

Is SUSY Alive and Well?
Madrid, September 2016

Dark Matter: Implications of a Saxion Condensate

Lawrence Hall
University of California, Berkeley



(I)

Where are We?

After 43 Years of BSM Theory

No Experimental BSM Discovery

Without data, no aspect of BSM is healthy

We don't know what is going on;
Everything is open for discussion

Where are we with SUSY?

We have discovered a highly
perturbative Higgs: $\lambda = 0.13$

$$m_h = 125 \text{ GeV}$$

SUSY is very much alive

But: Higgs mass needs boost of 40%: $\tilde{m} \gg v$?

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EWSB is fine-tuned: *Anthropics?*

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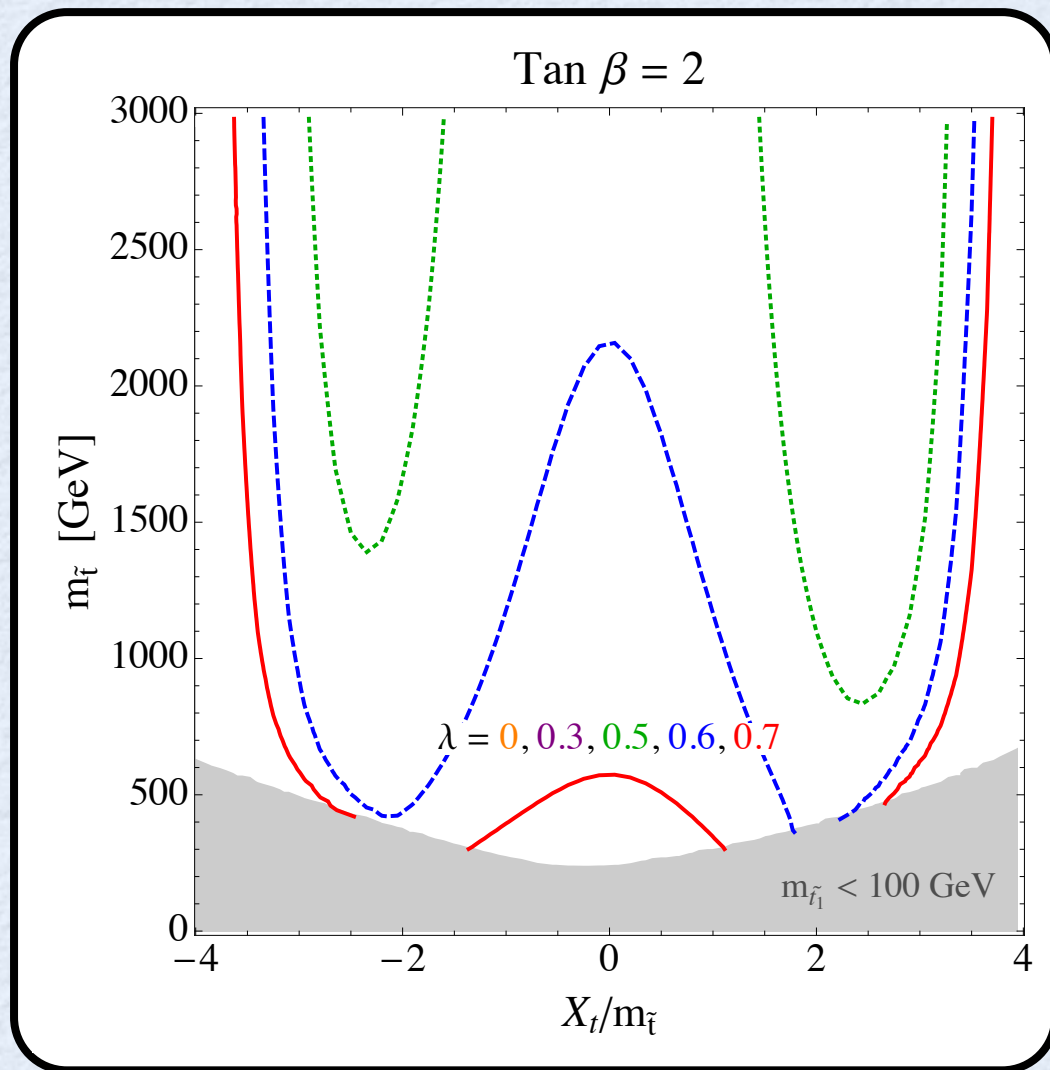
EWSB is fine-tuned: **Anthropics?**

$m_h = 125 \text{ GeV}$ & Gauge unification

Keeps me motivated

Higgs Mass: Some Favorite Possibilities

NMSSM



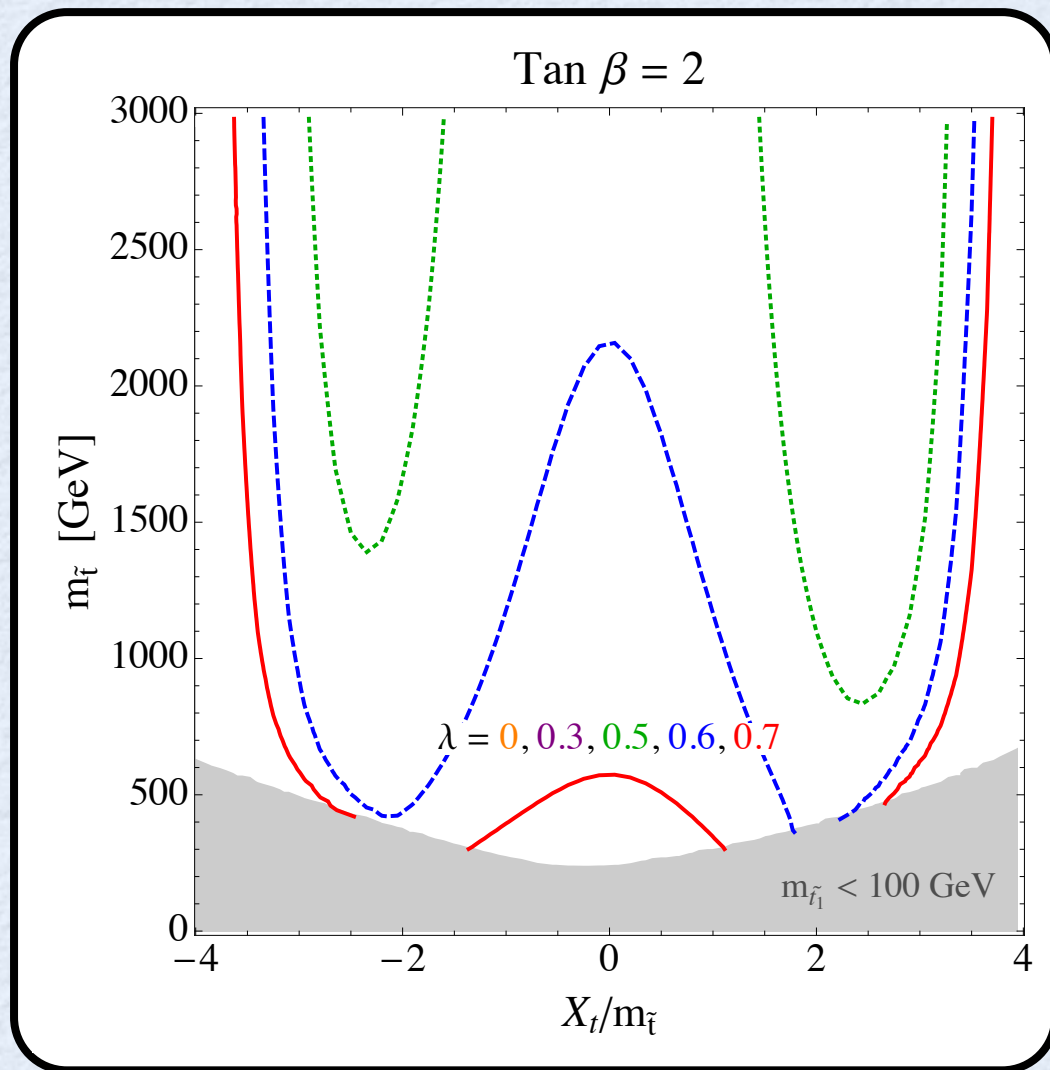
Hall, Ruderman, Pinner

arXiv:1112.2703

$$\tilde{m} \sim (1 - 3) \text{ TeV}$$

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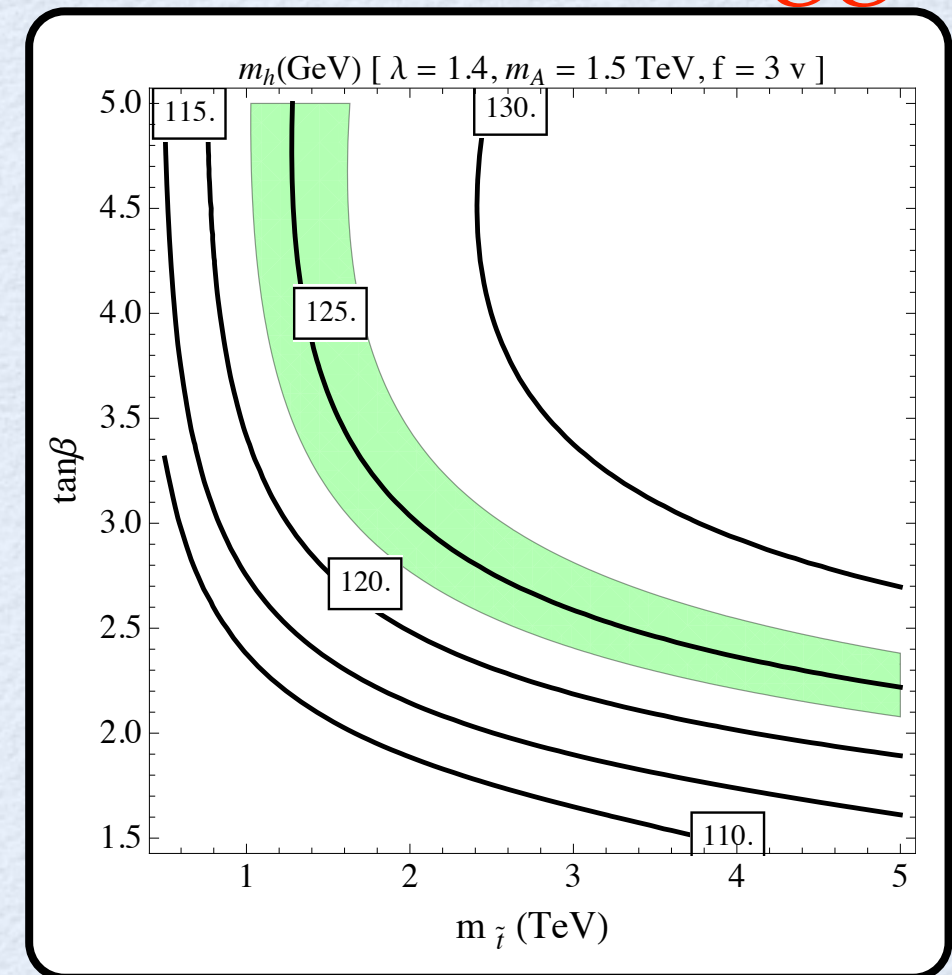
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SUSY Twin Higgs



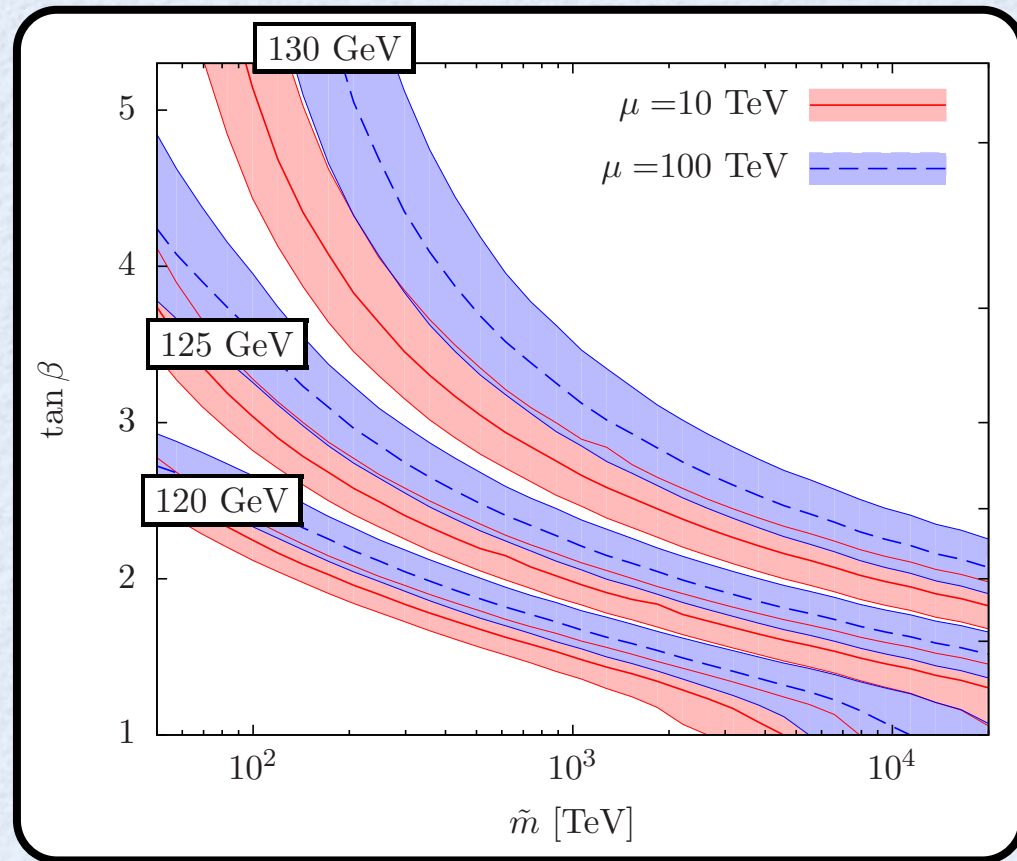
Craig, Howe
arXiv:1311.1341

$$\tilde{m} \sim (1 - 5) \text{ TeV}$$

$$m_\phi^2 = (m_Z^2 \cos^2 2\beta + 4\delta\lambda_u v^2 \sin^4 \beta) \left(2 - \frac{2v^2}{f^2} \right)$$

Higgs Mass: My Favorite Possibilities

“Mini-Split” or “Spread SUSY”

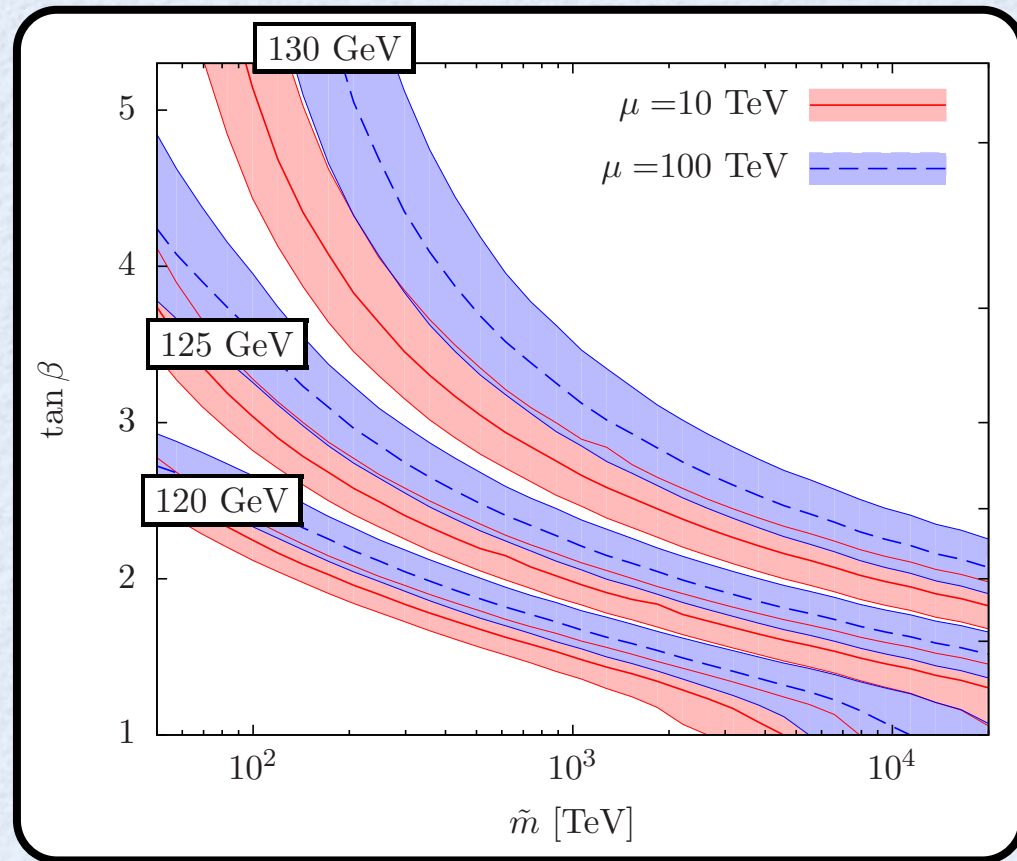


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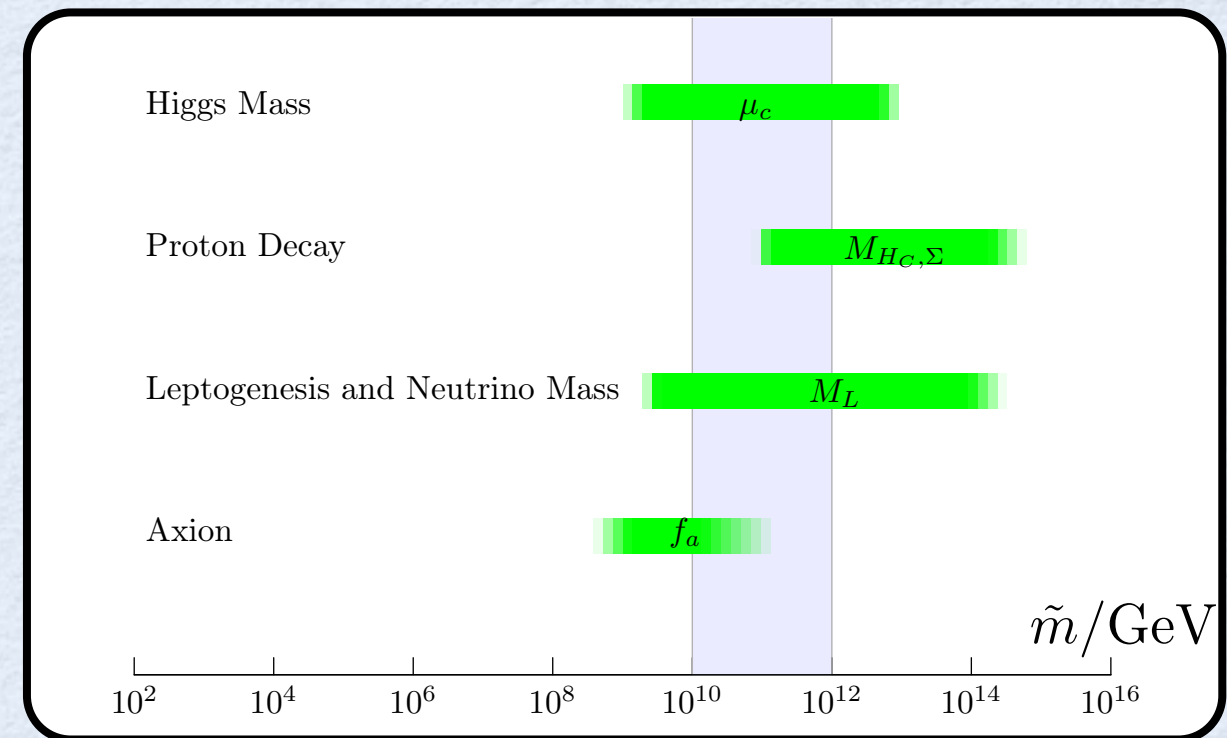
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“Intermediate Scale” SUSY

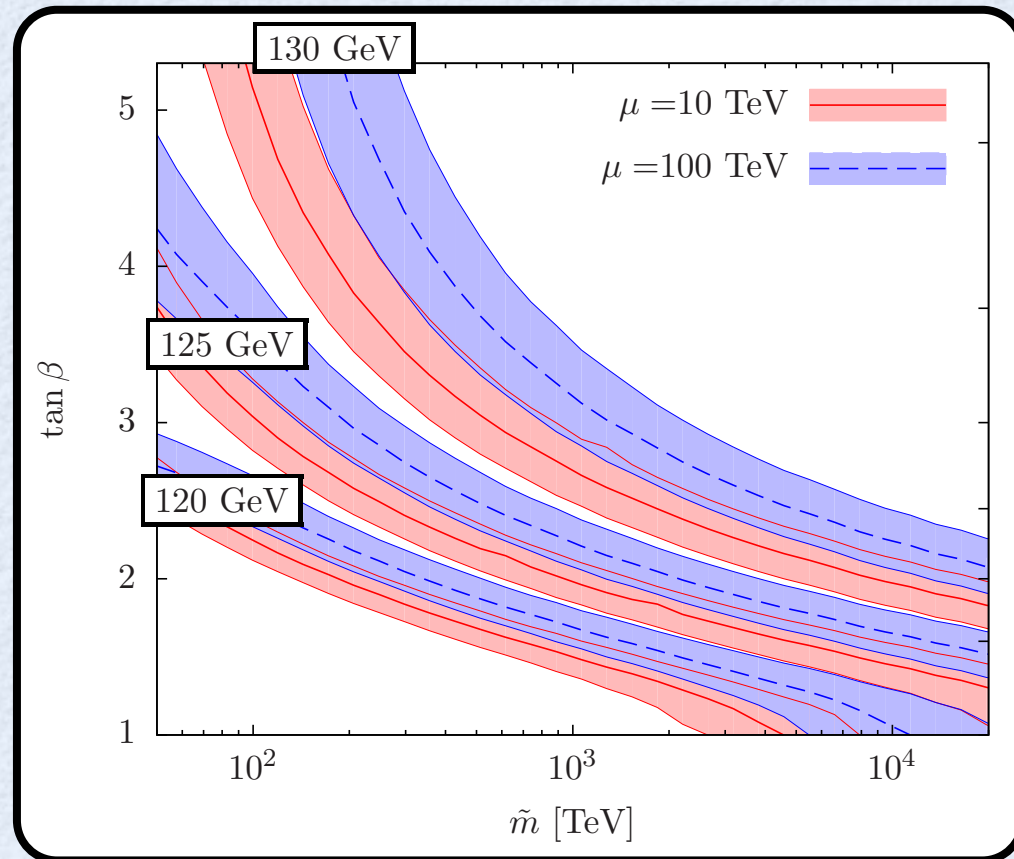


Hall, Nomura arXiv:1210.2395

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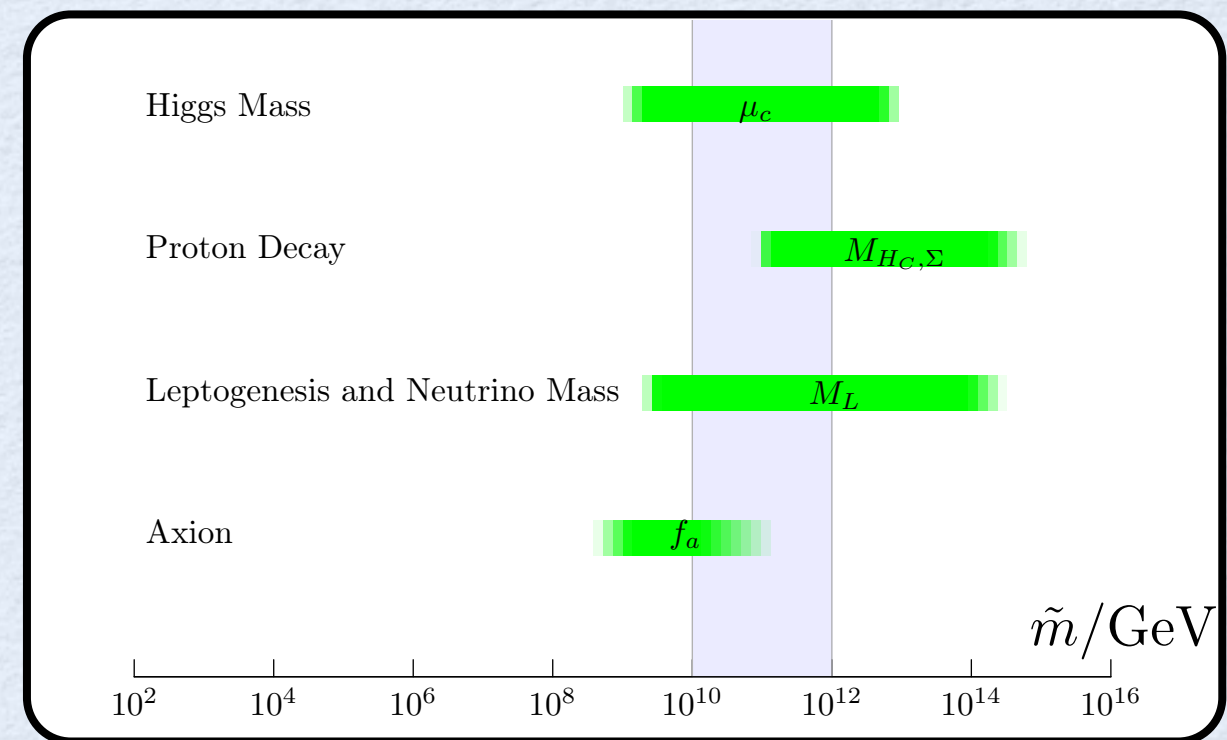
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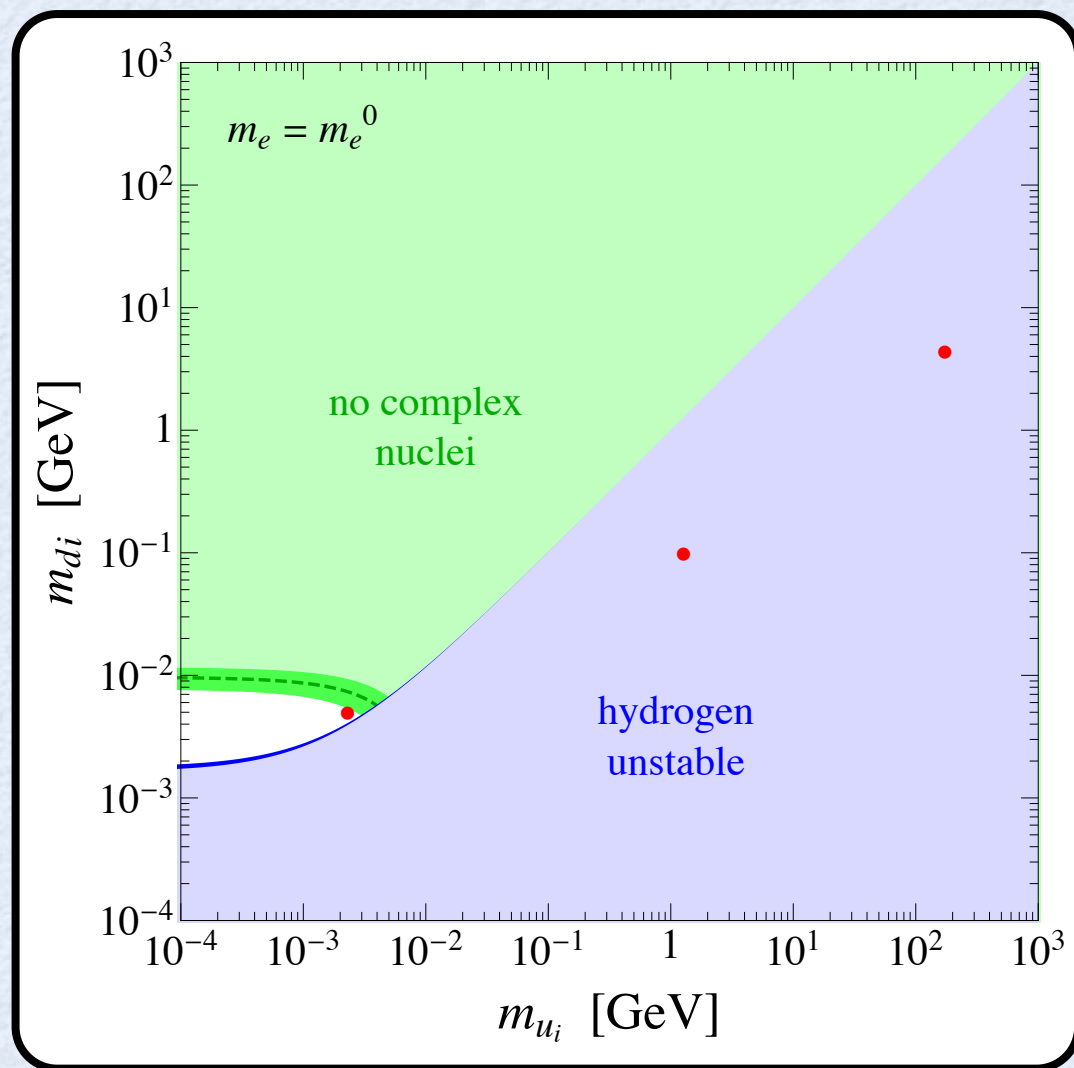
$$\tilde{m} \sim (10^{10} - 10^{12}) \text{ GeV}$$

Without naturalness

$m_h = 125 \text{ GeV}$ & Gauge unification
insufficient to determine \tilde{m}

An Anthropic Weak Scale?

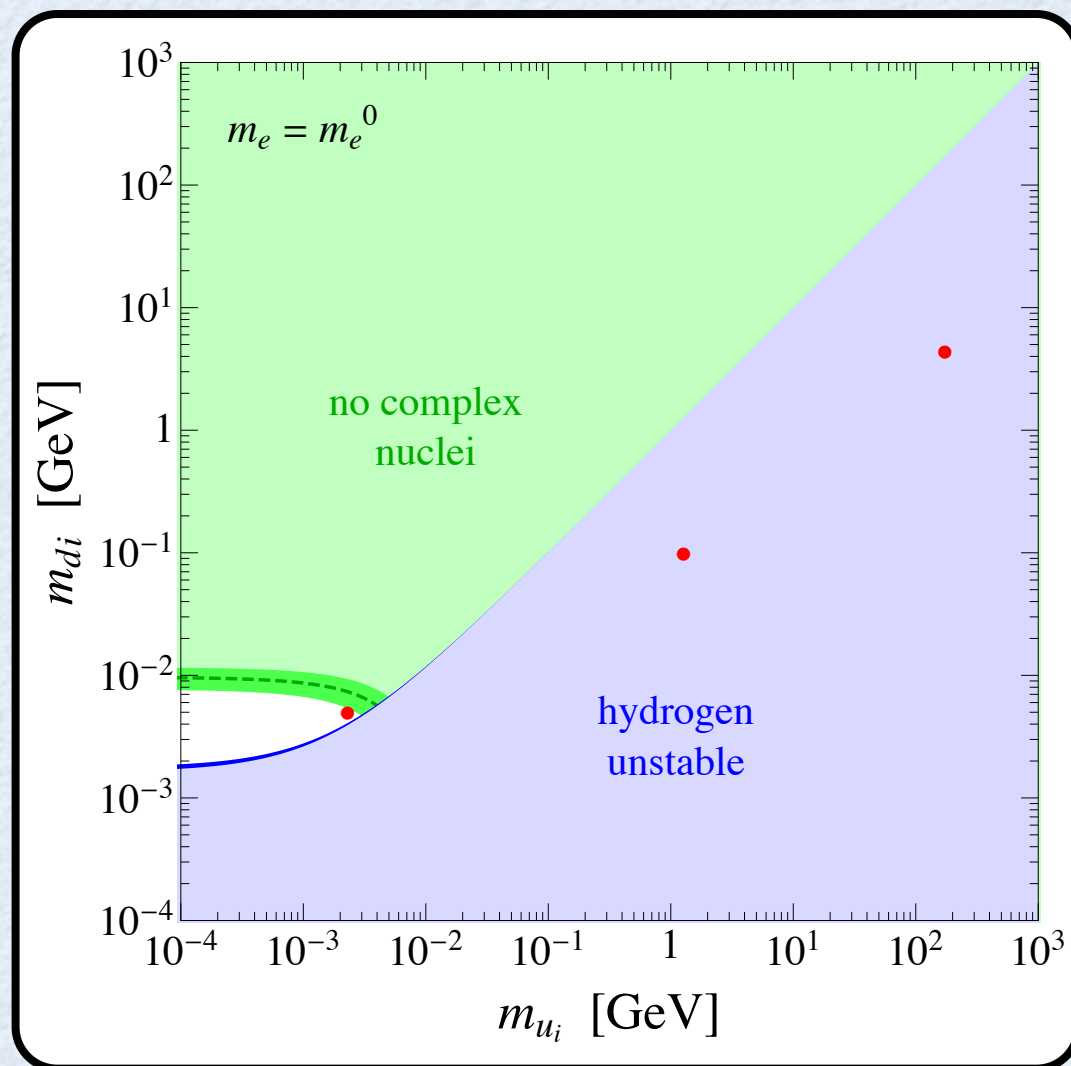
Atomic Boundaries



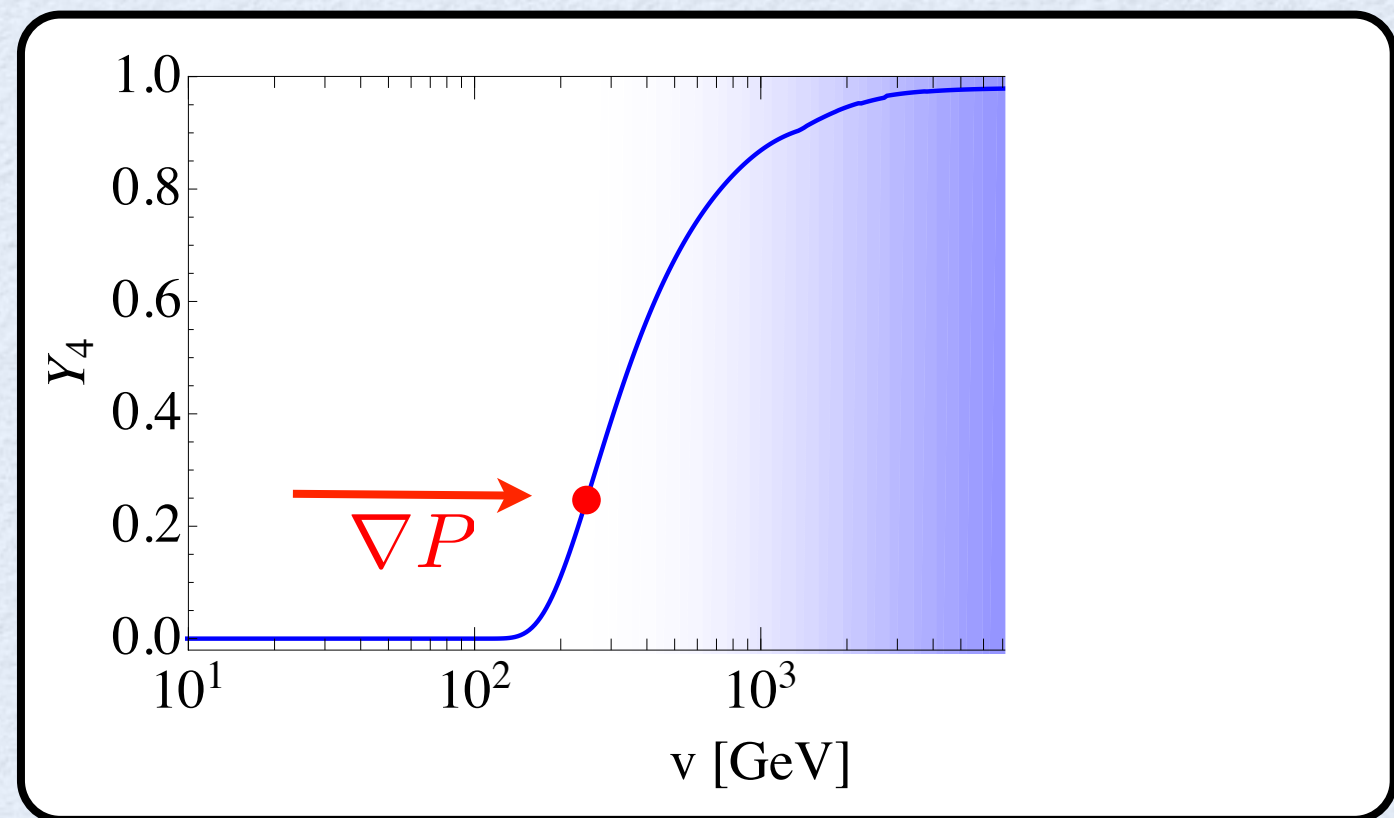
$m_{u,d}$ both scan

An Anthropic Weak Scale?

Atomic Boundaries



He-4 BBN Boundary



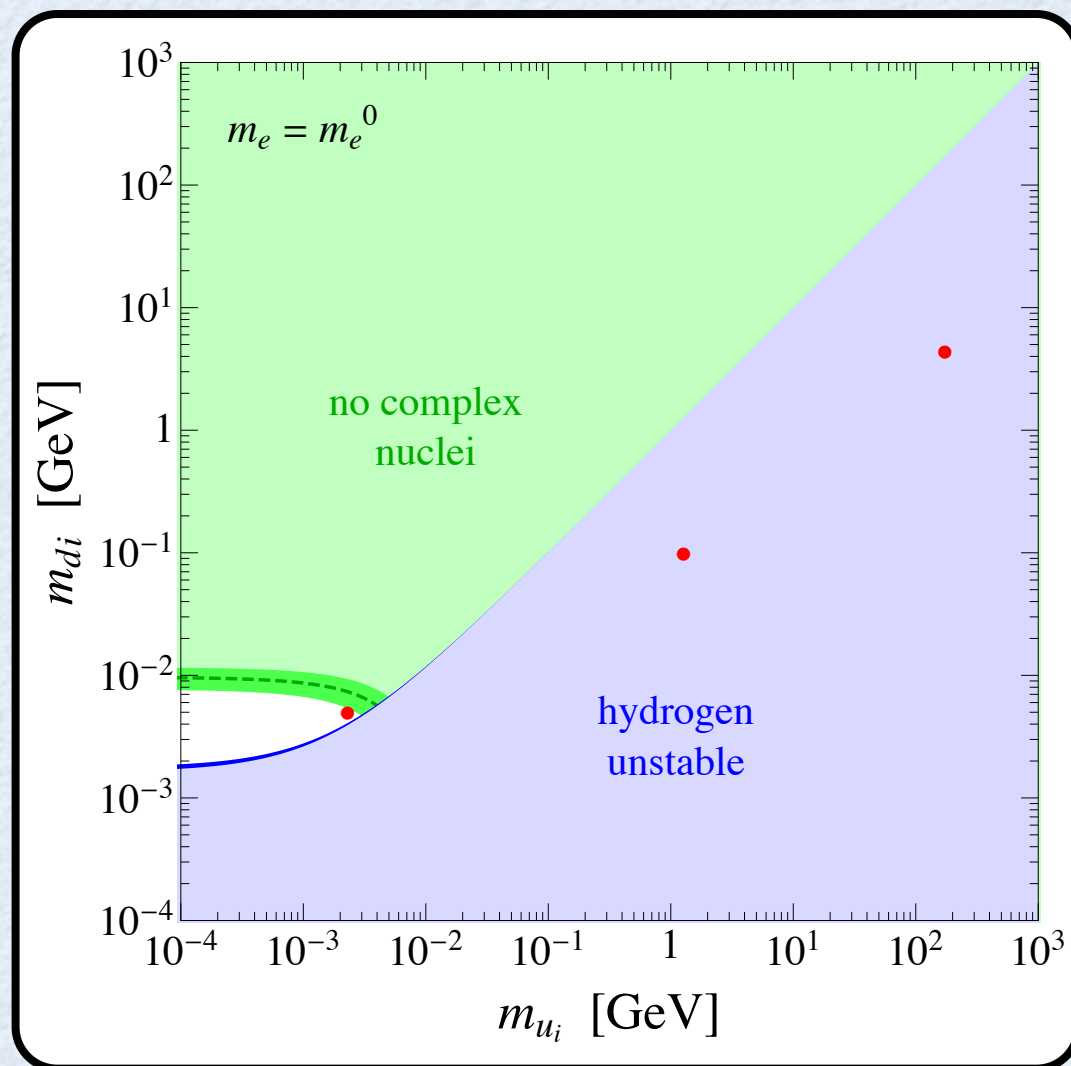
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Hall, Pinner, Ruderman

arXiv:1409.0551

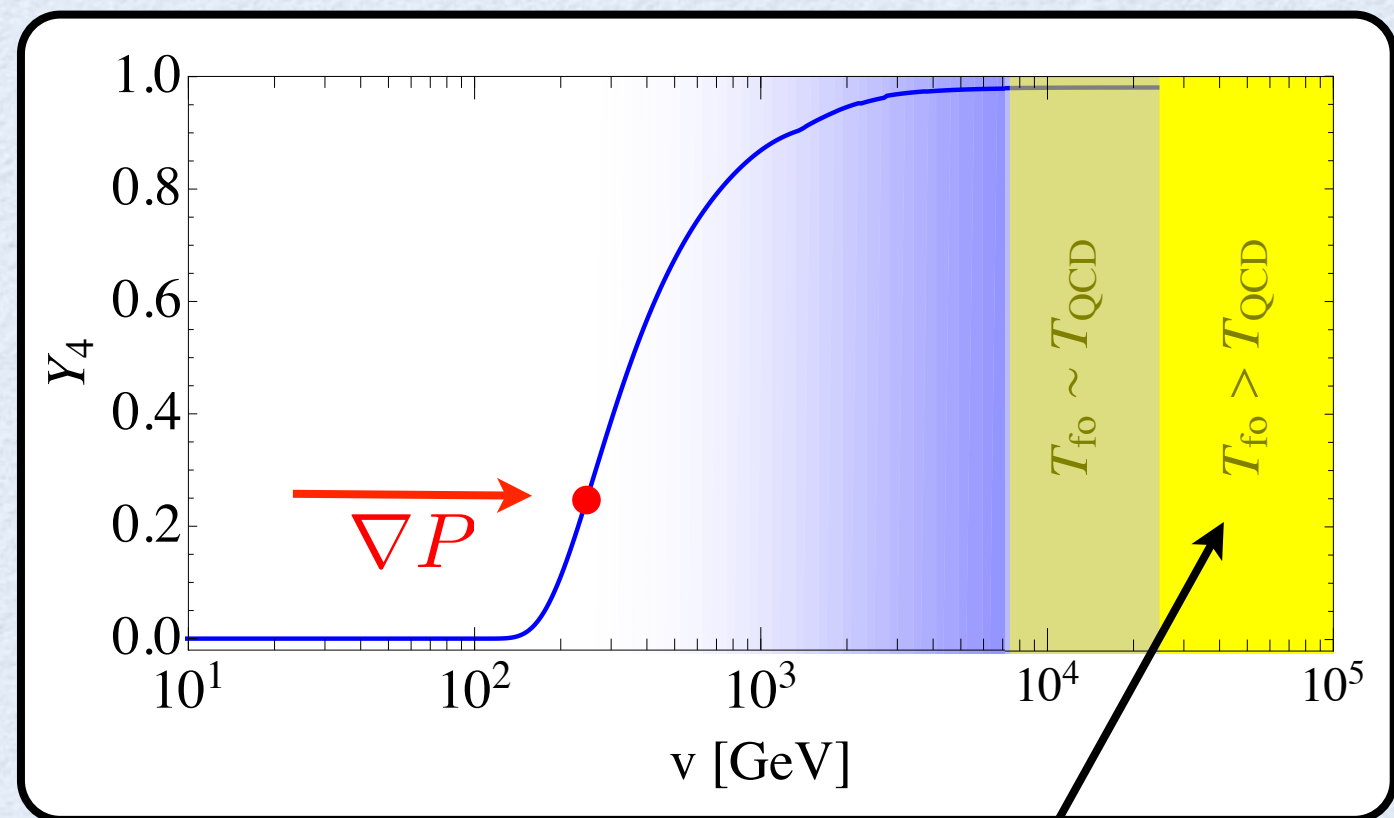
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$m_{u,d}$ both scan

He-4 BBN Boundary



He-4 depends on
asymmetries, not v

Hall, Pinner, Ruderman

arXiv:1409.0551

My View

Without data, no aspect of BSM is healthy

We don't know what is going on;
Everything is open for discussion

(II)

Dark Matter in (SUSY + PQ)

Raymond Co, Francesco D'Eramo, Lawrence Hall
1603.04439, 1610.xxxxx

Two Favorite DM Candidates

- **Axion (a)**

$$f_a \sim 10^{12} \text{ GeV} \qquad \theta_{mis} \sim 1$$

$$f_a \sim 10^{16-18} \text{ GeV} \qquad \theta_{mis} \ll 1 \qquad \text{“anthropic window”}$$

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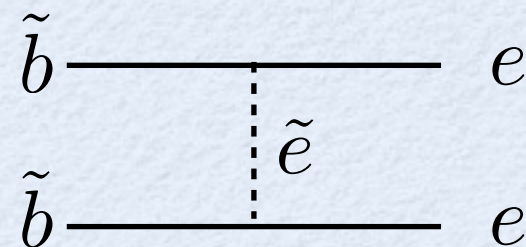
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$$f_a \sim 10^{16-18} \text{ GeV}$$

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- **LSP($\tilde{b}, \tilde{h}, \dots \tilde{G}_{3/2}$)**

- Freeze-Out



Excluded; but there are others

- Gravitino Problem

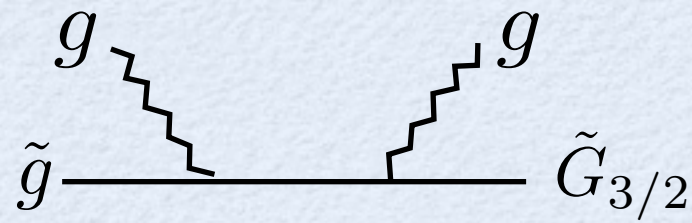


Abundance

Late Decays

TeV-scale SUSY: Gravitino Problem

- Abundance:



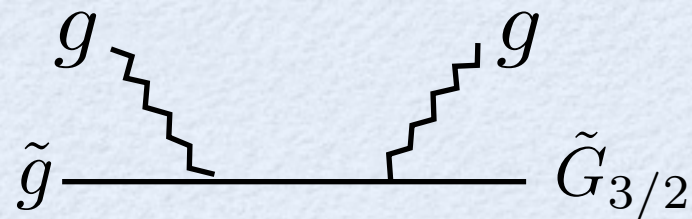
UV $\tilde{G}_{3/2}$

$$T_{RI} < 10^9 \text{ GeV} \left(\frac{m_{3/2}}{\text{TeV}} \right)$$

severe for
Low Scale Mediation

TeV-scale SUSY: Gravitino Problem

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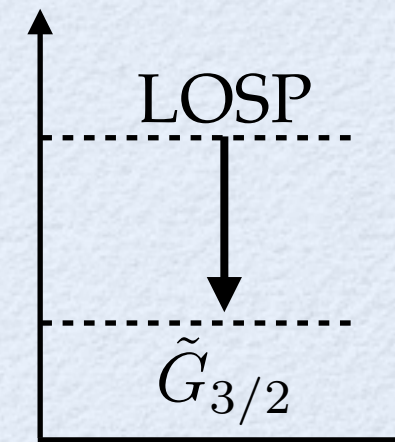
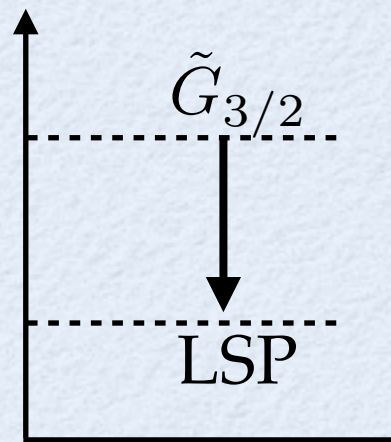


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- Decays



$$\tau_{3/2} \sim 10^6 \text{ s} \left(\frac{\text{TeV}}{m_{3/2}} \right)^3$$

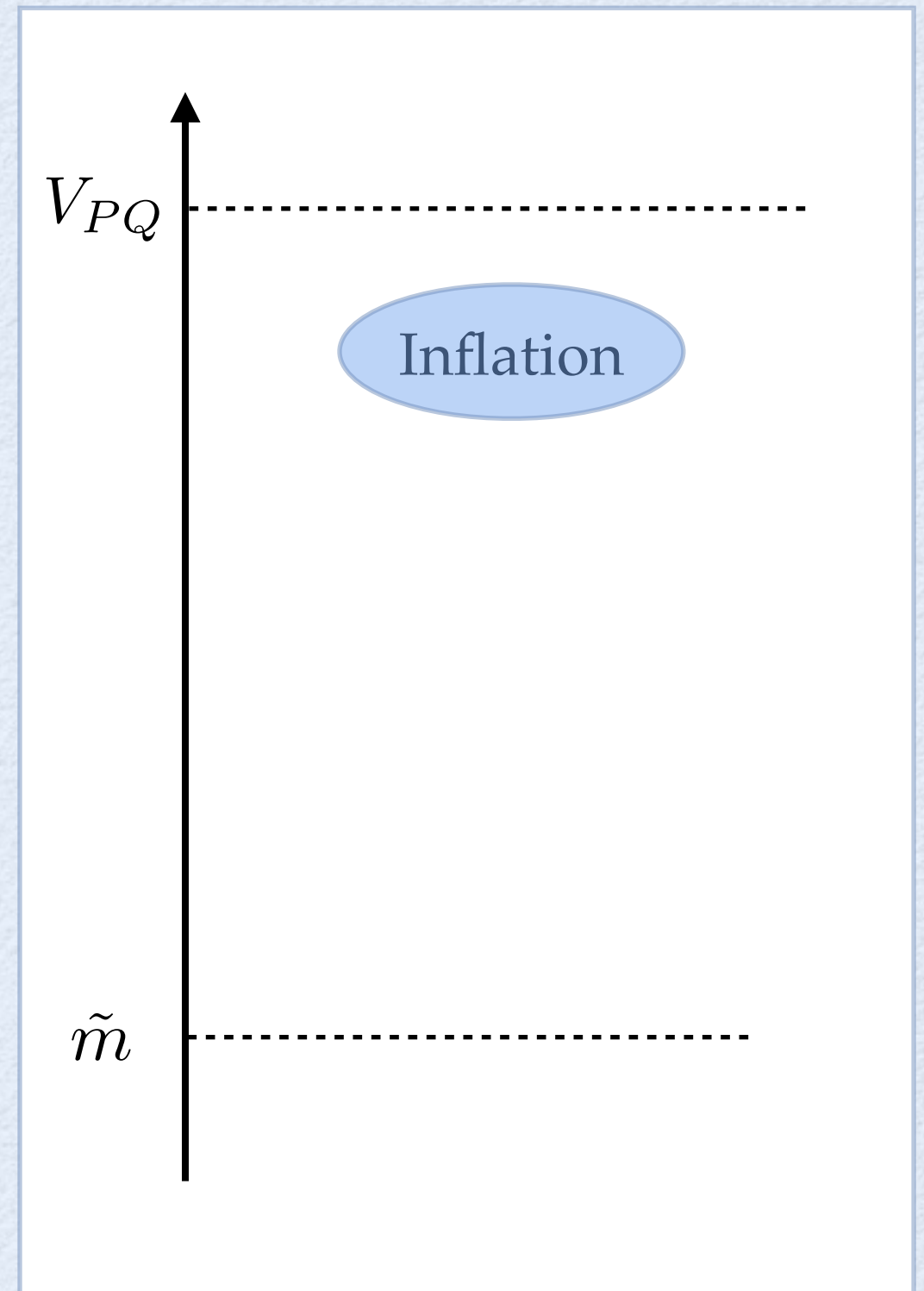
$$\tau_{LOSP} \sim 10^4 \text{ s} \left(\frac{\text{TeV}}{m_{LOSP}} \right)^5 \left(\frac{m_{3/2}}{100 \text{ GeV}} \right)^2$$

severe for
High Scale Mediation

Dark Matter in (SUSY + PQ)

- Everything changes!!

- $$V_{PQ} = \frac{N_{DW}}{\sqrt{2}} f_a$$

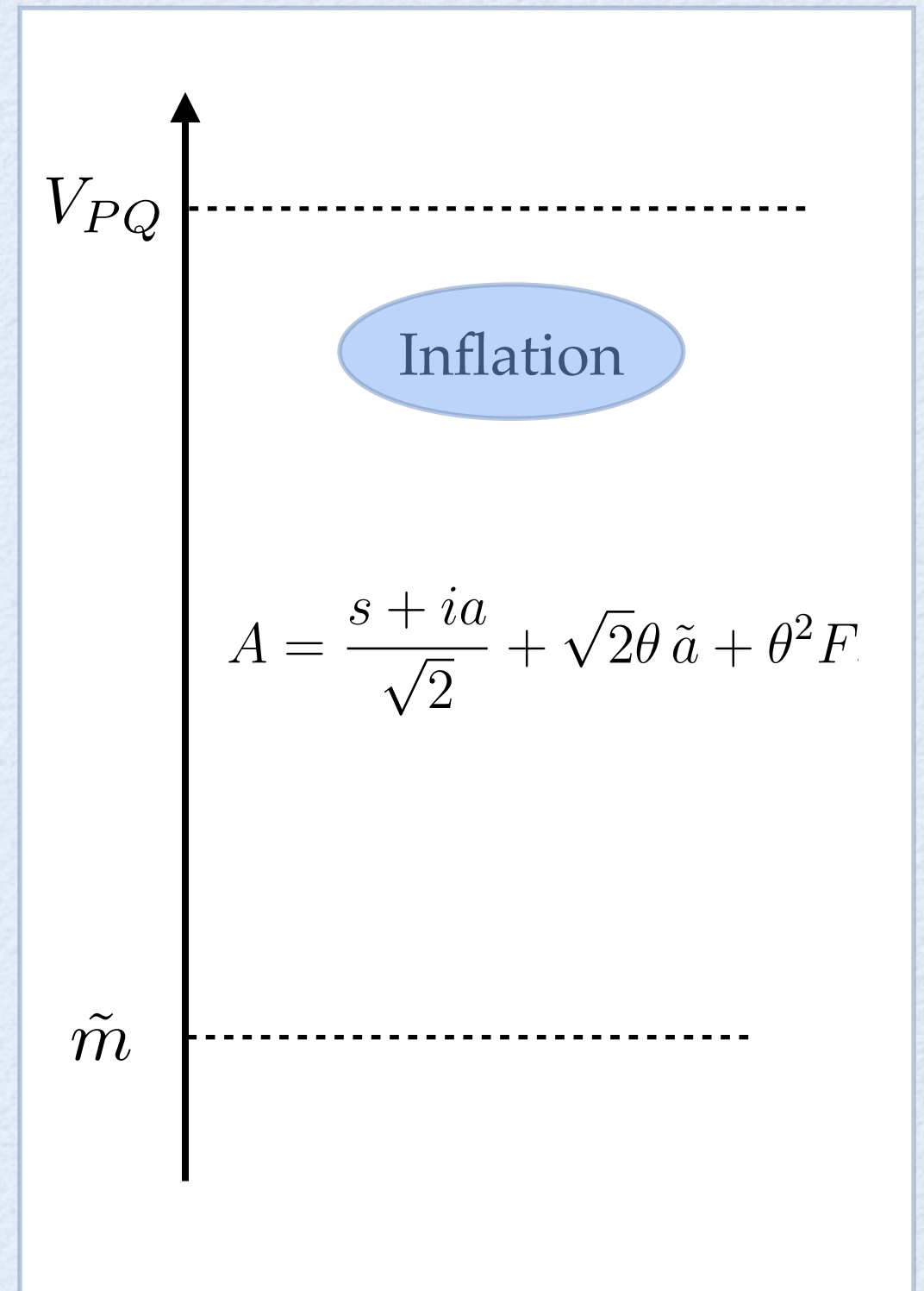


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- saxion (s) and axino (\tilde{a})



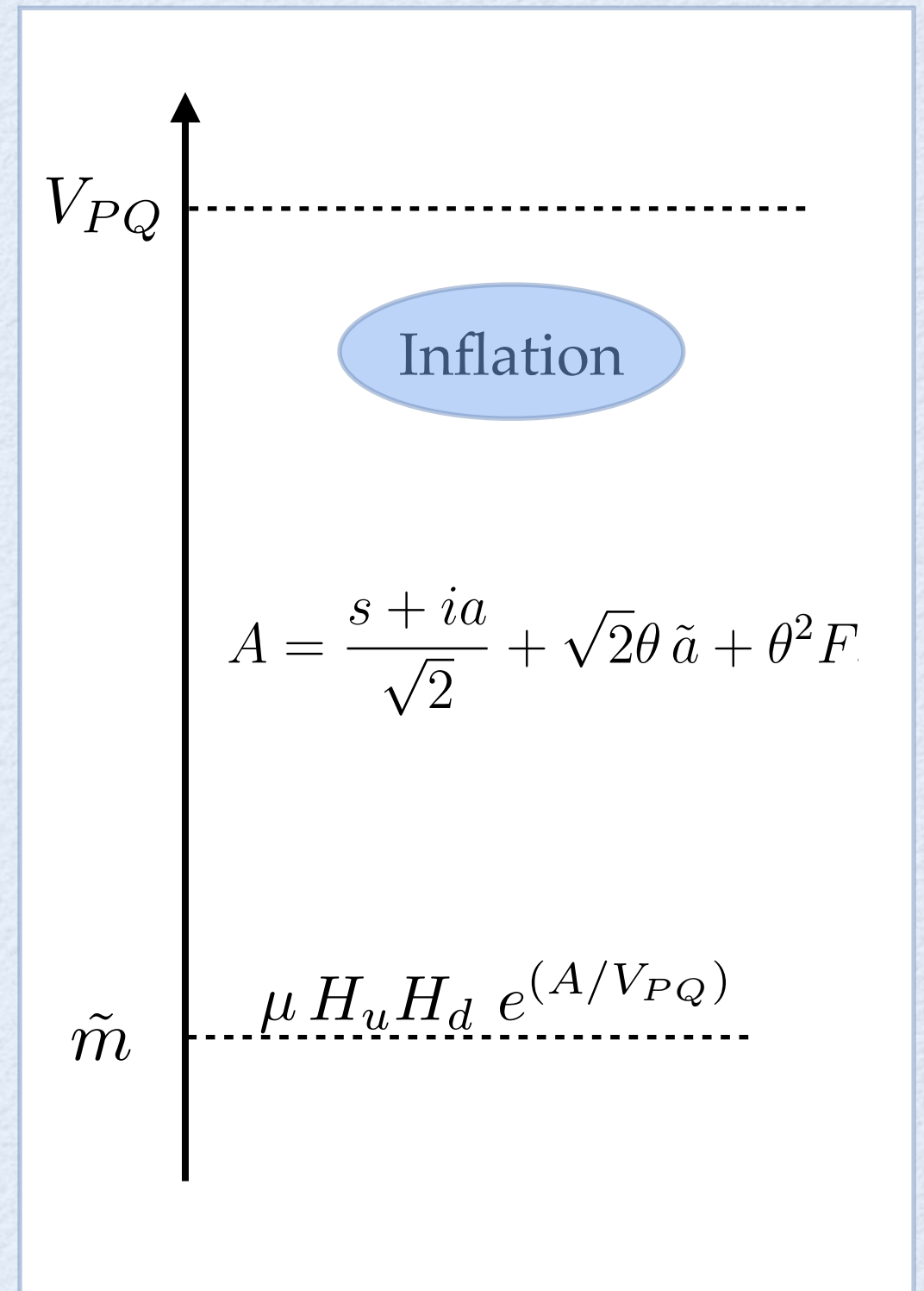
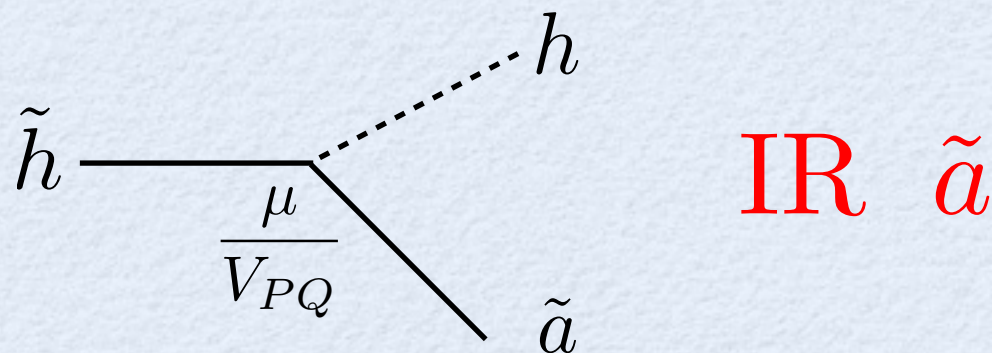
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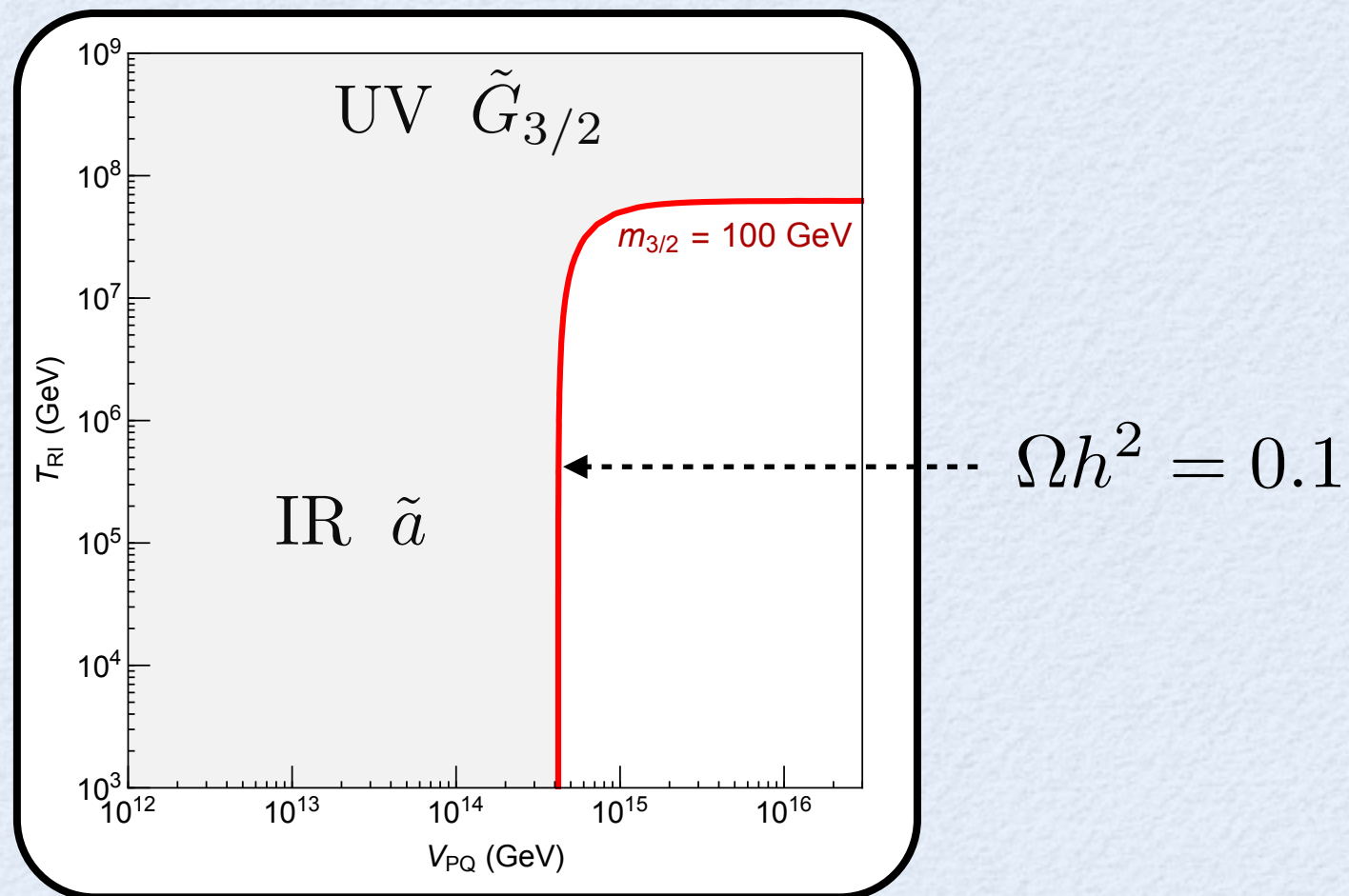
- saxion (s) and axino (\tilde{a})

- **DFSZ** Axino Freeze-In



Axino - Gravitino Problem

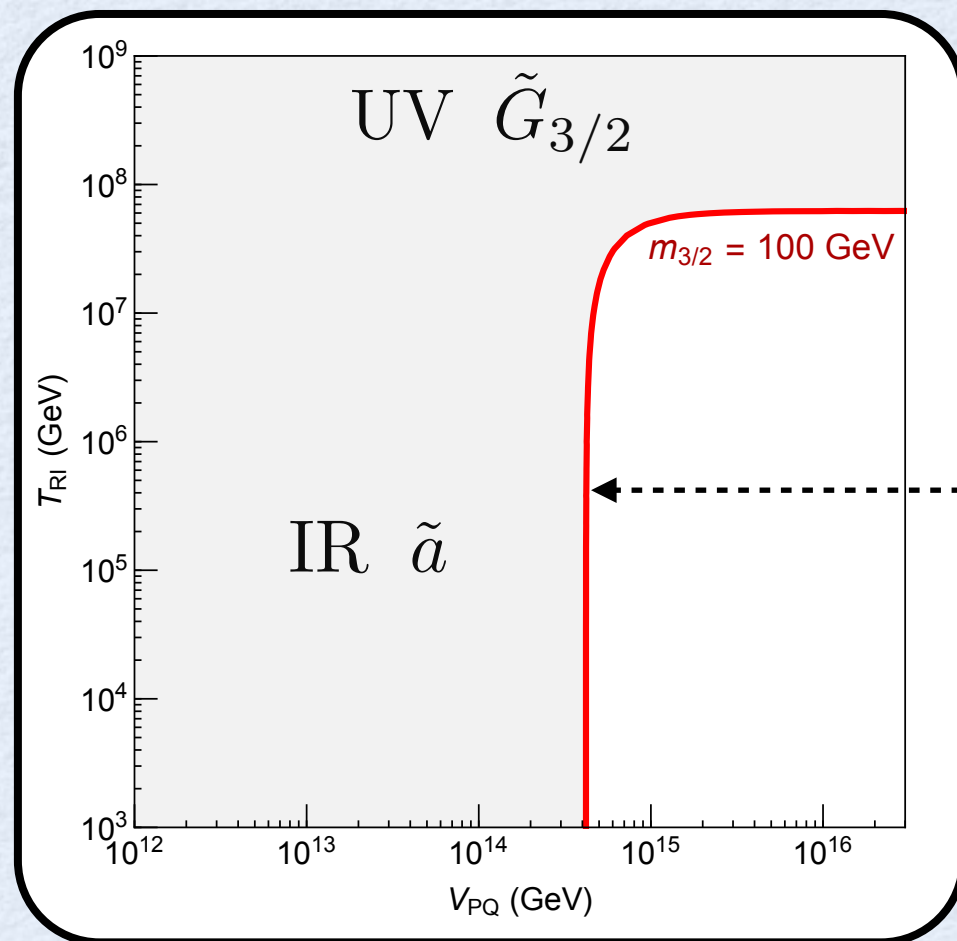
High Scale Mediation



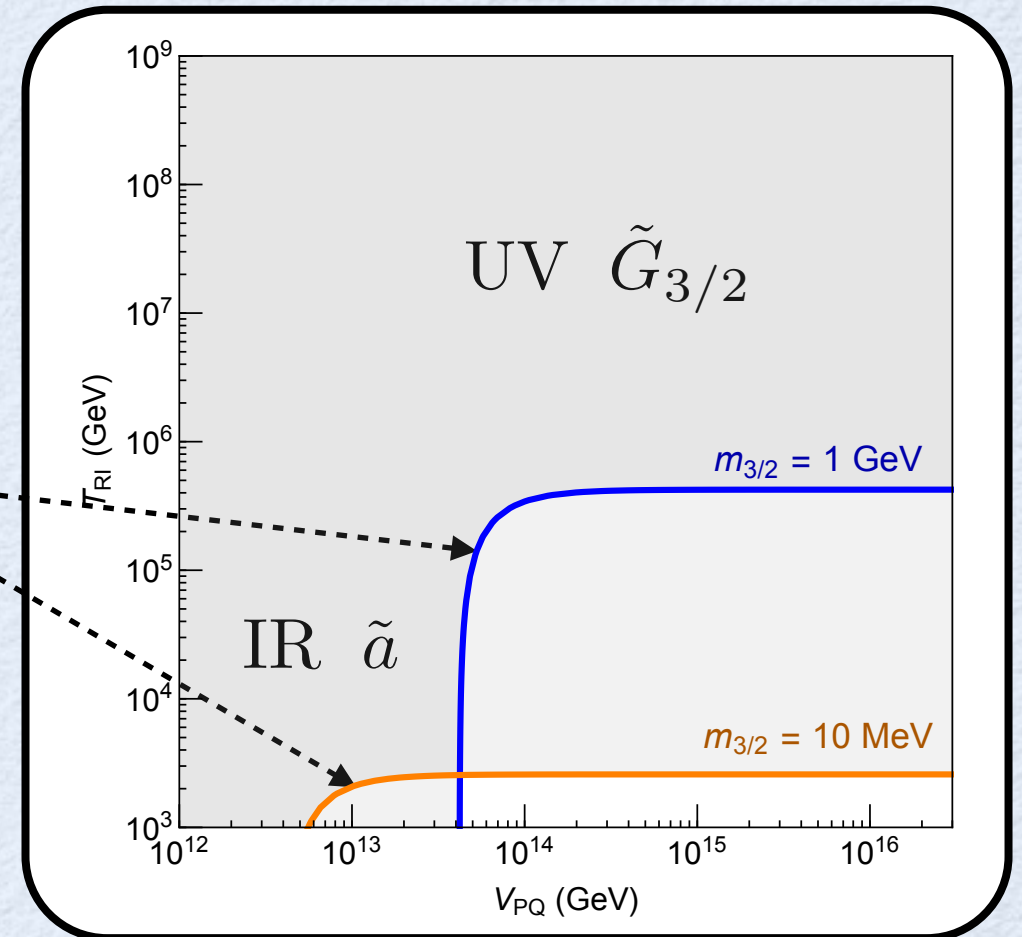
$$m_{3/2} < m_{\tilde{a}} \lesssim 1 \text{ TeV}$$

Axino - Gravitino Problem

High Scale Mediation



Low Scale Mediation



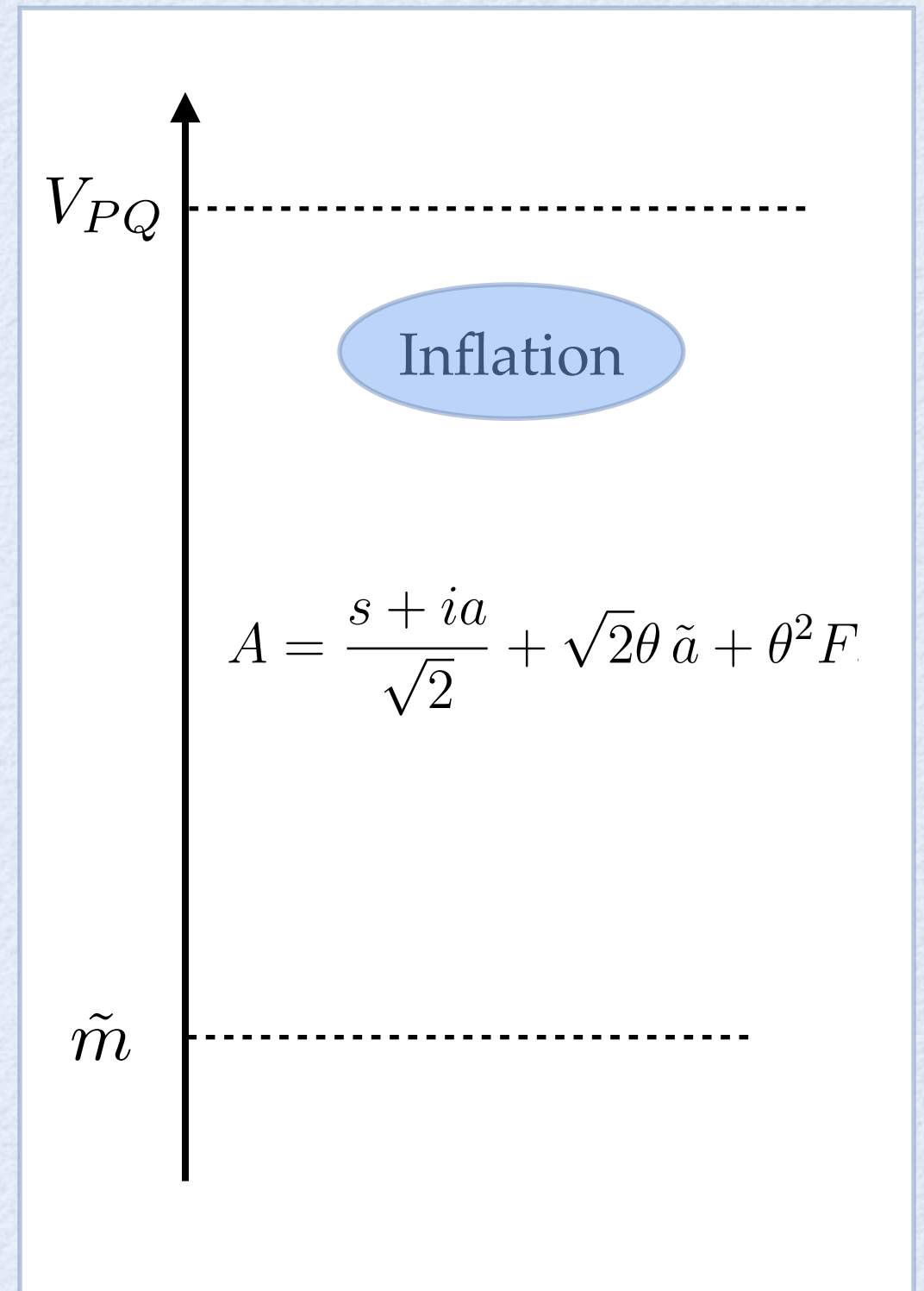
$$\Omega h^2 = 0.1$$

$$m_{3/2} < m_{\tilde{a}} \lesssim 1 \text{ TeV}$$

The Saxion Condensate

- Forms during inflation

$$\sigma_i \sim V_{PQ}, M_*$$



The Saxion Condensate

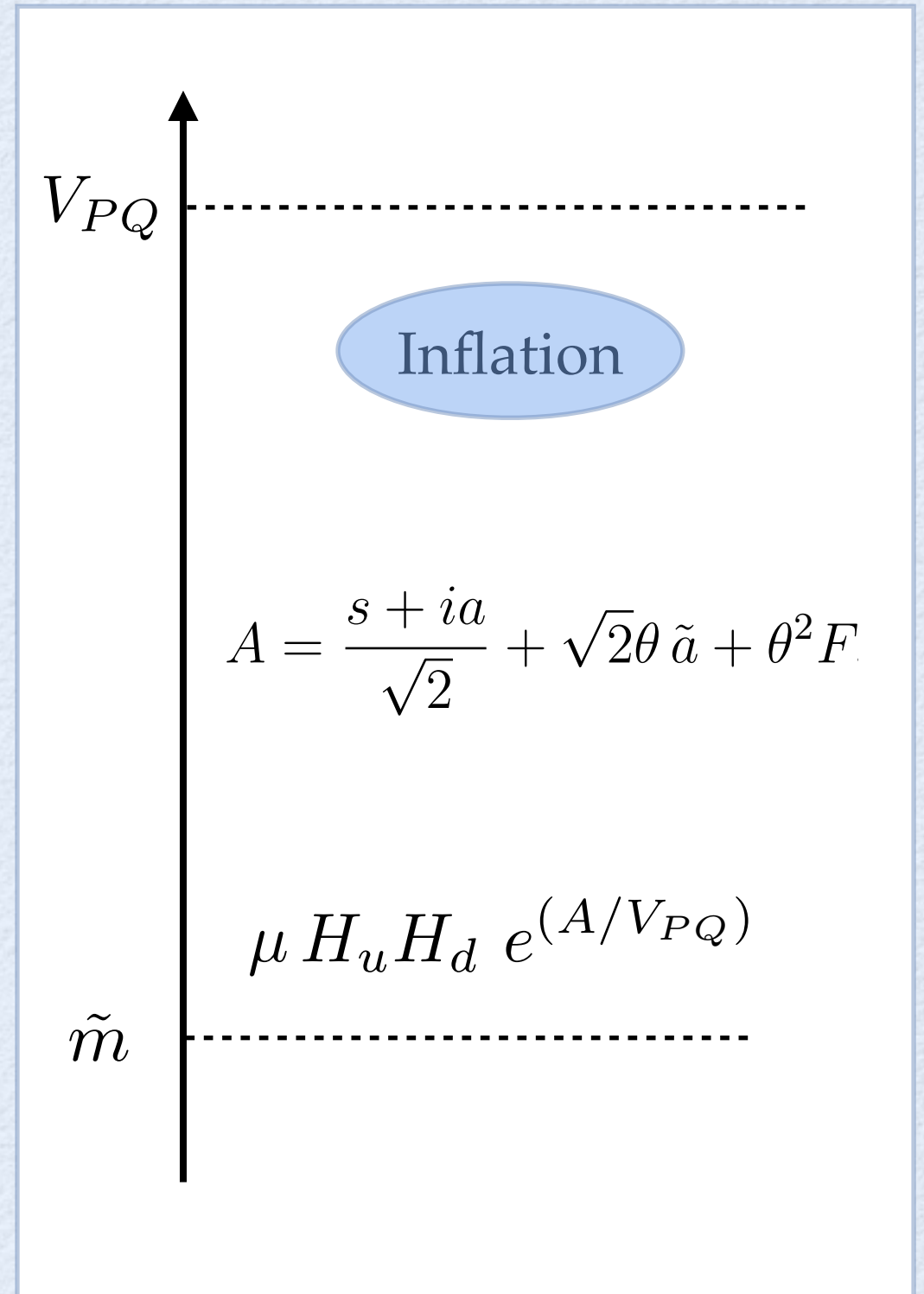
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- Condensate decays late to Higgs bosons

A Feynman diagram showing a scalar particle s decaying into two Higgs bosons h . The diagram consists of a horizontal dashed line on the left labeled s . This line connects to a triangular loop of top quarks (t). The top quark is represented by a solid line with an arrow indicating its flow. The loop is closed by a vertical dashed line on the right, which then splits into two outgoing dashed lines labeled h . Below the diagram is the label $(s \rightarrow \tilde{h} \tilde{h})$.

$$\frac{\mu^2}{V_{PQ}}$$

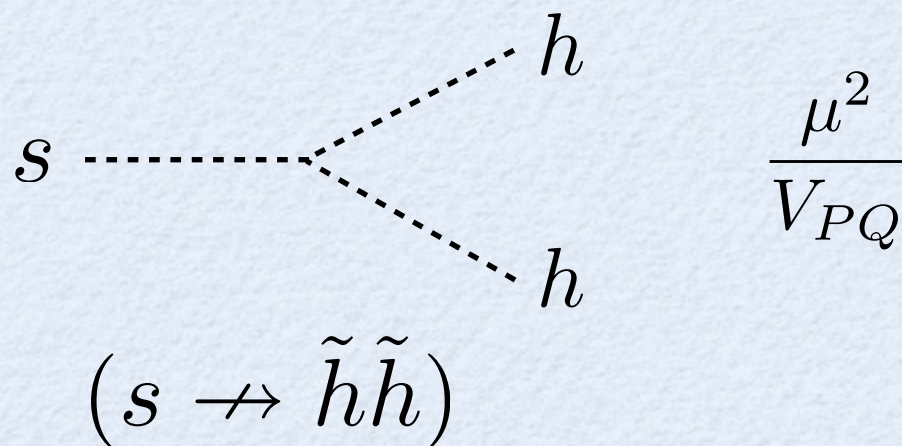


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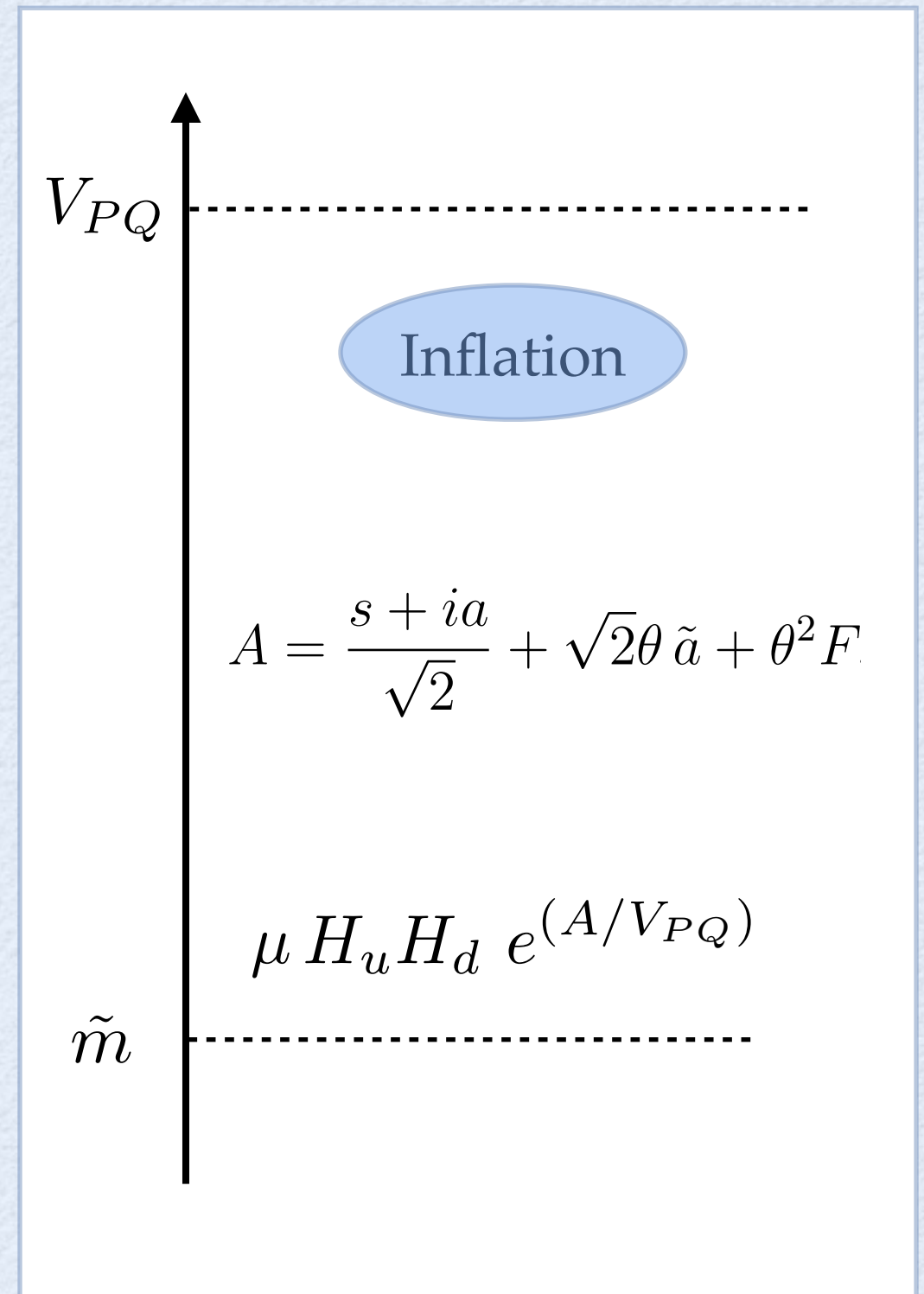
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$$\frac{\mu^2}{V_{PQ}}$$

$(s \rightarrow \tilde{h}\tilde{h})$

Everything changes!!



Warnings

- Saxion Condensate is Not New!

Hashimoto, Izawa, Yamaguchi, Yanagida hep-ph/9803263

...
Kawasaki, Nakayama arXiv:0802.2487

...

Baer, Lessa, Sreethawong arXiv:1110.2491

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Under-appreciated; Complex; Much still to do

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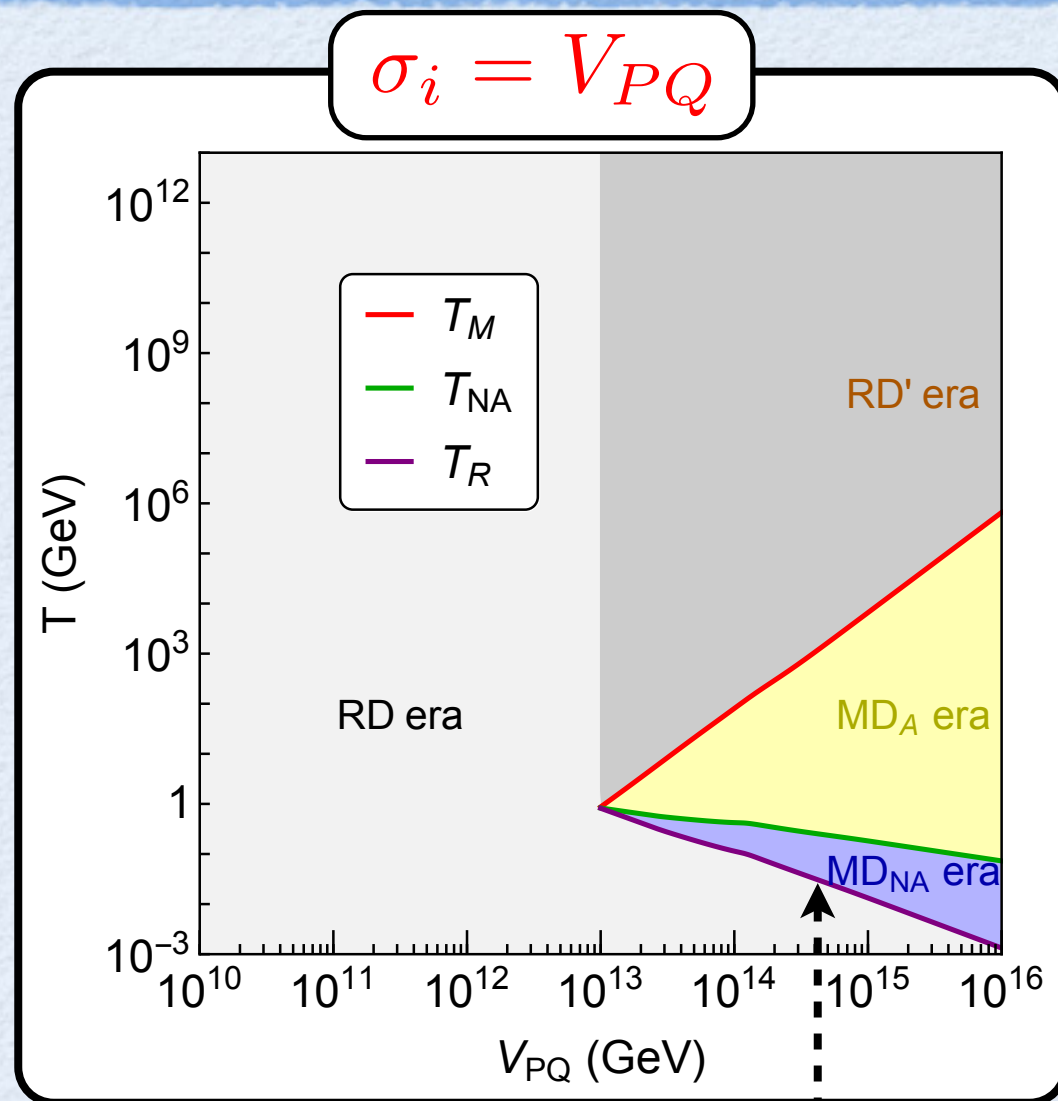
- Suppressed Parameters!

$$\mu, M_i, m_s \sim \mathcal{O}(\text{TeV})$$

$$N_{DW} \sim \mathcal{O}(10)$$

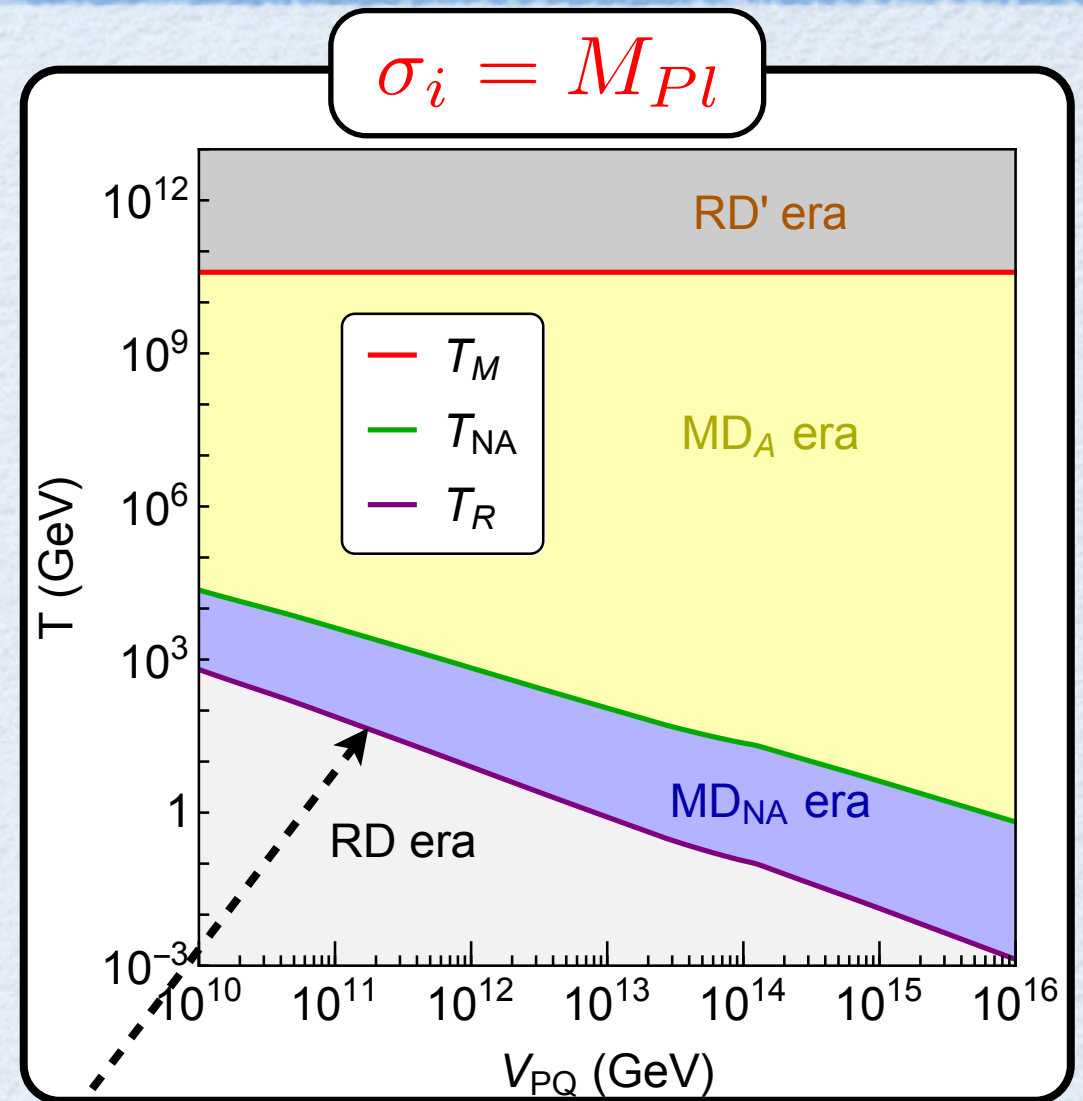
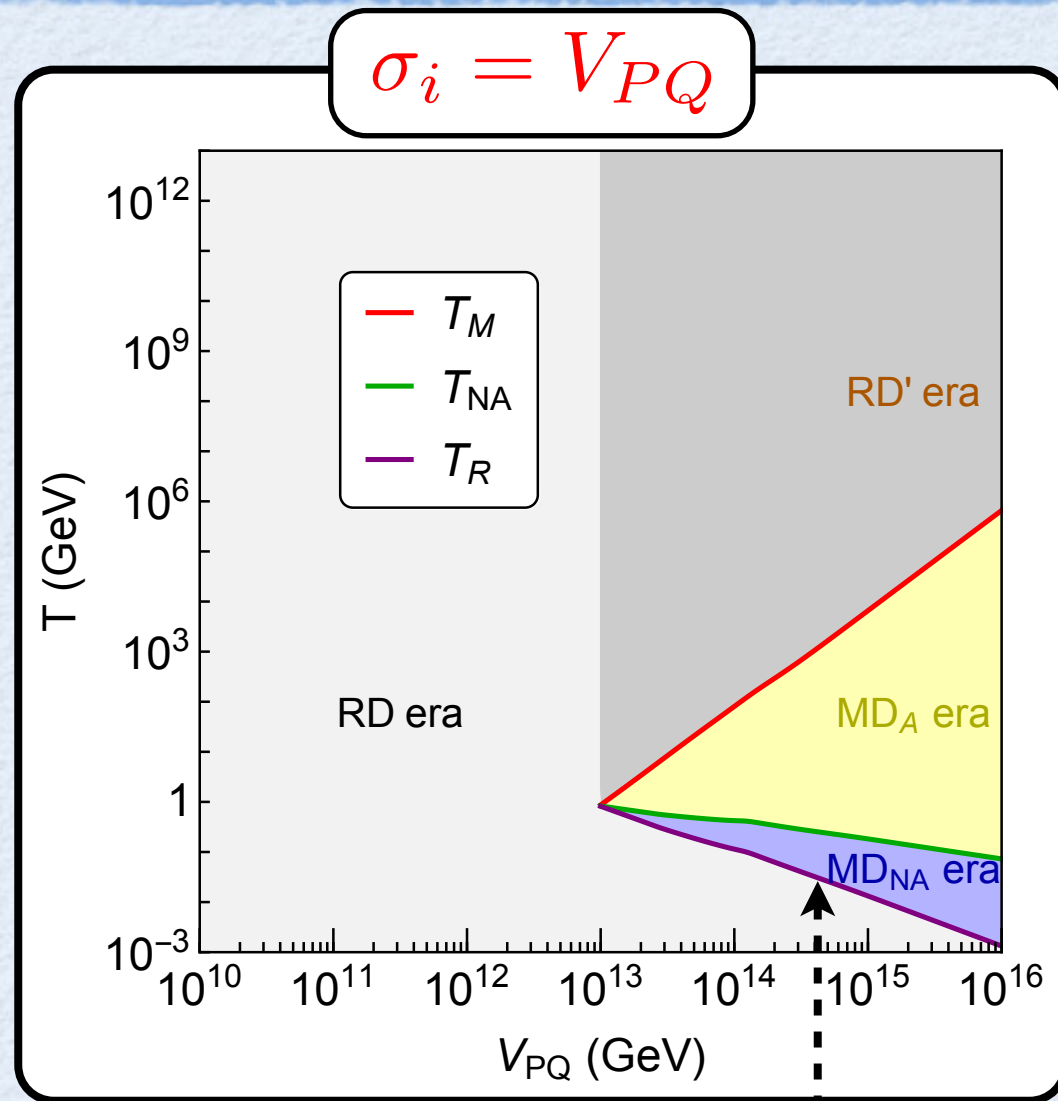
$$q_\mu \sim \mathcal{O}(1)$$

A Saxion Matter Dominated Era



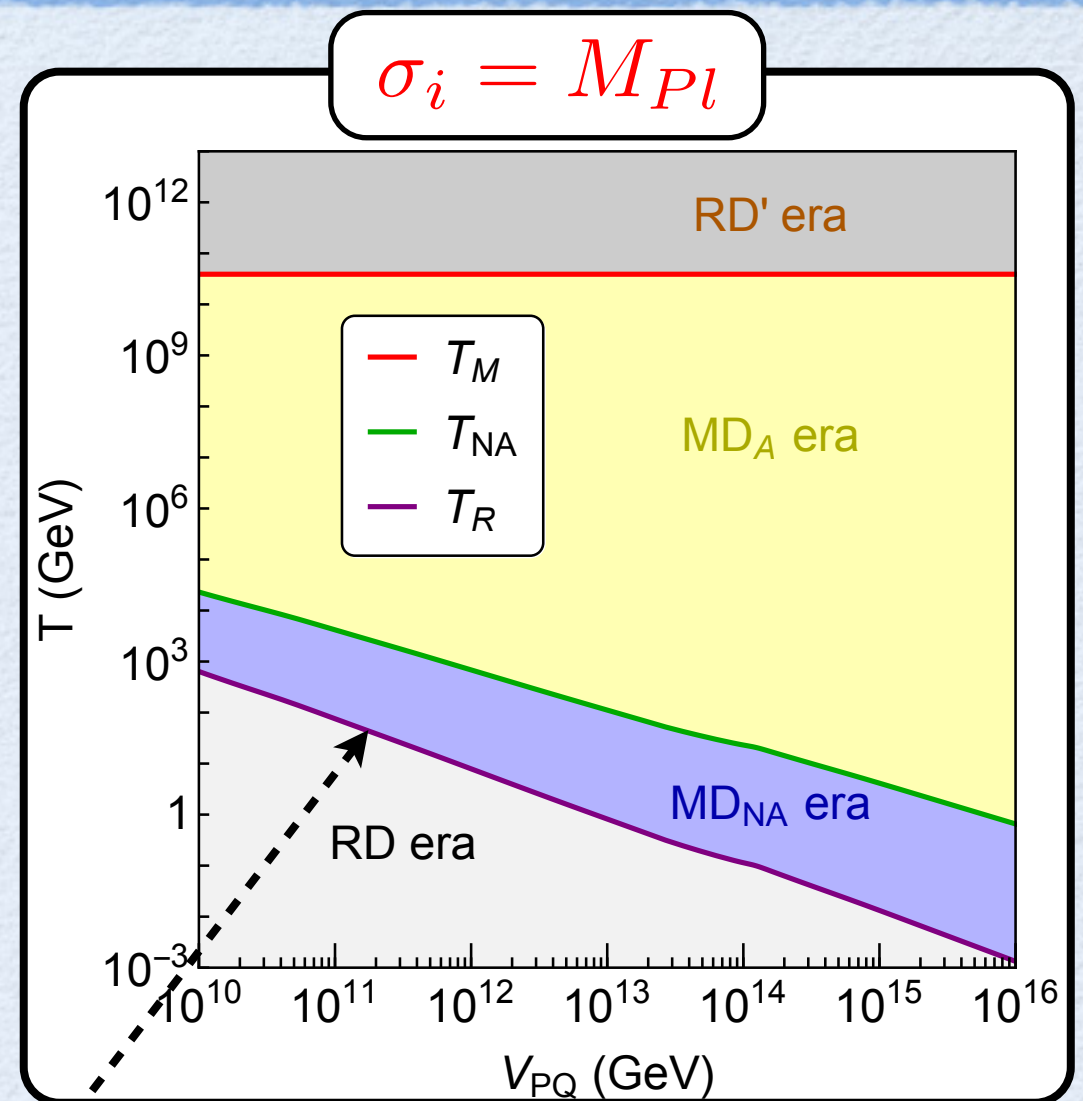
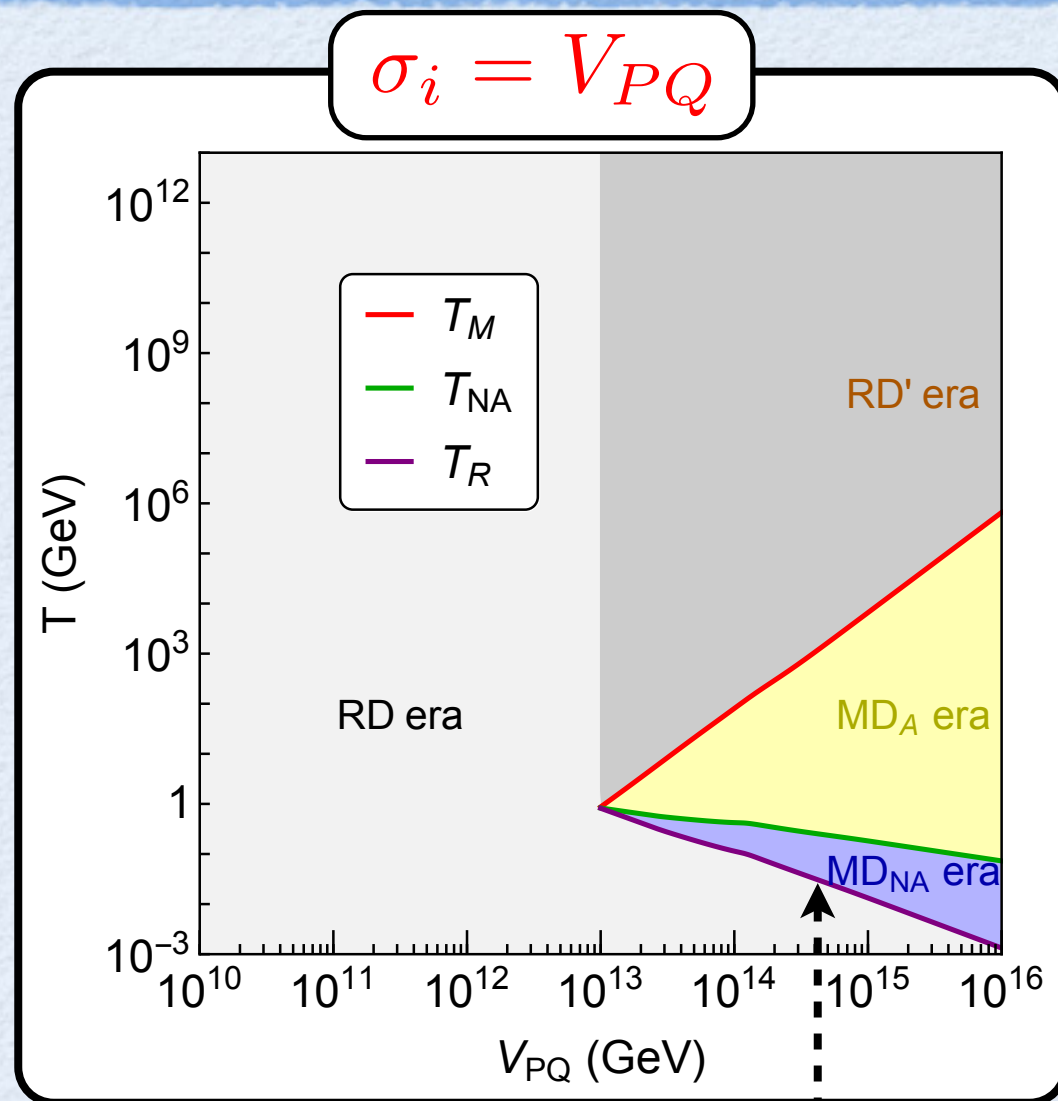
DFSZ: $s \rightarrow hh$

A Saxion Matter Dominated Era



DFSZ: $s \rightarrow hh$

A Saxion Matter Dominated Era



DFSZ: $s \rightarrow hh$

$$T_R \simeq 10 \text{ MeV } q_\mu \left(\frac{10.75}{g_*(T_R)} \right)^{\frac{1}{4}} \left(\frac{\mathcal{D}}{4} \right)^{\frac{1}{2}} \left(\frac{\mu}{1 \text{ TeV}} \right)^{\frac{3}{2}} \left(\frac{\mu}{m_s} \right)^{\frac{1}{2}} \left(\frac{10^{15} \text{ GeV}}{V_{PQ}} \right)$$

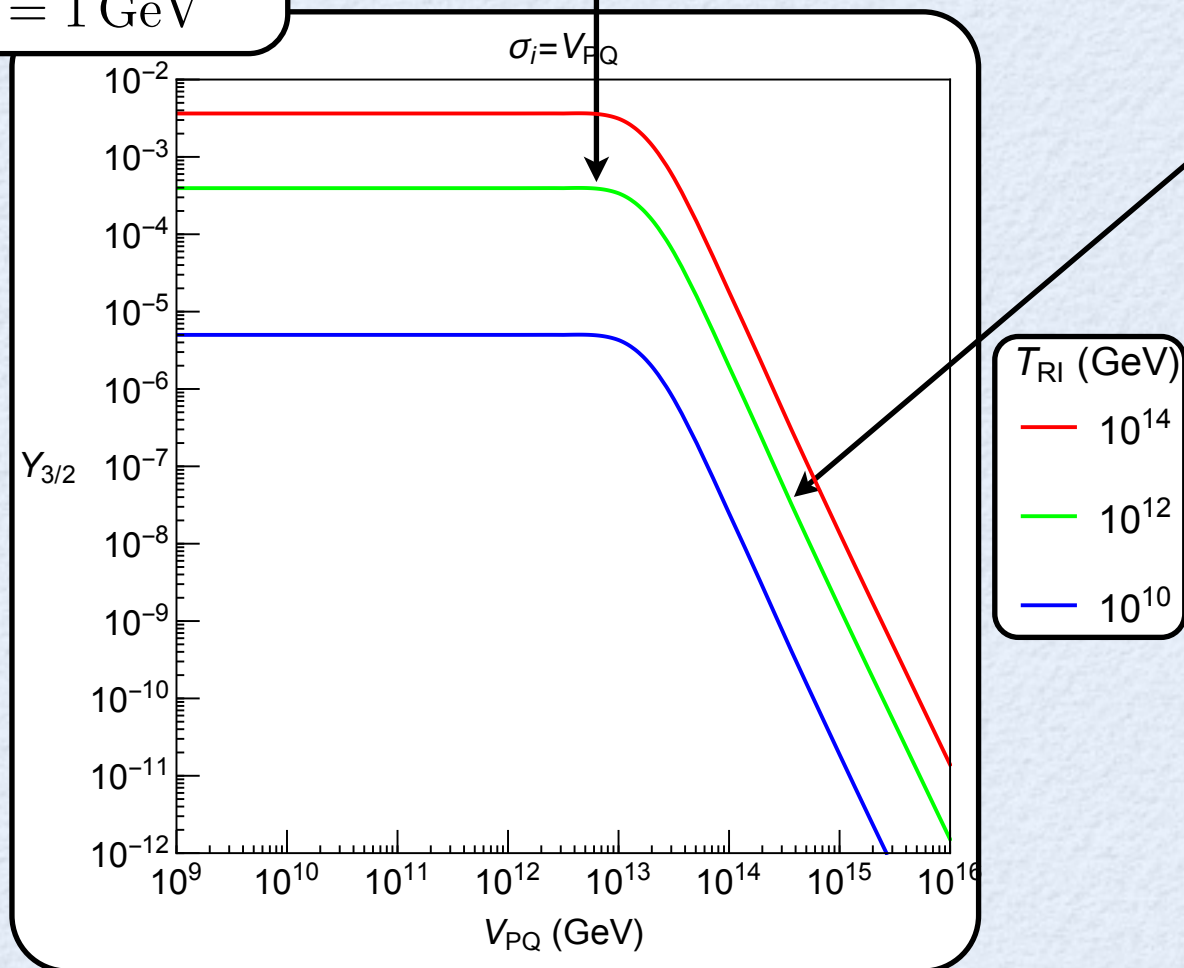
Gravitino Problem Solved

$$Y_{3/2}^{UV} = 6.11 \times 10^{-12} \frac{T_{RI}}{10^{10} \text{ GeV}} \sum_i \gamma_i(T_{RI}) \left(1 + \frac{m_i^2}{3m_{3/2}^2} \right)$$

No Dilution

$$\sigma_i = V_{PQ}$$

$m_{3/2} = 1 \text{ GeV}$



Large Dilution

$$D \propto \sigma_i^2 V_{PQ}$$

$$Y_{3/2} \propto \frac{1}{m_{3/2}^2}$$

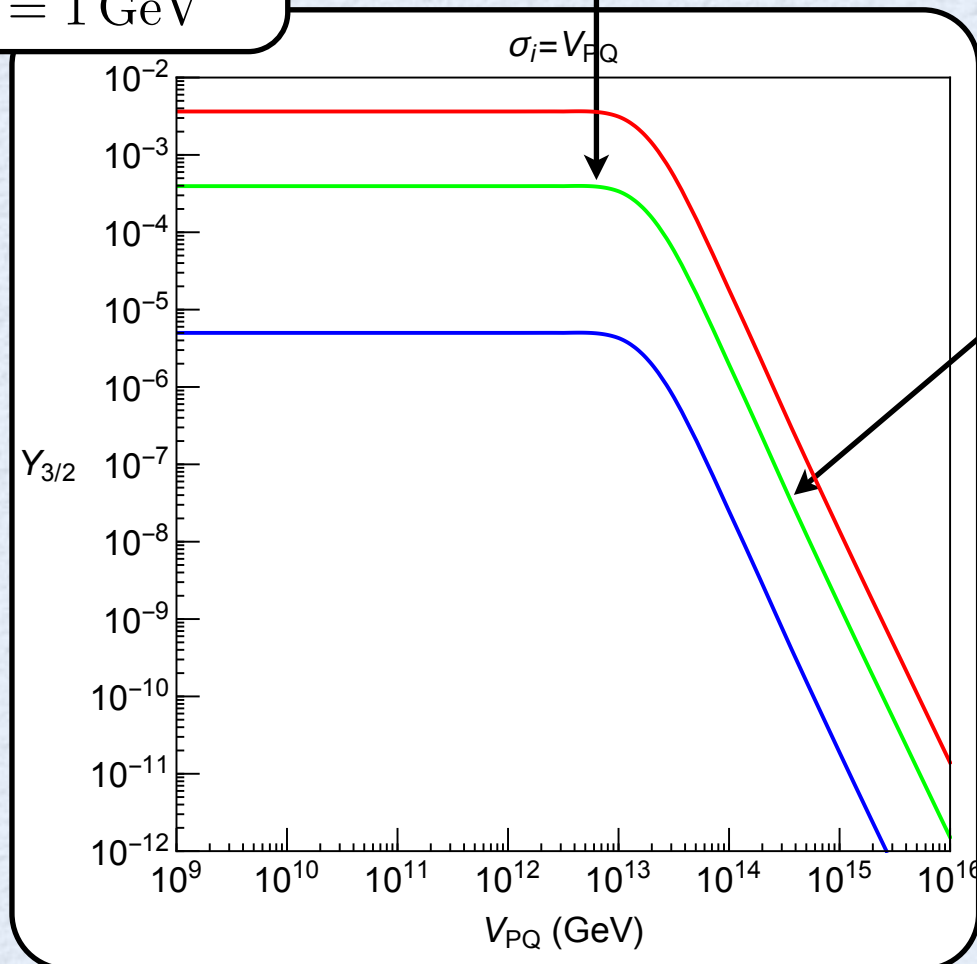
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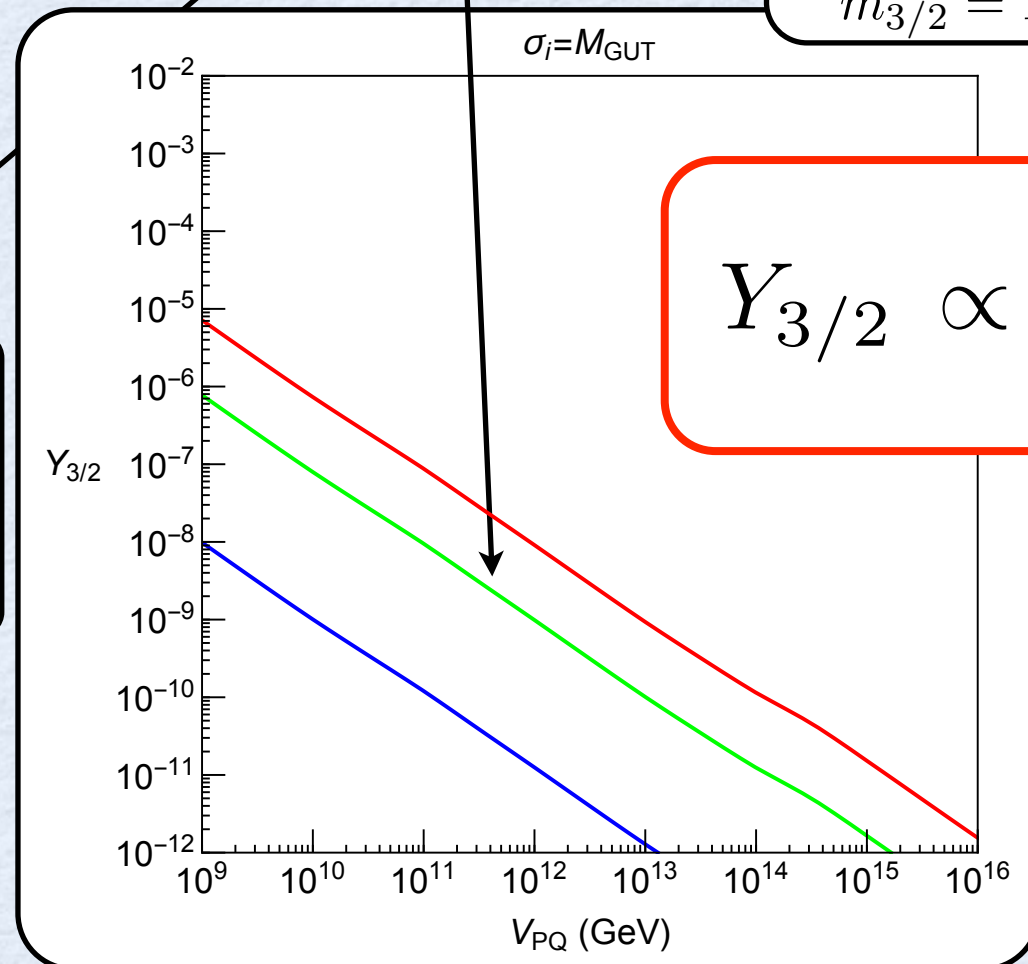


Large Dilution

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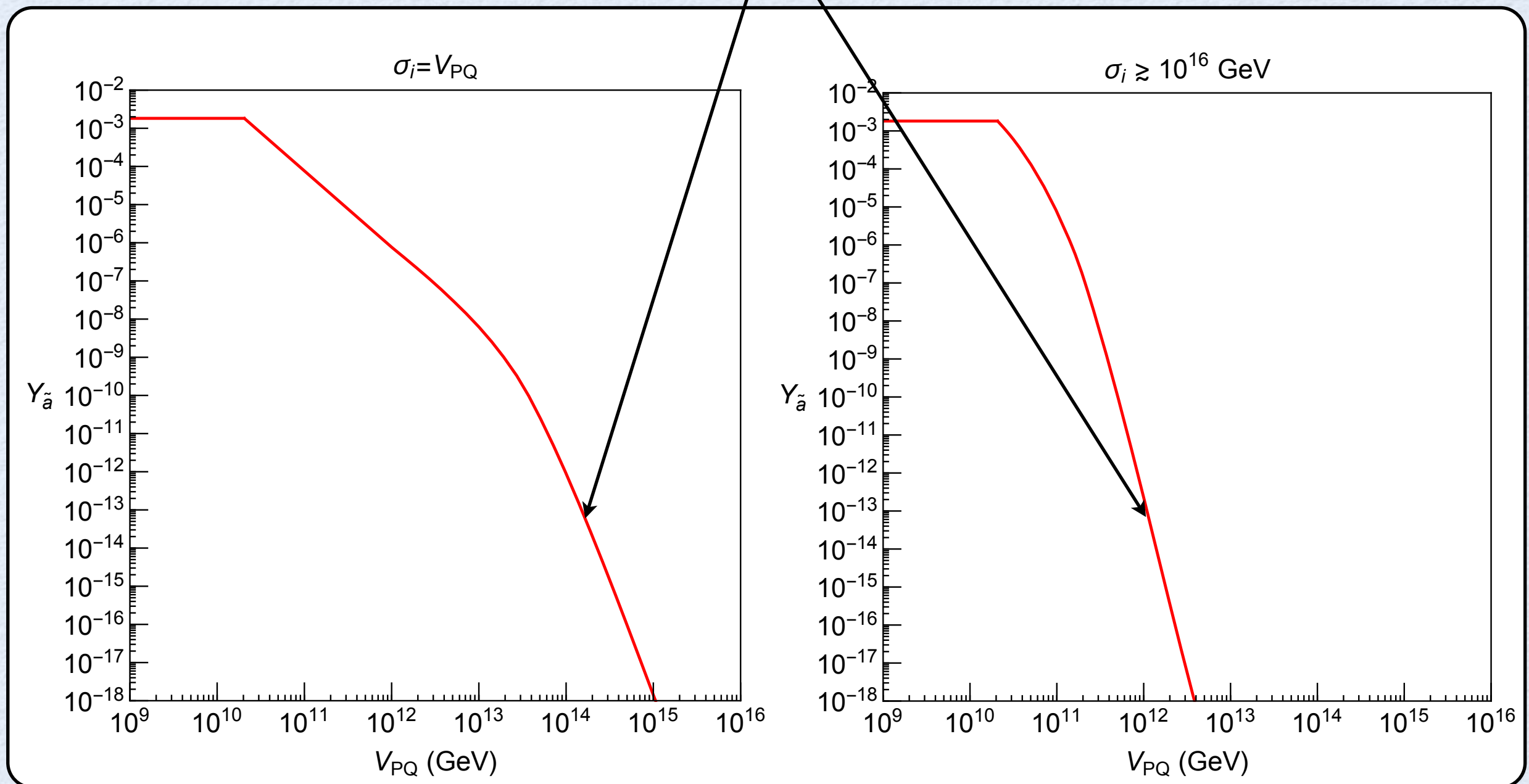
$$\sigma_i = M_{GUT}$$

$$m_{3/2} = 1 \text{ GeV}$$



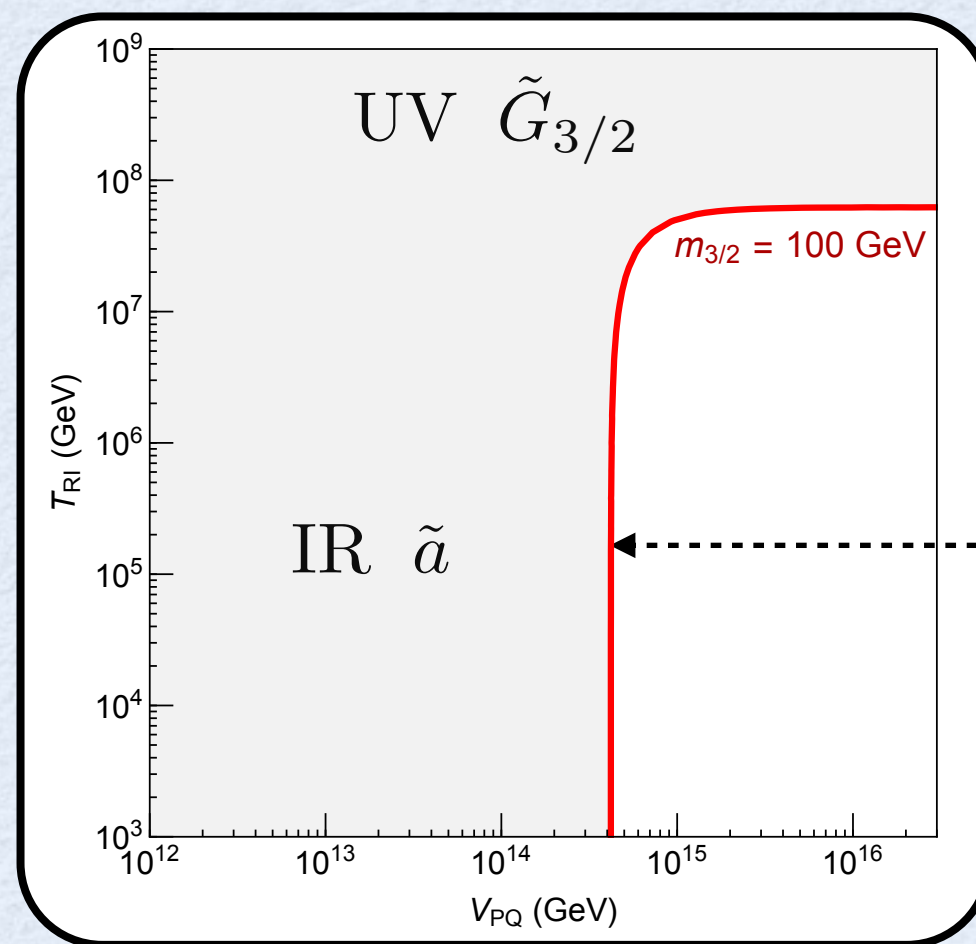
Axino Freeze-In Problem Solved

Large Dilution



High Scale Mediation

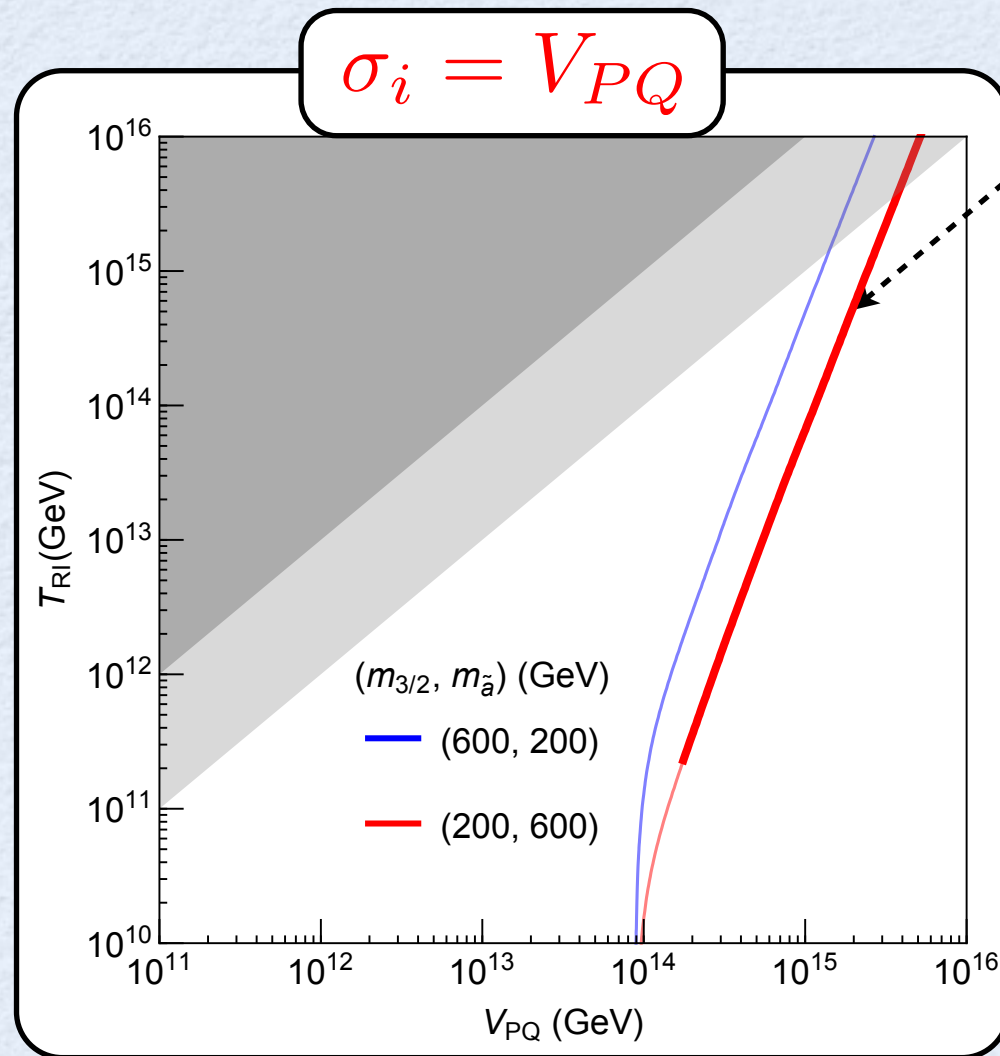
Gravitino/Axino DM



Expect saxion condensate
opens up high T_{RI}

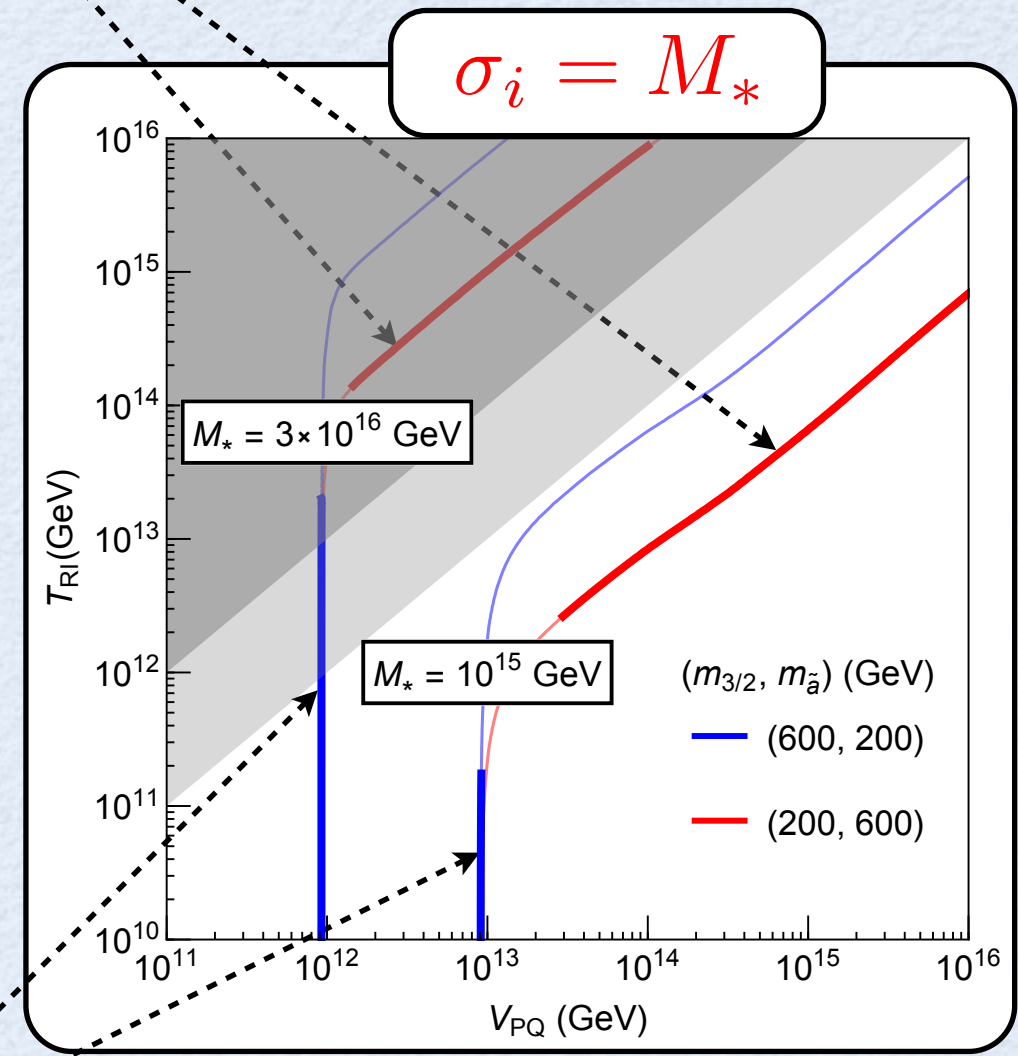
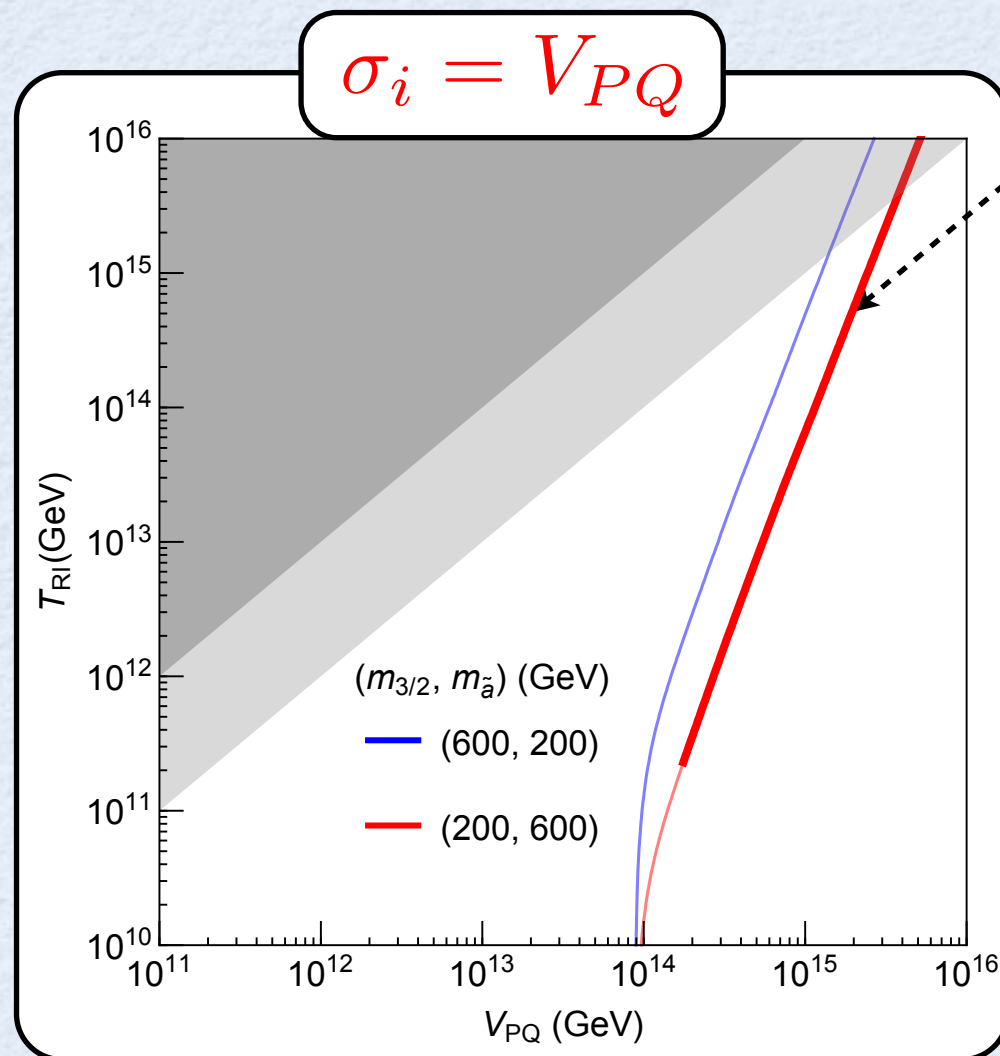
High Scale Mediation

Gravitino DM from UV scattering



High Scale Mediation

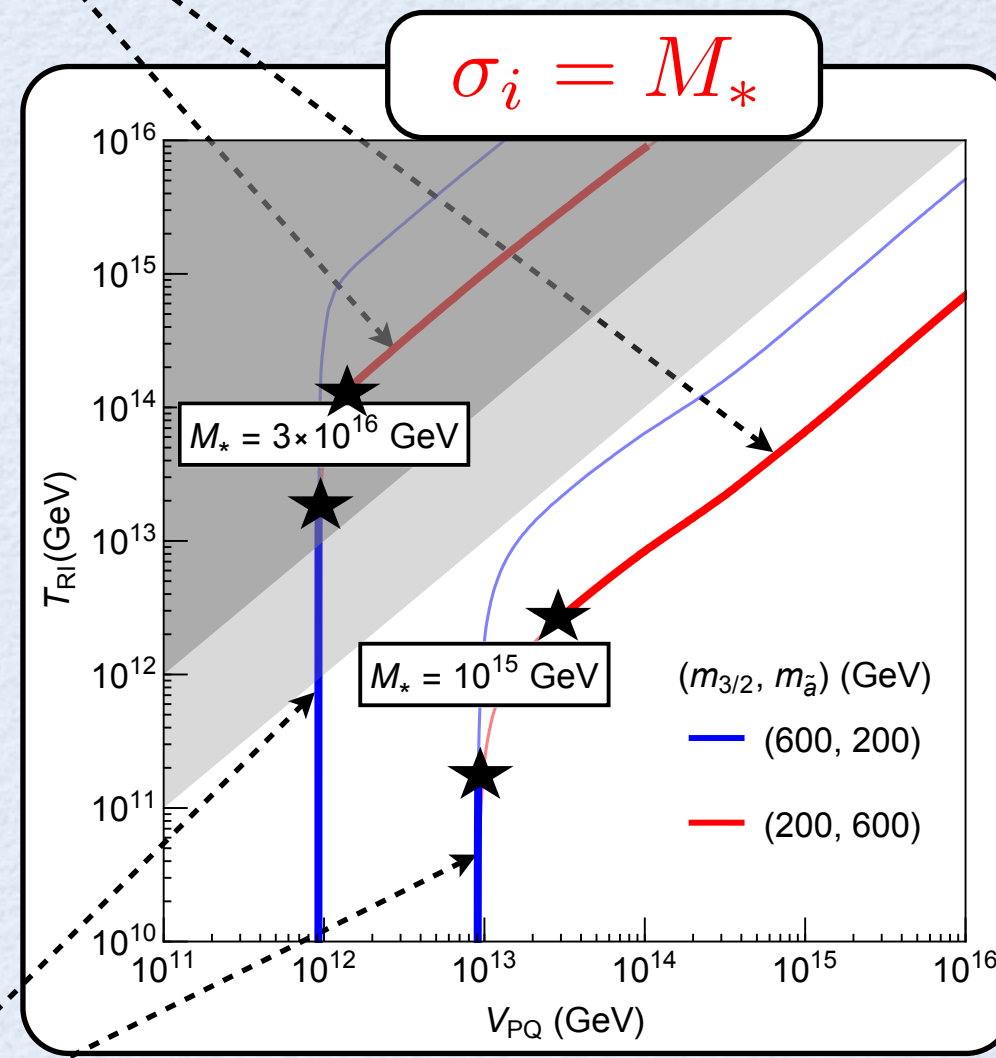
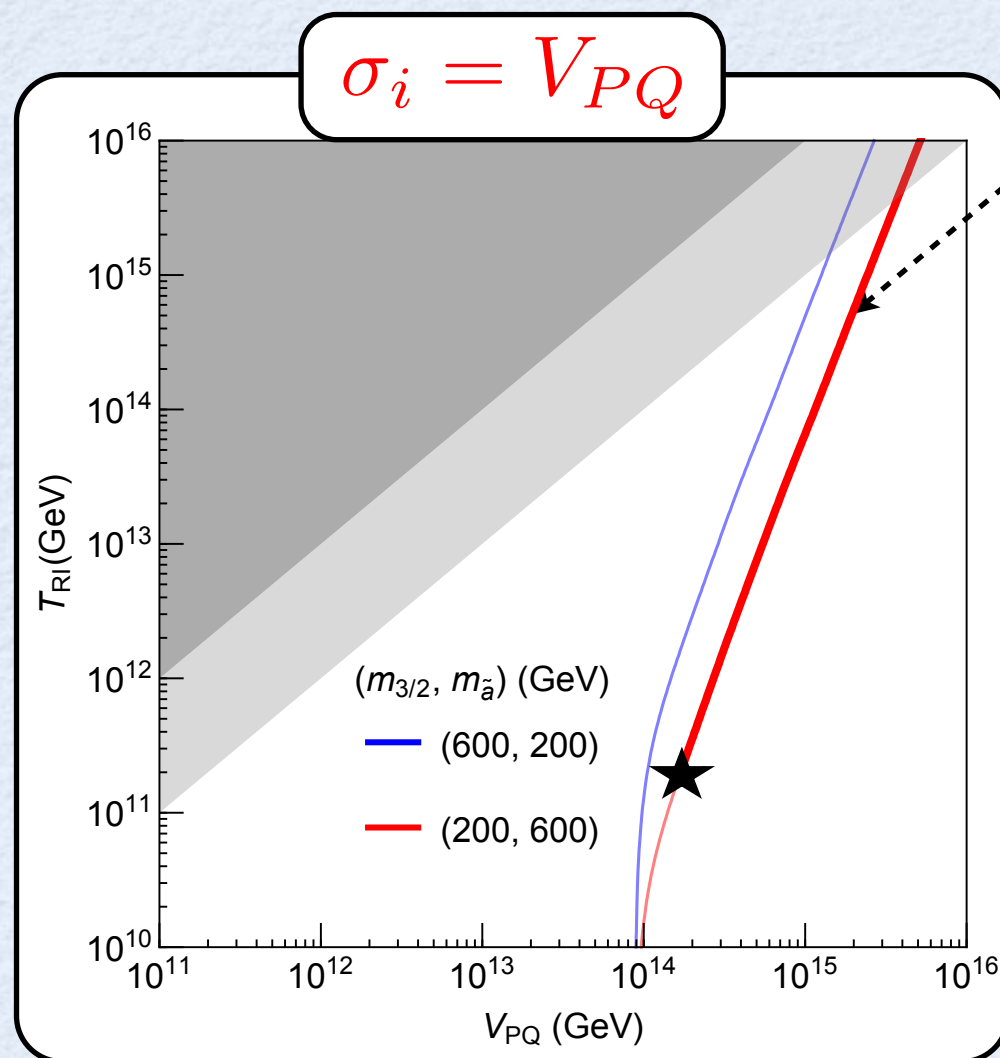
Gravitino DM from UV scattering



Axino DM from Freeze-In

High Scale Mediation

Gravitino DM from UV scattering



Axino DM from Freeze-In

★ A warm sub-dominant component

Displaced Vertices at Colliders

High Scale Mediation

Axino DM from Freeze-In

Neutralino LOSP

$$\tilde{\chi} \rightarrow \tilde{a} + (h/Z)$$

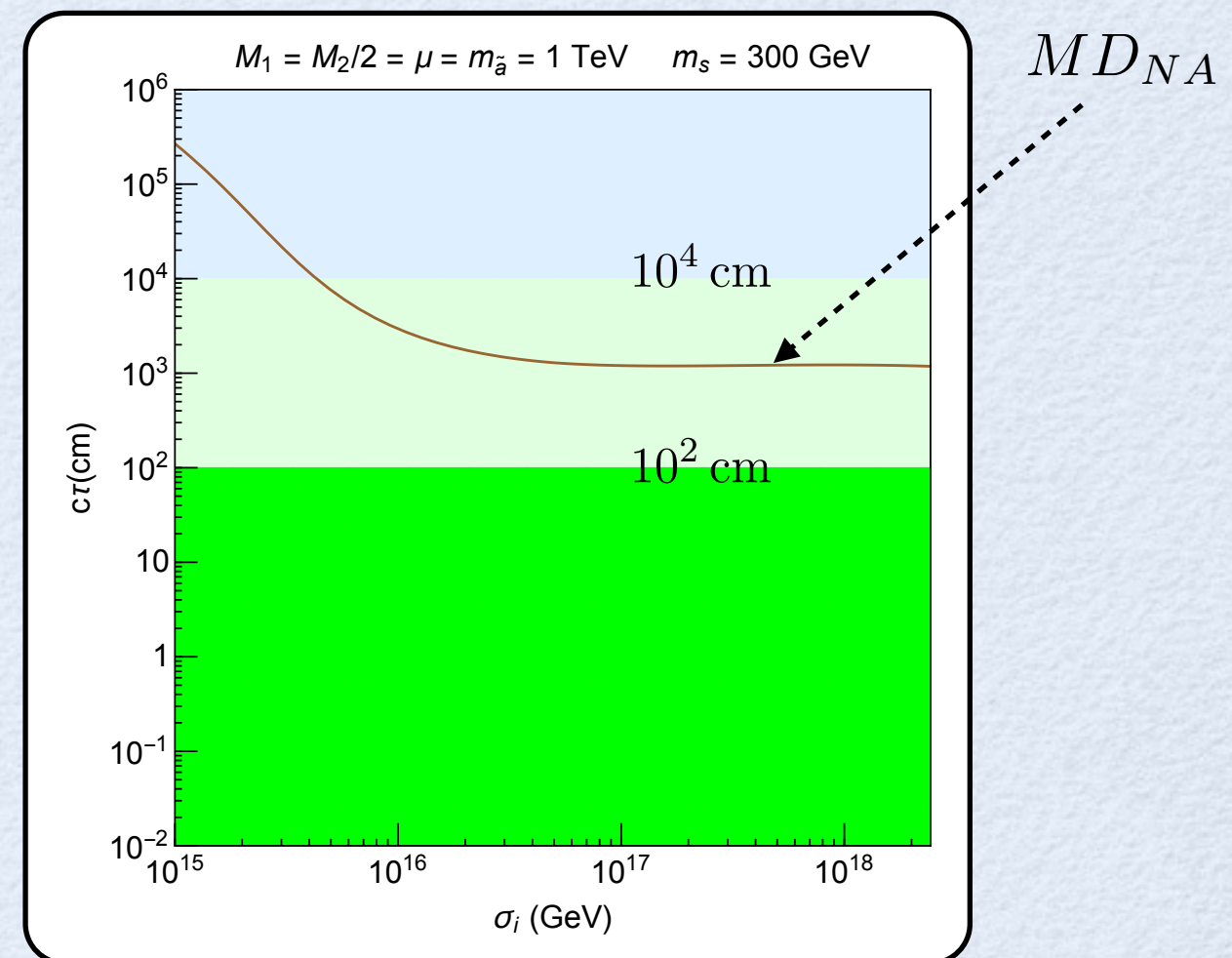
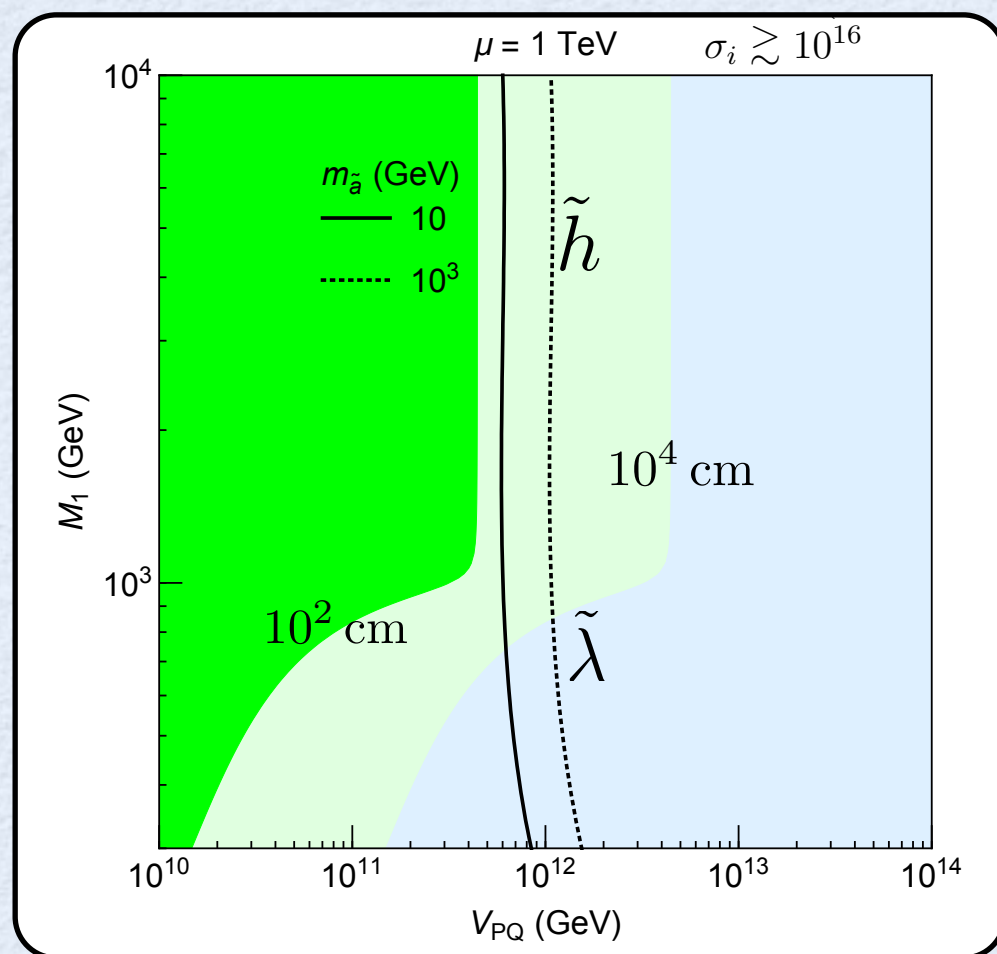
Displaced Vertices at Colliders

High Scale Mediation

Axino DM from Freeze-In

Neutralino LOSP

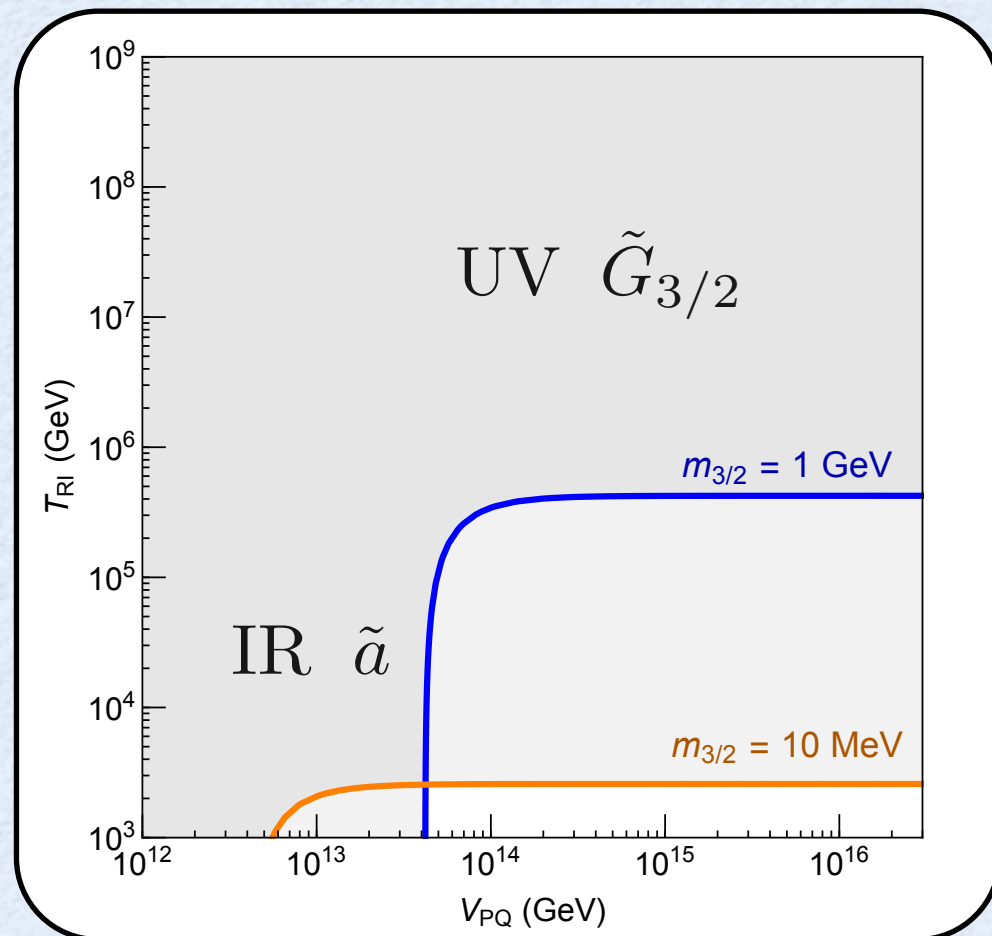
$$\tilde{\chi} \rightarrow \tilde{a} + (h/Z)$$



More generally: Co, D'Eramo, Hall, Pappadopulo arXiv:1506.07532

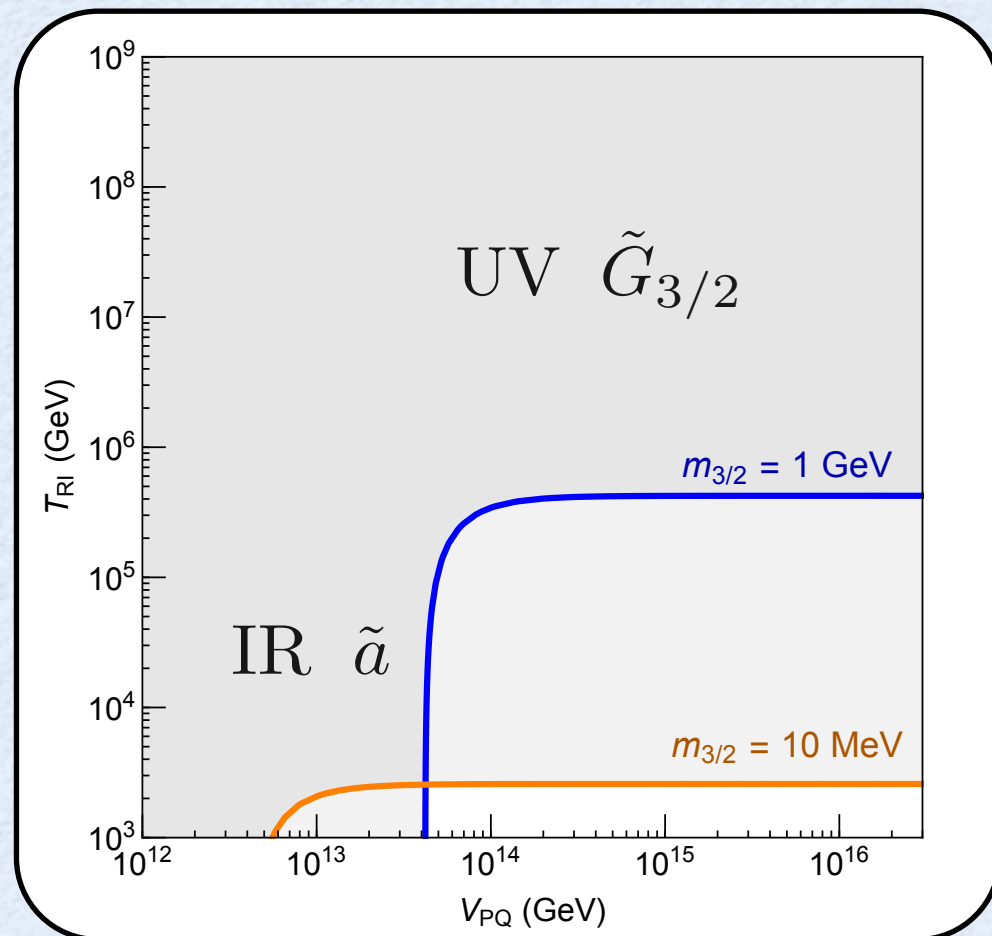
Low Scale Mediation

No Dilution



Low Scale Mediation

No Dilution



Conventional displaced vertex signal

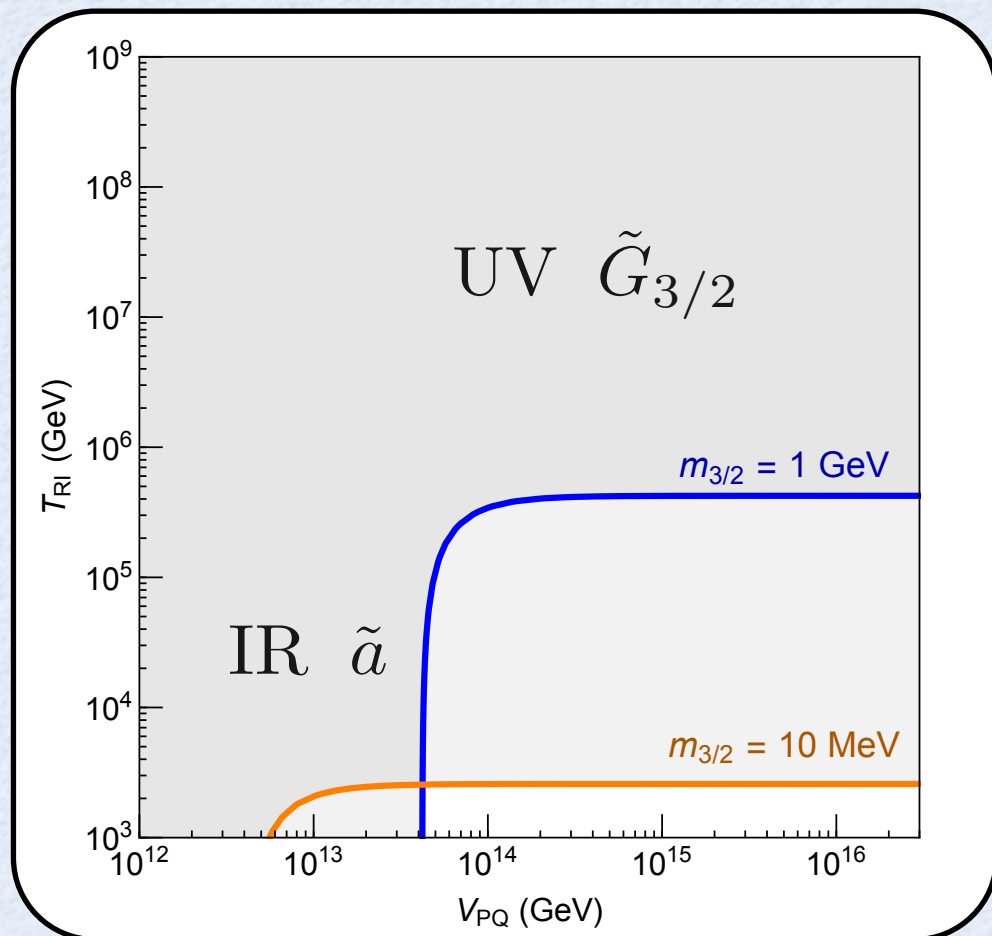
$$\text{LOSP} \rightarrow \tilde{G}_{3/2}$$

requires $m_{3/2} \leq \text{MeV}$

What is the cosmology?

Low Scale Mediation

No Dilution

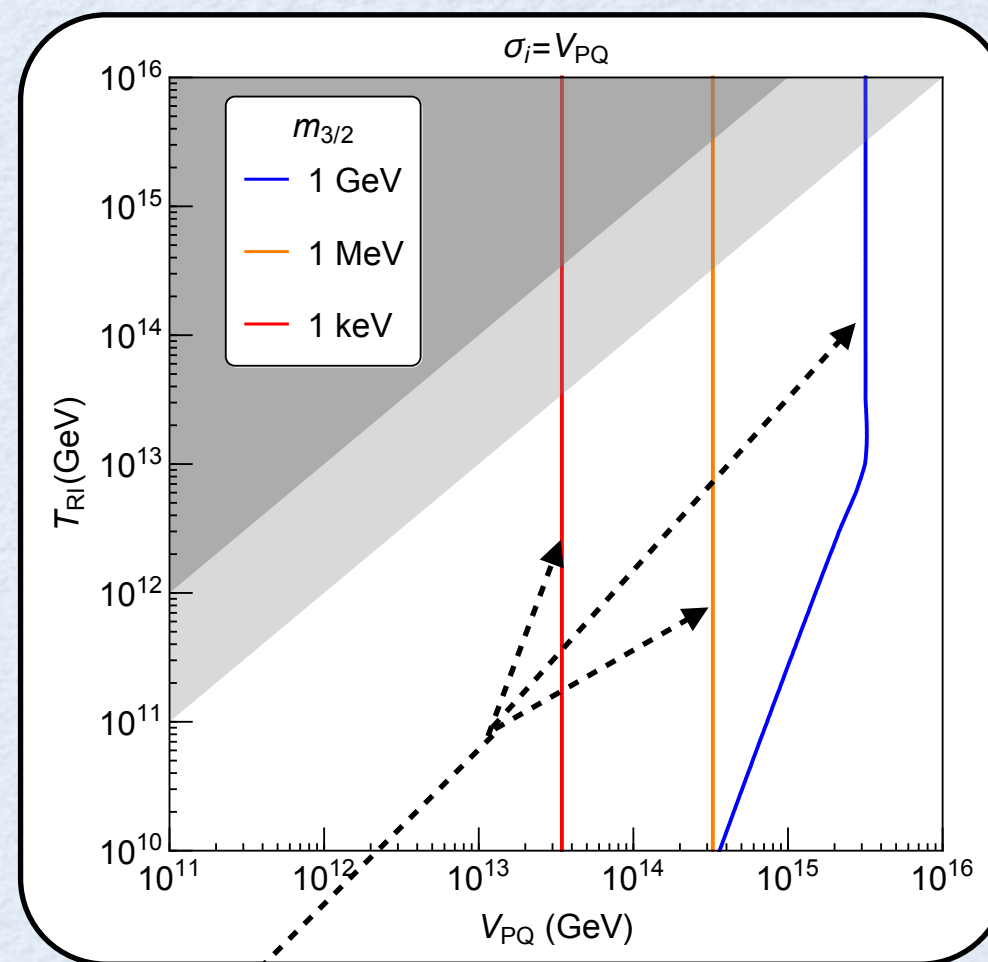


Conventional displaced vertex signal

LOSP $\rightarrow \tilde{G}_{3/2}$
requires $m_{3/2} \leq \text{MeV}$

What is the cosmology?

Saxion Condensate



UV $\tilde{G}_{3/2}$ thermalize

Dilution gives:
 $V_{PQ} \sim 10^{14}$ GeV

IR \tilde{a} negligible

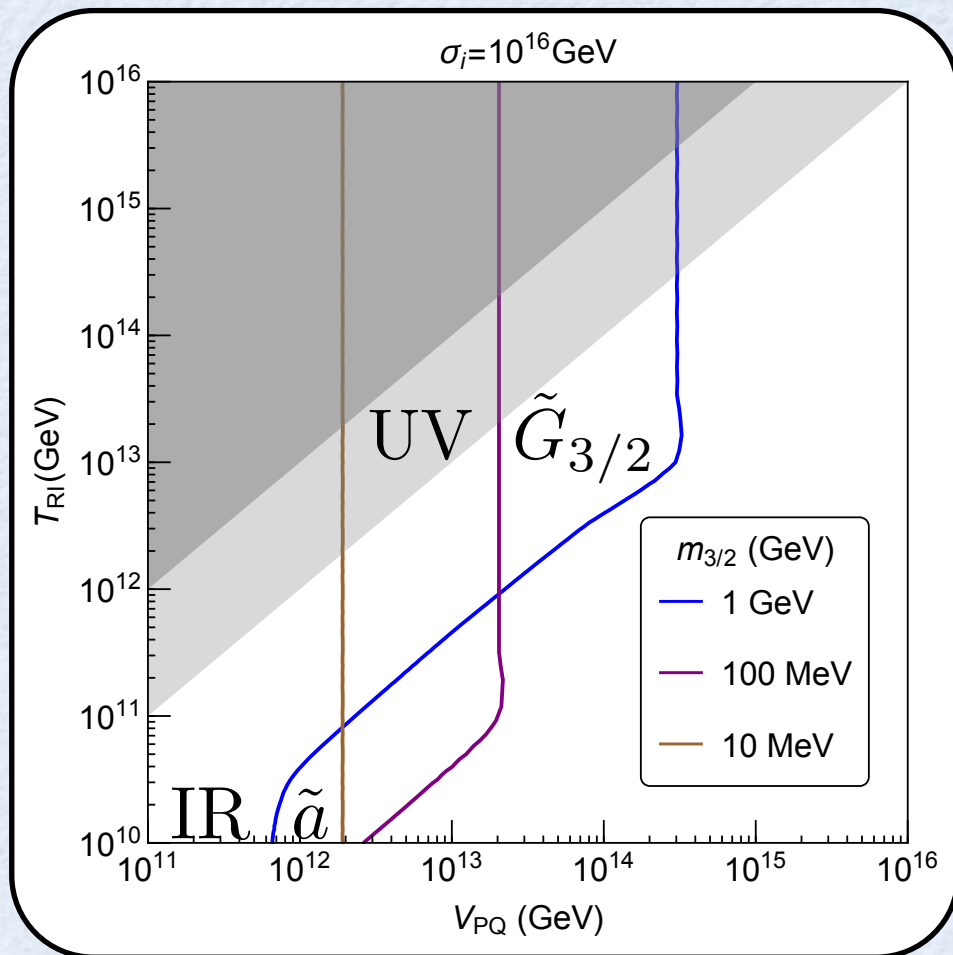
LOSP $\rightarrow \tilde{G}_{3/2}$

$T_{RI} \leq 10^{14}$ GeV

Low Scale Mediation

Larger Saxion Condensate

→ Lower V_{PQ}

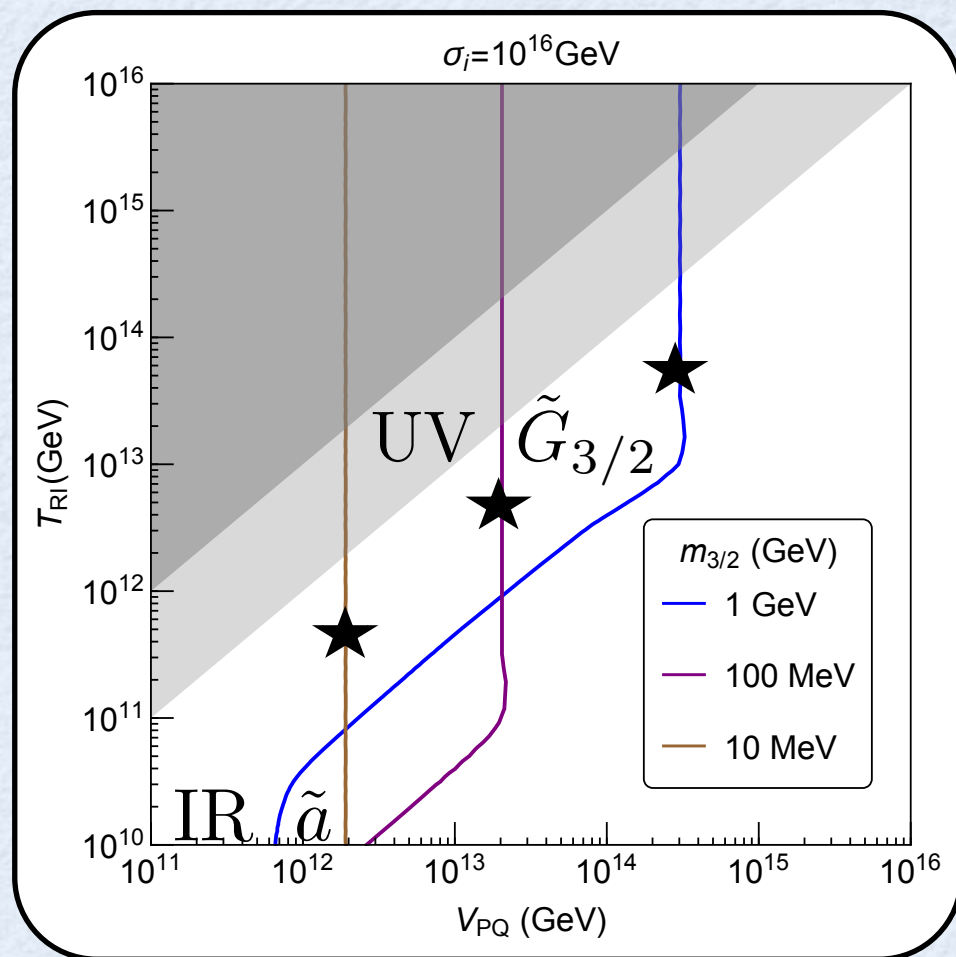


Lower V_{PQ} → LOSP → \tilde{a}

Low Scale Mediation

Larger Saxion Condensate

→ Lower V_{PQ}



Lower V_{PQ} → LOSP → \tilde{a}

★ UV $\tilde{G}_{3/2}$ thermalize

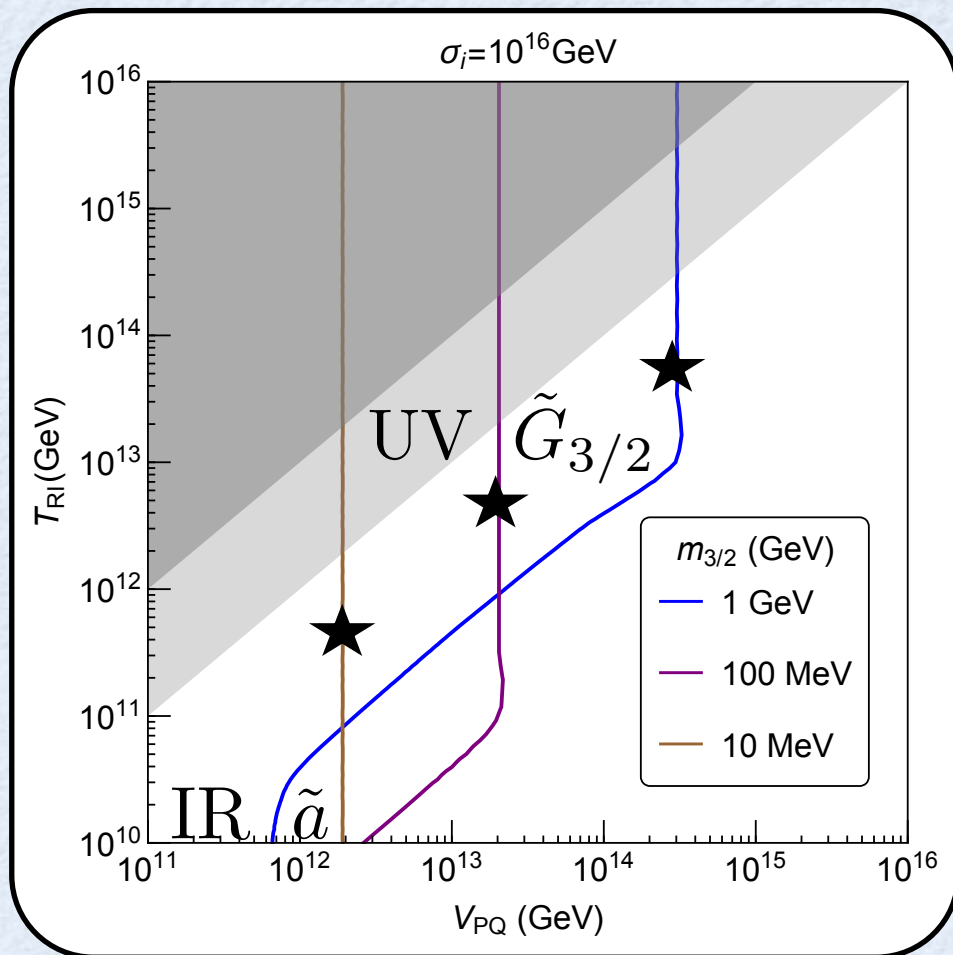
$$\Omega h^2(\sigma_i, V_{PQ}, m_{3/2})$$

Low Scale Mediation

Larger Saxion Condensate

→ Lower V_{PQ}

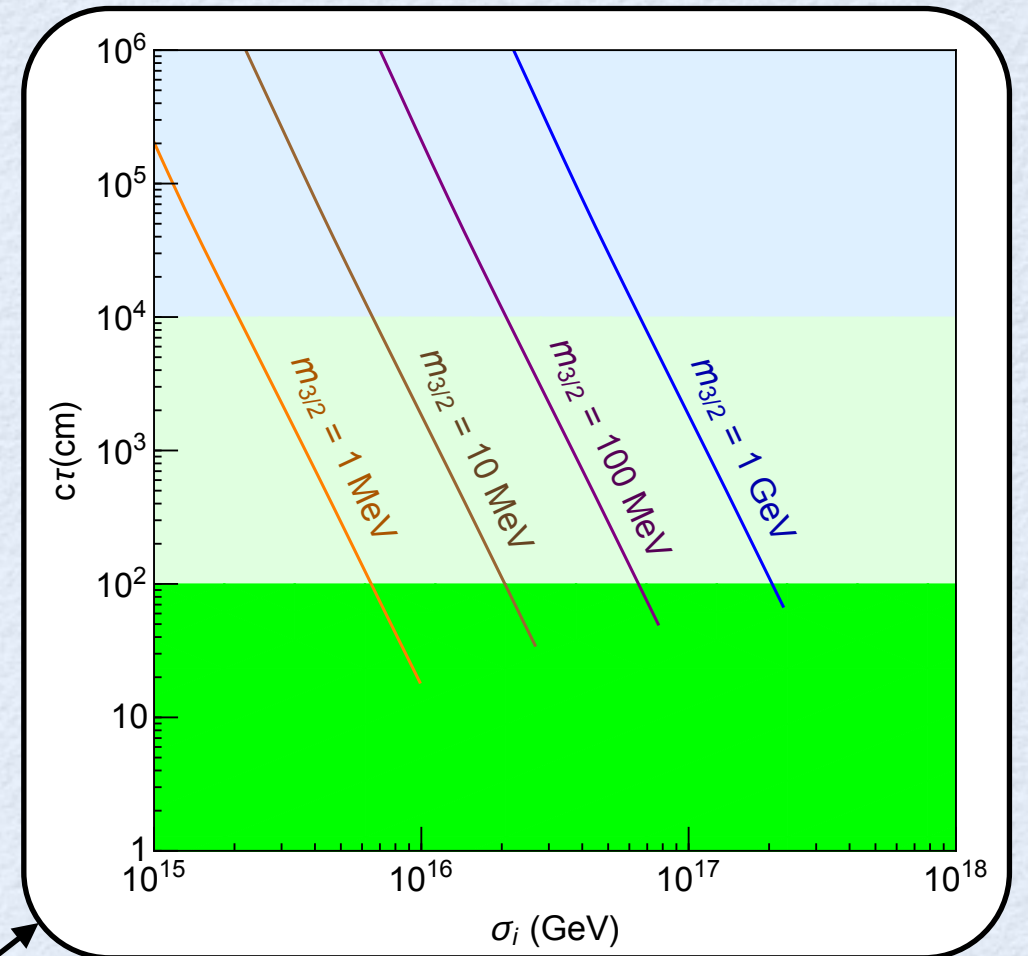
Higgsino-like LOSP lifetime



Lower V_{PQ} → LOSP → \tilde{a}

★ UV $\tilde{G}_{3/2}$ thermalize

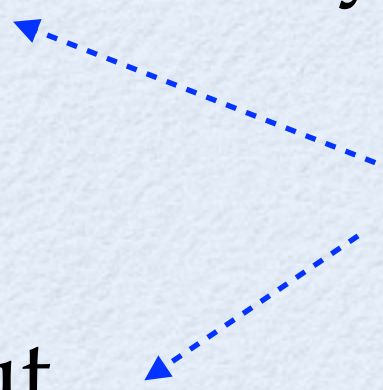
$$\Omega h^2(\sigma_i, V_{PQ}, m_{3/2})$$



Even smaller lifetimes for lower T_{RI}
where $\tilde{G}_{3/2}$ not thermalized

LSP Neutralino Dark Matter

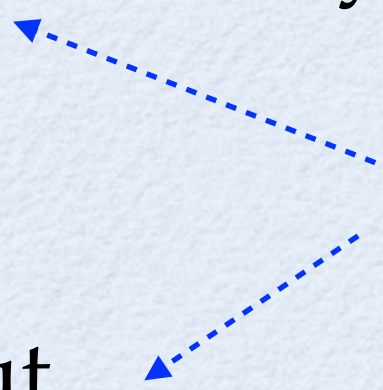
Two production mechanisms:

- \tilde{a} Freeze-In and Decay to LSP
 - LSP Freeze-Out
- typically over-produce
- 
- ```
graph LR; A[typically over-produce] -.-> B[● \tilde{a} Freeze-In and Decay to LSP]; A -.-> C[● LSP Freeze-Out]
```



# LSP Neutralino Dark Matter

Two production mechanisms:

- $\tilde{a}$  Freeze-In and Decay to LSP
  - LSP Freeze-Out
- typically over-produce
- 

+ Saxion Dilution



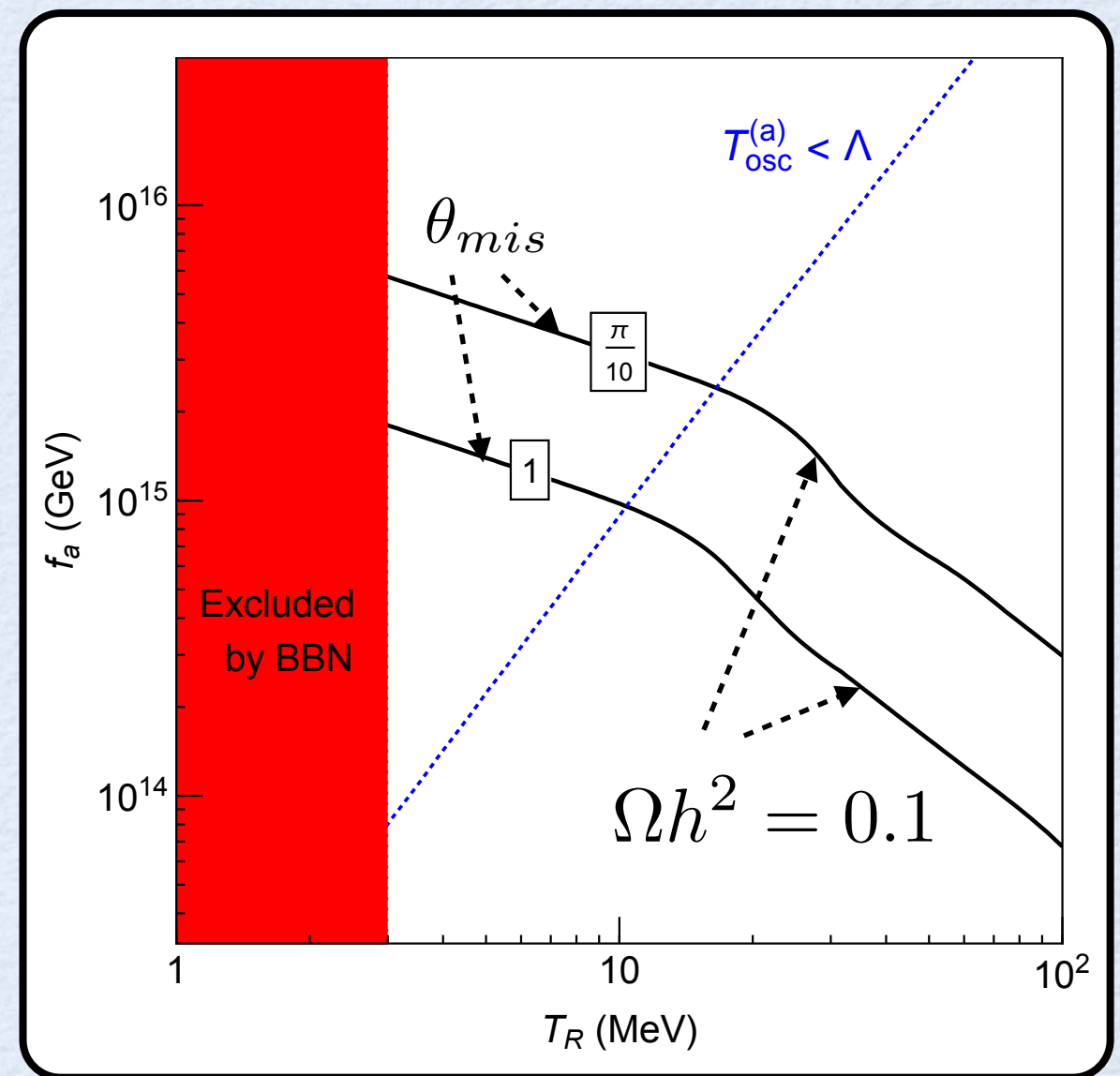
# Misalignment Axion DM at Large $V_{PQ}$

- Axion field oscillates during saxion MD era
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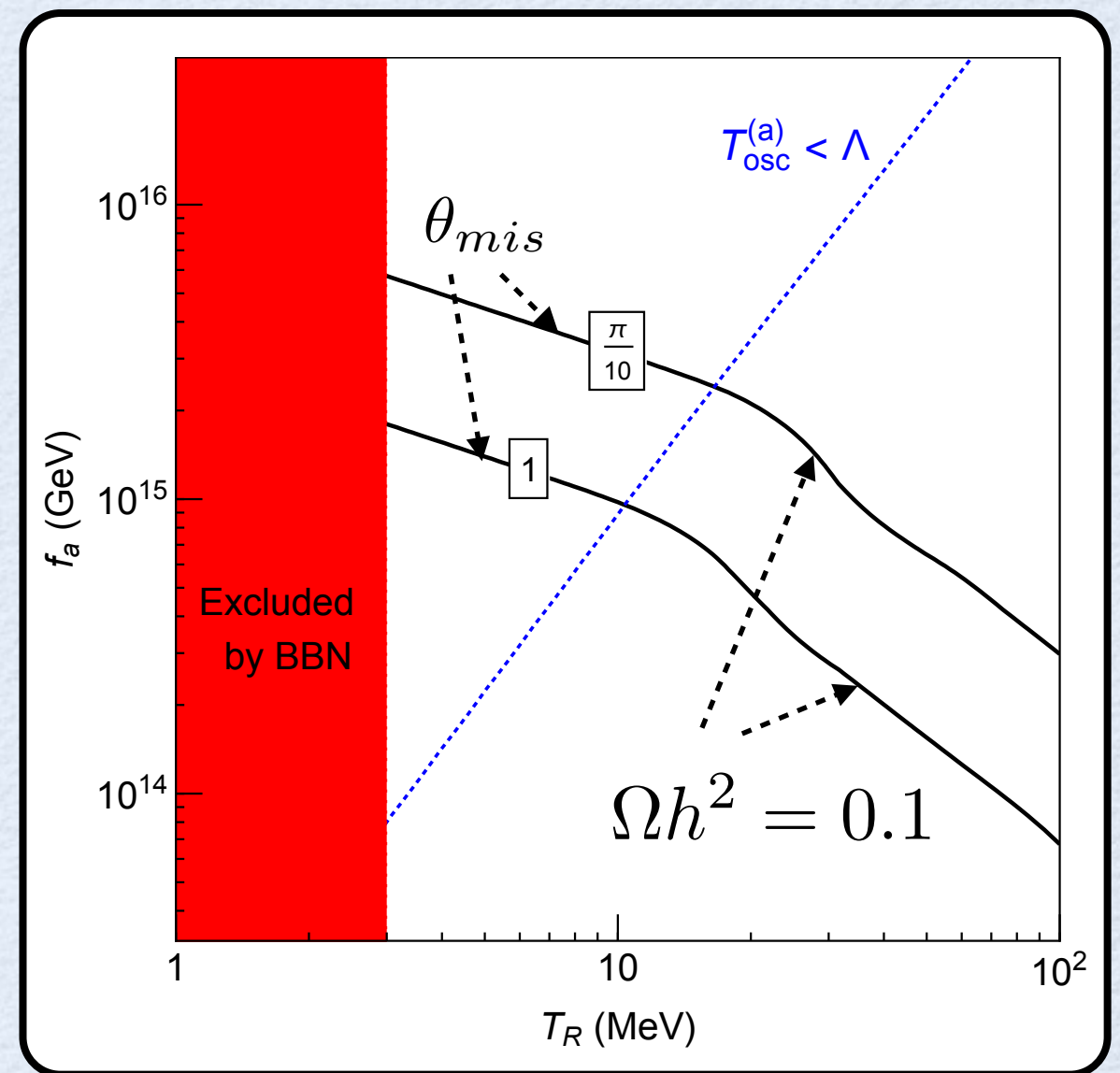
- $\frac{V_{PQ}}{f_a} \sim N_{DW} \sim 10 - 100$



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“SaxiGUTs”

Raymond Co, Francesco D'Eramo, LH 1603.04439





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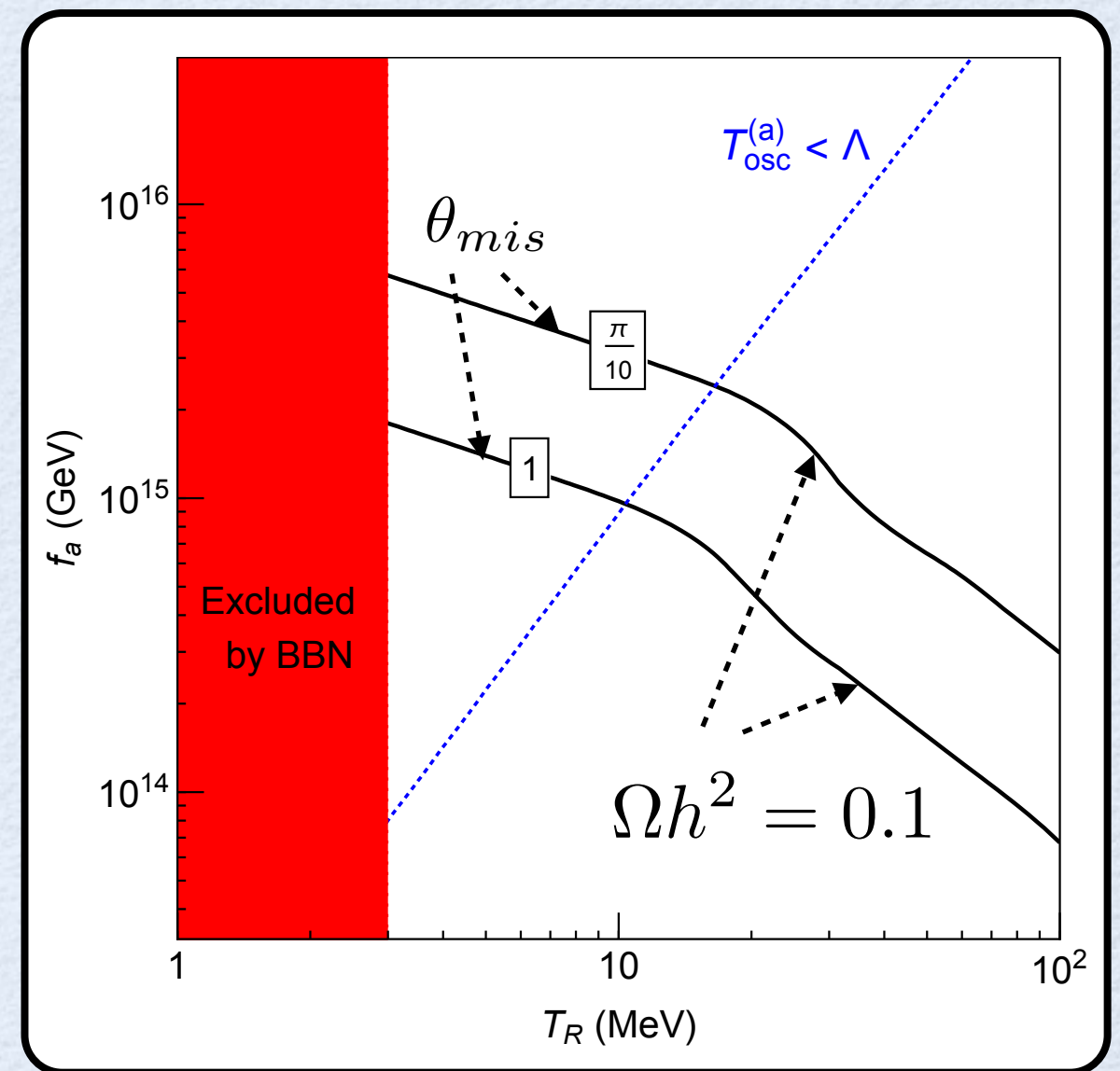
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Earlier work: Hashimoto, Izawa, Yamaguchi, Yanagida hep-ph/9803263



# Dark Radiation from $s \rightarrow aa$

$$\mathbf{K} = \sum_i v_i^2 \exp \left[ q_i \left( \frac{\mathbf{A} + \mathbf{A}^\dagger}{V_{PQ}} \right) \right] = \mathbf{A}^\dagger \mathbf{A} + \frac{1}{2} \sum_i \frac{q_i^3 v_i^2}{V_{PQ}^3} \mathbf{A}^\dagger \mathbf{A} (\mathbf{A} + \mathbf{A}^\dagger) + \dots$$

$$\kappa = \sum_i \frac{q_i^3 v_i^2}{V_{PQ}^2}$$

typically  $\mathcal{O}(1)$

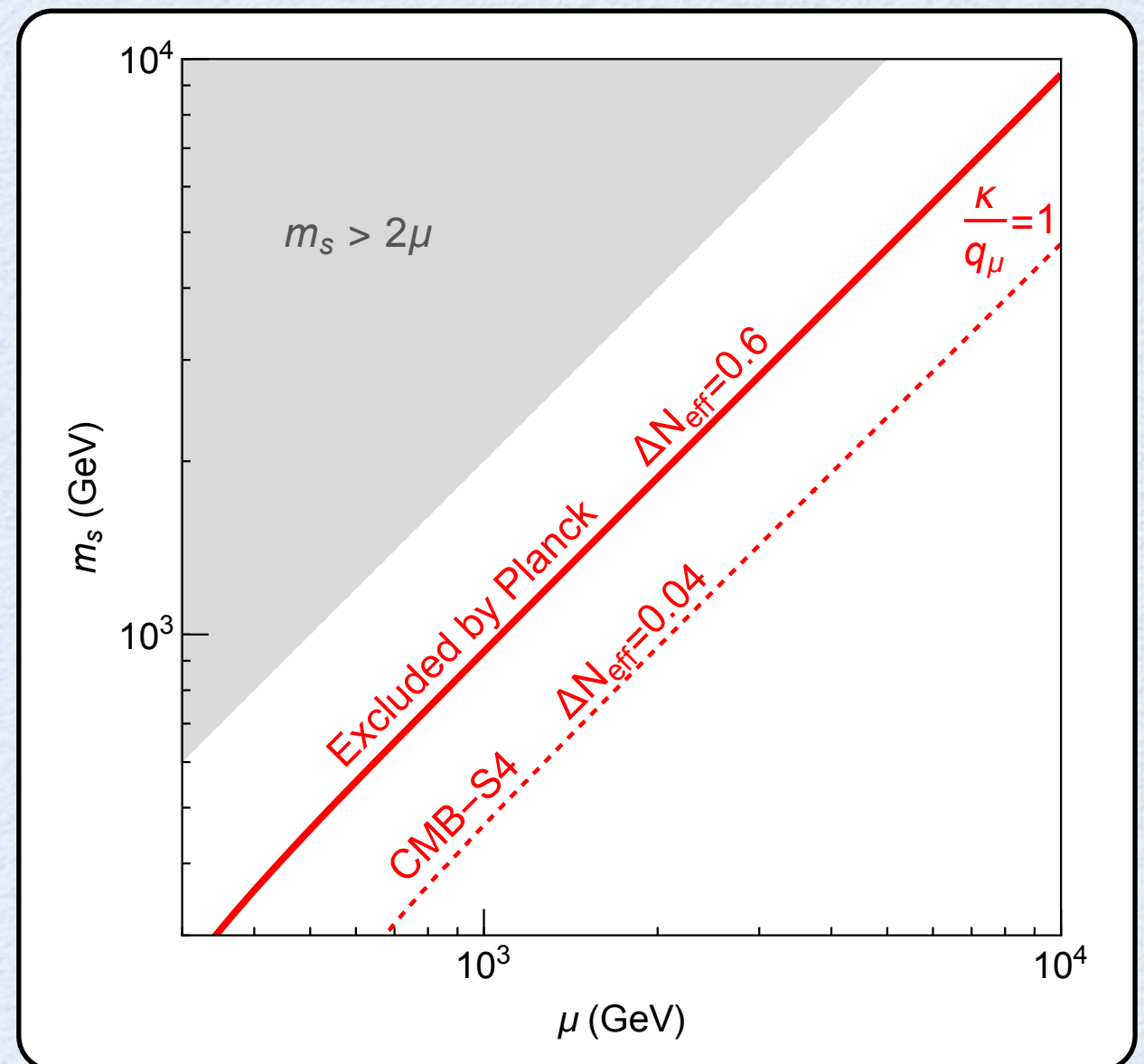


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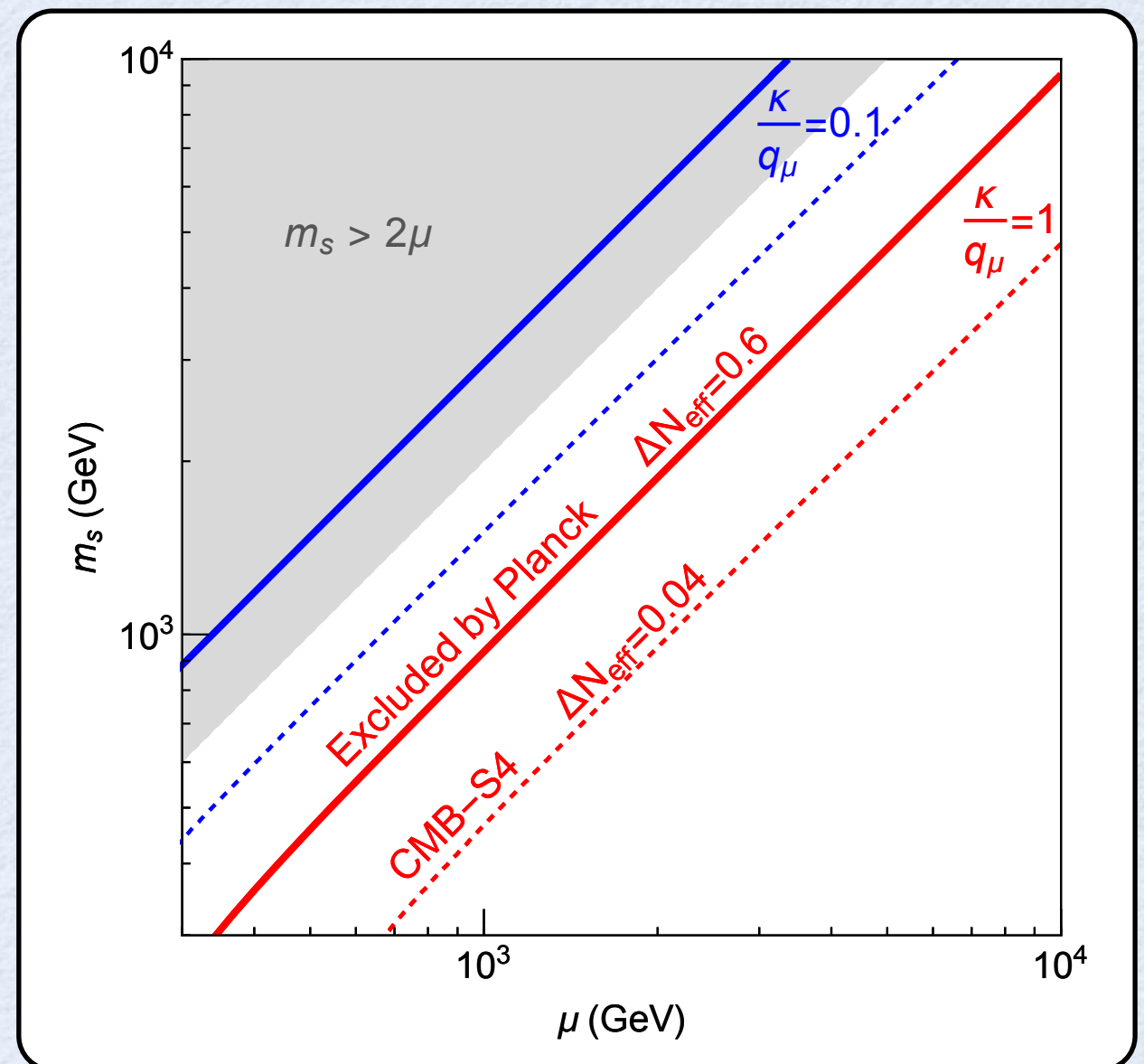


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# Conclusions

- SUSY + PQ       $T_{RI} > V_{PQ}$       Domain Wall Problem  
                          $T_{RI} < V_{PQ}$       Saxion Condensate
- DFSZ       $s \rightarrow hh$
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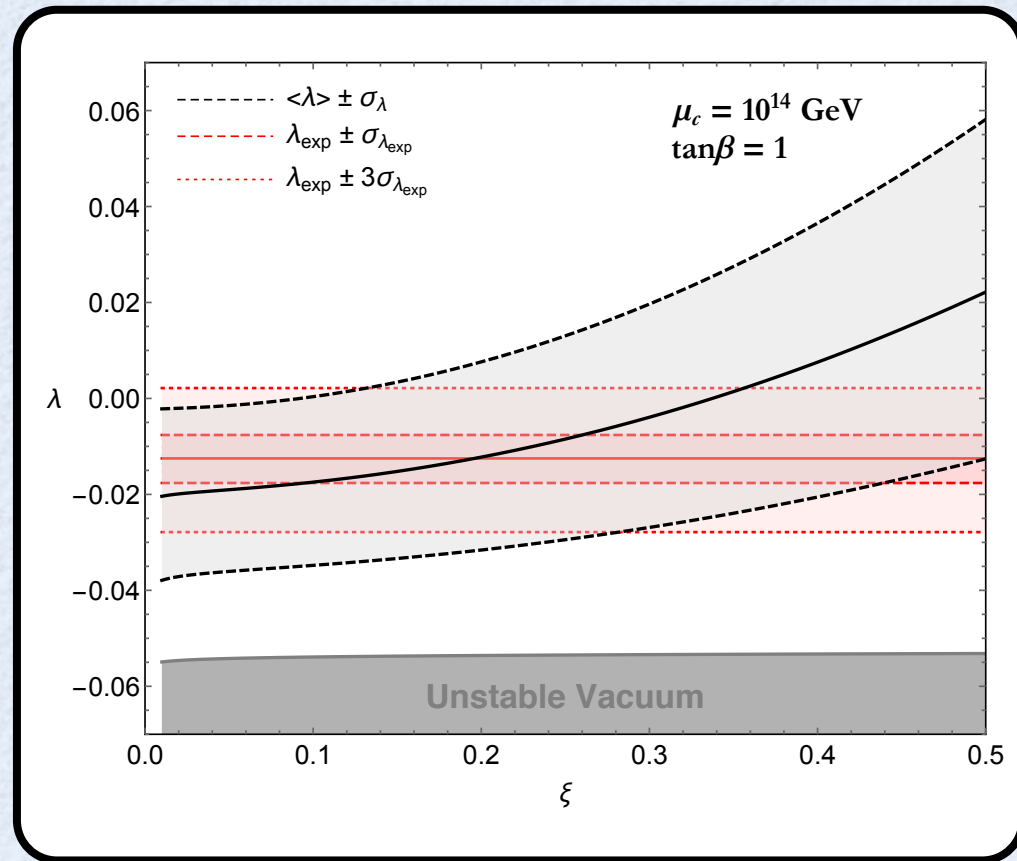
## Examples

- UV Scattering       $\tilde{G}_{3/2}$       Independent of  $T_{RI}$        $T_{RI} \sim 10^{15}$  GeV
- IR Freeze-In       $\tilde{a}$        $10^{11}$  GeV  $< V_{PQ} < 10^{15}$  GeV      Displaced Vertices
- Misalignment       $a$        $\theta_{mis} \sim 1$       and       $V_{PQ} \sim V_{GUT}$



# Higgs Mass: My Favorite Possibilities

## High Scale SUSY + PQ



D'Eramo, Hall, Pappadopulo arXiv:1502.06963

$$\tilde{m} > 10^{10} \text{ GeV}$$