

Flavour Physics

Antonio Pich
IFIC, Univ. Valencia - CSIC

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Flavour Structure of the Standard Model

$$\begin{pmatrix} u & \nu_e \\ d & e^- \end{pmatrix}, \begin{pmatrix} c & \nu_\mu \\ s & \mu^- \end{pmatrix}, \begin{pmatrix} t & \nu_\tau \\ b & \tau^- \end{pmatrix}$$



- Pattern of masses

- Flavour Mixing, ~~\mathcal{CP}~~



Related to **SSB**

Scalar Sector (Higgs)

$$\mathcal{L}_Y = - \sum_{jk} \left\{ (\bar{u}'_j, \bar{d}'_j)_L \left[c_{jk}^{(d)} \begin{pmatrix} \phi^{(+)} \\ \phi^{(0)} \end{pmatrix} d'_{kR} + c_{jk}^{(u)} \begin{pmatrix} \phi^{(0)\dagger} \\ -\phi^{(+)\dagger} \end{pmatrix} u'_{kR} \right] - (\bar{\nu}'_j, \bar{l}'_j)_L c_{jk}^{(l)} \begin{pmatrix} \phi^{(+)} \\ \phi^{(0)} \end{pmatrix} l'_{kR} \right\} + \text{h.c.}$$

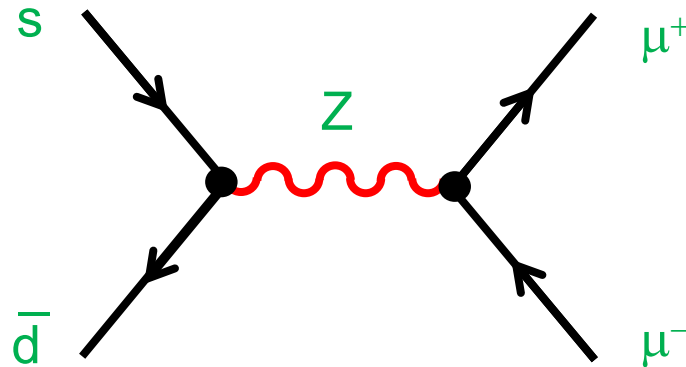


$$\mathcal{L}_Y = - \left(1 + \frac{H}{v} \right) \left\{ \bar{d}'_L \cdot \mathbf{M}'_d \cdot d'_R + \bar{u}'_L \cdot \mathbf{M}'_u \cdot u'_R + \bar{l}'_L \cdot \mathbf{M}'_l \cdot l'_R + \text{h.c.} \right\}$$

$$\left[\mathbf{M}'_d, \mathbf{M}'_u, \mathbf{M}'_l \right]_{jk} = \left[c_{jk}^{(d)}, c_{jk}^{(u)}, c_{jk}^{(l)} \right] \frac{v}{\sqrt{2}}$$

Flavour Conserving Neutral Currents (GIM)

$$\mathcal{L}_{\text{NC}}^Z = - \frac{e}{2 \sin \theta_W \cos \theta_W} Z_\mu \sum_f \bar{f} \gamma^\mu [v_f - a_f \gamma_5] f$$



NO

$$\text{Br}(K_L \rightarrow \mu^+ \mu^-) = (6.84 \pm 0.11) \times 10^{-9} \quad , \quad \text{Br}(K_S \rightarrow \mu^+ \mu^-) < 1.0 \times 10^{-9} \quad (95\% \text{ CL})$$

LHCb, 1706.00758

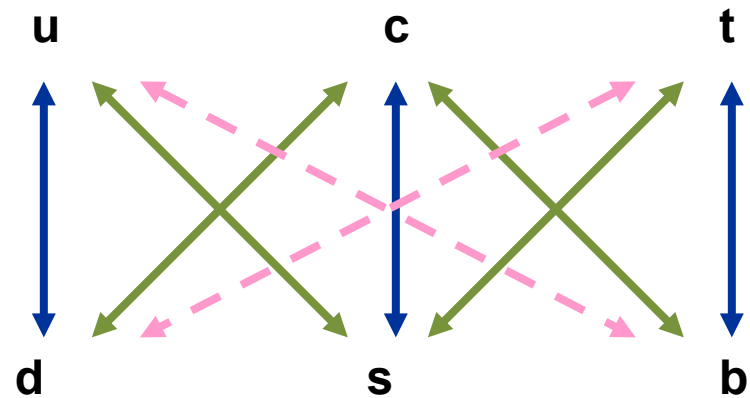
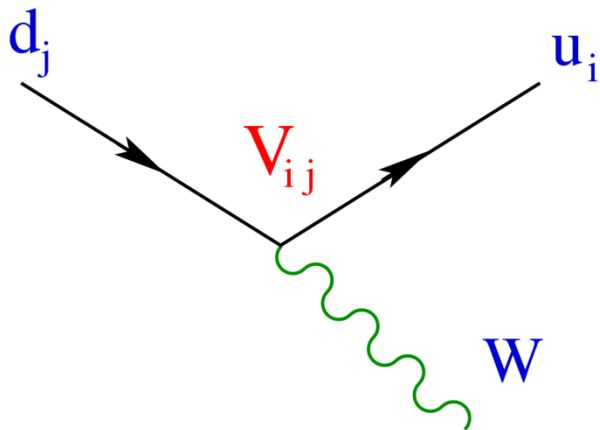
$$K_L \rightarrow \pi^{0*} \rightarrow (\gamma\gamma)^* \rightarrow \mu^+ \mu^-$$

$$K_S \rightarrow (\pi^+ \pi^-)^* \rightarrow (\gamma\gamma)^* \rightarrow \mu^+ \mu^-$$

Flavour Changing Charged Currents

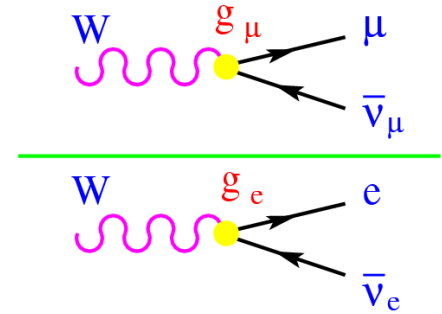
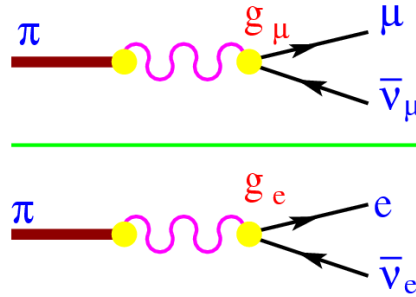
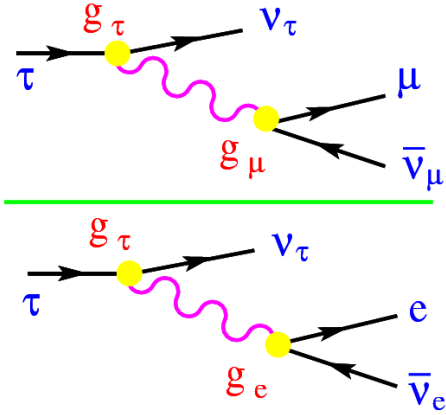
$$\mathcal{L}_{\text{CC}} = -\frac{g}{2\sqrt{2}} W_{\mu}^{\dagger} \left[\sum_{ij} \bar{u}_i \gamma^{\mu} (1-\gamma_5) \mathbf{V}_{ij} d_j + \sum_l \bar{\nu}_l \gamma^{\mu} (1-\gamma_5) l \right] + \text{h.c.}$$

$$(\bar{\nu}_{l_j} \equiv \bar{\nu}_i \mathbf{V}_{ij}^{(l)})$$

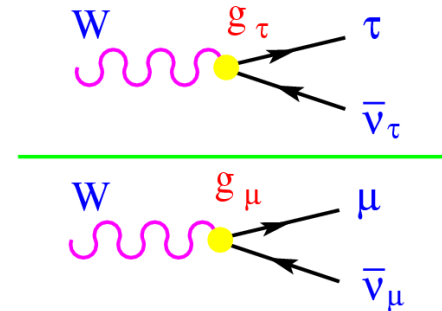
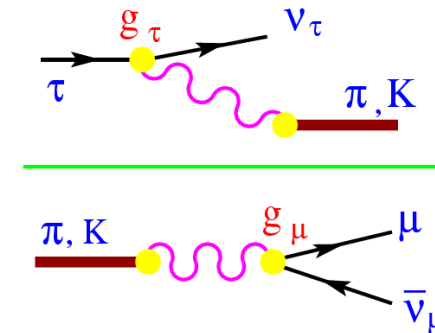
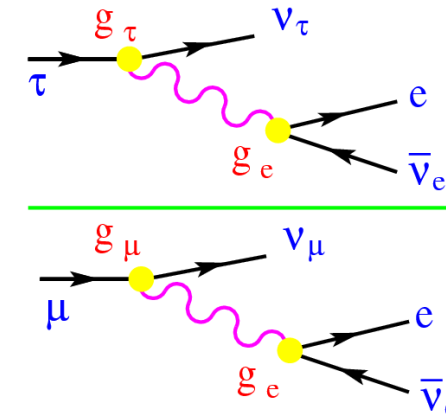


LEPTON UNIVERSALITY

$\frac{\sigma_\mu}{\sigma_e}$



$\frac{\sigma_\tau}{\sigma_\mu}$



CHARGED CURRENT UNIVERSALITY

$$|g_\mu / g_e|$$

$B_{\tau \rightarrow \mu} / B_{\tau \rightarrow e}$	1.0018 ± 0.0014
$B_{\pi \rightarrow \mu} / B_{\pi \rightarrow e}$	1.0021 ± 0.0016
$B_{K \rightarrow \mu} / B_{K \rightarrow e}$	0.9978 ± 0.0020
$B_{K \rightarrow \pi\mu} / B_{K \rightarrow \pi e}$	1.0010 ± 0.0025
$B_{W \rightarrow \mu} / B_{W \rightarrow e}$	0.996 ± 0.010

$$|g_\tau / g_\mu|$$

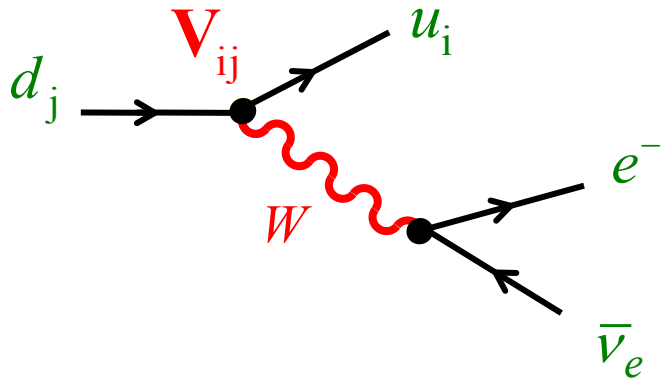
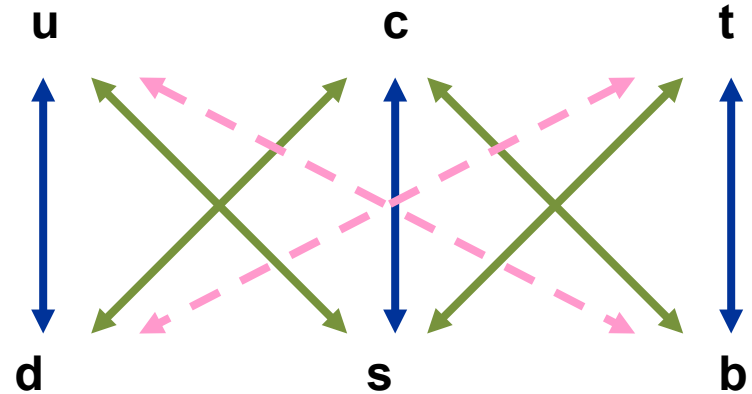
$B_{\tau \rightarrow e} \tau_\mu / \tau_\tau$	1.0011 ± 0.0015
$\Gamma_{\tau \rightarrow \pi} / \Gamma_{\pi \rightarrow \mu}$	0.9962 ± 0.0027
$\Gamma_{\tau \rightarrow K} / \Gamma_{K \rightarrow \mu}$	0.9858 ± 0.0070
$B_{W \rightarrow \tau} / B_{W \rightarrow \mu}$	1.034 ± 0.013

$$|g_\tau / g_e|$$

$B_{\tau \rightarrow \mu} \tau_\mu / \tau_\tau$	1.0030 ± 0.0015
$B_{W \rightarrow \tau} / B_{W \rightarrow e}$	1.031 ± 0.013

A. Pich, arXiv:1310.7922

Flavour Changing Charged Currents



$$\Gamma(d_j \rightarrow u_i e^- \bar{\nu}_e) \propto |V_{ij}|^2$$

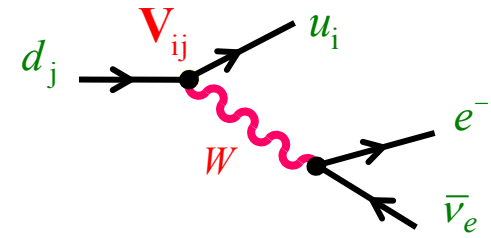
We measure decays of hadrons (no free quarks)

Important QCD Uncertainties

V_{ij} Determination

$(0^- \rightarrow 0^-)$

$K \rightarrow \pi \ell \nu, D \rightarrow K \ell \nu \dots$



$$\langle P'(k') | \bar{u}_i \gamma^\mu d_j | P(k) \rangle = C_{PP'} \{ (k+k')^\mu f_+(q^2) + (k-k')^\mu f_-(q^2) \}$$

$$\Gamma(P \rightarrow P' l \nu) = \frac{G_F^2 M_P^5}{192 \pi^3} |V_{ij}|^2 C_{PP'}^2 |f_+(0)|^2 \mathbf{I} (1 + \delta_{RC})$$

$$\mathbf{I} \approx \int_0^{(M_P - M_{P'})^2} \frac{dq^2}{M_P^8} \lambda^{3/2}(q^2, M_P^2, M_{P'}^2) \left| \frac{f_+(q^2)}{f_+(0)} \right|^2$$

$f_-(q^2)$ suppressed

$(k-k')^\mu \bar{l} \gamma_\mu (1-\gamma_5) \nu_l \sim m_l$

- Measure the q^2 distribution $\longrightarrow \mathbf{I}$
- Measure Γ $\longrightarrow f_+(0) |V_{ij}|$
- Get a theoretical prediction for $f_+(0)$ $\longrightarrow |V_{ij}|$

Theory is always needed: Symmetries

$|V_{ud}|$

$$f_+(0) = 1 + O[(m_u - m_d)^2]$$

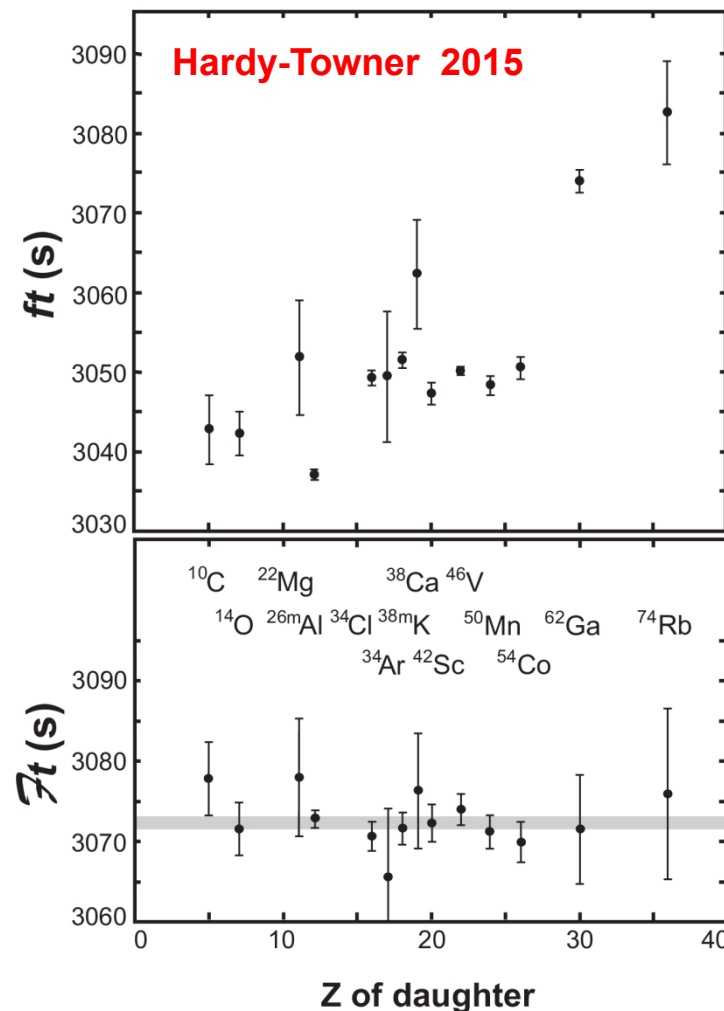
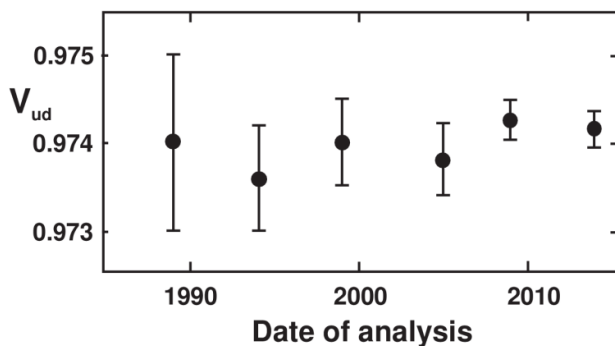
Superallowed Nuclear β Transitions ($0^+ \rightarrow 0^+$)

$$|V_{ud}|^2 = \frac{\pi^3 \ln 2}{ft G_F^2 m_e^5 (1 + \delta_{RC})} = \frac{(2984.48 \pm 0.05) \text{ s}}{ft (1 + \delta_{RC})}$$

(Marciano – Sirlin)



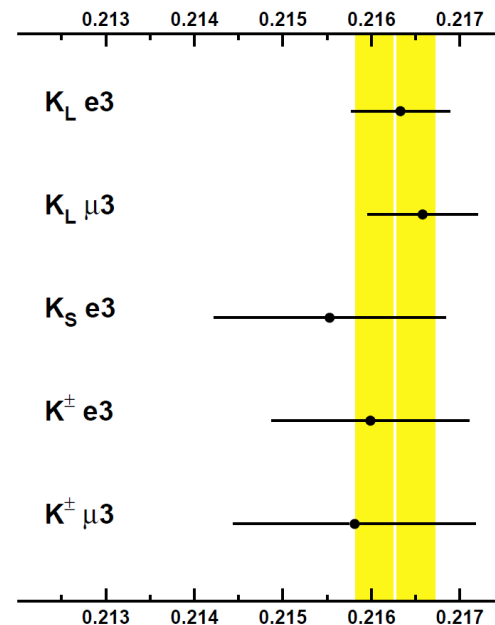
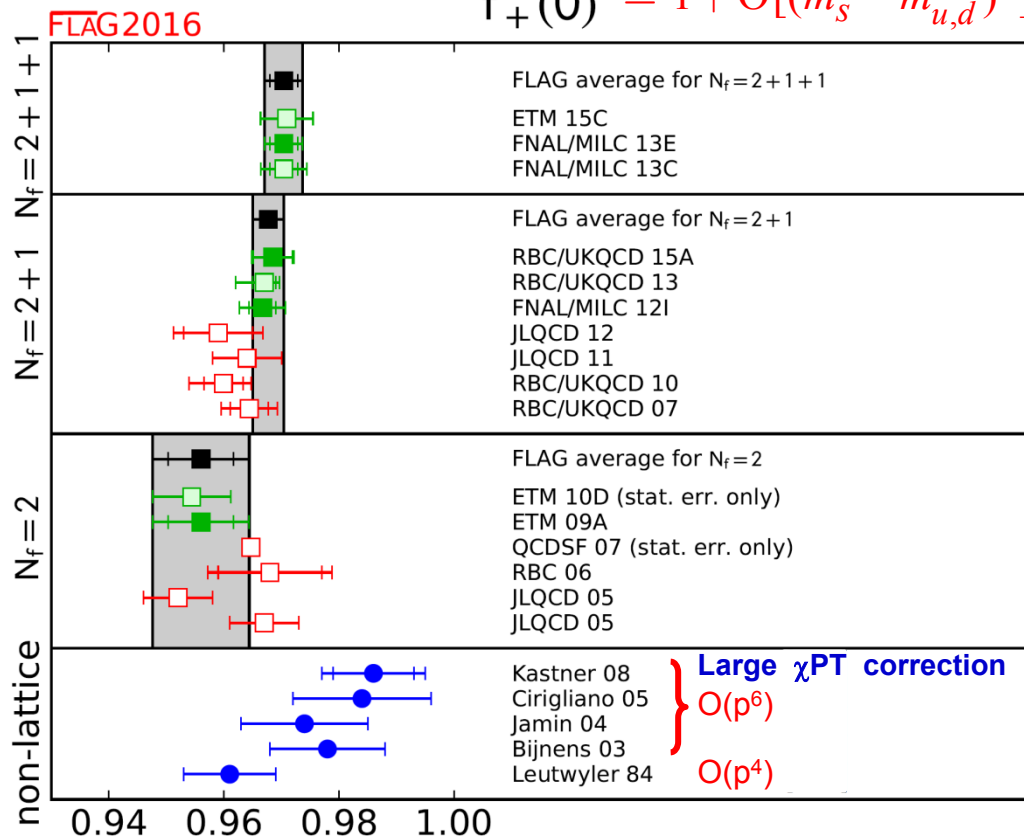
$$|V_{ud}| = 0.97417 \pm 0.00021$$



K \rightarrow $\pi \ell \nu$ Decays

Flavianet, arXiv:1005.2323 [hep-ph]
Moulson, arXiv:1411.5252 [hep-ph]

$$f_+(0) = 1 + O[(m_s - m_{u,d})^2]$$



$$|f_+(0) V_{us}| = 0.2165 \pm 0.0004$$

2012: $f_+(0) = 0.959 \pm 0.005$



$$|V_{us}| = 0.2255 \pm 0.0014$$

2016: $f_+(0) = 0.970 \pm 0.003$

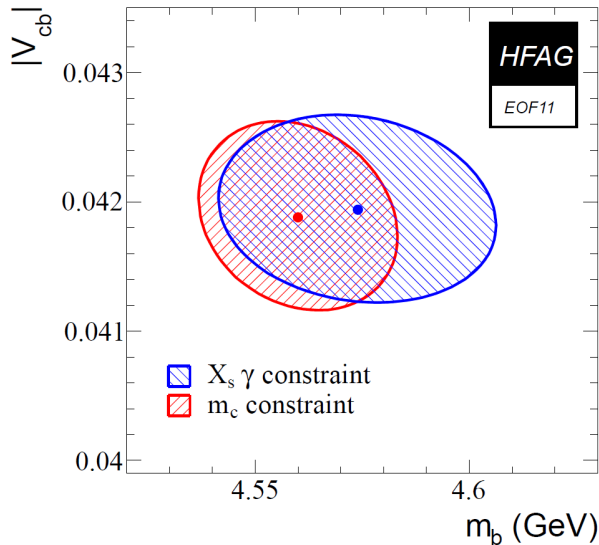


$$|V_{us}| = 0.2232 \pm 0.0008$$

Inclusive B Decays

(OPE, HQET)

$$\Gamma(\bar{B} \rightarrow X_c \ell \bar{\nu}) = \frac{G_F^2 |V_{cb}|^2 m_b^5}{192\pi^3} \left\{ f(\rho) + k(\rho) \frac{\mu_\pi^2}{2m_b^2} + g(\rho) \frac{\mu_G^2}{2m_b^2} \right\} \quad \rho = m_c/m_b$$



Fits to lepton energy, hadronic invariant mass and photon energy moments

HFAG 2016: $|V_{cb}|_{\text{incl}} = \begin{cases} (42.19 \pm 0.78) \cdot 10^{-3} & \text{Kinetic mass} \\ (41.98 \pm 0.45) \cdot 10^{-3} & \text{1S mass} \end{cases}$

PDG 2016: $|V_{cb}|_{\text{incl}} = (42.2 \pm 0.8) \cdot 10^{-3}$

Gambino- Healey-Turczyk, 1606.06174

Higher Power Corrections

$$|V_{cb}| = (42.00 \pm 0.63) \times 10^{-3}$$

B → D ℓ ν

B → D* ℓ ν

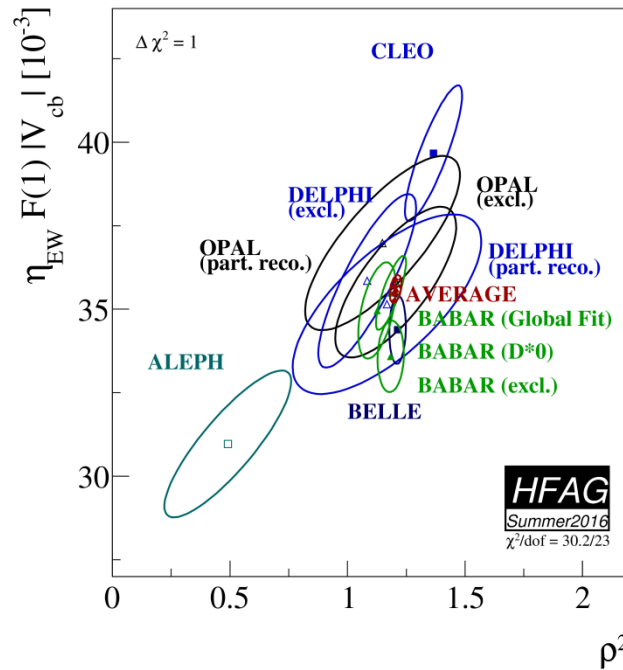
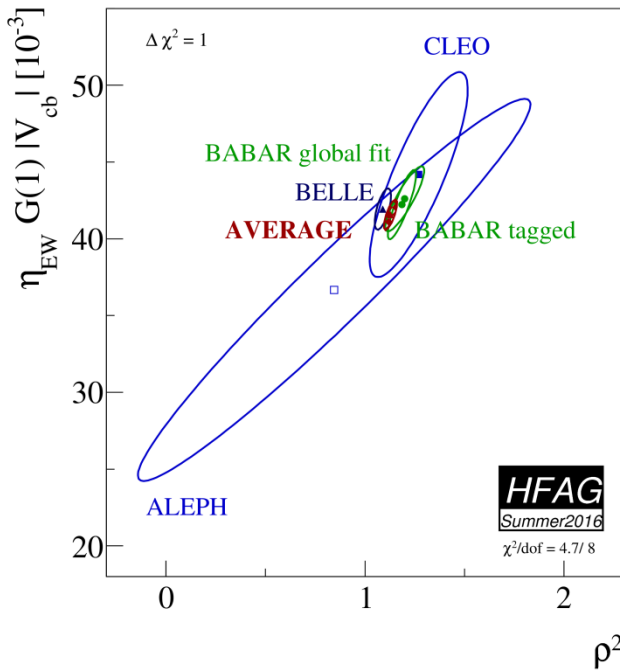
QCD Symmetries at 1/M_Q → 0

HQET

Caprini-Lellouch-Neubert parametrization

$$\eta_{EW} G(1) |V_{cb}| = (41.57 \pm 1.00) \cdot 10^{-3}$$

$$\eta_{EW} F(1) |V_{cb}| = (35.61 \pm 0.43) \cdot 10^{-3}$$



FNAL / MILC :

$$\eta_{EW} G(1) = 1.061 \pm 0.010 \quad \Rightarrow \quad |V_{cb}| = (39.18 \pm 0.94_{\text{exp}} \pm 0.36_{\text{th}}) \cdot 10^{-3}$$

$$\eta_{EW} F(1) = 0.912 \pm 0.014 \quad \Rightarrow \quad |V_{cb}| = (39.05 \pm 0.47_{\text{exp}} \pm 0.58_{\text{th}}) \cdot 10^{-3}$$

$$\Rightarrow \quad |V_{cb}|_{\text{excl}} = (39.10 \pm 0.60) \cdot 10^{-3}$$

3.3 σ discrepancy with inclusive measurement

Parametrization Dependence

Analyticity, Unitarity
Crossing Symmetry

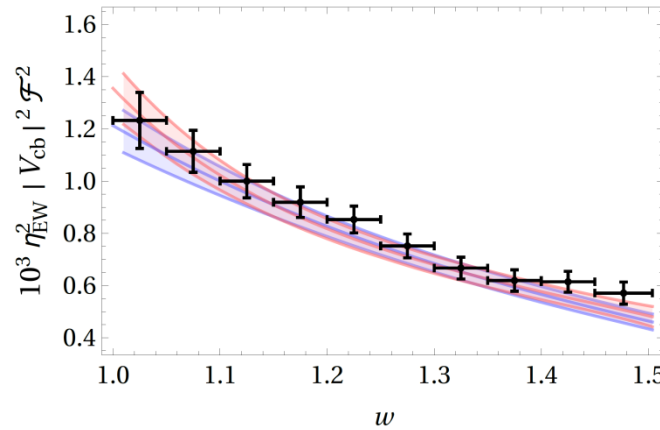
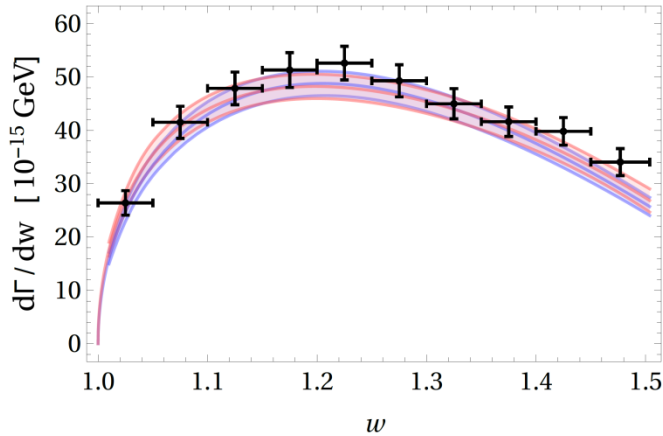


- Boyd-Grinstein-Lebed (BGL)
- Caprini-Lellouch-Neubert (CLN) (HQET relations valid within 2%)

● $B \rightarrow D^* \ell \nu$

Belle data (1702.01521) + Lattice + LCSRs

Bigi-Gambino-Schacht, 1703.06124, 1707.09509



— CLN
— BGL

$$10^{-3} \cdot |V_{cb}|$$

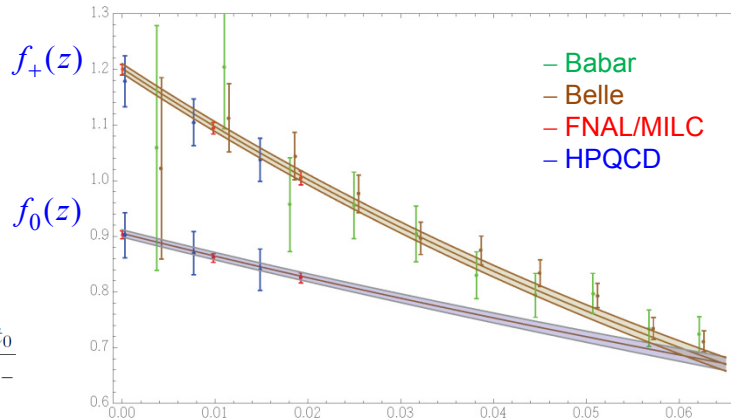
$$39.2 \pm 1.1$$

$$40.6 \pm 1.3$$

$$w = v_B \Gamma_{D^*}$$

See also Grinstein-Kobach, 1703.08170; Bernlochner-Ligeti-Papucci-Robinson, 1703.05330, 1708.07134

● $B \rightarrow D \ell \nu$



Bigi-Gambino-Schacht, 1606.08030

$$|V_{cb}| = (40.49 \pm 0.97) \cdot 10^{-3}$$

$$t_+ = (m_B + m_D)^2, \quad t_- = (m_B - m_D)^2,$$

$$z(w, \mathcal{N}) = \frac{\sqrt{1+w} - \sqrt{2\mathcal{N}}}{\sqrt{1+w} + \sqrt{2\mathcal{N}}}, \quad \mathcal{N} = \frac{t_+ - t_0}{t_+ - t_-}$$

CKM V_{ij}

CKM entry	Value	Source
$ V_{ud} $	0.97417 ± 0.00021 0.9758 ± 0.0016 0.9749 ± 0.0026	Nuclear β decay $n \rightarrow p e^- \bar{\nu}_e$ $\pi^+ \rightarrow \pi^0 e^+ \nu_e$
$ V_{us} $	0.2232 ± 0.0008 0.2253 ± 0.0007 0.2213 ± 0.0023	$K \rightarrow \pi e^- \bar{\nu}_e$ $K/\pi \rightarrow \mu \nu$, Lattice, V_{ud} τ decays
$ V_{cd} $	0.230 ± 0.011 0.216 ± 0.005	$\nu d \rightarrow c X$ $D \rightarrow (\pi) l \nu$, Lattice
$ V_{cs} $	0.997 ± 0.017	$D \rightarrow K l \nu$, $D_s \rightarrow l \nu$, Lattice
$ V_{cb} $	0.0405 ± 0.0010 0.0420 ± 0.0006	$B \rightarrow D^* l \bar{\nu}_l, D l \bar{\nu}_l$ $b \rightarrow c l \bar{\nu}_l$
$ V_{ub} $	0.00367 ± 0.00015 0.00451 ± 0.00020 0.00398 ± 0.00040	$B \rightarrow \pi l \bar{\nu}_l$ $b \rightarrow u l \bar{\nu}_l$
$ V_{tb} / \sqrt{\sum_q V_{tq} ^2}$ $ V_{tb} $	> 0.92 (95% CL) 1.009 ± 0.031	$t \rightarrow b W / t \rightarrow q W$ $p \bar{p} \rightarrow t b + X$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9988 \pm 0.0005$$

$$|V_{ub}|^2 + |V_{cb}|^2 + |V_{tb}|^2 = 1.020 \pm 0.063$$

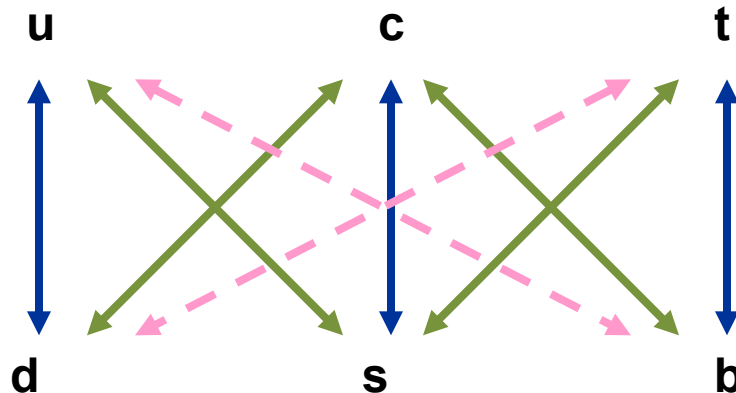
$$|V_{cd}|^2 + |V_{cs}|^2 + |V_{cb}|^2 = 1.042 \pm 0.034$$

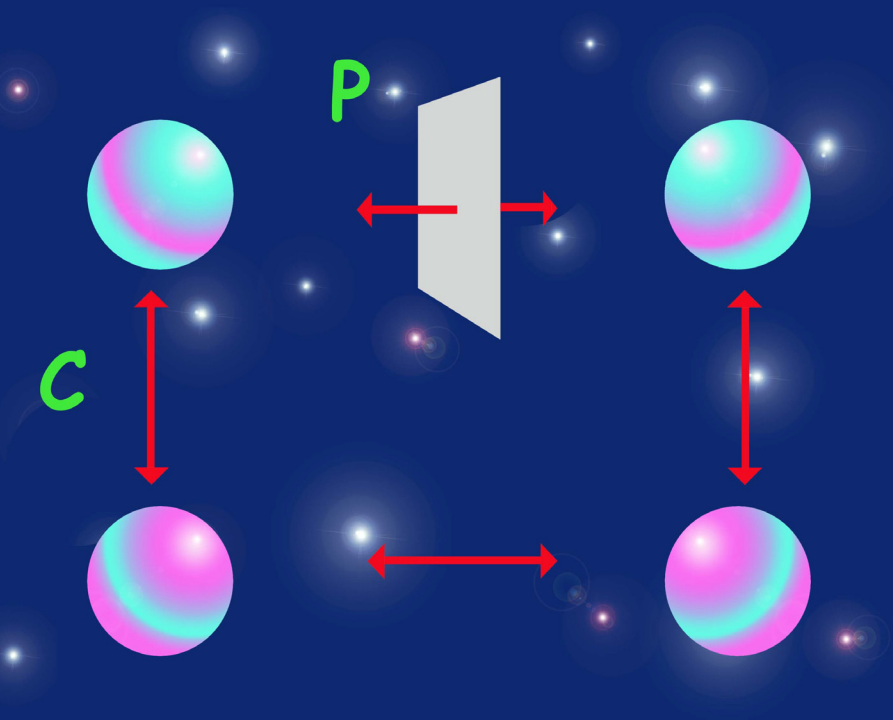
$$\sum_j (|V_{uj}|^2 + |V_{cj}|^2) = 2.002 \pm 0.027 \quad (\text{LEP})$$

Hierarchical Structure

$$\mathbf{V} \approx \begin{bmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{bmatrix} + \mathcal{O}(\lambda^4)$$

$$\lambda \approx \sin \theta_C \approx 0.223 \quad ; \quad A \approx 0.84 \quad ; \quad \sqrt{\rho^2 + \eta^2} \approx 0.4$$





- C, P : Violated maximally in weak inter.
- CP : Symmetry of nearly all phenom.
- Slight ($\sim 0.2\%$) CP in K^0 decays (1964)
- Sizeable CP in B^0 decays (2001)
- Huge Matter-Antimatter Asymmetry
➔ Baryogenesis

CPT Theorem: $CP \leftrightarrow T$

Thus, CP requires:

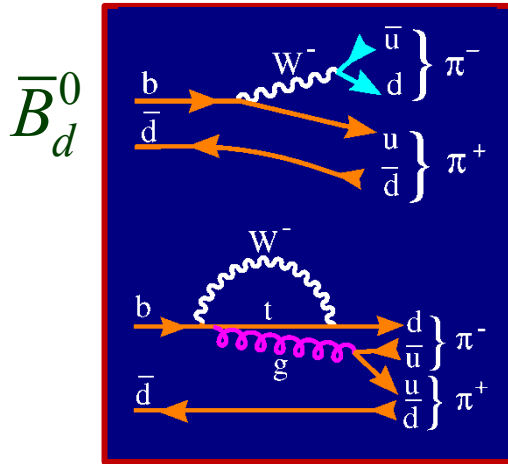
- Complex Phases
- Interferences

Standard Model CP : 3 fermion families needed

DIRECT

C/\mathcal{P}

$$|\mathbf{T}(P \rightarrow f)| \neq |\mathbf{T}(\bar{P} \rightarrow \bar{f})|$$



$$\mathbf{T}(P \rightarrow f) = T_1 e^{i\phi_1} e^{i\delta_1} + T_2 e^{i\phi_2} e^{i\delta_2}$$

\downarrow $C\mathcal{P}$

$$\mathbf{T}(\bar{P} \rightarrow \bar{f}) = T_1 e^{-i\phi_1} e^{i\delta_1} + T_2 e^{-i\phi_2} e^{i\delta_2}$$

$$A_{P \rightarrow f}^{\text{CP}} \equiv \frac{\Gamma(P \rightarrow f) - \Gamma(\bar{P} \rightarrow \bar{f})}{\Gamma(P \rightarrow f) + \Gamma(\bar{P} \rightarrow \bar{f})} = \frac{-2 T_1 T_2 \sin(\phi_2 - \phi_1) \sin(\delta_2 - \delta_1)}{T_1^2 + T_2^2 + 2 T_1 T_2 \cos(\phi_2 - \phi_1) \cos(\delta_2 - \delta_1)}$$

One needs:

- 2 Interfering Amplitudes
- 2 Different Weak Phases $[\sin(\phi_2 - \phi_1) \neq 0]$
- 2 Different FSI Phases $[\sin(\delta_2 - \delta_1) \neq 0]$

DIRECT ~~CP~~

$$A_{CP}(B \rightarrow f) \equiv \frac{\text{Br}(\bar{B} \rightarrow \bar{f}) - \text{Br}(B \rightarrow f)}{\text{Br}(\bar{B} \rightarrow \bar{f}) + \text{Br}(B \rightarrow f)}$$

$$A_{CP}(B_d^0 \rightarrow \pi^- K^+) = -0.082 \pm 0.006 \quad (13.7 \sigma)$$

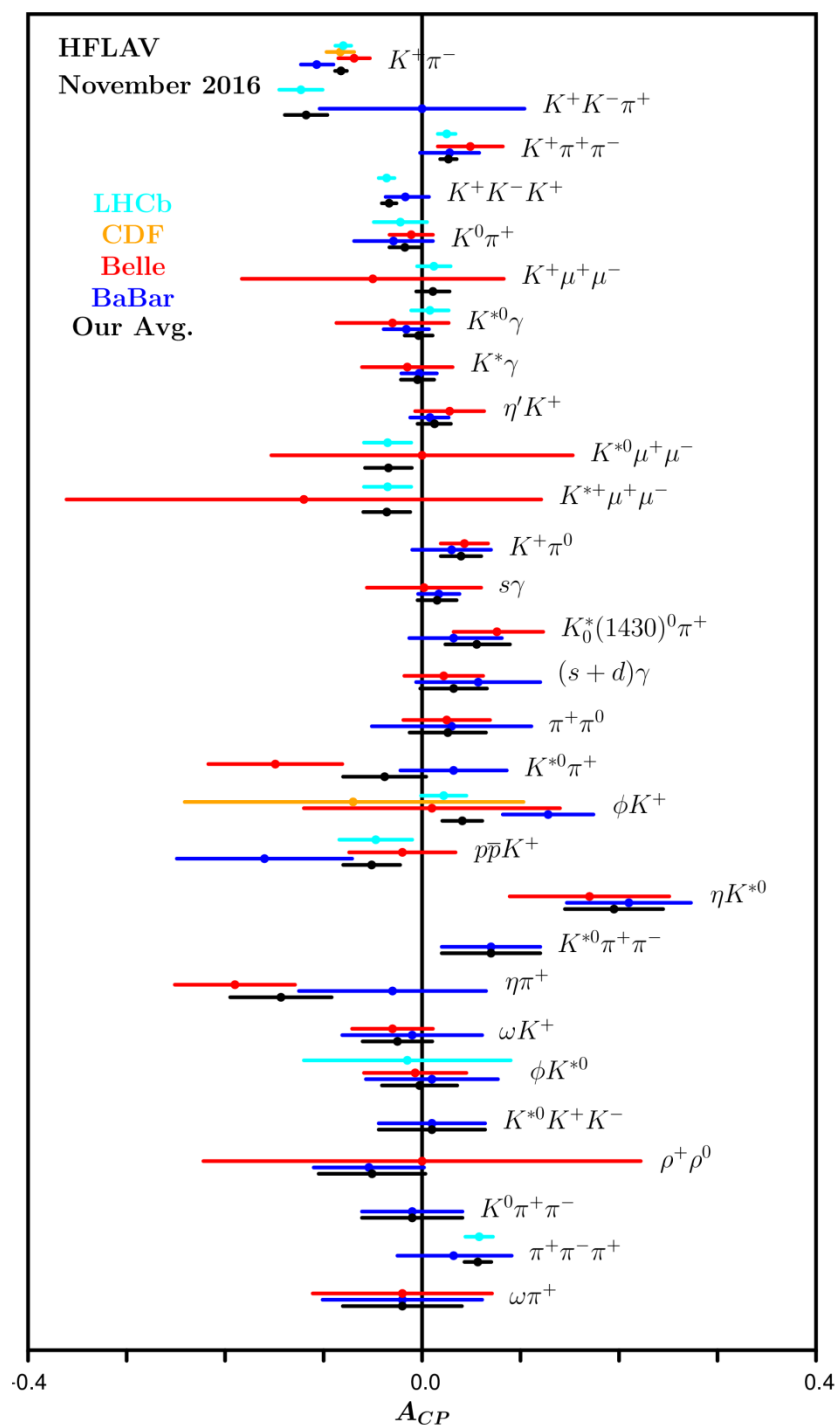
$$A(B_s^0 \rightarrow \pi^- K^+) = -0.26 \pm 0.04 \quad (6.5 \sigma)$$

$$A_{CP}(B^+ \rightarrow K^+ K^- \pi^+) = -0.118 \pm 0.022 \quad (5.4 \sigma)$$

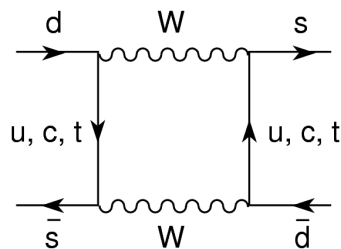
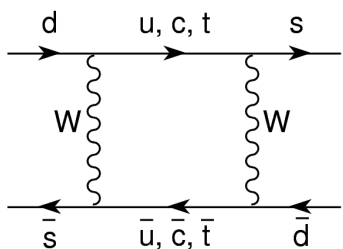
Large & Interesting Signals

Big challenge: Get reliable SM predictions

Severe hadronic uncertainties



INDIRECT \mathcal{CP} : $K^0 - \bar{K}^0$ MIXING



$$|K_{S,L}^0\rangle \sim p |K^0\rangle \mp q |\bar{K}^0\rangle$$

$$q/p \equiv (1 - \bar{\epsilon}_K)/(1 + \bar{\epsilon}_K)$$

$$\langle \bar{K}^0 | \mathbf{H} | K^0 \rangle \sim \sum_{ij} \lambda_i \lambda_j S(r_i, r_j) \eta_{ij} \langle O_{\Delta S=2} \rangle$$

$$\langle O_{\Delta S=2} \rangle = \alpha_s(\mu)^{-2/9} \langle \bar{K}^0 | (\bar{s}_L \gamma^\alpha d_L)(\bar{s}_L \gamma_\alpha d_L) | K^0 \rangle \equiv \left(\frac{4}{3} M_K^2 f_K^2 \right) \hat{B}_K$$

$$\lambda_i \equiv V_{id} V_{is}^* \quad ; \quad r_i \equiv m_i^2 / M_W^2 \quad (i = u, c, t)$$

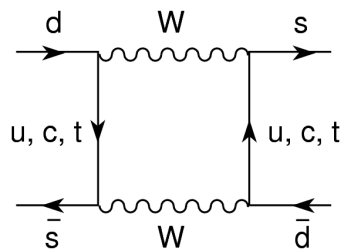
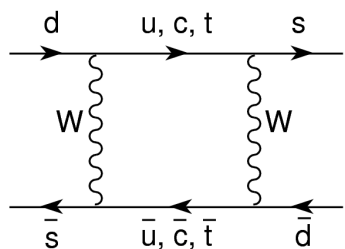
- **GIM Mechanism:** $\lambda_u + \lambda_c + \lambda_t = 0$

$$(M_{K_L} - M_{K_S}) / M_{K^0} = (7.00 \pm 0.01) \times 10^{-15}$$

- \mathcal{CP} : $\text{Im} \lambda_t = -\text{Im} \lambda_c \simeq \eta \lambda^5 A^2$

- **Hard GIM Breaking:** $S(r_i, r_i) \sim r_i \rightarrow$ **t quark**

INDIRECT CP : $K^0 - \bar{K}^0$ MIXING



$$|K_{S,L}^0\rangle \sim p |K^0\rangle \mp q |\bar{K}^0\rangle$$

$$q/p \equiv (1 - \bar{\varepsilon}_K)/(1 + \bar{\varepsilon}_K)$$

$$K^0 \rightarrow \pi^- l^+ \nu_l \quad (\bar{s} \rightarrow \bar{u}) \quad ; \quad \bar{K}^0 \rightarrow \pi^+ l^- \bar{\nu}_l \quad (s \rightarrow u)$$

$$\frac{\Gamma(K_L^0 \rightarrow \pi^- l^+ \nu_l) - \Gamma(K_L^0 \rightarrow \pi^+ l^- \bar{\nu}_l)}{\Gamma(K_L^0 \rightarrow \pi^- l^+ \nu_l) + \Gamma(K_L^0 \rightarrow \pi^+ l^- \bar{\nu}_l)} = \frac{|p|^2 - |q|^2}{|p|^2 + |q|^2} = \frac{2 \operatorname{Re}(\bar{\varepsilon}_K)}{1 + |\bar{\varepsilon}_K|^2} = (0.332 \pm 0.006)\%$$



$$\operatorname{Re}(\bar{\varepsilon}_K) = (1.66 \pm 0.03) \cdot 10^{-3}$$

$$\eta_{+-} \equiv \frac{T(K_L \rightarrow \pi^+ \pi^-)}{T(K_S \rightarrow \pi^+ \pi^-)} \approx \varepsilon_K$$

$$\eta_{00} \equiv \frac{T(K_L \rightarrow \pi^0 \pi^0)}{T(K_S \rightarrow \pi^0 \pi^0)} \approx \varepsilon_K$$

$$\varepsilon_K = (2.228 \pm 0.011) \cdot 10^{-3} e^{i\phi_\varepsilon}$$



$$\eta \left[(1 - \rho) A^2 + 0.22 \right] A^2 \hat{B}_K = 0.143$$

$$\phi_\varepsilon = (43.52 \pm 0.05)^\circ$$

Buras et al

DIRECT C/P in $K \rightarrow \pi \pi$

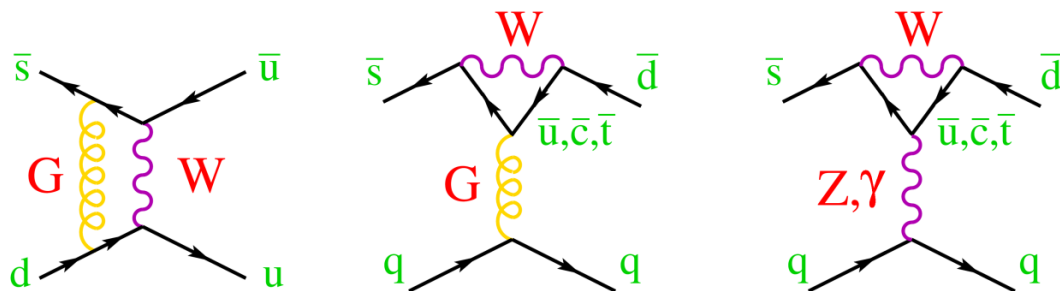
$$\eta_{+-} \equiv \frac{T(K_L \rightarrow \pi^+ \pi^-)}{T(K_S \rightarrow \pi^+ \pi^-)} \approx \varepsilon_K + \varepsilon'_K$$

$$\eta_{00} \equiv \frac{T(K_L \rightarrow \pi^0 \pi^0)}{T(K_S \rightarrow \pi^0 \pi^0)} \approx \varepsilon_K - 2\varepsilon'_K$$

$$\text{Re}(\varepsilon'_K / \varepsilon_K) \approx \frac{1}{6} \left\{ 1 - \left| \frac{\eta_{00}}{\eta_{+-}} \right|^2 \right\} = (16.6 \pm 2.3) \cdot 10^{-4}$$

NA48, NA31 (1988-2003)

KTeV, E731 (1993-2010)



$$\text{Re}(\varepsilon'_K / \varepsilon_K)_{\text{Th}} = (19^{+11}_{-9}) \cdot 10^{-4}$$

- Short-distance OPE

Ciuchini et al, Buras et al

- Long-distance χ PT

Pallante-Pich-Scimemi (2001)

Cirigliano-Ecker-Neufeld-Pich (2003)

Recent $K \rightarrow (\pi\pi)_I$ Lattice Results

Isospin limit:

RBC-UKQCD 1505.07863, 1502.00263


$\sqrt{\frac{3}{2}} \text{Re } A_2 = (1.50 \pm 0.04 \pm 0.14) \cdot 10^{-8} \text{ GeV}$	exp : $1.482(2) \cdot 10^{-8} \text{ GeV}$ 0.1 σ
$\sqrt{\frac{3}{2}} \text{Im } A_2 = -(6.99 \pm 0.20 \pm 0.84) \cdot 10^{-13} \text{ GeV}$	
$\sqrt{\frac{3}{2}} \text{Re } A_0 = (4.66 \pm 1.00 \pm 1.26) \cdot 10^{-7} \text{ GeV}$	exp : $3.112(1) \cdot 10^{-7} \text{ GeV}$ 1.0 σ
$\sqrt{\frac{3}{2}} \text{Im } A_0 = -(1.90 \pm 1.23 \pm 1.08) \cdot 10^{-11} \text{ GeV}$	
$\text{Re}(\varepsilon'/\varepsilon) = (1.38 \pm 5.15 \pm 4.59) \cdot 10^{-4}$	exp : $(16.6 \pm 2.3) \cdot 10^{-4}$ 2.1 σ
$\delta_0 = (23.8 \pm 4.9 \pm 1.2)^\circ$	exp : $(39.2 \pm 1.5)^\circ$ 2.9 σ
$\delta_2 = -(11.6 \pm 2.5 \pm 1.2)^\circ$	exp : $-(8.5 \pm 1.5)^\circ$ 1.0 σ

$\Delta I = 1/2$ Rule

$$\omega \equiv \frac{\text{Re } A_2}{\text{Re } A_0} \approx \frac{1}{22}$$

Large phase shift

$$\delta_0 - \delta_2 = (47.5 \pm 0.9)^\circ$$

Anomaly?  New-physics ? (Buras et al, Kitahara et al, Endo et al, Cirigliano et al...)

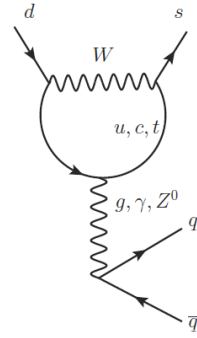
$$\text{Re}(\varepsilon'_K / \varepsilon_K)_{\text{SM}} = -\frac{\omega}{\sqrt{2} |\varepsilon_K|} \left[\frac{\text{Im } A_0}{\text{Re } A_0} (1 - \Omega_{\text{eff}}) - \frac{\text{Im } A_2^{\text{emp}}}{\text{Re } A_2} \right] \approx 2.2 \cdot 10^{-3} \left\{ B_6^{(1/2)} (1 - \Omega_{\text{eff}}) - 0.48 B_8^{(3/2)} \right\}$$

$$\Omega_{\text{eff}} = 0.060 \pm 0.077$$

Cirigliano-Ecker-Neufeld-Pich (2003)

Effective Field Theory: Long & Short distance dynamics

M_W
 W, Z, γ, g
 τ, μ, e, ν_i
 t, b, c, s, d, u
 Standard Model

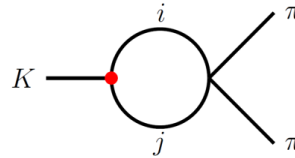


$$\mathcal{L}_{\text{eff}}^{\Delta S=1} = -\frac{G_F}{\sqrt{2}} V_{ud} V_{us}^* \sum_i C_i(\mu) Q_i(\mu)$$

$\lesssim m_c$
 $\gamma, g; \mu, e, \nu_i$
 s, d, u
 $\mathcal{L}_{\text{QCD}}^{(n_f=3)}, \mathcal{L}_{\text{eff}}^{\Delta S=1,2}$

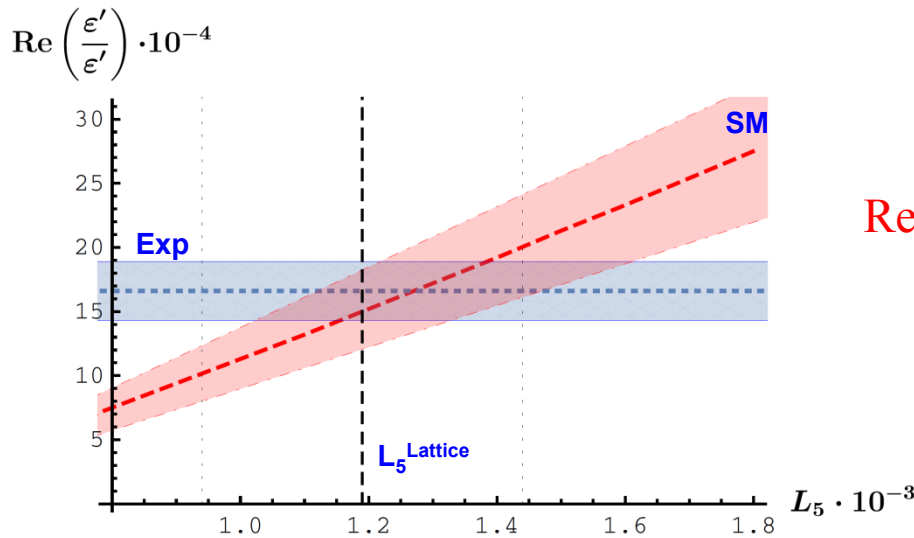
Large logarithmic corrections

M_K
 $\gamma; \mu, e, \nu_i$
 π, K, η
 χPT



OPE: $\alpha_s^k(\mu) \log^n(M_W/\mu)$

χPT : $\log(\mu/m_\pi)$

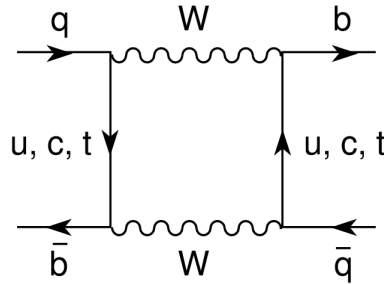
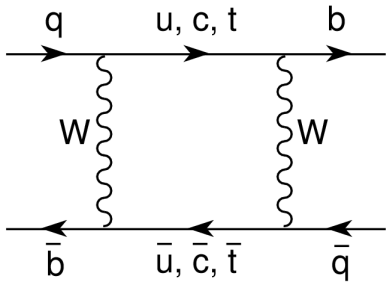


Gisbert-Pich, arXiv:1712.xxxx

$$\begin{aligned} \text{Re}(\varepsilon'_K / \varepsilon_K)_{\text{SM}} &= (15 \pm 2_\mu \pm 2_{m_s} \pm 2_{\Omega_{\text{eff}}} \pm 6_{1/N_c}) \cdot 10^{-4} \\ &= (15 \pm 7) \cdot 10^{-4} \end{aligned}$$

Large uncertainty, but no anomaly!

$B^0 - \bar{B}^0$ MIXING



$$V_{ud} V_{ub}^* \sim V_{cd} V_{cb}^* \sim V_{td} V_{tb}^* \sim A \lambda^3$$

$$\langle \bar{B}^0 | \mathbf{H} | B^0 \rangle \sim |V_{td}|^2 S(r_t, r_t) \left(\frac{4}{3} M_B^2 f_B^2 \right) \hat{B}_B$$

$$\Delta M_{B_d^0} = (0.5064 \pm 0.0019) \text{ ps}^{-1}$$



$$|V_{td}|$$

- $\Delta M_{B_d^0} / \Gamma_{B_d^0} = 0.770 \pm 0.004$
- $\Delta M_{B_s^0} = (17.757 \pm 0.021) \text{ ps}^{-1}$
- $\Delta \Gamma_{B^0} / \Delta M_{B^0} \sim m_b^2 / m_t^2 \ll 1$
- $\text{Re}(\bar{\varepsilon}_{B_d^0}) = -0.0005 \pm 0.0004$

$$\Delta M_{B_s^0} / \Gamma_{B_s^0} = 26.72 \pm 0.09$$

$$|V_{ts}|^2 \gg |V_{td}|^2$$

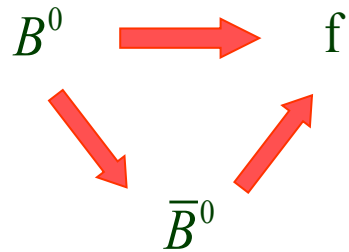
$$\Delta \Gamma_{B_s^0} / \Gamma_{B_s^0} = -0.130 \pm 0.009$$

$$\text{Re}(\bar{\varepsilon}_{B_s^0}) = -0.0002 \pm 0.0007$$

C/P very small

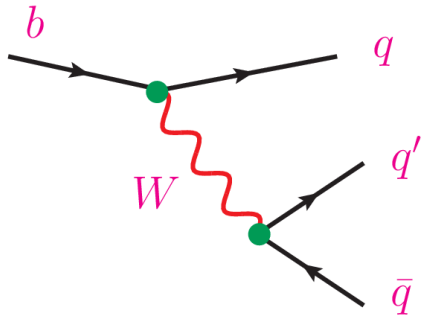
$$|q/p| - 1 \sim m_c^2 / m_t^2$$

$B^0 - \bar{B}^0$ MIXING AND DIRECT ~~CP~~



CP self-conjugate: $\bar{f} = \eta_f f$

$$\frac{q}{p} \approx \frac{V_{tb}^* V_{tq}}{V_{tb} V_{tq}^*} = e^{-2i\phi_M} \quad ; \quad \phi_M \approx \begin{cases} \beta & (B_d^0) \\ -\beta_s \approx -\lambda^2 \eta & (B_s^0) \end{cases}$$



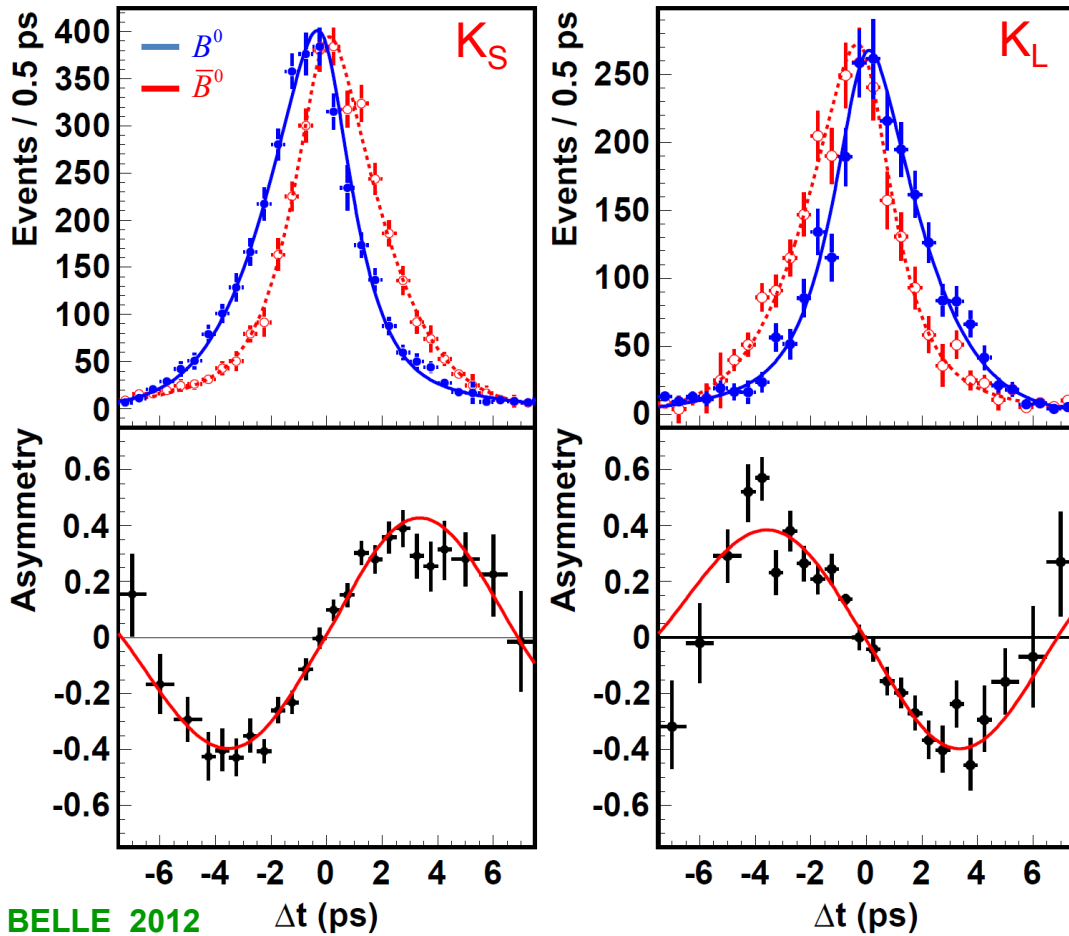
Assumption: **Only 1 decay amplitude**

$$\frac{A_{b \rightarrow q\bar{q}q'}}{A_{\bar{b} \rightarrow \bar{q}qq'}} = \frac{V_{qb} V_{qq'}^*}{V_{qb}^* V_{qq'}} = e^{-2i\phi_D} \quad \longrightarrow \quad \begin{aligned} \rho_{\bar{f}} &= \bar{\rho}_f^* = \eta_f e^{2i\phi_D} \\ C_f &= 0 \end{aligned}$$

$$\longrightarrow \frac{\Gamma(\bar{B}^0 \rightarrow \bar{f}) - \Gamma(B^0 \rightarrow f)}{\Gamma(\bar{B}^0 \rightarrow \bar{f}) + \Gamma(B^0 \rightarrow f)} = -\eta_f \sin(2\phi) \sin(\Delta M t) \quad ; \quad \phi = \phi_M + \phi_D$$

Direct information on the CKM matrix

$$\frac{\Gamma(\bar{B}^0 \rightarrow J/\psi K_S) - \Gamma(B^0 \rightarrow J/\psi K_S)}{\Gamma(\bar{B}^0 \rightarrow J/\psi K_S) + \Gamma(B^0 \rightarrow J/\psi K_S)} = -\eta_f \sin(2\beta) \sin(\Delta M t)$$



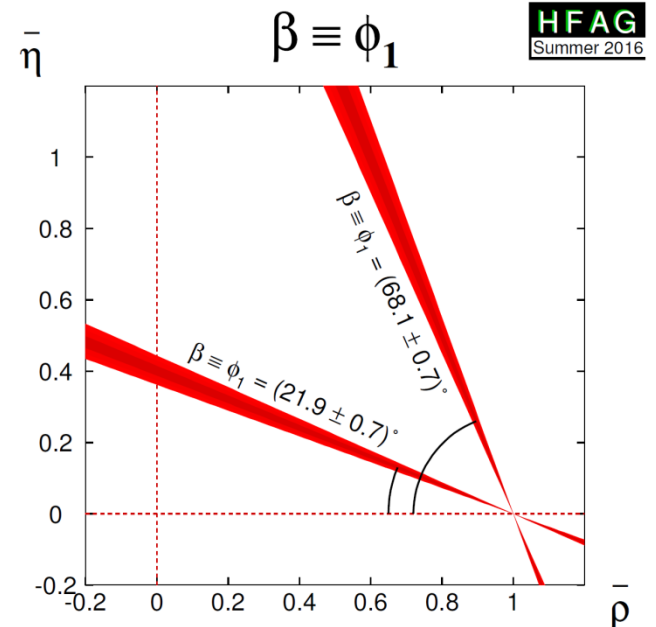
BELLE 2012

~~CP~~ Signal

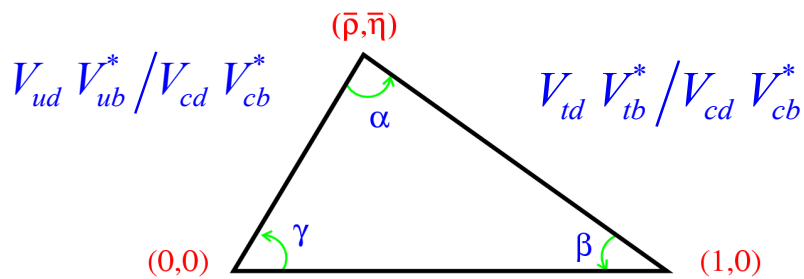
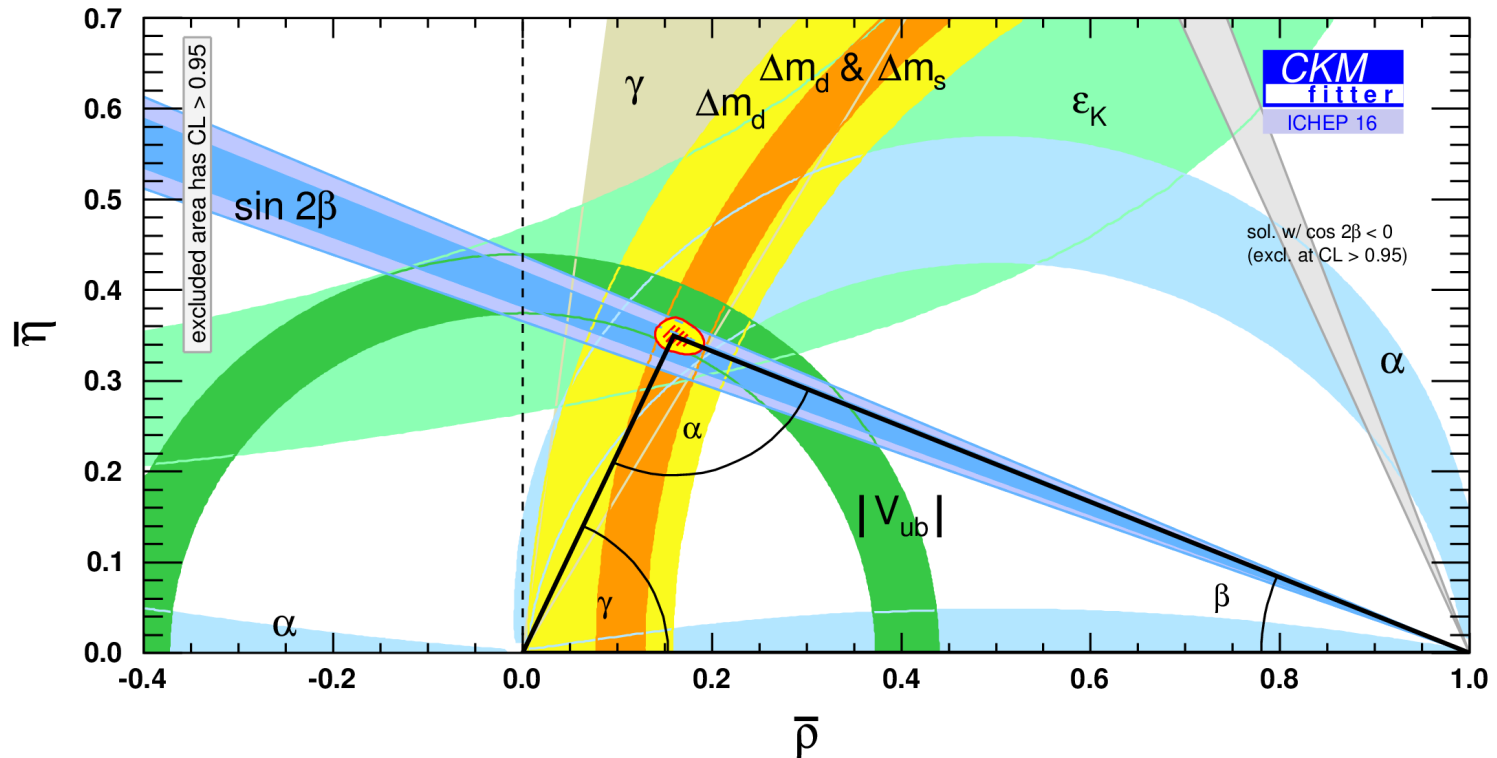
HFAG:

$$\sin(2\beta) = 0.69 \pm 0.02$$

$B^0 \rightarrow J/\psi K_{S,L}, \psi(2S) K_S, \chi_c K_S, \eta_c K_S$



$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$



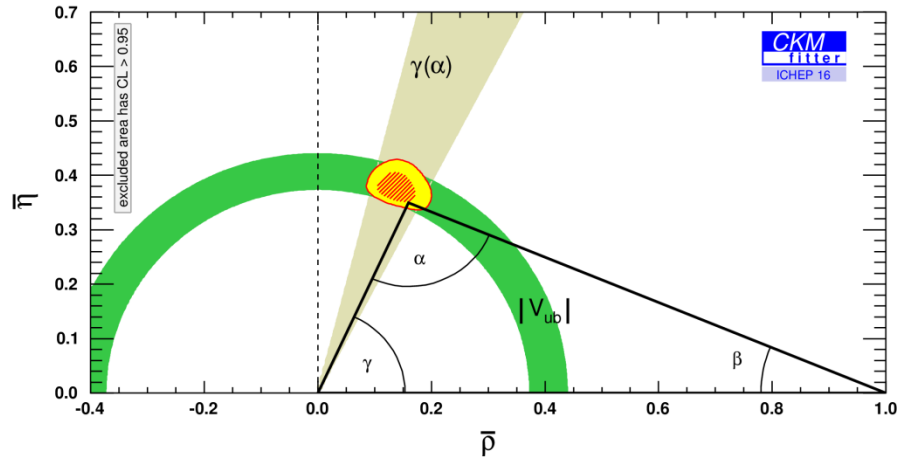
UT_{fit}

$$\bar{\eta} \equiv \eta \left(1 - \frac{1}{2} \lambda^2 \right) = 0.343 \pm 0.011$$

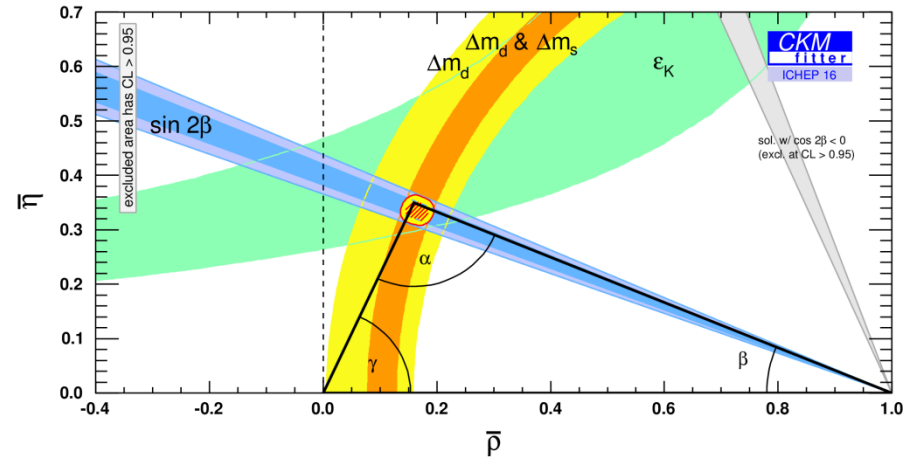
$$\bar{\rho} \equiv \rho \left(1 - \frac{1}{2} \lambda^2 \right) = 0.153 \pm 0.013$$

$$\alpha = 91.0 \pm 2.5^\circ ; \beta = 23.2 \pm 1.2^\circ ; \gamma = 65.3 \pm 2.0^\circ$$

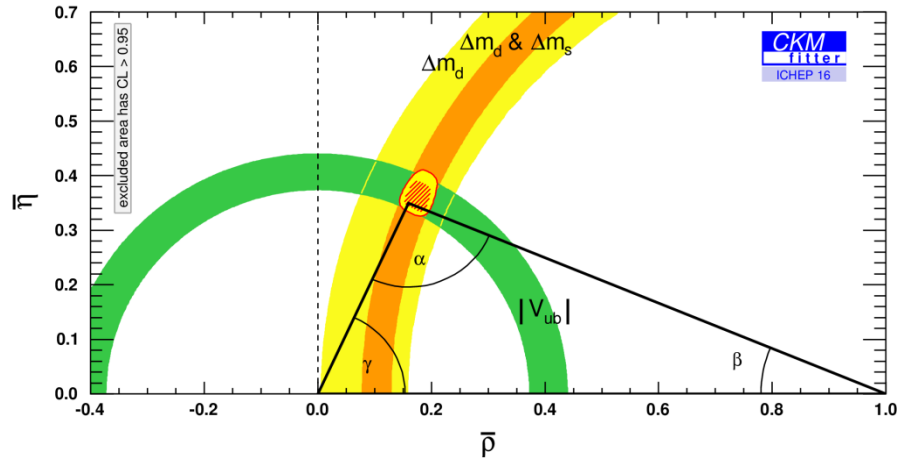
Tree-level determinations



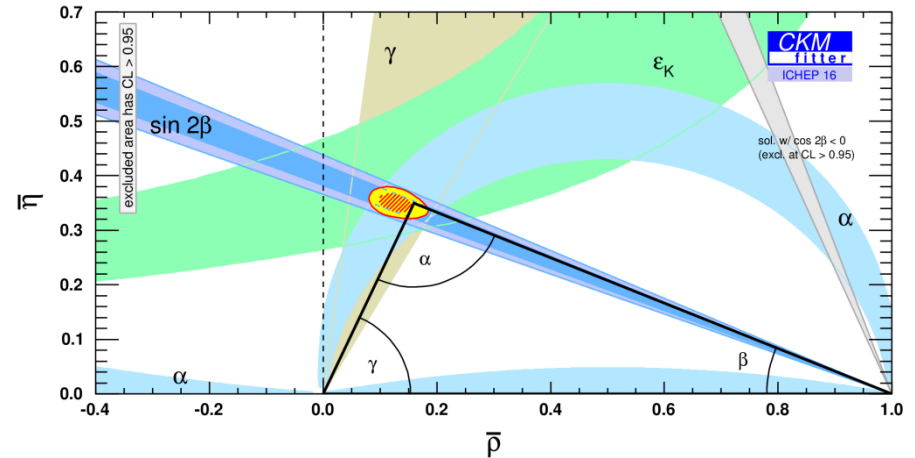
Loop processes



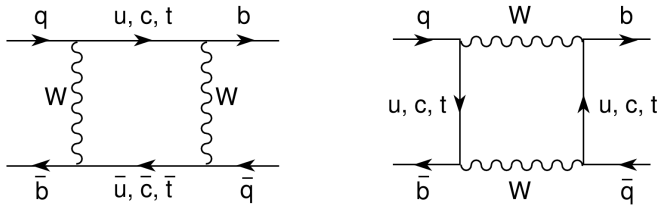
CP Conserving



CP Violating



Bounds on New Flavour Physics



$$L_{\text{eff}} = L_{\text{SM}} + \sum_{D>4} \sum_k \frac{c_k^{(D)}}{\Lambda_{\text{NP}}^{D-4}} O_k^{(D)}$$

Isidori, 1302.0661

Operator	Bounds on Λ in TeV ($c_{\text{NP}} = 1$)		Bounds on c_{NP} ($\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	9.8×10^2	1.6×10^4	9.0×10^{-7}	3.4×10^{-9}	$\Delta m_K; \epsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	1.8×10^4	3.2×10^5	6.9×10^{-9}	2.6×10^{-11}	$\Delta m_K; \epsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	1.2×10^3	2.9×10^3	5.6×10^{-7}	1.0×10^{-7}	$\Delta m_D; q/p , \phi_D$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	6.2×10^3	1.5×10^4	5.7×10^{-8}	1.1×10^{-8}	$\Delta m_D; q/p , \phi_D$
$(\bar{b}_L \gamma^\mu d_L)^2$	6.6×10^2	9.3×10^2	2.3×10^{-6}	1.1×10^{-6}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	2.5×10^3	3.6×10^3	3.9×10^{-7}	1.9×10^{-7}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_L \gamma^\mu s_L)^2$	1.4×10^2	2.5×10^2	5.0×10^{-5}	1.7×10^{-5}	$\Delta m_{B_s}; S_{\psi \phi}$
$(\bar{b}_R s_L)(\bar{b}_L s_R)$	4.8×10^2	8.3×10^2	8.8×10^{-6}	2.9×10^{-6}	$\Delta m_{B_s}; S_{\psi \phi}$

- Generic flavour structure [$c_{\text{NP}} \sim \mathcal{O}(1)$] ruled out at the TeV scale
- $\Lambda_{\text{NP}} \sim 1$ TeV requires c_{NP} to inherit the strong SM suppressions (GIM)

Minimal Flavour Violation: The up and down Yukawa matrices are the only source of quark-flavour symmetry breaking

D'Ambrosio et al, Buras et al

Yukawa Interactions in 2HDMs

$$L_Y = -\bar{Q}'_L (\Gamma_1 \phi_1 + \Gamma_2 \phi_2) d'_R - \bar{Q}'_L (\Delta_1 \tilde{\phi}_1 + \Delta_2 \tilde{\phi}_2) u'_R$$

SSB ↓

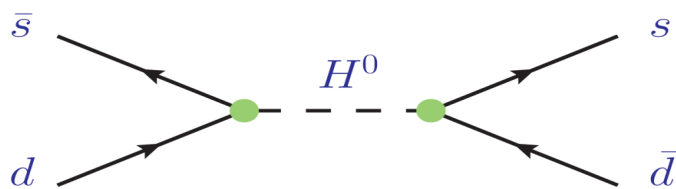
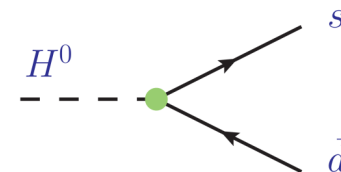
$$\phi_i^{(0)} = \frac{v_i}{\sqrt{2}}, \quad v = \sqrt{v_1^2 + v_2^2}$$

$$L_Y = -\frac{\sqrt{2}}{v} \left\{ \bar{Q}'_L (M'_d \Phi_1 + Y'_d \Phi_2) d'_R - \bar{Q}'_L (M'_u \tilde{\Phi}_1 + Y'_u \tilde{\Phi}_2) u'_R \right\}$$

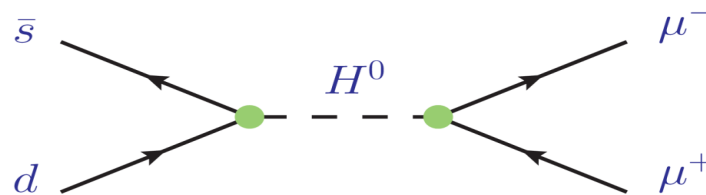
M'_q and Y'_q unrelated



FCNCs



$K^0 \leftrightarrow \bar{K}^0$



$K^0 \rightarrow \mu^- \mu^+$

Phenomenological disaster!

Aligned 2HDM

Pich-Tuzón, 0908.1554

Yukawa alignment in Flavour Space: $Y_{d,l} = \varsigma_{d,l} M_{d,l}$, $Y_u = \varsigma_u^* M_u$

$$\mathcal{L}_Y = -\frac{\sqrt{2}}{v} H^+ \left\{ \bar{u} \left[\varsigma_d V_{\text{CKM}} M_d \mathcal{P}_R - \varsigma_u M_u^\dagger V_{\text{CKM}} \mathcal{P}_L \right] d + \varsigma_l (\bar{\nu} M_l \mathcal{P}_R l) \right\} \\ - \frac{1}{v} \sum_{\varphi_i^0, f} y_f^{\varphi_i^0} \varphi_i^0 (\bar{f} M_f \mathcal{P}_R f) + \text{h.c.}$$

$$y_{d,l}^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} + i \mathcal{R}_{i3}) \varsigma_{d,l} \quad , \quad y_u^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} - i \mathcal{R}_{i3}) \varsigma_u^*$$

$\varsigma_f \longrightarrow$ **New sources of CP violation without tree-level FCNCs**

\mathcal{Z}_2 models:

Model	ς_d	ς_u	ς_l
Type I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type II	$-\tan \beta$	$\cot \beta$	$-\tan \beta$
Type X	$\cot \beta$	$\cot \beta$	$-\tan \beta$
Type Y	$-\tan \beta$	$\cot \beta$	$\cot \beta$
Inert	0	0	0

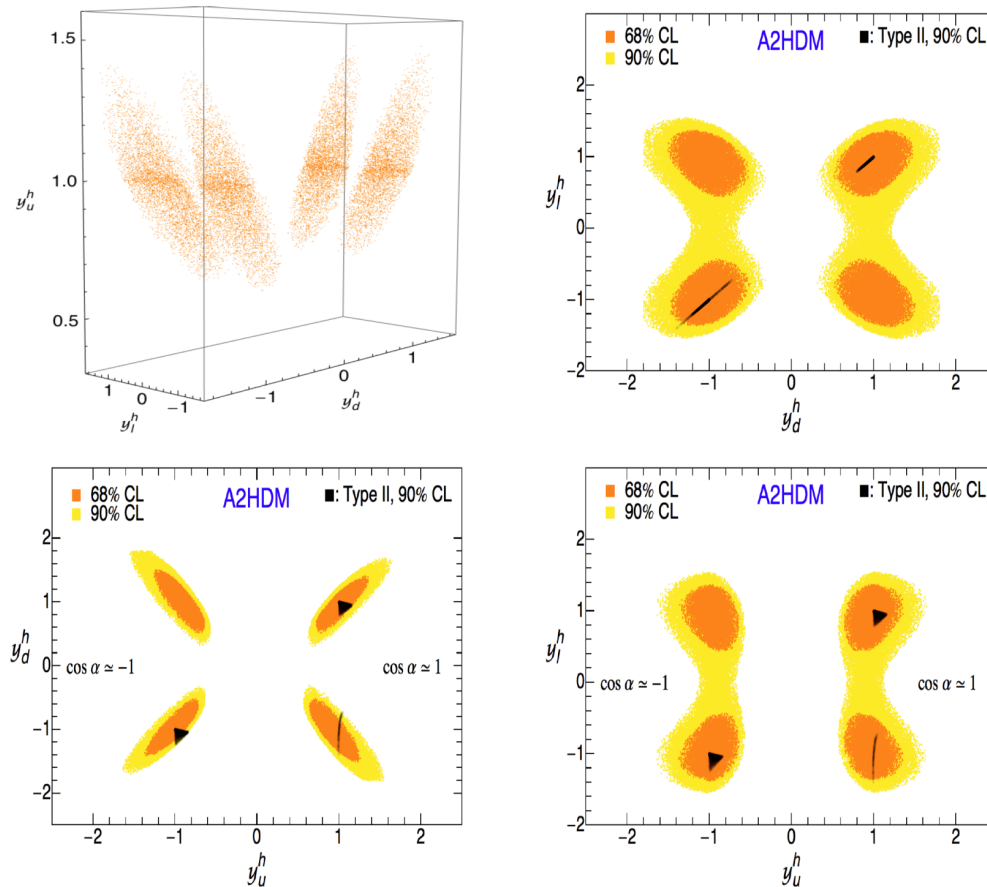
Only one ϕ_a couples to f_R
(Glashow-Weinberg, Paschos '77)

Flavour Alignment

(Aligned 2HDM)

AP-Tuzón

Celis-Ilisie-AP, 1302.4022, 1310.7941



$$|\cos \tilde{\alpha}| > 0.80 \quad (90\% \text{ CL})$$

General setting without FCNCs
& new sources of CP violation

$$Y_{d,l} = \zeta_{d,l} M_{d,l} \quad , \quad Y_u = \zeta_u^* M_u$$

Rich phenomenology @ LHC

Altmannshofer et al, Barger et al, Celis et al,
Cervero-Gerard, López-Val et al...

Many allowed possibilities

Search for light H^\pm, H, A

CP violation

Flavour constraints fulfilled

Celis et al, Jung et al, Li et al

EDMs

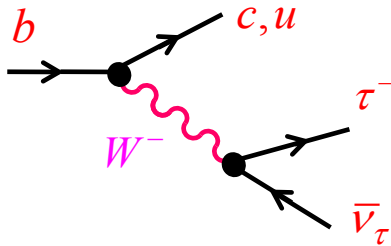
Jung-AP, 1308.6283

Usual Z_2 models recovered in particular (CP-conserving) limits

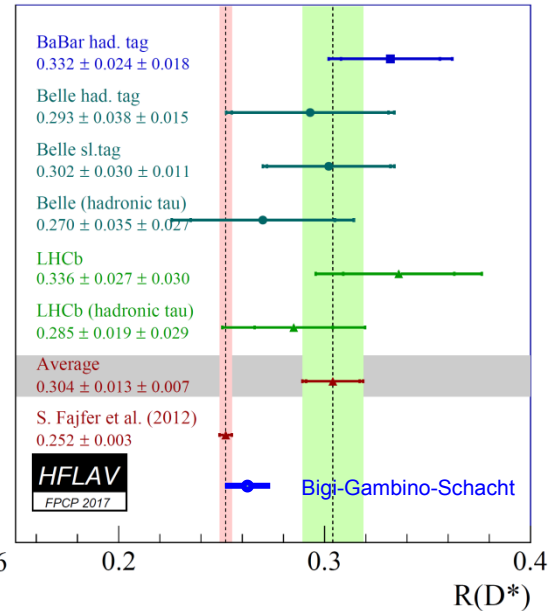
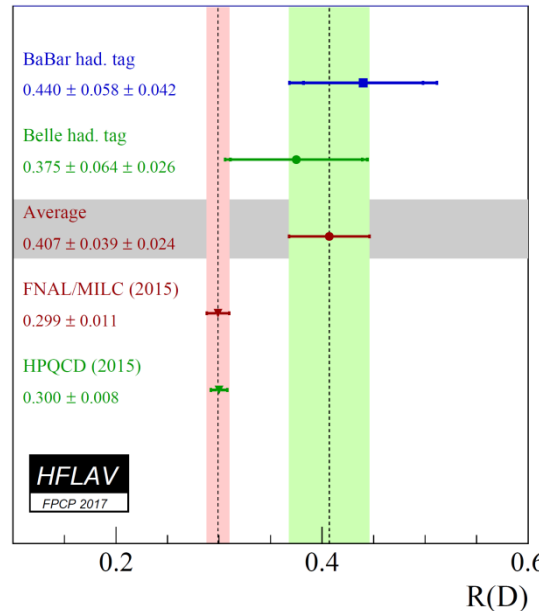
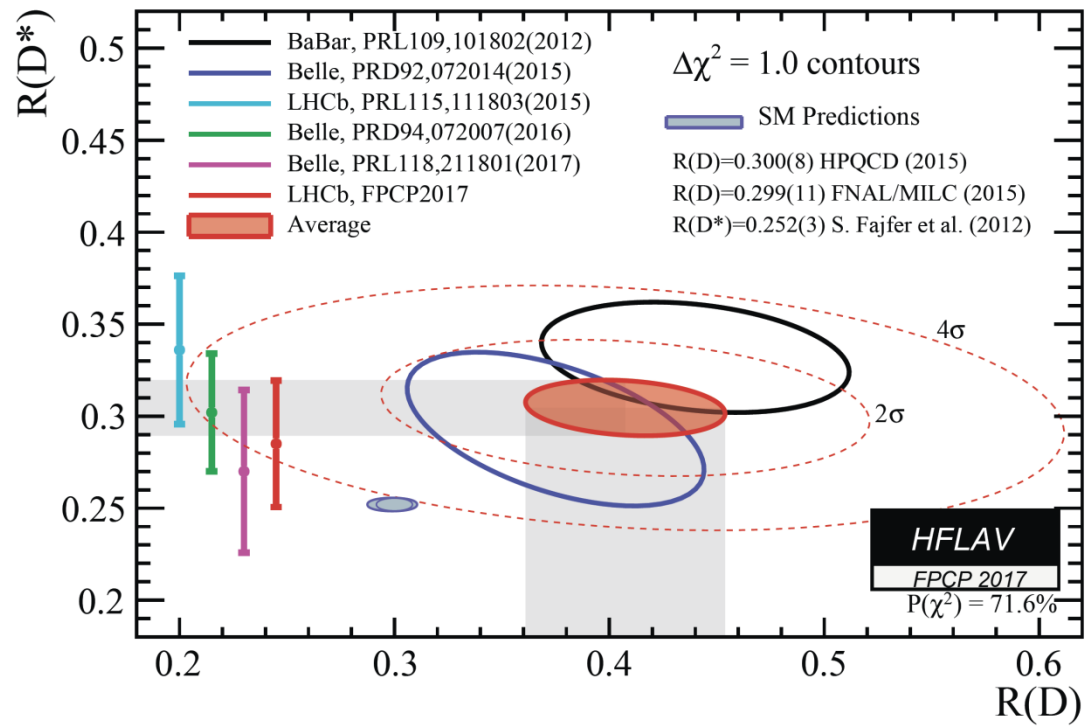
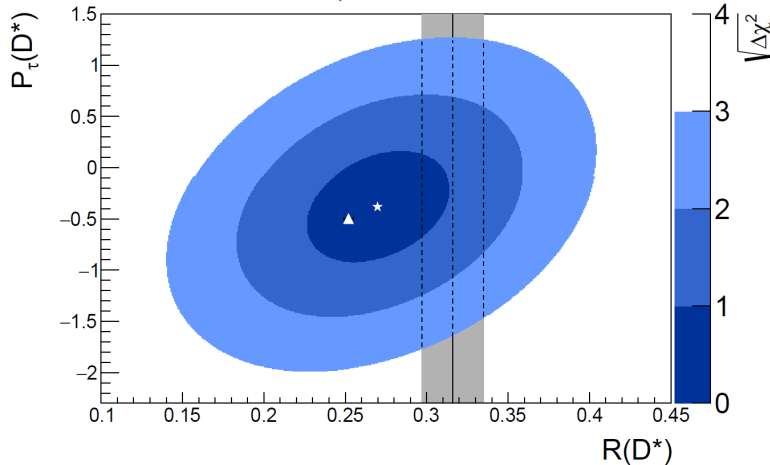
Flavour Anomaly

4 σ discrepancy

$$R(D^{(*)}) \equiv \frac{\text{Br}(\bar{B} \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau)}{\text{Br}(\bar{B} \rightarrow D^{(*)} \ell^- \bar{\nu}_\ell)}$$



Belle, 1612.00529



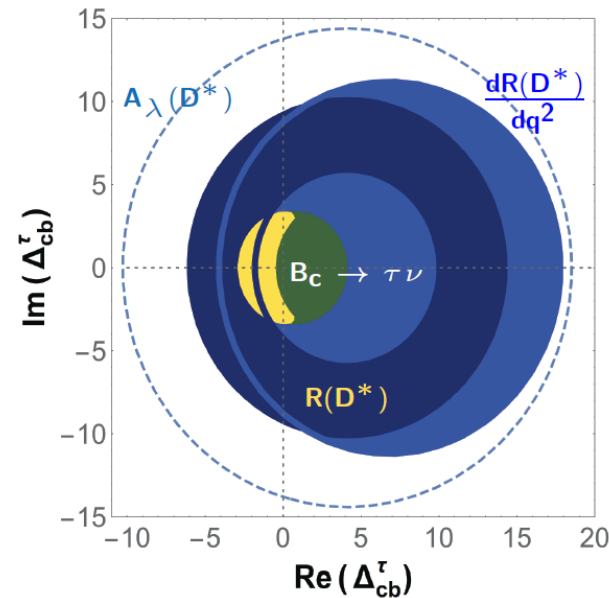
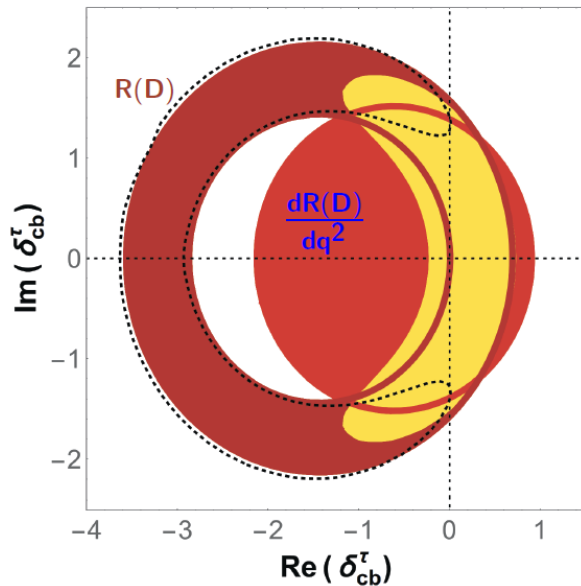
Model-Independent Analysis of $R(D^{(*)})$

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{q_u q_d} [\bar{q}_u (g_L^{q_u q_d \ell} \mathcal{P}_L + g_R^{q_u q_d \ell} \mathcal{P}_R) q_d] [\bar{\ell} \mathcal{P}_L \nu_\ell]$$

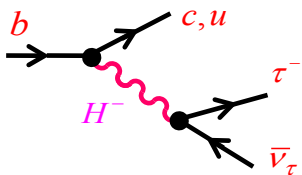
Scalar Form Factors

$$\left\{ \begin{array}{l} \delta R(D) \longleftrightarrow \delta_{cb}^\ell \equiv (g_L^{cbl} + g_R^{cbl}) \frac{(m_B - m_D)^2}{m_\ell (\bar{m}_b - \bar{m}_c)} \\ \delta R(D^*) \longleftrightarrow \Delta_{cb}^\ell \equiv (g_L^{cbl} - g_R^{cbl}) \frac{m_B^2}{m_\ell (\bar{m}_b + \bar{m}_c)} \end{array} \right.$$

95% CL

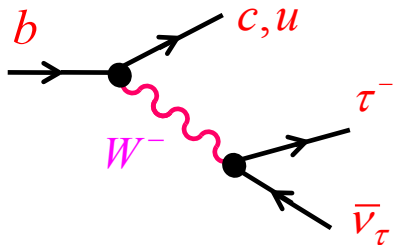


Celis et al.
1612.07757



$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu)} = 0.71 \pm 0.17 (\text{stat}) \pm 0.18 (\text{syst})$$

2 σ above SM prediction



$$\mathcal{R}(J/\psi)_{\text{SM}} \approx 0.25 - 0.28$$

Yu et al, Ivanov et al, Kiselev, Hernández et al

1) New physics only contributes to the SM operator

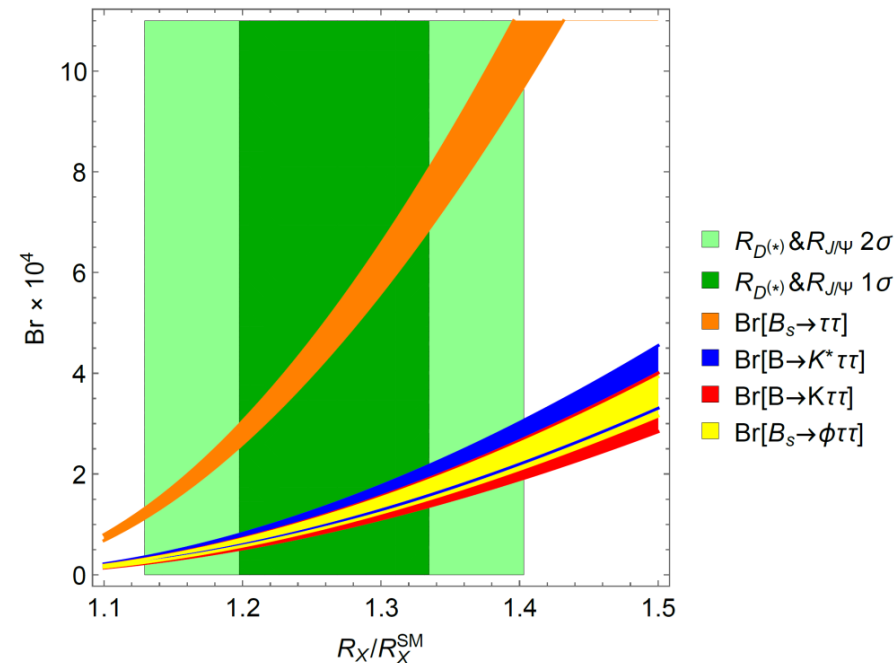
$$[\bar{c}\gamma^\mu P_L b][\bar{\tau}\gamma_\mu P_L \nu_\tau]$$

➔ $R_{J/\psi}/R_{J/\psi}^{\text{SM}} = R_D/R_D^{\text{SM}} = R_{D^*}/R_{D^*}^{\text{SM}}$

2) At higher scales, it originates from (avoids $b \rightarrow s\nu\nu$ constraints)

$$[\bar{Q}_2\gamma^\mu Q_3][\bar{L}_3\gamma_\mu L_3] + [\bar{Q}_2\gamma^\mu\sigma^I Q_3][\bar{L}_3\gamma_\mu\sigma^I L_3] \approx 2 [(\bar{c}_L\gamma_\mu b_L)(\bar{\tau}_L\gamma^\mu\nu_{\tau L}) + (\bar{s}_L\gamma_\mu b_L)(\bar{\tau}_L\gamma^\mu\tau_L)]$$

➔ Large $\text{Br}(b \rightarrow s\tau^+\tau^-)$



See also:

Alonso et al, 1505.05164
 Crivellin et al, 1703.09226

Rare Decays

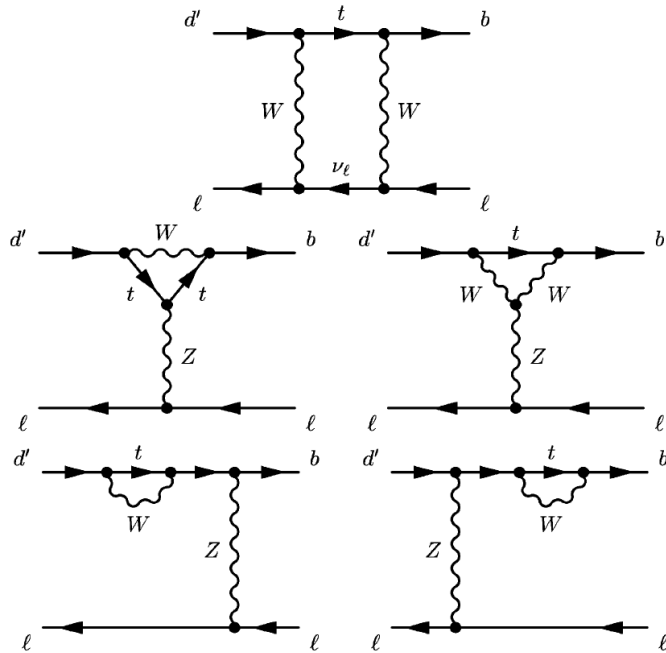
Loop & CKM suppression
 → NP sensitivity

$$B_{s,d} \rightarrow \mu^+ \mu^-$$

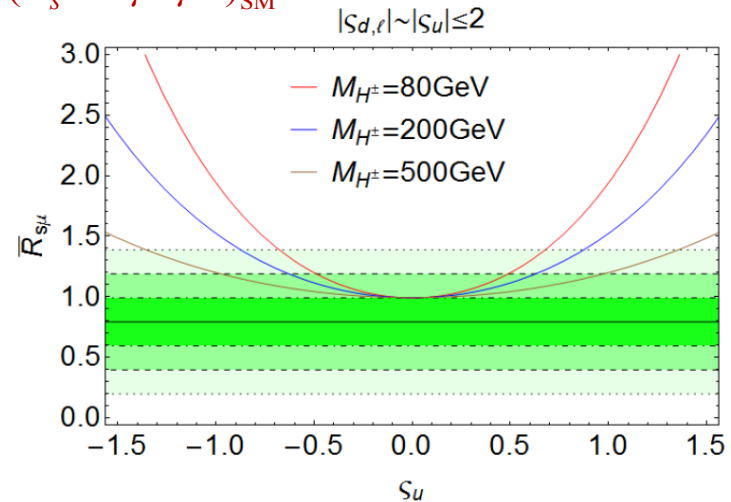
Sensitive to (pseudo) scalar contributions

$$\bar{R}_{s\mu} \equiv \frac{\bar{B}(B_s^0 \rightarrow \mu^+ \mu^-)}{\bar{B}(B_s^0 \rightarrow \mu^+ \mu^-)_{\text{SM}}}$$

Li-Lu-Pich, 1404.5865



$$W^\pm \leftrightarrow H^\pm, \quad Z \leftrightarrow H^0, A^0$$



$$\bar{B}(B_q^0 \rightarrow \mu^+ \mu^-) = \frac{1 + A_{\Delta\Gamma}^{\ell\ell} y_q}{1 - y_q^2} \text{Br}(B_q^0 \rightarrow \mu^+ \mu^-)$$

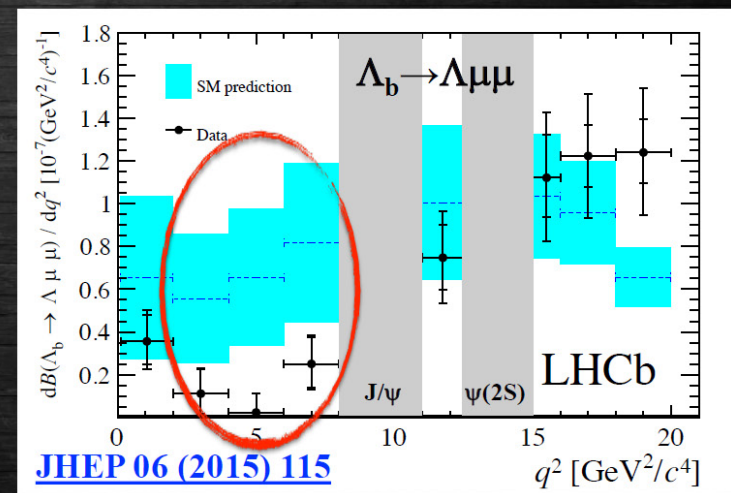
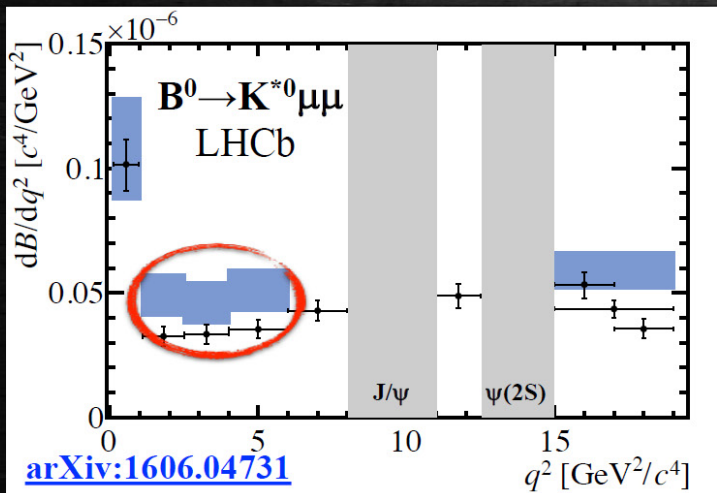
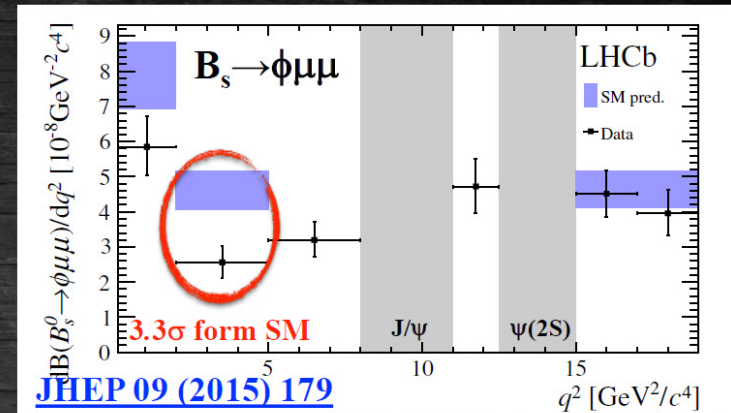
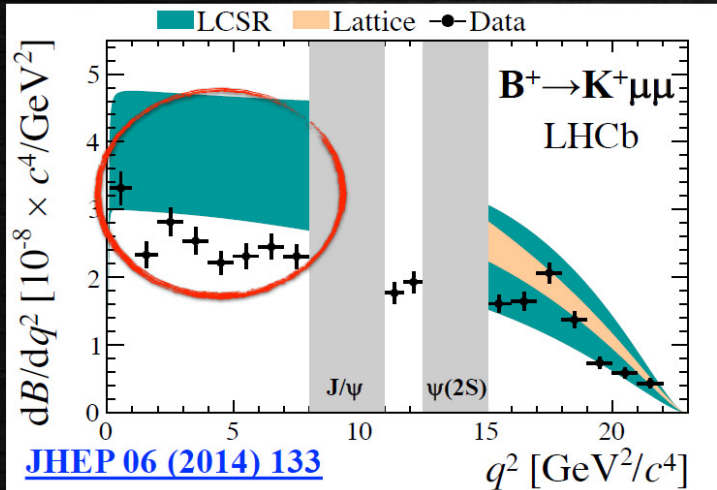
LHCb, 1703.05747: $\bar{B}(B_s^0 \rightarrow \mu^+ \mu^-)_{\text{exp}} = (3.0 \pm 0.6^{+0.3}_{-0.2}) \cdot 10^{-9}$, $\bar{B}(B_d^0 \rightarrow \mu^+ \mu^-)_{\text{exp}} < 3.4 \cdot 10^{-10}$ (95% CL)

[SM: $(3.65 \pm 0.23) \cdot 10^{-9}$] [SM: $(1.06 \pm 0.09) \cdot 10^{-10}$]

LHCb, 1703.02528: $\bar{B}(B_s^0 \rightarrow \tau^+ \tau^-)_{\text{exp}} < 6.8 \cdot 10^{-3}$, $\bar{B}(B_d^0 \rightarrow \tau^+ \tau^-)_{\text{exp}} < 2.1 \cdot 10^{-3}$ (95% CL)

$b \rightarrow s \mu^+ \mu^-$ Differential Branching Ratios

> Results consistently lower than SM predictions



$B^0 \rightarrow K^{*0} \mu^+ \mu^- \rightarrow K^+ \pi^- \mu^+ \mu^-$

$$\frac{1}{d\Gamma/dq^2 d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right.$$

$$- F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi$$

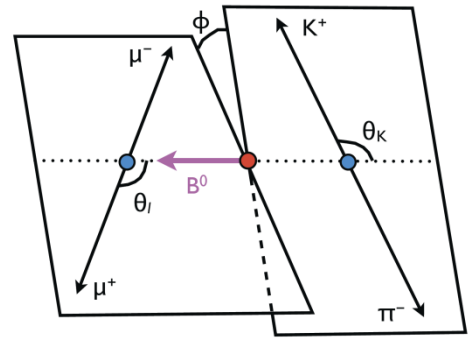
$$+ S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi$$

$$+ S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi$$

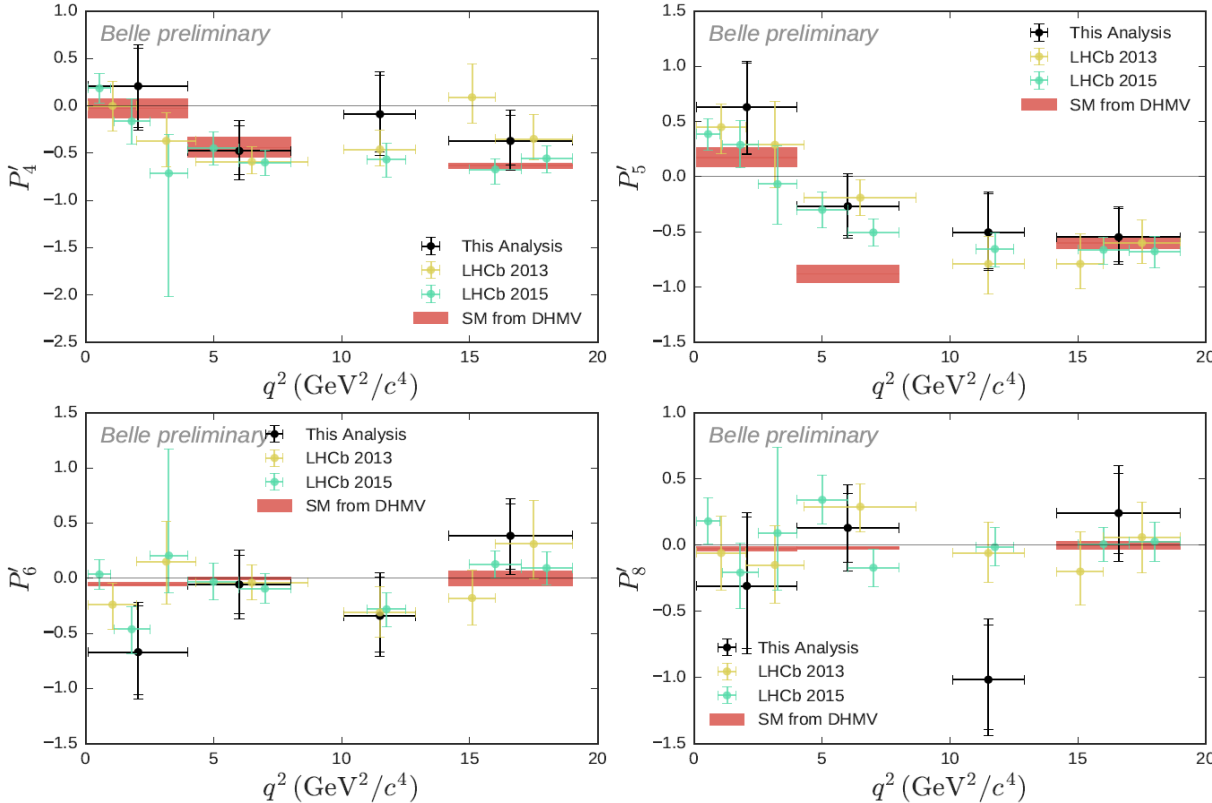
$$\left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

$$q^2 = s_{\mu^+ \mu^-}$$

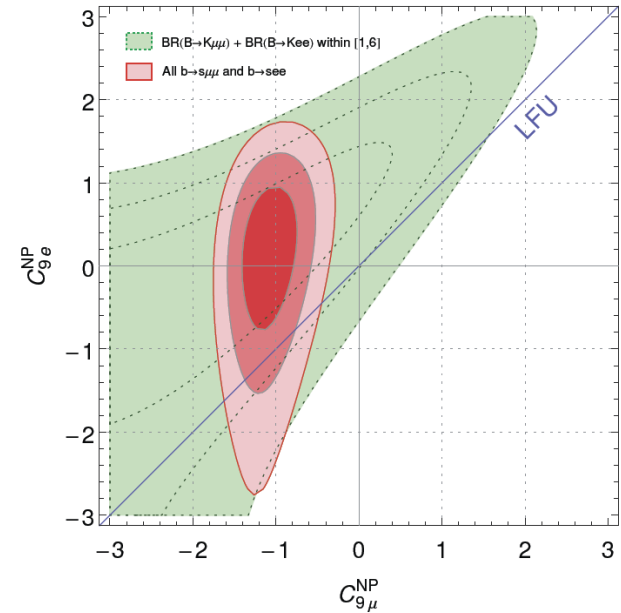
$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$



Belle 1604.04042

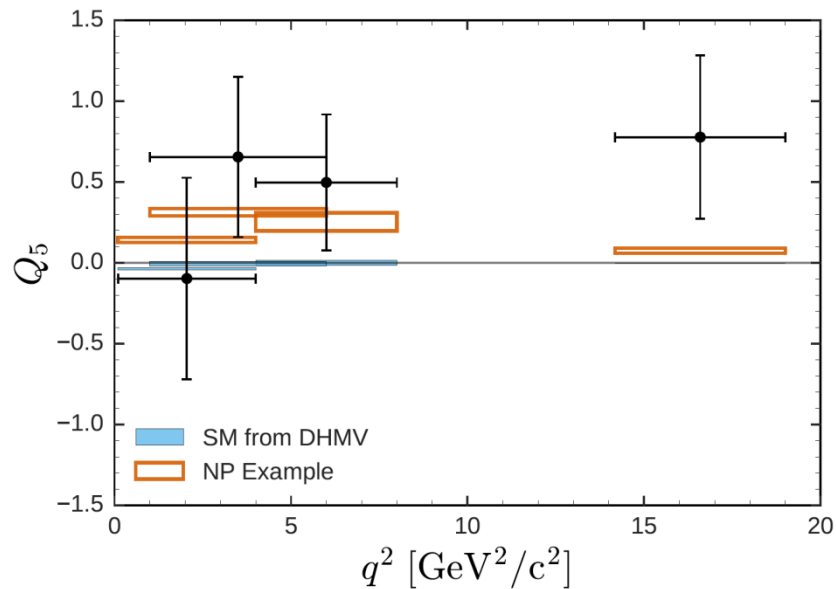
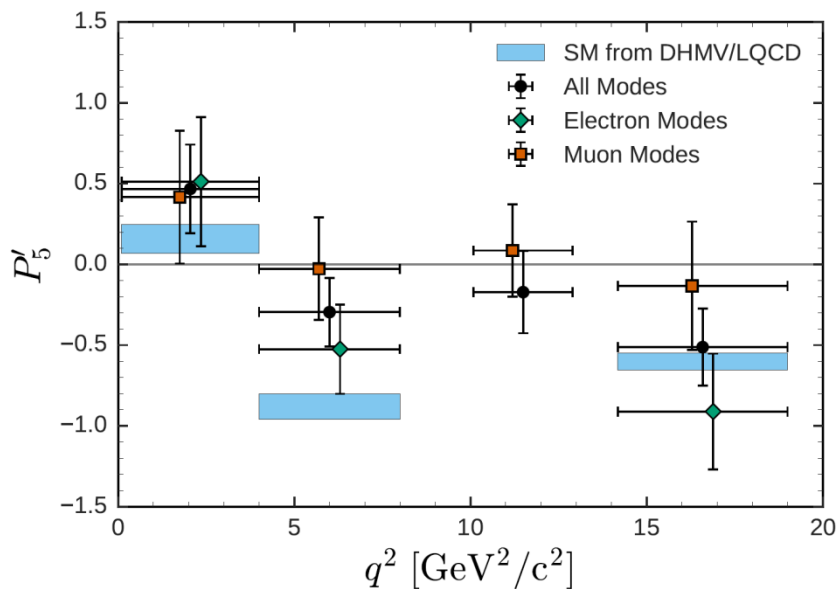
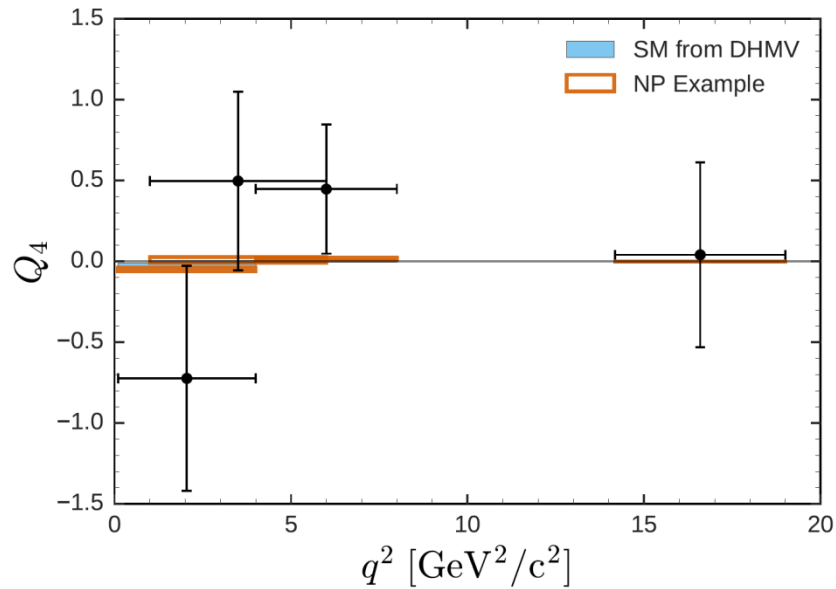
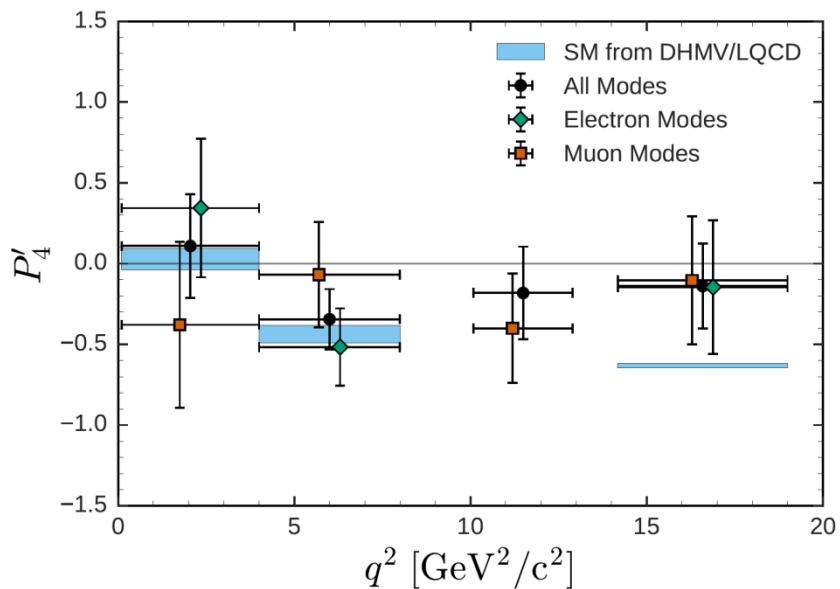


Descotes-Genon et al, 1510.04239



$$O_9 = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell)$$

$$Q_i \equiv P_i^{\mu} - P_i^e$$

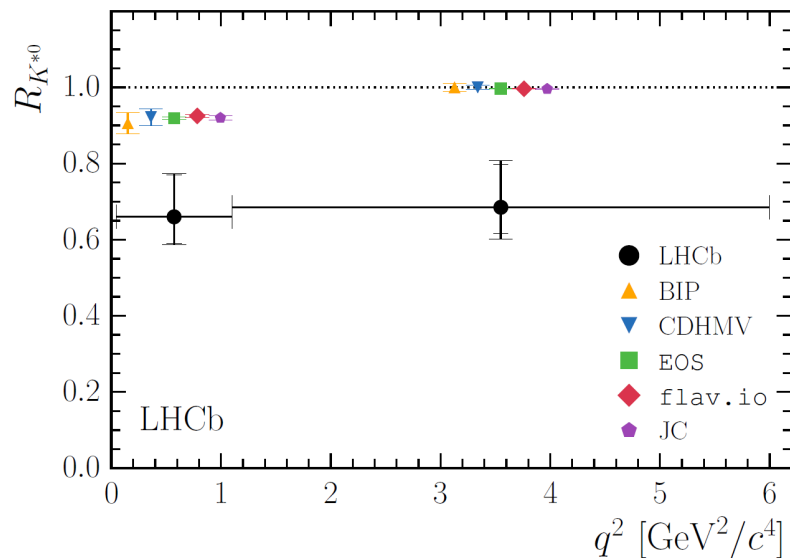


Violations of Lepton Flavour

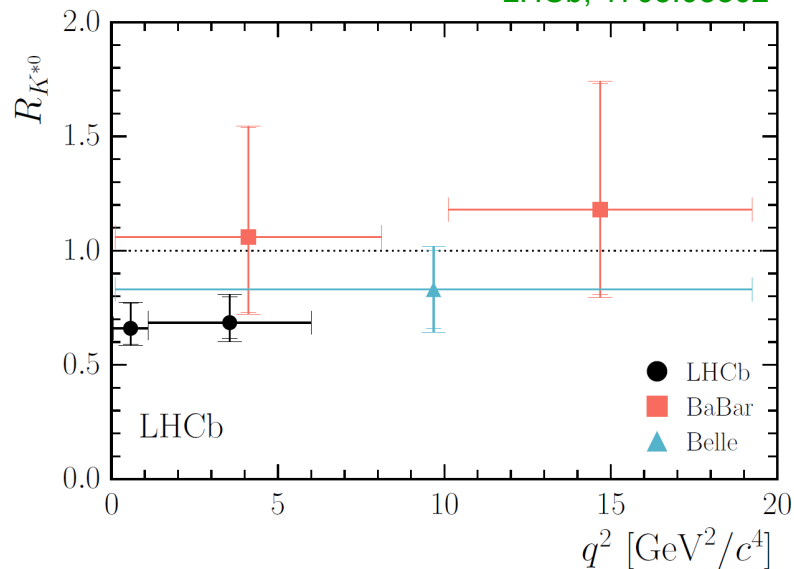
$$R_{K^{*0}} = \frac{\text{Br}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{\text{Br}(B^0 \rightarrow K^{*0} J/\psi (\rightarrow \mu^+ \mu^-))} \bigg/ \frac{\text{Br}(B^0 \rightarrow K^{*0} e^+ e^-)}{\text{Br}(B^0 \rightarrow K^{*0} J/\psi (\rightarrow e^+ e^-))}$$

	low- q^2	central- q^2
$R_{K^{*0}}$	$0.66 \pm_{-0.07}^{+0.11} \pm 0.03$	$0.69 \pm_{-0.07}^{+0.11} \pm 0.05$
95.4% CL	[0.52, 0.89]	[0.53, 0.94]
99.7% CL	[0.45, 1.04]	[0.46, 1.10]

2.1 – 2.5 σ deviation from SM



LHCb, 1705.05802

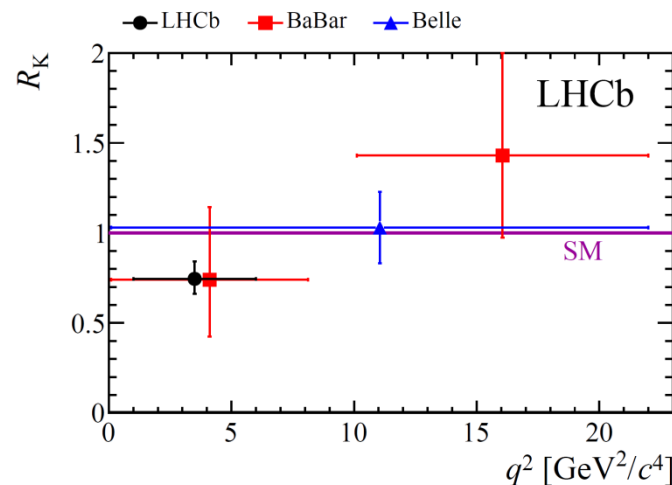


LHCb: 1406.6482

($q^2 \in [1, 6] \text{ GeV}^2$)

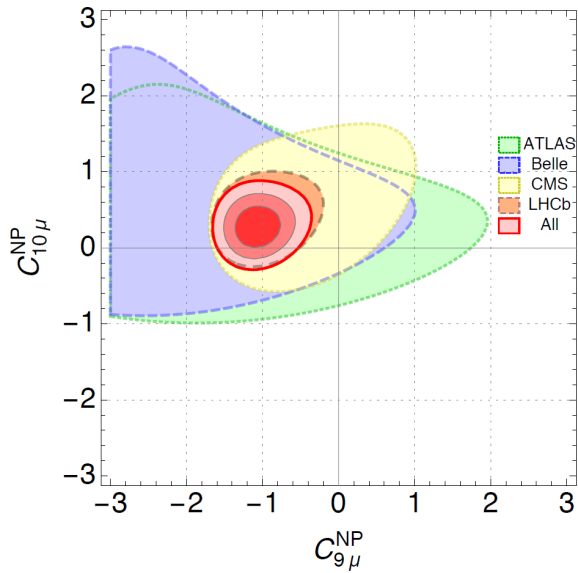
$$\frac{\text{Br}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\text{Br}(B^+ \rightarrow K^+ e^+ e^-)} = 0.745 \pm_{-0.074}^{+0.090} \pm 0.036$$

2.6 σ below the SM

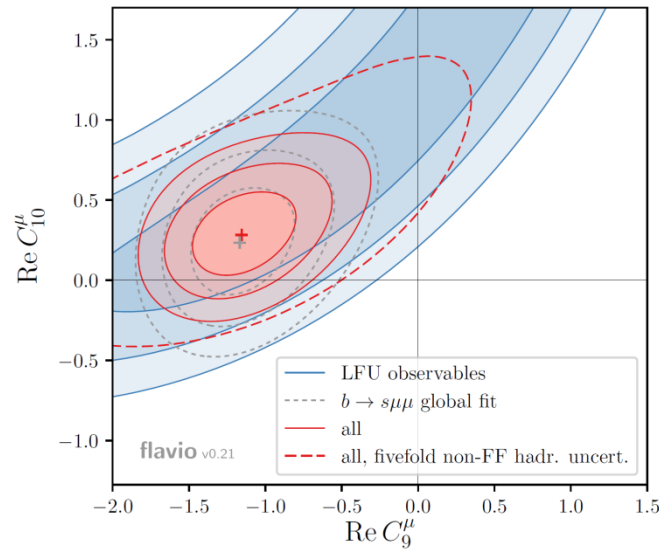


New-Physics Fits with Effective Operators

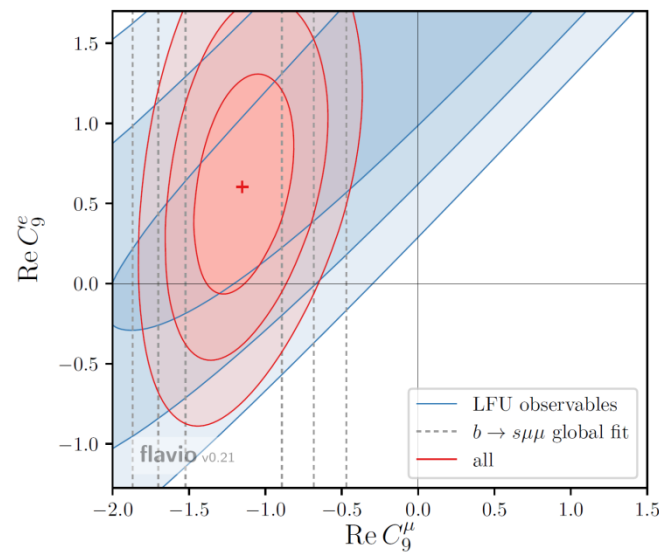
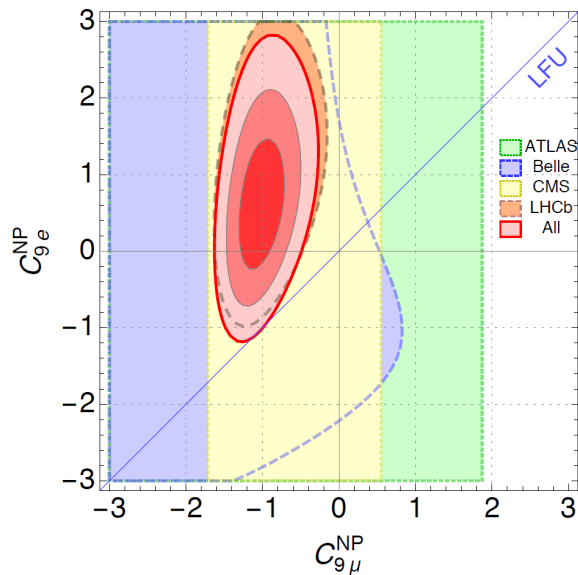
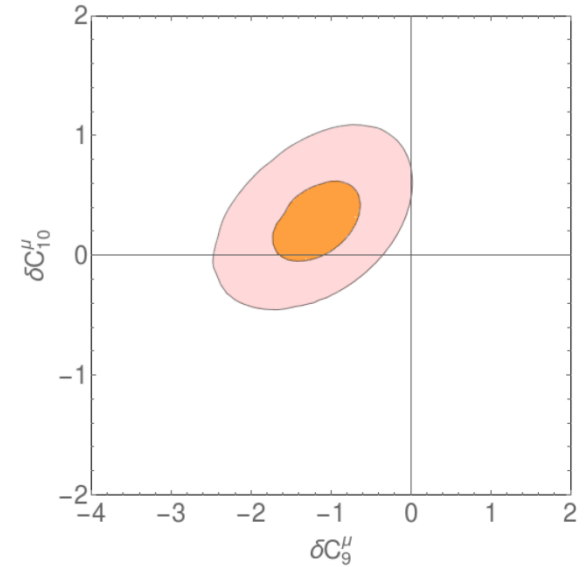
Capdevila et al, 1704.05340



Altmannshofer et al, 1704.05435



Geng et al, 1704.05446



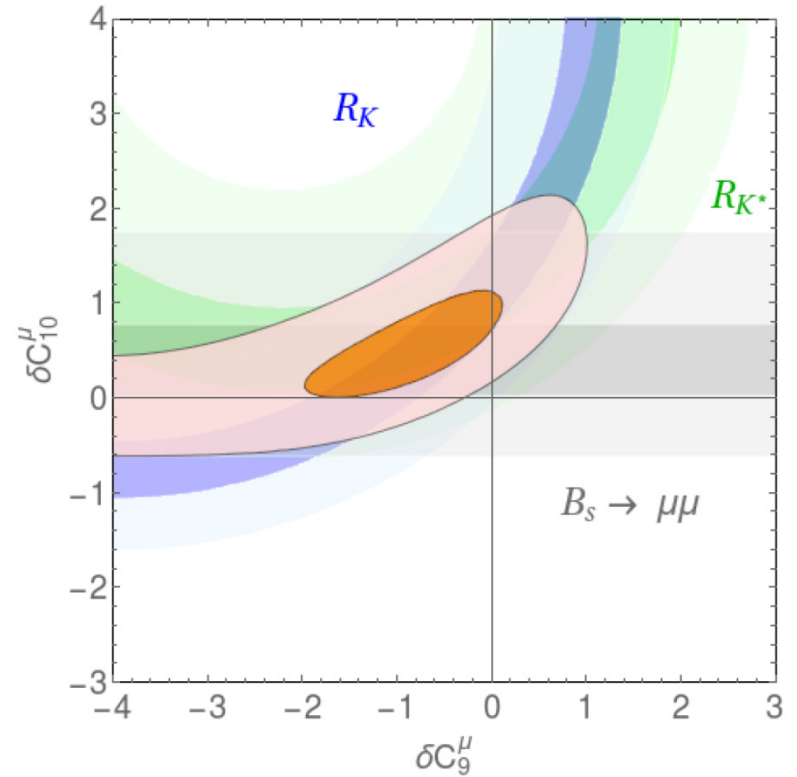
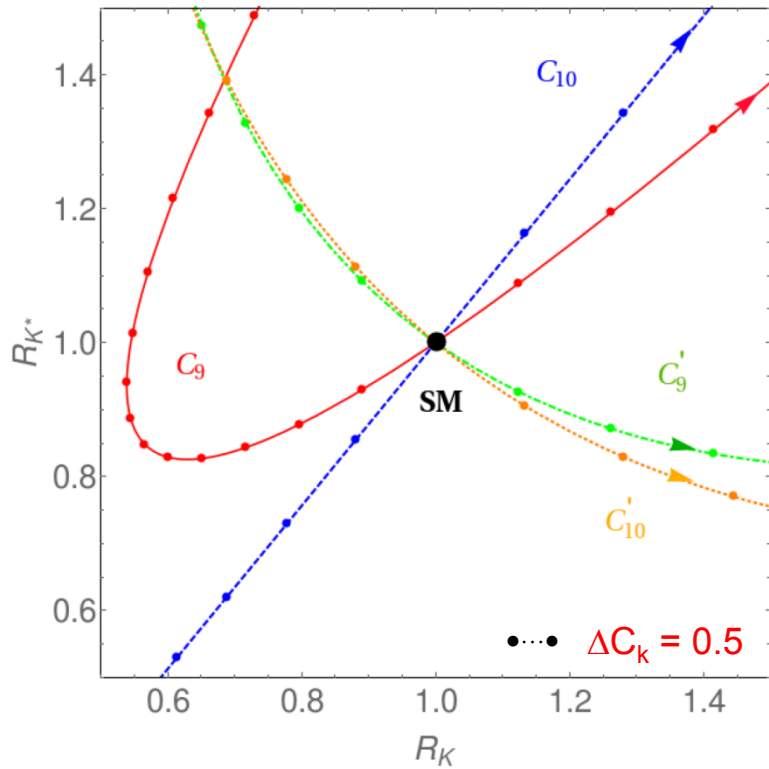
$$C_9^\mu - C_9^e - C_{10}^\mu + C_{10}^e \approx -1.4$$

$$H_{\text{eff}}^{\text{NP}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha}{4\pi} \sum_{i,\ell} C_i^\ell O_i^\ell$$

$$O_9^\ell = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell)$$

$$O_{10}^\ell = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

SM: $C_9(m_b) \approx -C_{10}(m_b) = 4.27$

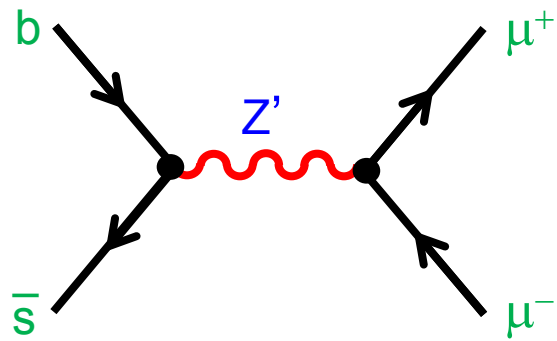


$$O_9^\ell = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell)$$

$$O_{10}^\ell = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

$$O_9^{\prime\ell} = (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \ell)$$

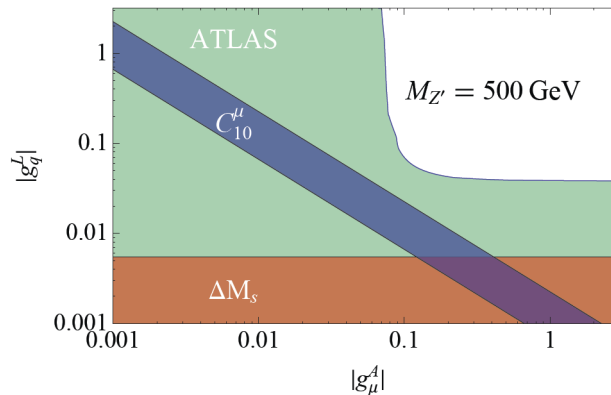
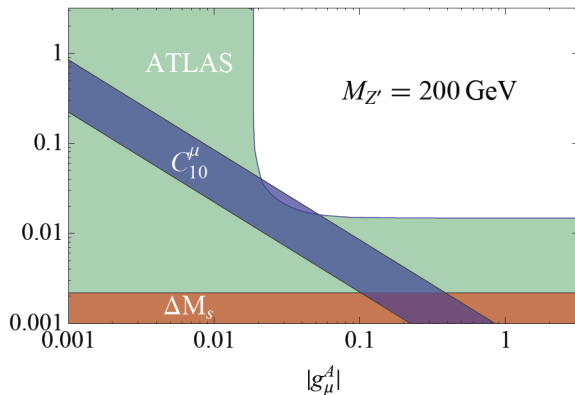
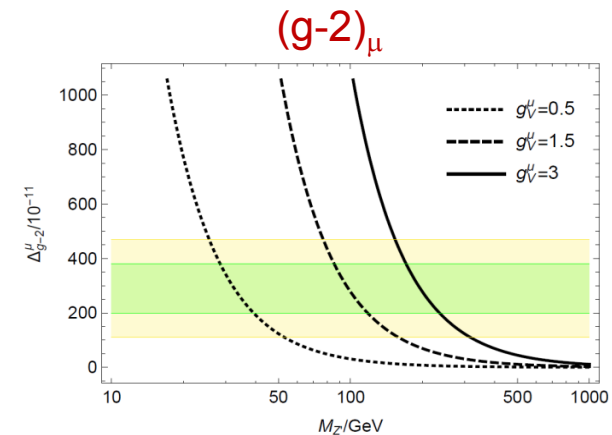
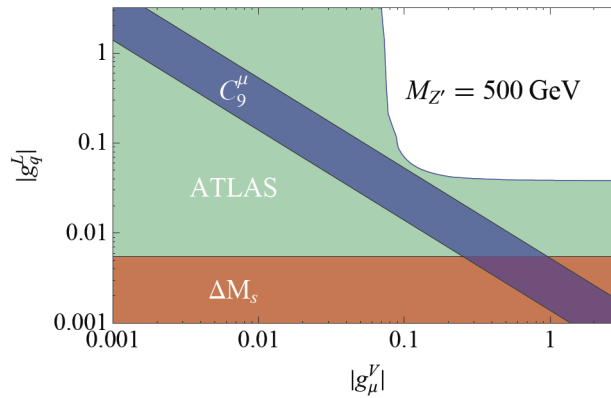
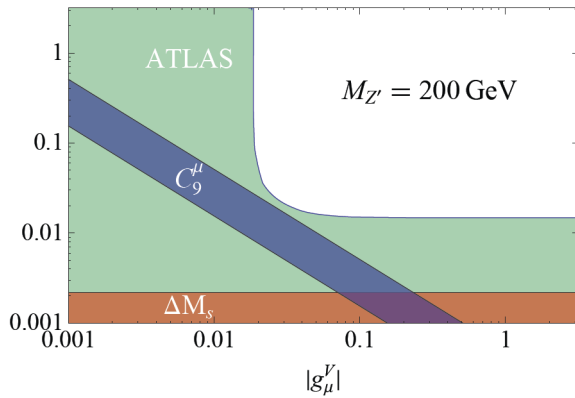
$$O_{10}^{\prime\ell} = (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$



$$\mathcal{L} \supset \frac{g_2}{2c_W} Z'_\alpha \left\{ \left[\bar{s} \gamma^\alpha (g_L^Q P_L + g_R^Q P_R) b + h.c. \right] + \bar{\ell} \gamma^\alpha (g_V^\ell + \gamma_5 g_A^\ell) \ell \right\}$$

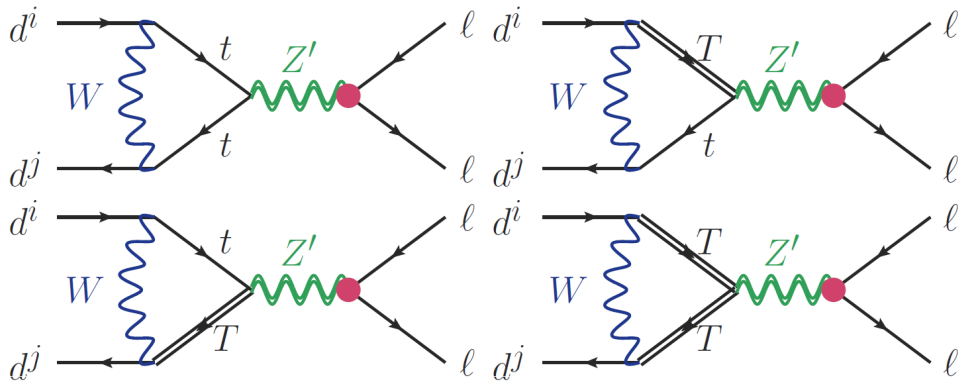


$$\frac{e^2}{16\pi^2} V_{tb} V_{ts}^* \cdot \left\{ C_9^\mu, C_{10}^\mu \right\} = \frac{M_{Z'}^2}{2m_{Z'}^2} \cdot \left\{ g_L^Q g_V^\ell, g_L^Q g_A^\ell \right\}$$



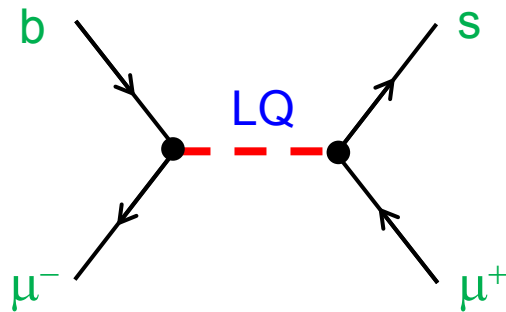
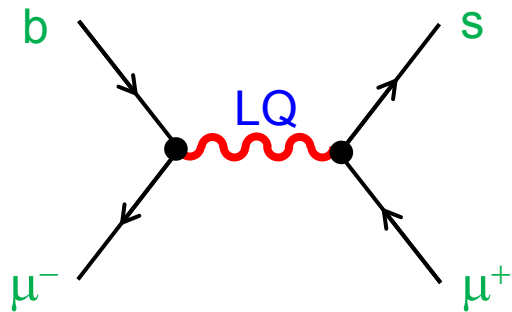
Di Chiara et al, 1704.06200

More possibilities...



Flavour conserving Z'

Kamenik et al, 1704.06005

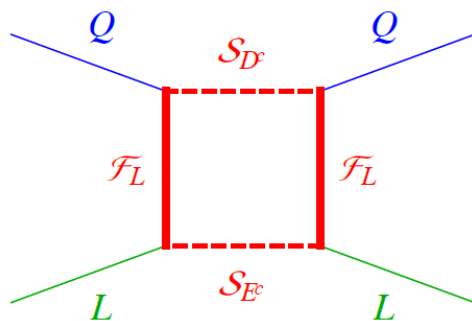


Leptoquarks

Hiller- Nisandzic, 1704.05444

D'Amico et al, 1704.05438

Becirevic-Sumensari, 1704.05835

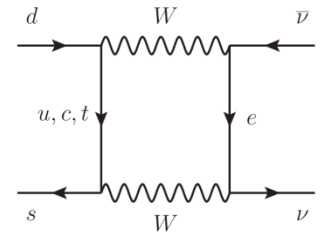
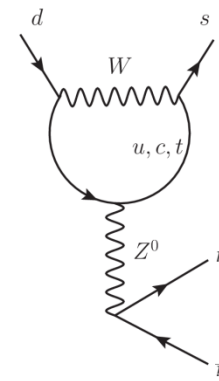


New Fermions and Scalars

D'Amico et al, 1704.05438

$$K \rightarrow \pi \nu \bar{\nu}$$

$$\mathbf{T} \sim F(V_{is}^* V_{id}, m_i^2/M_W^2) (\bar{\nu}_L \gamma_\mu \nu_L) \langle \pi | \bar{s}_L \gamma_\mu d_L | K \rangle$$



$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (7.8 \pm 0.8) \times 10^{-11} \sim A^4 [\eta^2 + (1.4 - \rho)^2]$$

$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (2.4 \pm 0.4) \times 10^{-11} \sim A^4 \eta^2$$

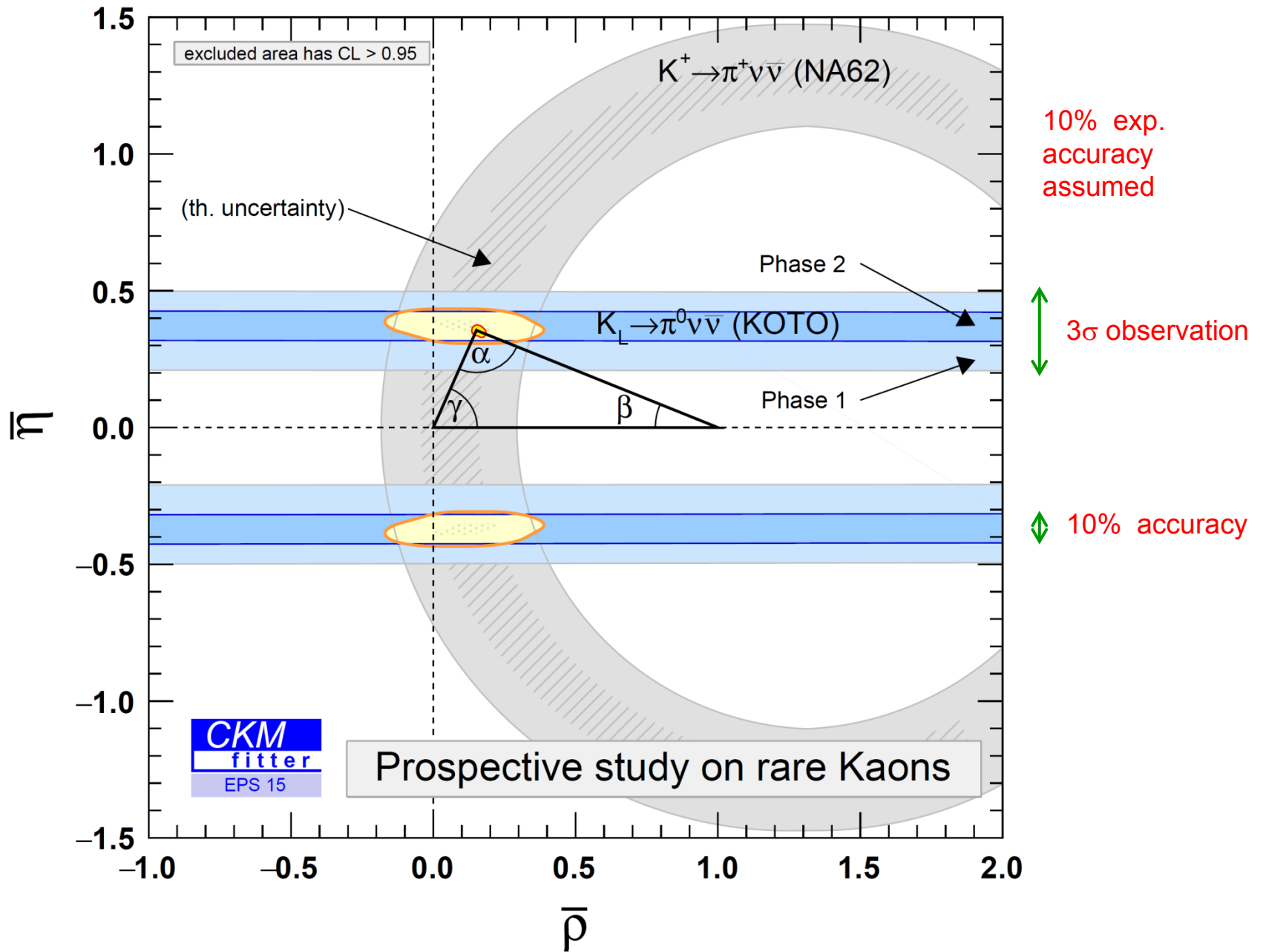
Buras et al

Long-distance contributions are negligible


$$\mathbf{T}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \neq 0 \quad \longrightarrow \quad \cancel{CP}$$

- BNL-E949: few events! \longrightarrow $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (1.73^{+1.15}_{-1.05}) \cdot 10^{-10}$
- KEK-E391a: $\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 2.6 \times 10^{-8}$ (90% C.L.)

New Experiments Needed: NA62, KOTO (ORKA, Project-X)



SUMMARY

- **Flavour Structure and CP** are major pending questions
- **Related to SSB**  **Scalar Sector (Higgs)**
- Important **cosmological implications (Baryogenesis)**
- Sensitive to **New Physics: Flavour Anomalies!**
- CP is highly constrained in the SM: **1 phase only**
- Many interesting CP signals within experimental reach
- Better control of **QCD** effects urgently needed
- **Challenging future ahead:**
BES-III, LHCb, NA62, J-Parc, Super-Belle, τcF , ...