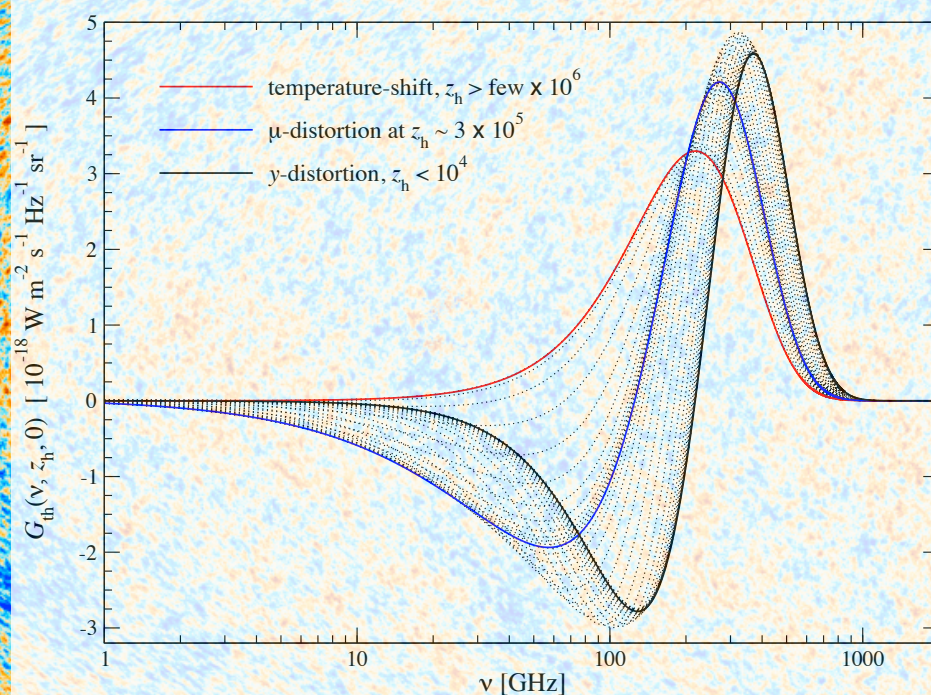
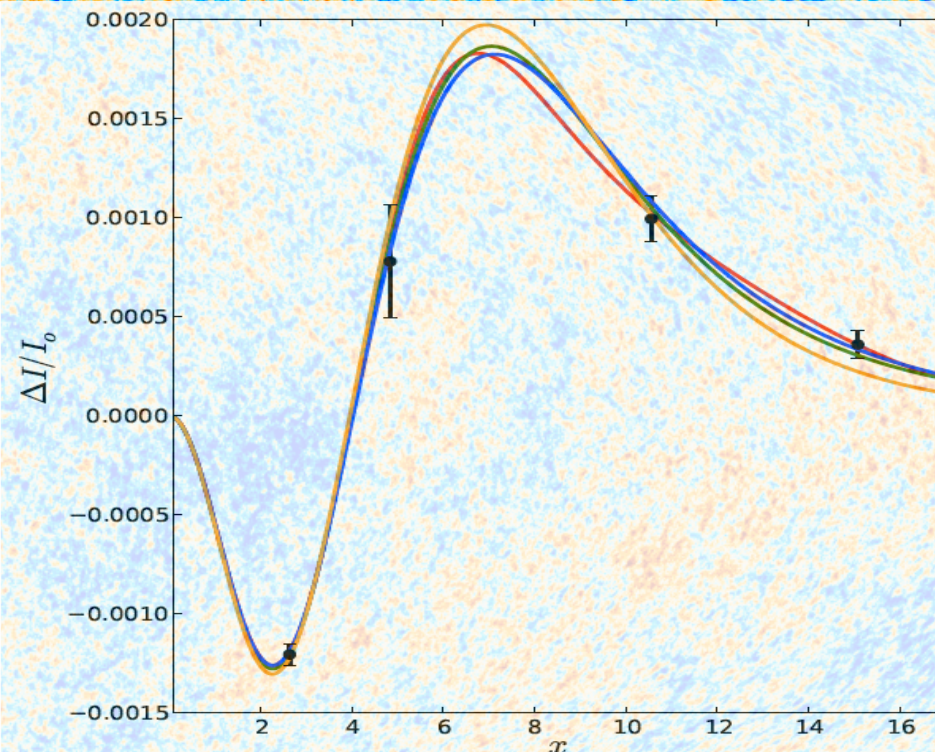


CMB Spectral Distortion Computations using *CosmoTherm* and *SZpack*

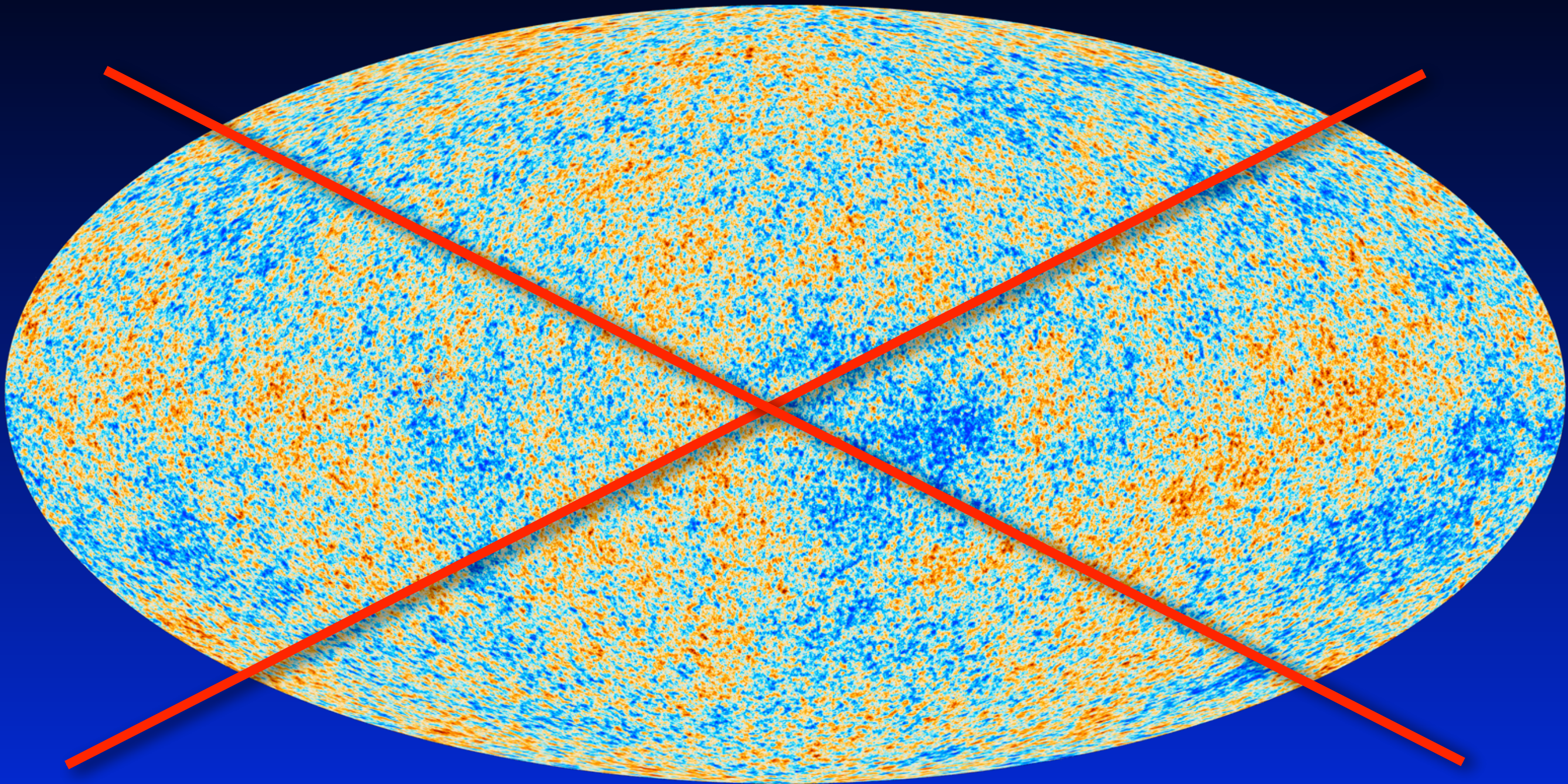
Primordial Distortions



Sunyaev-Zeldovich effect



Cosmic Microwave Background Anisotropies



Planck all-sky
temperature map

- CMB has a blackbody spectrum in every direction
- tiny variations of the CMB temperature $\Delta T/T \sim 10^{-5}$

CMB provides another independent piece of information!

COBE/FIRAS

$$T_0 = (2.726 \pm 0.001) \text{ K}$$

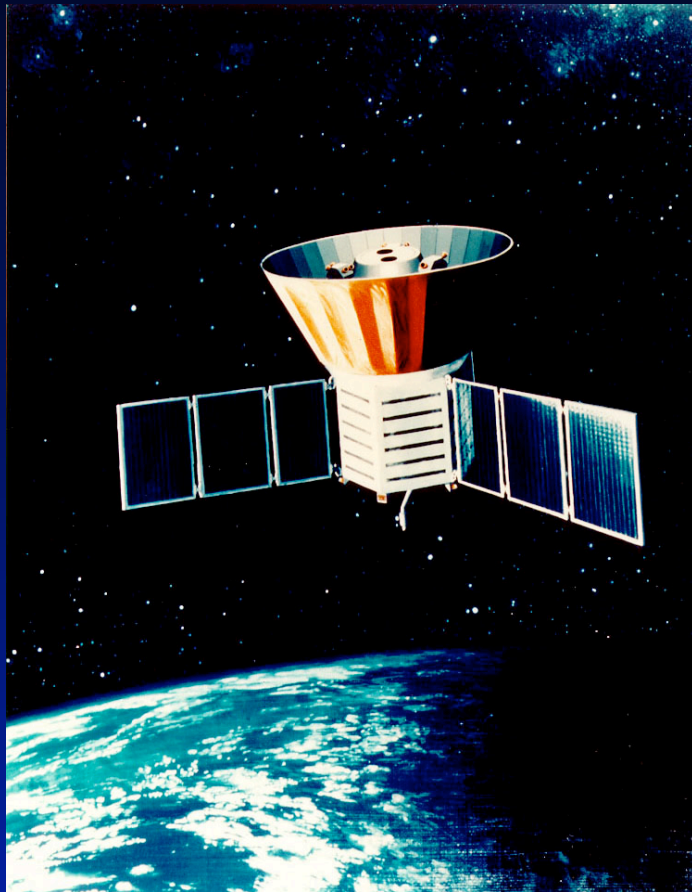
Absolute measurement required!

One has to go to space...

Mather et al., 1994, ApJ, 420, 439
Fixsen et al., 1996, ApJ, 473, 576
Fixsen, 2003, ApJ, 594, 67
Fixsen, 2009, ApJ, 707, 916

- CMB monopole is 10000 - 100000 times larger than the fluctuations

COBE / FIRAS (Far InfraRed Absolute Spectrophotometer)

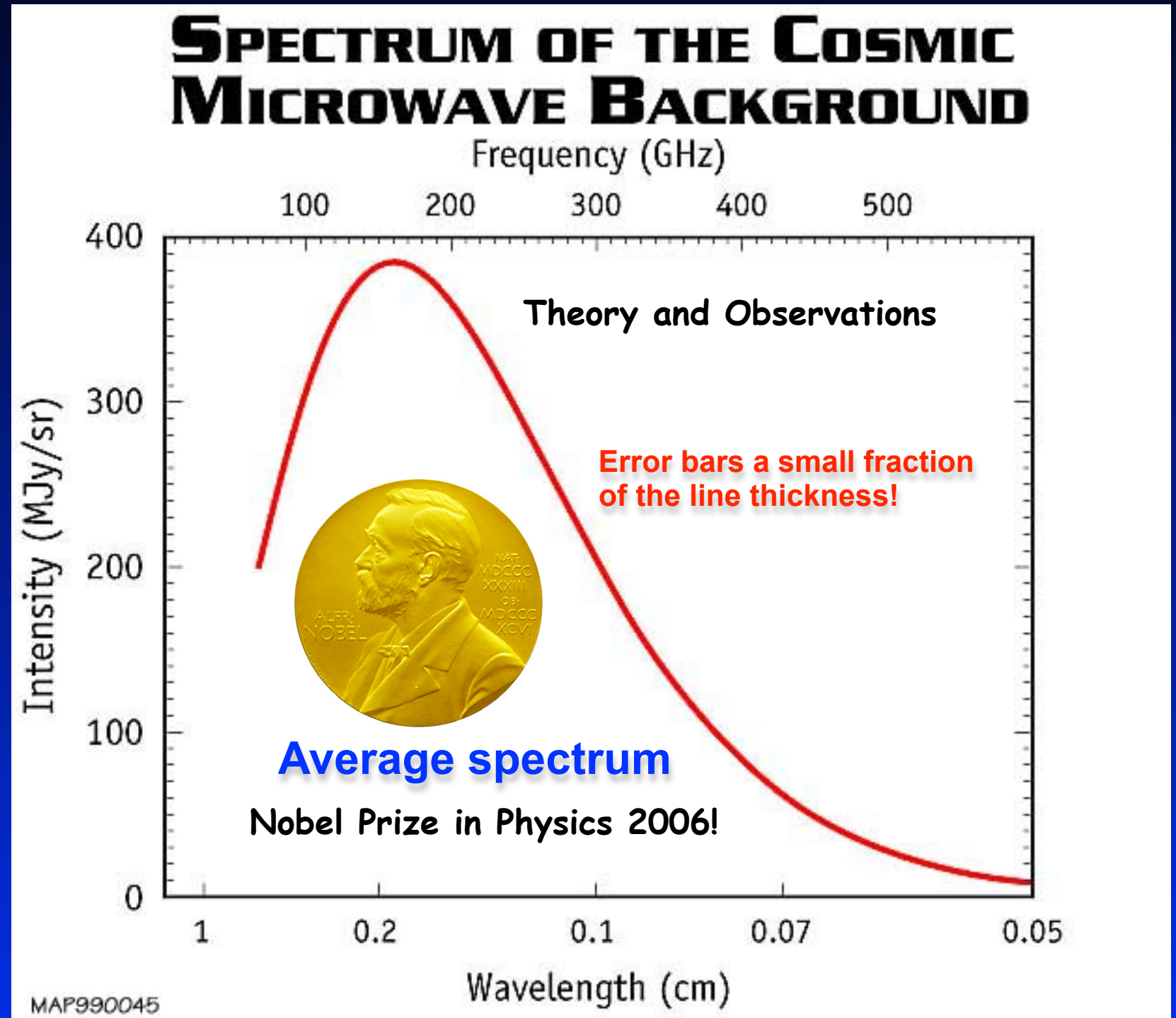


$$T_0 = 2.725 \pm 0.001 \text{ K}$$

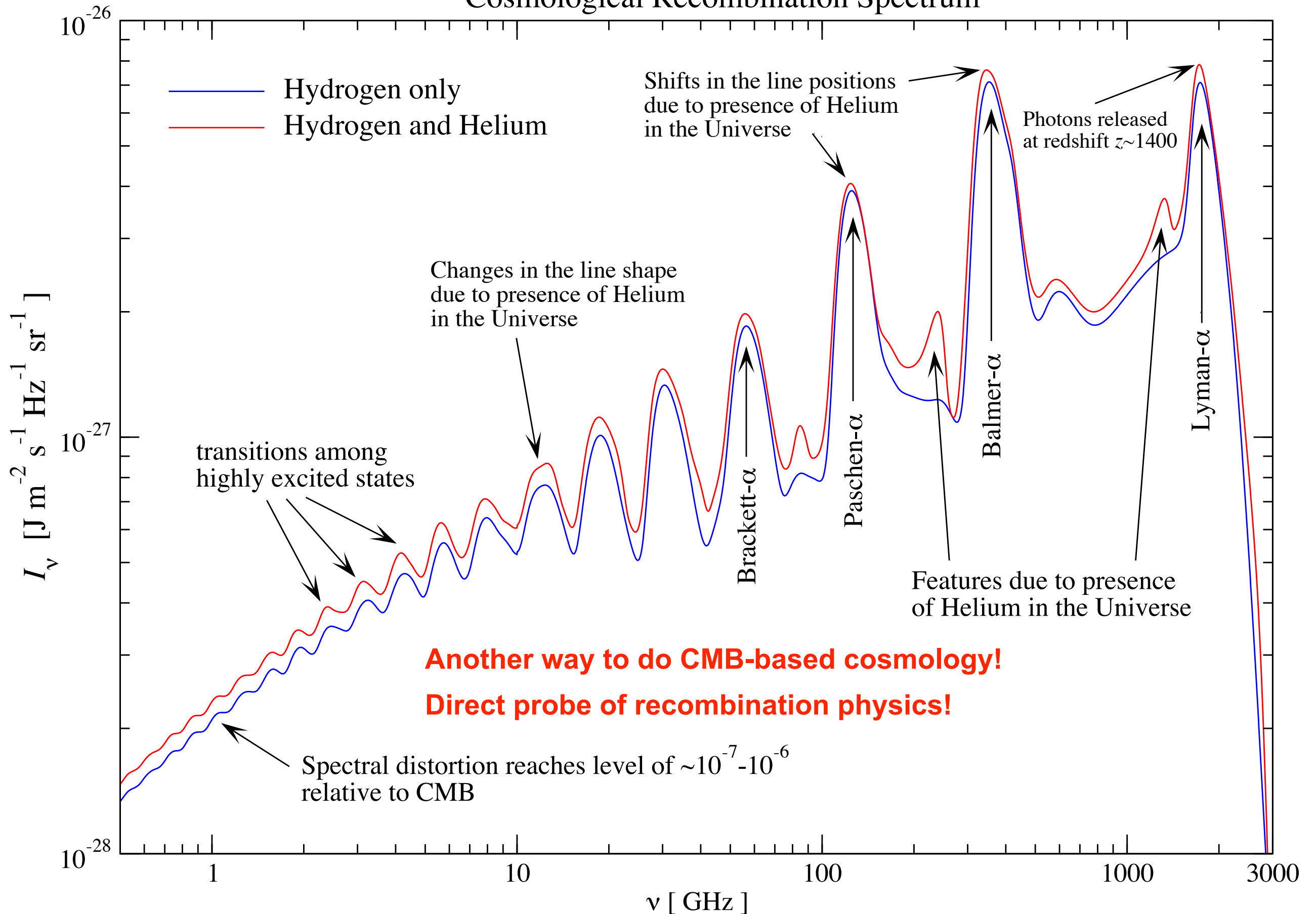
$$|y| \leq 1.5 \times 10^{-5}$$

$$|\mu| \leq 9 \times 10^{-5}$$

Mather et al., 1994, ApJ, 420, 439
Fixsen et al., 1996, ApJ, 473, 576
Fixsen et al., 2003, ApJ, 594, 67



Cosmological Recombination Spectrum



Why should one expect some spectral distortion?

Full thermodynamic equilibrium (certainly valid at very high redshift)

- CMB has a blackbody spectrum at every time (not affected by expansion)
- Photon number density and energy density determined by temperature T_γ

$$T_\gamma \sim 2.726 (1+z) \text{ K}$$

$$N_\gamma \sim 411 \text{ cm}^{-3} (1+z)^3 \sim 2 \times 10^9 N_b \text{ (entropy density dominated by photons)}$$

$$\rho_\gamma \sim 5.1 \times 10^{-7} m_e c^2 \text{ cm}^{-3} (1+z)^4 \sim \rho_b \times (1+z) / 925 \sim 0.26 \text{ eV cm}^{-3} (1+z)^4$$

Perturbing full equilibrium by

- Energy injection (interaction *matter* \leftrightarrow *photons*)
- Production of (energetic) photons and/or particles (i.e. change of entropy)

→ CMB spectrum deviates from a pure blackbody

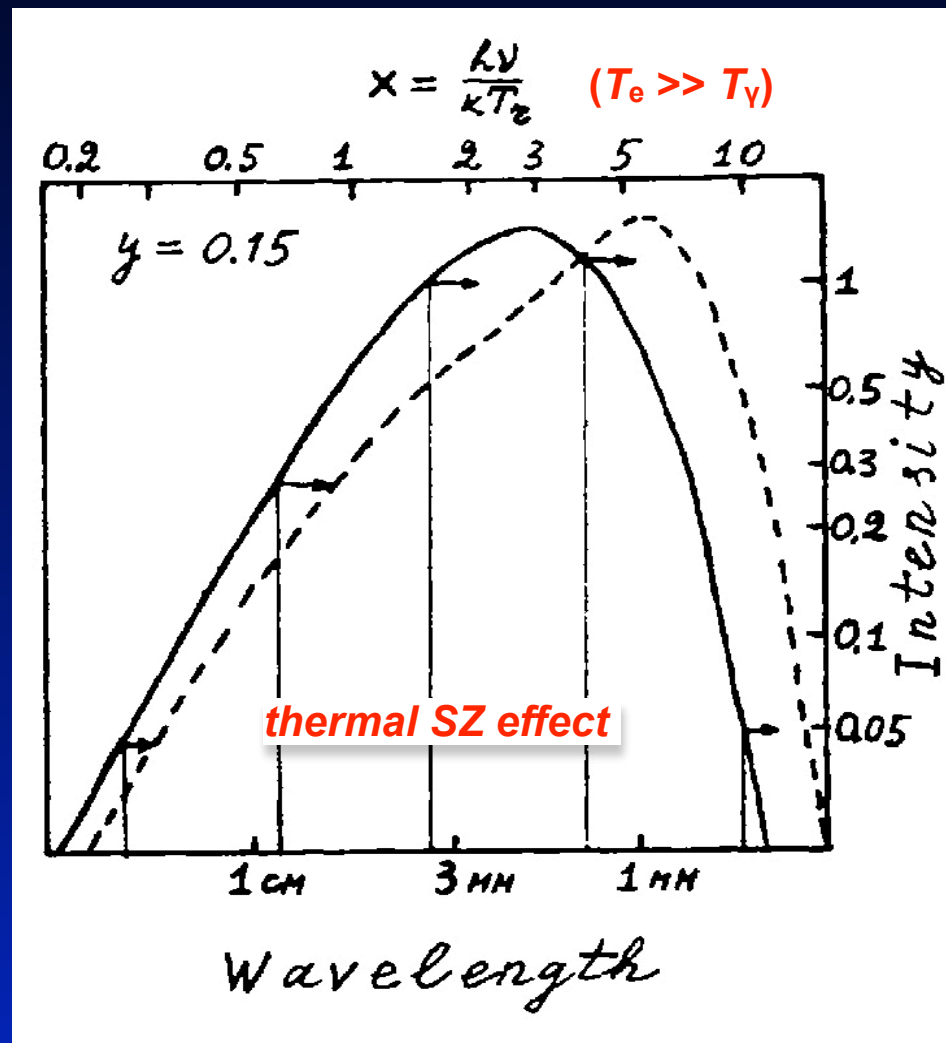
→ thermalization process (partially) erases distortions

(Compton scattering, double Compton and Bremsstrahlung in the expanding Universe)

Measurements of CMB spectrum place very tight limits on the thermal history of our Universe!

Standard types of primordial CMB distortions

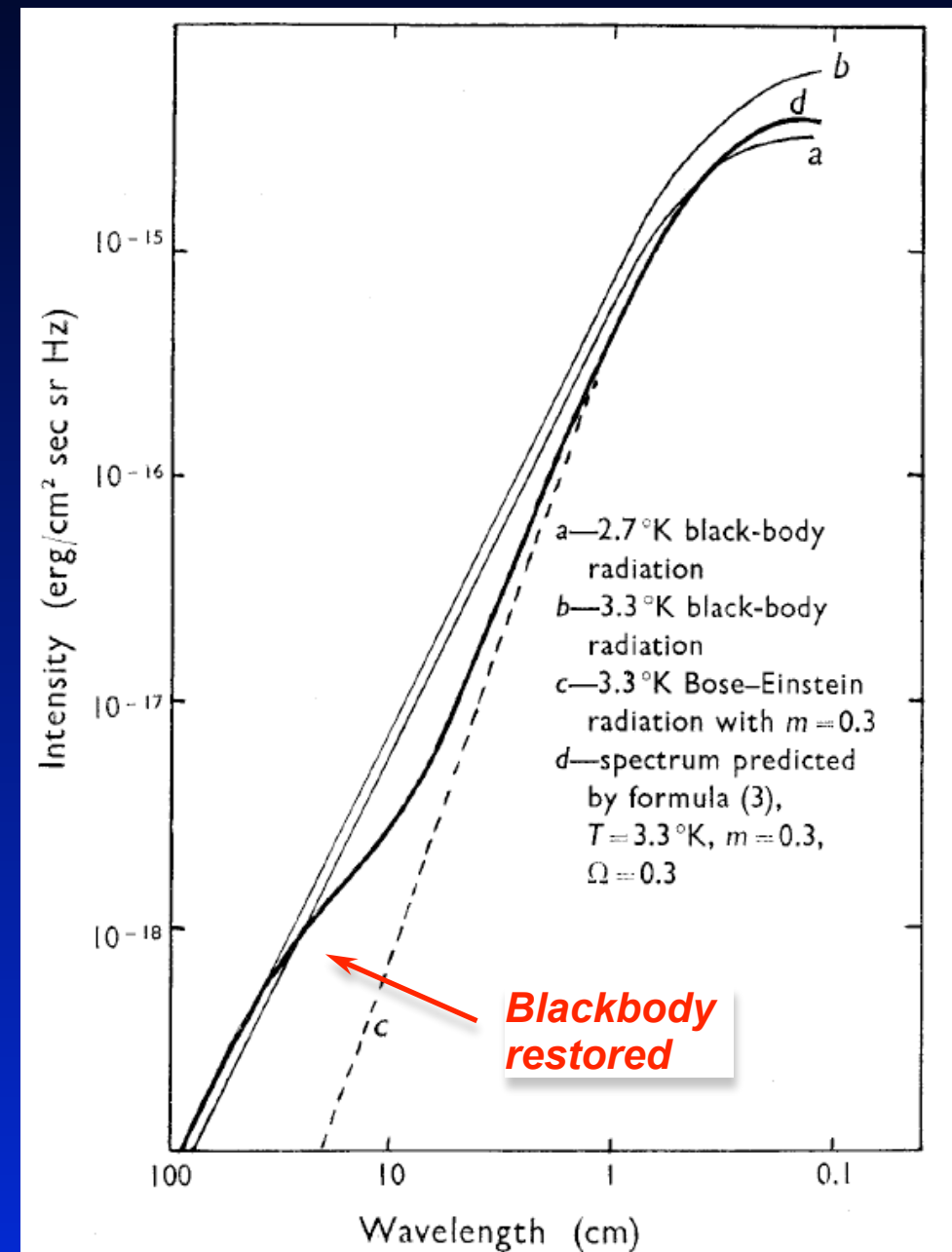
Compton y -distortion



Sunyaev & Zeldovich, 1980, ARAA, 18, 537

- also known from thSZ effect
- up-scattering of CMB photon
- important at late times ($z < 50000$)
- scattering inefficient

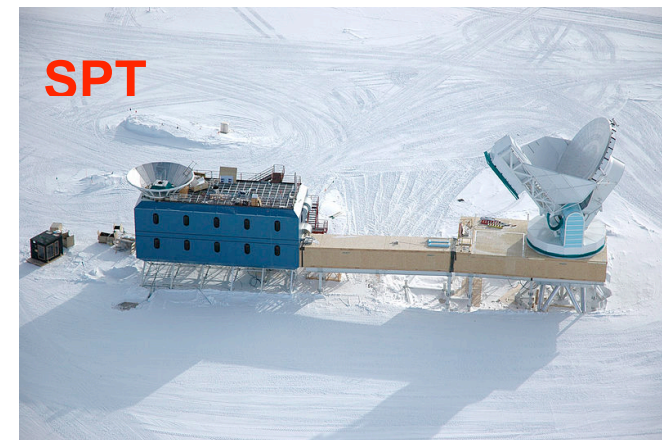
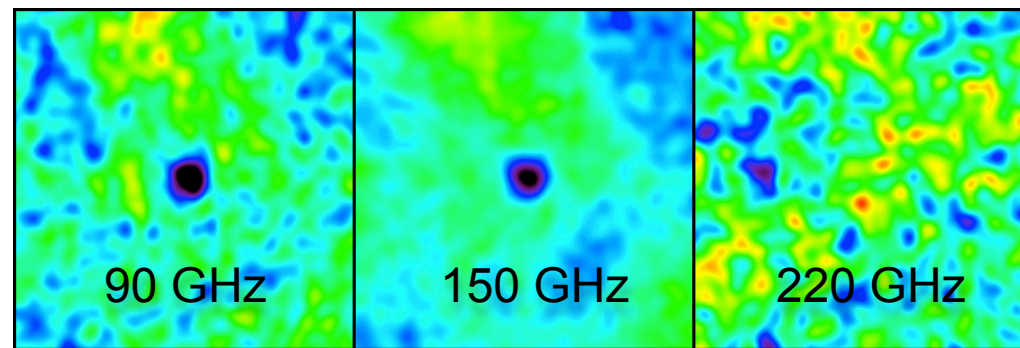
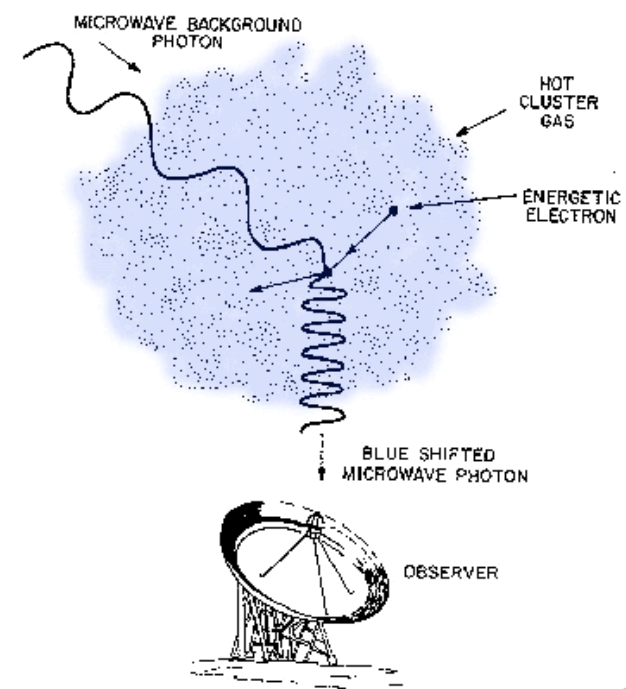
Chemical potential μ -distortion



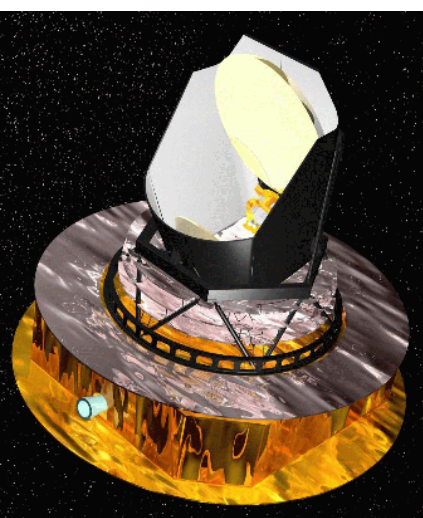
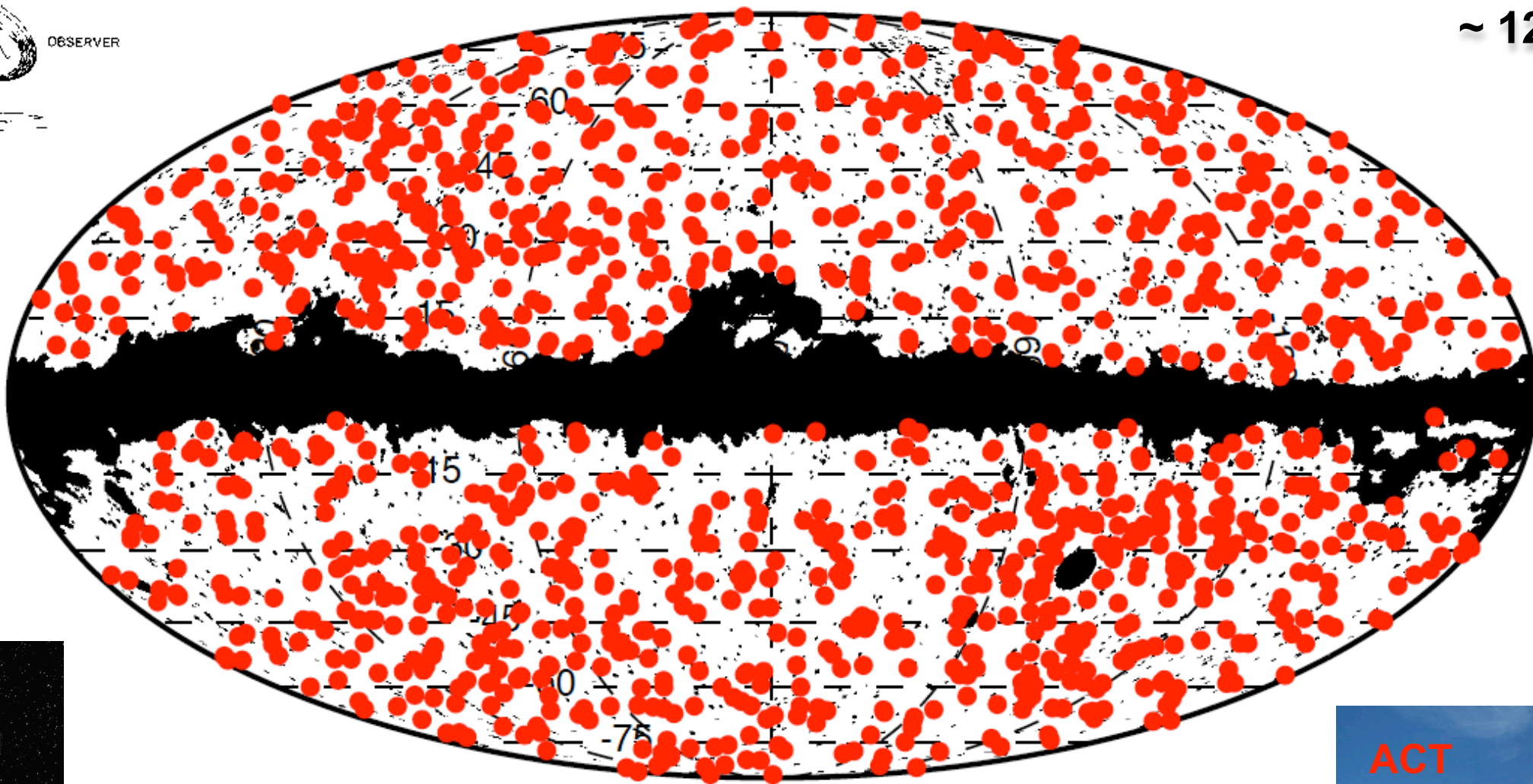
Sunyaev & Zeldovich, 1970, ApSS, 2, 66

- important at very times ($z > 50000$)
- scattering very efficient

Thermal SZ effect is now routinely observed!



~ 1230 objects

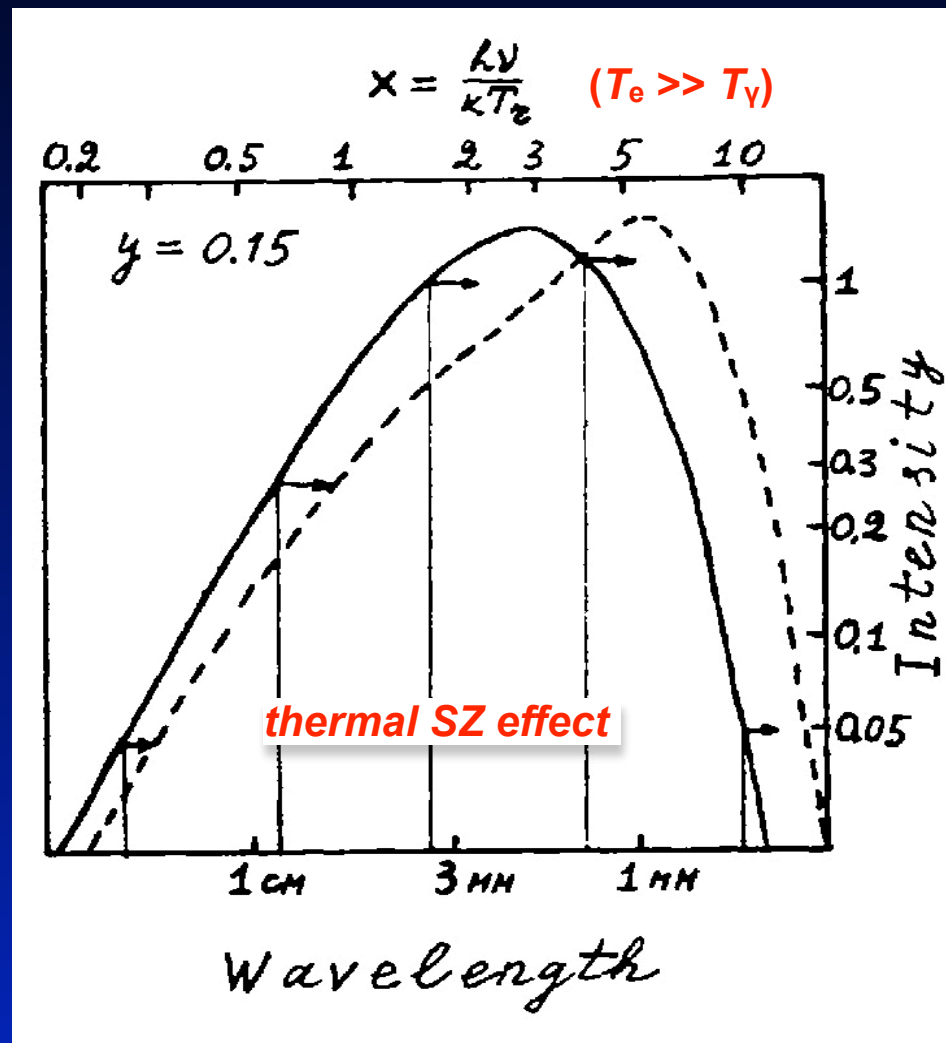


Planck Collaboration, 2013, paper XXIV



Standard types of primordial CMB distortions

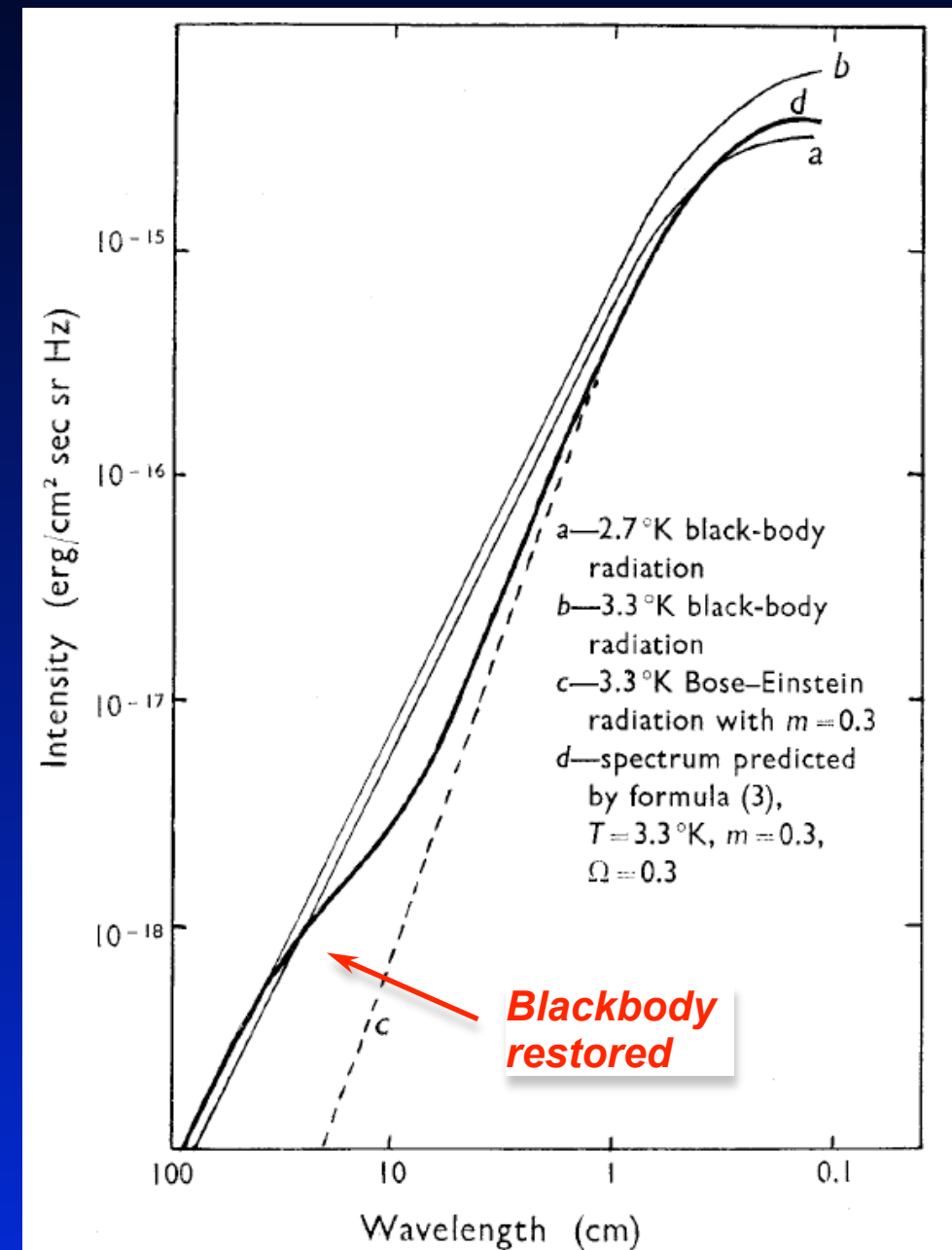
Compton y -distortion



Sunyaev & Zeldovich, 1980, ARAA, 18, 537

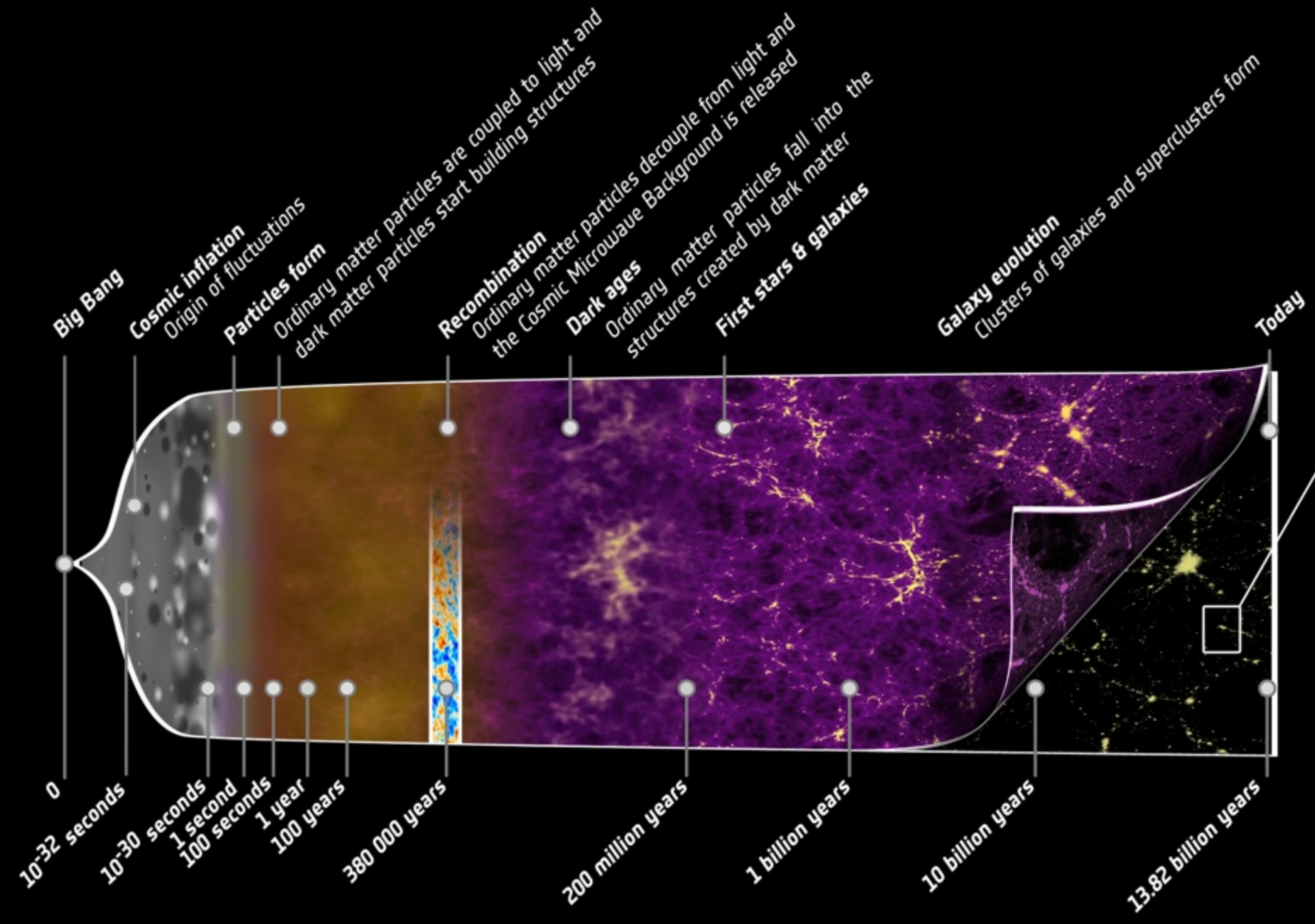
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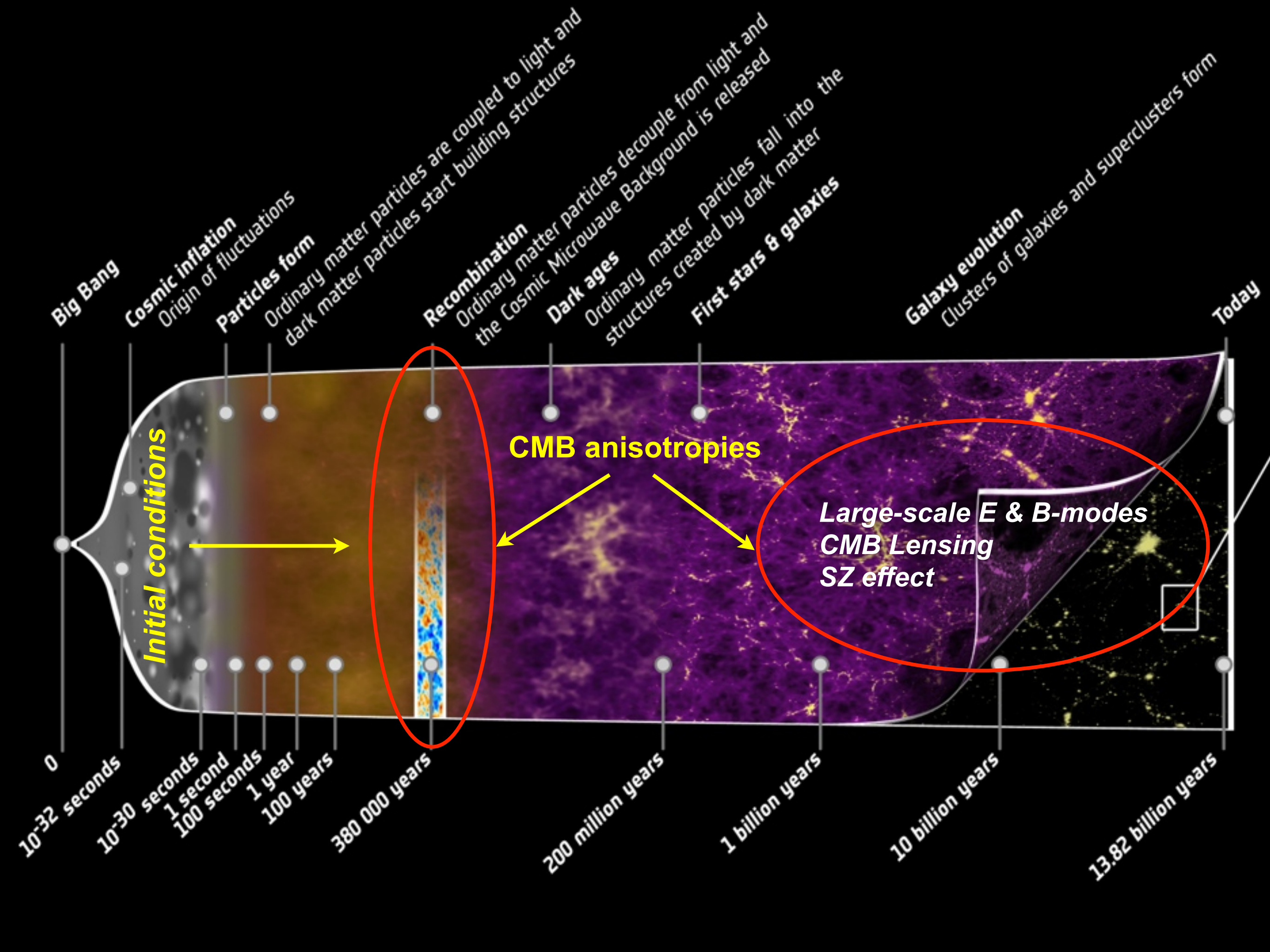
Chemical potential μ -distortion



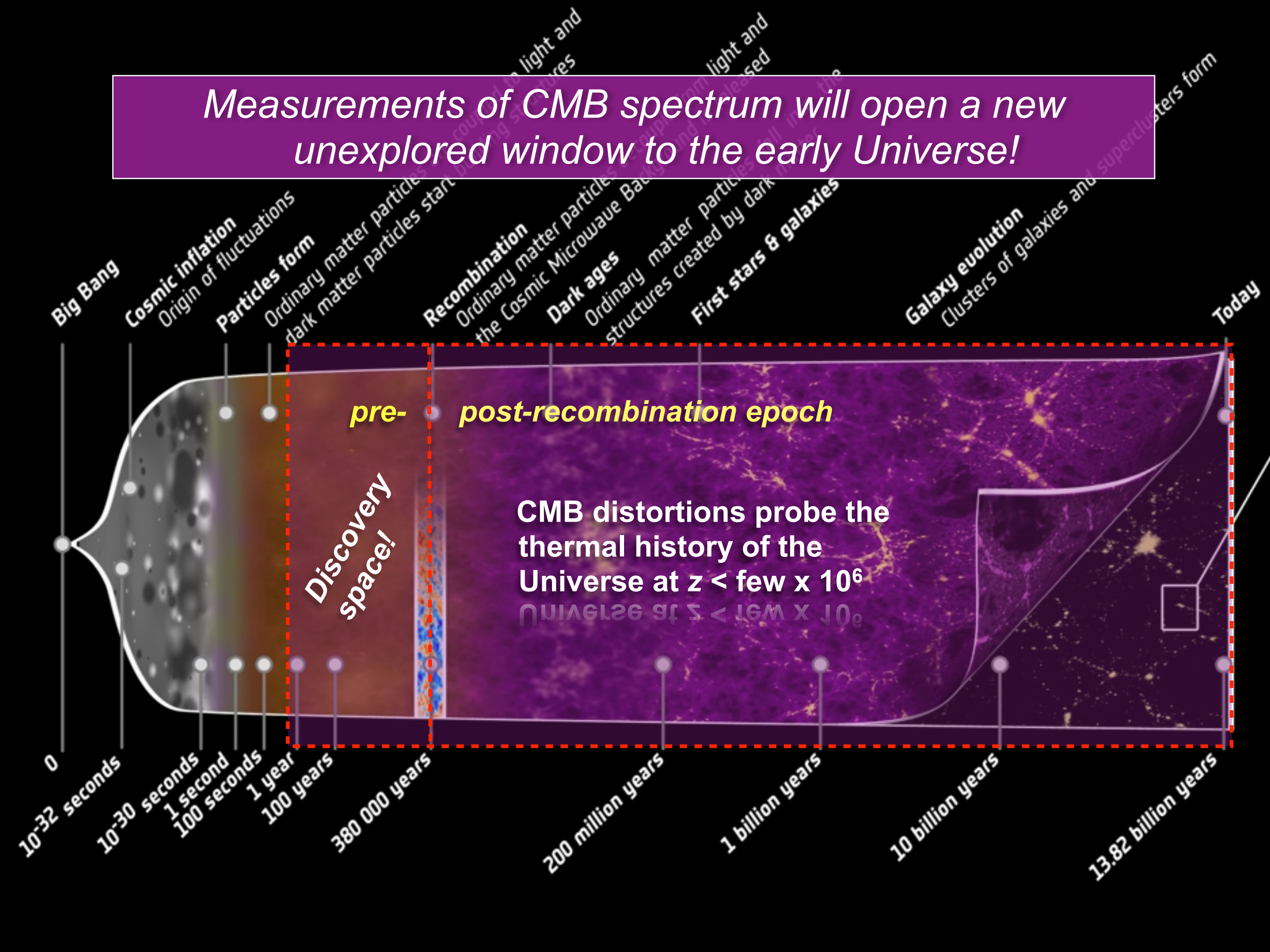
Sunyaev & Zeldovich, 1970, ApSS, 2, 66

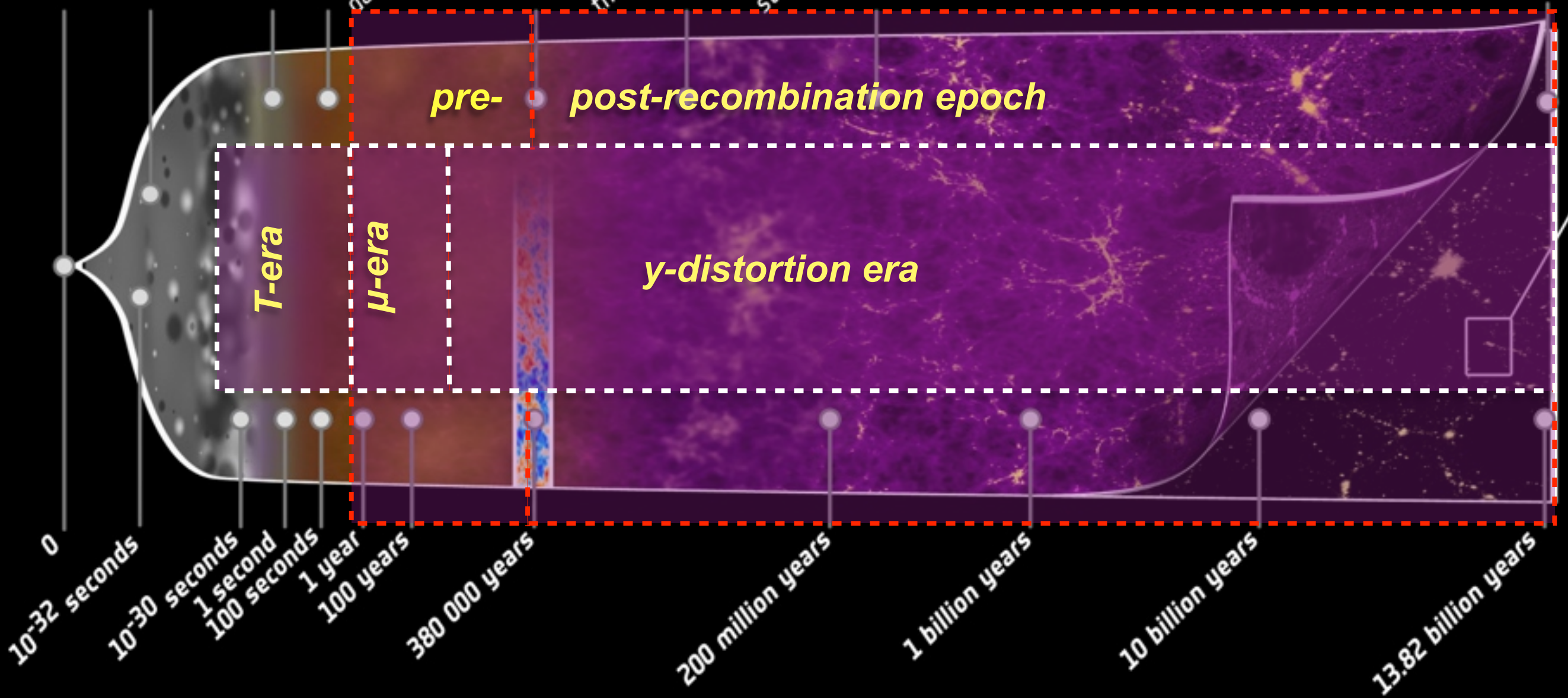
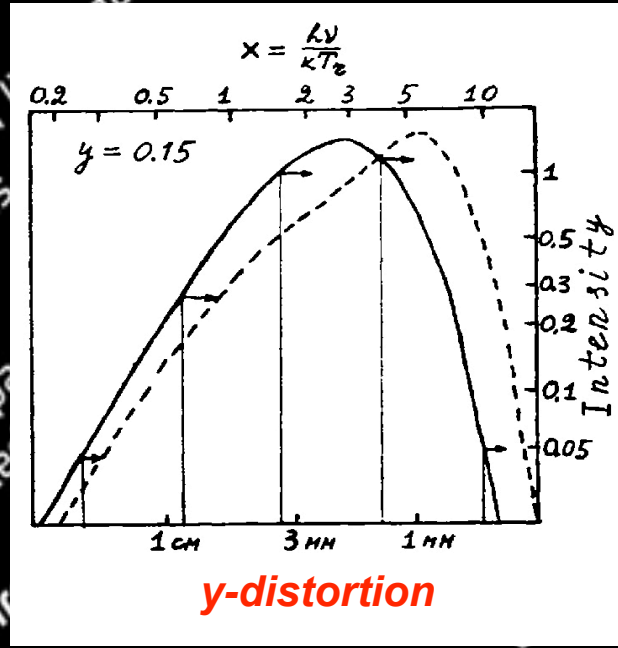
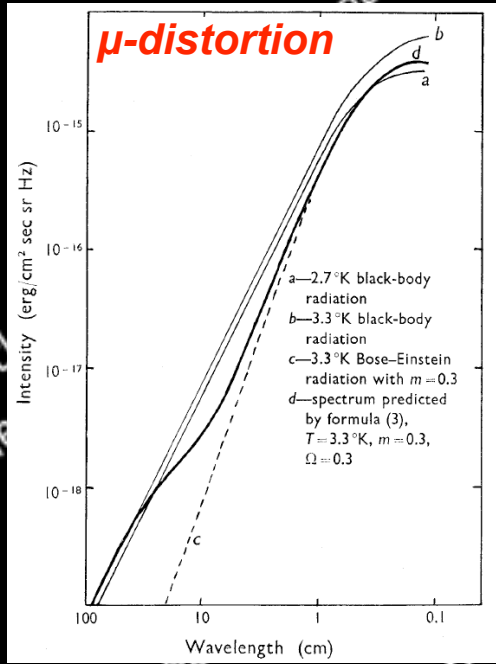
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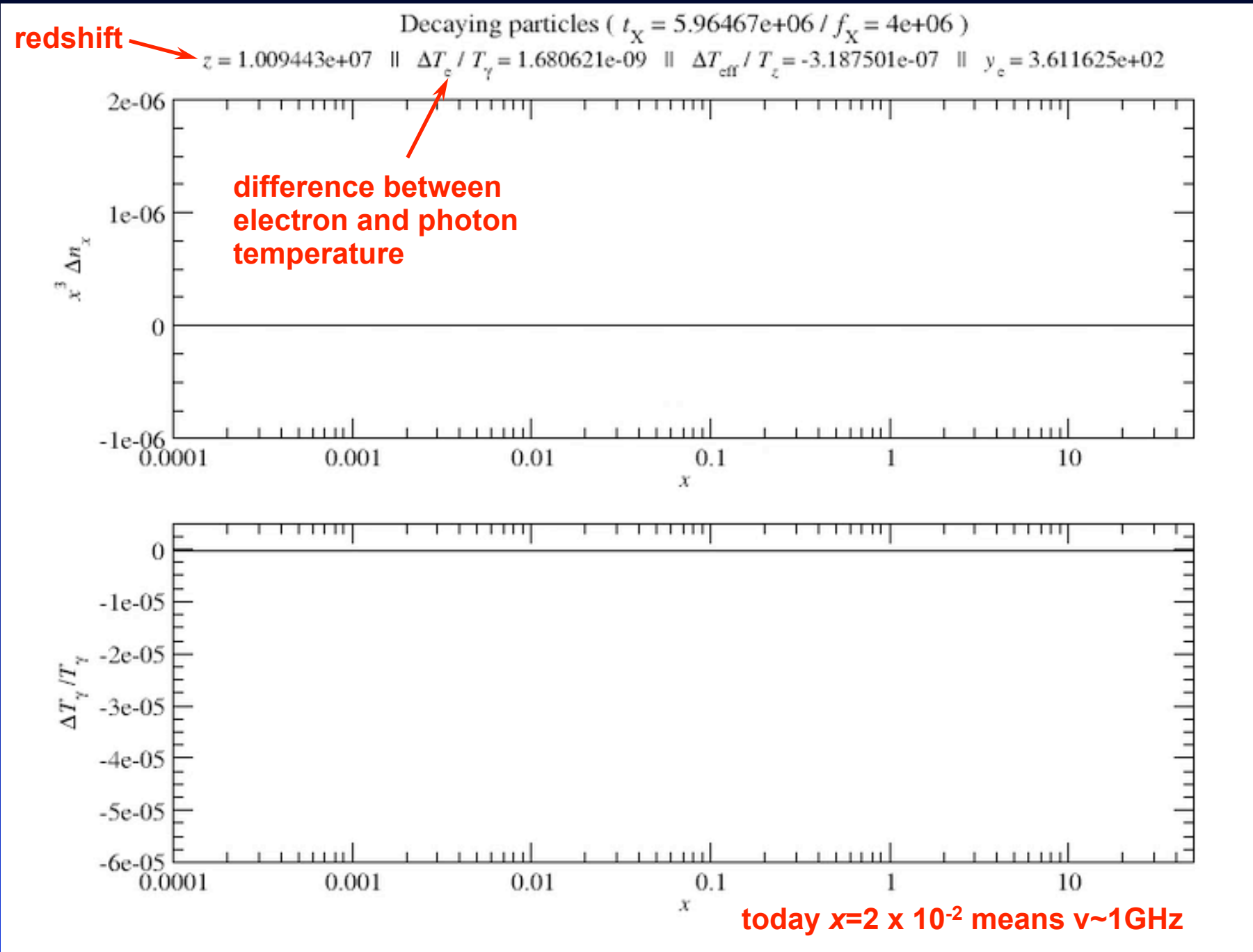


*Measurements of CMB spectrum will open a new
unexplored window to the early Universe!*





Example: *Energy release by decaying relict particle*



- initial condition: *full equilibrium*
- total energy release:
 $\Delta\rho/\rho \sim 1.3 \times 10^{-6}$
- most of energy release around:
 $z_X \sim 2 \times 10^6$
- positive μ -distortion
- high frequency distortion frozen around $z \approx 5 \times 10^5$
- late ($z < 10^3$) free-free absorption at very low

Quasi-Exact Treatment of the Thermalization Problem

- *For real forecasts of future prospects a precise & fast method for computing the spectral distortion is needed!*
- *Case-by-case computation of the distortion (e.g., with **CosmoTherm**, JC & Sunyaev, 2012, ArXiv:1109.6552) still rather time-consuming*
- ***But**: distortions are small \Rightarrow thermalization problem becomes linear!*
- ***Simple solution**: compute “response function” of the thermalization problem \Rightarrow Green’s function approach (JC, 2013, ArXiv:1304.6120)*
- *Final distortion for fixed energy-release history given by*

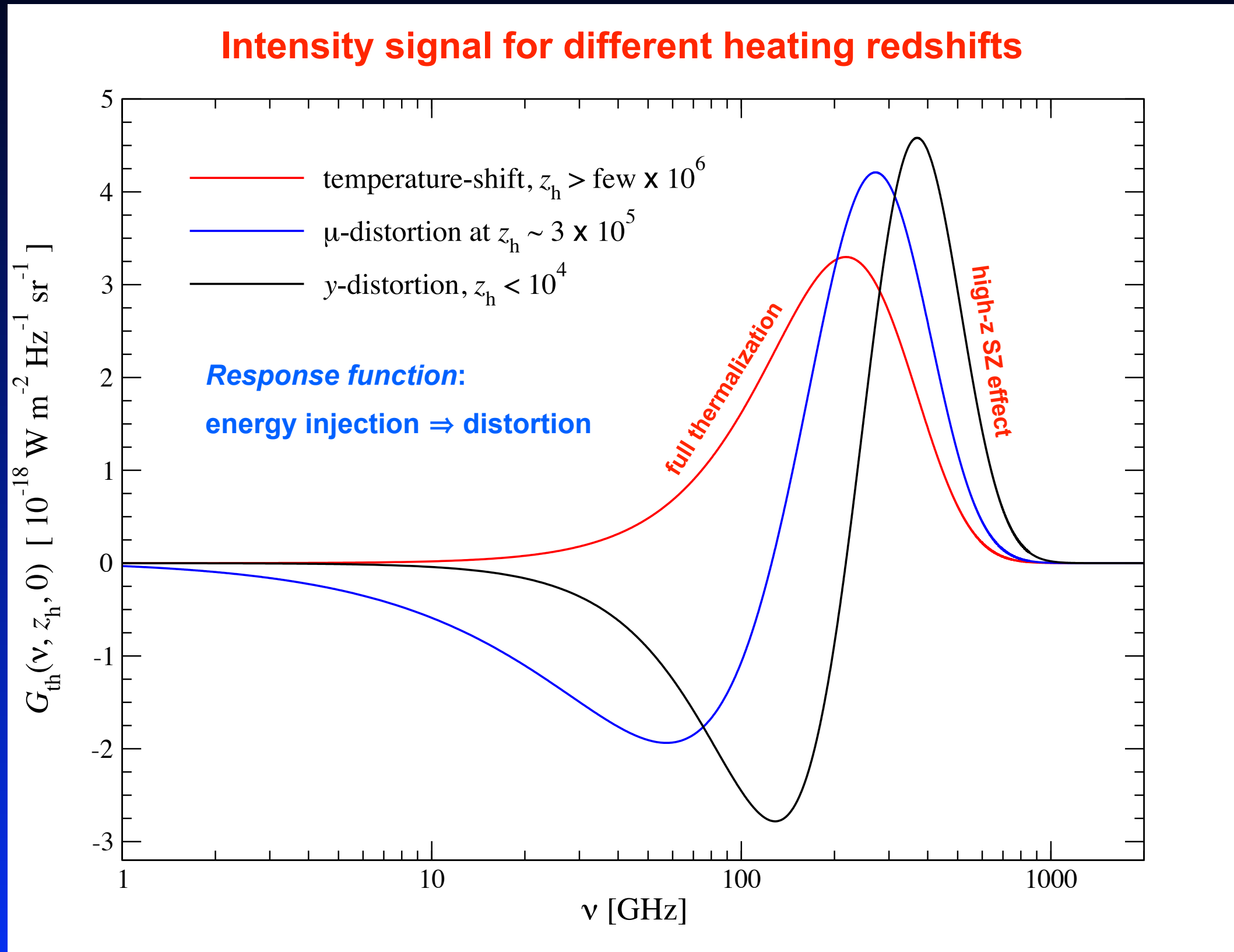
$$\Delta I_\nu \approx \int_0^\infty G_{\text{th}}(\nu, z') \frac{d(Q/\rho_\gamma)}{dz'} dz'$$

 **Thermalization Green's function**

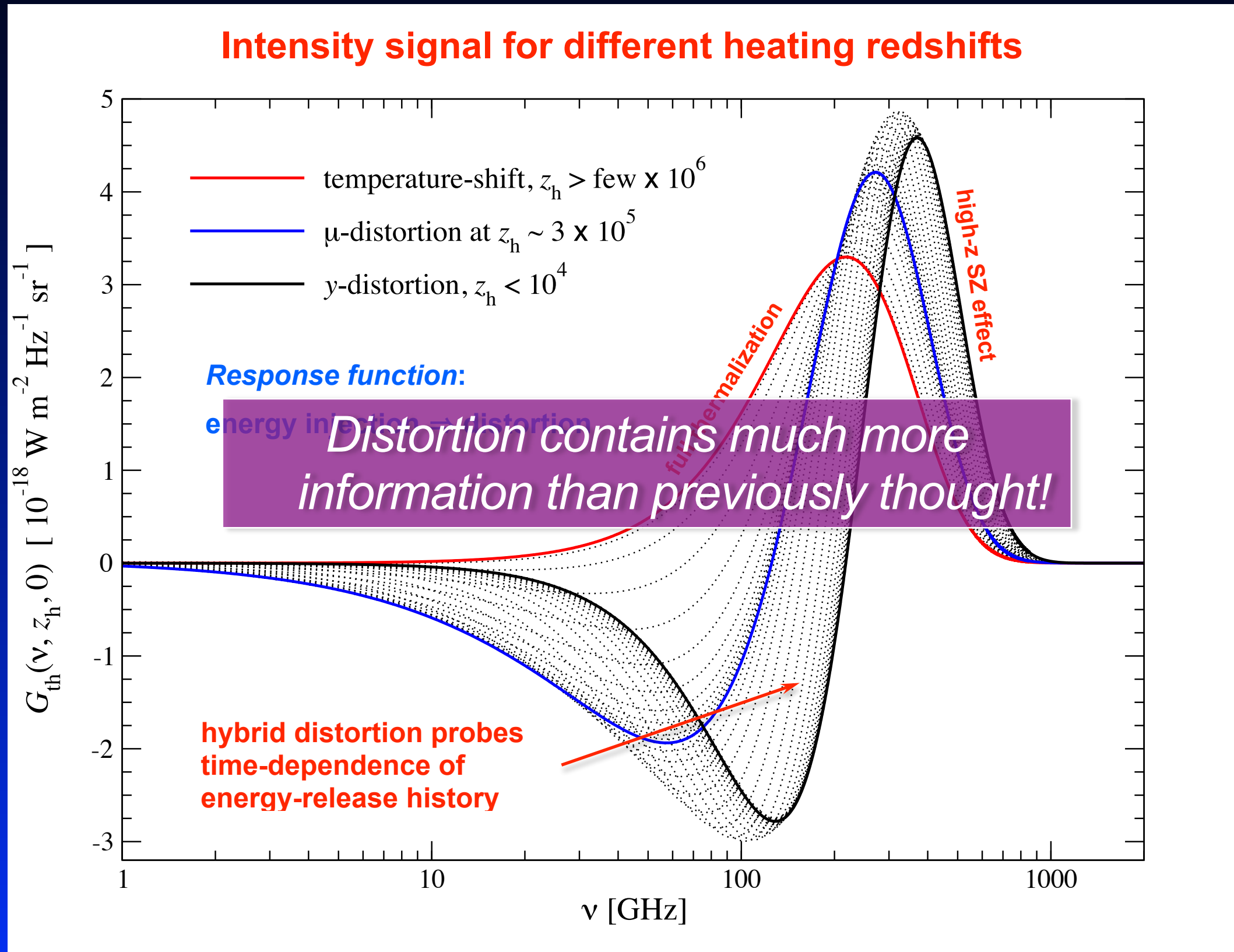
- *Fast and quasi-exact! No additional approximations!*

CosmoTherm available at: www.Chluba.de/CosmoTherm

What does the spectrum look like after energy injection?



What does the spectrum look like after energy injection?



Transition from y -distortion $\rightarrow \mu$ -distortion

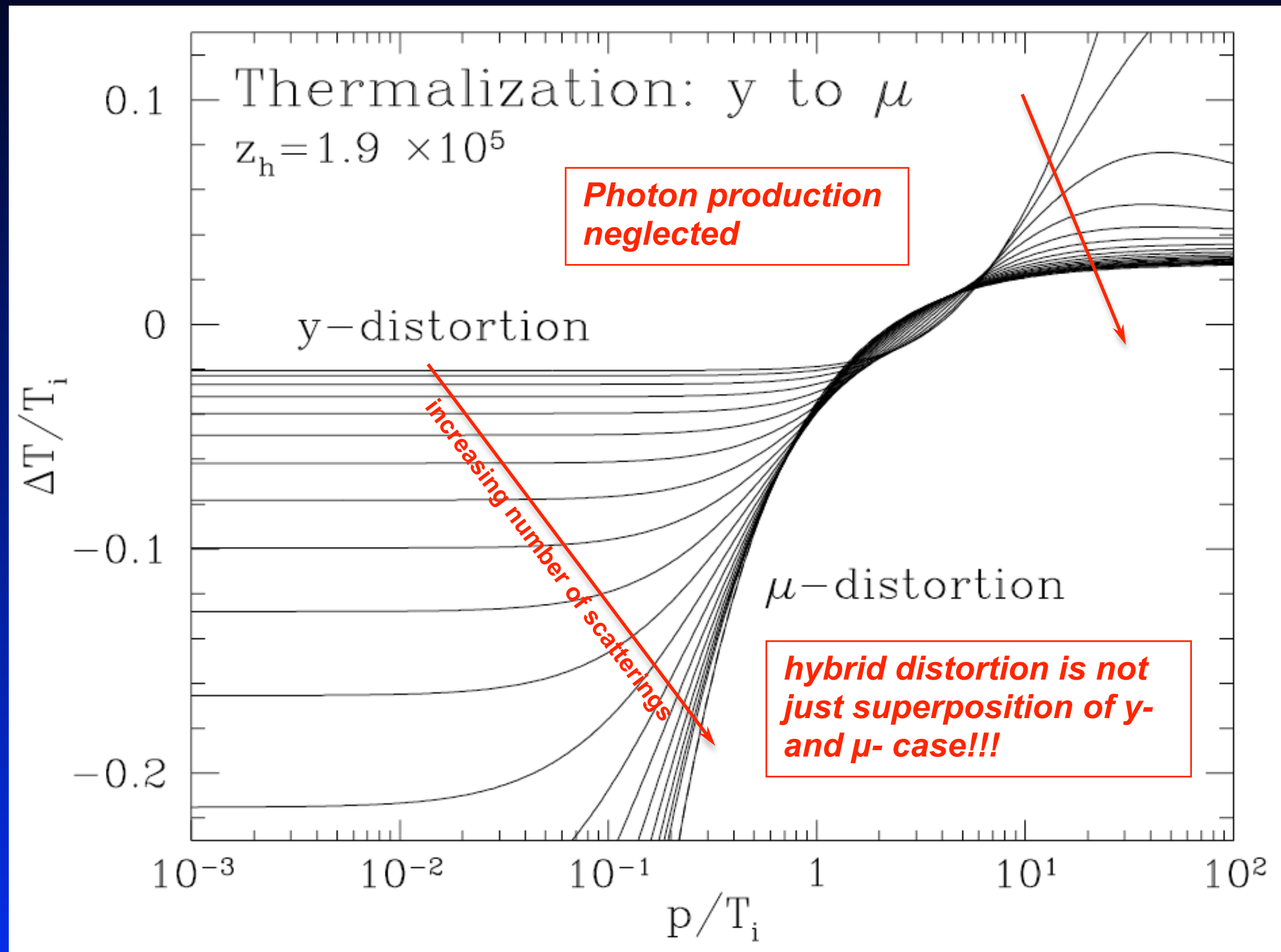
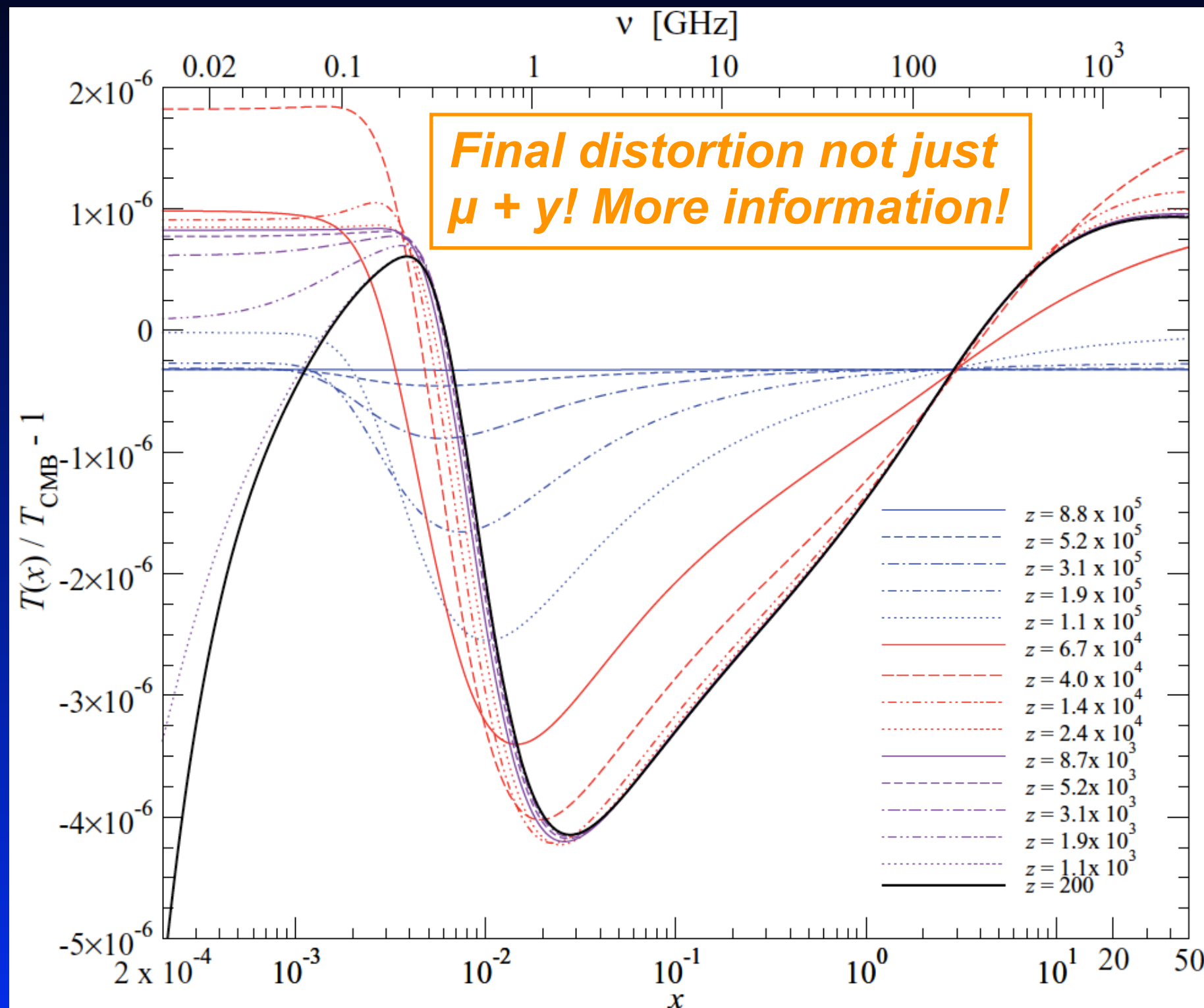
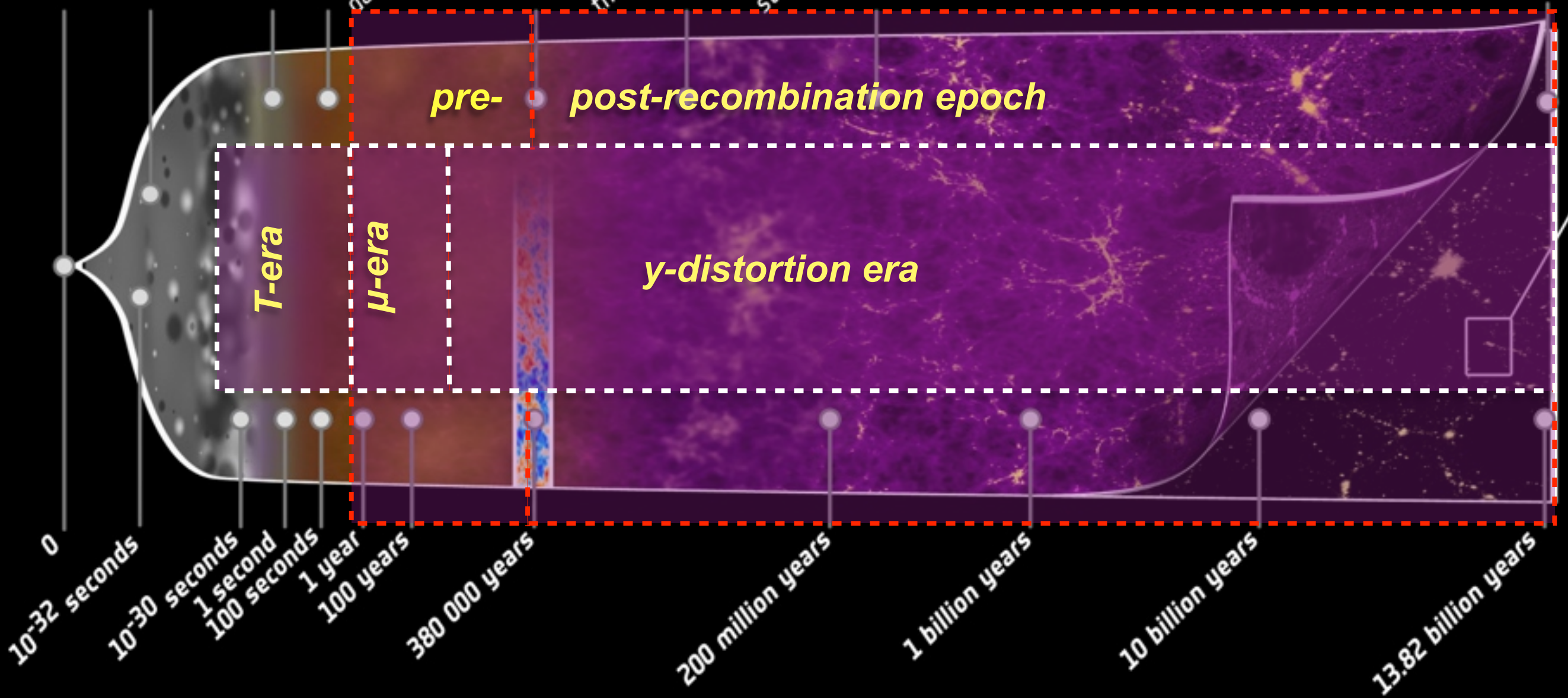
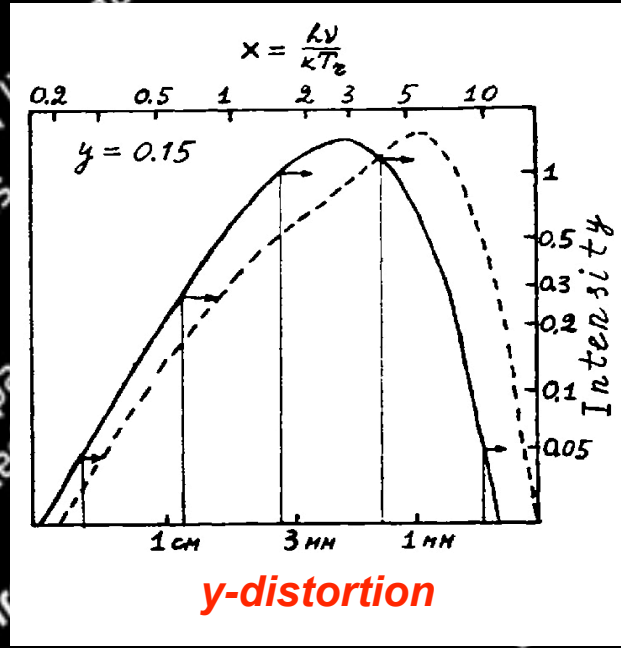
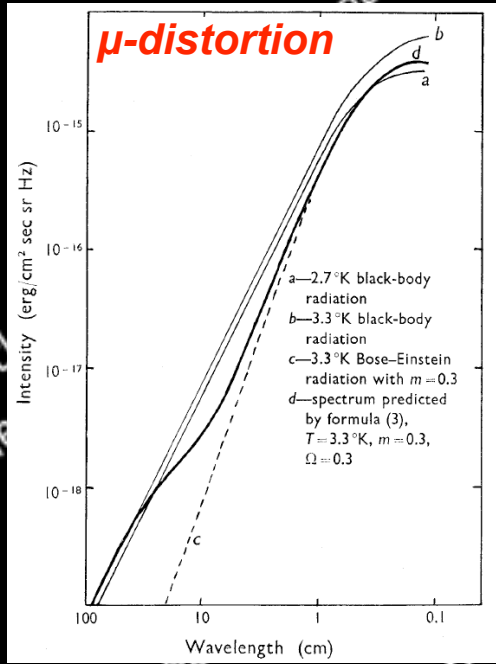
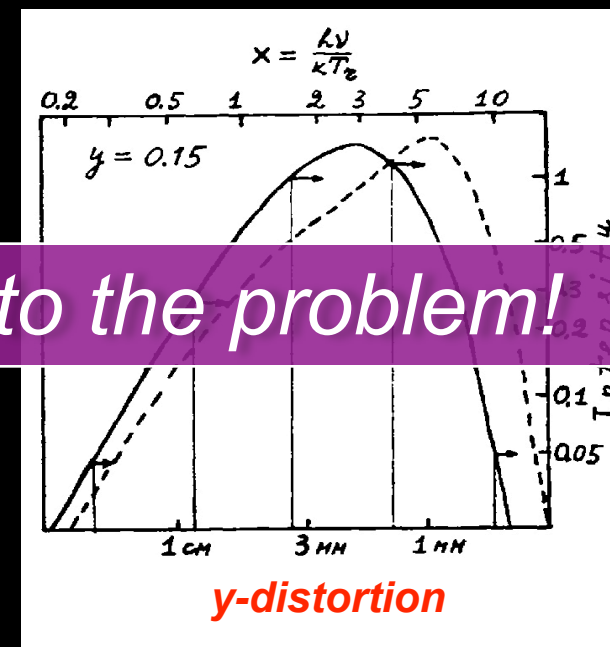
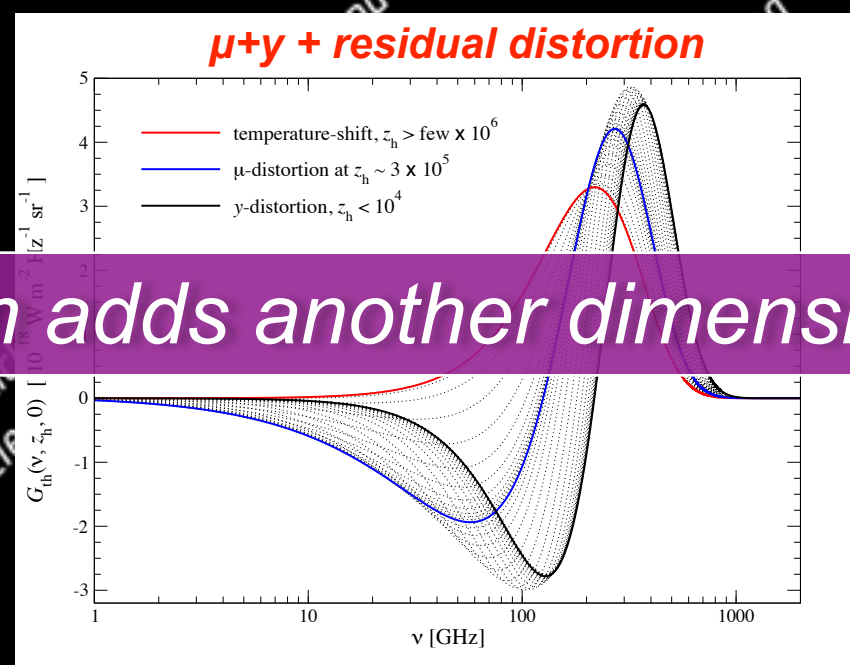
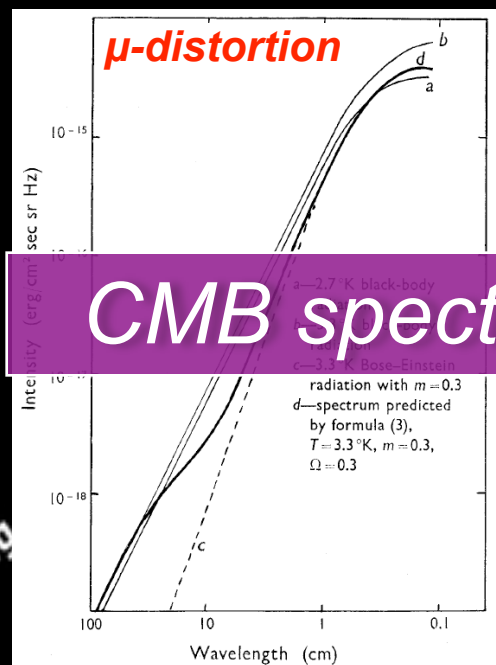


Figure from Wayne Hu's PhD thesis, 1995, but see also discussion in Burigana, 1991

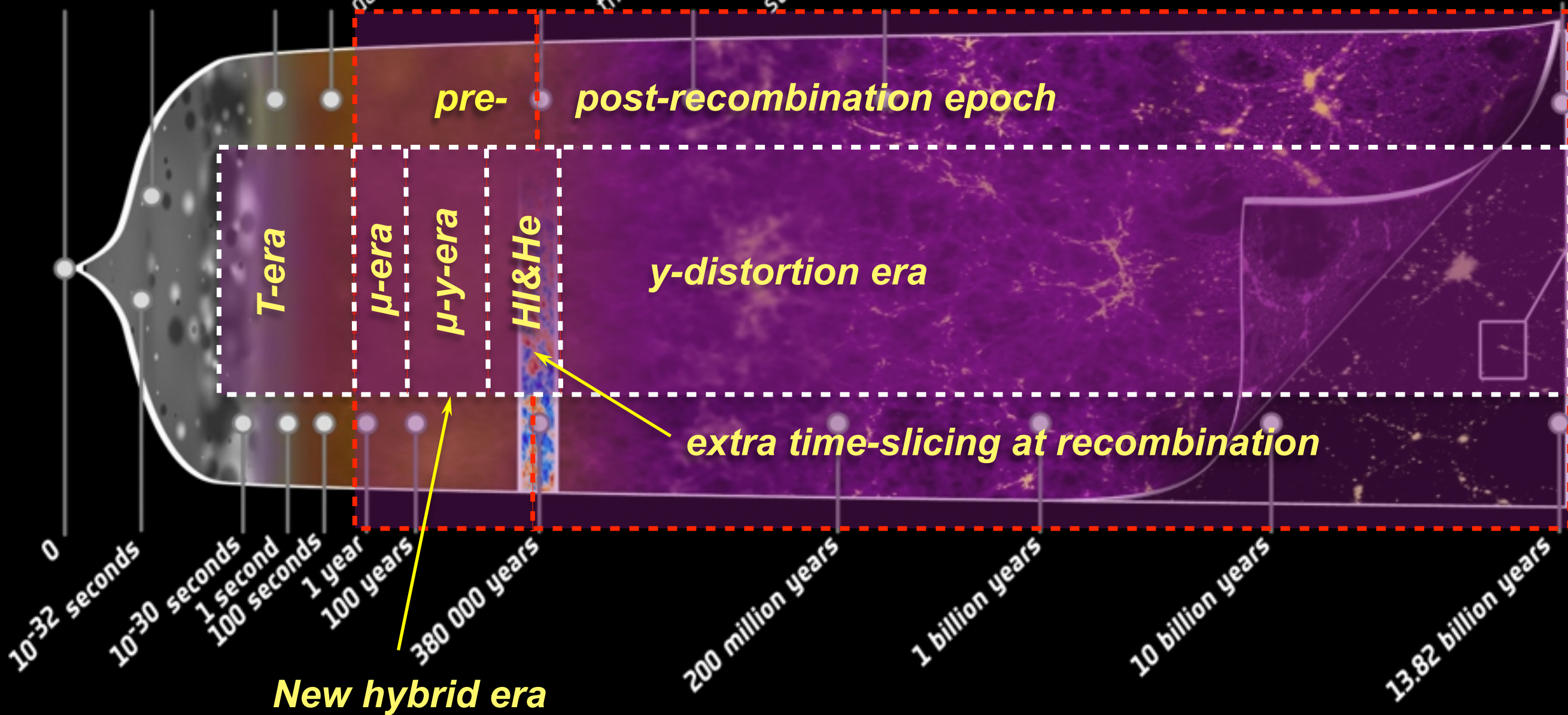
Distortion *not* just superposition of μ and y -distortion!



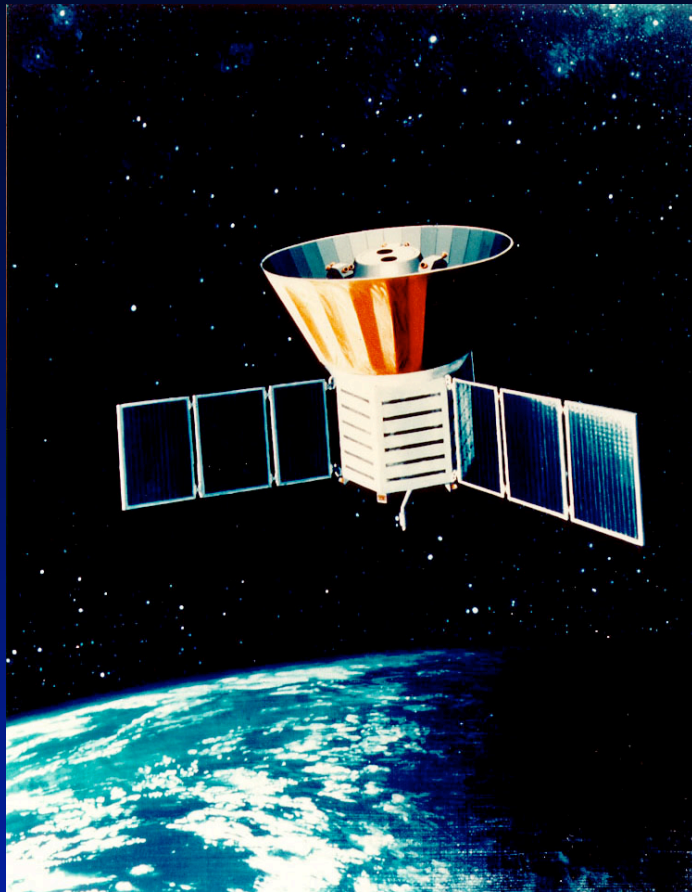




CMB spectrum adds another dimension to the problem!



COBE / FIRAS (Far InfraRed Absolute Spectrophotometer)

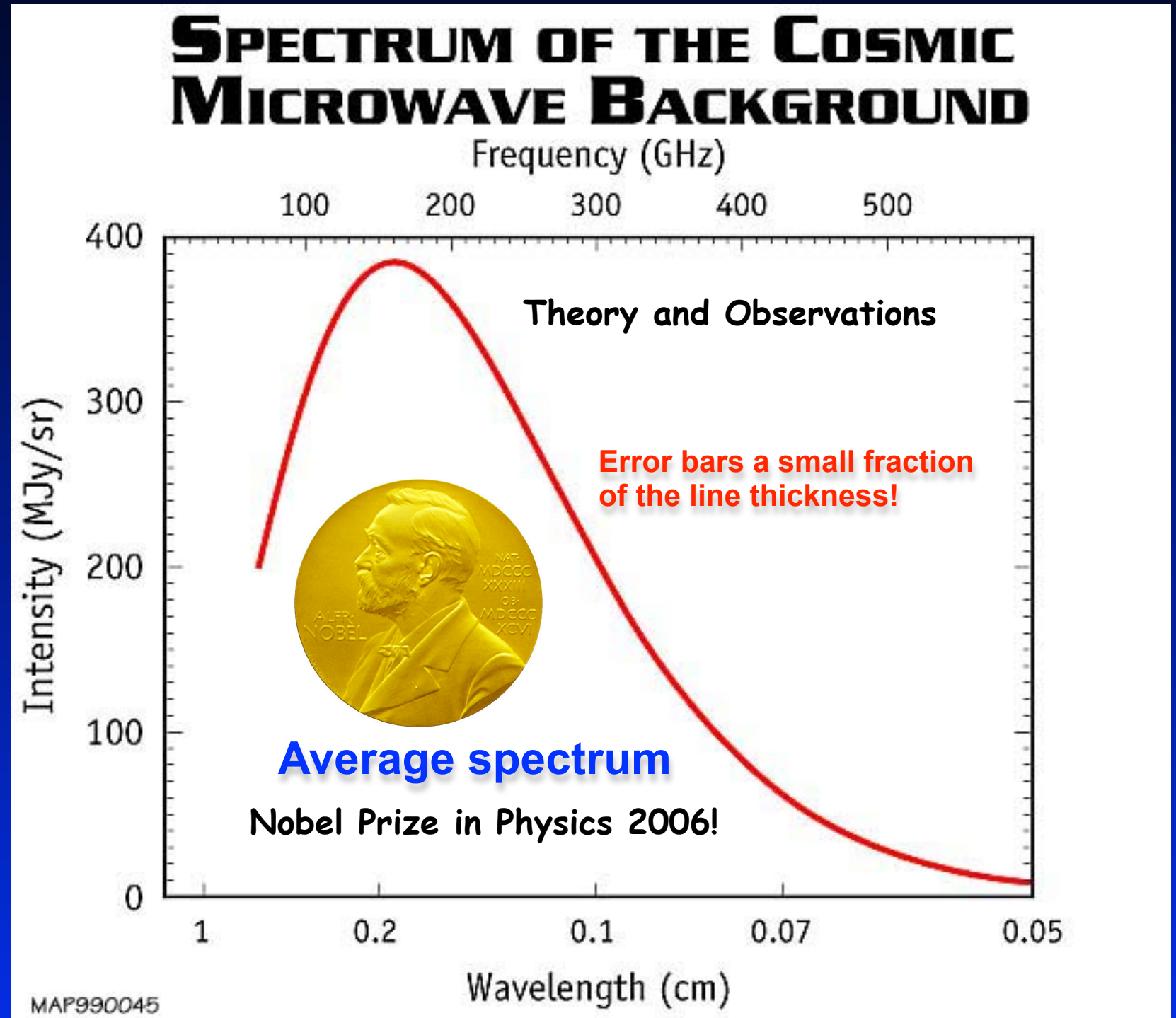


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$$|\mu| \leq 9 \times 10^{-5}$$

Mather et al., 1994, ApJ, 420, 439
Fixsen et al., 1996, ApJ, 473, 576
Fixsen et al., 2003, ApJ, 594, 67



Only very small distortions of CMB spectrum are still allowed!

Physical mechanisms that lead to spectral distortions

- *Cooling by adiabatically expanding ordinary matter*
(JC, 2005; JC & Sunyaev 2011; Khatri, Sunyaev & JC, 2011)
 - Heating by *decaying* or *annihilating* relic particles
(Kawasaki et al., 1987; Hu & Silk, 1993; McDonald et al., 2001; JC, 2005; JC & Sunyaev, 2011; JC, 2013; JC & Jeong, 2013)
 - *Evaporation of primordial black holes & superconducting strings*
(Carr et al. 2010; Ostriker & Thompson, 1987; Tashiro et al. 2012; Pani & Loeb, 2013)
 - *Dissipation of primordial acoustic modes & magnetic fields*
(Sunyaev & Zeldovich, 1970; Daly 1991; Hu et al. 1994; JC & Sunyaev, 2011; JC et al. 2012 - Jedamzik et al. 2000; Kunze & Komatsu, 2013)
 - *Cosmological recombination radiation*
(Zeldovich et al., 1968; Peebles, 1968; Dubrovich, 1977; Rubino-Martin et al., 2006; JC & Sunyaev, 2006; Sunyaev & JC, 2009)
-
- Signatures due to first supernovae and their remnants
(Oh, Cooray & Kamionkowski, 2003)
 - Shock waves arising due to large-scale structure formation
(Sunyaev & Zeldovich, 1972; Cen & Ostriker, 1999)
 - SZ-effect from clusters; effects of reionization
(Refregier et al., 2003; Zhang et al. 2004; Trac et al. 2008)
 - more exotic processes
(Lochan et al. 2012; Bull & Kamionkowski, 2013; Brax et al., 2013; Tashiro et al. 2013)

„high“ redshifts

„low“ redshifts

pre-recombination epoch

post-recombination

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*Standard sources
of distortions*

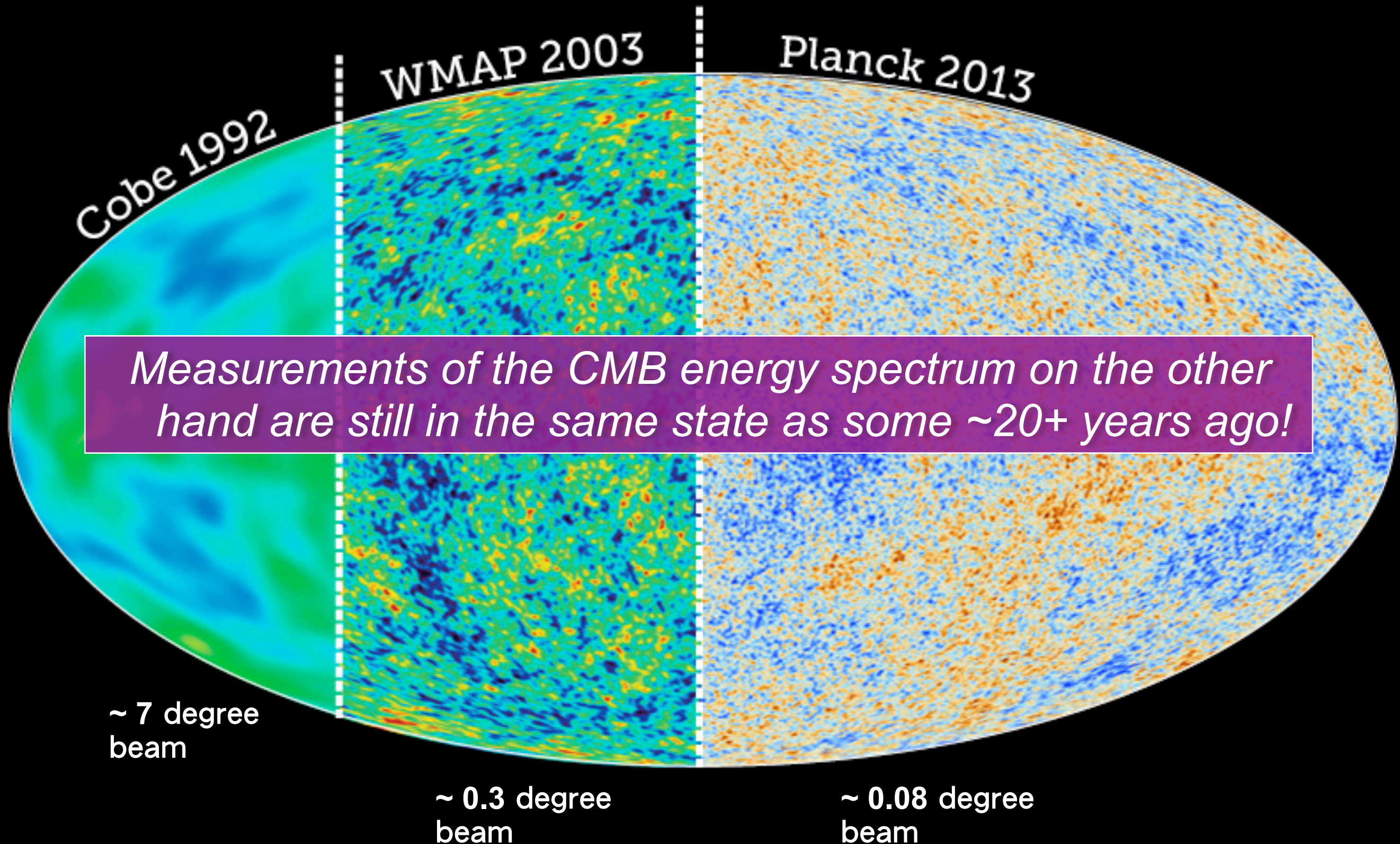
pre-recombination epoch

„high“ redshifts

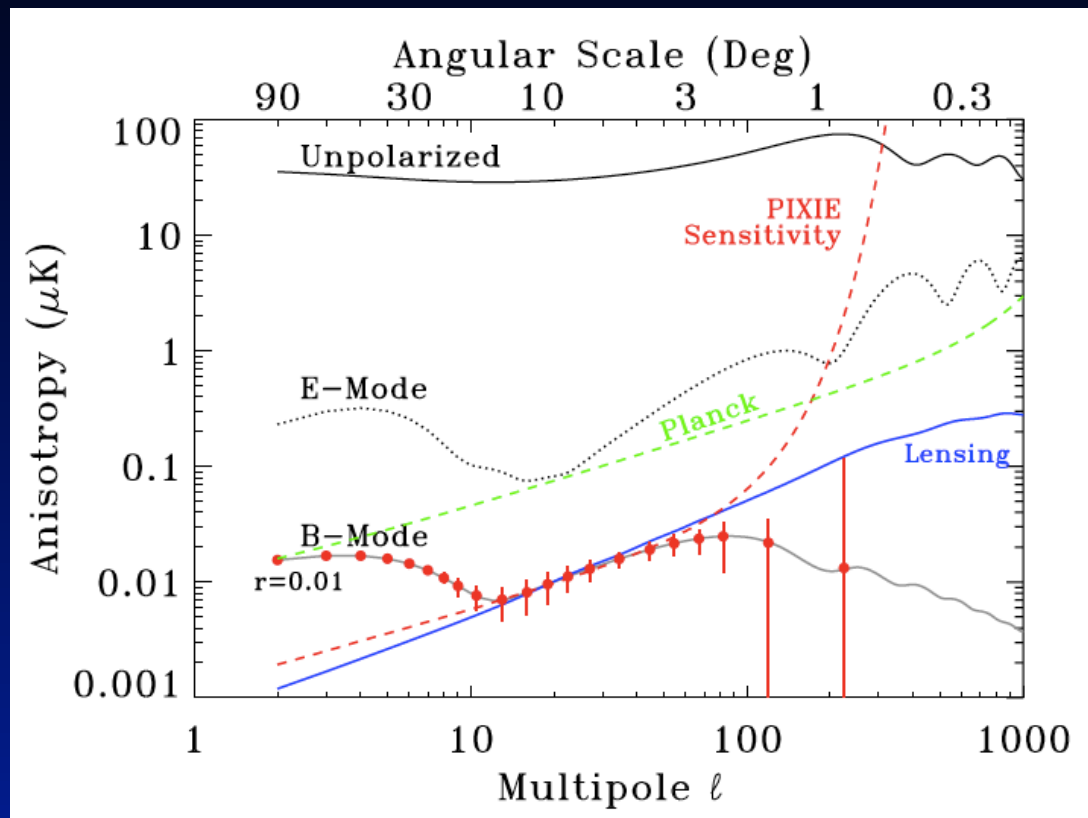
„low“ redshifts

post-recombination

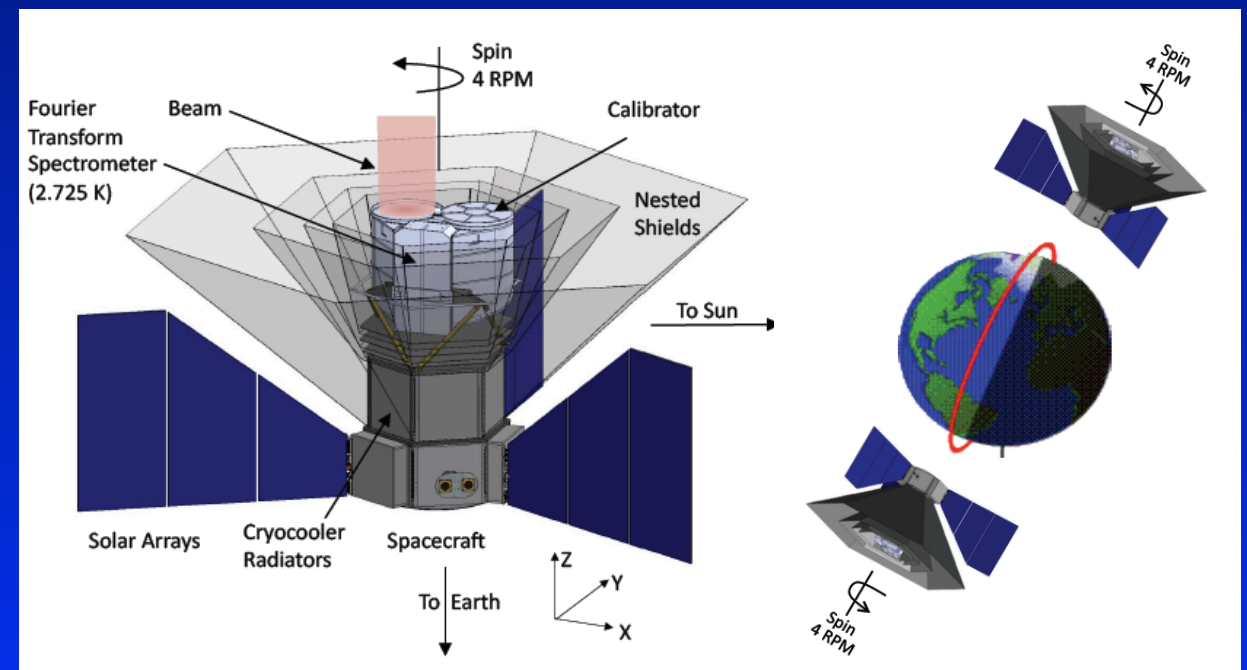
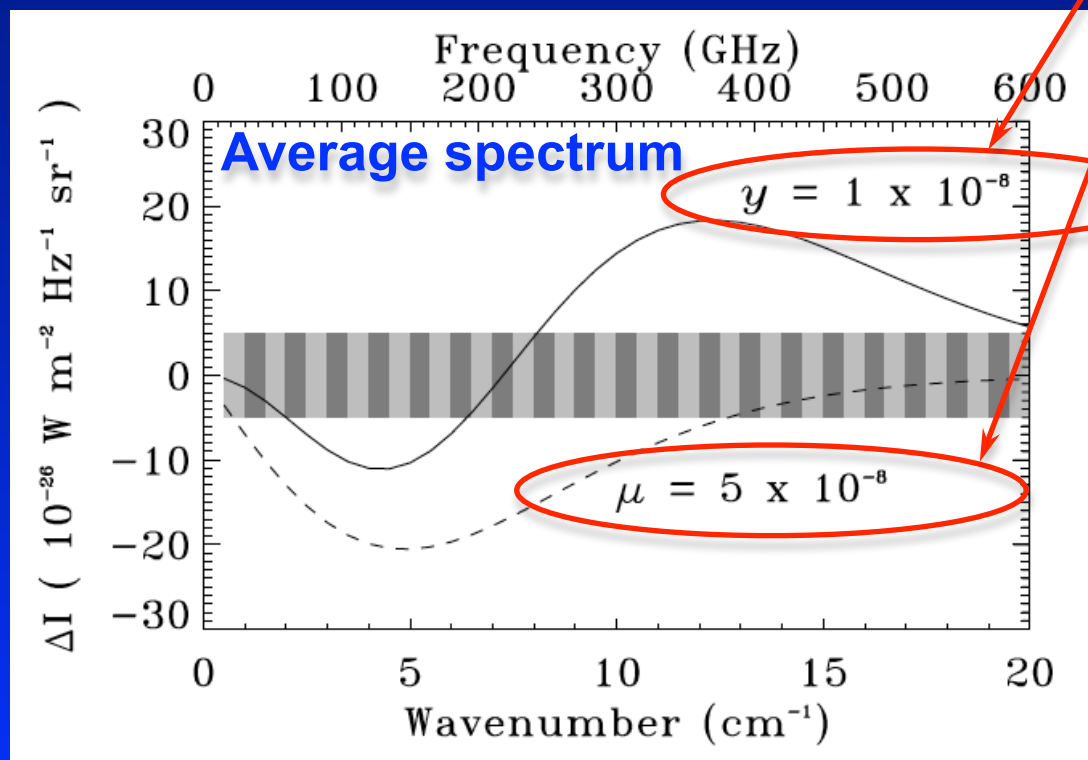
Dramatic improvements in angular resolution and sensitivity over the past decades!



PIXIE: Primordial Inflation Explorer



- 400 spectral channel in the frequency range 30 GHz and 6THz ($\Delta\nu \sim 15\text{GHz}$)
- about 1000 (!!!) times more sensitive than COBE/FIRAS
- B-mode polarization from inflation ($r \approx 10^{-3}$)
- improved limits on μ and y
- was proposed 2011 as NASA EX mission





Enduring Quests Daring Visions

NASA Astrophysics in the Next Three Decades

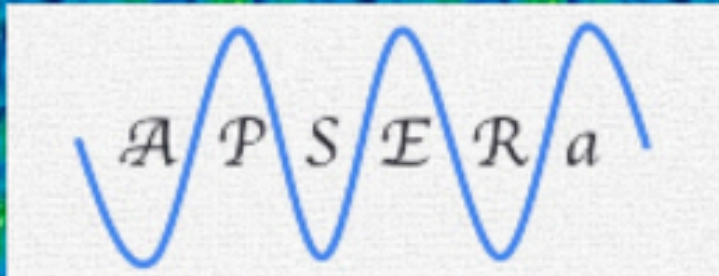
NASA 30-yr Roadmap Study

(published Dec 2013)

How does the Universe work?

"Measure the spectrum of the **CMB** with precision several orders of magnitude higher than COBE FIRAS, from a **moderate-scale mission** or an instrument on **CMB Polarization Surveyor**."

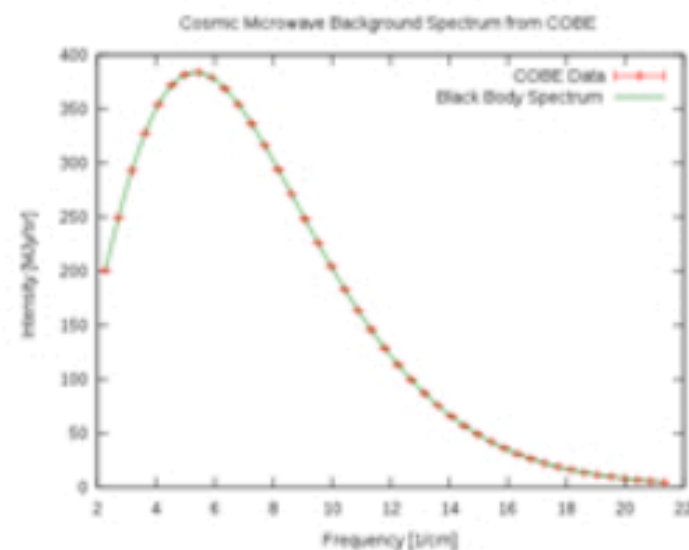
*PIXIE was proposed to
NASA in Dec 2016.
Decision this year!*



Array of Precision Spectrometers for detecting spectral ripples from the Epoch of RecombinAtion

HOME

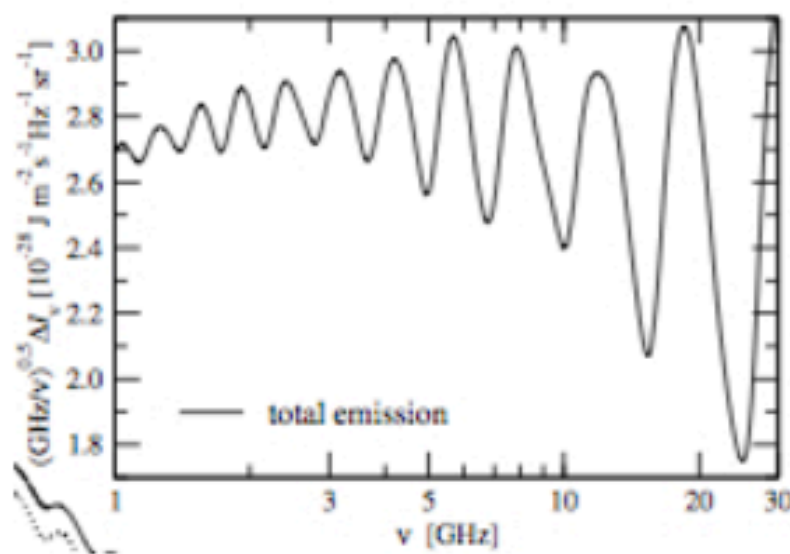
PEOPLE



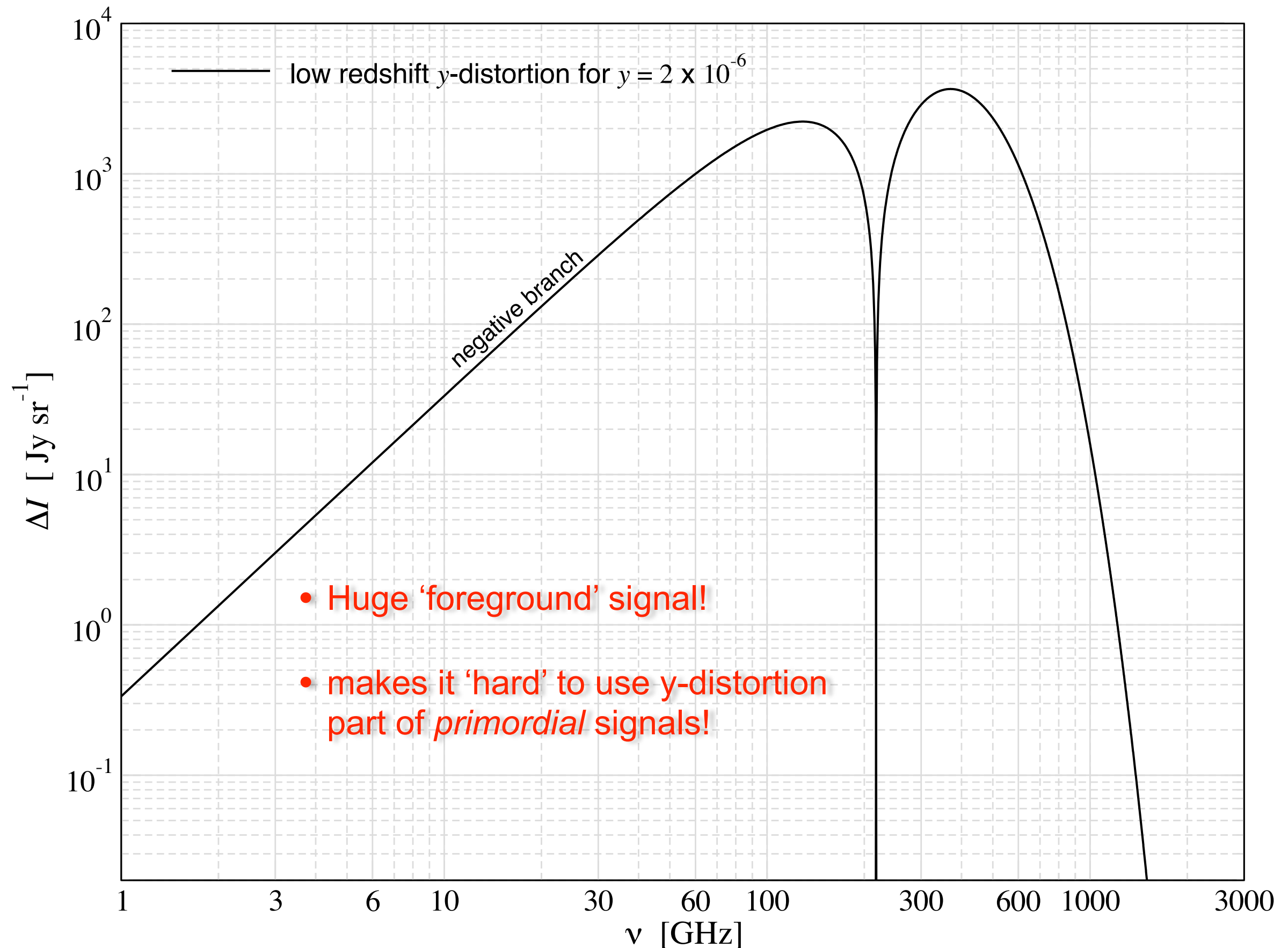
About APSERa

The Array of Precision Spectrometers for the Epoch of RecombinAtion - APSERa - is a venture to detect recombination lines from the Epoch of Cosmological Recombination. These are predicted to manifest as 'ripples' in wideband spectra of the cosmic radio background (CRB) since recombination of the primeval plasma in the early Universe adds broad spectral lines to the relic Cosmic Radiation. The lines are extremely wide because recombination is stalled and extended over redshift space. The spectral features are expected to be isotropic over the whole sky.

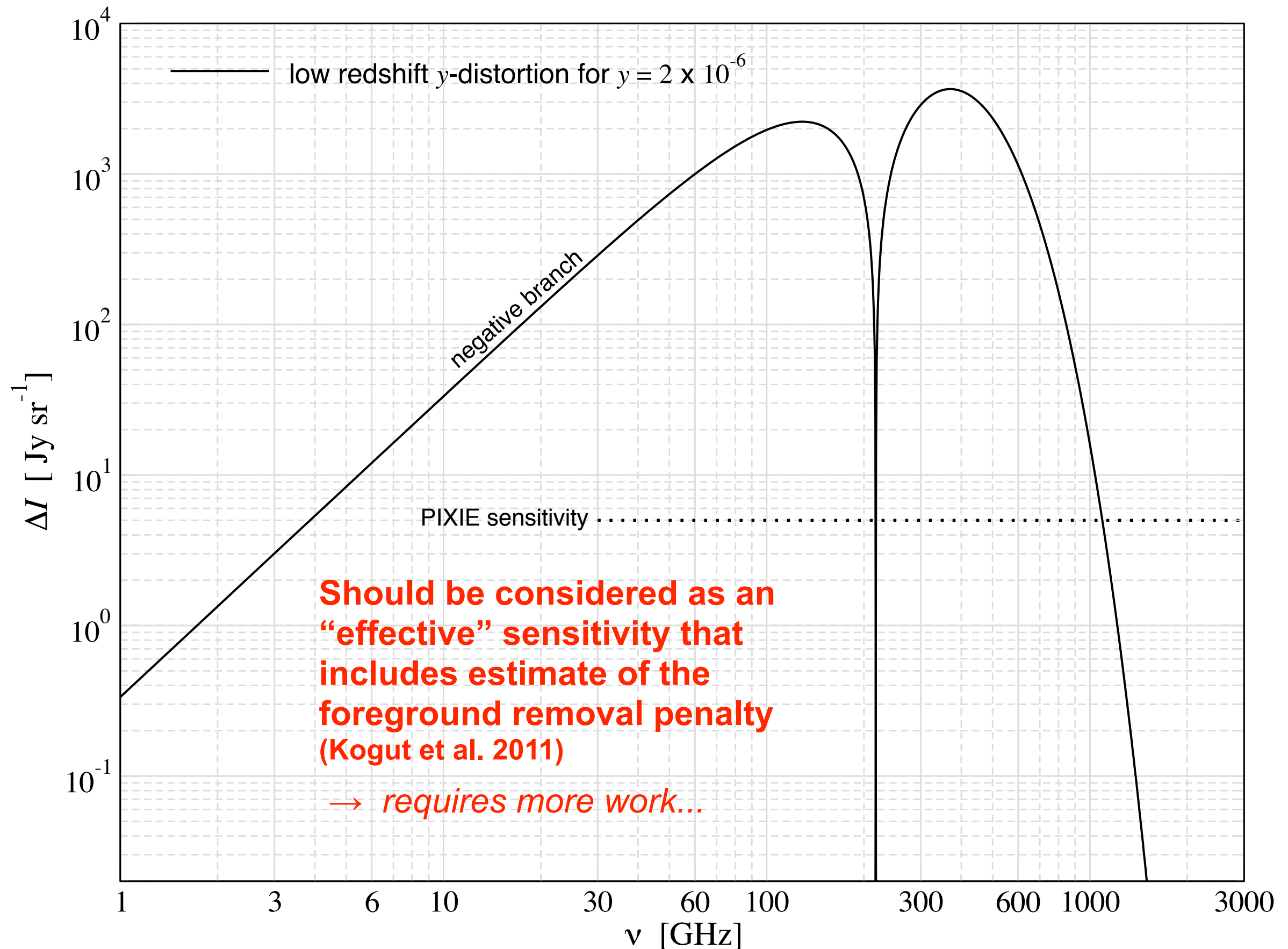
The project will comprise of an array of 128 small telescopes that are purpose built to detect a set of adjacent lines from cosmological recombination in the spectrum of the radio sky in the 2-6 GHz range. The radio receivers are being designed and built at the Raman Research Institute, tested in nearby radio-quiet locations and relocated to a remote site for long duration exposures to detect the subtle features in the cosmic radio background arising from recombination. The observing site would be appropriately chosen to minimize RFI from geostationary satellites and to be able to observe towards sky regions relatively low in foreground brightness.



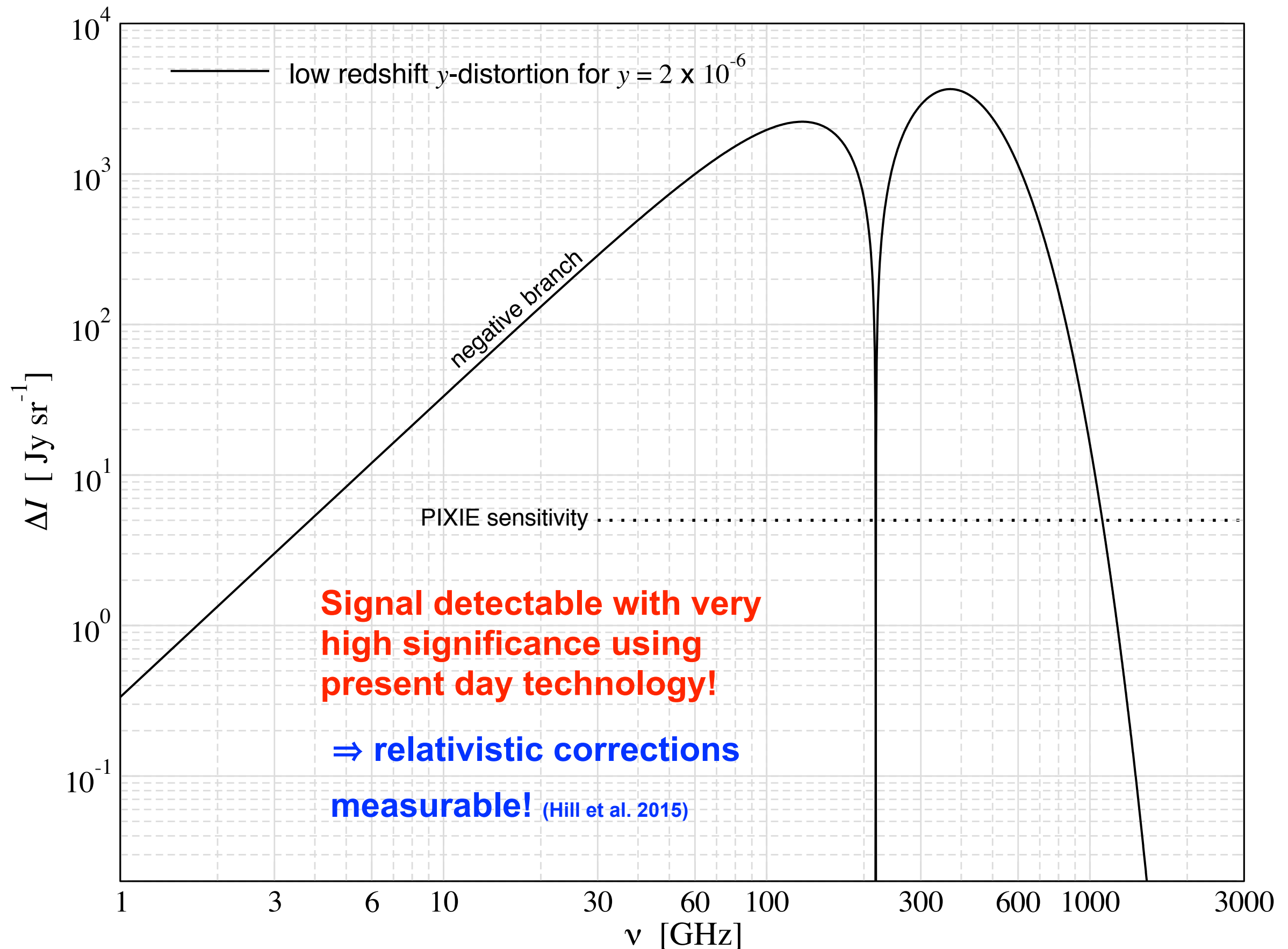
Average CMB spectral distortions



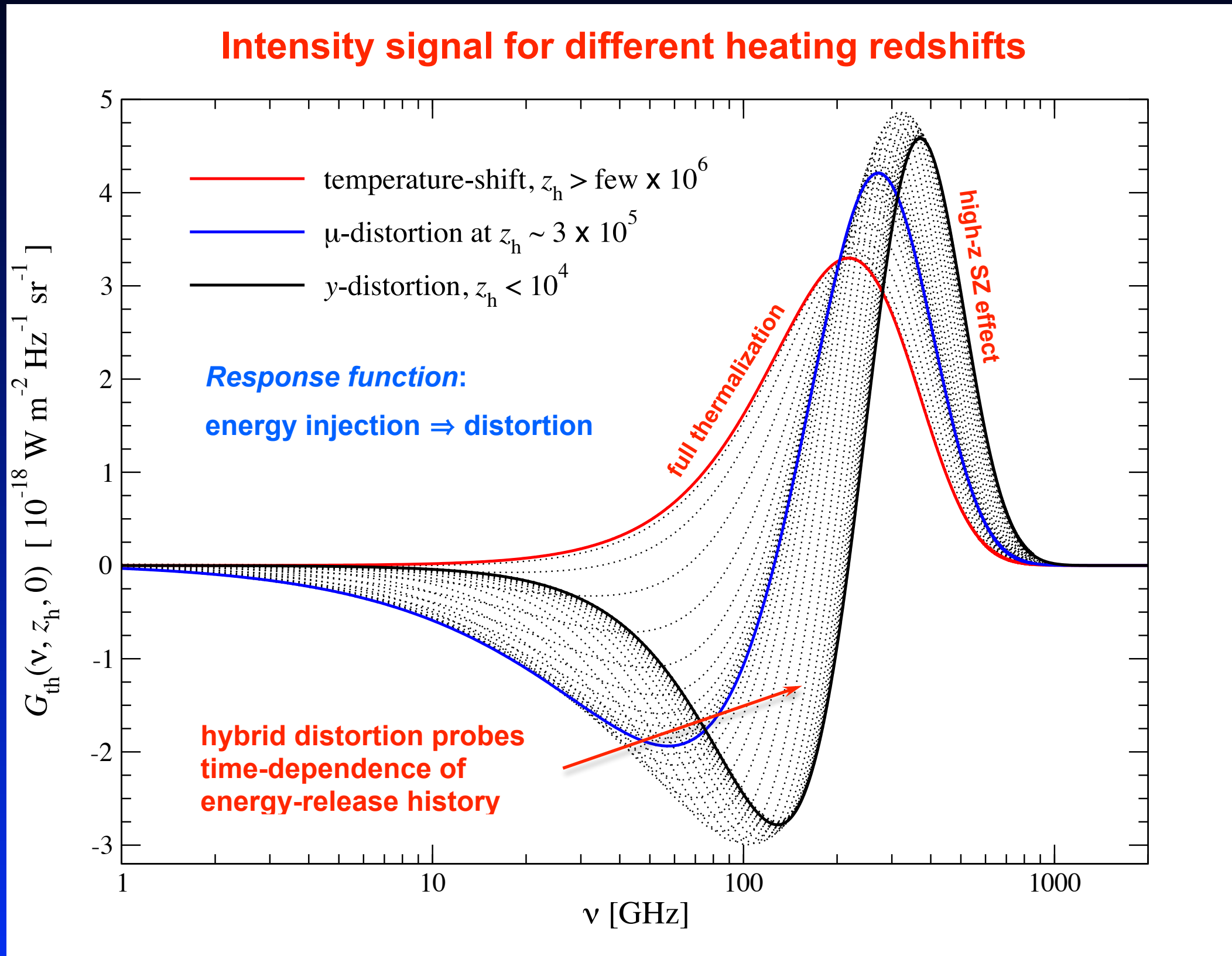
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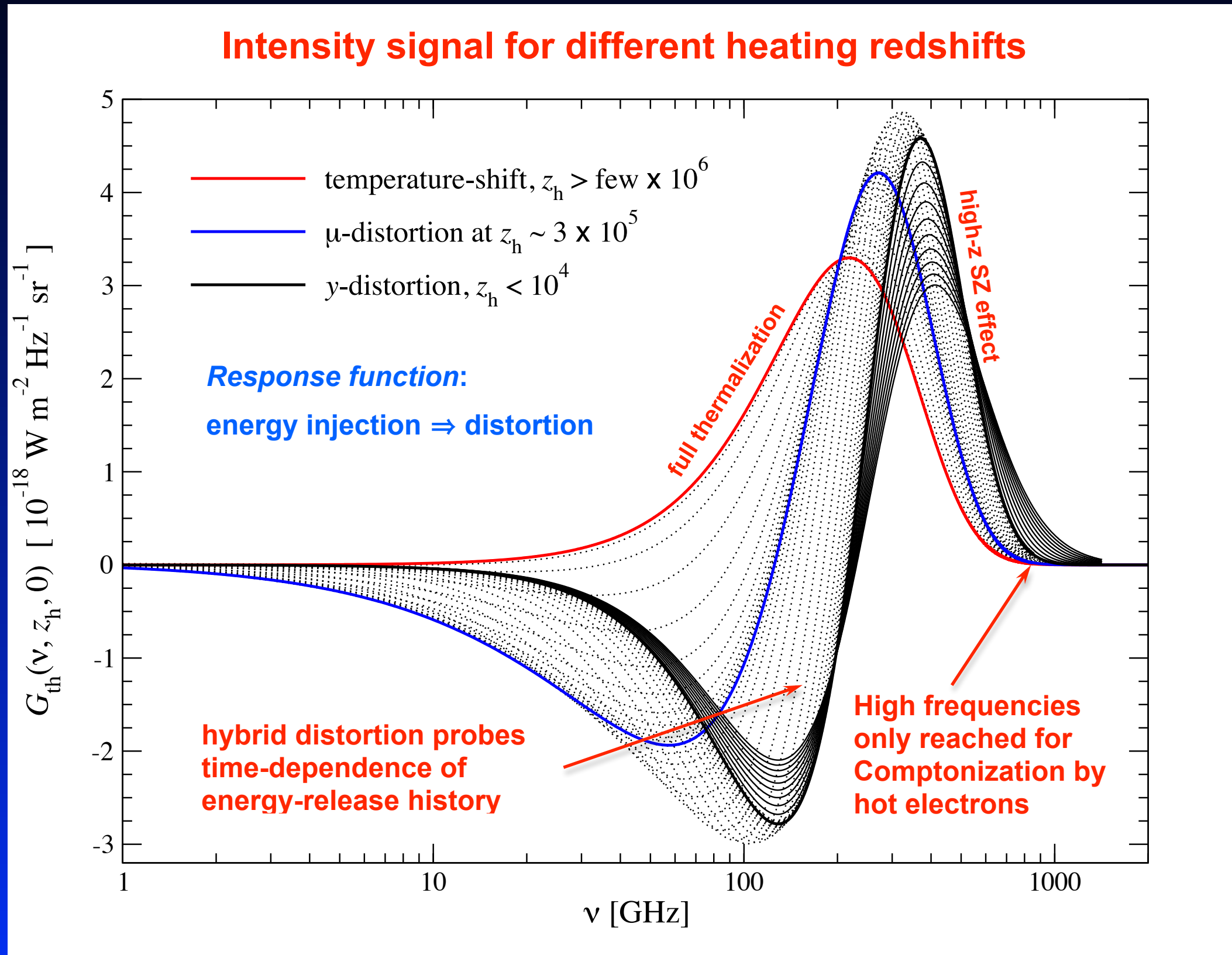
Average CMB spectral distortions



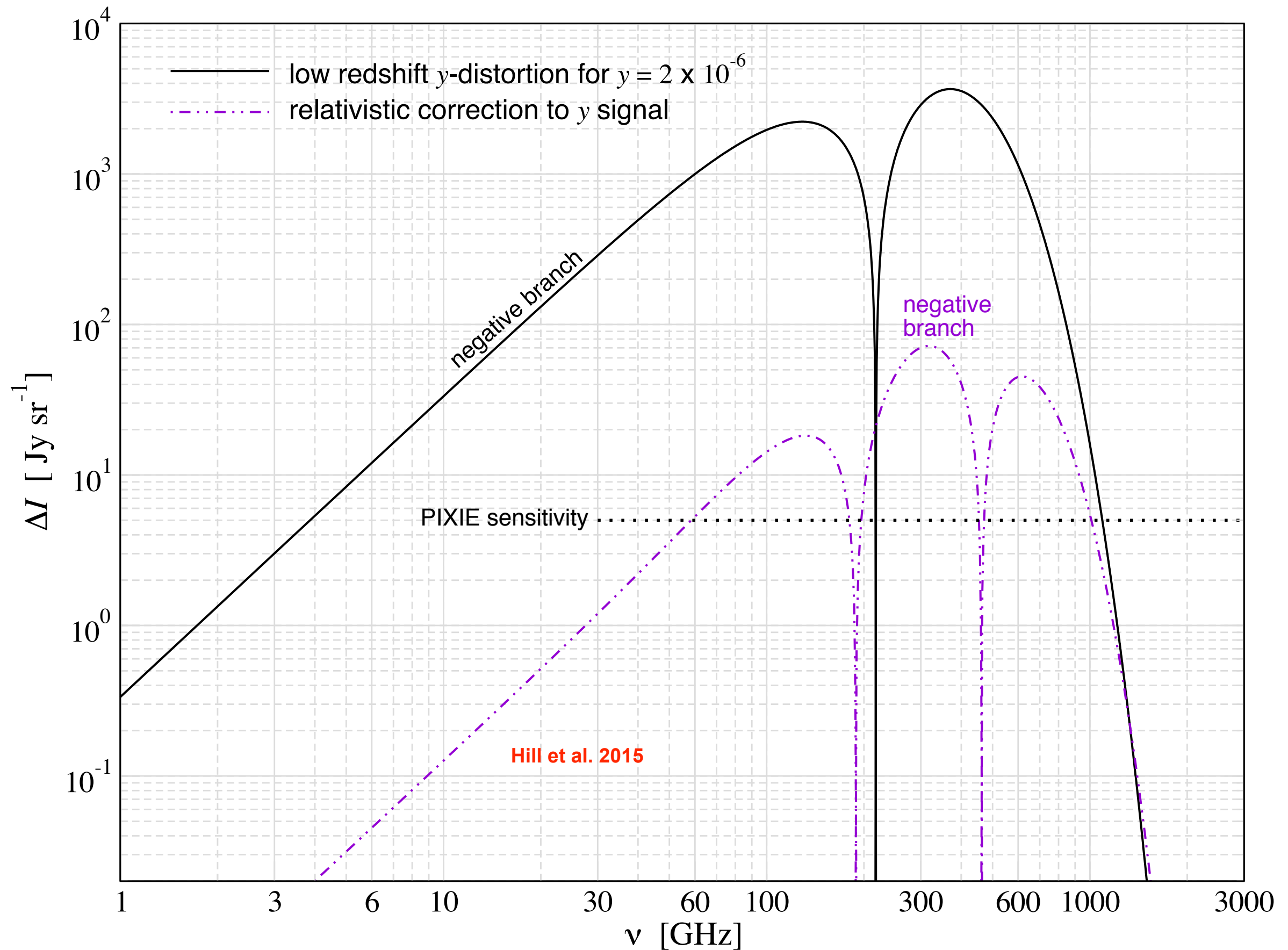
What does the spectrum look like after energy injection?



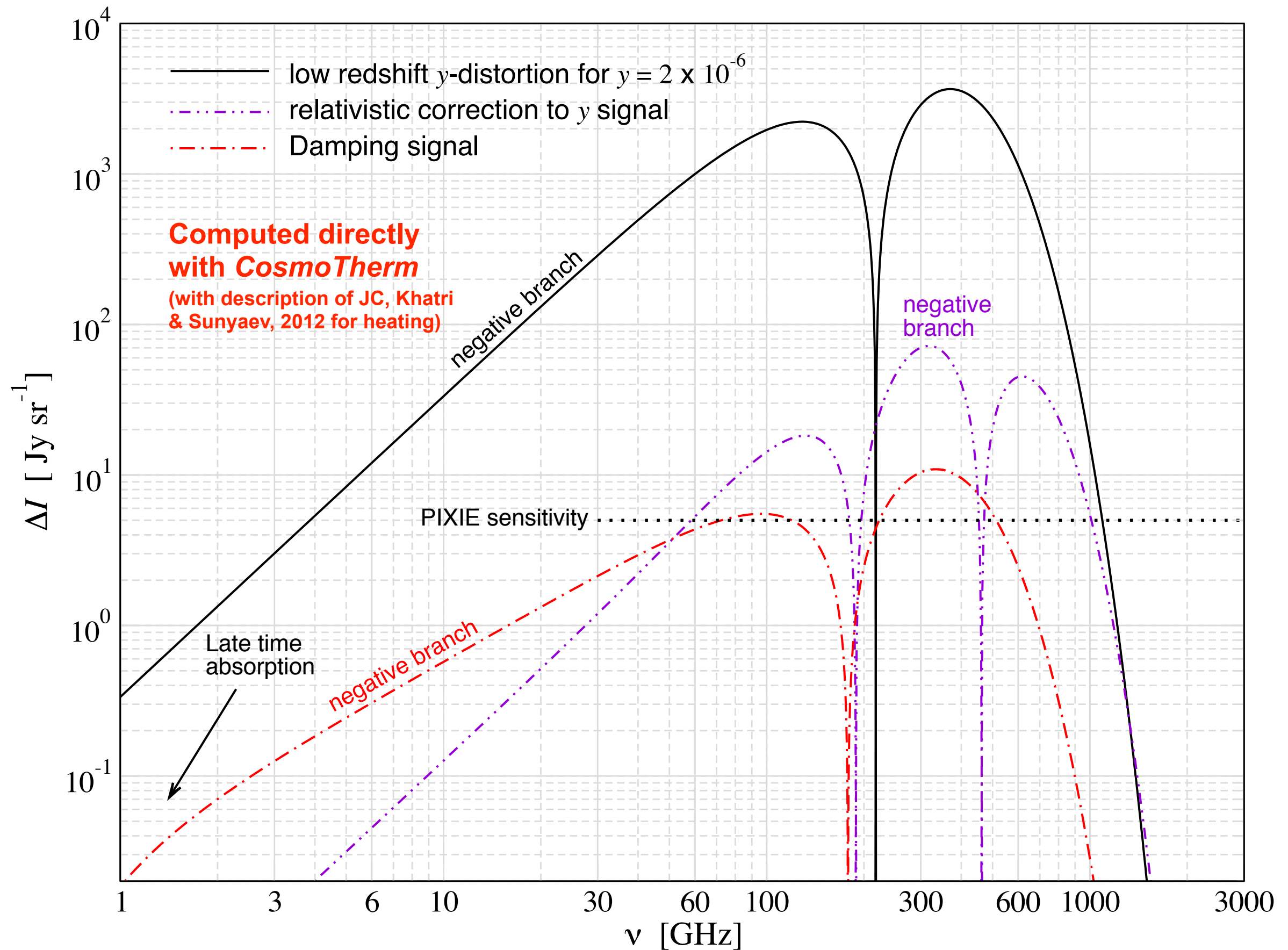
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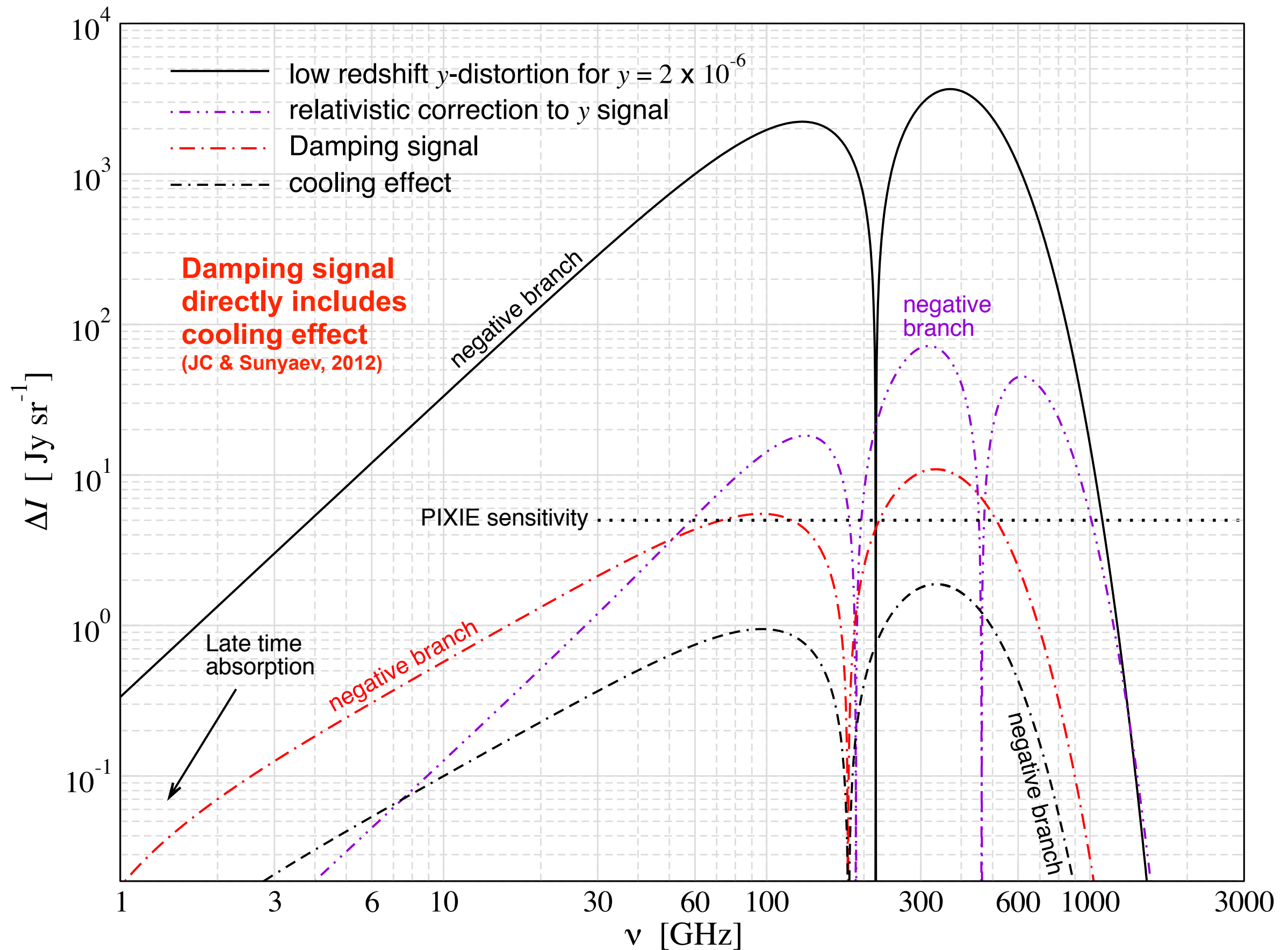
Average CMB spectral distortions



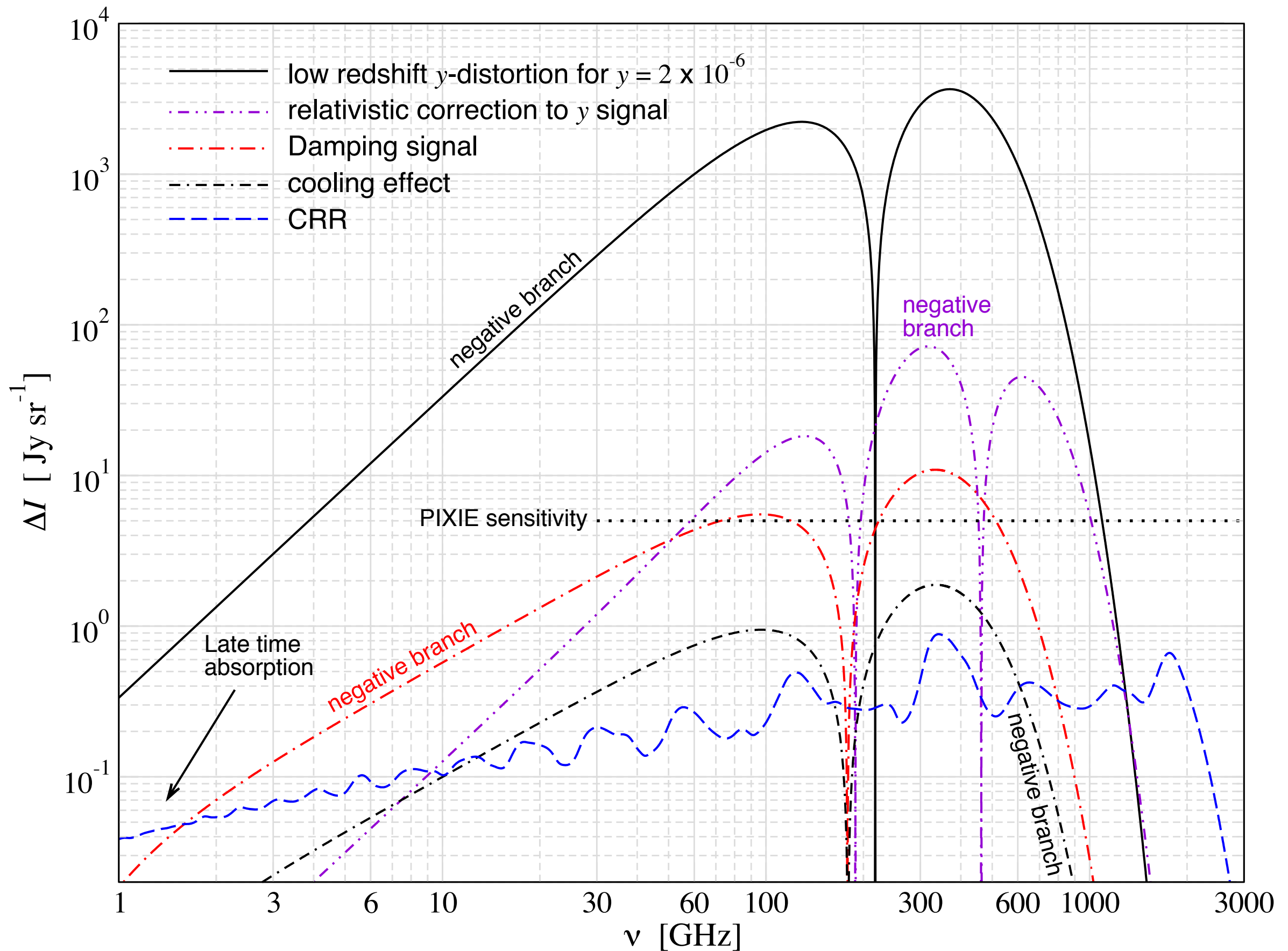
Average CMB spectral distortions



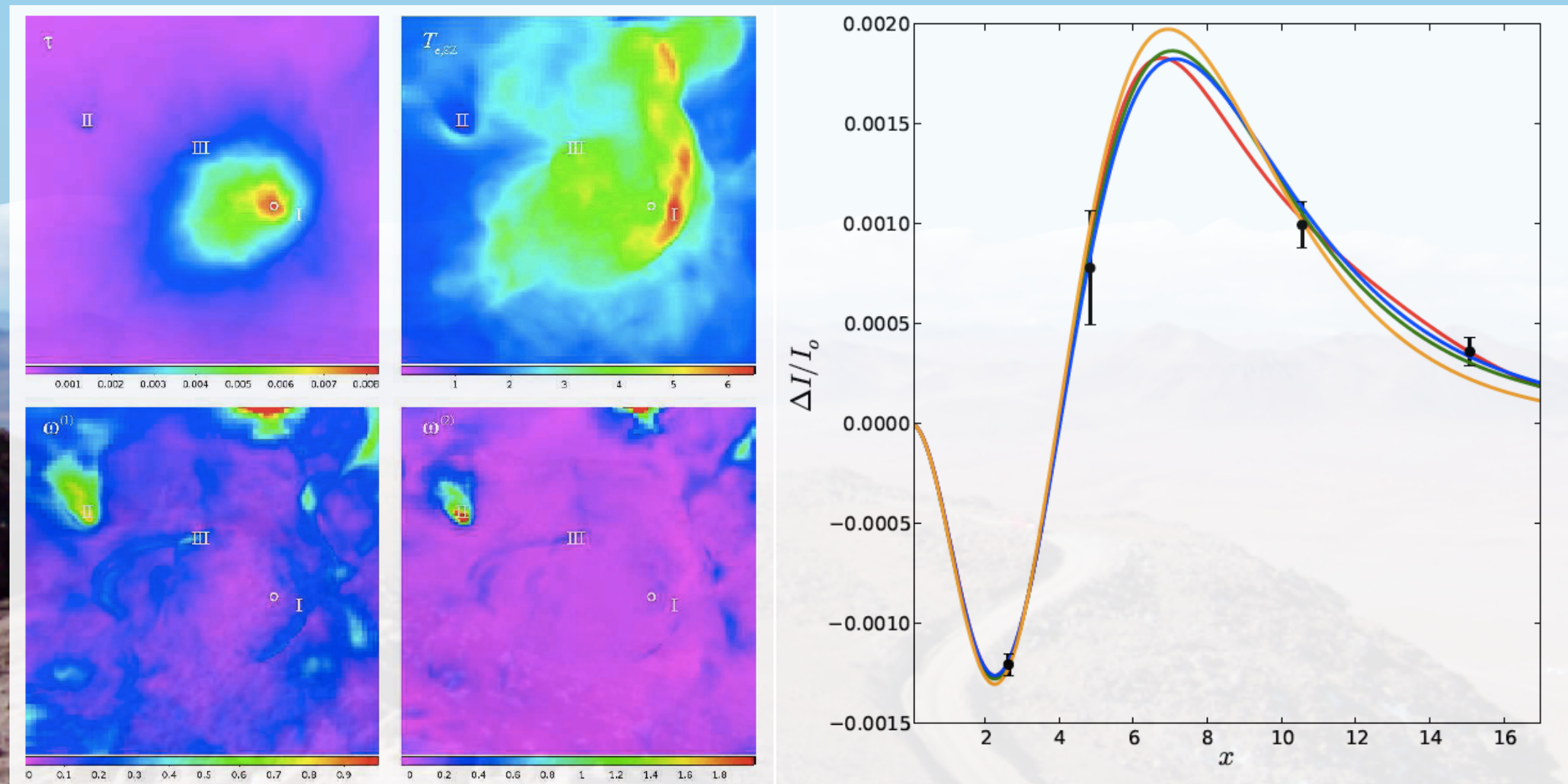
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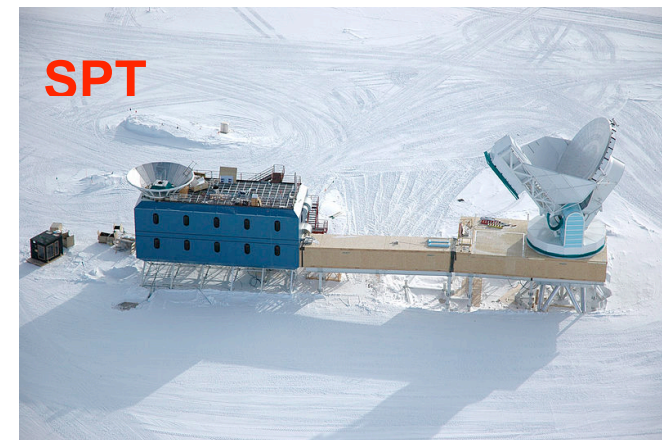
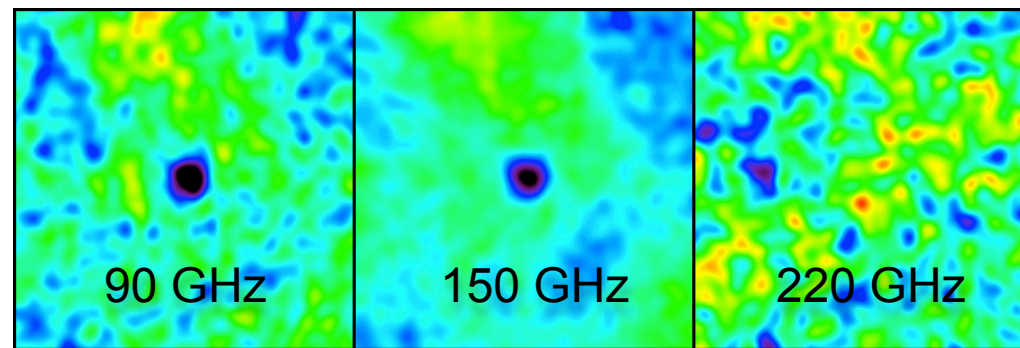
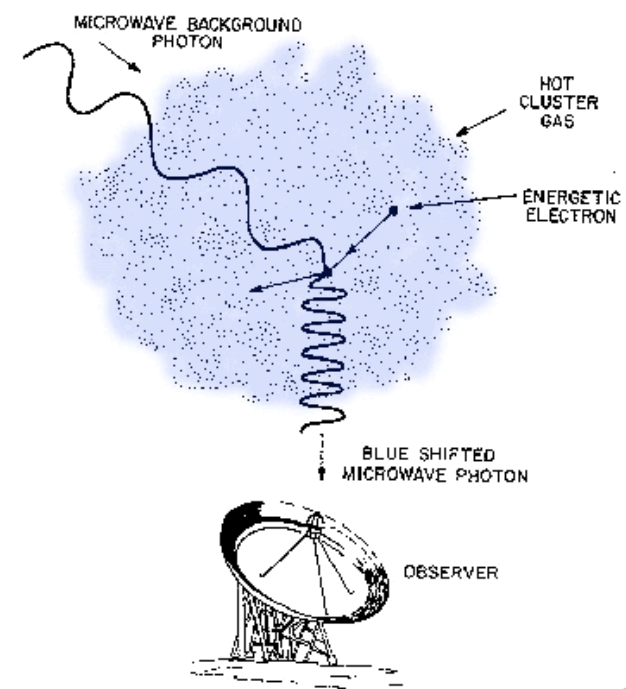
Average CMB spectral distortions in Λ CDM



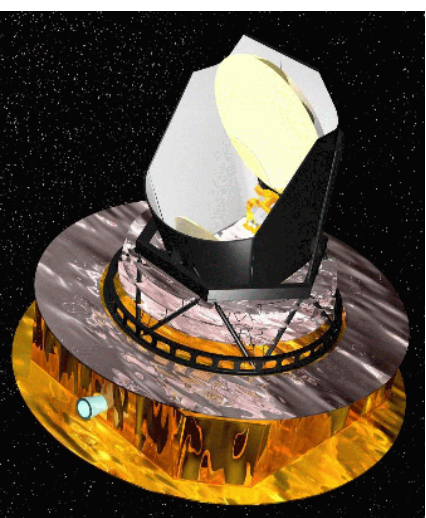
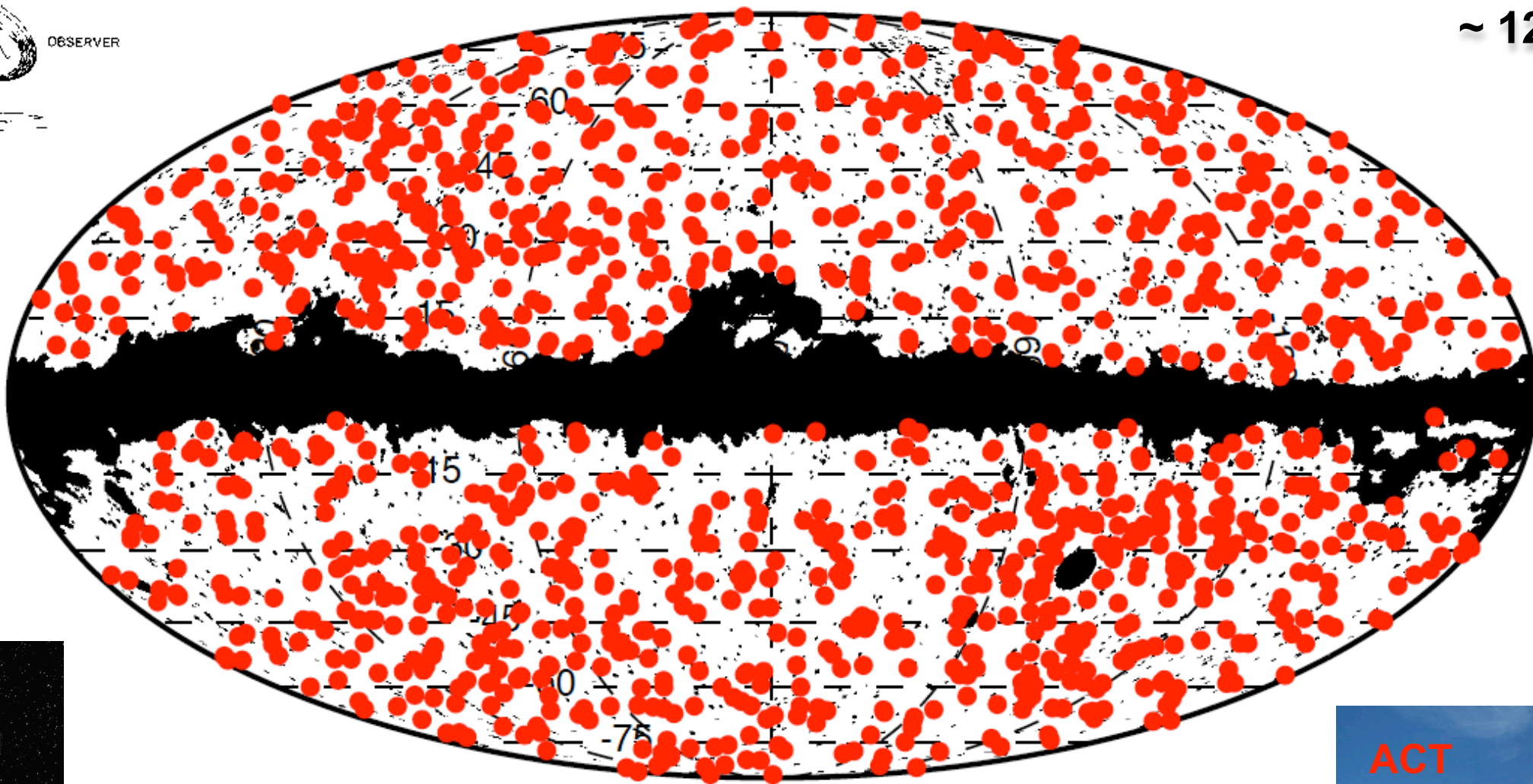
SZpack: fast computation of the SZ-effect using temperature and velocity moments



Thermal SZ effect is now routinely observed!



~ 1230 objects



Planck Collaboration, 2013, paper XXIV



What is the problem?

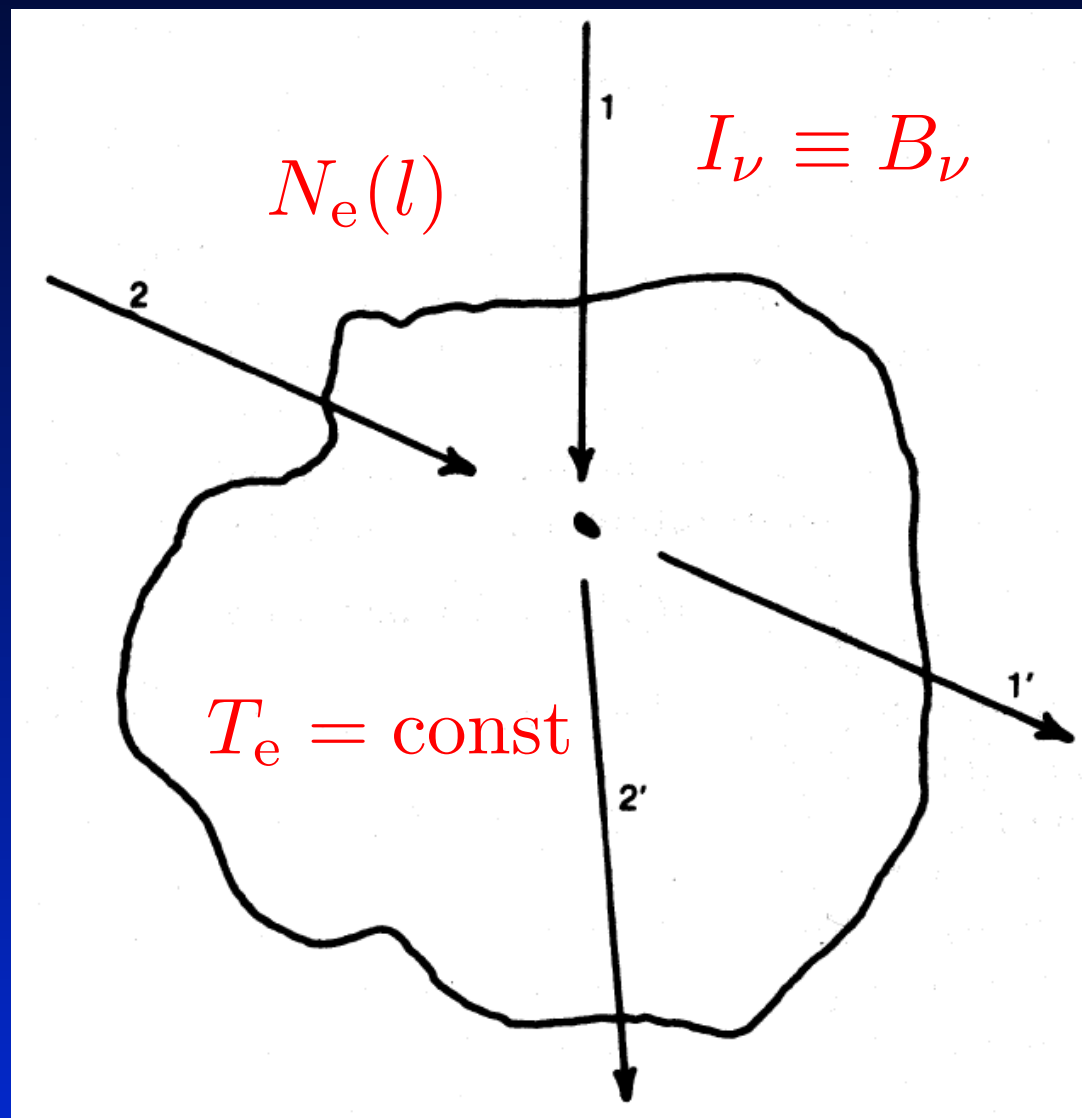
- Future high resolution & high sensitivity SZ observations
 - will allow us to address detailed questions about the state of the ICM
 - require accurate model for the SZ signal (*along different lines of sight...*)
 - which parameters actually determine it?

What is the problem?

- Future high resolution & high sensitivity SZ observations
 - will allow us to address detailed questions about the state of the ICM
 - require accurate model for the SZ signal (*along different lines of sight...*)
 - which parameters actually determine it?
- Computation of the SZ signal (*e.g., from a simulation or in analysis*)
 - depends on the electron number density, temperature and velocity structure
 - *brute force* calculation pretty expensive & link to parameters complicated
 - previous analytic approximations have *limited applicability*
 - *variations* of the temperature and velocity structure not accounted for
 - previous treatment of multiple scattering correction too simplistic...

SZpack overcomes all these problems!

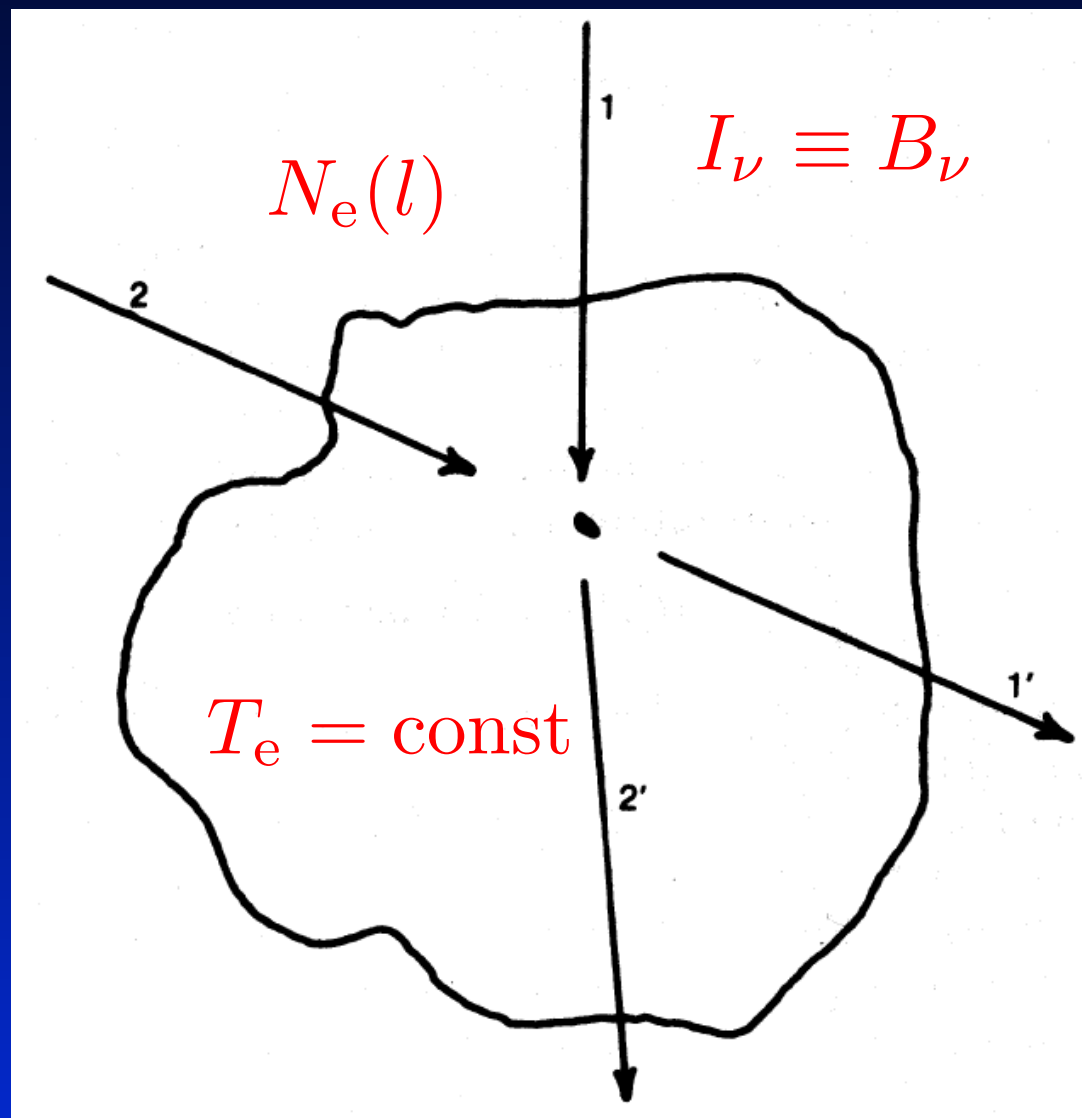
Thermal SZ effect for isothermal cluster



Scattering physics

- SZ signal depends on # of photons scattering *in* and *out* of the line-of-sight
- optically thin case $\Delta I_\nu \sim \tau S(\nu, T_e)$
- computation of $S(\nu, T_e)$ demanding

Thermal SZ effect for isothermal cluster

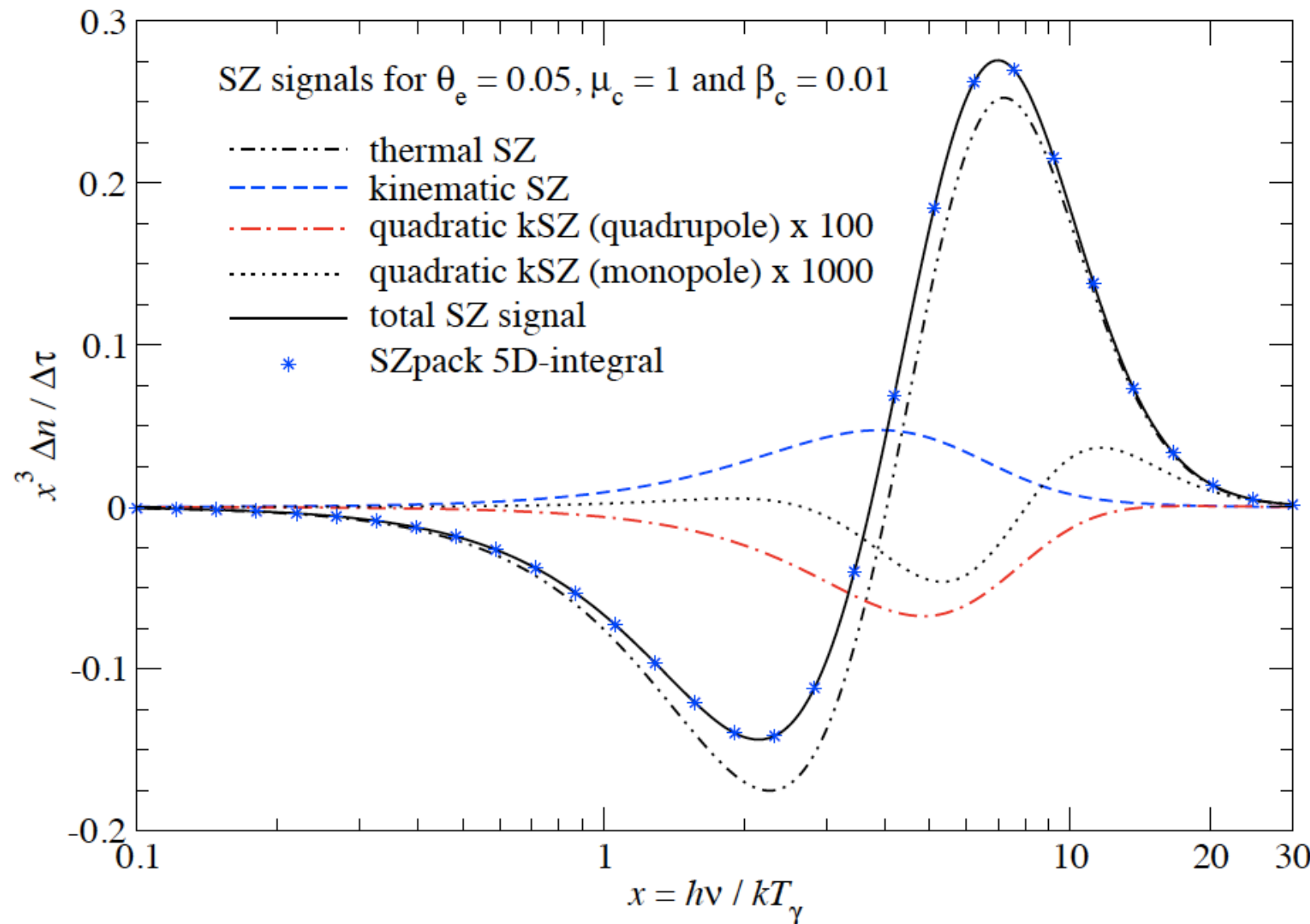


Scattering physics

- SZ signal depends on # of photons scattering *in* and *out* of the line-of-sight
- optically thin case $\Delta I_\nu \sim \tau S(\nu, T_e)$
- computation of $S(\nu, T_e)$ demanding asymptotic expansion (e.g., Itoh et al 1998)
- assumption $kT_e \ll mc^2$ and $\Delta\nu/\nu \ll 1$
- \Rightarrow convergence issues at high frequencies for $kT_e > 8$ keV

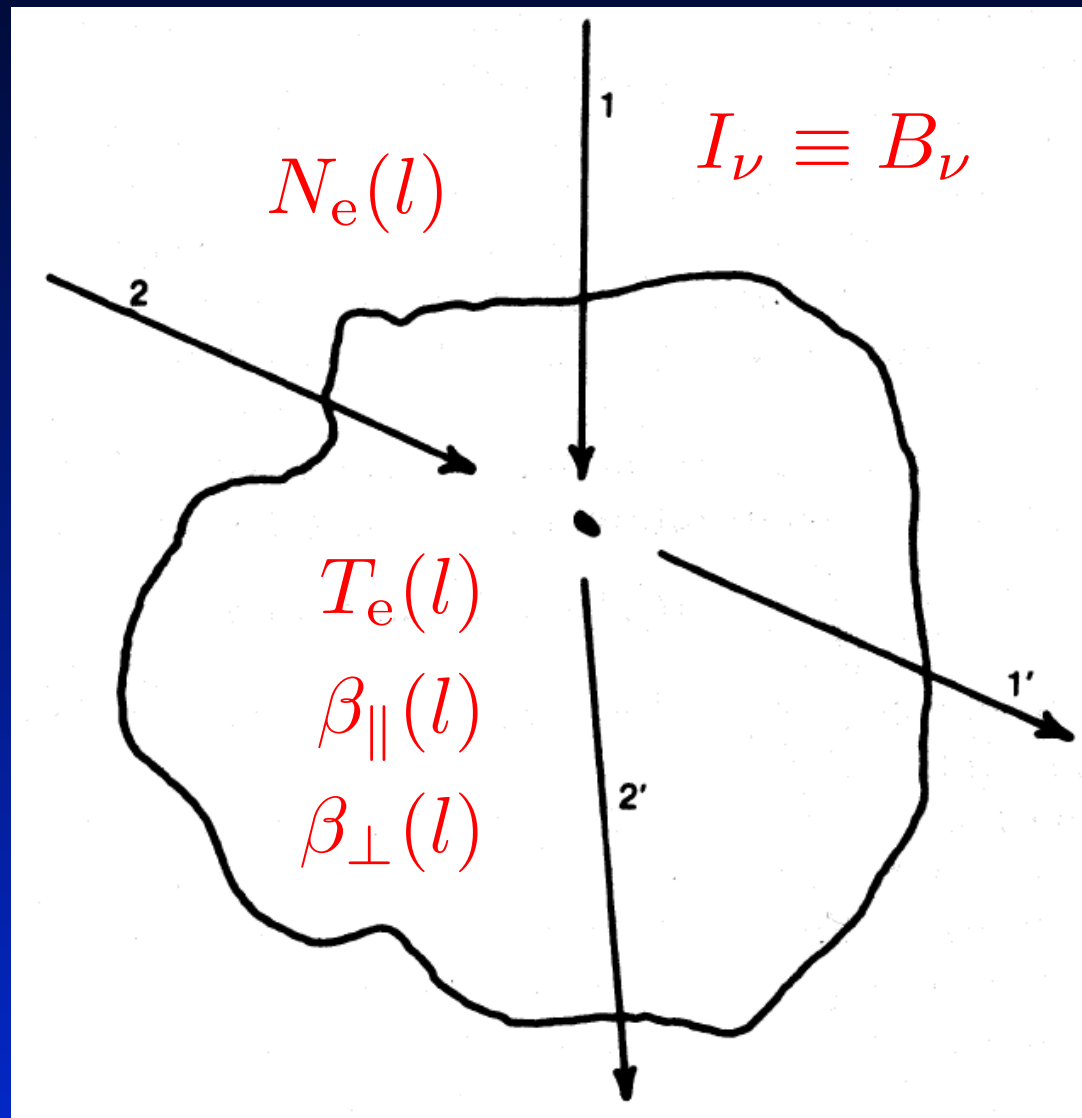
Thermal and kinematic SZ effect for isothermal cluster

SZpack approach



- T_e derivatives analytically
- collision integral numerically for given reference temperature
- set of smooth basis functions that is motivated by scattering physics
- excellent convergence properties
- precise representation of SZ signal for $kT_e < 75$ keV and $x < 30$

Non-isothermality and effect of internal motions



- SZ signal given by additional integral over line-of-sight
- problem becomes very demanding
- *Question*: what are the real parameters/observables?

Simple Solution:

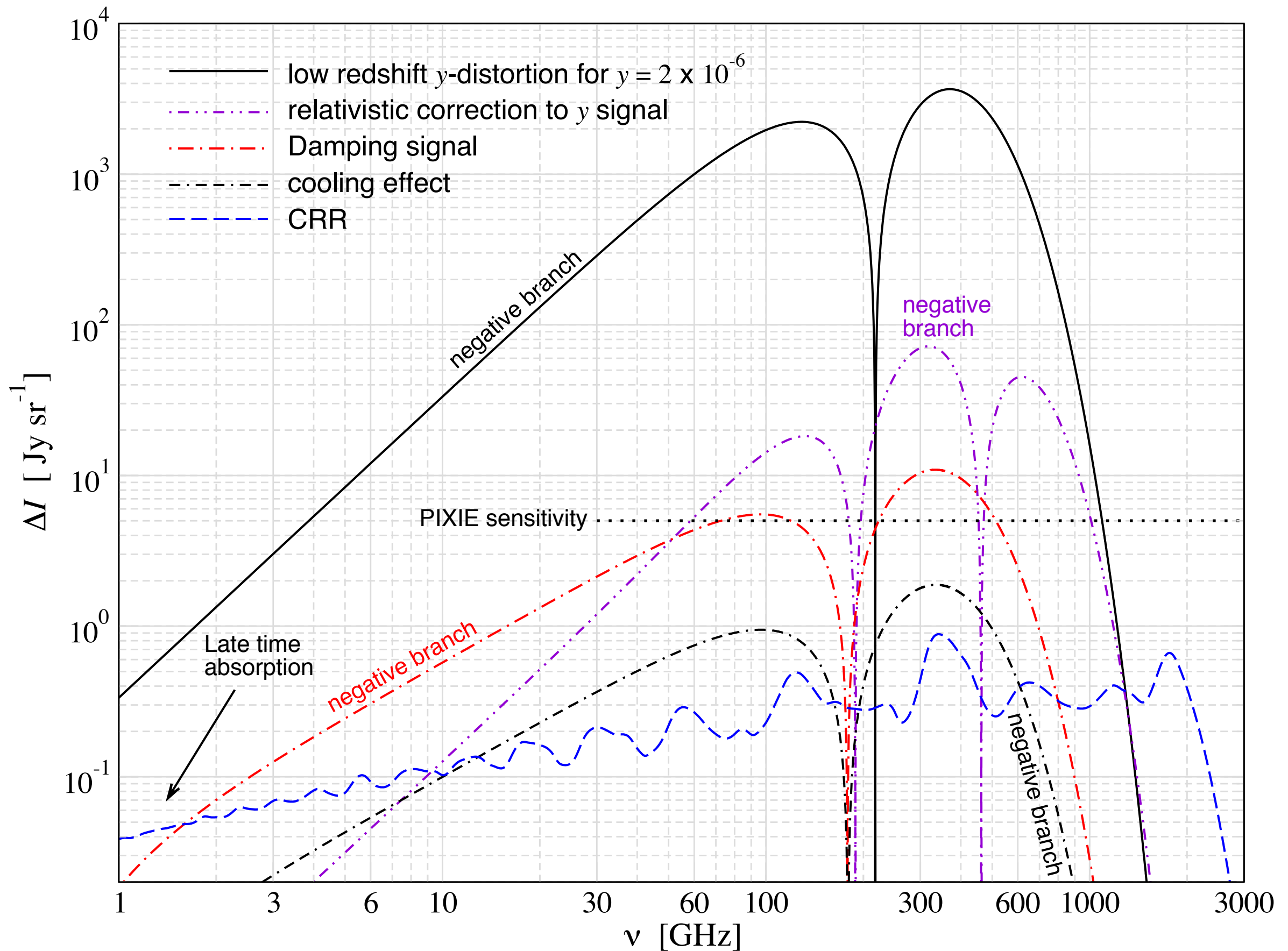
- perform expansion around mean values of main variables!
- *temperature-velocity moments* define new set of parameters:

$$p = \{\tau, T_e, \omega^{(k)}, \sigma^{(k)}, \kappa^{(k)}, \beta_{||}, \beta_{\perp}^2\}$$

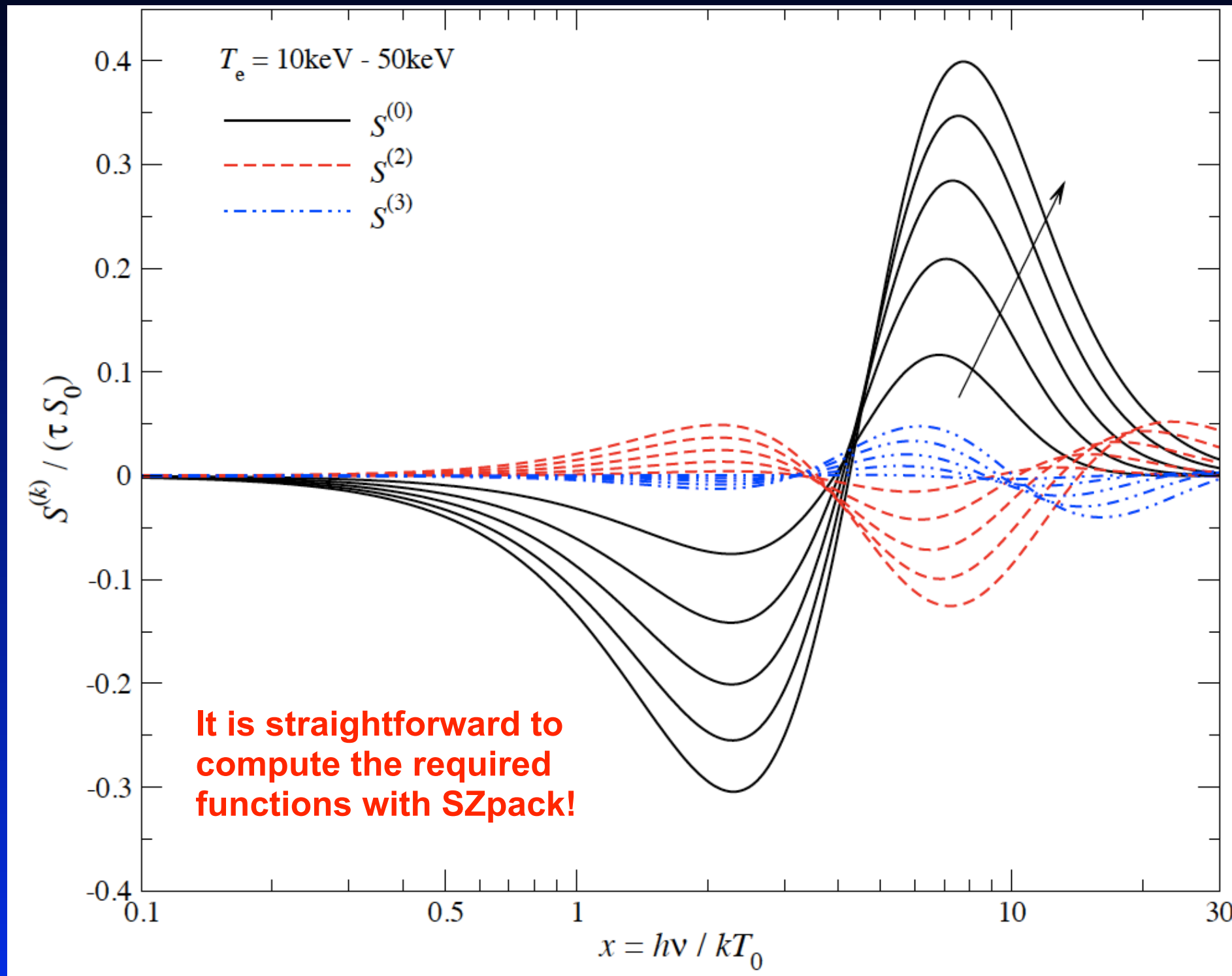
$$S \approx S_{\text{iso}}^{(0)} + S_{\text{iso}}^{(2)} \omega^{(1)} + C_{\text{iso}}^{(1)} \sigma^{(1)} + D_{\text{iso}}^{(2)} \kappa^{(1)} + E_{\text{iso}}^{(2)} \beta_{\text{c},\perp,\text{SZ}}^2 + \dots,$$

all functions of T_e , τ and $\beta_{||}$

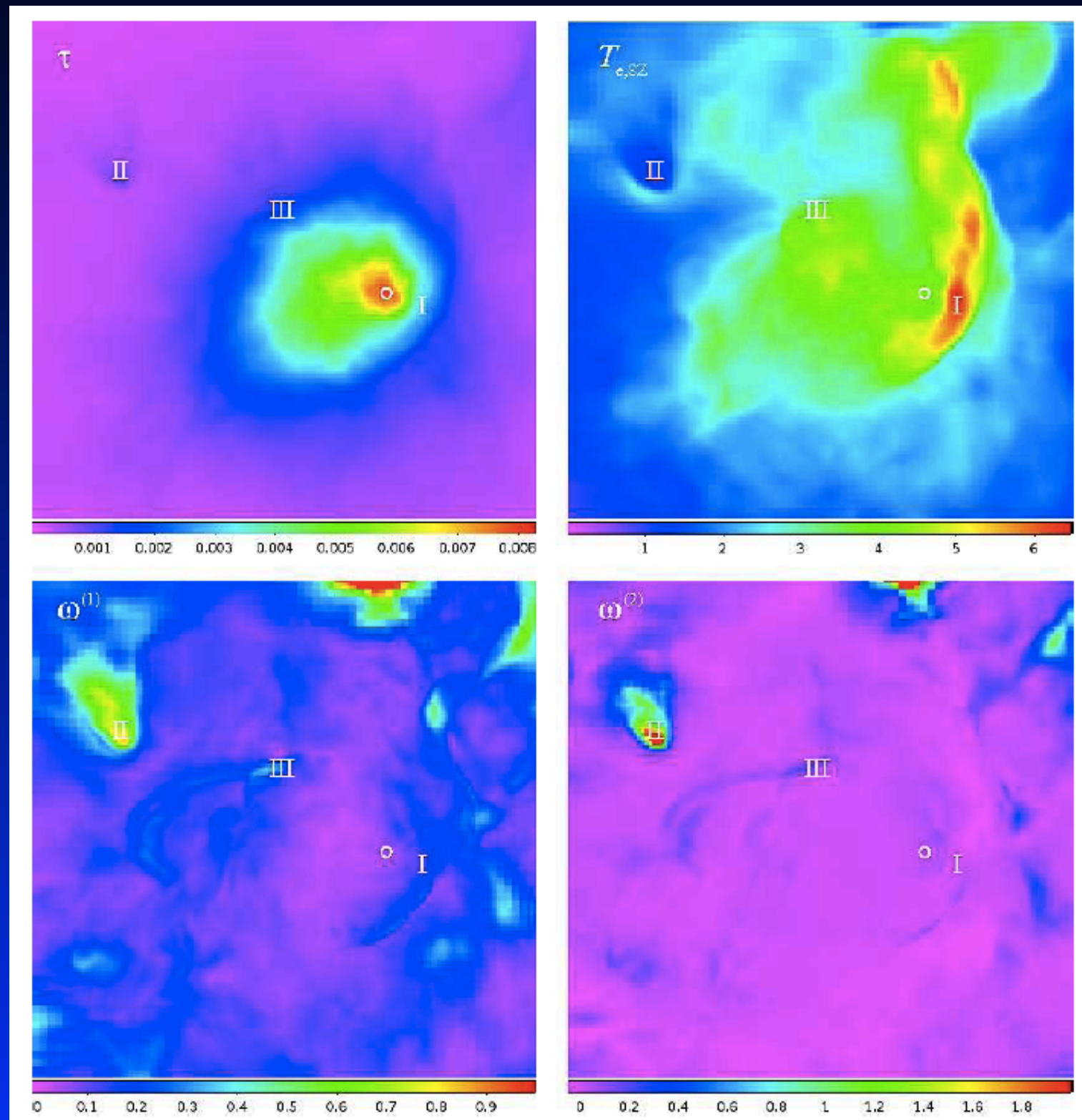
Average CMB spectral distortions in Λ CDM



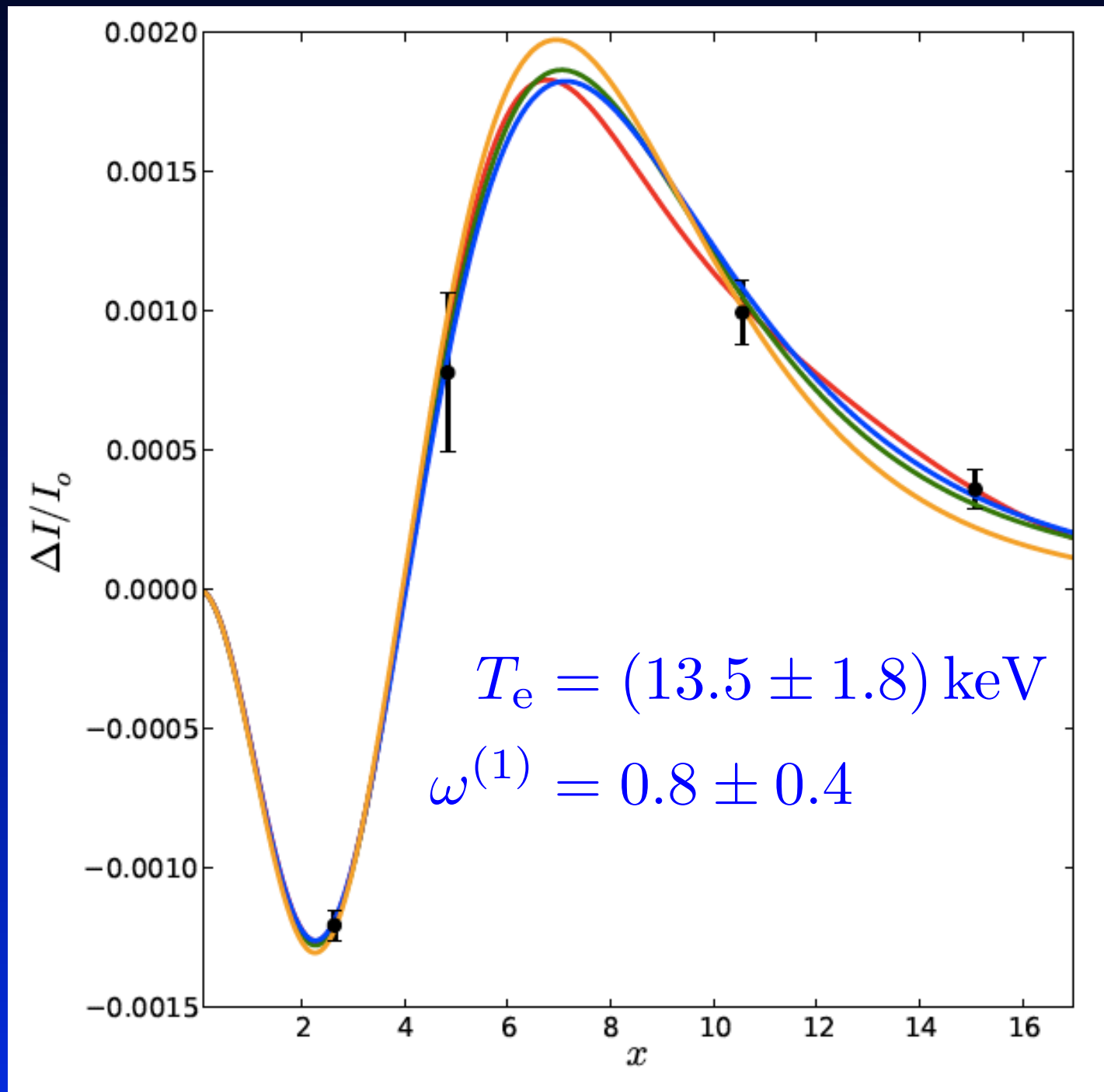
Basis functions to include non-isothermality



Can be directly used to compute signal morphologies



Analysis of Bullet cluster data (Prokhorov et al)



- MCMC analysis with extended set of parameters
- consistent analysis for mean and dispersion
- isothermal model in tension with data (**orange**)
- two-temperature (**green**) and simple dispersion (**blue**) models indistinguishable
- high frequency spectrum very important
- Itoh expansion (**red**) in this case not meaningful although at current level of precision consistent with data...

