT accounts for non-potential terms as well. They provide loop corrections to the leading potential picture. Retardation effects are typically related to the nonperturbative physics
- ✱ The Quantum Mechanical divergences are cancelled by the NRQCD matching coefficients.
- ✱ Poincare' invariance is intact and is realized via exact relations among the matching coefficients (potentials)

QCD singlet static potential and singlet static energy

$$\begin{array}{c} \boxed{e^{ig \oint dz^\mu A_\mu}} \\ \text{NRQCD} \end{array} = \begin{array}{c} \text{---} + \text{---} \oplus \text{---} \oplus \text{---} + \dots \\ \text{pNRQCD} \end{array}$$

The diagram shows the expansion of the NRQCD static potential into pNRQCD terms. On the left, a rectangular loop with arrows on all four sides is labeled $e^{ig \oint dz^\mu A_\mu}$ and NRQCD. This is set equal to a series of terms. The first term is a single horizontal line. The second term is a horizontal line with a gluon loop (represented by a wavy line) connecting two vertices on the line, each marked with a cross in a circle. This is followed by an ellipsis.

QCD singlet static potential and singlet static energy

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 \boxed{e^{ig \oint dz^\mu A_\mu}} \\
 \text{NRQCD}
 \end{array}
 =
 \begin{array}{c}
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 \text{pNRQCD}
 \end{array}
 + \dots$$

potential

$$\lim_{T \rightarrow \infty} \frac{i}{T} \ln \langle \boxed{\phantom{e^{ig \oint dz^\mu A_\mu}}} \rangle = V_s(r, \mu) - i \frac{g^2}{N_c} V_A^2 \int_0^\infty dt e^{-it(V_o - V_s)} \langle \text{Tr}(r \cdot E(t) r \cdot E(0)) \rangle(\mu) + \dots$$

static energy

ultrasoft contribution
contributes from 3 loops

QCD singlet static potential and singlet static energy

The diagram shows the expansion of the NRQCD Wilson loop into pNRQCD terms. On the left, a rectangular loop with arrows on all four sides is labeled 'NRQCD' and contains the expression $e^{ig \oint dz^\mu A_\mu}$. This is set equal to a series of terms. The first term is a simple horizontal line. The second term is a horizontal line with a gluon loop (represented by a wavy line) attached to the top, with a cross in a circle at each vertex. This is labeled 'pNRQCD'. The series continues with an ellipsis '...'. The entire diagram is on a yellow background.

potential

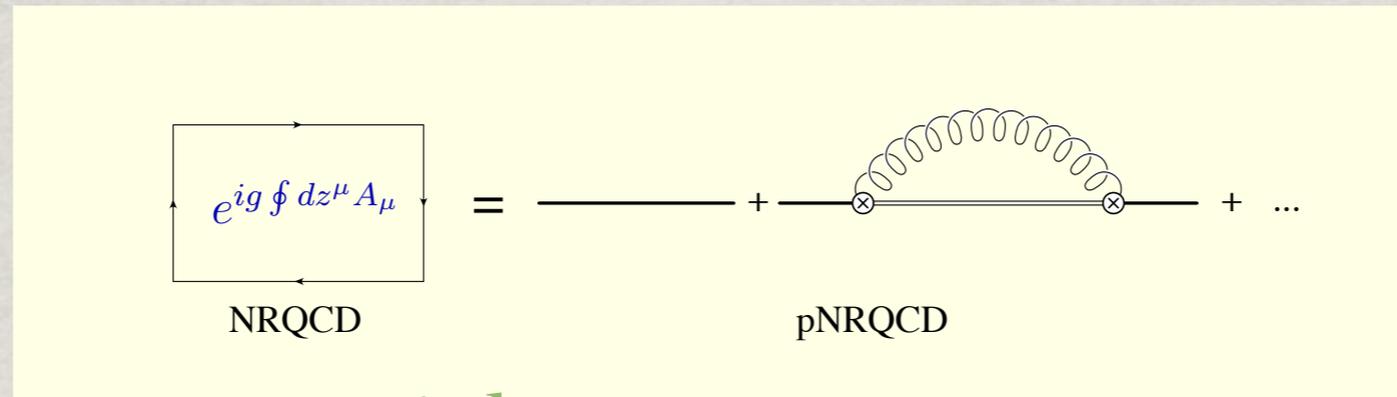
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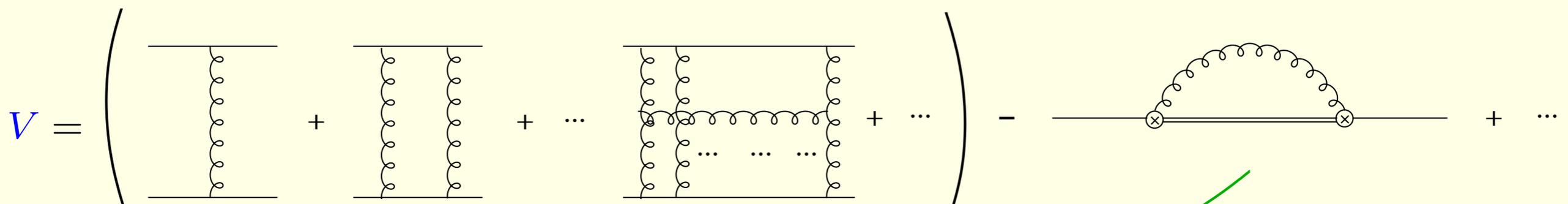
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Quarkonium singlet static potential at N⁴LO

$$\begin{aligned} V_s(r, \mu) = & -C_F \frac{\alpha_s(1/r)}{r} \left[1 + a_1 \frac{\alpha_s(1/r)}{4\pi} + a_2 \left(\frac{\alpha_s(1/r)}{4\pi} \right)^2 \right. \\ & + \left(\frac{16\pi^2}{3} C_A^3 \ln r\mu + a_3 \right) \left(\frac{\alpha_s(1/r)}{4\pi} \right)^3 \\ & \left. + \left(a_4^{L2} \ln^2 r\mu + \left(a_4^L + \frac{16}{9} \pi^2 C_A^3 \beta_0 (-5 + 6 \ln 2) \right) \ln r\mu + a_4 \right) \left(\frac{\alpha_s(1/r)}{4\pi} \right)^4 \right] \end{aligned}$$

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a_1 Billoire 80

a_2 Schroeder 99, Peter 97

coeff $\ln r\mu$ N.B. Pineda, Soto, Vairo 99

a_4^{L2}, a_4^L N.B., Garcia, Soto, Vairo 06

a_3 Anzai, Kiyo, Sumino 09, Smirnov, Smirnov, Steinhauser 09

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a_4^{L2}, a_4^L N.B., Garcia, Soto, [Vainshtein 00](#) **4LOOPS REDUCES TO 2LOOPS IN THE EFT**

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Two problems:

- 1) Bad convergence of the series due to large beta₀ terms
- 2) Large logs

Quarkonium singlet static potential at N⁴LO

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for long it was believed that such series was not convergent

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 \end{aligned}$$

Two problems:

for long it was believed that such series was not convergent
 problem for any phenomenological application

1) Bad convergence of the series due to large beta₀ terms

2) Large logs

The eft cures both:

1) Renormalon subtracted scheme

Beneke 98, Hoang, Lee 99, Pineda 01, N.B. Pineda

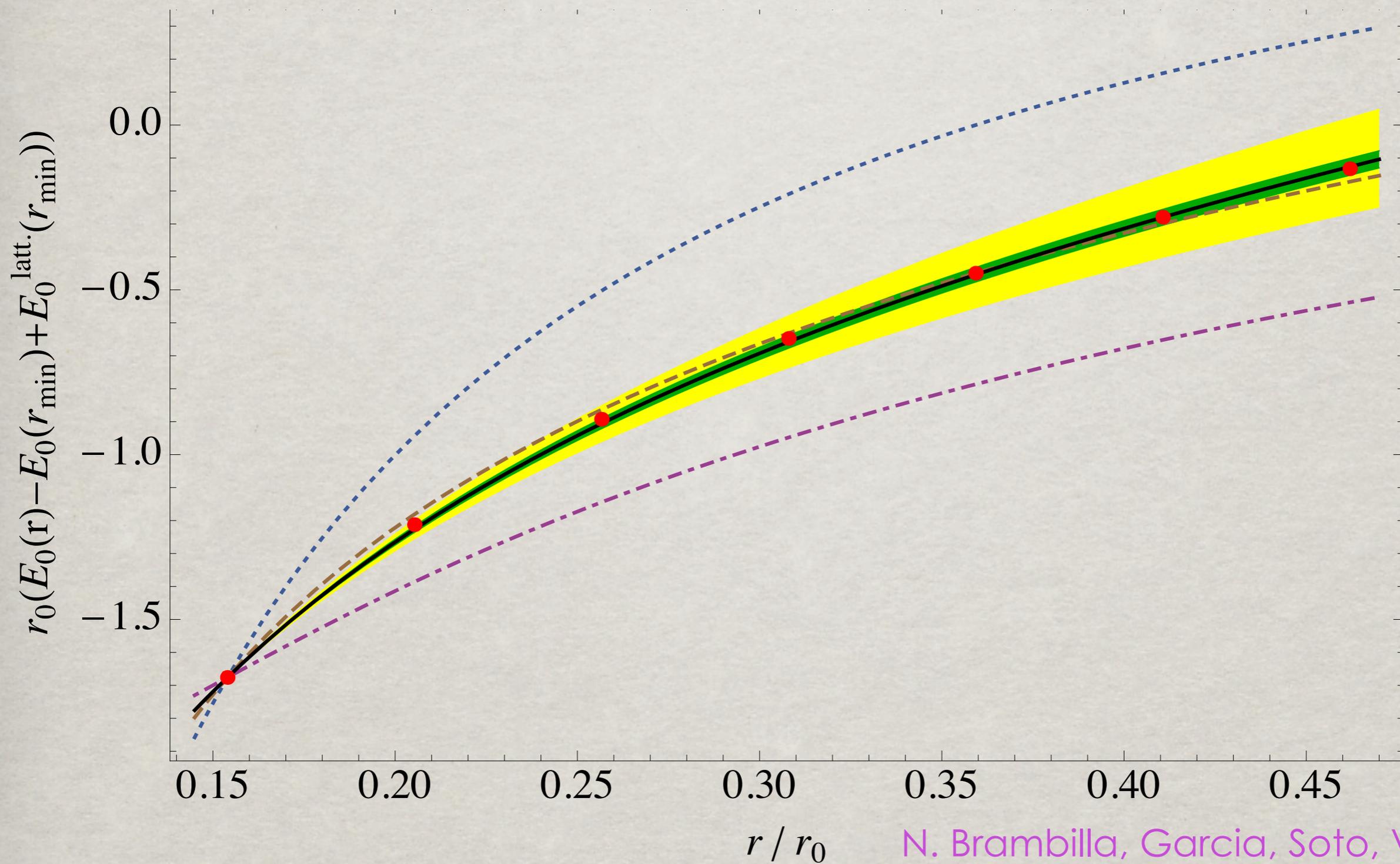
2) Renormalization group summation of the logs

Soto, Vairo 09

up to N³LL $(\alpha_s^{4+n} \ln^n \alpha_s)$ N. B Garcia, Soto Vairo 2007, 2009, Pineda, Soto

Quarkonium singlet static energy at N^3L in comparison with lattice data (red points

Necco Sommer 2002)

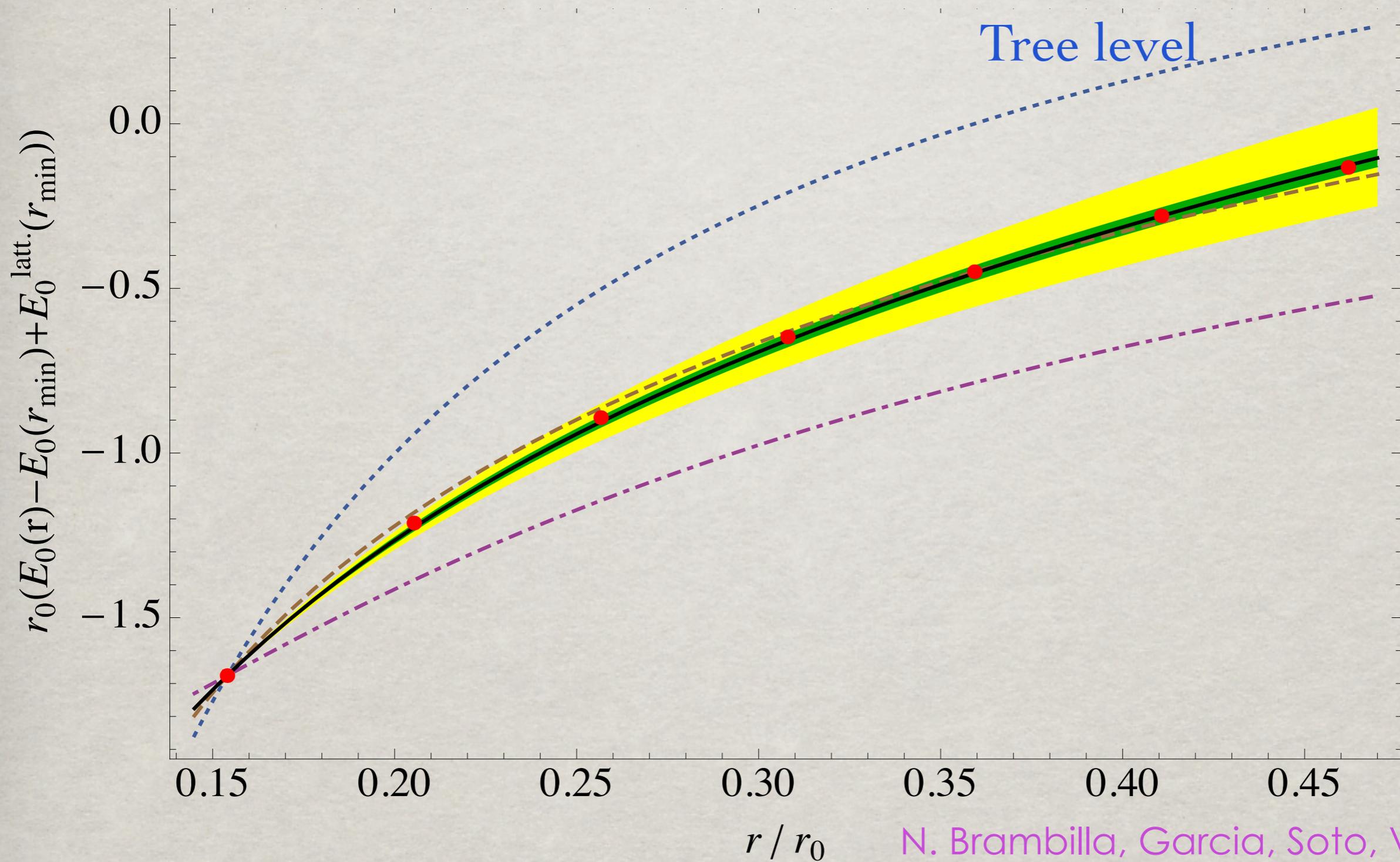


Yellow band : uncertainty in α_s ($r_0 \cdot \Lambda_{\text{QCD}}(\overline{\text{MS}})$)

Green band: uncertainty in higher order terms

Quarkonium singlet static energy at N³L in comparison with lattice data (red points

Necco Sommer 2002)



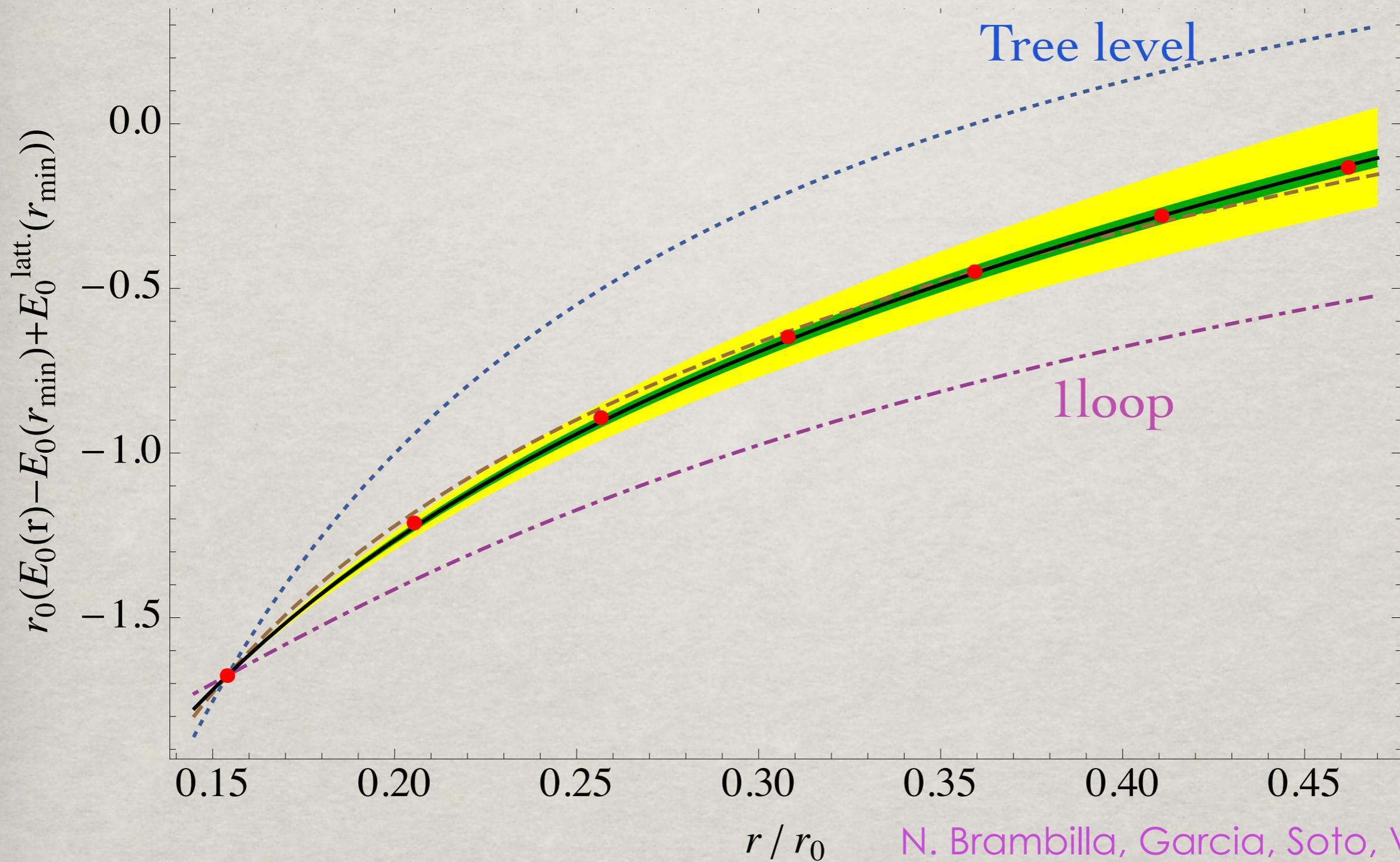
N. Brambilla, Garcia, Soto, Vairo 010

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Quarkonium singlet static energy at N³L in comparison with lattice data (red points

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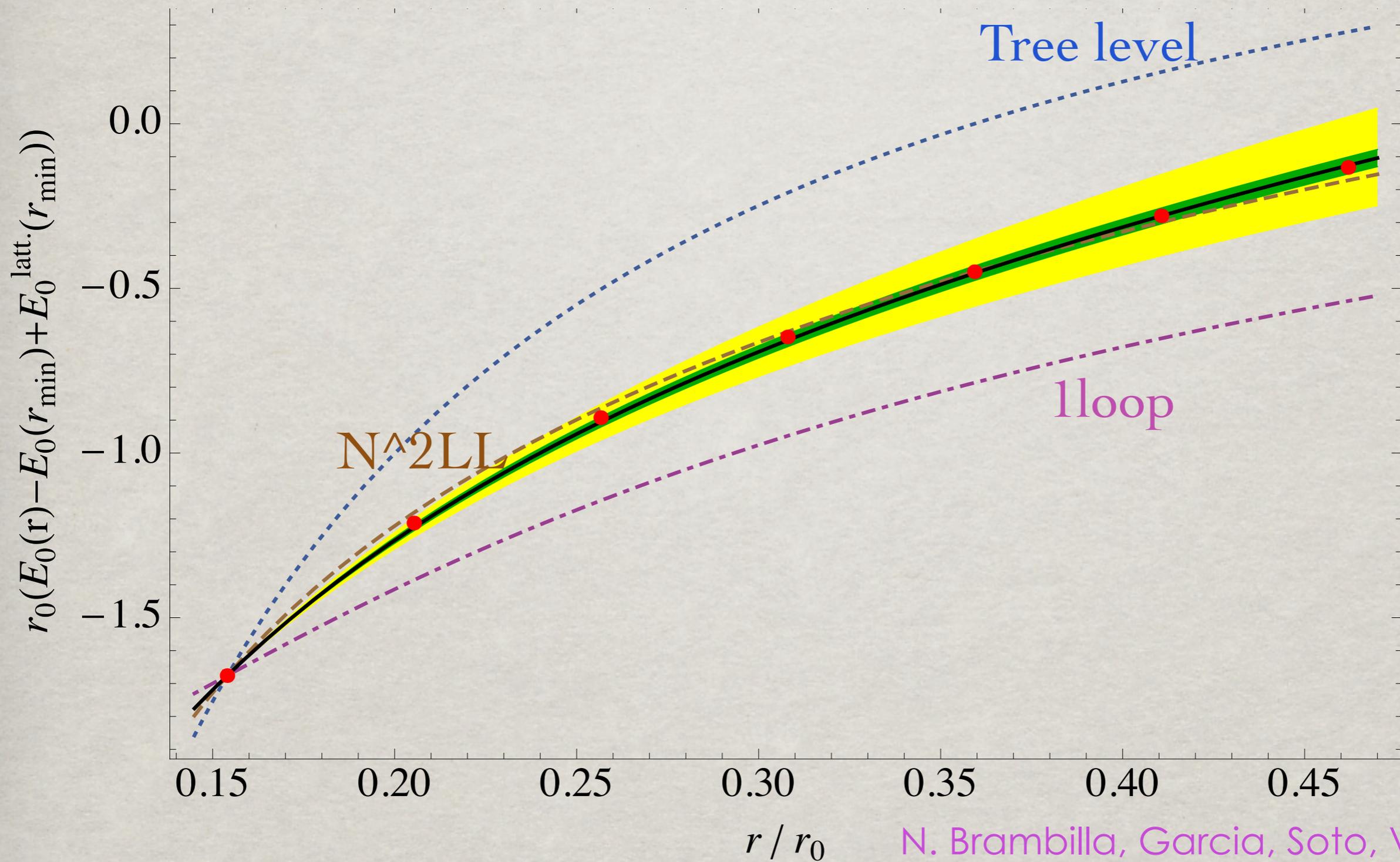
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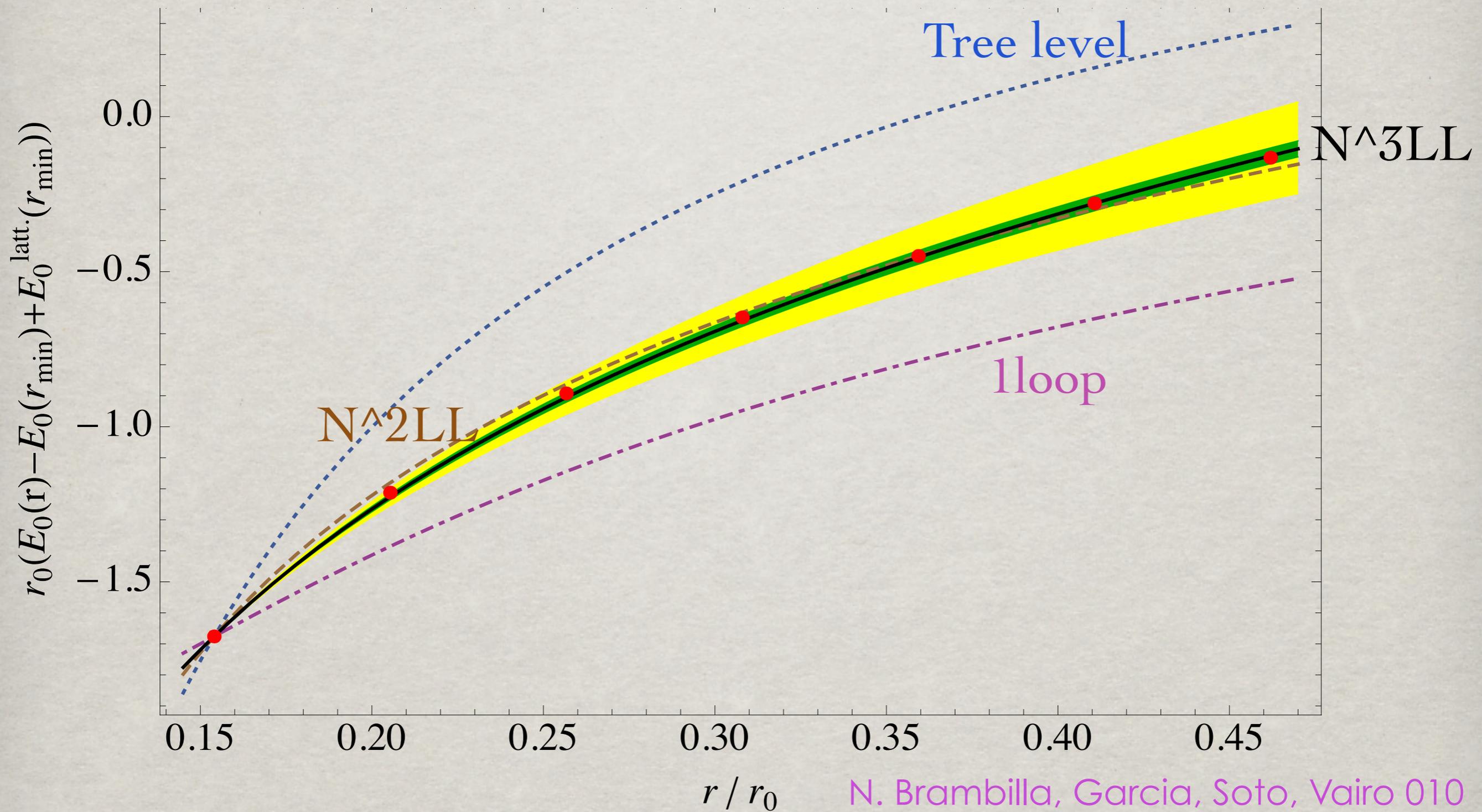
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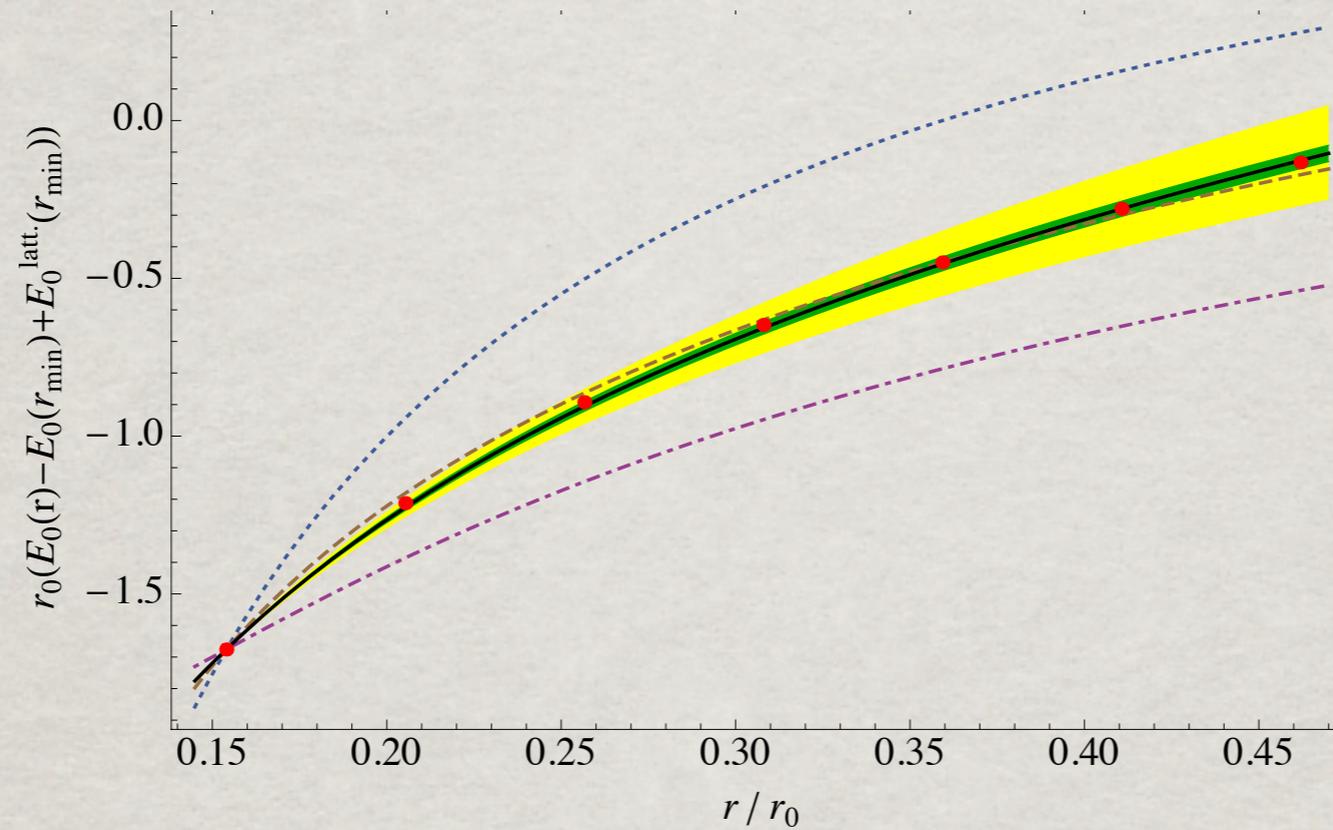
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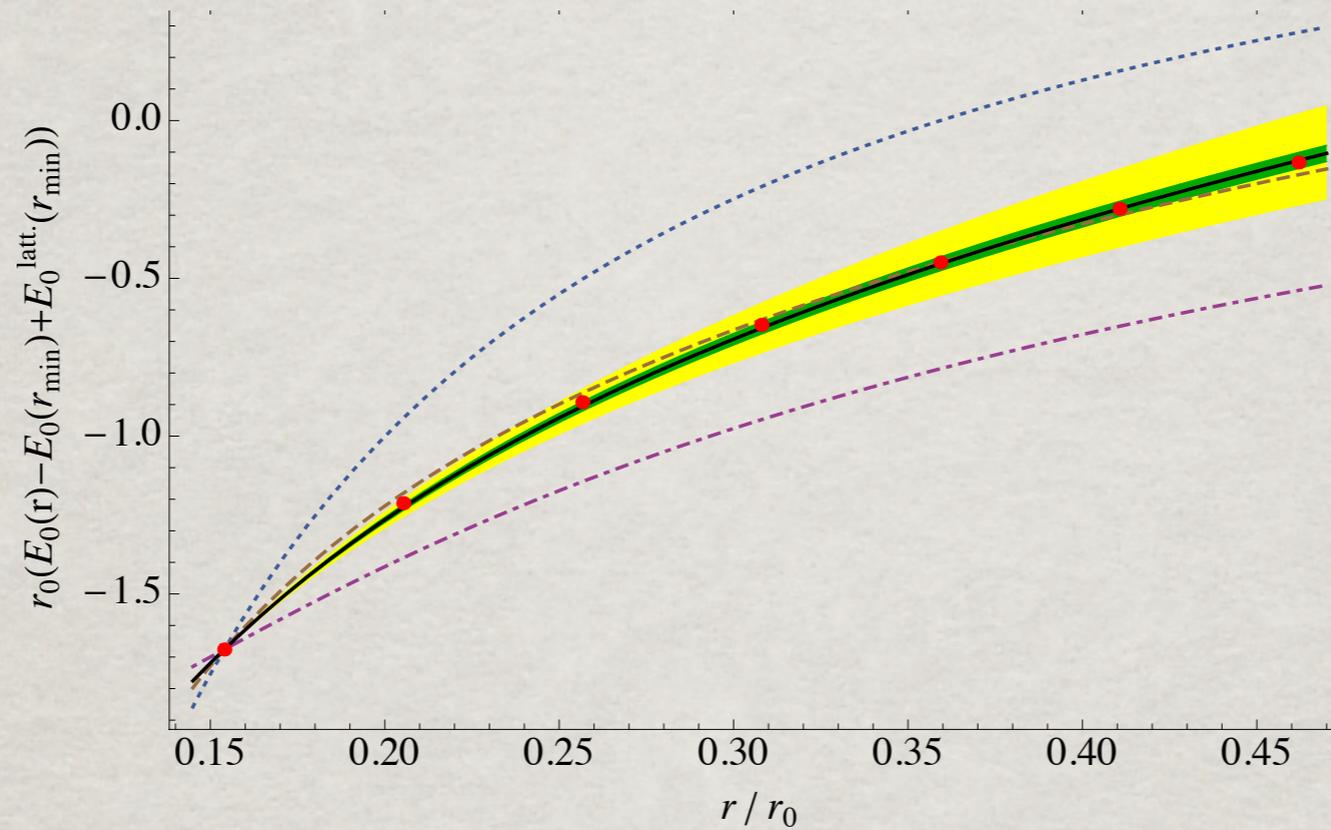
Quarkonium singlet static energy at N³L1 in comparison with lattice data (red points

Necco Sommer 2002)



Quarkonium singlet static energy at N³L in comparison with lattice data (red points

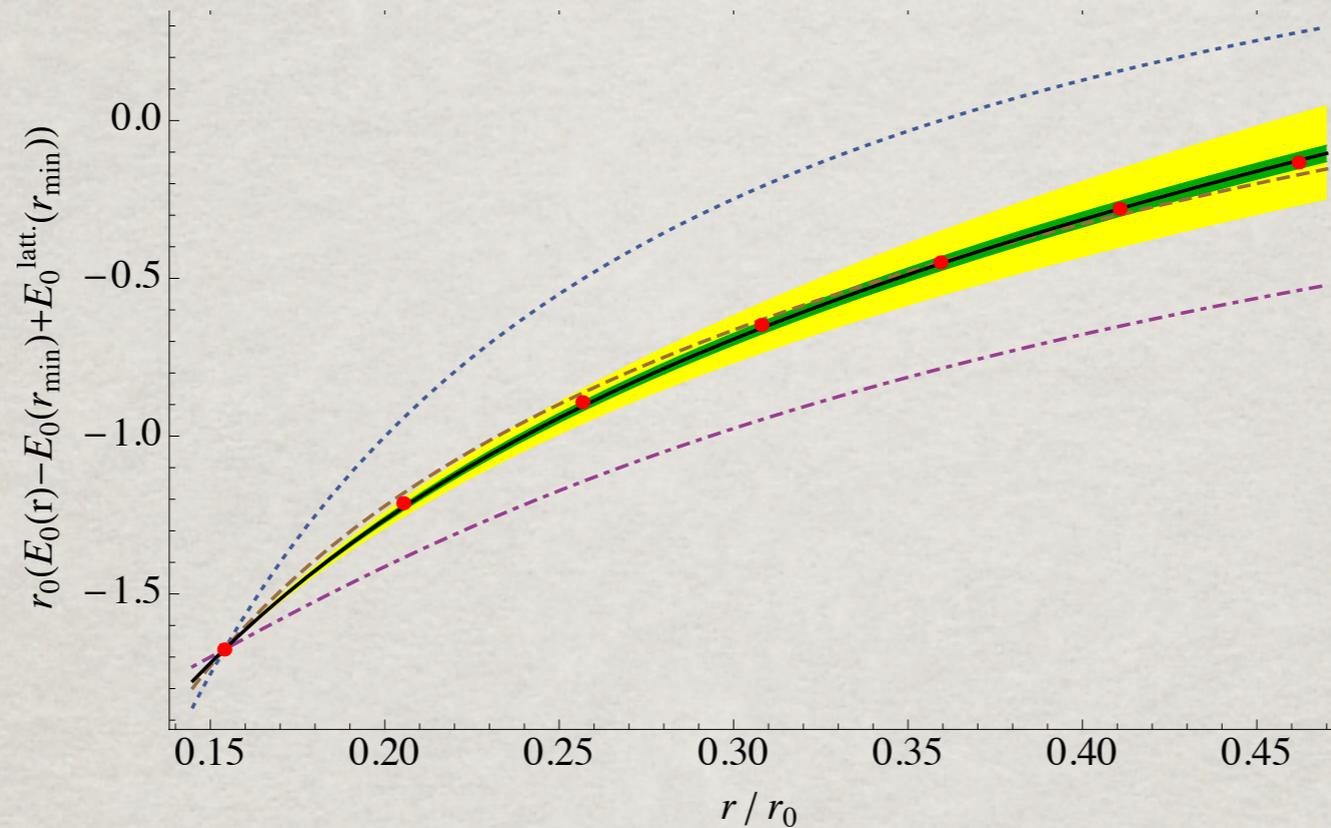
Necco Sommer 2002)



- Very good convergence of the QCD bound state perturbative series

Quarkonium singlet static energy at N³LO in comparison with lattice data (red points

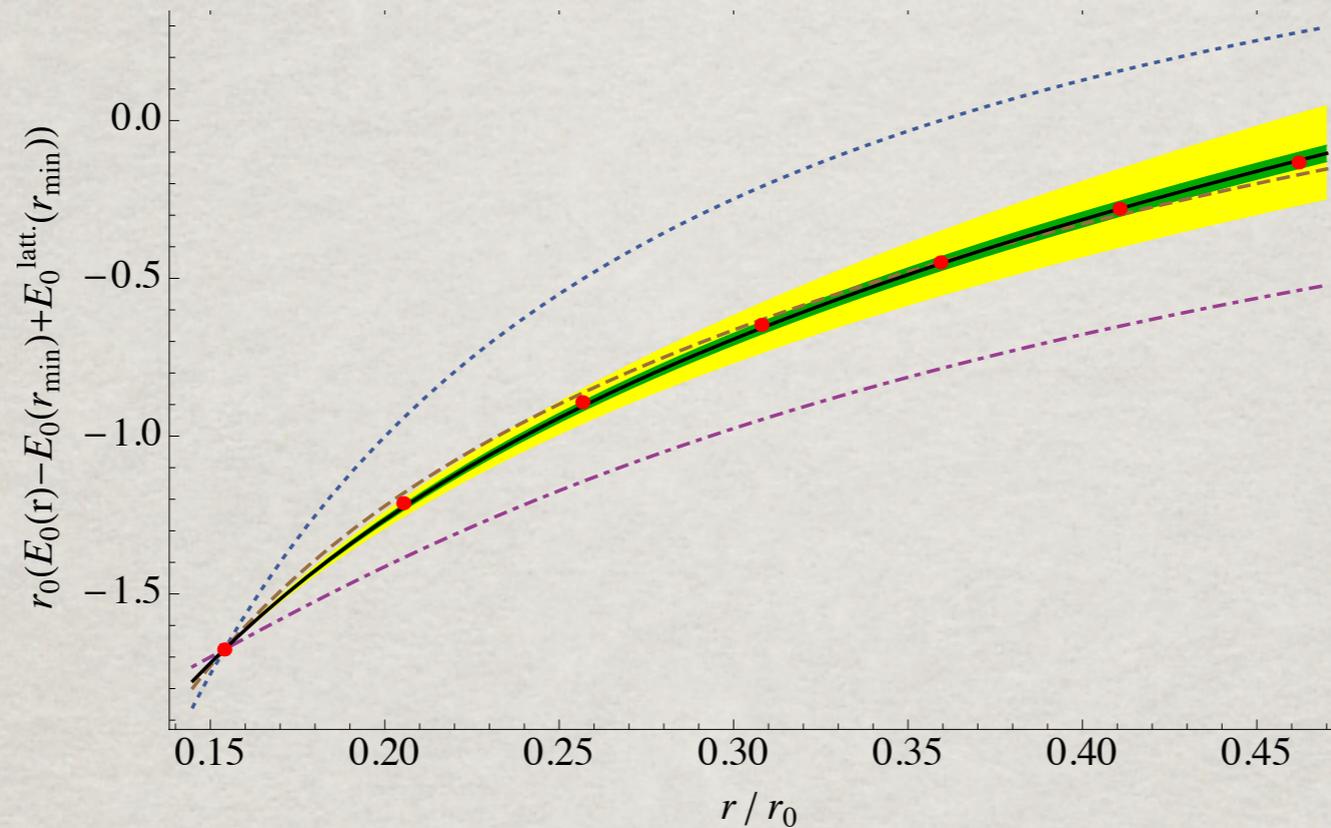
Necco Sommer 2002)



- Very good convergence of the QCD bound state perturbative series
- The lattice data are perfectly described from perturbation theory up to more than 0.2 fm

Quarkonium singlet static energy at N³L1 in comparison with lattice data (red points

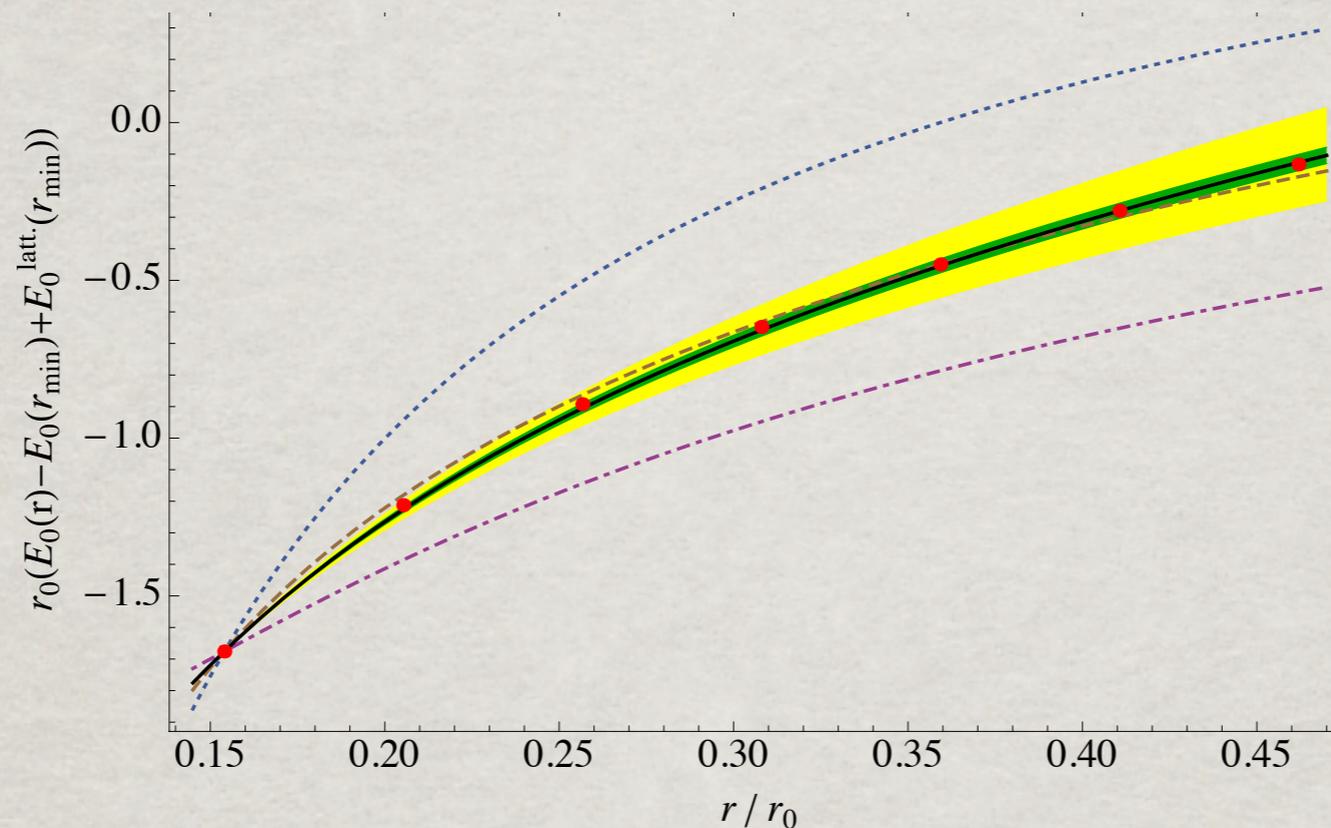
Necco Sommer 2002)



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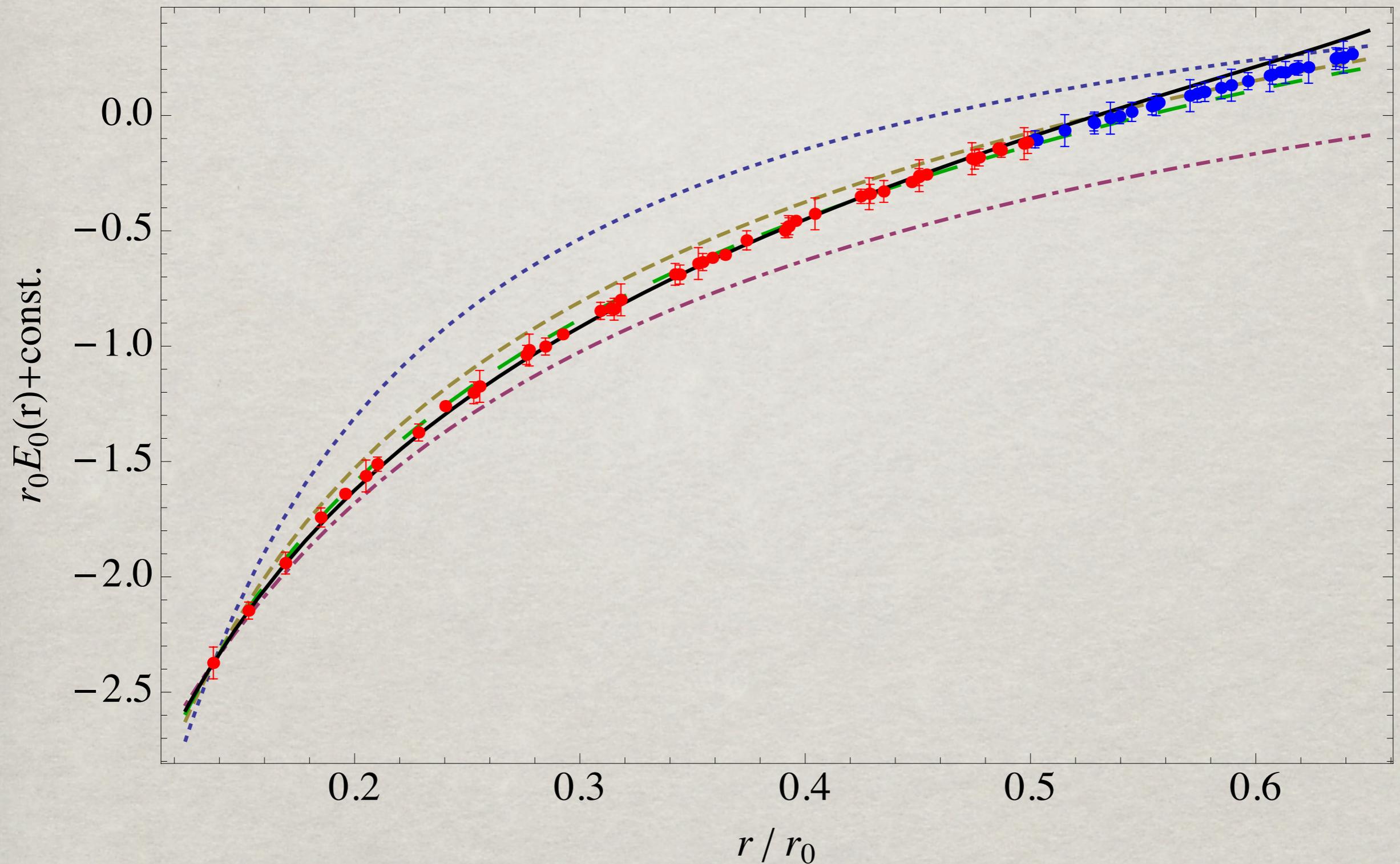
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N. Brambilla, Garcia, Soto, Vairo 010)

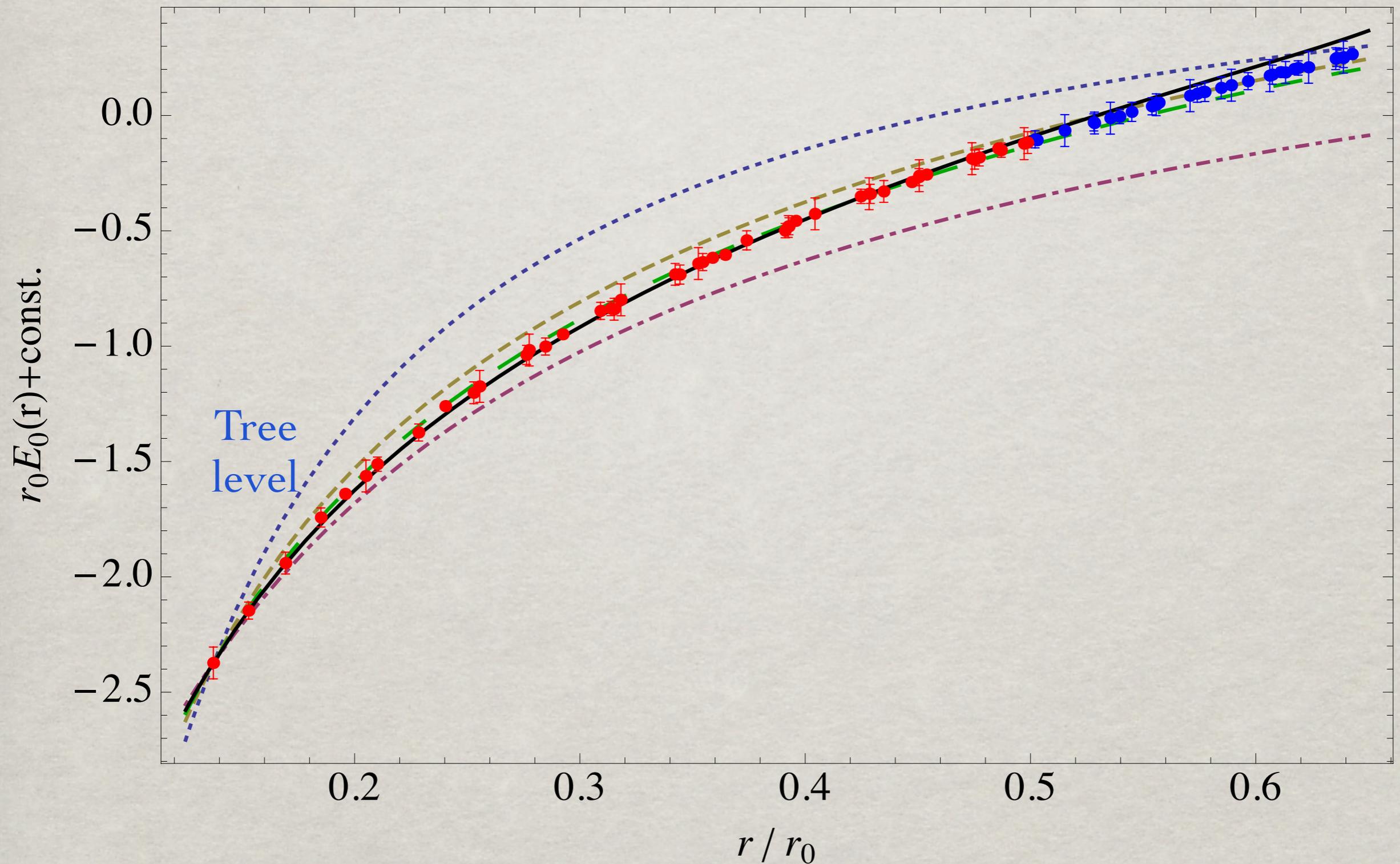
QQbar singlet static energy at N³L in comparison with unquenched (n_f=2+1) lattice data (red points, blue points)

Bazanov, N. B., Garcia, Petreczky, Soto, Vairo , 2012, 2014



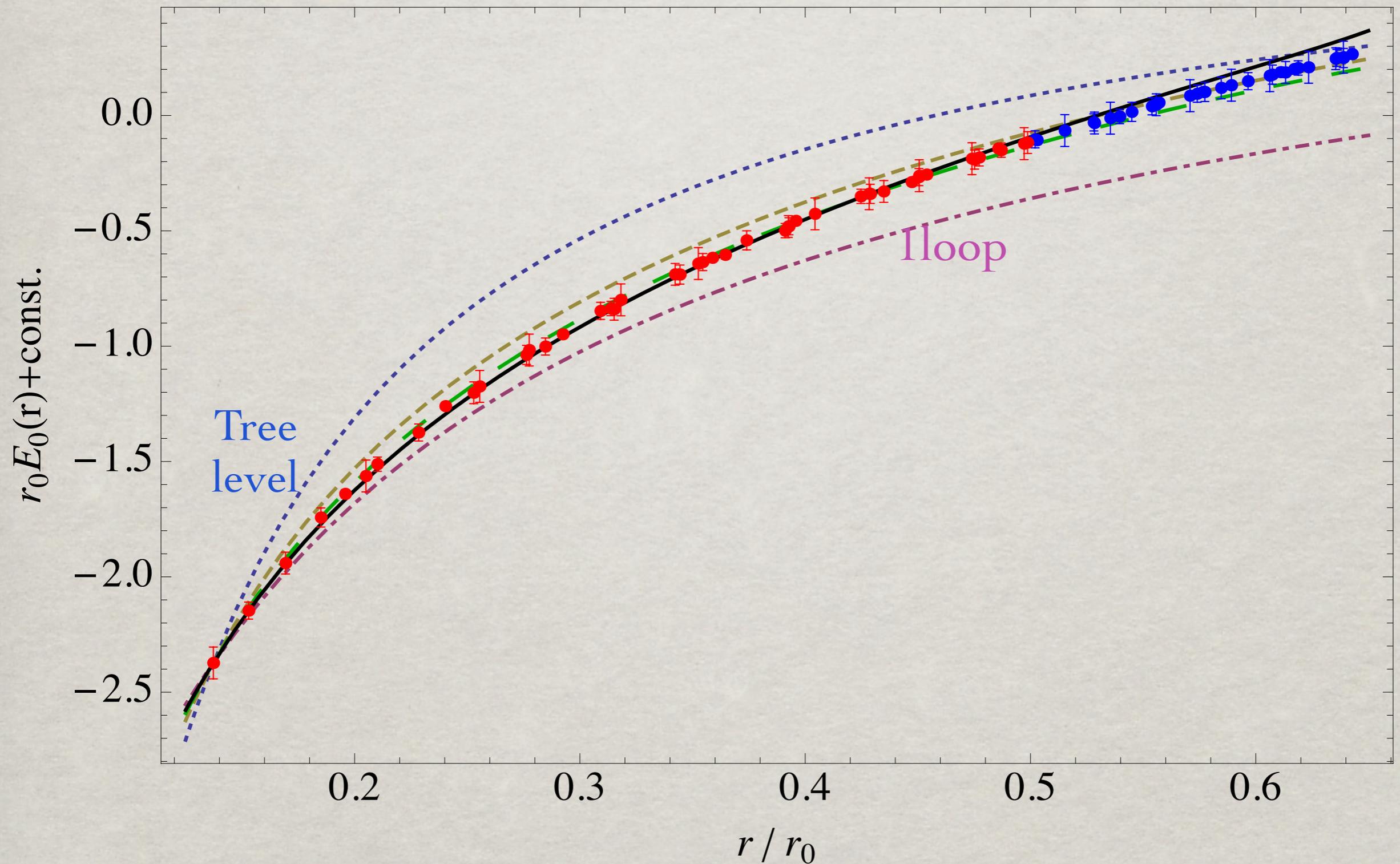
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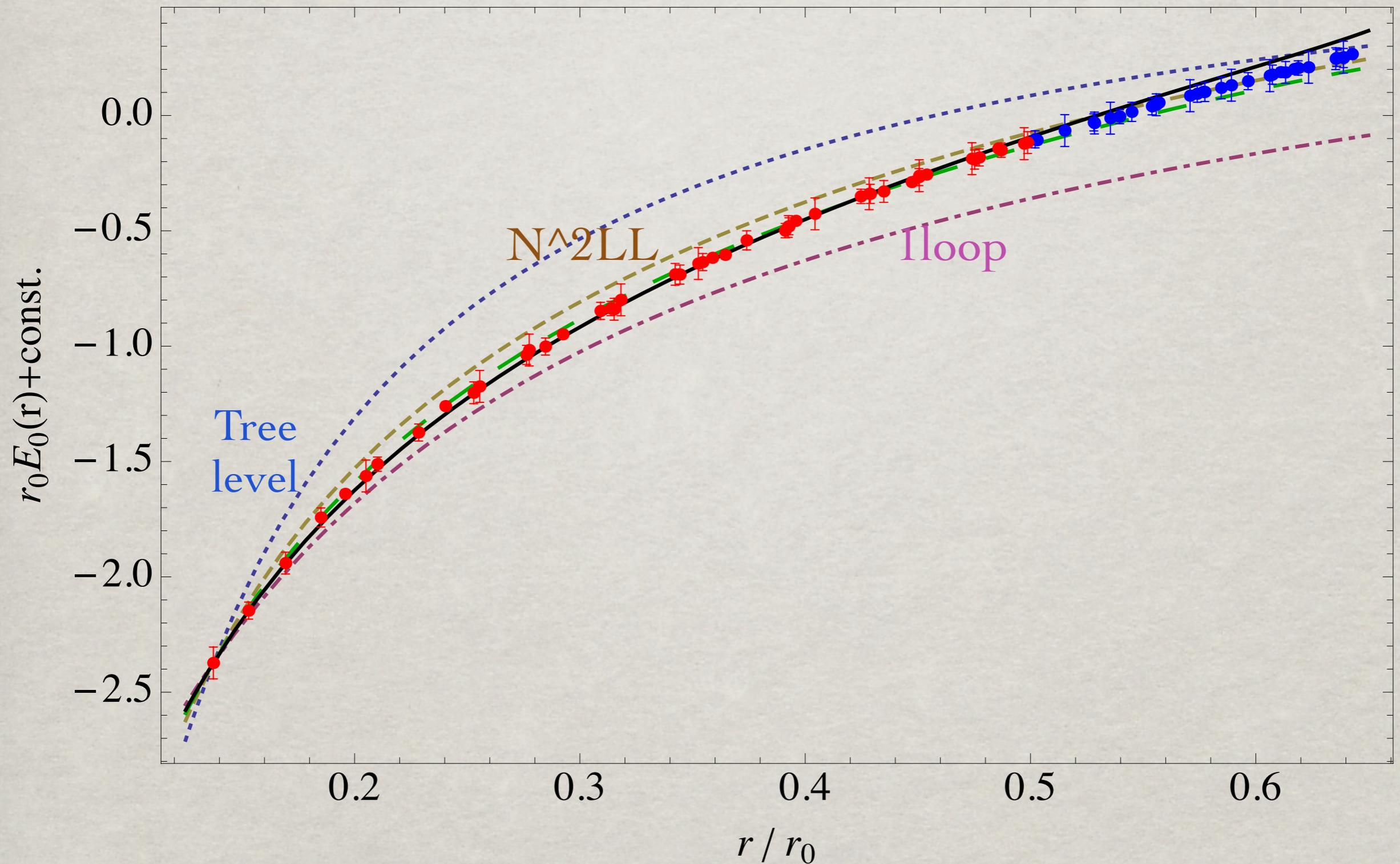
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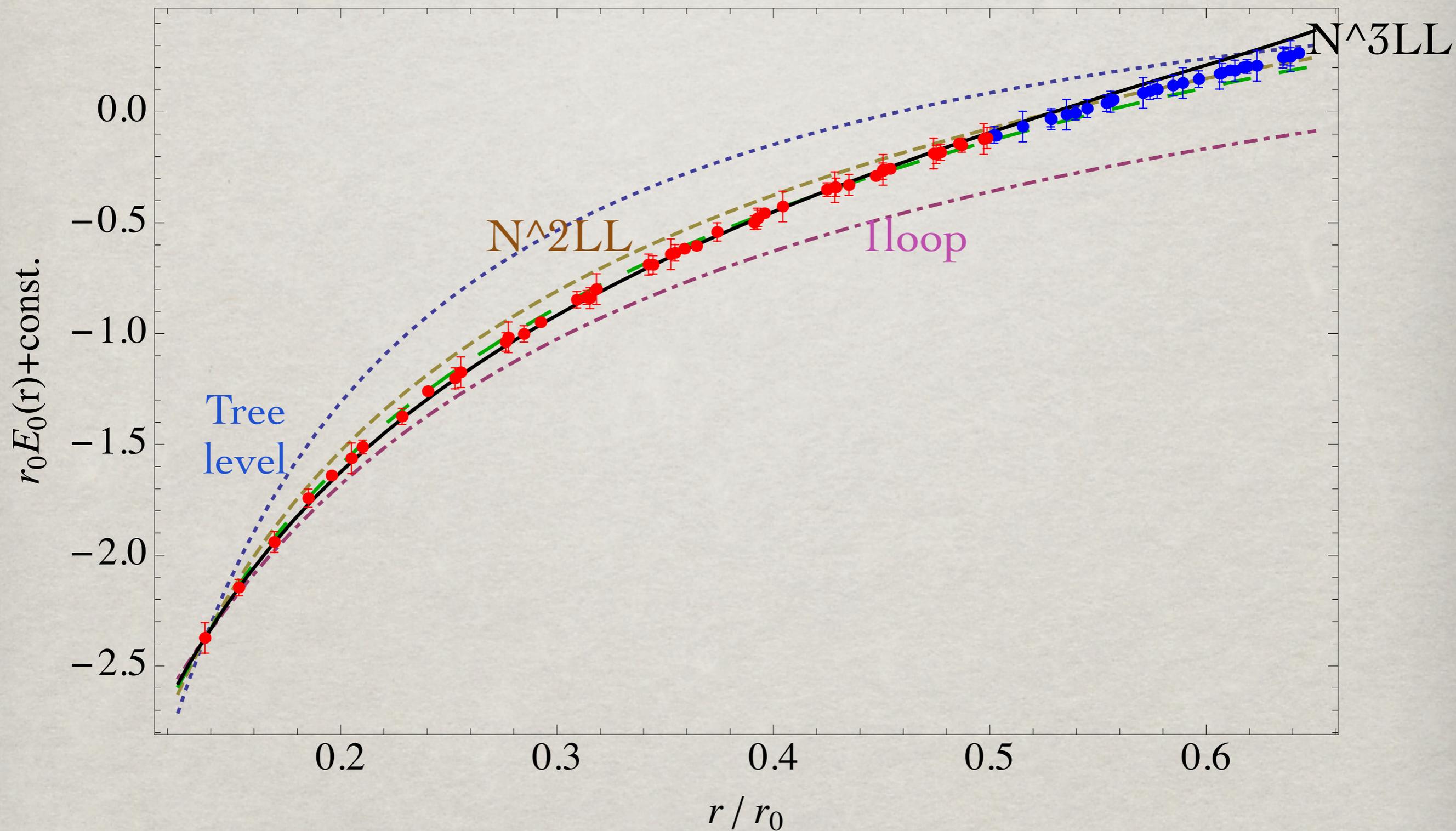
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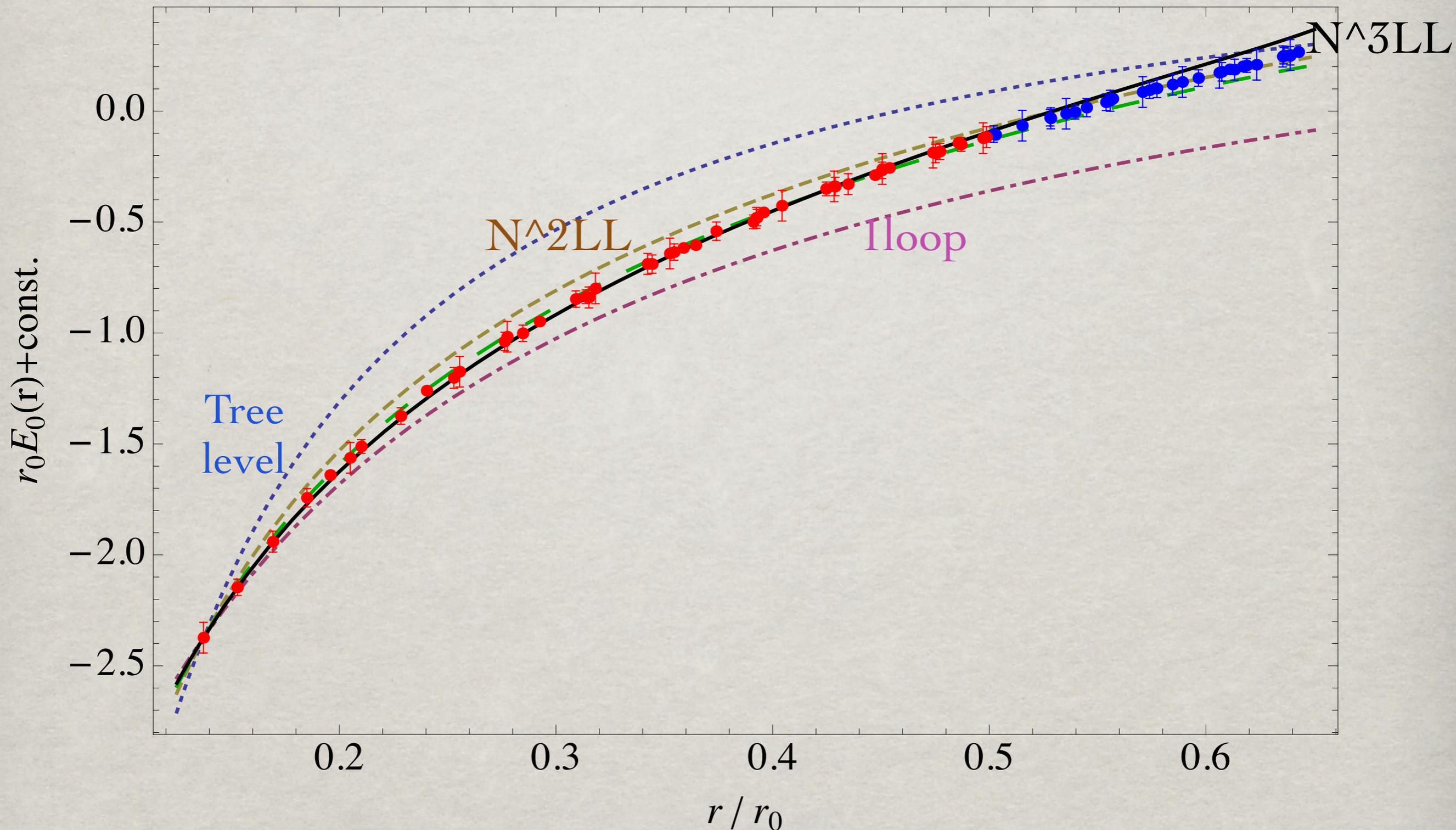
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Bazanov, N. B., Garcia, Petreczky, Soto, Vairo , 2012, 2014



Good convergence to the lattice data

Lattice data less accurate in the unquenched case

α_s extraction

Bazanov, N. B., Garcia, Petreczky, Soto, Vairo , 2014

We obtain an extraction of alphas at **N³LO** plus leading log resummation

$$\alpha_s(1.5\text{GeV}, n_f = 3) = 0.336_{-0.008}^{+0.012}$$

corresponding to

$$\alpha_s(M_z, n_f = 5) = 0.1166_{-0.0008}^{+0.0012}$$

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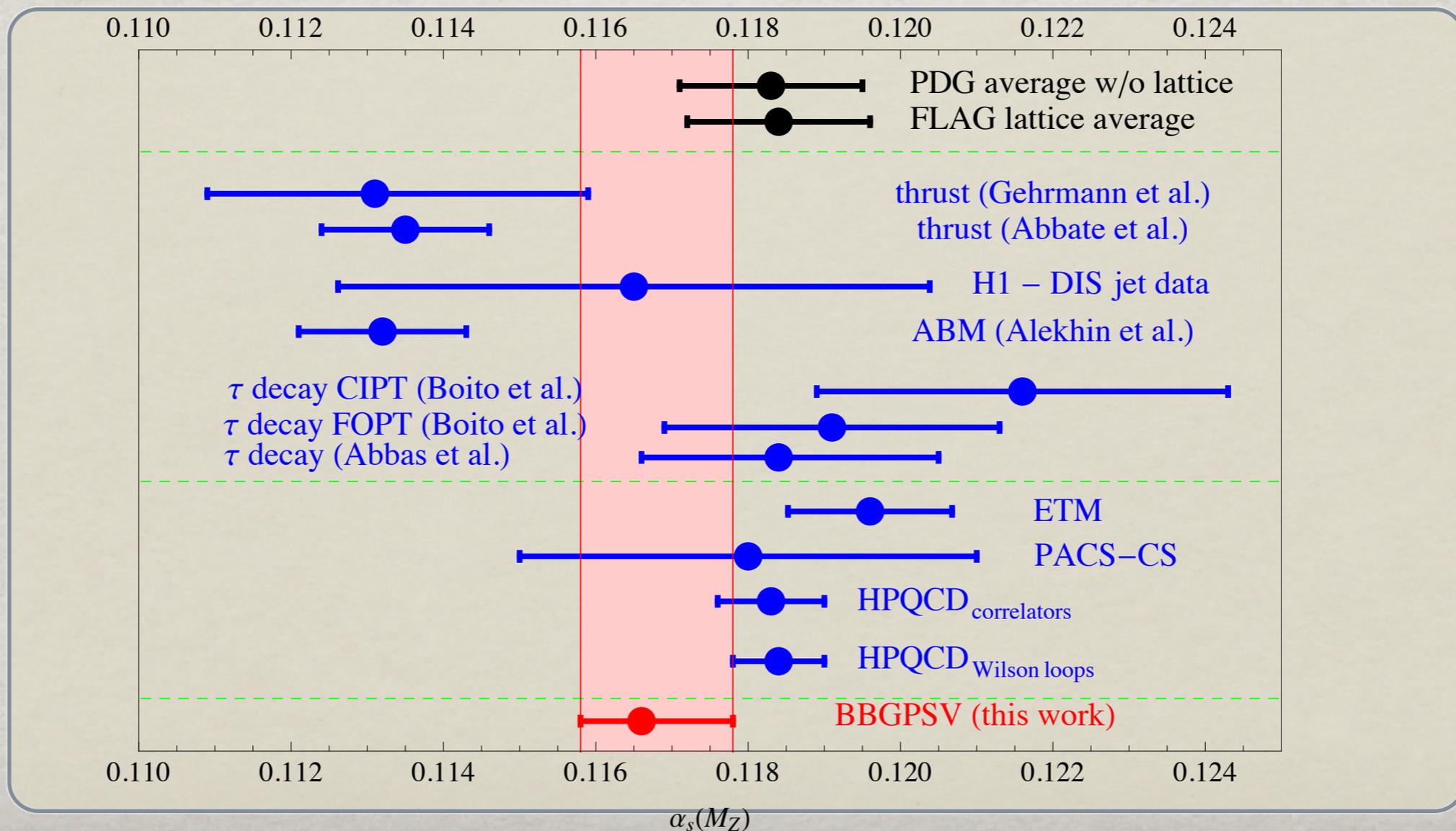
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Low-lying quarkonia

Physical observables of the $\Upsilon(1S)$, η_b , B_c , J/ψ , η_c , ... may be understood in terms of PT.

E.g. the spectrum up to $\mathcal{O}(M\alpha_s^5)$

$$E_n = \langle n | \frac{\mathbf{p}^2}{M} + V_s + \dots | n \rangle - i \frac{g^2}{3N_c} \int_0^\infty dt \langle n | \mathbf{r} e^{it(E_n^{(0)} - H_o)} \mathbf{r} | n \rangle \langle \mathbf{E}(t) \mathbf{E}(0) \rangle$$

Non-perturbative corrections are small and encoded in (local or non-local) condensates.

Applications to Quarkonium physics: systems with small radius

for references see the QWG doc
[arXiv:1010.5827](https://arxiv.org/abs/1010.5827)

- c and b masses at NNLO, $N^3\text{LO}^*$, NNLL^* ;
- B_c mass at NNLO; Penin et al 04
- B_c^* , η_c , η_b masses at NLL; Kniehl et al 04
- Quarkonium $1P$ fine splittings at NLO;
- $\Upsilon(1S)$, η_b electromagnetic decays at NNLL;
- $\Upsilon(1S)$ and J/ψ radiative decays at NLO;
- $\Upsilon(1S) \rightarrow \gamma\eta_b$, $J/\psi \rightarrow \gamma\eta_c$ at NNLO;
- $t\bar{t}$ cross section at NNLL;
- QQq and QQQ baryons: potentials at NNLO, masses, hyperfine splitting, ... ; N. B. et al 010
- Thermal effects on quarkonium in medium: potential, masses (at $m\alpha_s^5$), widths, ...;

$$\mathcal{B}(J/\psi \rightarrow \gamma\eta_c(1S)) = (1.6 \pm 1.1)\%$$

N. B. Yu Jia A. Vairo 2005

$$\mathcal{B}(\Upsilon(1S) \rightarrow \gamma\eta_b(1S)) = (2.85 \pm 0.30) \times 10^{-4}$$

$$\Gamma(\eta_b(1S) \rightarrow \gamma\gamma) = 0.54 \pm 0.15 \text{ keV}.$$

Y. Kiyo, A. Pineda, A. Signer 2010

$$\Gamma(\eta_b(1S) \rightarrow \text{LH}) = 7\text{-}16 \text{ MeV}$$

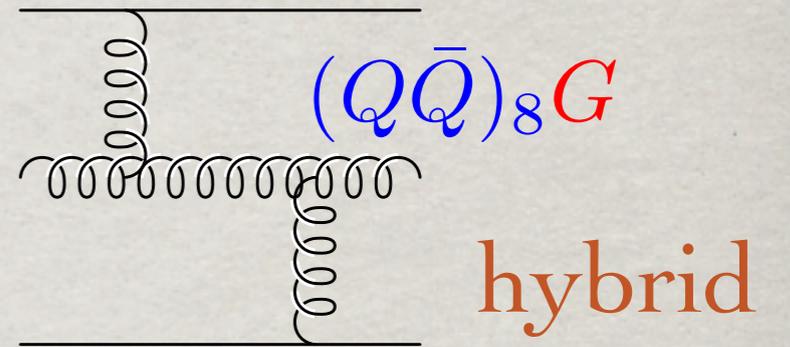
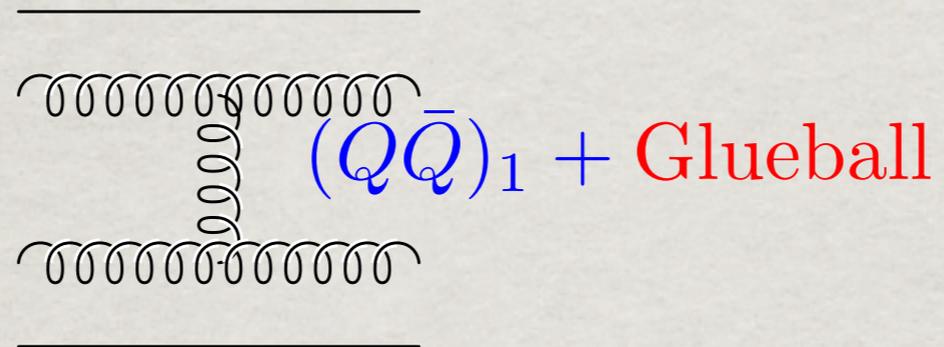
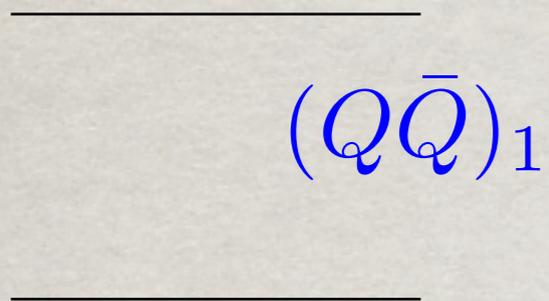
Quarkonium systems with
large radius $r \sim \Lambda_{QCD}^{-1}$

— Hitting the scale Λ_{QCD}

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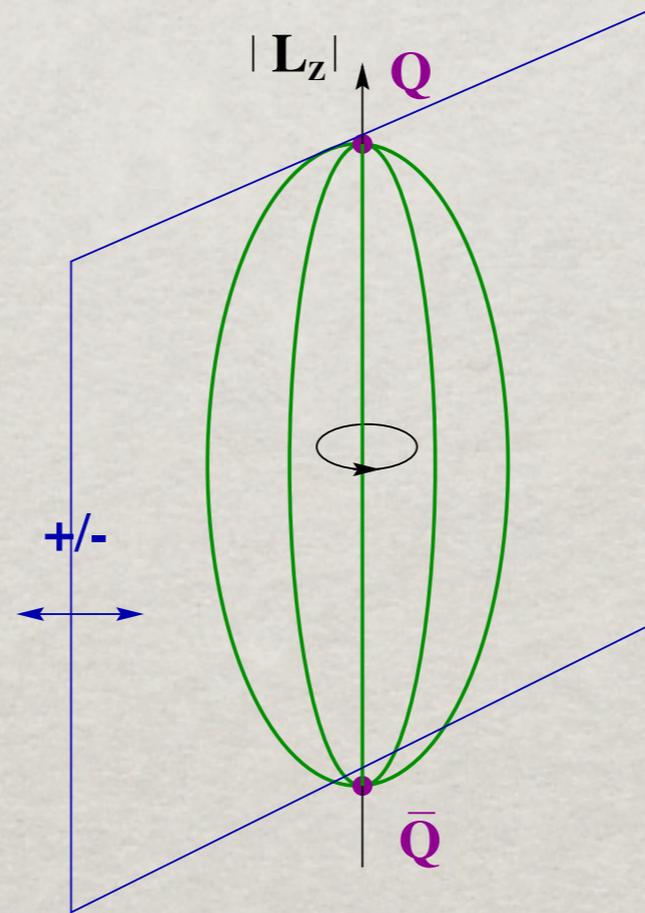
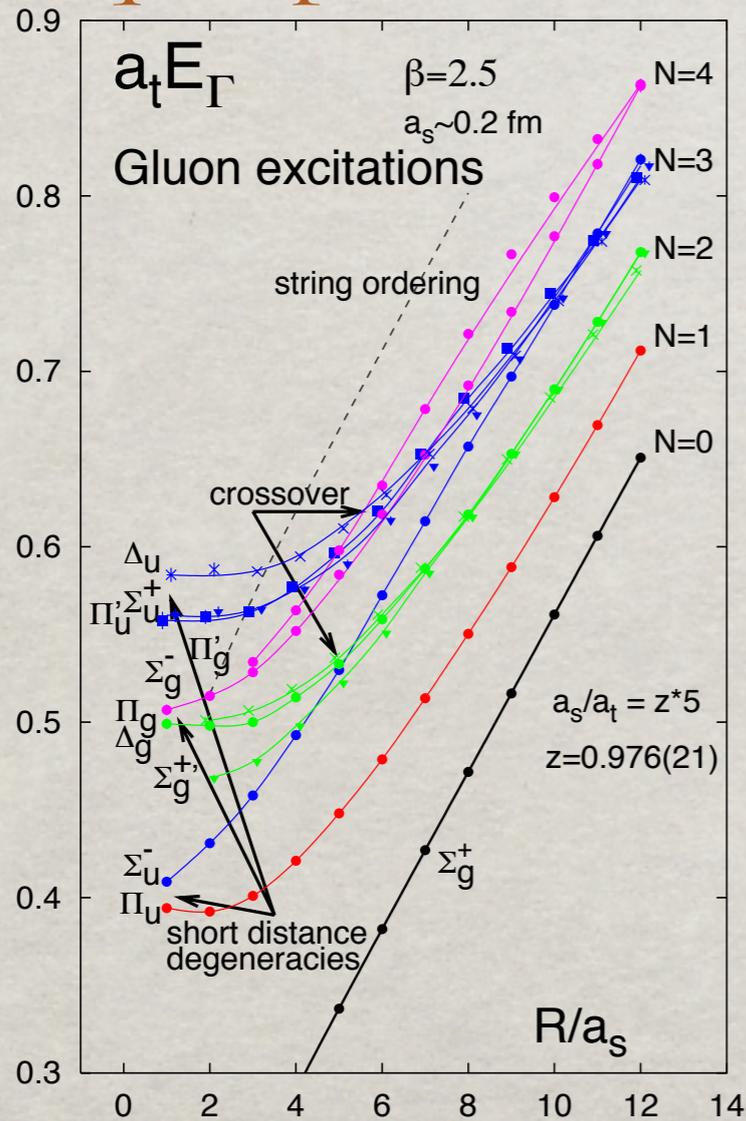
$(Q\bar{Q})_1$

$(Q\bar{Q})_1 + \text{Glueball}$

$(Q\bar{Q})_8 G$
hybrid

Static qcd spectrum

L
a
t
t
i
c
e

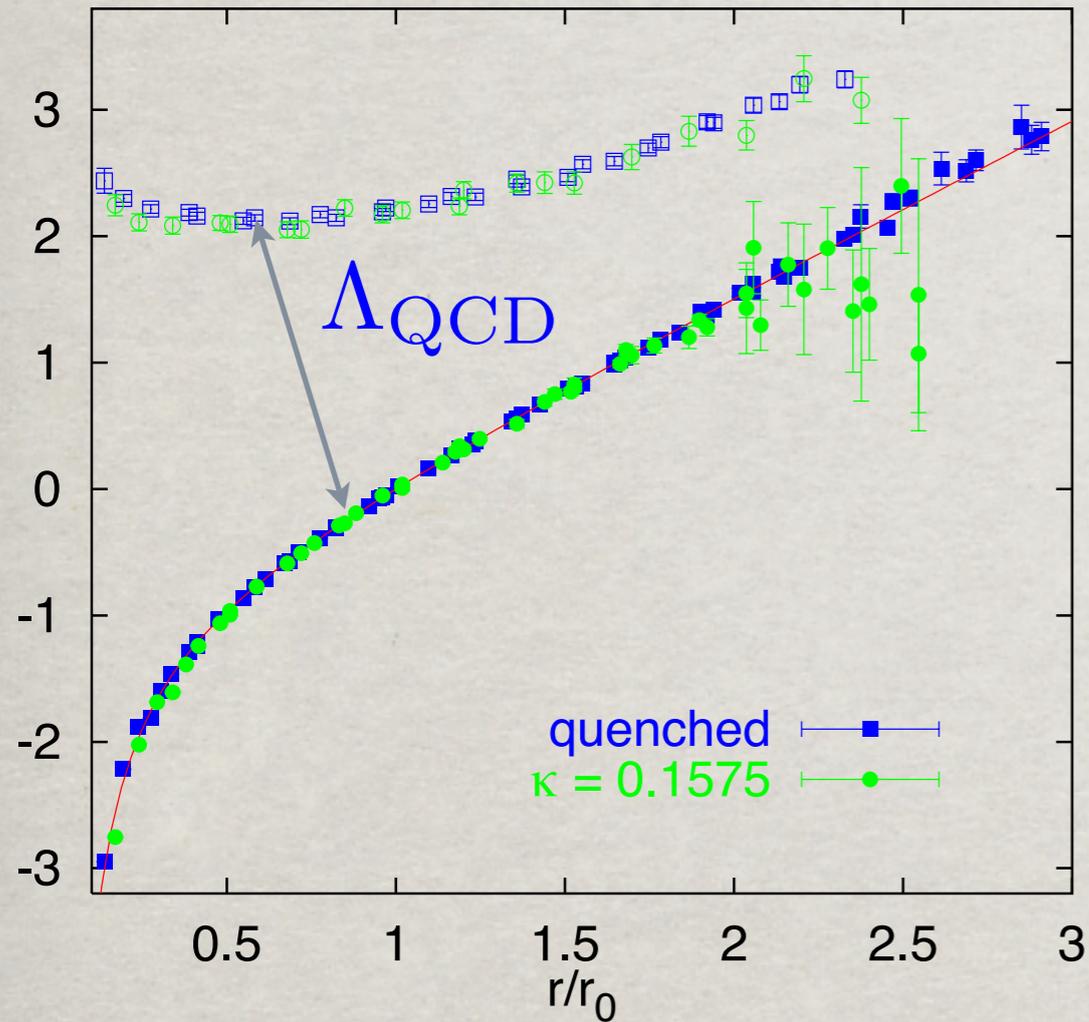


Symmetries of a diatomic molecule + C.C.

- a) $|L_z| = 0, 1, 2, \dots = \Sigma, \Pi, \Delta \dots$
- b) CP (u/g)
- c) Reflection (+/-) (for Σ only)

Quarkonium develops a gap to hybrids

Bali et al. 98



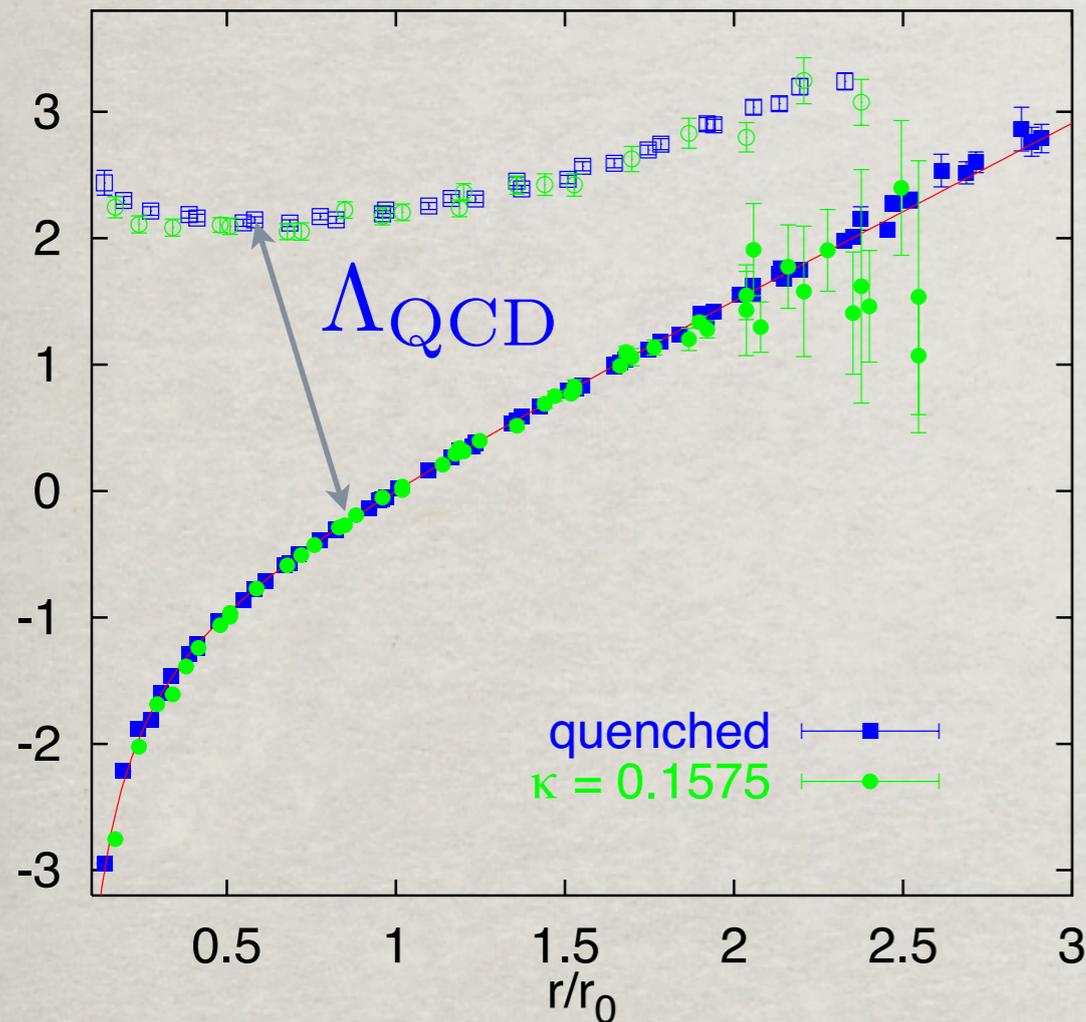
- $mv \sim \Lambda_{QCD}$

- integrate out all scales above mv^2

- gluonic excitations develop a gap Λ_{QCD} and are integrated out

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Brambilla Pineda Soto Vairo 00

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Brambilla Pineda Soto Vairo 00

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- The potentials $V = \text{Re}V + \text{Im}V$ from QCD in the matching: get spectra and decays
- V to be calculated on the lattice or in QCD vacuum models

Quarkonium singlet static potential

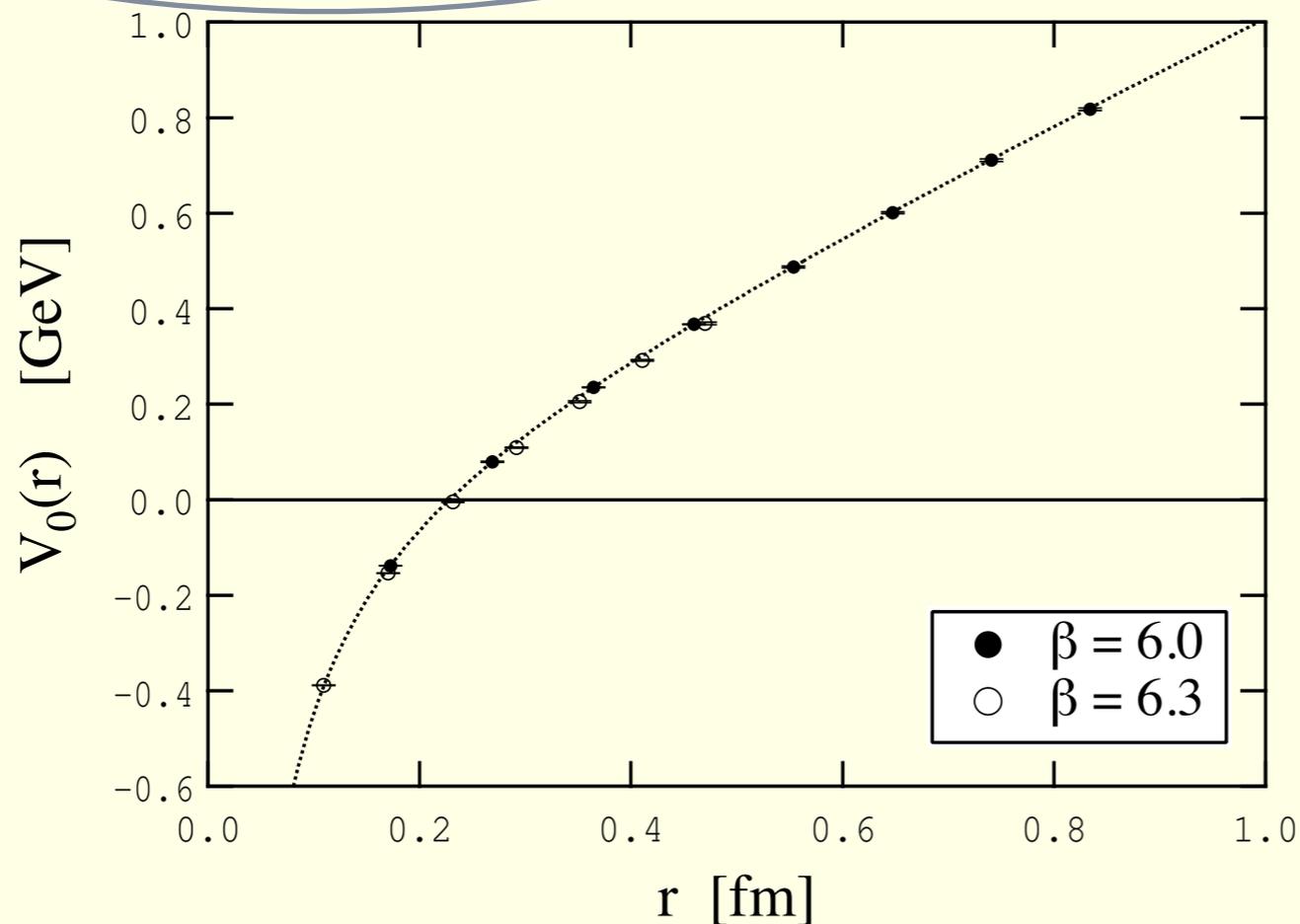
$$V = V_0 + \frac{1}{m} V_1 + \frac{1}{m^2} (V_{SD} + V_{VD})$$

Quarkonium singlet static potential

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$$V_s^{(0)} = \lim_{T \rightarrow \infty} \frac{i}{T} \ln \langle W(r \times T) \rangle = \lim_{T \rightarrow \infty} \frac{i}{T} \ln \langle \square \rangle$$

$$W = \langle \exp\{ig \oint A^\mu dx_\mu\} \rangle$$

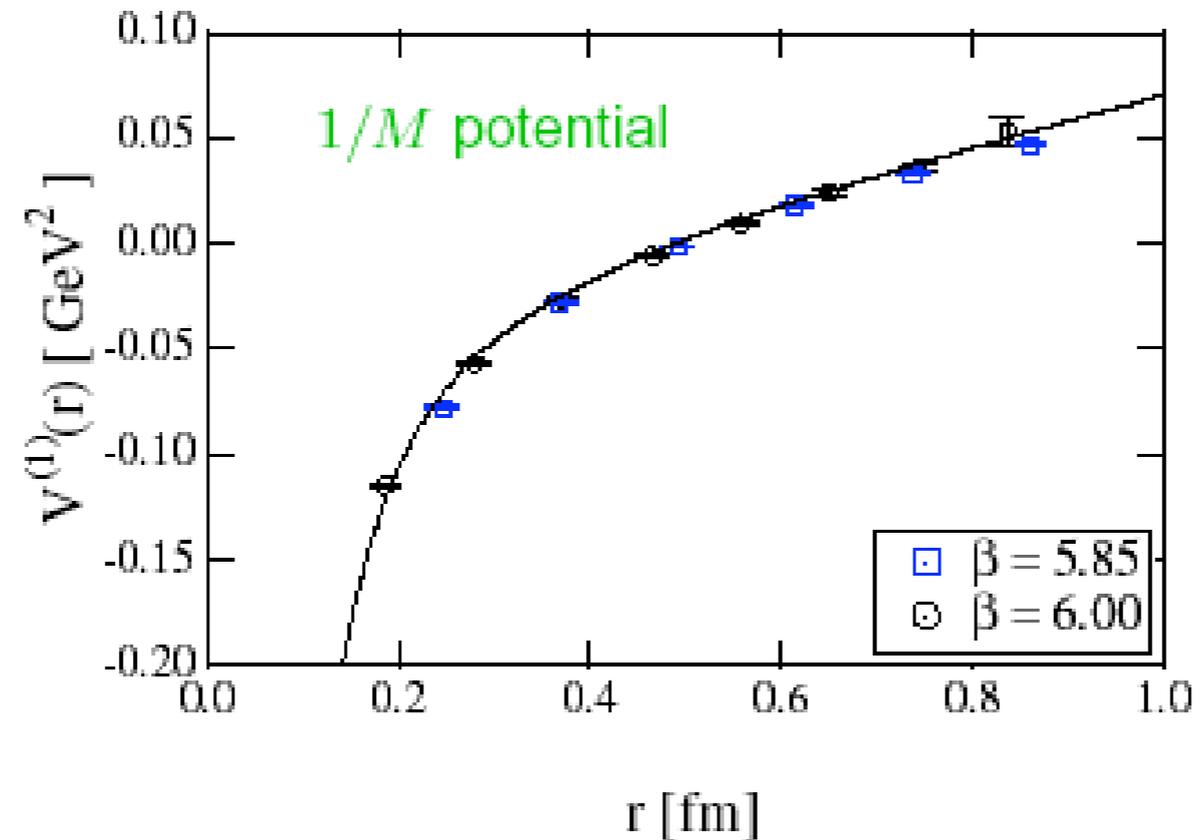


Quarkonium singlet static potential

Potentials are given in a factorized form as product of NRQCD matching coefficients and low energy terms. These are gauge invariant wilson loop with electric and magnetic insertions

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o Koma Koma Wittig PoS LAT2007(07)111

$$\frac{V_s^{(1)}}{m} = -\frac{1}{2m} \int_0^\infty dt t \langle \text{Wilson Loop with Electric Insertions} \rangle$$

QCD Spin dependent potentials

$$\begin{aligned}
 V_{\text{SD}}^{(2)} = & \frac{1}{r} \left(C_F \epsilon^{kij} \frac{2r^k}{r} i \int_0^\infty dt t \langle \text{diag}_1 \rangle - \frac{1}{2} V_s^{(0)'} \right) (\mathbf{S}_1 + \mathbf{S}_2) \cdot \mathbf{L} \\
 & - C_F^2 \hat{r}_i \hat{r}_j i \int_0^\infty dt \left(\langle \text{diag}_2 \rangle - \frac{\delta_{ij}}{3} \langle \text{diag}_3 \rangle \right) \\
 & \quad \times \left(\mathbf{S}_1 \cdot \mathbf{S}_2 - 3(\mathbf{S}_1 \cdot \hat{\mathbf{r}})(\mathbf{S}_2 \cdot \hat{\mathbf{r}}) \right) \\
 & + \left(\frac{2}{3} C_F^2 i \int_0^\infty dt \langle \text{diag}_4 \rangle - 4(d_2 + C_F d_4) \delta^{(3)}(\mathbf{r}) \right) \mathbf{S}_1 \cdot \mathbf{S}_2
 \end{aligned}$$

Eichten Feinberg 81, Gromes 84, Chen et al. 95 Brambilla Vairo 99 Pineda, Vairo 00

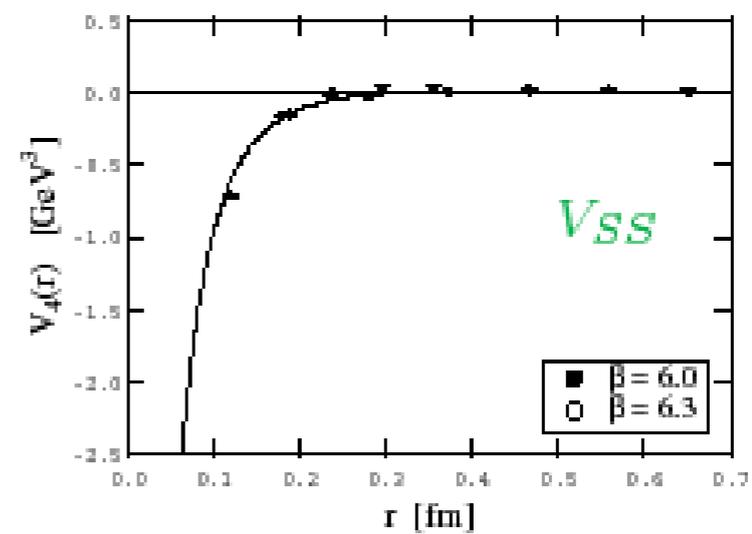
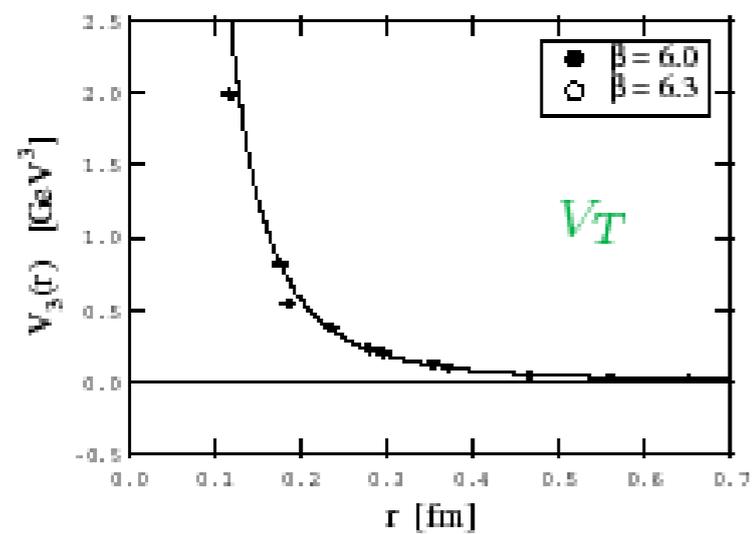
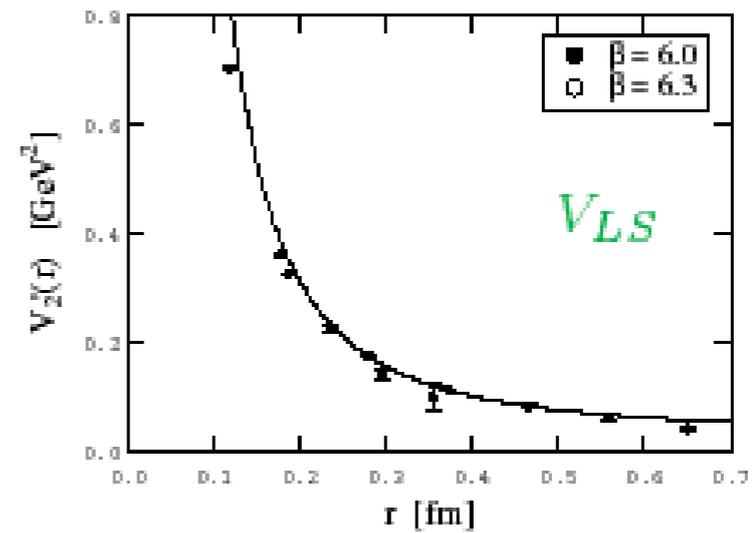
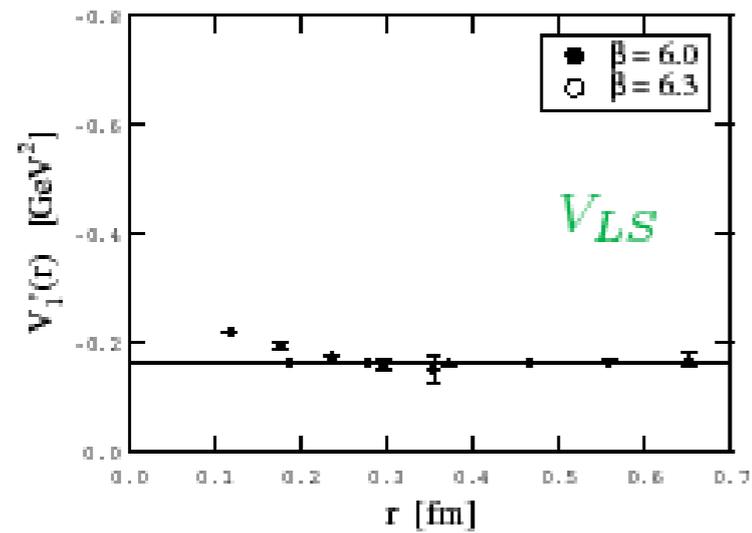
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Eichten Feinberg 81, Gromes 84, Chen et al. 95 Brambilla Vairo 99 Pineda, Vairo 00

-factorization; power counting;
 QM divergences absorbed by
 NRQCD matching coefficients

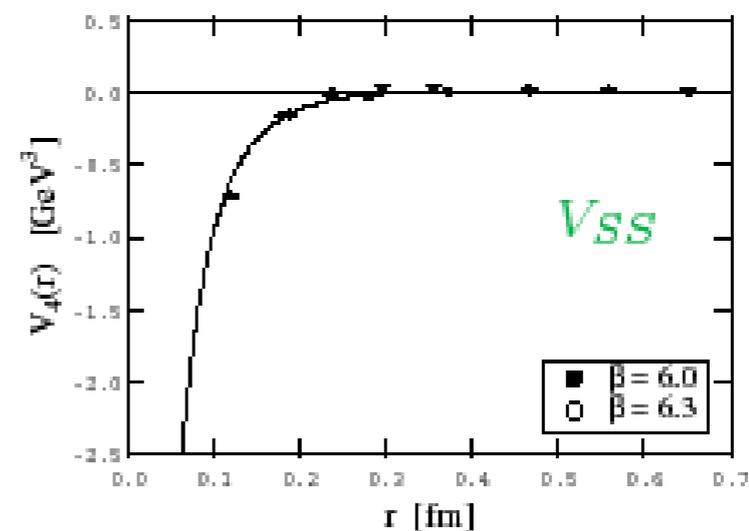
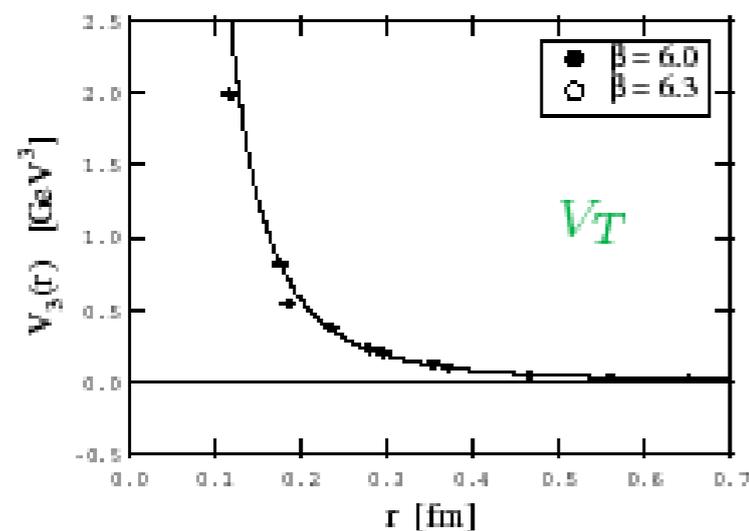
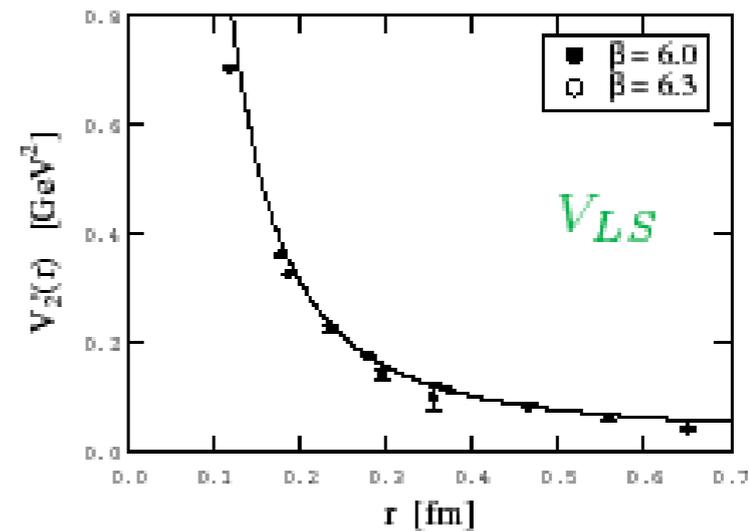
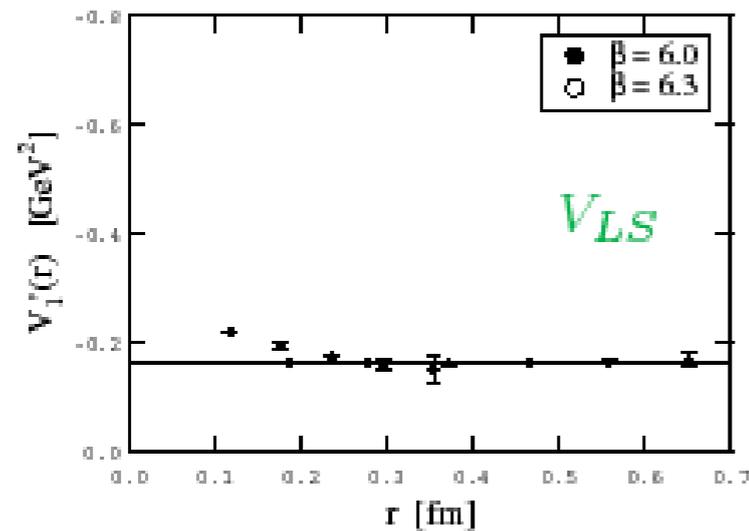
Spin dependent potentials



Koma Koma Wittig 05, Koma Koma 06

Terrific advance in the data precision with Lüscher multivel algorithm!

Spin dependent potentials



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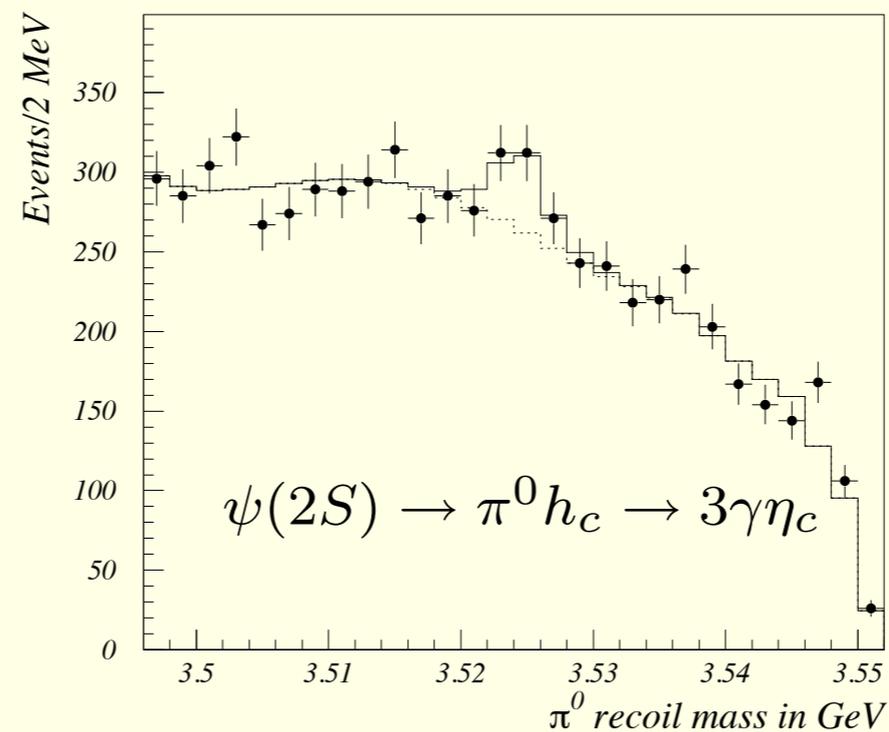
Terrific advance in the data precision with Lüscher multivel algorithm!

Such data can distinguish different models for the dynamics of low energy QCD e.g. effective string model

N. B., Martinez, Vairo 2014

Confirmed in the spectrum, e.g. no long range spin-spin interaction

h_c, h_b



$M_{h_c} = 3524.4 \pm 0.6 \pm 0.4 \text{ MeV}$ ○ CLEO PRL 95 (2005) 102003

$M_{h_c} = 3525.8 \pm 0.2 \pm 0.2 \text{ MeV}, \quad \Gamma < 1 \text{ MeV}$ ○ E835 PRD 72 (2005) 032001

$M_{h_c} = 3525.40 \pm 0.13 \pm 0.18 \text{ MeV}, \quad \Gamma < 1.44 \text{ MeV}$ ○ BES PRL 104 (2010) 132002

To be compared with $M_{c.o.g.}(1P) = 3525.36 \pm 0.2 \pm 0.2 \text{ MeV}$.

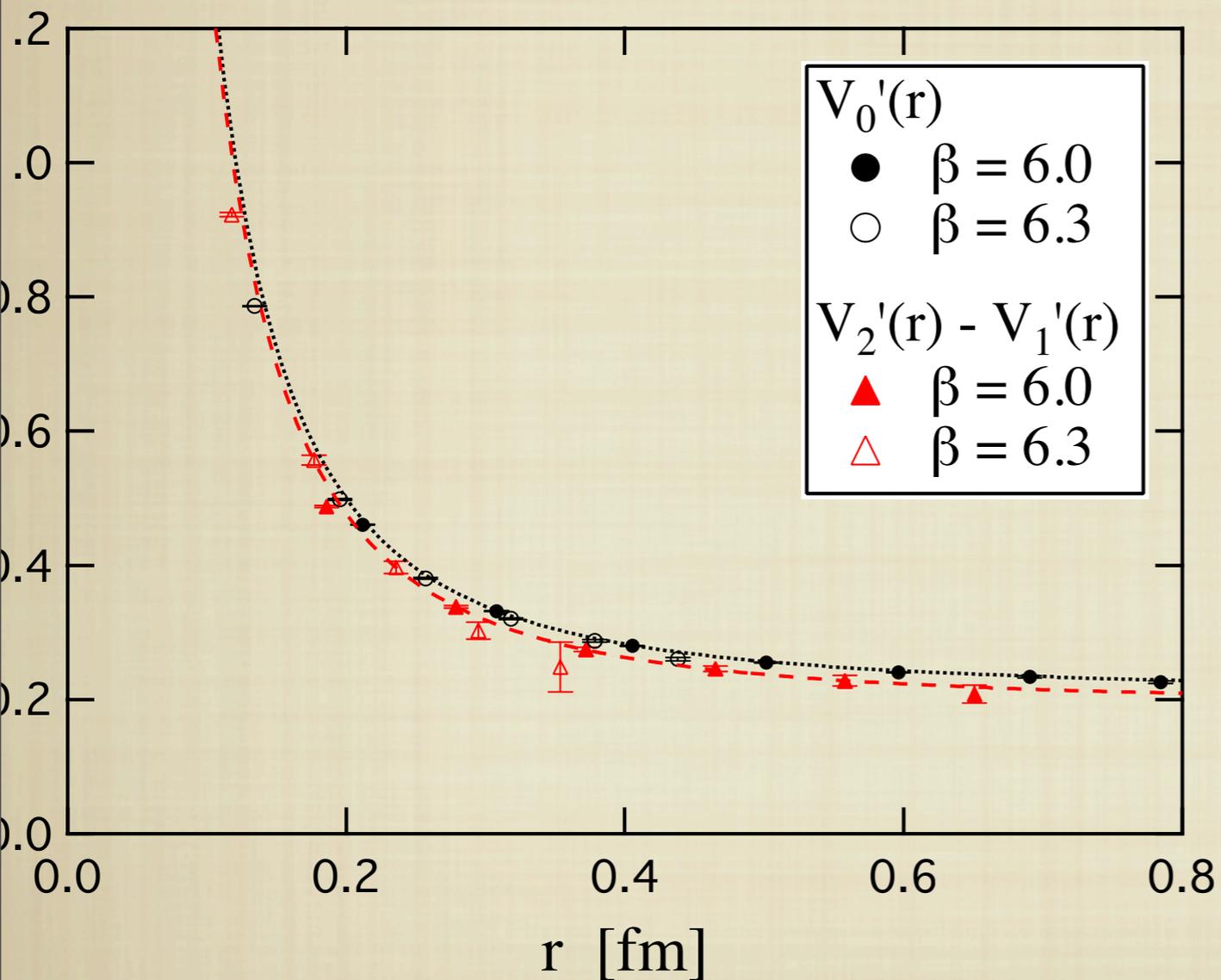
● Also

$M_{h_b} = 9902 \pm 4 \pm 1 \text{ MeV}$ ○ BABAR arXiv:1102.4565

To be compared with $M_{c.o.g.}(1P) = 9899.87 \pm 0.28 \pm 0.31 \text{ MeV}$.

Exact relations from Poincare' invariance

The EFT is still Poincare' invariant \rightarrow this induces relations among the potentials (this corresponds to reparameterization invariance \rightarrow one can reformulate it with Poincare' algebra)



e. g. $V_0'(r) = V_2'(r) - V_1'(r)$
It can be used a check of the lattice calculation

many other relations among potentials in the EFT
N. B, D. Gromes, A. Vairo

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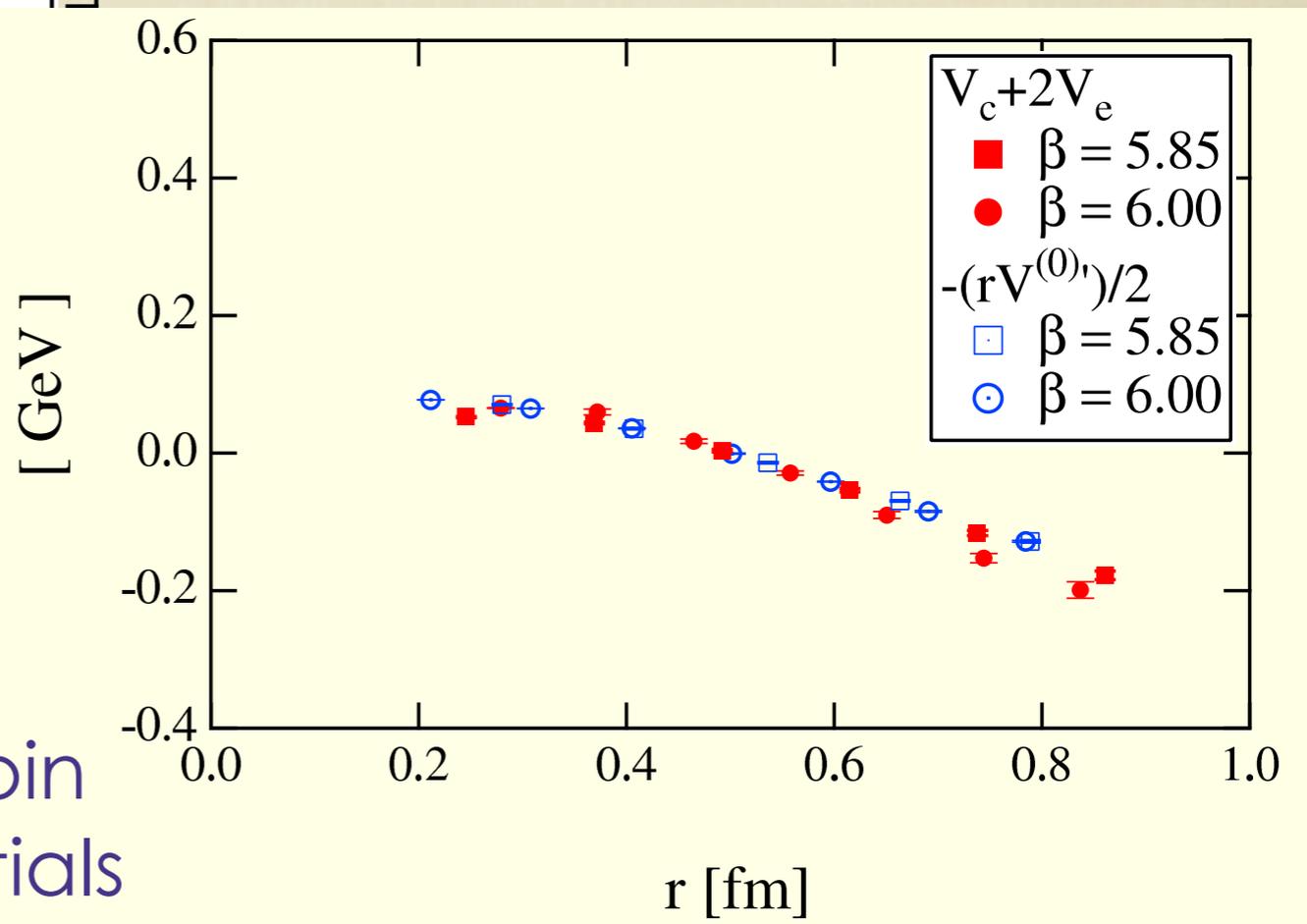
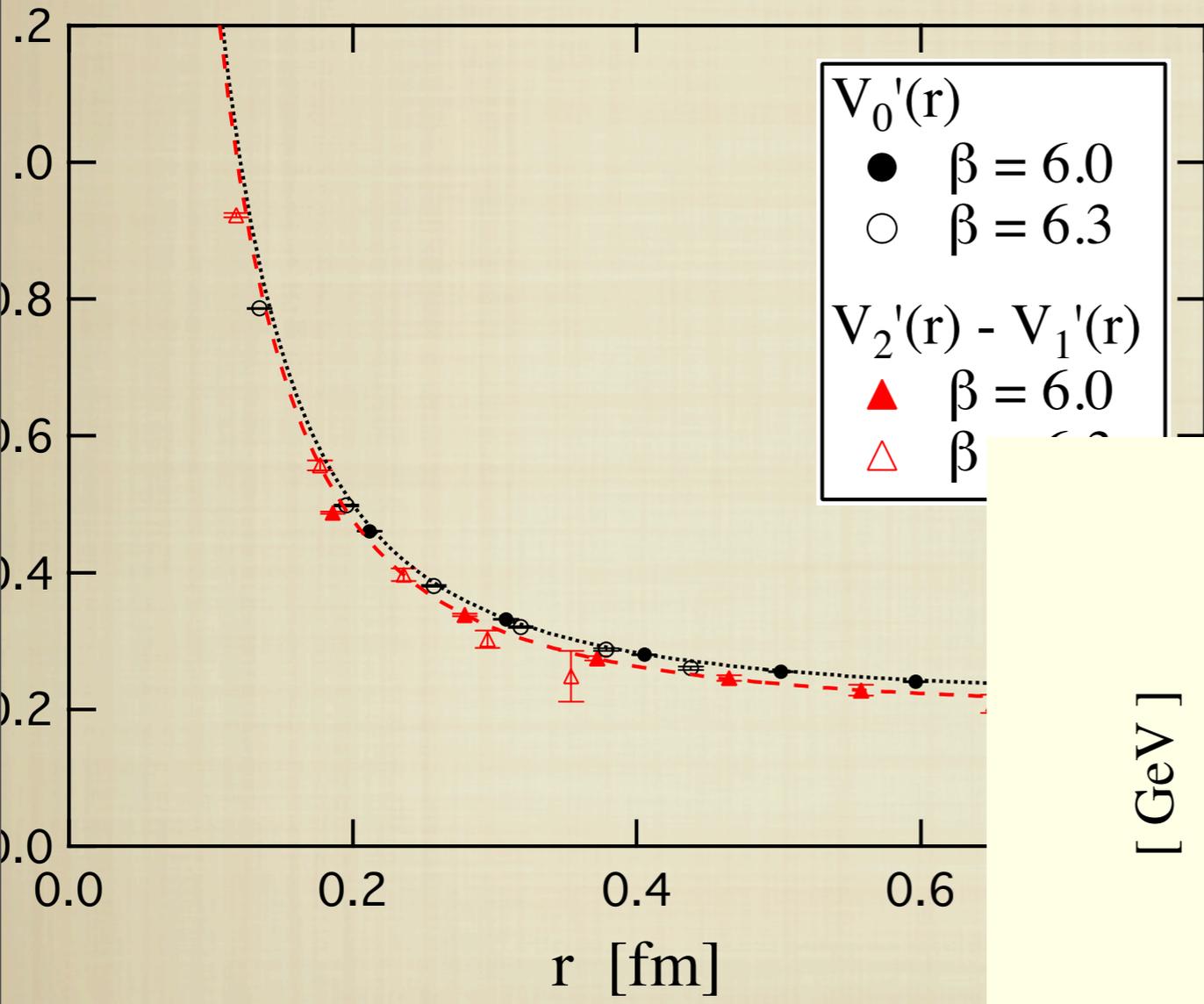
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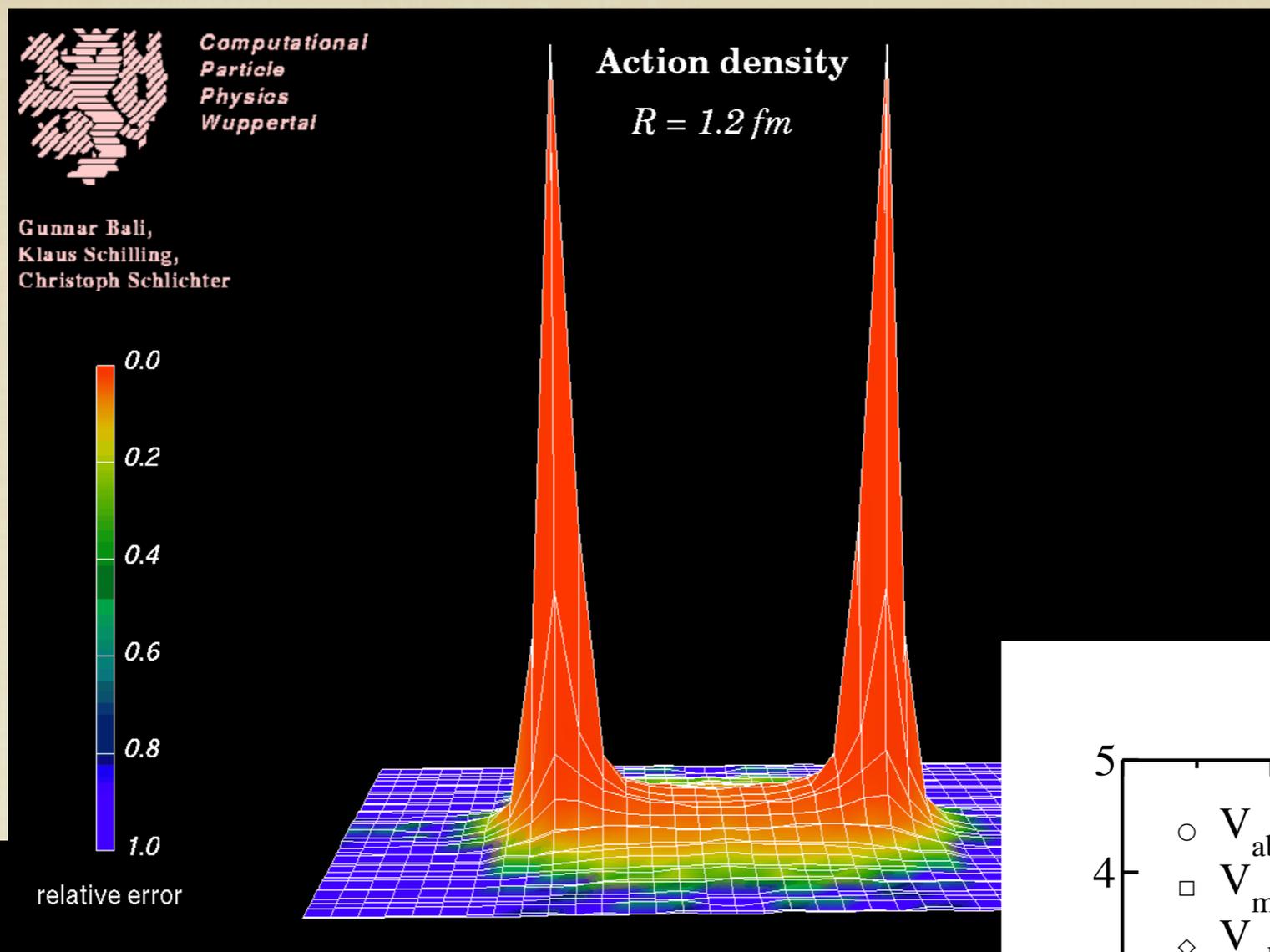
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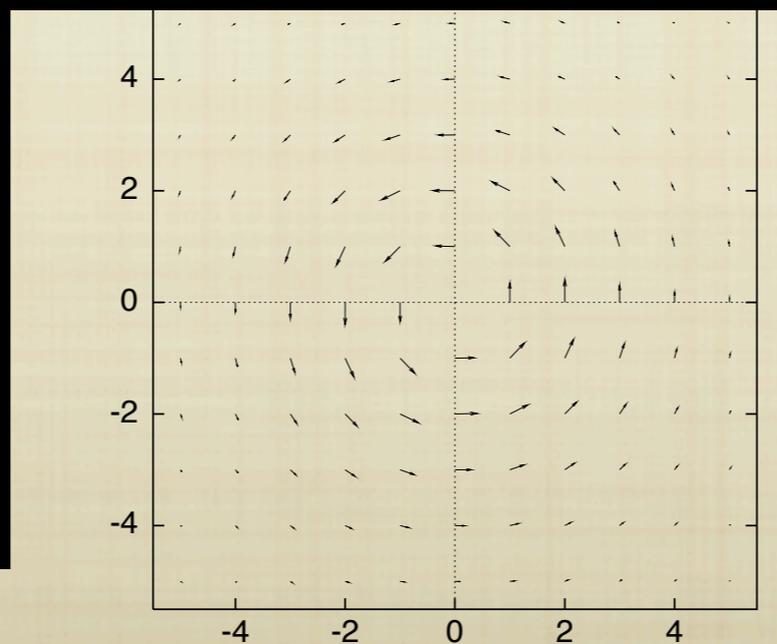
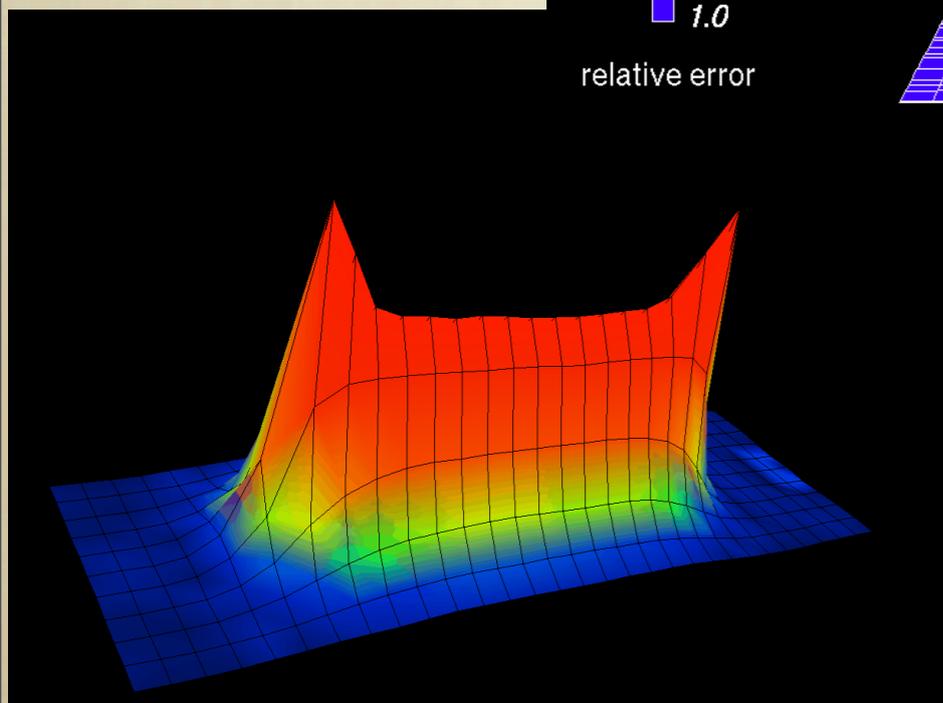
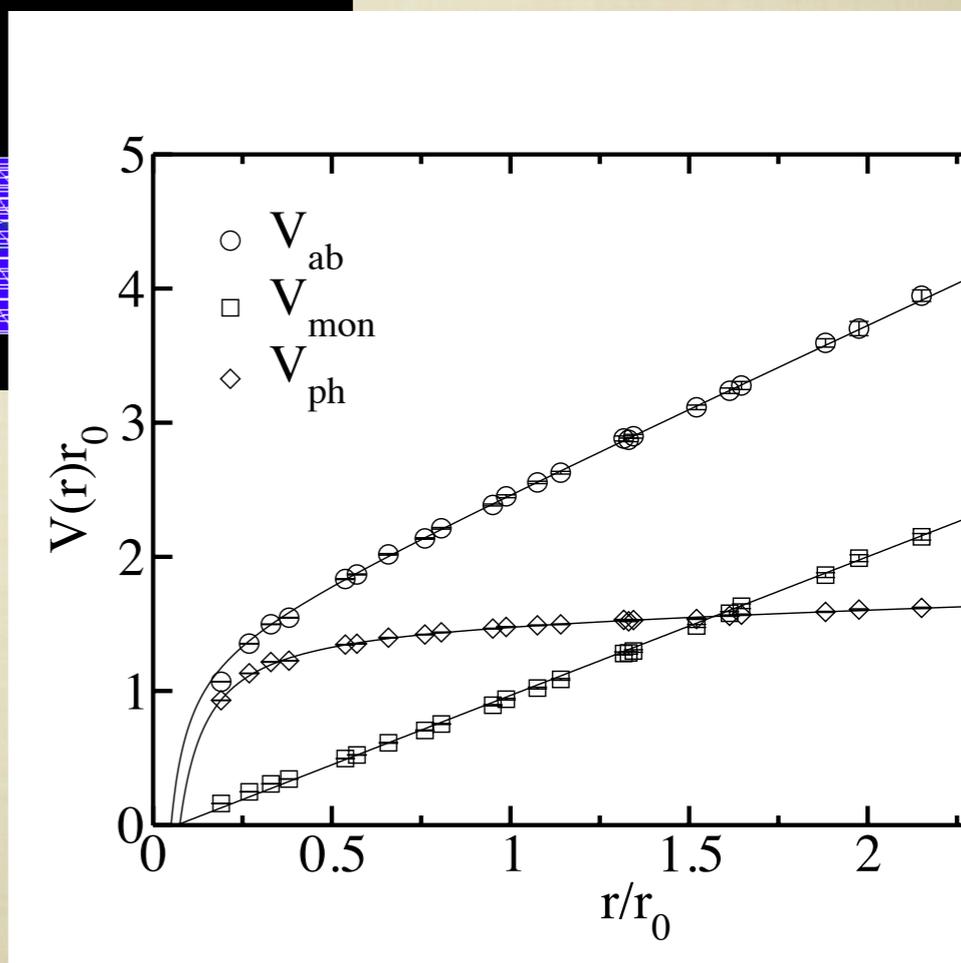
relations involving spin independent potentials

Low energy physics factorized in Wilson loops: can be used to probe the confinement mechanism

Bali et al



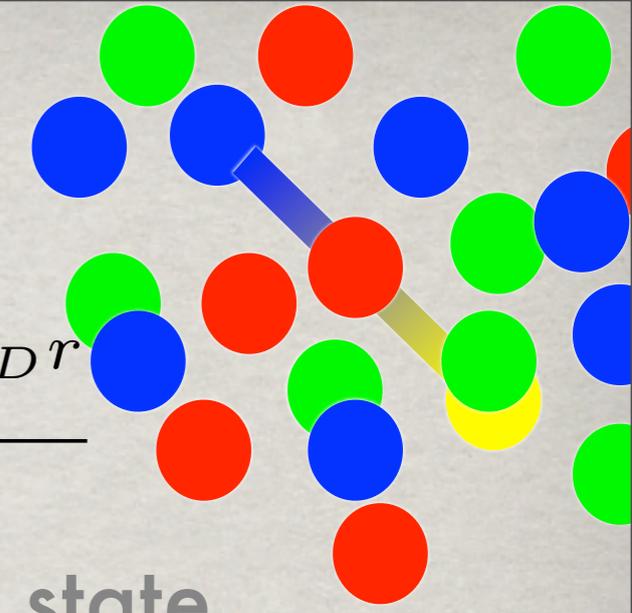
Boryakov et al. 04



Heating quarkonium systems

$$T > 0$$

Quarkonium in a hot medium



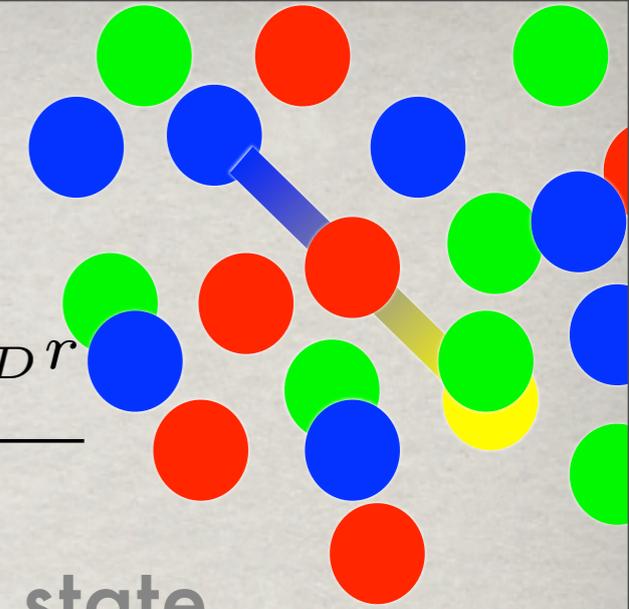
Matsui Satz 86

color screening of the potential
originates quarkonium dissociation

Debye charge screening
(electromagnetic plasma)

$$V(r) \sim -\alpha_s \frac{e^{-m_D r}}{r}$$
$$r \sim \frac{1}{m_D} \longrightarrow \text{Bound state dissolves}$$

Quarkonium in a hot medium



Matsui Satz 86

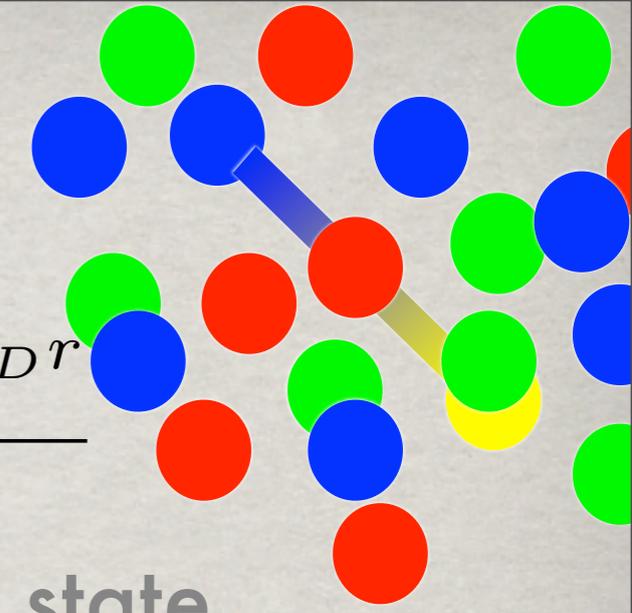
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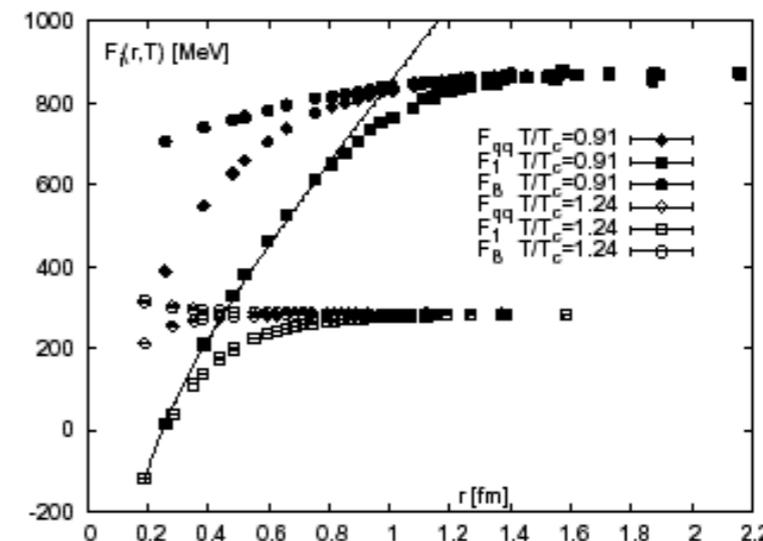
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But what is the potential at finite T?

up to few years ago phenomenological potentials used or hints from other observable calculated on the lattice

Free energy vs potential

- Either phenomenological potentials have been used so far or the free energy calculated on the lattice.
- The free energy is not the static potential: the average free energy ($\sim \langle \text{Tr} L^\dagger(r) \text{Tr} L(0) \rangle$) is an overlap of singlet and octet quark-antiquark states, what is called the singlet ($\sim \langle \text{Tr} L^\dagger(r) L(0) \rangle$) and the octet ($\sim \langle \text{Tr} L^\dagger(r) \text{Tr} L(0) \rangle - 1/3 \langle \text{Tr} L^\dagger(r) L(0) \rangle$) free energy are gauge dependent;



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$$T \gg gT \gg g^2T \dots$$

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more scales $m \gg mv \gg mv^2$

?

$$T \gg gT \gg g^2T \dots$$

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Debye mass
Screening Scale

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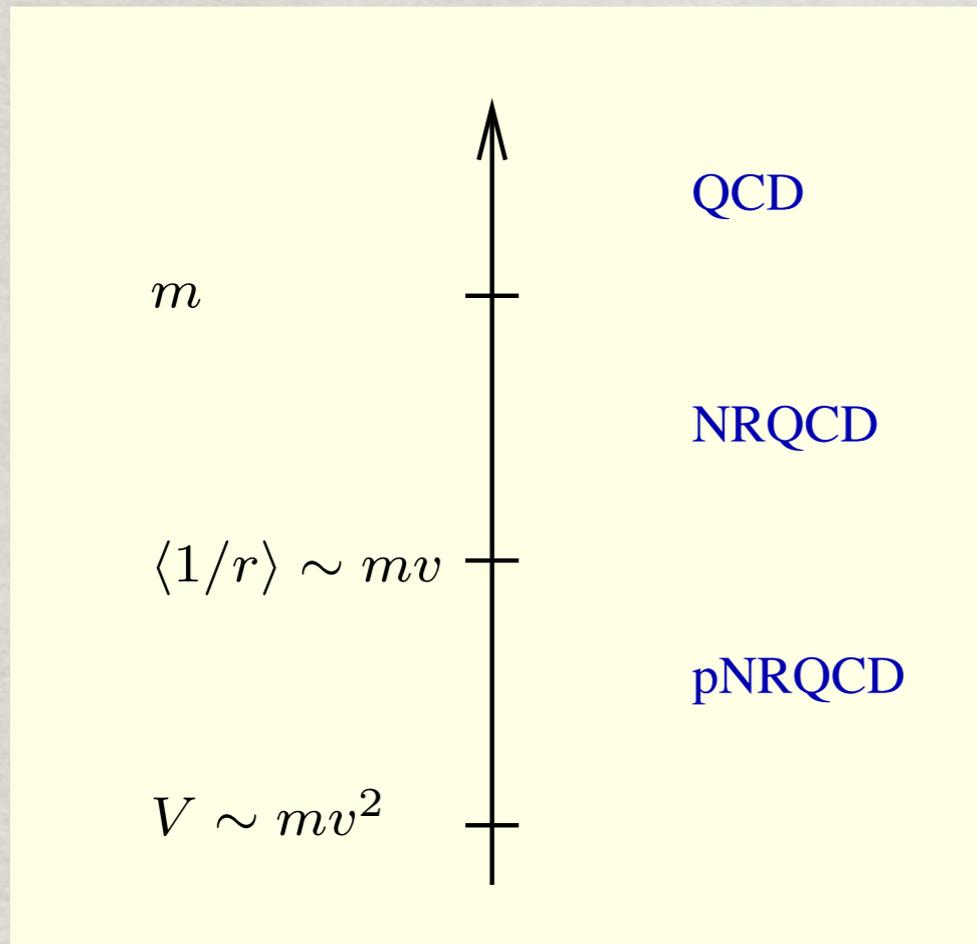
Without heavy quarks an EFT already exists that comes from integrating out hard gluon of $p \sim T$:

Hard Thermal Loop EFT

\rightarrow obtain pNRQCD at finite T

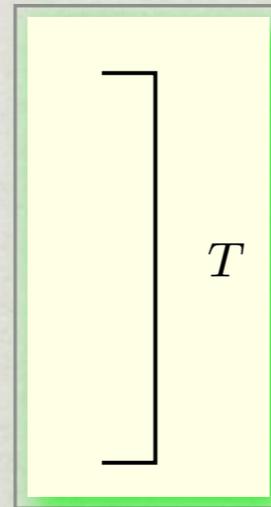
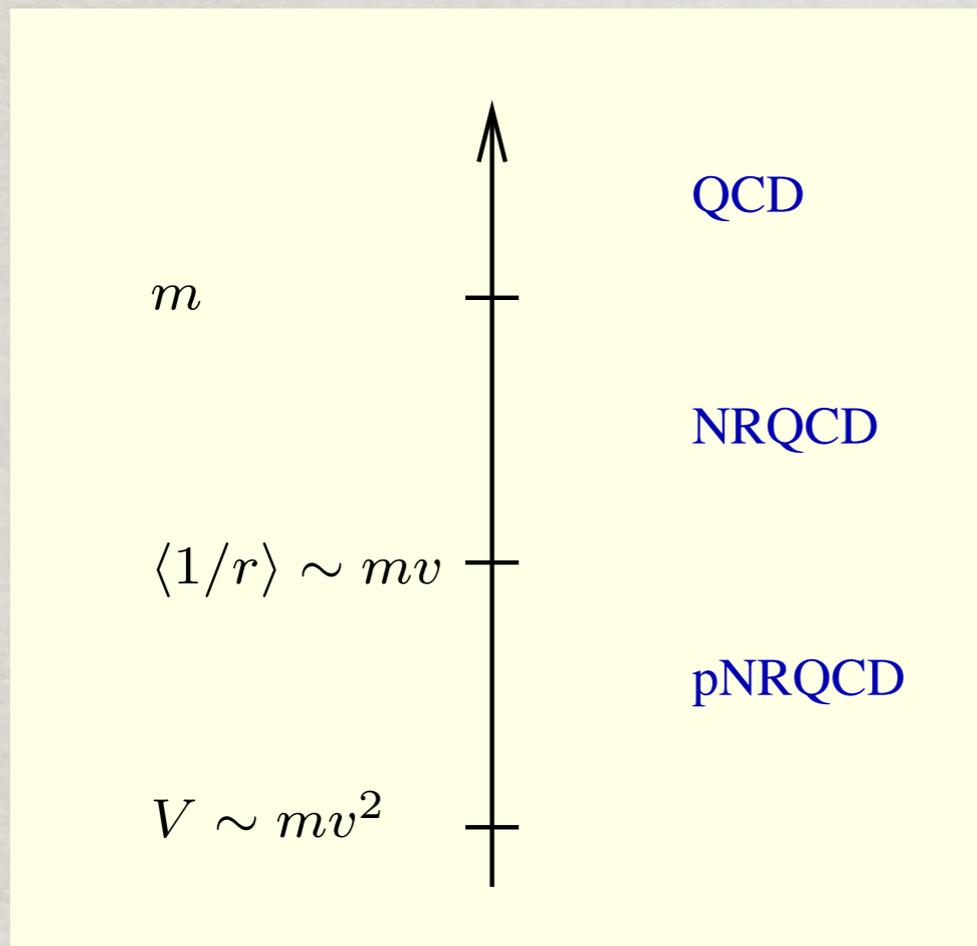
Quarkonium at finite T with pNRQCD

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08



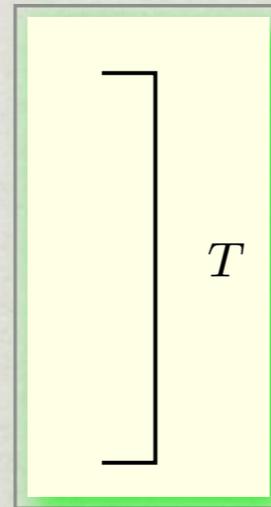
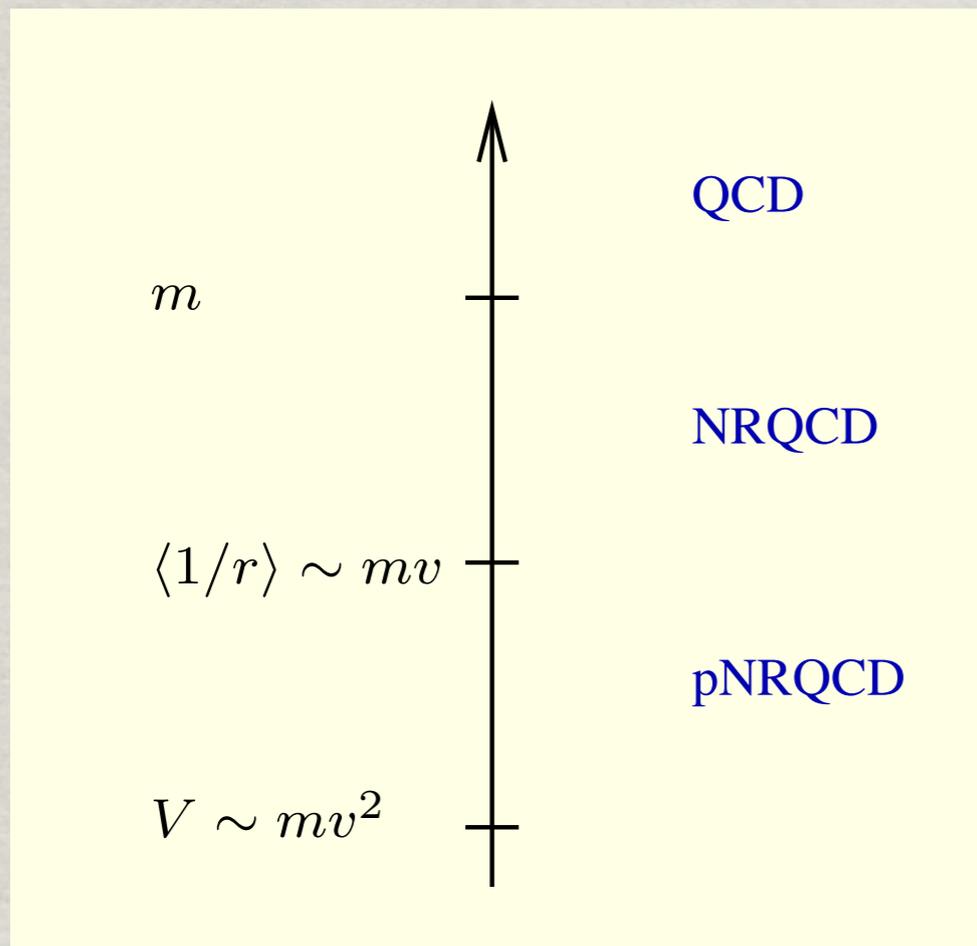
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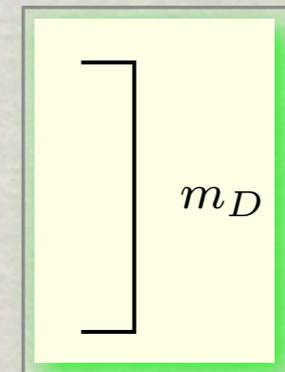
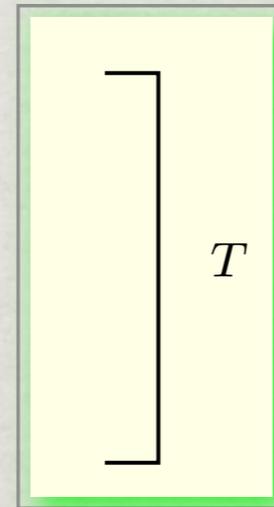
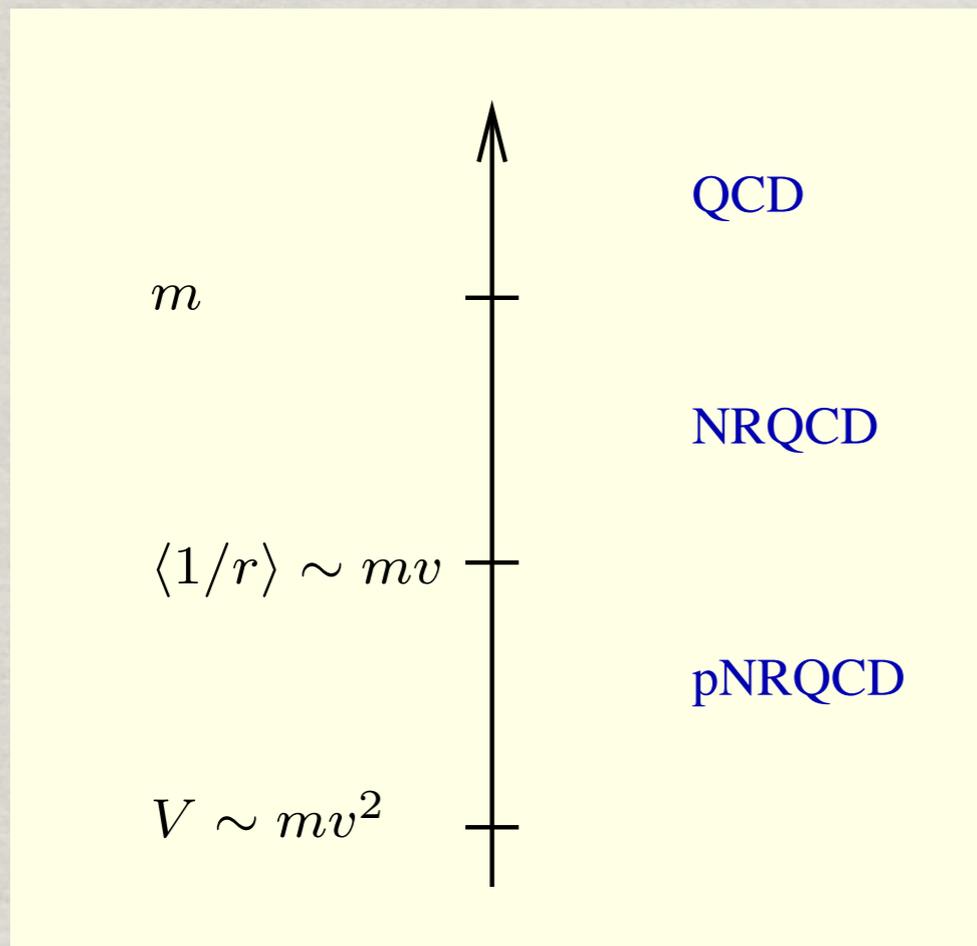
Quarkonium at finite T with pNRQCD

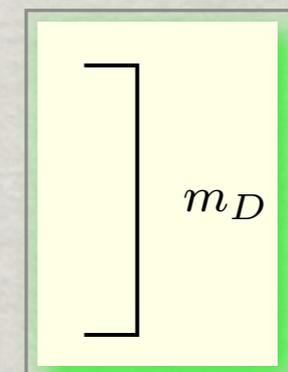
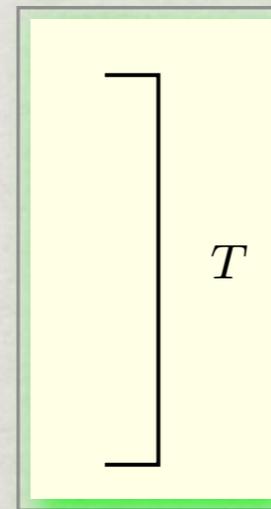
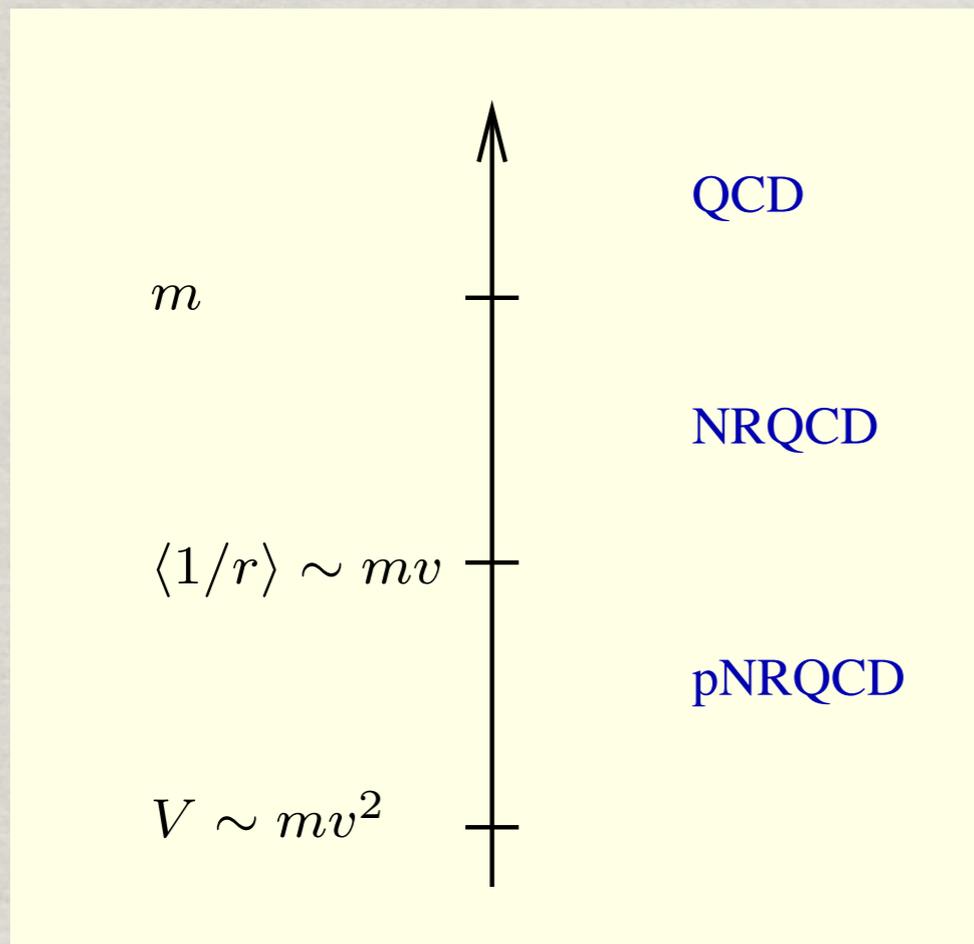
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Quarkonium at finite T with pNRQCD

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08





We work under the conditions:

We assume that bound states exist for

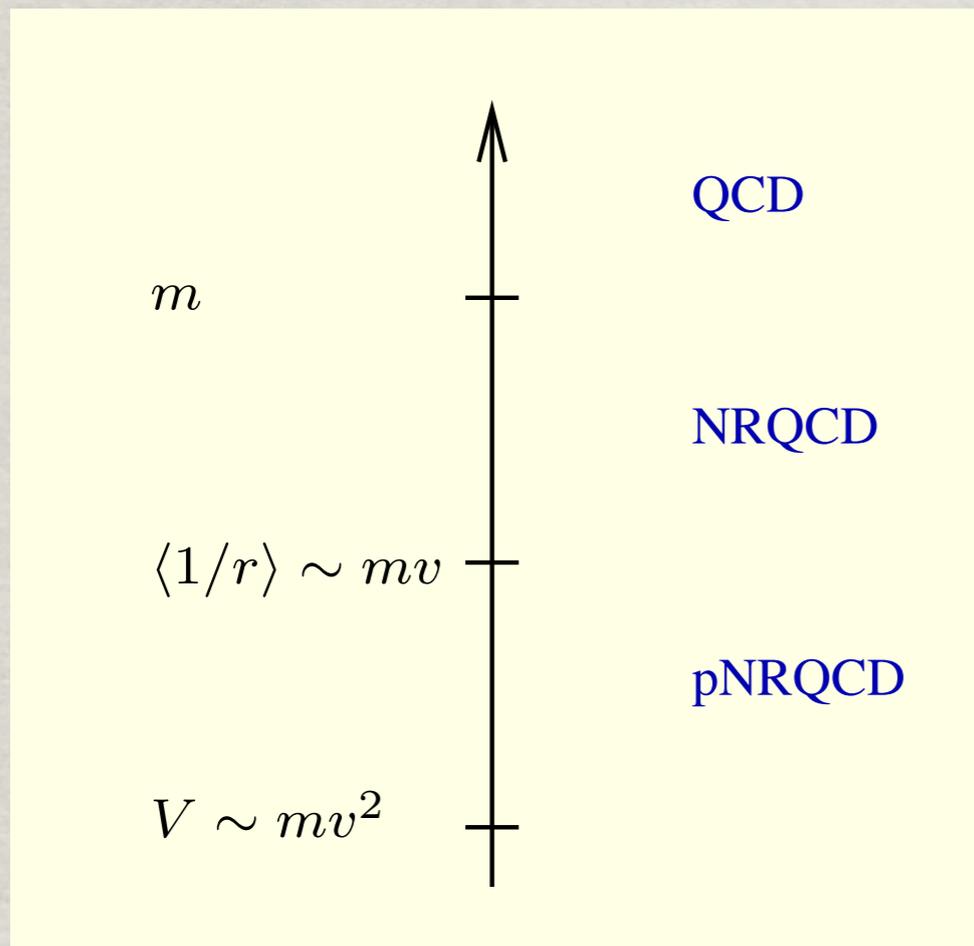
- $T \ll m$
- $\langle 1/r \rangle \sim mv \gtrsim m_D$

We neglect smaller thermodynamical scales.

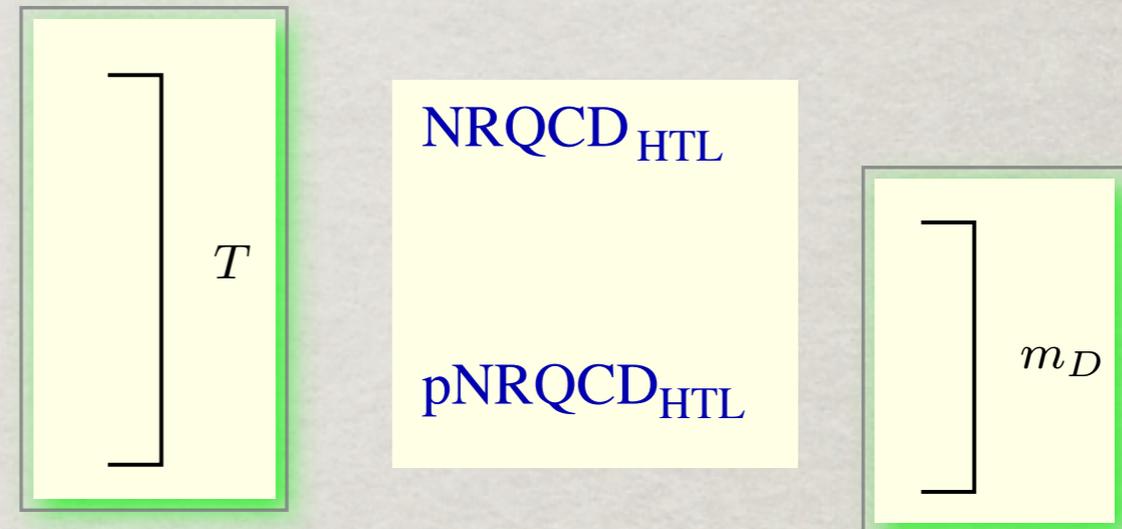
In the weak coupling regime:

- $v \sim \alpha_s \ll 1$; valid for tightly bound states: $\Upsilon(1S)$, J/ψ , ...
- $T \gg gT \sim m_D$.

Effects due to the scale Λ_{QCD} will not be considered.



pNRQCD at finite T allows us to define the static QQbar potential in the medium in real time



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- $T \ll m$
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pNRQCD supply the potential (weak coupling regime $T \gg gT$)

- The thermal part of the potential has a real and an imaginary part

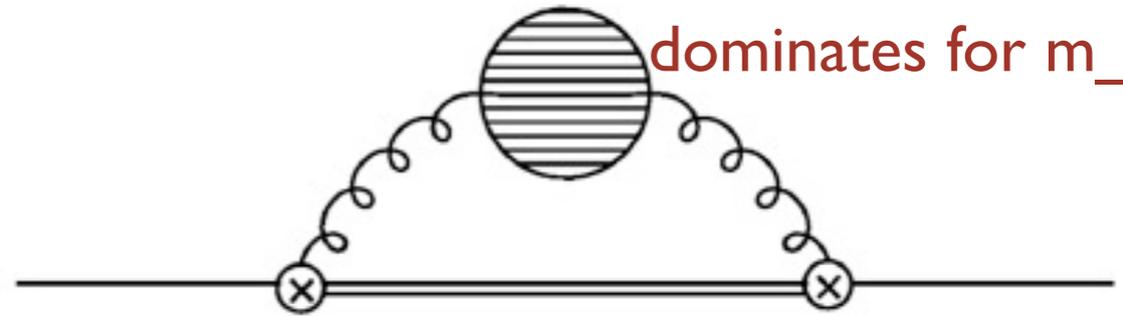
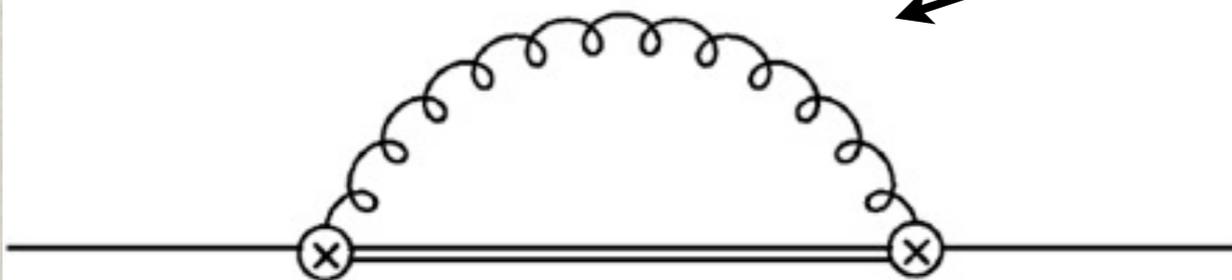
$\text{Re}V_s(r,T)$

$\text{Im}V_s(r,T)$

thermal width of $Q\bar{Q}$

New effect, specific of QCD
dominates for $E/m_D \gg 1$

Known from QED
dominates for $m_D/E \gg 1$



Singlet-to-octet

Landau damping

N.B Ghiglieri, Petreczky, Vairo 2008

Laine et al 07, Escobedo Soto 07

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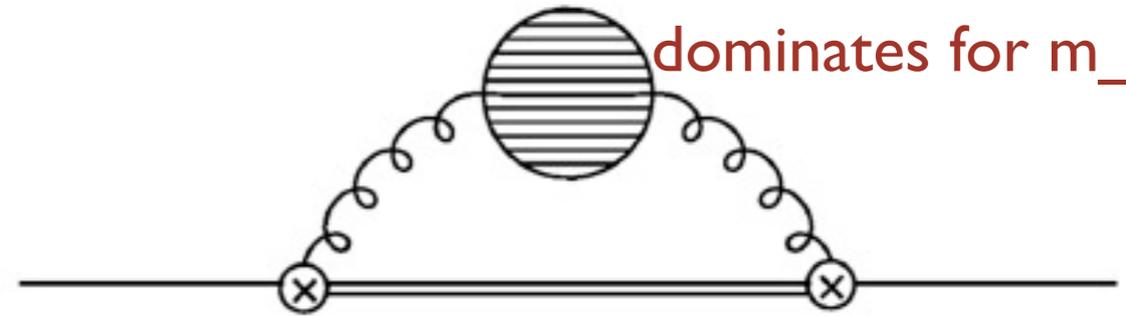
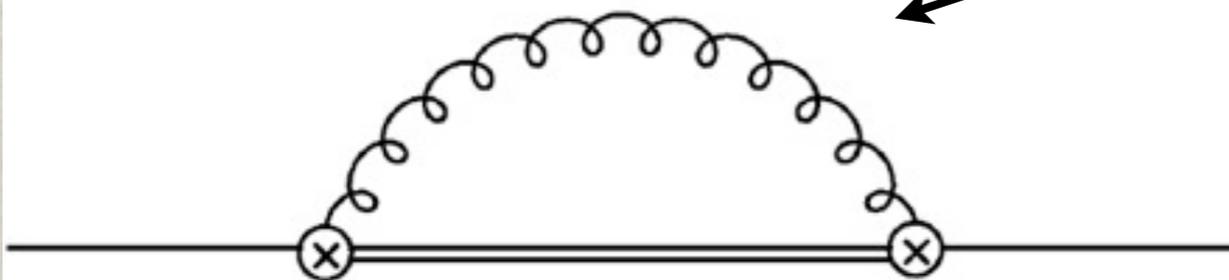
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(gluo dissociation)

N. B. Escobedo, Ghiglieri, Vairo 2011

Landau damping

Laine et al 07, Escobedo Soto 07

(inelastic parton scattering)

N. B. Escobedo, Ghiglieri, Vairo 2013

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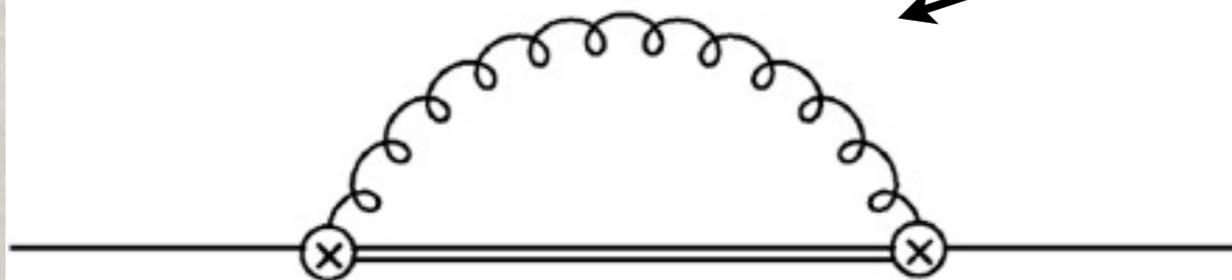
differs from the free energy

N. B., Ghiglieri, Petreczky, Vairo 010

$\text{Im}V_s(r, T)$

thermal width of $Q\bar{Q}$

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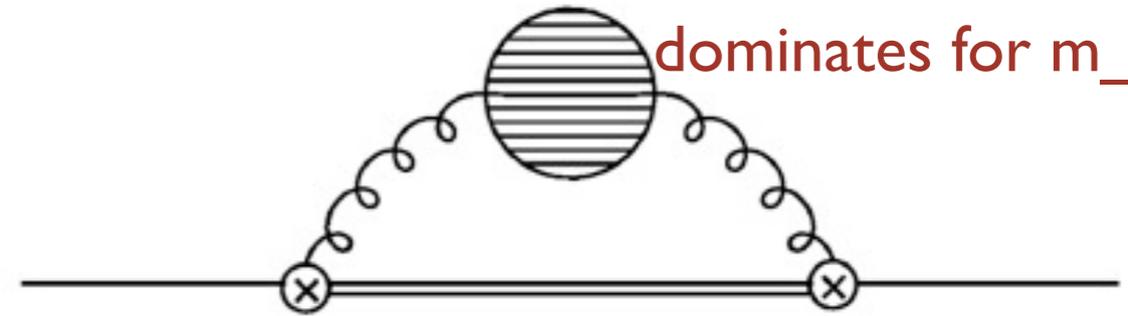
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N. B. Escobedo, Ghiglieri, Vairo 2013

The singlet static potential and the static energy (pNRQCD)

- Temperature effects can be other than screening

$$T > 1/r \text{ and } 1/r \sim m_D \sim gT$$

exponential screening but $\text{Im}V \gg \text{Re}V$

$$T > 1/r \text{ and } 1/r > m_D \sim gT$$

no exponential screening but
power-like T corrections

$$T < E_{\text{bin}}$$

no corrections to the potential,
corrections to the energy

We calculated the potential in the EFT for all the different scales hierarchies. There are preliminary lattice attempts to obtain the static potential

The singlet static potential and the static energy (pNRQCD)

We have calculated the potential for all the situations from T bigger than the inverse radius $1/r$ to smaller than the energy E

N.B., Ghiglieri,
Petreczsky, Vairo

The imaginary part is bigger than the real part before the screening $\exp\{-m_D r\}$ sets in

->the imaginary part is responsible for $QQ\bar{q}$ dissociation !

$T \gg 1/r \gg m_D \gg V$: Quarkonium melts in the medium

$$E_{\text{binding}} \sim \Gamma$$

$$\pi T_{\text{melting}} \sim m g^{4/3}$$

o Escobedo Soto arXiv:0804.0691

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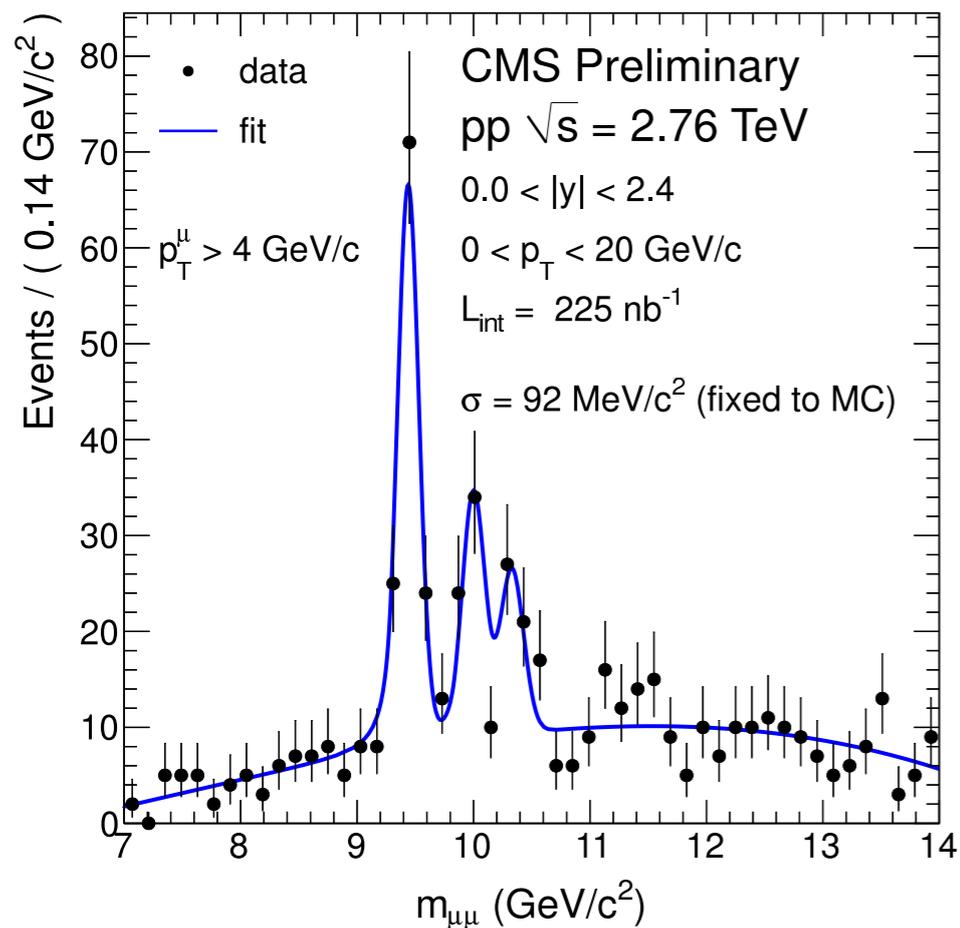
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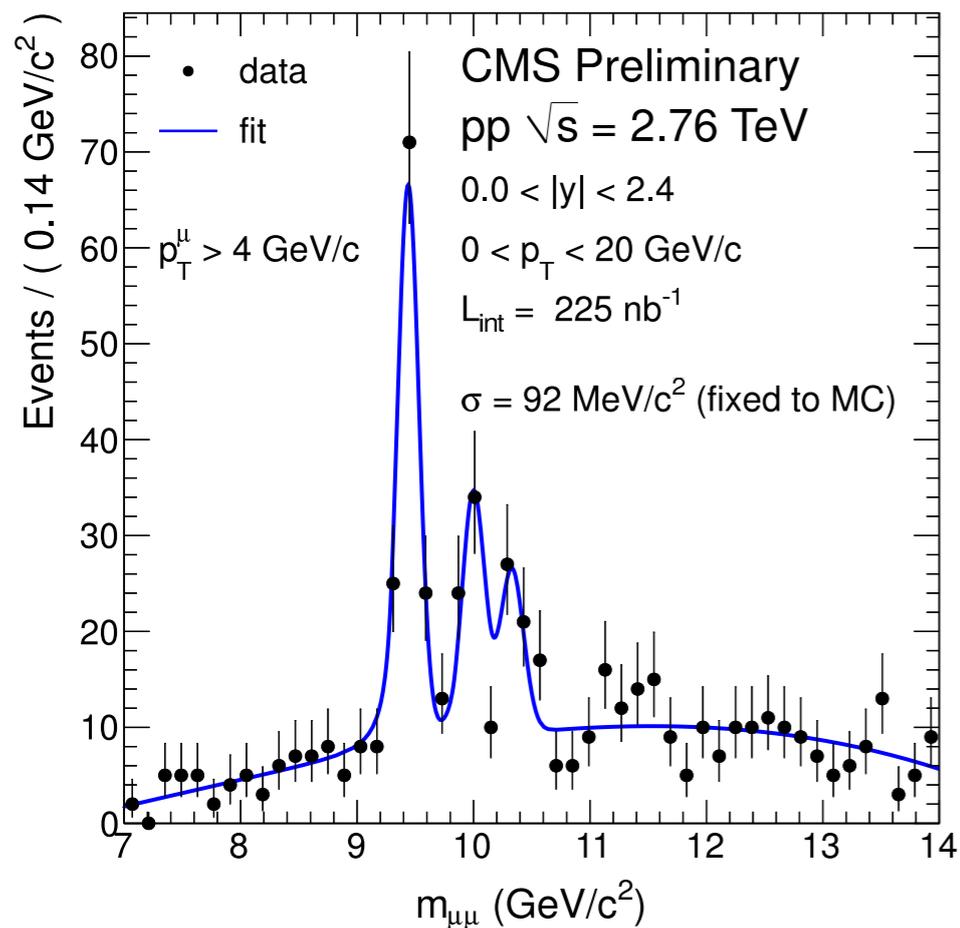
offer a systematic framework to do the calculation for the first time, inspired calculations in lattice, strings ..

The EFT supplies the potential and a scheme to calculate quarkonium energy levels at finite T



application to the study of
Y(1S) in hot medium at
LHC experiments
below the melting temperature T_d

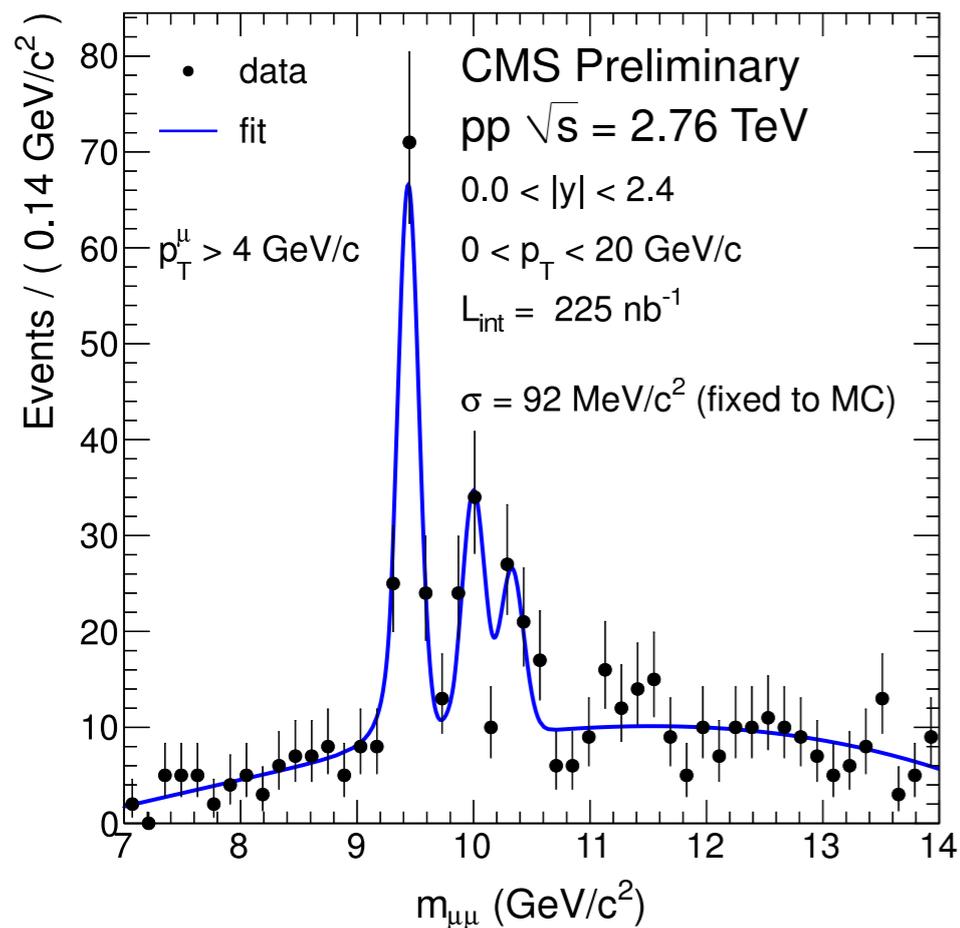
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The relative size of non-relativistic and thermal scales depends on the medium and on the quarkonium state.

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application to the study of
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 LHC experiments
 below the melting temperature T_d

The relative size of non-relativistic and thermal scales depends on the medium and on the quarkonium state.

The **bottomonium ground state**, which is a weakly coupled non-relativistic bound state: $mv \sim m\alpha_s$, $mv^2 \sim m\alpha_s^2 \gtrsim \Lambda_{\text{QCD}}$, produced in the QCD medium of heavy-ion collisions at the LHC may possibly realize the hierarchy

$$m \approx 5 \text{ GeV} > m\alpha_s \approx 1.5 \text{ GeV} > \pi T \approx 1 \text{ GeV} > m\alpha_s^2 \approx 0.5 \text{ GeV} \gtrsim m_D, \Lambda_{\text{QCD}}$$

case of interest for LHC: bottomonium 1S below the melting temperature T_d

The complete mass and width up to $\mathcal{O}(m\alpha_s^5)$

$$\delta E_{1S}^{(\text{thermal})} = \frac{34\pi}{27} \alpha_s^2 T^2 a_0 + \frac{7225}{324} \frac{E_1 \alpha_s^3}{\pi} \left[\ln \left(\frac{2\pi T}{E_1} \right)^2 - 2\gamma_E \right] + \frac{128 E_1 \alpha_s^3}{81\pi} L_{1,0} - 3a_0^2 \left\{ \left[\frac{6}{\pi} \zeta(3) + \frac{4\pi}{3} \right] \alpha_s T m_D^2 - \frac{8}{3} \zeta(3) \alpha_s^2 T^3 \right\}$$

$$\Gamma_{1S}^{(\text{thermal})} = \frac{1156}{81} \alpha_s^3 T + \frac{7225}{162} E_1 \alpha_s^3 + \frac{32}{9} \alpha_s T m_D^2 a_0^2 I_{1,0} - \left[\frac{4}{3} \alpha_s T m_D^2 \left(\ln \frac{E_1^2}{T^2} + 2\gamma_E - 3 - \ln 4 - 2 \frac{\zeta'(2)}{\zeta(2)} \right) + \frac{32\pi}{3} \ln 2 \alpha_s^2 T^3 \right] a_0^2$$

where $E_1 = -\frac{4m\alpha_s^2}{9}$, $a_0 = \frac{3}{2m\alpha_s}$ and $L_{1,0}$ (similar $I_{1,0}$) is the Bethe logarithm.

◦ Brambilla Escobedo Ghiglieri Soto Vairo JHEP 1009 (2010) 038

Consistent with lattice calculations of spectral functions

◦ Aarts Allton Kim Lombardo Oktay Ryan Sinclair Skullerud
JHEP 1111 (2011) 103

Quarkonium systems close or
above

threshold

no gap: close and above threshold

Λ_{QCD}

Quarkonium systems close or
above

threshold

no gap: close and above threshold

Λ_{QCD}

Important to understand the
X, Y, Z puzzles of the dozen of
unexpected states showing up
at the LHC and other collider
experiments

TABLE 12: Quarkonium-like states above the corresponding open flavor thresholds. For charged states, the C -parity is given for the neutral members of the corresponding isotriplets.

State	M , MeV	Γ , MeV	J^{PC}	Process (mode)	Experiment ($\#\sigma$)	Year	Status
$Y(3915)$	3918.4 ± 1.9	20 ± 5	$0/2^{?+}$	$B \rightarrow K(\omega J/\psi)$ $e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle [1050] (8), BaBar [1000, 1051] (19) Belle [1052] (7.7), BaBar [1053] (7.6)	2004 2009	Ok Ok
$\chi_{c2}(2P)$	3927.2 ± 2.6	24 ± 6	2^{++}	$e^+e^- \rightarrow e^+e^-(D\bar{D})$	Belle [1054] (5.3), BaBar [1055] (5.8)	2005	Ok
$X(3940)$	3942_{-8}^{+9}	37_{-17}^{+27}	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D\bar{D}^*)$	Belle [1048, 1049] (6)	2005	NC!
$Y(4008)$	3891 ± 42	255 ± 42	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^- J/\psi)$	Belle [1008, 1056] (7.4)	2007	NC!
$\psi(4040)$	4039 ± 1	80 ± 10	1^{--}	$e^+e^- \rightarrow (D^{(*)}\bar{D}^{(*)}(\pi))$ $e^+e^- \rightarrow (\eta J/\psi)$	PDG [1] Belle [1057] (6.0)	1978 2013	Ok NC!
$Z(4050)^+$	4051_{-43}^{+24}	82_{-55}^{+51}	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+\chi_{c1})$	Belle [1058] (5.0), BaBar [1059] (1.1)	2008	NC!
$Y(4140)$	4145.8 ± 2.6	18 ± 8	$?^{?+}$	$B^+ \rightarrow K^+(\phi J/\psi)$	CDF [1060] (5.0), Belle [1061] (1.9), LHCb [1062] (1.4), CMS [1063] (>5) D0 [1064] (3.1)	2009	NC!
$\psi(4160)$	4153 ± 3	103 ± 8	1^{--}	$e^+e^- \rightarrow (D^{(*)}\bar{D}^{(*)})$ $e^+e^- \rightarrow (\eta J/\psi)$	PDG [1] Belle [1057] (6.5)	1978 2013	Ok NC!
$X(4160)$	4156_{-25}^{+29}	139_{-65}^{+113}	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D^*\bar{D}^*)$	Belle [1049] (5.5)	2007	NC!
$Z(4200)^+$	4196_{-30}^{+35}	370_{-110}^{+99}	1^{+-}	$\bar{B}^0 \rightarrow K^-(\pi^+ J/\psi)$	Belle [1065] (7.2)	2014	NC!
$Z(4250)^+$	4248_{-45}^{+185}	177_{-72}^{+321}	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+\chi_{c1})$	Belle [1058] (5.0), BaBar [1059] (2.0)	2008	NC!
$Y(4260)$	4250 ± 9	108 ± 12	1^{--}	$e^+e^- \rightarrow (\pi\pi J/\psi)$ $e^+e^- \rightarrow (f_0(980)J/\psi)$ $e^+e^- \rightarrow (\pi^- Z_c(3900)^+)$ $e^+e^- \rightarrow (\gamma X(3872))$	BaBar [1066, 1067] (8), CLEO [1068, 1069] (11) Belle [1008, 1056] (15), BES III [1007] (np) BaBar [1067] (np), Belle [1008] (np) BES III [1007] (8), Belle [1008] (5.2) BES III [1070] (5.3)	2005 2012 2013 2013	Ok Ok Ok NC!
$Y(4274)$	4293 ± 20	35 ± 16	$?^{?+}$	$B^+ \rightarrow K^+(\phi J/\psi)$	CDF [1060] (3.1), LHCb [1062] (1.0), CMS [1063] (>3), D0 [1064] (np)	2011	NC!
$X(4350)$	$4350.6_{-5.1}^{+4.6}$	13_{-10}^{+18}	$0/2^{?+}$	$e^+e^- \rightarrow e^+e^-(\phi J/\psi)$	Belle [1071] (3.2)	2009	NC!
$Y(4360)$	4354 ± 11	78 ± 16	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	Belle [1072] (8), BaBar [1073] (np)	2007	Ok
$Z(4430)^+$	4458 ± 15	166_{-32}^{+37}	1^{+-}	$\bar{B}^0 \rightarrow K^-(\pi^+\psi(2S))$ $\bar{B}^0 \rightarrow K^-(\pi^+ J/\psi)$	Belle [1074, 1075] (6.4), BaBar [1076] (2.4) LHCb [1077] (13.9) Belle [1065] (4.0)	2007 2014	Ok NC!
$X(4630)$	4634_{-11}^{+9}	92_{-32}^{+41}	1^{--}	$e^+e^- \rightarrow (\Lambda_c^+\bar{\Lambda}_c^-)$	Belle [1078] (8.2)	2007	NC!
$Y(4660)$	4665 ± 10	53 ± 14	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	Belle [1072] (5.8), BaBar [1073] (5)	2007	Ok
$\Upsilon(10860)$	10876 ± 11	55 ± 28	1^{--}	$e^+e^- \rightarrow (B_{(s)}^{(*)}\bar{B}_{(s)}^{(*)}(\pi))$ $e^+e^- \rightarrow (\pi\pi\Upsilon(1S, 2S, 3S))$ $e^+e^- \rightarrow (f_0(980)\Upsilon(1S))$ $e^+e^- \rightarrow (\pi Z_b(10610, 10650))$ $e^+e^- \rightarrow (\eta\Upsilon(1S, 2S))$ $e^+e^- \rightarrow (\pi^+\pi^-\Upsilon(1D))$	PDG [1] Belle [1013, 1014, 1079] (>10) Belle [1013, 1014] (>5) Belle [1013, 1014] (>10) Belle [948] (10) Belle [948] (9)	1985 2007 2011 2011 2012 2012	Ok Ok Ok Ok Ok Ok
$Y_b(10888)$	10888.4 ± 3.0	$30.7_{-7.7}^{+8.9}$	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^-\Upsilon(nS))$	Belle [1080] (2.3)	2008	NC!

TABLE 10: Quarkonium-like states at the open flavor thresholds. For charged states, the C -parity is given for the neutral members of the corresponding isotriplets.

State	M , MeV	Γ , MeV	J^{PC}	Process (mode)	Experiment ($\#\sigma$)	Year	Status
$X(3872)$	3871.68 ± 0.17	< 1.2	1^{++}	$B \rightarrow K(\pi^+\pi^-J/\psi)$	Belle [772, 992] (>10), BaBar [993] (8.6)	2003	Ok
				$p\bar{p} \rightarrow (\pi^+\pi^-J/\psi) \dots$	CDF [994, 995] (11.6), D0 [996] (5.2)	2003	Ok
				$pp \rightarrow (\pi^+\pi^-J/\psi) \dots$	LHCb [997, 998] (np)	2012	Ok
				$B \rightarrow K(\pi^+\pi^-\pi^0J/\psi)$	Belle [999] (4.3), BaBar [1000] (4.0)	2005	Ok
				$B \rightarrow K(\gamma J/\psi)$	Belle [1001] (5.5), BaBar [1002] (3.5)	2005	Ok
				$B \rightarrow K(\gamma\psi(2S))$	LHCb [1003] (> 10)		
				$B \rightarrow K(\gamma\psi(2S))$	BaBar [1002] (3.6), Belle [1001] (0.2)	2008	NC!
				$B \rightarrow K(D\bar{D}^*)$	LHCb [1003] (4.4)		
$Z_c(3885)^+$	3883.9 ± 4.5	25 ± 12	1^{+-}	$Y(4260) \rightarrow \pi^-(D\bar{D}^*)^+$	Belle [1004] (6.4), BaBar [1005] (4.9)	2006	Ok
$Z_c(3900)^+$	3891.2 ± 3.3	40 ± 8	$?^{?-}$	$Y(4260) \rightarrow \pi^-(\pi^+J/\psi)$	BES III [1006] (np)	2013	NC!
					BES III [1007] (8), Belle [1008] (5.2)	2013	Ok
					T. Xiao <i>et al.</i> [CLEO data] [1009] (>5)		
$Z_c(4020)^+$	4022.9 ± 2.8	7.9 ± 3.7	$?^{?-}$	$Y(4260, 4360) \rightarrow \pi^-(\pi^+h_c)$	BES III [1010] (8.9)	2013	NC!
$Z_c(4025)^+$	4026.3 ± 4.5	24.8 ± 9.5	$?^{?-}$	$Y(4260) \rightarrow \pi^-(D^*\bar{D}^*)^+$	BES III [1011] (10)	2013	NC!
$Z_b(10610)^+$	10607.2 ± 2.0	18.4 ± 2.4	1^{+-}	$\Upsilon(10860) \rightarrow \pi(\pi\Upsilon(1S, 2S, 3S))$	Belle [1012–1014] (>10)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(\pi^+h_b(1P, 2P))$	Belle [1013] (16)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(B\bar{B}^*)^+$	Belle [1015] (8)	2012	NC!
$Z_b(10650)^+$	10652.2 ± 1.5	11.5 ± 2.2	1^{+-}	$\Upsilon(10860) \rightarrow \pi^-(\pi^+\Upsilon(1S, 2S, 3S))$	Belle [1012, 1013] (>10)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(\pi^+h_b(1P, 2P))$	Belle [1013] (16)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(B^*\bar{B}^*)^+$	Belle [1015] (6.8)	2012	NC!

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				$pp \rightarrow (\pi^+\pi^-J/\psi) \dots$	LHCb [997, 998] (np)	2012	Ok
				$B \rightarrow K(\pi^+\pi^-\pi^0J/\psi)$	Belle [999] (4.3), BaBar [1000] (4.0)	2005	Ok
				$B \rightarrow K(\gamma J/\psi)$	Belle [1001] (5.5), BaBar [1002] (3.5)	2005	Ok
				$B \rightarrow K(\gamma\psi(2S))$	LHCb [1003] (> 10)		
				$B \rightarrow K(D\bar{D}^*)$	BaBar [1002] (3.6), Belle [1001] (0.2)	2008	NC!
				$B \rightarrow K(D\bar{D}^*)$	LHCb [1003] (4.4)		
$Z_c(3885)^+$	3883.9 ± 4.5	25 ± 12	1^{+-}	$Y(4260) \rightarrow \pi^-(D\bar{D}^*)^+$	Belle [1004] (6.4), BaBar [1005] (4.9)	2006	Ok
$Z_c(3900)^+$	3891.2 ± 3.3	40 ± 8	$?^{? -}$	$Y(4260) \rightarrow \pi^-(\pi^+J/\psi)$	BES III [1006] (np)	2013	NC!
					BES III [1007] (8), Belle [1008] (5.2)	2013	Ok
					T. Xiao <i>et al.</i> [CLEO data] [1009] (>5)		
$Z_c(4020)^+$	4022.9 ± 2.8	7.9 ± 3.7	$?^{? -}$	$Y(4260, 4360) \rightarrow \pi^-(\pi^+h_c)$	BES III [1010] (8.9)	2013	NC!
$Z_c(4025)^+$	4026.3 ± 4.5	24.8 ± 9.5	$?^{? -}$	$Y(4260) \rightarrow \pi^-(D^*\bar{D}^*)^+$	BES III [1011] (10)	2013	NC!
$Z_b(10610)^+$	10607.2 ± 2.0	18.4 ± 2.4	1^{+-}	$\Upsilon(10860) \rightarrow \pi(\pi\Upsilon(1S, 2S, 3S))$	Belle [1012–1014] (>10)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(\pi^+h_b(1P, 2P))$	Belle [1013] (16)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(B\bar{B}^*)^+$	Belle [1015] (8)	2012	NC!
$Z_b(10650)^+$	10652.2 ± 1.5	11.5 ± 2.2	1^{+-}	$\Upsilon(10860) \rightarrow \pi^-(\pi^+\Upsilon(1S, 2S, 3S))$	Belle [1012, 1013] (>10)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(\pi^+h_b(1P, 2P))$	Belle [1013] (16)	2011	Ok
				$\Upsilon(10860) \rightarrow \pi^-(B^*\bar{B}^*)^+$	Belle [1015] (6.8)	2012	NC!

Near threshold heavy-light mesons have to be included and many additional degrees of freedom considered

No systematic treatment is available; lattice calculations are also challenging and in the infancy state in this case

We need a description of states close or above threshold from

QCD

Already the case of QCD without light quark is very interesting. The degrees of freedom are heavy quarkonium, heavy hybrids and glueballs

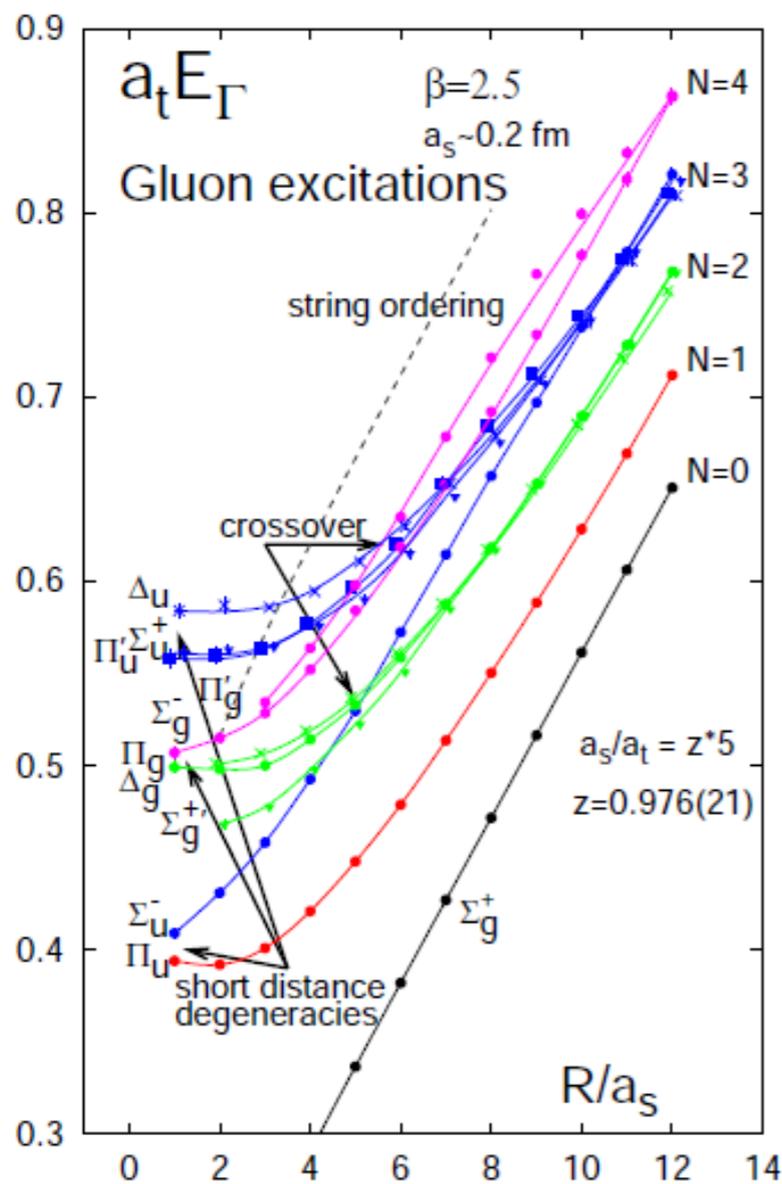
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Static

Lattice energies

Juge Kuti Morningstar 2003

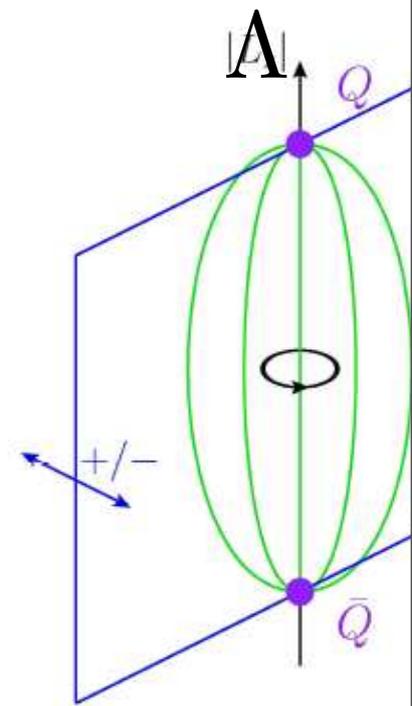


Symmetries

Static states classified by symmetry group $D_{\infty h}$
 Representations labeled Λ_{η}^{σ}

- ▶ Λ rotational quantum number
 $|\hat{n} \cdot \mathbf{K}| = 0, 1, 2 \dots$ corresponds to
 $\Lambda = \Sigma, \Pi, \Delta \dots$
- ▶ η eigenvalue of CP :
 $g \hat{=} +1$ (gerade), $u \hat{=} -1$ (ungerade)
- ▶ σ eigenvalue of reflections
- ▶ σ label only displayed on Σ states
 (others are degenerate)

- The static energies correspond to the irreducible representations of $D_{\infty h}$
- In general it can be more than one state for each irreducible representation of $D_{\infty h}$, usually denoted by primes, e.g. $\Pi_u, \Pi'_u, \Pi''_u \dots$



We define symmetries and states in NRQCD

We match the energy and the states to pNRQCD at order $1/m$ in the expansion (but no spin for now) and identify coupled Schroedinger equations for Σ_u and Π_u

These are nonperturbative but would require lattice calculations of matrix elements

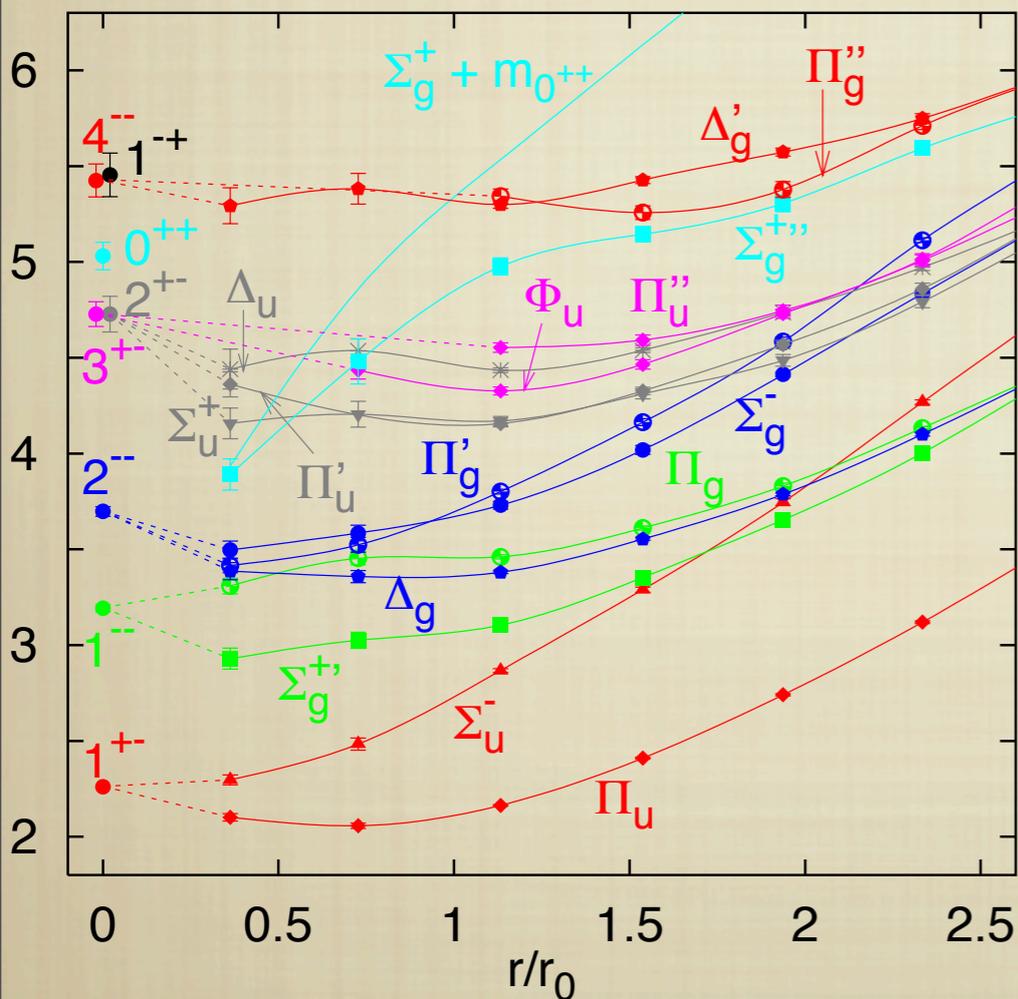
Lacking the lattice calculation, we identify the potentials with a multipole expansion in pNRQCD, solve the coupled equations and get the lowest $c\bar{c}$, $b\bar{b}$ and $b\bar{c}$ multiplets

Gluonic excitations in pNRQCD: one can determine the form of the potential

- At lowest order in the multipole expansion, the *singlet decouples* while the *octet is still coupled to gluons*.

- Static hybrids at short distance are called *gluelumps* and are described by a *static adjoint source* (O) in the presence of a *gluonic field* (H):

$$H(R, r, t) = \text{Tr}\{OH\}$$



$$\begin{array}{c}
 H \quad \quad \quad H \\
 \bullet \text{---} \text{---} \bullet = e^{-iT E_H} \\
 E_H = V_o + \frac{i}{T} \ln \langle H^a(\frac{T}{2}) \phi_{ab}^{\text{adj}} H^b(-\frac{T}{2}) \rangle
 \end{array}$$

$$\langle H^a(\frac{T}{2}) \phi_{ab}^{\text{adj}} H^b(-\frac{T}{2}) \rangle_{\text{np}} \sim h e^{-iT \Lambda_H}$$

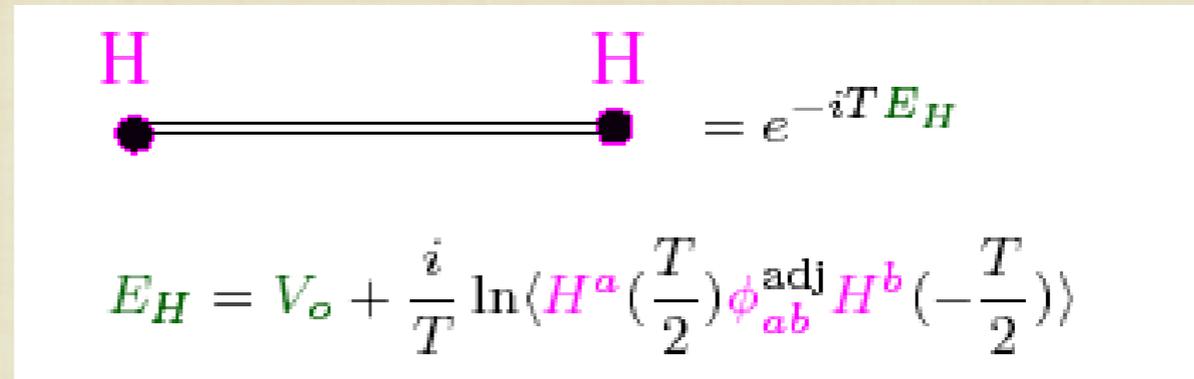
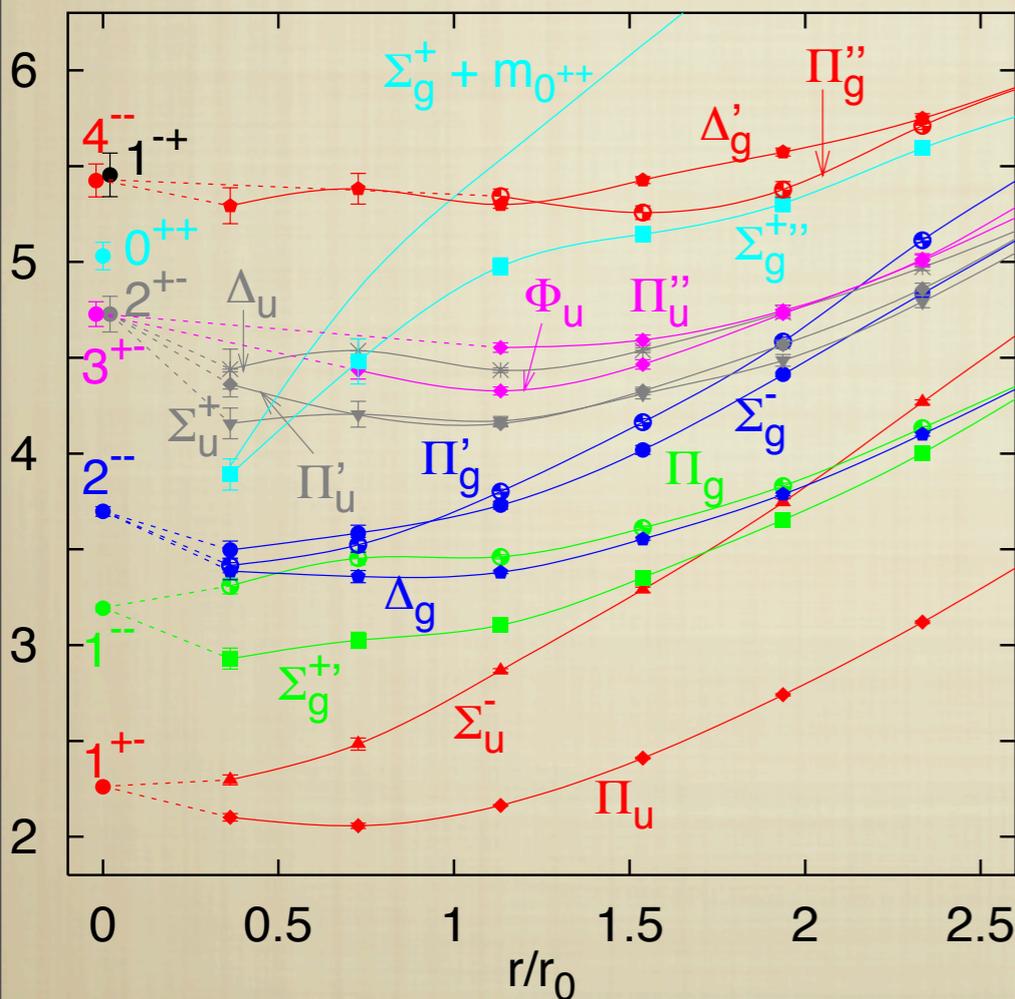
$$E_H(r) = V_o(r) + \Lambda_H + O(r^2)$$

Gluonic excitations in pNRQCD: one can determine the form of the potential

- At lowest order in the multipole expansion, the **singlet decouples** while the **octet is still coupled to gluons**.

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$$H(R, r, t) = \text{Tr}\{OH\}$$



$$\langle H^a(\frac{T}{2}) \phi_{ab}^{adj} H^b(-\frac{T}{2}) \rangle^{np} \sim h e^{-iT\Lambda_H}$$

$$E_H(r) = V_o(r) + \Lambda_H + O(r^2)$$

octet potential
gluelump mass
correction softly breaking the symmetry

Lowest energy multiplet $\Sigma_u^- - \Pi_u$

- ▶ The two lowest lying hybrid static energies are Π_u and Σ_u^- .
- ▶ They are generated by a gluelump with quantum numbers 1^{+-} and thus are degenerate at short distances.
- ▶ The kinetic operator mixes them but not with other multiplets.
- ▶ Well separated by a gap of ~ 1 GeV from the next multiplet with the same CP.

$$V_H = V_o + \Lambda_H + b_H r^2$$

Λ_H and b_H are nonperturbative and should be obtained from lattice calculations

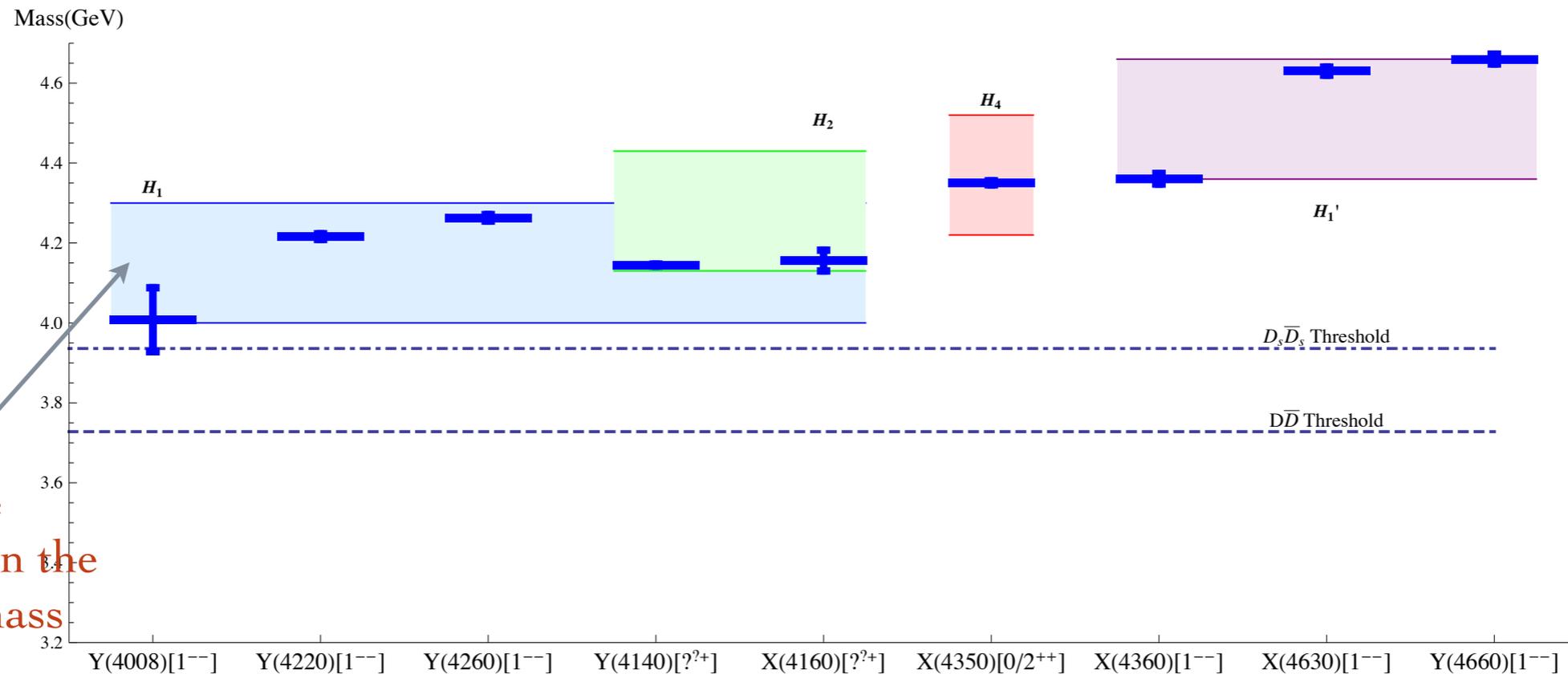
	l	$J^{PC} \{s = 0, s = 1\}$	$E_n^{(0)}$
H_1	1	$\{1^{--}, (0, 1, 2)^{-+}\}$	Σ_u^-, Π_u
H_2	1	$\{1^{++}, (0, 1, 2)^{+-}\}$	Π_u
H_3	0	$\{0^{++}, 1^{+-}\}$	Σ_u^-
H_4	2	$\{2^{++}, (1, 2, 3)^{+-}\}$	Σ_u^-, Π_u
H_5	2	$\{2^{--}, (1, 2, 3)^{-+}\}$	Π_u

TABLE II. J^{PC} multiplets with $l \leq 2$ for the Σ_u^- and Π_u gluonic states. We follow the naming notation H_i used in [20, 26], which orders the multiplets from lower to higher mass. The last column shows the gluonic static energies that appear in the Schrödinger equation of the respective

Identification with experimental states

Most of the candidates have 1^{--} or $0^{++}/2^{++}$ since the main observation channels are production by e^+e^- or $\gamma\gamma$ annihilation respectively.

- ▶ Charmonium states (Belle, CDF, BESIII, Babar):



- ▶ Bottomonium states: $Y_b(10890)[1^{--}]$, $m = 10.8884 \pm 3.0$ (Belle). Possible H_1 candidate, $m_{H_1} = 10.79 \pm 0.15$.

However, except for $Y(4220)$, all other candidates observed decay modes violate Heavy Quark Spin Symmetry.

Comparison to direct lattice calculations

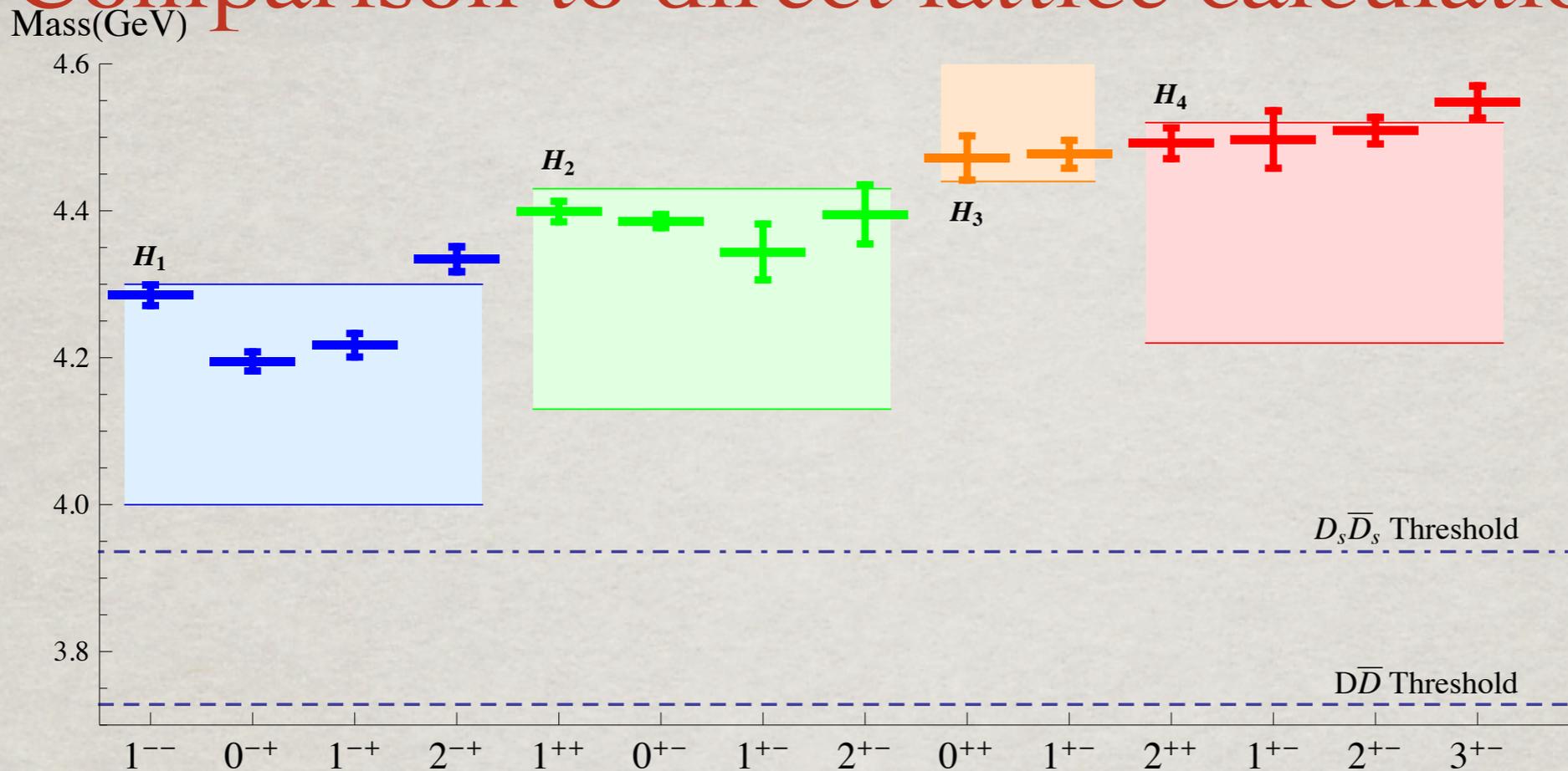


FIG. 5. Comparison of the results from direct lattice computations of the masses for charmonium hybrids [48] with our results using the $V^{(0.25)}$ potential. The direct lattice mass predictions are plotted in solid lines with error bars corresponding to the mass uncertainties. Our results for the H_1 , H_2 , H_3 , and H_4 multiplets have been plotted in error bands corresponding to the gluelump mass uncertainty of ± 0.15 GeV.

We observe the same Lambda-doubling pattern in lattice calculations, multiplets that receive mixed contributions from Σ_u and Π_u have lower masses than those that remain pure Π_u states

Conclusions

Quarkonium is a golden system to study strong interactions

Nonrelativistic Effective Field Theories provide a systematic tool to investigate a wide range of heavy quarkonium observables in the realm of QCD

At $T=0$, away from threshold, EFTs allow us to make calculations with unprecedented precision, where high order perturbative calculations are possible and to systematically factorize short from long range contributions where observables are sensitive to the nonperturbative dynamics of QCD.

Some lattice calculations are still needed (glue correlators, quenched and unquenched Wilson loops with field insertions).

At finite T allow us to give the appropriate definition and define a calculational scheme for quantities of huge phenomenological interest like the $q\bar{q}$ potential and energies at finite T

In the EFT framework heavy quark bound states become a unique laboratory for the study of strong interaction from the high energy to the low energy scales

Outlook

the EFT gives us a definition of physical objects that can then be evaluated with other tools

the EFT gives us a factorization between high energy and low energy contributions: tools to evaluate the nonperturbative physics should be applied only to the low energy part

the EFT approach is very versatile and flexible can be applied to many different problems in

in quarkonium (the low energy part will be typically contained in some type of Wilson loops), in QCD, in QED, in atomic physics, condensed matter, etc..



EU BET

European Bridges with Effective Theories:

from high energy to condensed matter

The intended network brings together leading scientists in the fields of particle, nuclear, atomic, condensed-matter, quantum optics, and computational physics. The resulting group of researchers will have the capacity to address some of the most interesting open physics problems such as, for instance, the understanding of universal features in the equilibrium and transport properties of novel states of matter found in contexts as diverse as graphene, cold atom systems, and the quark-gluon plasma. It will develop needed novel numerical, analytic and computational tools,