

The Birth of Supersymmetry

(1970-1976)

Pierre Ramond

University of Florida

still alive

Supersymmetry

born on both sides

of the iron curtain

in the west

S-Matrix to Superstrings

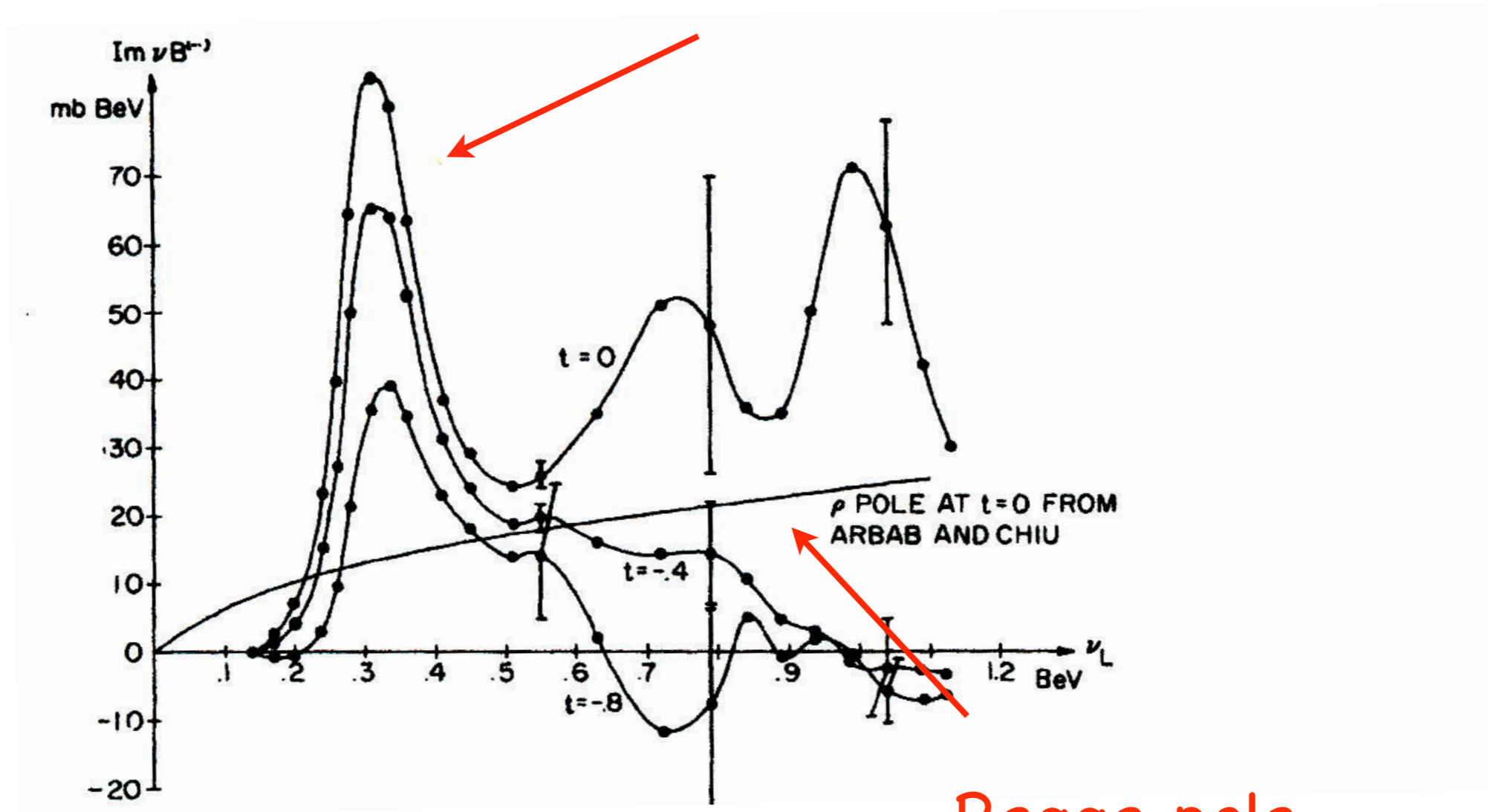
PREDICTION OF REGGE PARAMETERS OF ρ POLES FROM LOW-ENERGY πN DATA*

R. Dolen, D. Horn,[†] and C. Schmid
California Institute of Technology, Pasadena, California
(Received 23 June 1967)

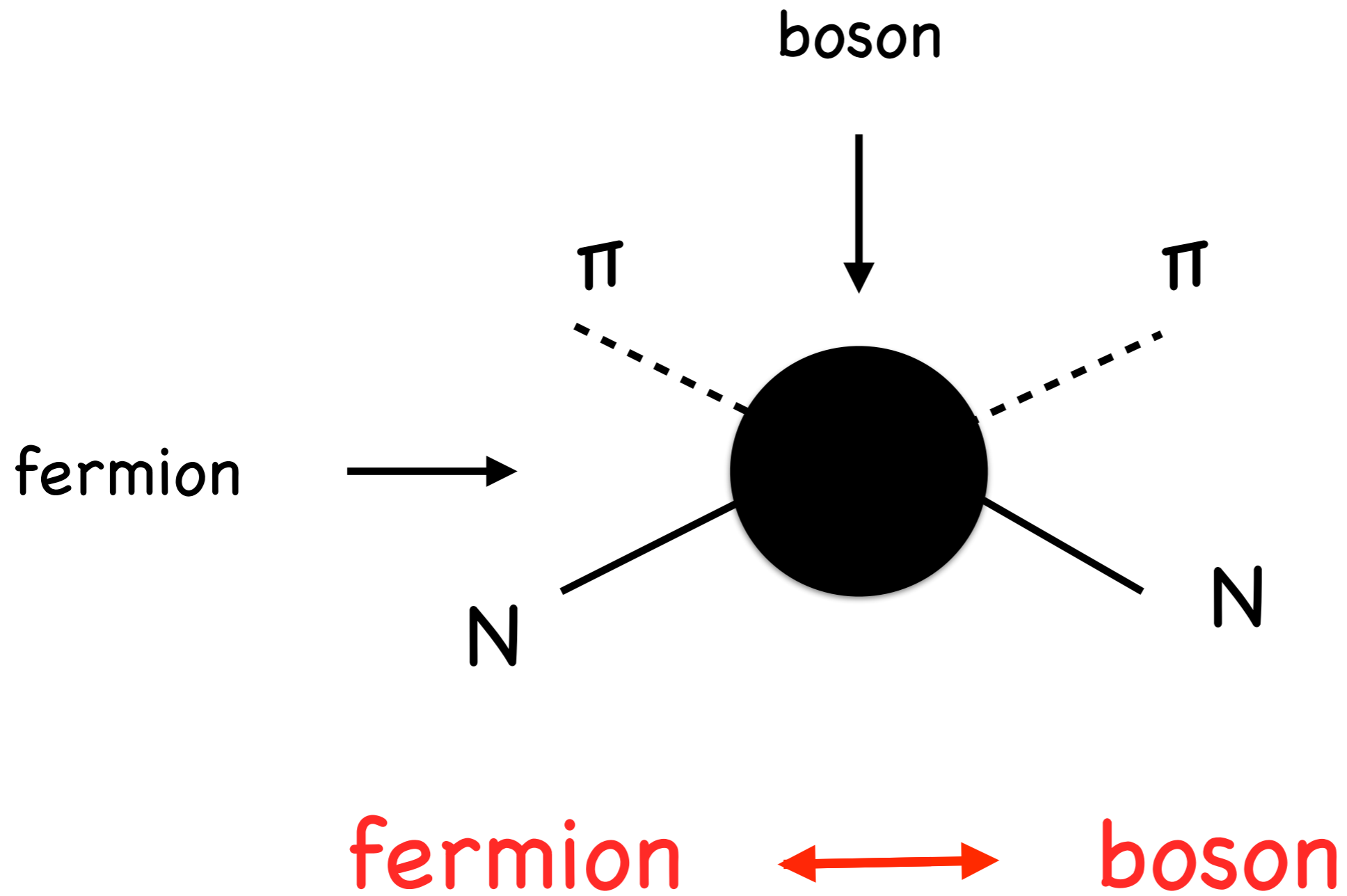
Using finite-energy sum rules we predict important features of the Regge structure of ρ poles from low-energy πN data. The combined effect of N^* resonances in generating (via the sum rules) properties of the exchanged ρ poles is discussed, thus starting a new type of bootstrap calculation.

$\pi - N$ scattering

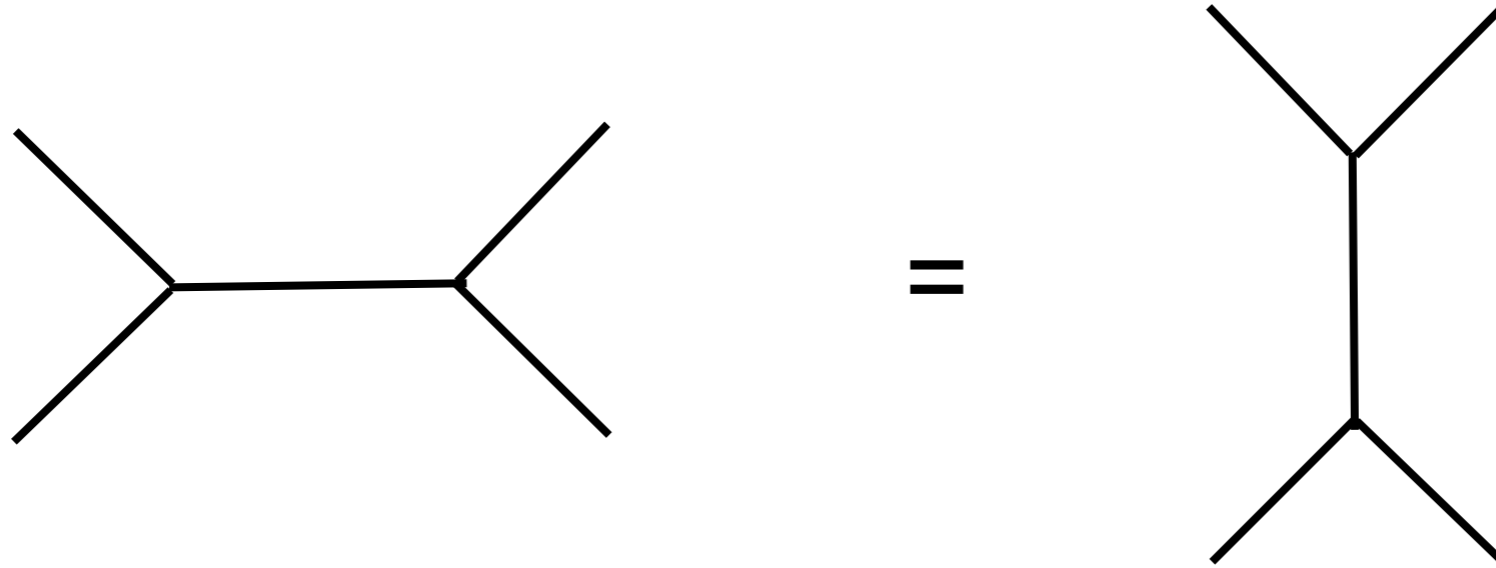
resonances



$\pi - N$ scattering



Veneziano Model (bosons only)



extract vertex & propagator
from amplitudes

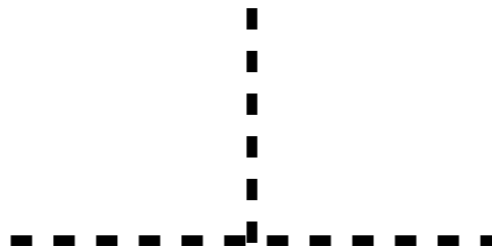
String Model



$$\frac{1}{L_0 + m^2}$$

$$L_0 = p^2 + \text{oscillators} = P \cdot P$$

$$P_\mu = p_\mu + (\text{oscillators})_\mu$$



$$e^{ik \cdot Q}$$

$$P_\mu = \dot{Q}_\mu$$

Dual Theory for Free Fermions

P. RAMOND

National Accelerator Laboratory, Batavia, Illinois 60150

(Received 4 January 1971)

A wave equation for free fermions is proposed based on the structure of the dual theory for bosons. Its formal properties preserve the role played by the Virasoro algebra. Additional Ward-like identities, compatible with the equation, are shown to exist. Its solutions lie on linear trajectories. In particular, the parent is shown to be doubly degenerate, but these solutions lie on different sheets of the cut j plane.

Dirac equation

$$\gamma_{\mu} p^{\mu} + m = 0$$

$$P_{\mu} = p_{\mu} + (\text{oscillators})_{\mu}$$

Generalized Dirac equation

$$\Gamma_{\mu} P_{\mu} + m = 0$$

$$\{\Gamma_{\mu}, \Gamma_{\nu}\} = \eta_{\mu\nu}$$

$$\gamma_{\mu} \rightarrow \Gamma_{\mu} = \gamma_{\mu} + \gamma_5 (\text{oscillators})_{\mu}$$

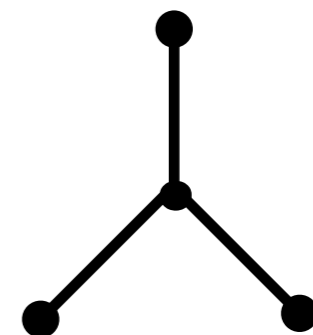
“The α 's are new dynamical variables which it is necessary to introduce in order to satisfy the conditions of the problem. They may be regarded as describing some internal motion of the electron. We shall call them the spin variables.” (Dirac)

Dirac structure requires
anticommuting oscillators with vector indices!!!!

Spin-Statistics?

learned much later that in $D=10$ space-time dimensions,
the little group vector and spinor
have the **same** dimension

Mercedes-Benz Dynkin diagram!



new kind of symmetry

(square root of the Virasoro algebra)

$$\{F_n, F_m\} = 2L_{n+m} \quad [L_n, F_m] = (2m - n)F_{m+n}$$

$$[L_n, L_m] = (m - n)L_{m+n}$$

L_n generate the (2-d conformal) Virasoro algebra

F_n generate 2-d superconformal algebra

2-d supersymmetry

Superstring



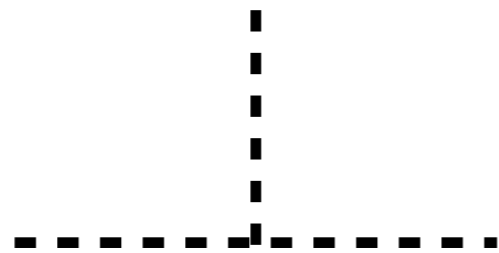
$$\frac{1}{L_0 + m^2}$$

$$L_0 = p^2 + \text{oscillators} = P \cdot P$$

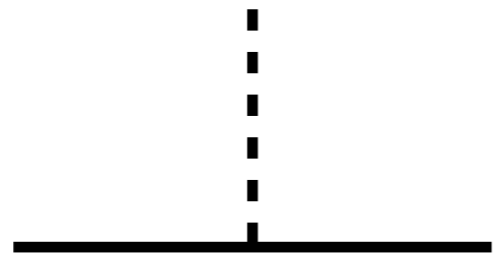


$$\frac{1}{F_0 + m}$$

$$F_0 = \Gamma \cdot P + m = \gamma \cdot p + \text{oscillators}$$



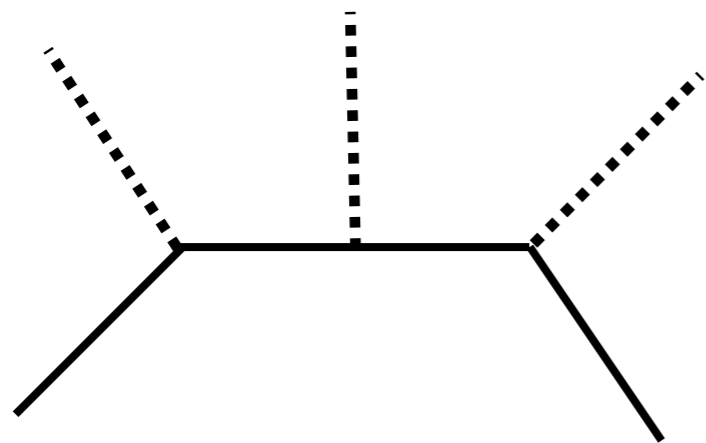
$$e^{ik \cdot Q}$$



$$\Gamma_5 e^{ik \cdot Q}$$

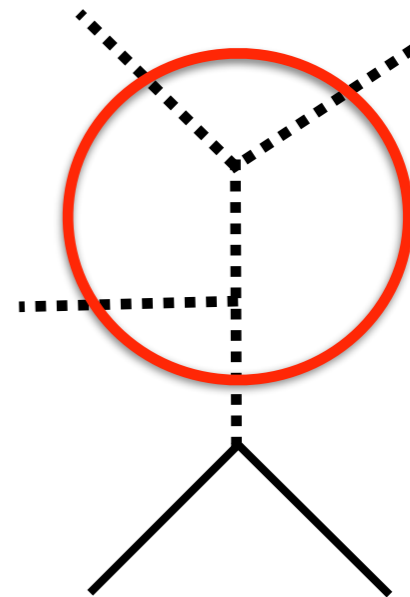
(Neveu & Schwarz)

Superstring amplitudes



=

Dual Pion Model



fermion



boson

8.A.1

FACTORIZABLE DUAL MODEL OF PIONS*

A. NEVEU** and J. H. SCHWARZ
*Joseph Henry Laboratories, Princeton University,
Princeton, New Jersey 08540*

Received 25 March 1971

TACHYON-FREE DUAL MODEL WITH A POSITIVE-INTERCEPT TRAJECTORY*

A. NEVEU** and J. H. SCHWARZ
Joseph Henry Laboratories, Princeton University, Princeton, New Jersey 08540, USA

Received 15 February 1971

A dual-resonance model with two kinds of trajectories split by one-half unit is constructed. The lowest mass state on the leading trajectory has spin one, although the G-parity assignments are unsuitable for an identification with π 's and ρ 's.

7.A.1
8.A.1

FIELD THEORY INTERPRETATION OF SUPERGAUGES IN DUAL MODELS

J. -L. GERVAIS
*Laboratoire de Physique Théorique et Hautes Energies, Orsay, France **

and

B. SAKITA **
*Institut des Hautes Etudes Scientifiques, 91-Bures-sur-Yvette, France
and
Laboratoire de Physique Théorique et Hautes Energies, Orsay, France*

Received 13 August 1971

Dual Pion Model

fermion and boson sectors:

supergauges

different boundary condition

long russian winters,

long soviet summers,



lead to

supersymmetry

Berezin & Kac, 1970

Mat. Sbornik
Tom 82 (124) (1970), No. 3

Math. USSR Sbornik
Vol. 11 (1970), No. 3

LIE GROUPS WITH COMMUTING AND ANTICOMMUTING PARAMETERS

F. A. BEREZIN AND G. I. KAC

UDC 519.46

Abstract. In this paper we study analogs of Lie algebras and formal Lie groups. These analogs of groups differ from usual Lie groups, roughly speaking, in that they admit anticommuting canonical parameters. The analogs of Lie algebras differ from usual Lie algebras by properties of the commutator. In the definition of these objects an essential role is played by the gradient. In case it is trivial they become Lie groups and algebras in the usual sense. To these generalized objects we carry over classical theorems on the connection between Lie groups and algebras and the basic representation theory.

Gol'fand & Likhtman, 1971

EXTENSION OF THE ALGEBRA OF POINCARÉ GROUP GENERATORS AND VIOLATION OF P INVARIANCE

Yu.A. Gol'fand and E.P. Likhtman
Physics Institute, USSR Academy of Sciences
Submitted 10 March 1971
ZhETF Pis. Red. 13, No. 8, 452 - 455 (20 April 1971)

The extension of the algebra \mathcal{P} is carried out in the following manner: we add to the generators P_μ and $M_{\mu\nu}$ the bispinor generators W_α and \bar{W}_α , which we shall call the generators of spinor translations.

$$[M_{\mu\nu}, M_{\sigma\lambda}]_- = i(\delta_{\mu\sigma}M_{\nu\lambda} + \delta_{\nu\lambda}M_{\mu\sigma} - \delta_{\mu\lambda}M_{\nu\sigma} - \delta_{\nu\sigma}M_{\mu\lambda}); [P_\mu, P_\nu]_- = 0;$$

$$[M_{\mu\nu}, P_\lambda]_- = i(\delta_{\mu\lambda}P_\nu - \delta_{\nu\lambda}P_\mu); [M_{\mu\nu}, W]_- = \frac{i}{4} [\gamma_\mu, \gamma_\nu] W; \bar{W} = W^\dagger \gamma_0.$$

$$[W_\pm, \bar{W}]_+ = \gamma_\mu^\dagger P_\mu; [W, W]_+ = 0; [P_\mu, W]_- = 0,$$

extension of space-time symmetries!

write invariant interaction between
(Wess-Zumino) and gauge supermultiplets

$$\begin{aligned}
 L(x) = & (\partial_a \phi^* - igA_a \phi^*)(\partial_a \phi + igA_a \phi) - m^2 \phi^* \phi + (\partial_a \omega^* - igA_a \omega^*) \\
 & \times (\partial_a \omega + igA_a \omega) - m^2 \omega^* \omega + \frac{i}{2} \psi_1 \gamma_a \overleftrightarrow{\partial}_a \psi_1 - m \bar{\psi}_1 \psi_1 - g \psi_1 \gamma_a \psi_1 A_a \\
 & + \frac{i}{2} \bar{\psi}_2 \gamma_a \overleftrightarrow{\partial}_a \psi_2 - \mu \bar{\psi}_2 \psi_2 - \frac{1}{2} (\partial_\beta A_a)^2 + \frac{\mu^2}{2} A_a A_a + \frac{1}{2} (\partial_a X)^2 - \frac{\mu^2}{2} X^2 \\
 & + g\mu (\phi^* \phi - \omega \omega^*) X - \frac{g^2}{2} (\phi^* \phi - \omega^* \omega)^2 + \sqrt{2} g (\bar{\phi}_1 \bar{s} \psi_2 \phi + \bar{\psi}_2 \bar{s} \psi_1 \phi^*) \\
 & - \sqrt{2} g (\psi_1^c \bar{s} \psi_2 \omega^* + \bar{\psi}_2 \bar{s} \psi_1^c \omega) .
 \end{aligned}$$

(not totally correct)

Volkov & Akulov, 1972

POSSIBLE UNIVERSAL NEUTRINO INTERACTION

D.V. Volkov and V.P. Akulov

Physico-technical Institute, Ukrainian Academy of Sciences

Submitted 13 October 1972

ZhETF Pis. Red. 16, No. 11, 621 - 624 (5 December 1972)

neutrino as a Nambu-Goldstone particle

$$\psi \rightarrow \psi' = \psi + \zeta \qquad x_\mu \rightarrow x'_\mu - \frac{a}{2i} (\zeta^\dagger \sigma_\mu \psi - \psi^\dagger \sigma_\mu \zeta)$$

nonlinear super σ -model

“ ... if we introduce gauge fields corresponding to the(se) transformations, then as a consequence of the Higgs effect, a massive gauge field with spin 3/2 arises and the Goldstone particle with spin 1/2 vanishes”

1970

Russians

Superstrings

1973

WZ

1976



SUPERGAUGE TRANSFORMATIONS IN FOUR DIMENSIONS

J. WESS

Karlsruhe University

B. ZUMINO

CERN, Geneva

Received 5 October 1973

from the superstring side to **four dimensions**

scalar and vector supermultiplets with auxiliary fields

no interactions

Wess & Zumino, 1974

A LAGRANGIAN MODEL INVARIANT UNDER
SUPERGAUGE TRANSFORMATIONS

J. WESS

Karlsruhe University, Germany

and

B. ZUMINO

CERN, Geneva, Switzerland

Received 4 January 1974

one loop structure of WZ multiplet

no quadratic divergences

only wave function renormalization

Likthman, 1975

Källen, 1949

Fields and the Super Poincaré Group

$$(\lambda, \lambda + \frac{1}{2}) \quad + \quad (-\lambda, -\lambda - \frac{1}{2})$$

CPT

Wess-Zumino multiplet
(Gol'fand&Likhman)

$$\left(\frac{1}{2}\right) + (0) + (0) + \left(-\frac{1}{2}\right)$$

SuperGauge multiplet

$$(1) + \left(\frac{1}{2}\right) + \left(-\frac{1}{2}\right) + (-1)$$

SuperGravity multiplet

$$(2) + \left(\frac{3}{2}\right) + \left(-\frac{3}{2}\right) + (-2)$$

Gell-Mann 1974

self-conjugate multiplets

N=4 Super Yang-Mills $(1) + 4\left(\frac{1}{2}\right) + 6(0) + 4\left(-\frac{1}{2}\right) + (-1)$

N=8 SuperGravity

$$(2) + 8\left(\frac{3}{2}\right) + 28(1) + 56\left(\frac{1}{2}\right) + 70(0) + 56\left(-\frac{1}{2}\right) + 28(-1) + 8\left(-\frac{3}{2}\right) + (-2)$$

SUPERGAUGE INVARIANT EXTENSION OF THE HIGGS MECHANISM AND A MODEL FOR THE ELECTRON AND ITS NEUTRINO

Pierre FAYET

*Laboratoire de Physique Théorique, Ecole Normale Supérieure,
Paris, France**

Received 4 December 1974

SuSy Higgs mechanism

R-symmetry

neutrino as Goldstone fermion!

1976

Ferrara, Freedman & van Nieuwenhuisen

PHYSICAL REVIEW D

VOLUME 13, NUMBER 12

15 JUNE 1976

Progress toward a theory of supergravity*

Daniel Z. Freedman and P. van Nieuwenhuisen

Institute for Theoretical Physics, State University of New York at Stony Brook, Stony Brook, New York 11794

S. Ferrara

Laboratoire de Physique Théorique de l'Ecole Normale Supérieure, 24 rue Lhomond, 75231 Paris Cedex 05, France

(Received 29 March 1976)

N=1 Supergravity

graviton and gravitino

Super Einstein tour de force!

1976

Brink, Schwarz & Scherk

N=4 SuperYang-Mills

Nuclear Physics B121 (1977) 77–92
© North-Holland Publishing Company

SUPERSYMMETRIC YANG-MILLS THEORIES *

Lars BRINK ** and John H. SCHWARZ

California Institute of Technology, Pasadena, California 91125

J. SCHERK

*Laboratoire de Physique Théorique de l'École Normale Supérieure, 24 rue Lhomond,
75231 Paris, France*

Received 22 December 1976

1976

Gliozzi & Olive & Scherk

Nuclear Physics B122 (1977) 253–290
© North-Holland Publishing Company

SUPERSYMMETRY, SUPERGRAVITY THEORIES AND THE DUAL SPINOR MODEL

F. GLIOZZI ^{*} and J. SCHERK

*Laboratoire de Physique Théorique de l'Ecole Normale Supérieure ^{**}*

D. OLIVE

CERN, Geneva

and

The Niels Bohr Institute, Copenhagen

Received 14 January 1977

It all comes together
superstring states are space-time supersymmetric
(in ten dimensions)

1976

Gildener & Weinberg

PHYSICAL REVIEW D

VOLUME 13, NUMBER 12

15 JUNE 1976

Symmetry breaking and scalar bosons*

Eldad Gildener and Steven Weinberg

Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138

(Received 19 January 1976)

One possibility is that the super-strong symmetry breakdown leaves both a chiral symmetry and a supersymmetry¹¹ unbroken, so that there is a multiplet including massless scalars and fermions. Unfortunately, the subsequent ordinary breakdown which gives masses to the intermediate vector bosons would then produce Goldstone fermions.

gauge hierarchy paper

1976

Fayet

Volume 64B, number 2

PHYSICS LETTERS

13 September 1976

SUPERSYMMETRY AND WEAK, ELECTROMAGNETIC AND STRONG INTERACTIONS

P. FAYET

Laboratoire de Physique Théorique de l'Ecole Normale Supérieure, Paris, France*

Received 9 July 1976

Birth of the Supersymmetric Standard Model

require two scalar superfields

leptons & quarks in WZ multiplets

continuous R-symmetry

1970

Russians

Superstrings

1973

WZ

1976

Sugra

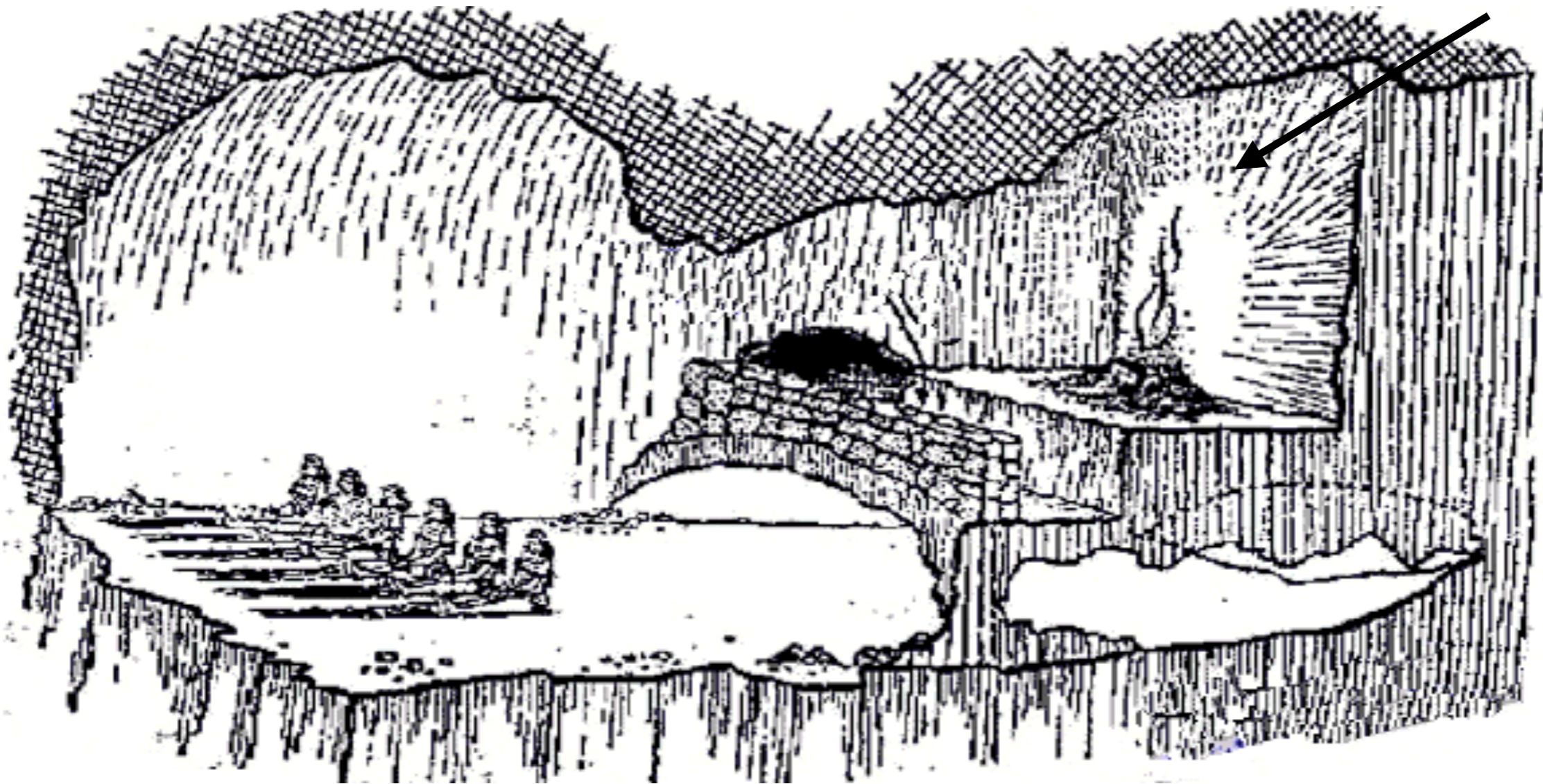
MSSM

Superstrings still in flight



Plato's Cave

Coset Physics



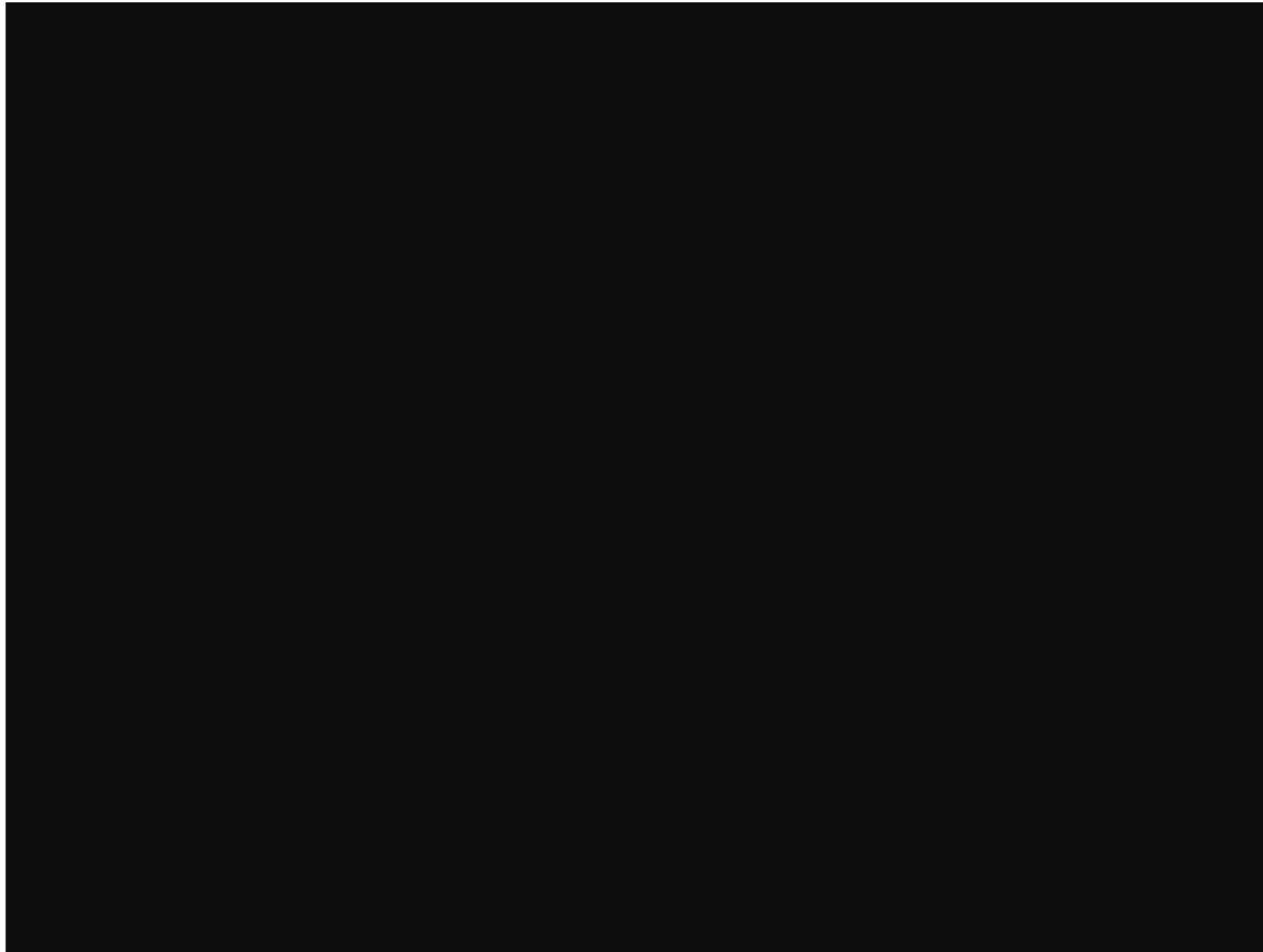
paraphrasing Dirac

Supersymmetry is

too beautiful to ignore

1931

Blanche Calloway



“It Looks like Susie”

It looks like Susie

It must be Susie

I'm sure it's Susie

But I don't know

Could be Virginia

With her eyes of Blue

Could be Mary

Sweet MaryLou

But it looks like Susy

She talks like Susy

She walks like Susy

.....

early hint: Wigner, 1939

Representations of the Poincaré Group

massless particle representations with fixed helicity λ

\vec{p}

momentum

energy $E = cp$

λ

helicity

$0, \pm\frac{1}{2}, \pm 1, \pm\frac{3}{2}, \pm 2, \pm\frac{5}{2}, \dots$

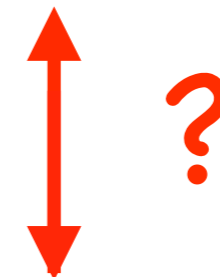
the familiar particles

Wigner: massless "Infinite Spin" representations

with **different** helicity strings

\vec{p} momentum energy $E = cp$

λ helicity string $\dots, -\frac{5}{2}, -\frac{3}{2}, -\frac{1}{2}, +\frac{1}{2}, +\frac{3}{2}, +\frac{5}{2}, \dots$



λ helicity string $\dots, -2, -1, 0, +1, +2, \dots$

not found in Nature