

# Soft terms in string models



Michele Cicoli  
Bologna Univ., INFN and ICTP  
Madrid, 29 September 2016



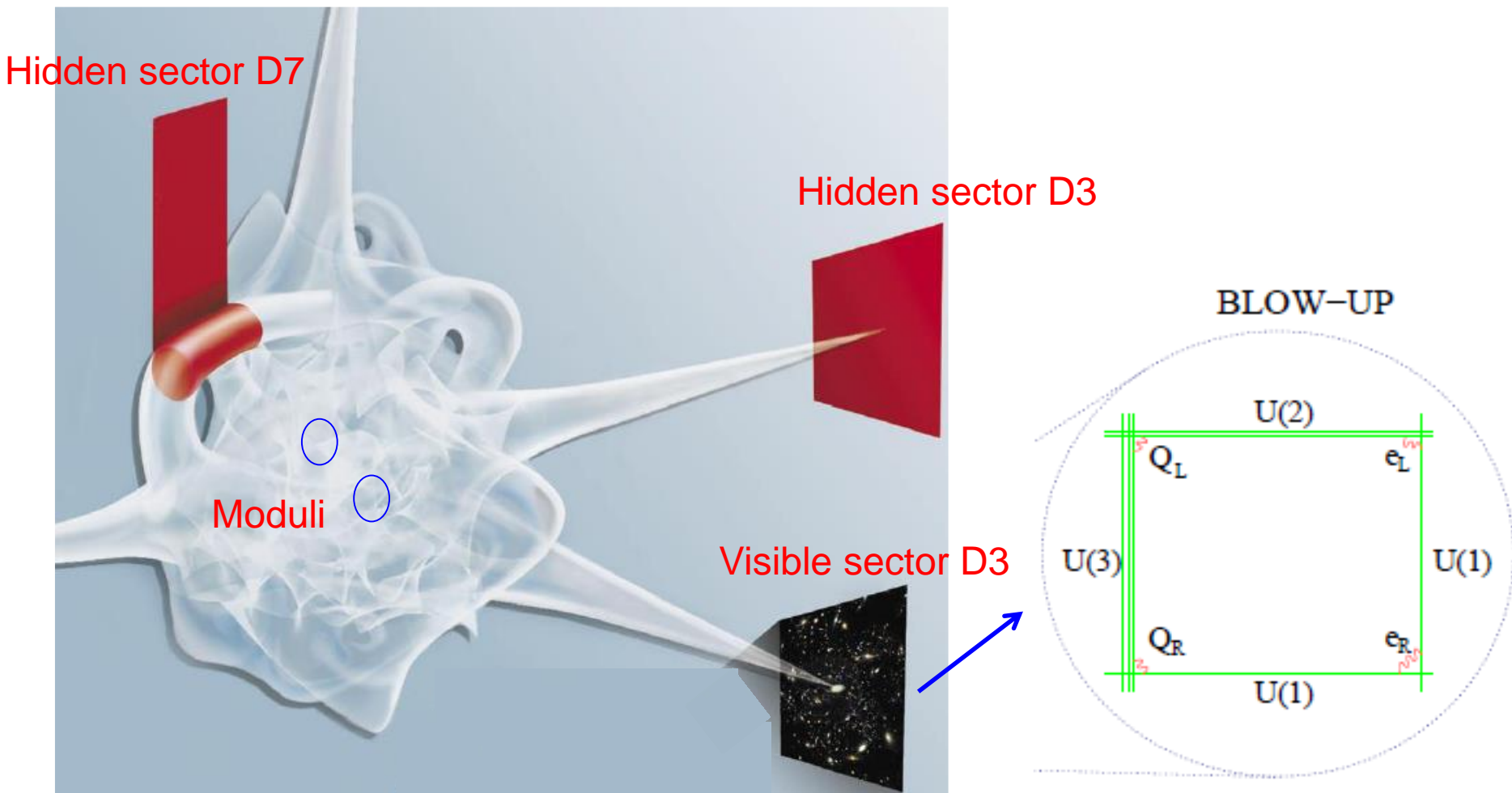
ALMA MATER STUDIORUM  
UNIVERSITÀ DI BOLOGNA

Based on papers written in collaboration with:

Allahverdi, Aparicio, Burgess, Ciupke, Conlon, deAlwis, Dutta, Krippendorf, Maharana, Marsh, Muia, Pedro, Quevedo, Rummel, Valandro

# String models

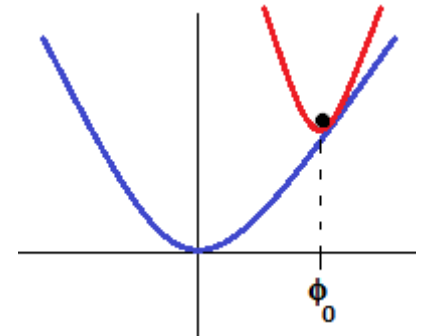
- Ubiquitous presence of geometric **moduli** (closed strings)
- Branes provide **non-Abelian** gauge symmetries and **chiral** matter (open strings)
- Standard Model (or MSSM/GUT theories) **localised** on branes (D3/D7 in type IIB)  
→ model-building is a **local** issue while moduli stabilisation/SUSY breaking is a **global** issue



# Generic problems

- **Cosmological moduli problem** [Coughlan et al] [Banks et al] [de Carlos et al]

- i) During inflation  $\phi$  displaced from  $\phi = 0$  to  $\phi = \phi_0 \sim M_p$
- ii)  $\phi$  starts oscillating when  $H \sim m_\phi \longrightarrow \phi$  stores energy
- iii)  $\phi$  redshifts as matter  $\longrightarrow$  dominates energy density
- iv)  $\phi$  decays when  $H \sim \Gamma \sim \varepsilon^2 m_\phi$  where  $\varepsilon \sim m_\phi / M_p \ll 1$
- v) Reheat temperature  $T_{rh} \sim \varepsilon^{1/2} m_\phi > T_{BBN} \sim 3 \text{ MeV} \longrightarrow m_\phi > 50 \text{ TeV}$



- **Gravitino problem** [Endo,Hamaguchi,Takahashi] [Nakamura, Yamaguchi]

- i) Gravitino production from  $\phi$  decay if  $2m_{3/2} < m_\phi$
- ii) If  $m_{3/2} < 50 \text{ TeV} \longrightarrow$  gravitino decay after BBN/overclosure
- iii) If  $m_{3/2} > 50 \text{ TeV} \longrightarrow$  DM overproduction from gravitino decay/annihilation (unless  $T_{3/2} > T_f$ )

Simplest way-out:  $m_{3/2} > m_\phi > 50 \text{ TeV}$

# Generic problems

- **Generically** in string compactifications:

i) ~~SUSY~~ generates  $m_\phi \sim m_{3/2}$   $\longrightarrow$  can avoid gravitino problem? [KKLT:  $m_{3/2} \sim m_\phi / (16\pi^2)$ ]

ii) Moduli mediate ~~SUSY~~ via gravitational interactions  $\longrightarrow M_{\text{soft}} \sim m_{3/2}$

iii) For  $M_{\text{soft}} \sim m_{3/2} > m_\phi > 50 \text{ TeV}$   $\longrightarrow$  do not get low-energy SUSY!

$\longrightarrow$  neutralino DM and gauge coupling unification do not work!

Way-out:  $M_{\text{soft}} \ll m_{3/2}$  due to **sequestering**

- **Axion DM overproduction** [Preskill et al] [Abbott, Sikivie]

i) O(100) axions in string compactifications

ii) Some projected out, eaten up by anomalous U(1)s or heavy from SUSY stabilisation

iii) Some remain light (perturbative stabilisation)  $\longrightarrow$  one can be QCD axion with  $f_a \sim M_s$

iv) GUTs and inflation need  $M_s \geq 10^{16} \text{ GeV}$   $\longrightarrow$  DM overproduction for  $f_a \sim M_s > 10^{12} \text{ GeV}$

Way-out:  $f_a \ll M_s$  due to **sequestering**

Dimensional reduction:  $m_{3/2} \sim M_s (M_s / M_p) \geq 10^{13} \text{ GeV}$  for  $M_s \geq 10^{16} \text{ GeV}$

$\longrightarrow$  sequestering with more than a loop-factor!

# Light moduli from no-scale

- Light moduli due to **no-scale structure** in type IIB string models:

$$K = -3 \ln(T + \bar{T}) \quad W = W_0$$

$$V = e^K \left( K^{T\bar{T}} D_T W D_{\bar{T}} \bar{W} - 3 |W|^2 \right) = \underbrace{e^K |W_0|^2}_{= m_{3/2}^2} \left( \underbrace{K^{T\bar{T}} K_T K_{\bar{T}} - 3}_{= 0} \right)$$

→ No-scale gives  $m_\phi \sim \varepsilon m_{3/2} \ll m_{3/2}$  → no gravitino problem

$\varepsilon \sim$  size of no-scale breaking effects ( $\alpha'$ , loop or non-perturbative corrections)

- More generically:  $K = -p \ln f(\tau_i) \quad \tau^i f_i = k f \quad \tau^i f_{ij} = (k-1) f_j$

$$K_i = -\frac{p}{f} f_i \quad K_{ij} = -\frac{p}{f} f_{ij} + \frac{p}{f^2} f_i f_j$$

$$\tau^i K_{ij} = -\frac{p}{f} (\tau^i f_{ij}) + \frac{p}{f^2} (\tau^i f_i) f_j = \frac{p}{f} f_j = -K_j$$

$$\tau^k = \tau^i \delta_i^k = \tau^i K_{ij} K^{jk} = -K_j K^{jk}$$

→

$$K_j K^{jk} K_k = -\tau^k K_k = \frac{p}{f} \tau^k f_k = k p$$

- Type IIB:

$$K = -2 \ln \mathcal{V} \quad \mathcal{V} = \frac{k_{ijk}}{3!} t^i t^j t^k \quad \tau_i = \frac{\partial \mathcal{V}}{\partial t^i} = \frac{k_{ijk}}{2!} t^j t^k \quad \rightarrow \quad p = 2 \quad k = \frac{3}{2}$$

# Sequestering from no-scale

- SUSY breaking from non-zero moduli F-terms:

$$F^T = e^{K/2} K^{T\bar{T}} D_{\bar{T}} \bar{W} = e^{K/2} \bar{W} K^{T\bar{T}} K_{\bar{T}} \neq 0$$

- D3 branes at singularities  $\longrightarrow$  locality:

$$\mathcal{K} = -3 \ln(T + \bar{T} - \varphi \bar{\varphi}) = -3 \ln(T + \bar{T}) - 3 \ln\left(1 - \frac{\varphi \bar{\varphi}}{T + \bar{T}}\right)$$

$$\simeq -3 \ln(T + \bar{T}) + 3 \frac{\varphi \bar{\varphi}}{T + \bar{T}} \equiv K + \tilde{K}(T + \bar{T}) \varphi \bar{\varphi} \quad \longrightarrow$$

$$\tilde{K}(T + \bar{T}) = 3 e^{K/3} \quad (*)$$

- Sequestering due to no-scale structure:

$$m_0^2 = m_{3/2}^2 - F^T \bar{F}^{\bar{T}} \partial_T \partial_{\bar{T}} \ln \tilde{K} = m_{3/2}^2 - \frac{1}{3} e^K |W_0|^2 K^{T\bar{T}} K_{\bar{T}} K_T K^{\bar{T}T} K_{T\bar{T}}$$

$$= m_{3/2}^2 \left(1 - \frac{1}{3} K^{T\bar{T}} K_{\bar{T}} K_T\right) = 0$$

No-scale gives  $m_0 \sim \varepsilon m_{3/2} \ll m_{3/2} \longrightarrow$  can have high  $m_{3/2}$  ( $\longrightarrow$  high  $M_s$ ) and low  $m_0$

$\varepsilon \sim$  size of effects breaking (\*) ( $\alpha'$ , loop or non-perturbative corrections)

- More generically:

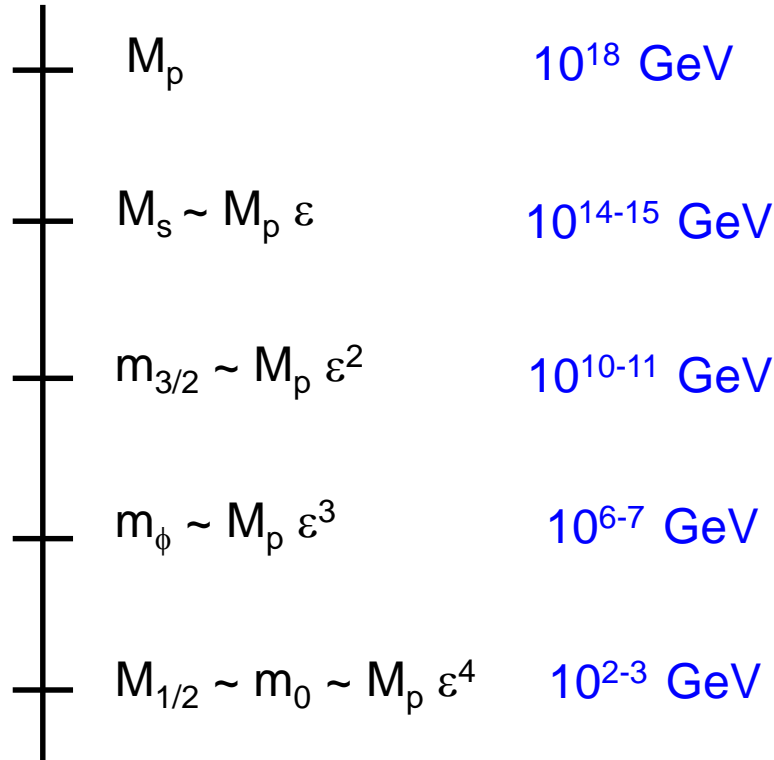
$$\tilde{K} = c e^{K/3}$$

$$\longrightarrow m_0^2 = m_{3/2}^2 - F^i \bar{F}^{\bar{j}} \partial_i \partial_{\bar{j}} \ln \tilde{K} = m_{3/2}^2 - \frac{1}{3} K_{i\bar{j}} F^i \bar{F}^{\bar{j}} = m_{3/2}^2 - \frac{1}{3} (V_0 + 3m_{3/2}^2) = 0$$

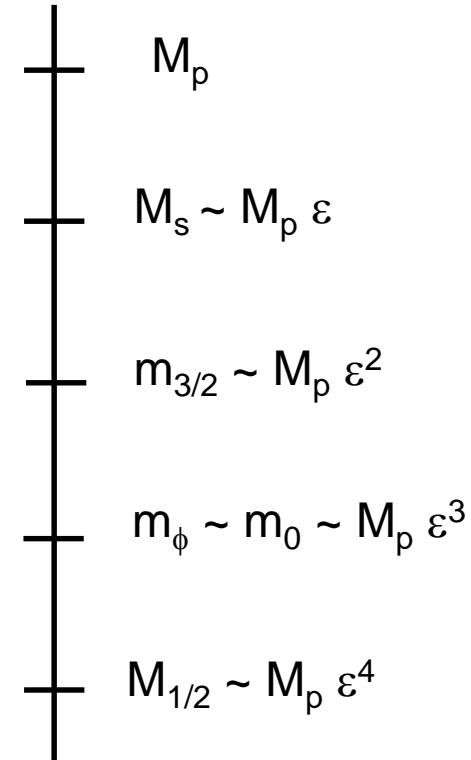
# Mass spectrum

[Aparicio, MC, Krippendorf, Maharana, Muia, Quevedo]  
[Reece, Xue]

## MSSM-like



## Split SUSY-like



Leading order no-scale breaking:  $\alpha'$  effects  $\longrightarrow \epsilon \sim \mathcal{V}^{-1/2} \sim 10^{-3/4}$

Unification scale in D3-brane models:  $M_{\text{GUT}} \sim M_s \epsilon^{-1/3} \sim 10^{16}$  GeV [Conlon, Palti]

No flavour problem (for MSSM-like): flavour and ~~SUSY~~ from two decoupled sectors [Conlon]

# Non-standard post-inflationary cosmology

- Lightest modulus mass:  $m_\phi \sim 10^{6-7} \text{ GeV} \gg 50 \text{ TeV} \longrightarrow T_{\text{rh}} \sim 1 - 10 \text{ GeV}$
- $\phi$  decay dilutes any previous relic: [Moroi,Randall]
- i) Baryon asymmetry  $\longrightarrow$  good if AD baryogenesis is too efficient [Kane,Shao,Watson,Yu] [MC, Muia]
- ii) Standard thermal WIMP DM since  $T_{\text{rh}} < T_f \sim m_{\text{DM}}/20 \sim 10 \text{ GeV} - 100 \text{ GeV}$   
[Allahverdi, Acharya, MC, Dutta, Kane,Kumar,Sinha,Watson]
- Products from  $\phi$  decay:

## i) Non-thermal DM

$$\frac{n_{\text{DM}}}{s} = \left( \frac{n_{\text{DM}}}{s} \right)_{\text{obs}} \frac{\langle \sigma_{\text{ann}} v \rangle_f^{\text{th}} \left( \frac{T_f}{T_{\text{rh}}} \right)}{\langle \sigma_{\text{ann}} v \rangle_f} \quad \text{where} \quad \left( \frac{n_{\text{DM}}}{s} \right)_{\text{obs}} \approx 5 \cdot 10^{-10} \left( \frac{1 \text{ GeV}}{m_{\text{DM}}} \right) \quad \text{and} \quad \langle \sigma_{\text{ann}} v \rangle_f^{\text{th}} \approx 3 \cdot 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

a) Need  $\langle \sigma_{\text{ann}} v \rangle_f = \langle \sigma_{\text{ann}} v \rangle_f^{\text{th}} (T_f / T_{\text{rh}})$

b) Since  $T_{\text{rh}} < T_f \longrightarrow \langle \sigma_{\text{ann}} v \rangle_f > \langle \sigma_{\text{ann}} v \rangle_f^{\text{th}} \longrightarrow$  Higgsino-like DM

c) Bino-like LSP:  $\langle \sigma_{\text{ann}} v \rangle_f < \langle \sigma_{\text{ann}} v \rangle_f^{\text{th}} \longrightarrow$  DM overproduction

## ii) Axionic dark radiation

a) Moduli are gauge singlets  $\longrightarrow$  non-zero branching ratio into hidden fields [MC, Conlon,Quevedo] [Higaki, Takahashi]

b) Light axions **unavoidable** in models with perturbative moduli stabilisation [Allahverdi, MC, Dutta,Sinha]  
 $\longrightarrow \Delta N_{\text{eff}} > 0$  **unavoidable**  $\Delta N_{\text{eff}} \leq 1$  within  $2\sigma$

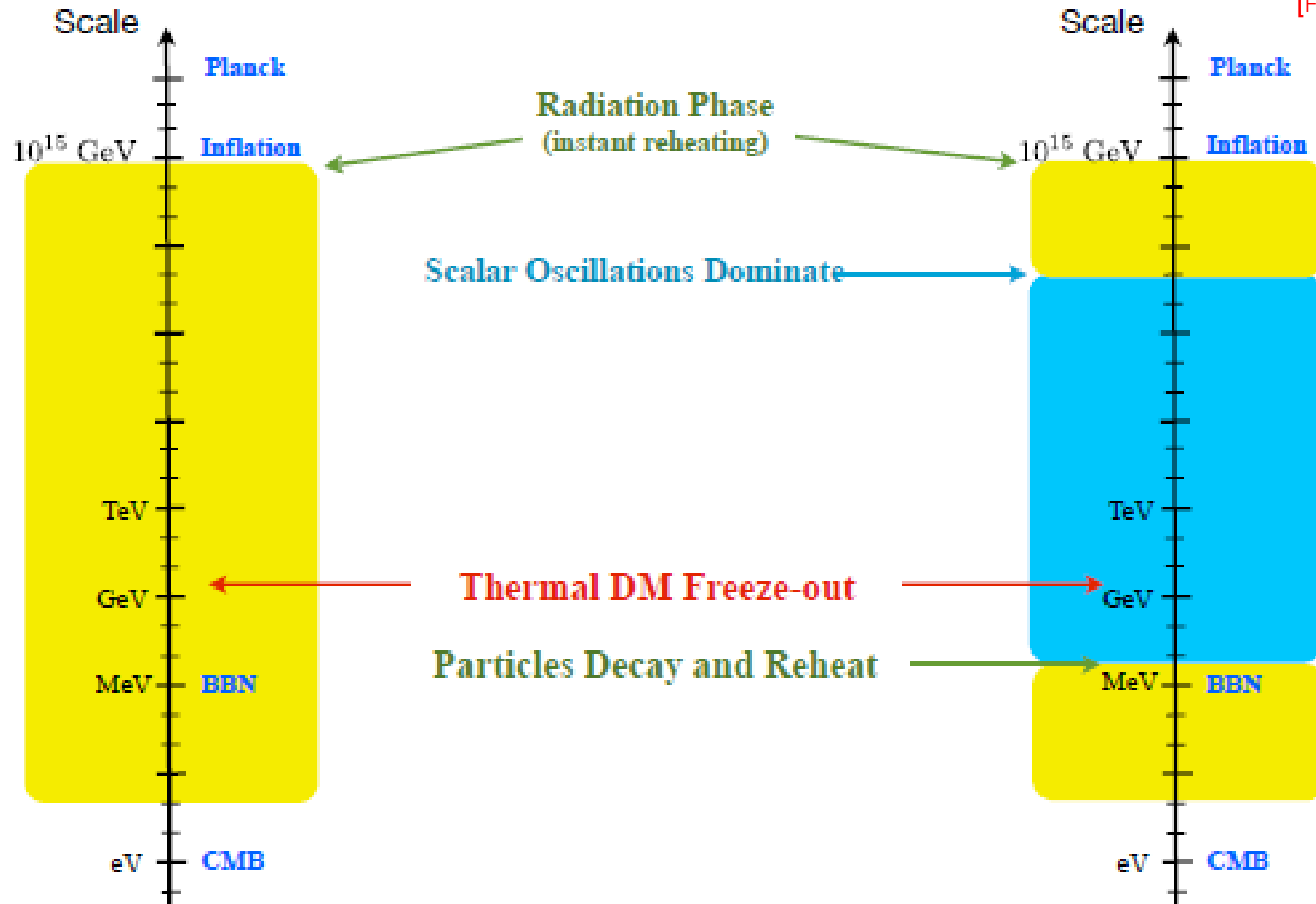


# Thermal vs Non-thermal cosmology

## Thermal History

## Alternative History

[Fig. From S. Watson]



# Non-thermal CMSSM

- Consider CMSSM with non-thermal LSP DM

- Impose:

- i) radiative EWSB + 125 GeV Higgs mass

- ii) no DM overproduction

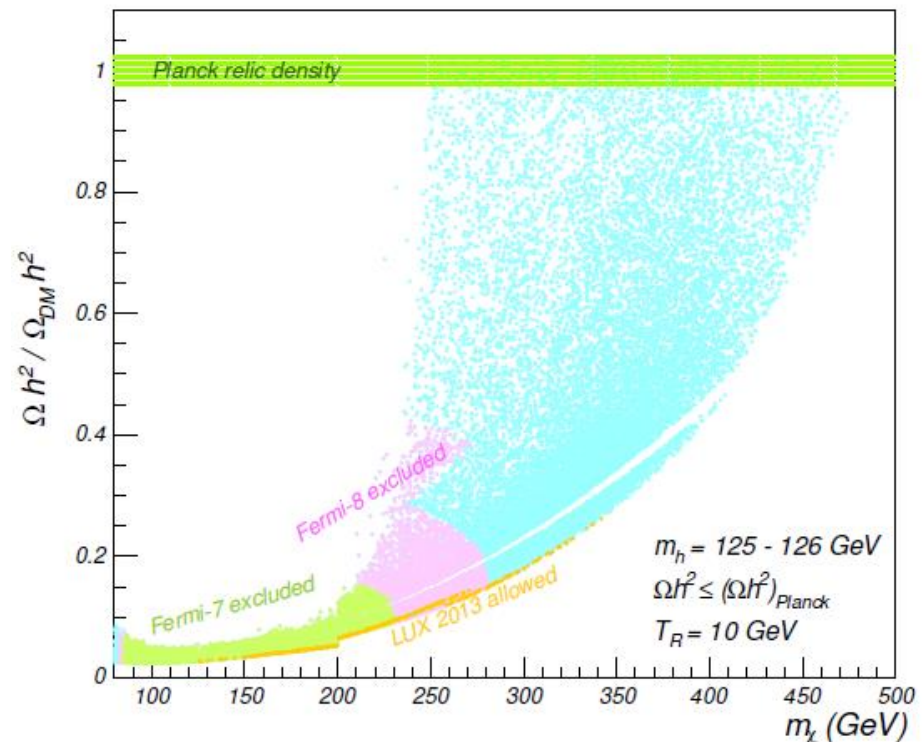
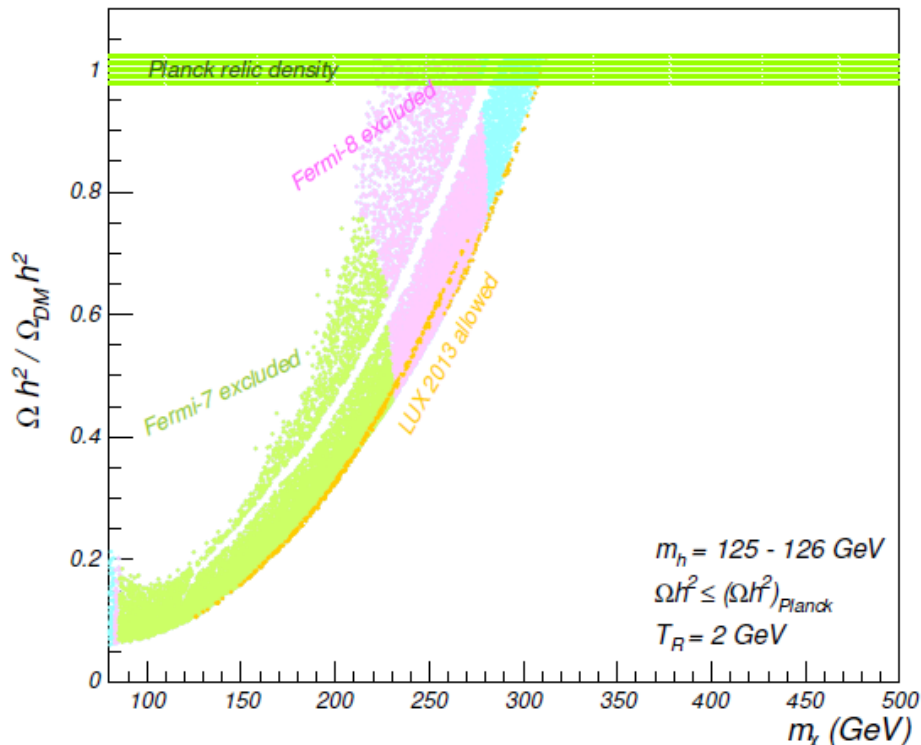
- iii) bounds from colliders (LHC), CMB (Planck), direct (LUX) and indirect (Fermi) DM searches

- a) observed DM content saturated for  $T_{rh} = 2 \text{ GeV}$  and 300 GeV Higgsino LSP

- b) stops around 4-5 TeV, gluinos around 2-3 TeV + light degenerate neutralinos

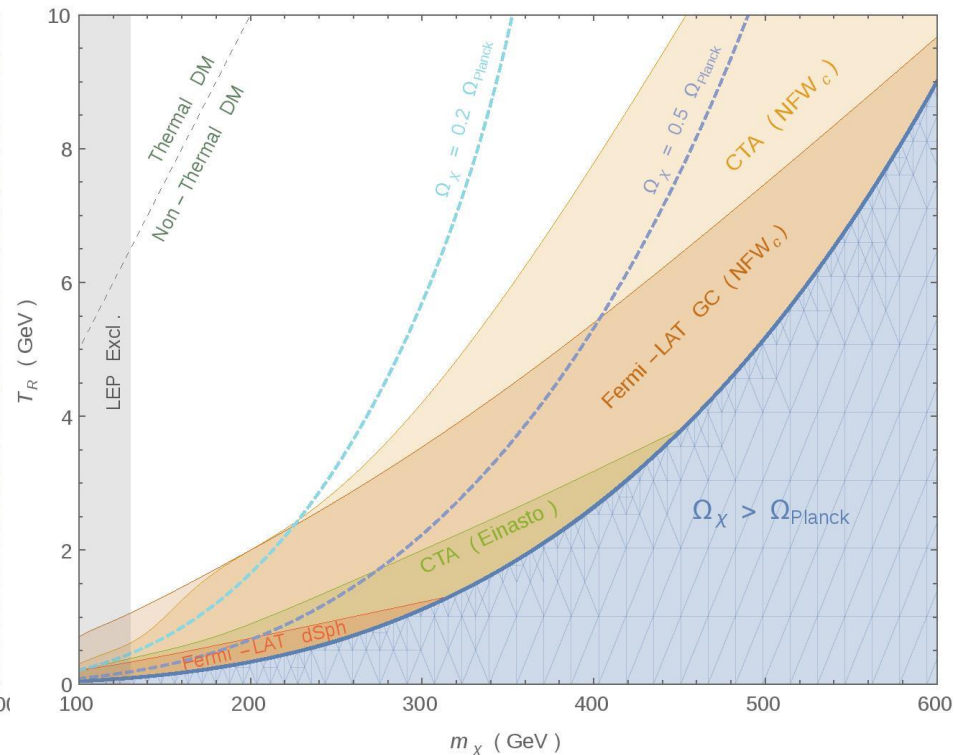
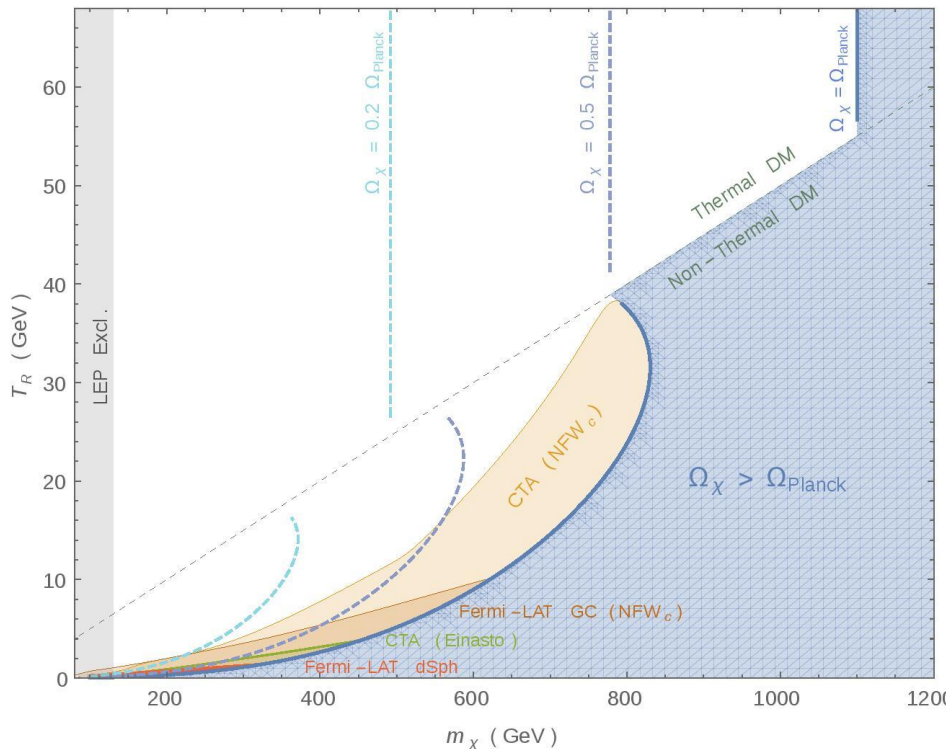
- c) realised in type IIB sequestered string models

[Aparicio,MC,Dutta,Krippendorf,Maharana,Muia,Quevedo]



# Non-thermal Higgsinos

- Model independent analysis of Higgsino LSP (for MSSM, NMSSM, split SUSY, ...)
- Impose (no radiative EWSB and no 125 GeV Higgs mass): [Aparicio,MC,Dutta,,Muia,Quevedo]
- i) no DM overproduction
- ii) bounds from colliders (LHC), CMB (Planck), direct (LUX) and indirect (Fermi) DM searches
  - a) observed DM content saturated for  $T_{rh} = 2-40$  GeV and 300-850 GeV Higgsino LSP
  - b) light degenerate neutralinos/charginos + rest heavier (model dependent)
  - c) collider signature: monojet + missing energy + soft leptons  
 LHC14:  $\mu < 200$  GeV (at  $5\sigma$ ) [Baer, Mustafayev, Tata] 100 TeV machine:  $\mu < 850$  GeV [Low, Wang]
  - d) realised in type IIB sequestered string models



# Dark radiation production

$$T_\gamma \approx T_{rh} \approx m_\phi \sqrt{m_\phi / M_P}$$

Decay of inflaton

$\Phi$

$$E_a = m_\phi / 2$$

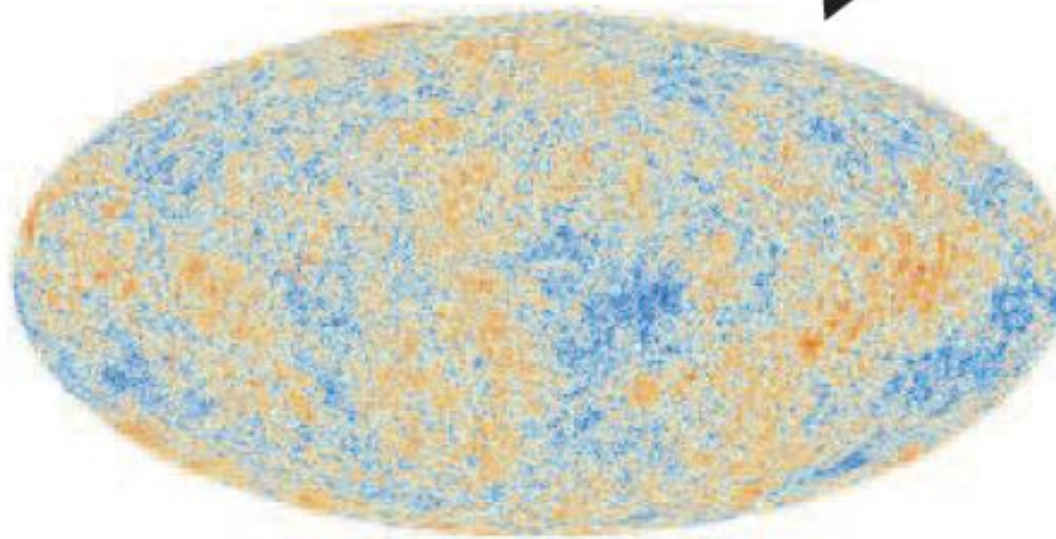
$$\frac{E_a}{T_\gamma} \approx \sqrt{\frac{M_P}{m_\phi}} \approx 10^6 \left( \frac{10^6 \text{ GeV}}{m_\phi} \right)^{1/2}$$

gg, qq, e+ e-, .....

VISIBLE SECTOR  
REHEATING

aa

DARK RADIATION



Free streaming

Ratio of energies retained through cosmic history

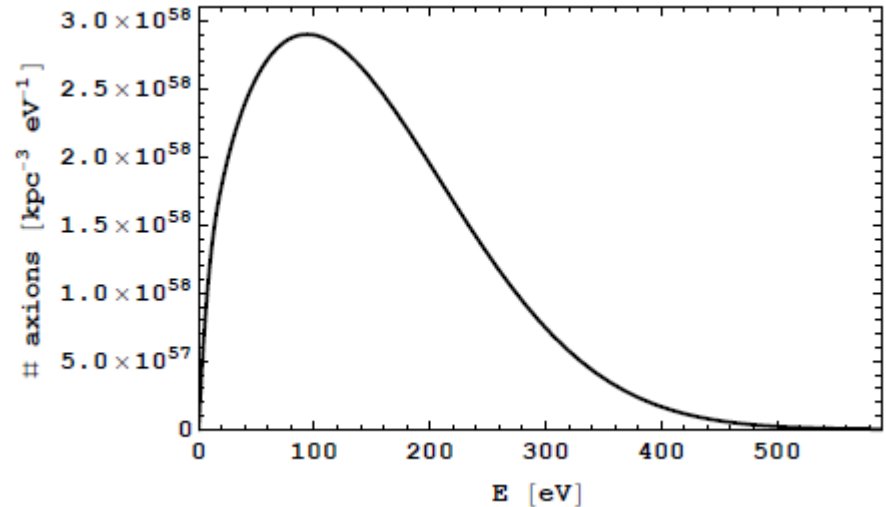


still valid **today!**

# Cosmic axion background and 3.5 keV line

PREDICTION: Cosmic Axion Background

$$E_a \approx 200 \text{ eV} \left( \frac{10^6 \text{ GeV}}{m_\phi} \right)^{1/2}$$



- For  $10^5 \text{ GeV} \leq m_\phi \leq 10^7 \text{ GeV}$ , CAB lies today in soft X-ray wavebands
- Detectable via axion-photon conversion in astrophysical **B**-fields  $\mathcal{L} \supset -\frac{a}{4M} F^{\mu\nu} \tilde{F}_{\mu\nu}$
- **Soft X-ray excess** in clusters observed since 1996 (EUVE, ROSAT, XMM-Newton, Suzaku, Chandra)
- Match data for

$$\Delta N_{\text{eff}} \approx 0.5 \quad m_a < 10^{-12} \text{ eV} \quad M \approx 10^{12} \text{ GeV} \quad [\text{Conlon, Marsh}]$$

- **3.5 keV line** from galaxy clusters (XMM-Newton, Suzaku, Chandra) due to **DM**  $\rightarrow$  **aa** converting to  $\gamma$
- Better than simplest explanation: **DM**  $\rightarrow$   $\gamma\gamma$  for  $m_{\text{DM}} \sim 7 \text{ keV}$  due to:
  - i) Inferred signal strength: flux depends on both DM density and **B**-field
  - ii) Morphology: stronger signal from cool core where **B**-field peaks
  - iii) Non-observation in dwarf galaxies and galaxies: small size and **B**-field
  - iv) Match data for same values which give soft X-ray excess

[MC, Conlon, Marsh, Rummel]

# LVS string models

- Tree-level: (i) cx str moduli  $U$  and dilaton  $S$  fixed by background fluxes at  $F^U = F^S = 0$   
(ii) Kahler moduli  $T$  flat because of no-scale cancellation

- Corrections beyond tree-level

$$\mathcal{V} = \tau_b^{3/2} - \sum_{i=1}^n \tau_i^{3/2} \quad K = -2 \ln \mathcal{V} - \frac{\xi}{g_s^{3/2} \mathcal{V}} \quad W = W_0 + \sum_{i=1}^n A_i e^{-a_i T_i}$$

- Scalar potential

$$V = \sum_{i=1}^n \left( \frac{8}{3} \sqrt{\tau_i} (a_i A_i)^2 \frac{e^{-2a_i \tau_i}}{\mathcal{V}} - 4 a_i A_i W_0 \tau_i \frac{e^{-a_i \tau_i}}{\mathcal{V}^2} \right) + \frac{3 \xi W_0^2}{4 g_s^{3/2} \mathcal{V}^3}$$

- AdS minimum at

$$\tau_i \approx \left( \frac{\xi}{2n} \right)^{2/3} g_s^{-1} \approx g_s^{-1} \approx O(10) \quad \text{for } g_s \approx 0.1$$

$$\mathcal{V} \approx W_0 e^{a_i \tau_i} \approx e^{1/g_s} \gg 1 \quad \longrightarrow \quad \text{trust approximations}$$

- dS vacua without anti-branes

dS<sub>1</sub> case: non-zero hidden matter F-terms induced by D-terms (T-branes) [MC, Quevedo, Valandro]

dS<sub>2</sub> case: non-perturbative effects at singularities [MC, Maharana, Quevedo, Burgess]

- Generate hierarchies naturally:  $m_{3/2} \approx \frac{W_0 M_p}{\mathcal{V}} \approx M_p e^{-1/g_s} \ll M_p$

- Spontaneous ~~SUSY~~:  $F^{T_b} \approx \frac{M_p^2}{\mathcal{V}^{1/3}} \neq 0 \quad F^{T_i} \approx \frac{M_p^2}{\mathcal{V}} \neq 0 \quad F^U \approx F^S \approx \frac{M_p^2}{\mathcal{V}^2} \neq 0$

# Visible sector on D3s

[MC, Krippendorff, Mayrhofer, Quevedo, Valandro]

- D3s at singularities

$$\mathcal{V} = \tau_b^{3/2} - \tau_s^{3/2} - \tau_{vs1}^{3/2} - \tau_{vs2}^{3/2}$$

- $\tau_{vs1} \leftrightarrow \tau_{vs2}$  orientifold projection

→ get U(N) groups

- D-terms for normalised matter fields  $\Phi = \rho e^{i\theta}$

$$V_D \simeq g^2 (\rho^2 - \xi)^2$$

- FI-term

$$\xi \simeq q_i K_i \simeq \frac{\tau_{vs}}{\mathcal{V}}$$

- $D = 0$  gives

$$\langle \rho \rangle = \sqrt{\xi} \simeq M_s \sqrt{\tau_{vs}}$$

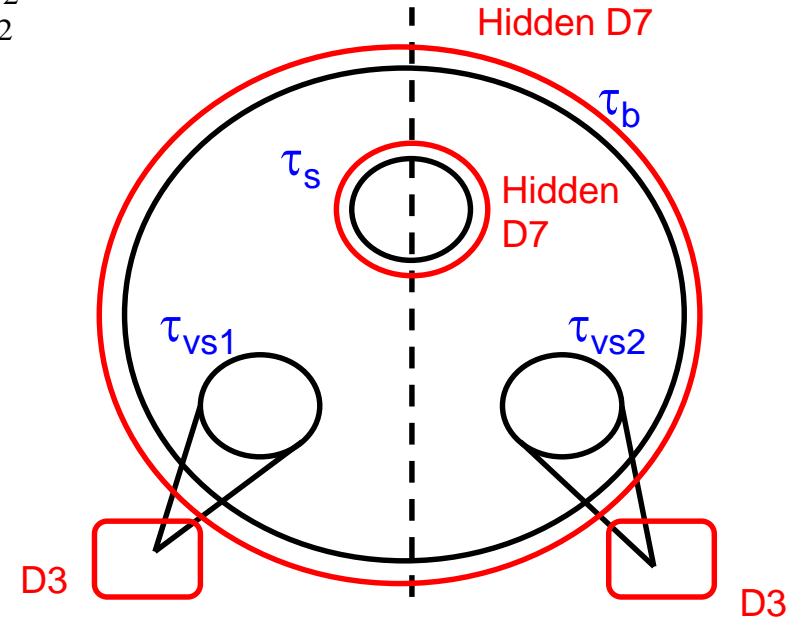
- Closed string axion  $\text{Im}(T_{vs})$  eaten up by anomalous U(1)s

- Subleading F-terms from SUSY breaking fix:

a) non-tachyonic scalars:  $\rho = 0 \rightarrow \xi = 0 \rightarrow \tau_{vs} = 0$

b) tachyonic scalar:  $\rho \sim 0 + 1/\mathcal{V} \sim M_s / \mathcal{V}^{1/2} \rightarrow \tau_{vs} \sim 0 + 1/\mathcal{V} \ll 1$

- Open string axion  $\theta$  can be QCD axion with  $f_a = \rho \sim M_s / \mathcal{V}^{1/2} \sim m_{3/2} \sim 10^{10-11} \text{ GeV}$



- Non-perturbative +  $\alpha'$  effects fix  $\tau_b$  and  $\tau_s$  at  $\tau_b^{3/2} \approx e^{\tau_s}$   $\tau_s \approx g_s^{-1}$

# Mass scales

- D3s at singularities  $\longrightarrow$  F-term of  $\tau_{vs}$  is zero:  $F^{vs} \propto \xi_{FI} \propto \tau_{vs} \rightarrow 0$
- Soft-terms (depending on matter Kahler metric and dS mechanism):

$$M_{1/2} \approx \frac{M_p}{\mathcal{V}^2} \ll m_{3/2} \approx \frac{M_p}{\mathcal{V}} \quad m_0 \approx \begin{cases} \frac{M_p}{\mathcal{V}^{3/2}} \approx m_{\tau_b} \\ \frac{M_p}{\mathcal{V}^2} \end{cases}$$

- Set  $\mathcal{V} \sim 10^7$  to get  $M_{1/2} \sim \mathcal{O}(1)$  TeV :

$$M_p \approx 10^{18} \text{ GeV}$$

$$M_{GUT} \approx M_s \mathcal{V}^{1/6} \approx 10^{16} \text{ GeV}$$

$$M_s \approx m_{\tau_{vs}} \approx m_{a_{vs}} \approx 10^{15} \text{ GeV}$$

$$M_{KK} \approx 10^{14} \text{ GeV}$$

$$m_{\tau_s} \approx m_{a_s} \approx 10^{12} \text{ GeV}$$

$$m_{3/2} \approx 10^{11} \text{ GeV}$$

$$m_{\tau_b} \approx 10^7 \text{ GeV} \quad \text{MSSM}$$

$$M_{1/2} \approx m_0 \approx M_p \mathcal{V}^{-2} \approx 1 \text{ TeV}$$

$$m_{a_{open}} \approx 1 \text{ meV}$$

$$m_{a_b} \approx 0$$

- 1) TeV scale SUSY
- 2) Standard GUTs and WIMP DM
- 3) Right inflationary scale
- 4) No CMP for  $\tau_b$  and no gravitino problem
- 5) QCD axion from open string modes
- 6) Reheating driven by the decay of  $\tau_b$
- 7)  $T_{rh} \sim 1\text{-}10 \text{ GeV}$
- 8) Non-thermal dark matter
- 9) Axionic dark radiation
- 10) Affleck-Dine baryogenesis

$$m_{\tau_b} \approx m_0 \approx 10^7 \text{ GeV} \quad \text{Split SUSY}$$

$$M_{1/2} \approx 1 \text{ TeV}$$





# (Ultra) - Locality

- Kahler potential

$$K = -2 \ln \left( \mathcal{V} + \frac{\hat{\xi}}{2} \right) + K(U, S)$$

$$\mathcal{K} = K + \tilde{K}_\alpha(U, S, T) \bar{C}^\alpha C^\alpha + [Z(U, S, T) H_u H_d + \text{h.c.}]$$

- Kahler matter metric from Yukawas

$$\hat{Y}_{\alpha\beta\gamma} = e^{K/2} \frac{Y_{\alpha\beta\gamma}(U, S)}{\sqrt{\tilde{K}_\alpha \tilde{K}_\beta \tilde{K}_\gamma}}$$

- **Locality** implies:

$$\tilde{K}_\alpha = f_\alpha(U, S) e^{K/3} \quad (*)$$

- Two limits:

i) **Ultra-local limit**: (\*) holds exactly

ii) **Local limit**: (\*) holds only at leading order in  $\mathcal{V}$ -expansion

$$e^{K/3} = \frac{e^{K(U, S)/3}}{\left( \mathcal{V} + \frac{\hat{\xi}}{2} \right)^{2/3}} = \frac{e^{K(U, S)/3}}{\mathcal{V}^{2/3}} \left( 1 - \frac{\hat{\xi}}{3\mathcal{V}} + \dots \right)$$

- Parametrisation of Kahler matter metric: 
$$\tilde{K}_\alpha = \frac{f_\alpha(U, S)}{\mathcal{V}^{2/3}} \left( 1 - c_\xi \frac{\hat{\xi}}{\mathcal{V}} + \dots \right)$$

- Ultra-local limit for  $c_\xi = 1/3$

# Soft terms

[Aparicio, MC, Krippendorff, Maharana, Muia, Quevedo]

- Gaugino masses

$$f_a = \kappa_a S + \lambda_a T_{SM} \rightarrow \kappa_a S \quad \longrightarrow \quad M_{1/2} = \frac{FS}{2s} \simeq \lambda(U, S) \frac{\hat{\xi} m_{3/2}}{\mathcal{V}}$$

- Scalar masses:

$$m_\alpha^2 = m_{3/2}^2 + V_0 - F^{T_i} F^{\bar{T}_j} \partial_{T_i} \partial_{\bar{T}_j} \ln \bar{K}_\alpha + \bar{K}_\alpha^{-1} \sum_a g_a^2 D_a \partial_\alpha \partial_{\bar{\alpha}} D_a \quad D_a = \sum_j Q_{ja} \phi_j \frac{\partial K}{\partial \phi_j} + \sum_i q_{ia} \partial_{T_i} K$$

- Ultra-local limit:

**dS<sub>1</sub> case:** generated by D-terms at  $O(\mathcal{V}^{-3})$

$$m_0^2 \simeq \frac{9}{64} \frac{\hat{\xi} m_{3/2}^2}{\mathcal{V} \ln \mathcal{V}}$$

**dS<sub>2</sub> case:** generated by F-terms of U and S at  $O(\mathcal{V}^{-4})$

$$m_\alpha^2 \simeq Q_\alpha(U, S) M_{1/2}^2$$

- Local limit: D-terms are negligible

$$m_0^2 \simeq \frac{15}{4} \left( c_\xi - \frac{1}{3} \right) \frac{\hat{\xi} m_{3/2}^2}{\mathcal{V}} \quad c_\xi > 1/3$$

- A-terms  $\sim M_{1/2}$

- Giudice-Masiero or non-perturbative W generate  $\mu$ -term  $\lesssim M_{1/2}$

- Two scenarios:

i) **MSSM-like:** ultra-local dS<sub>2</sub> case

$$M_{1/2} \sim m_\alpha \sim A_{\alpha\beta\gamma} \sim \frac{M_p}{\mathcal{V}^2}$$

ii) **Split SUSY:** other cases

$$M_{1/2} \sim A_{\alpha\beta\gamma} \sim \frac{M_p}{\mathcal{V}^2} \quad \text{while} \quad m_0 \sim \frac{M_p}{\mathcal{V}^{3/2}}$$

with tunable flux-dependent coefficients

# Conclusions

- **No-scale + locality** in 4D string models  $\longrightarrow$  sequestering:  $M_{1/2} \ll m_\phi \ll m_{3/2} \ll M_s$
- Avoid CMP + gravitino problem + axion DM overproduction
- Allow large  $M_s$  and TeV-scale  $M_{1/2}$   
 $\longrightarrow$  good for GUTs, inflation, WIMP DM
- Split SUSY-like spectra more generic with  $m_0 \sim m_\phi \sim 10^{6-7}$  GeV
- Reheating driven by lightest modulus decay
- **Non-standard cosmology**: dilution of thermal DM
- **Non-thermal dark matter**:
  - i) CMSSM with a **300 GeV** Higgsino LSP saturating DM for  $T_{rh} = 2$  GeV
  - ii) More in general: **300-850 GeV** Higgsino LSP saturating DM for  $T_{rh} = 2-40$  GeV
- Generic production of **axionic dark radiation**  $\longrightarrow \Delta N_{eff} \neq 0$
- Cosmic axion background with  $E_a \sim 200$  eV
- CAB detectable via axion-photon conversion in **B**
- Explain **soft X-ray excess** and **3.5 keV line** in galaxy clusters
- Realised in LVS type IIB compactifications with visible sector on D3-branes