



DIPARTIMENTO
DI FISICA
E ASTRONOMIA
Galileo Galilei



Effective field theory of 3d $\mathcal{N} = 2$ CFT's from holography

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University of Padova

based on: 1803.xxxx

with Stefano Cremonesi & Stefano Lanza

18xx.xxxx

with Stefano Cremonesi

1603.04470

with Alberto Zaffaroni

A motivation:

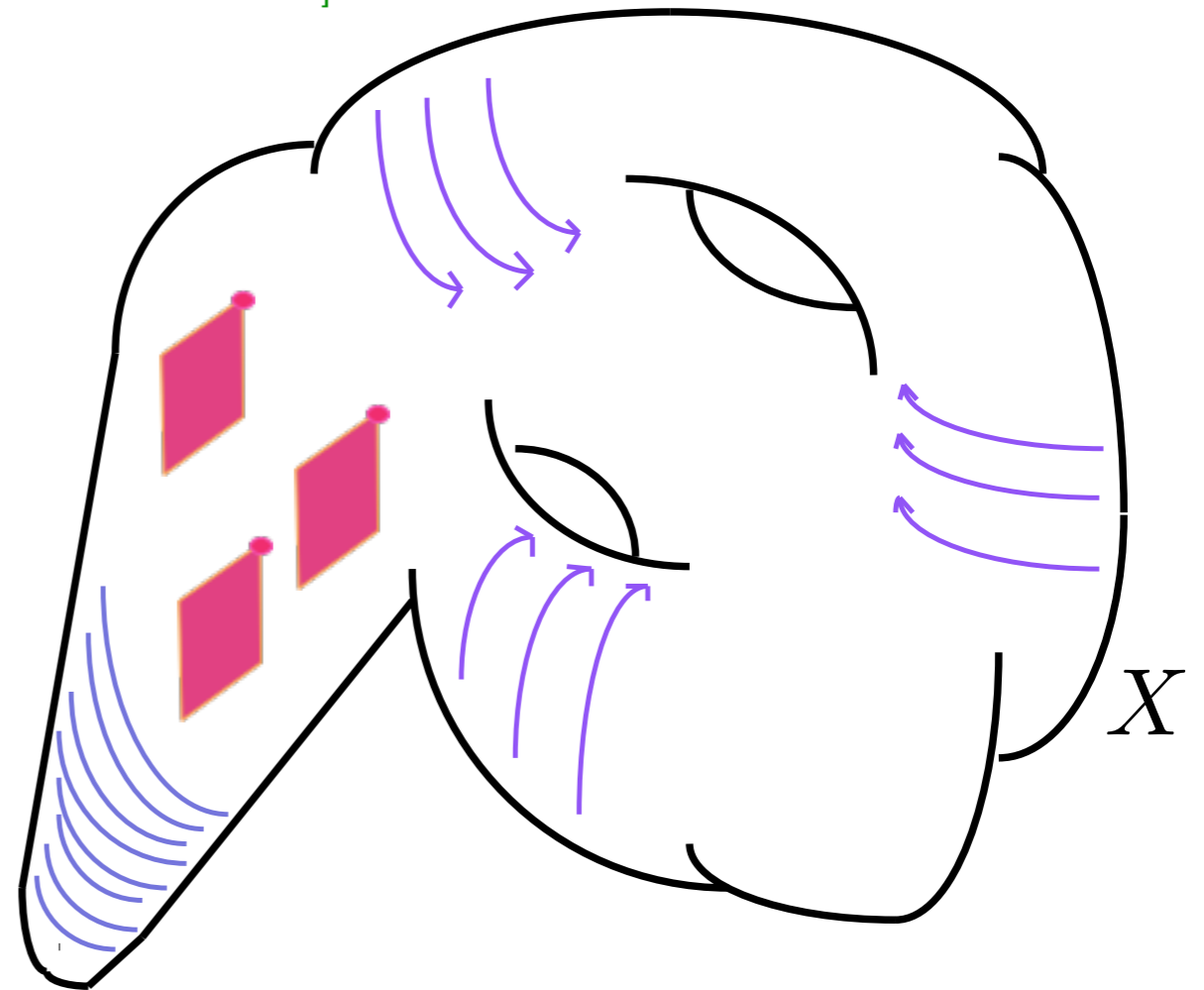
EFTs for warped compactifications?

📌 M-theory compactifications to d=3 are generically **warped**

$$ds_{11}^2 = H^{-\frac{2}{3}} ds_{\mathbb{R}^{1,2}}^2 + H^{\frac{1}{3}} ds_X^2 \quad [\text{Becker-Becker '96}]$$

warping generated by:

- * mobile M2-branes
- * G_4 -flux



📌 M/F-theory duality \rightarrow IIB warped compactifications to d=4

[Grana-Polchinski, Gubser, Giddings-Kachru-Polchinski '00]

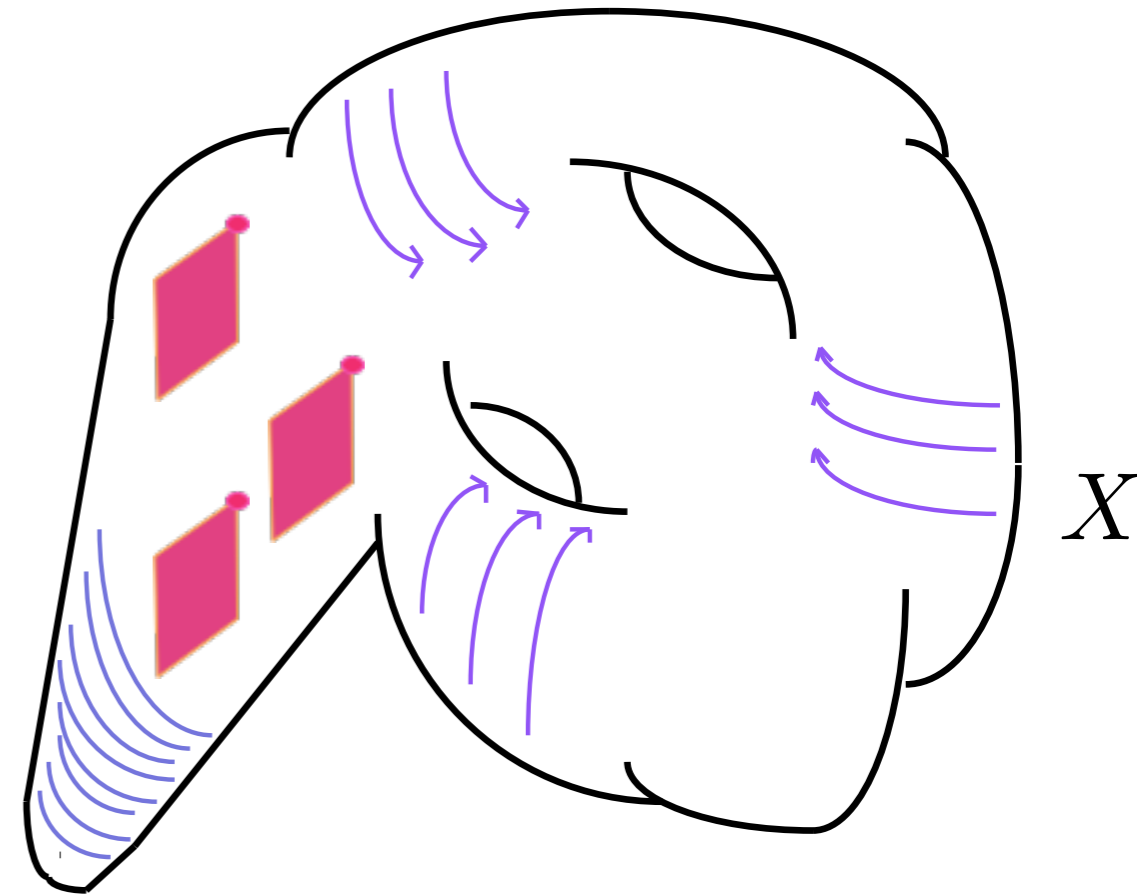
📌 Tree-level moduli space \mathcal{M} :

- * M2-brane positions
- * Kähler + axionic moduli

📌 Effective $K(\Phi, \bar{\Phi})$ explicitly depends on:

- * internal flux G_4 [LM '14-'16]
- * detailed form of the CY metric

'NON-TOPOLOGICAL' !



E.g: Kähler moduli space metric includes:

[Frey-Roberts '13] [Covnden-Frey-David Marsh-Underwood '16] [LM '16]

$$\int_X H \omega_a \wedge *_{X} \omega_b + \int_X d\Lambda_a \wedge *_{X} d\Lambda_b$$

\swarrow $\Delta_X^{-1} [*_{X} (\omega_a \wedge G_4)]$

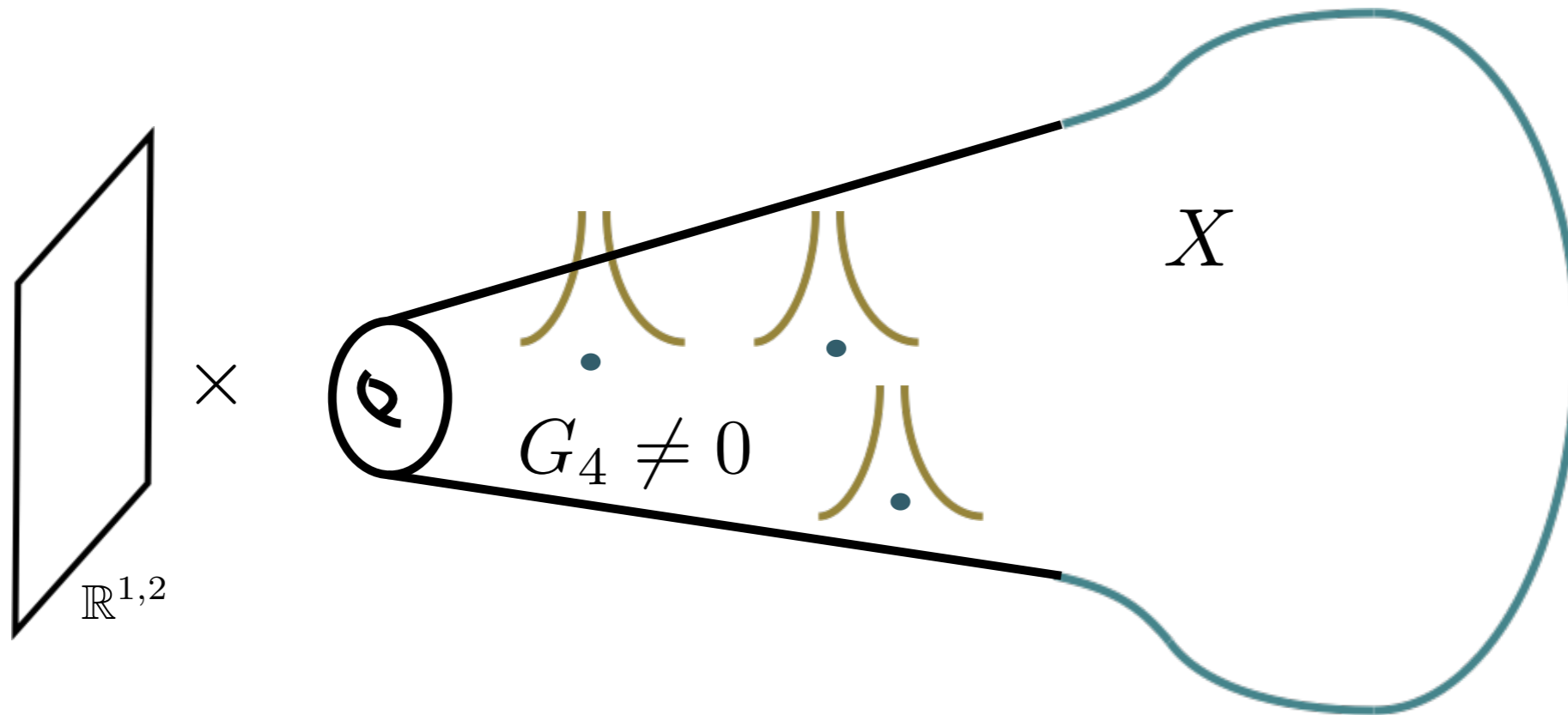
📌 Further corrections from M-theory higher derivative terms

[Grimm-Pugh-Weissenbacker '14-'15]

[Grimm-Mayer-Weissenbacker '17]

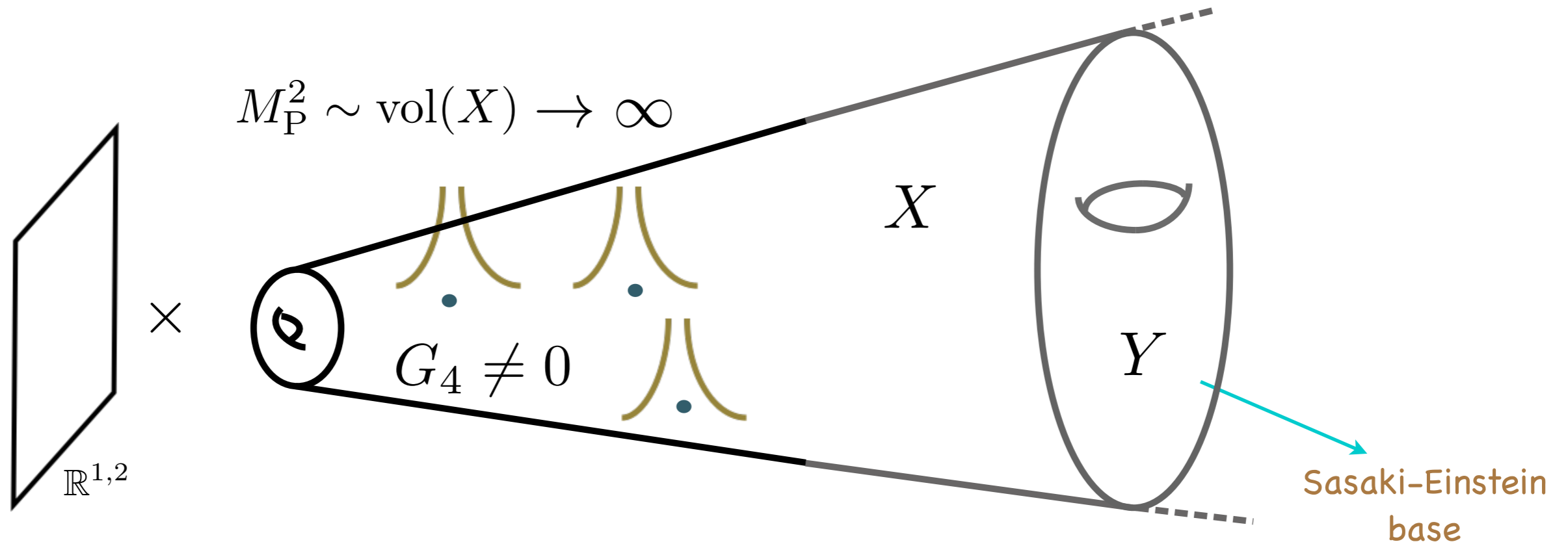
Computable EFTs?

I will consider **local models** ...



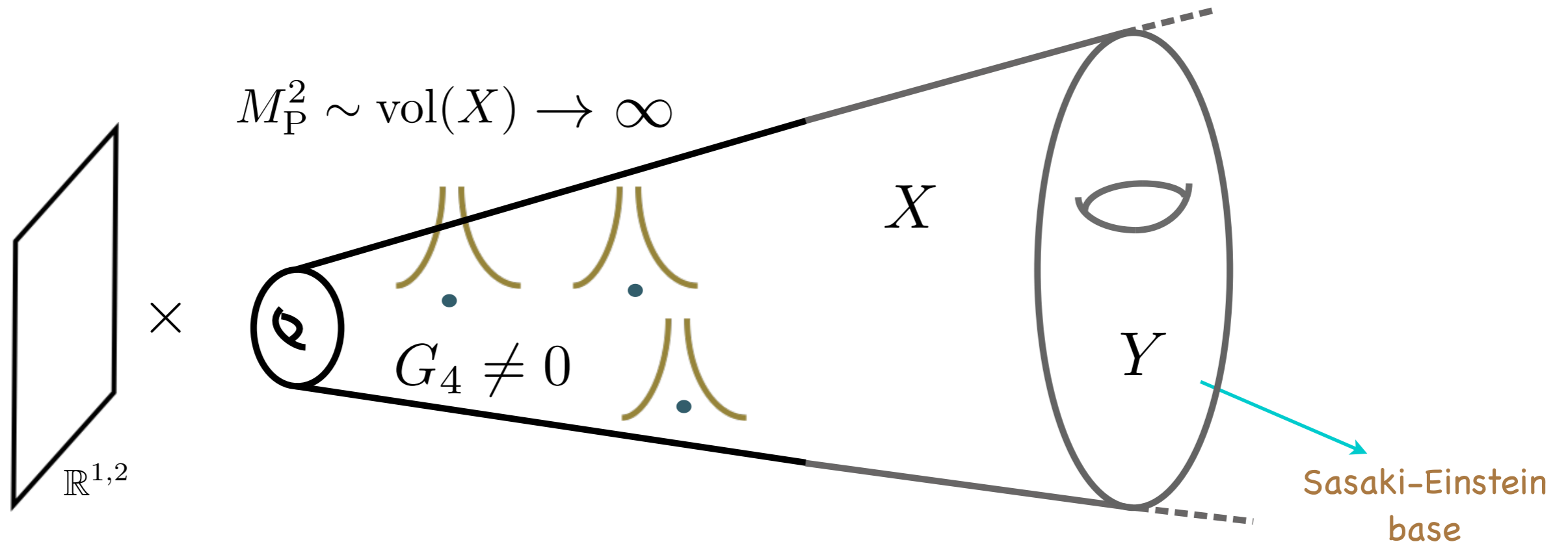
Computable EFTs?

I will consider **local models** ...



Computable EFTs?

I will consider **local models** ...



... in the **near-horizon** limit:

$$H \sim a + \frac{L^6}{r^6} \xrightarrow{a \rightarrow 0} H \sim \frac{L^6}{r^6}$$

asymptotically
 $\text{AdS}_4 \times Y$

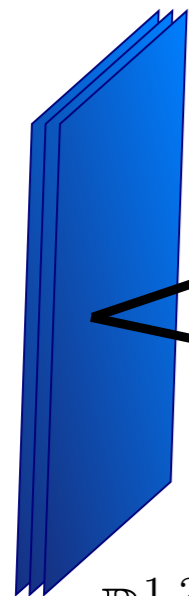


(Rigid) **holographic EFT** for dual $\mathcal{N} = 2$ CFT_3

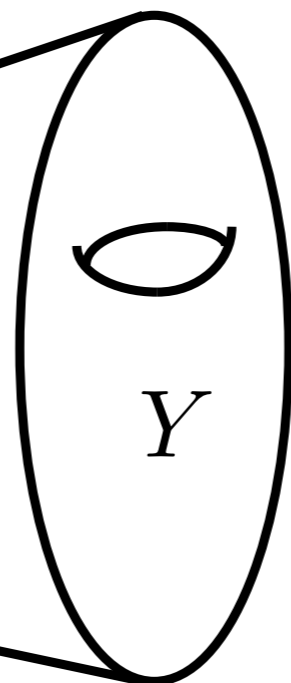
Large-N EFTs
from supergravity

Dual $\mathcal{N} = 2$ CFTs

N M2



$\mathbb{R}^{1,2}$



generalizations of
 $\mathcal{N} = 6$ ABJM theory

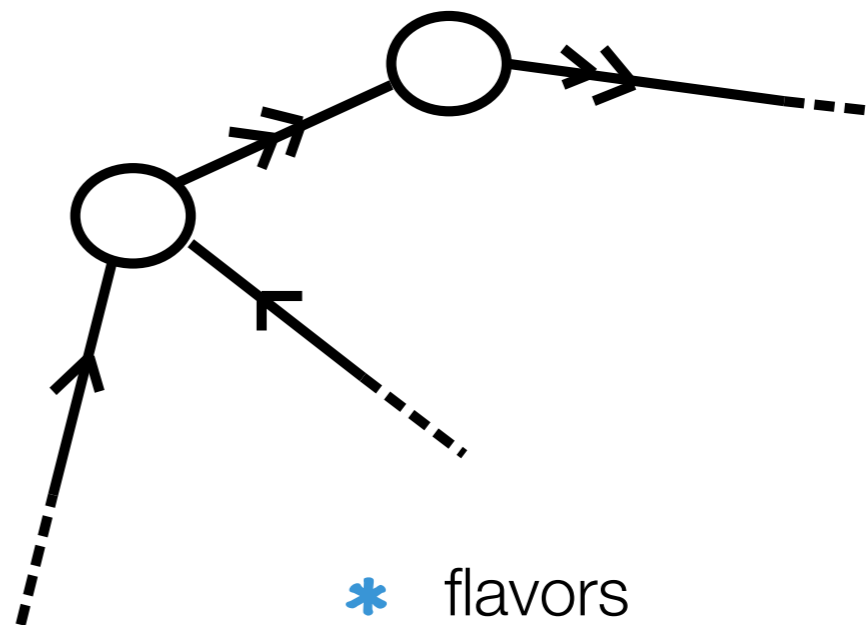
[Aharony-Bergman-Jafferis-Maldacena '08]

3d $\mathcal{N} = 2$ quiver models

RG-flow

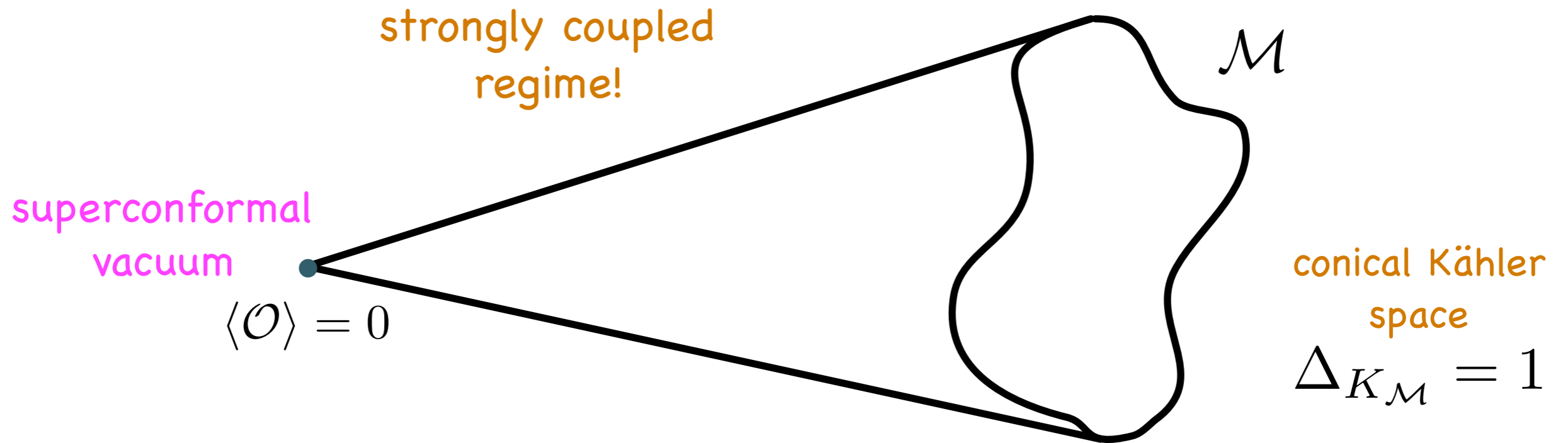
3d $\mathcal{N} = 2$ SCFTs

strongly coupled!

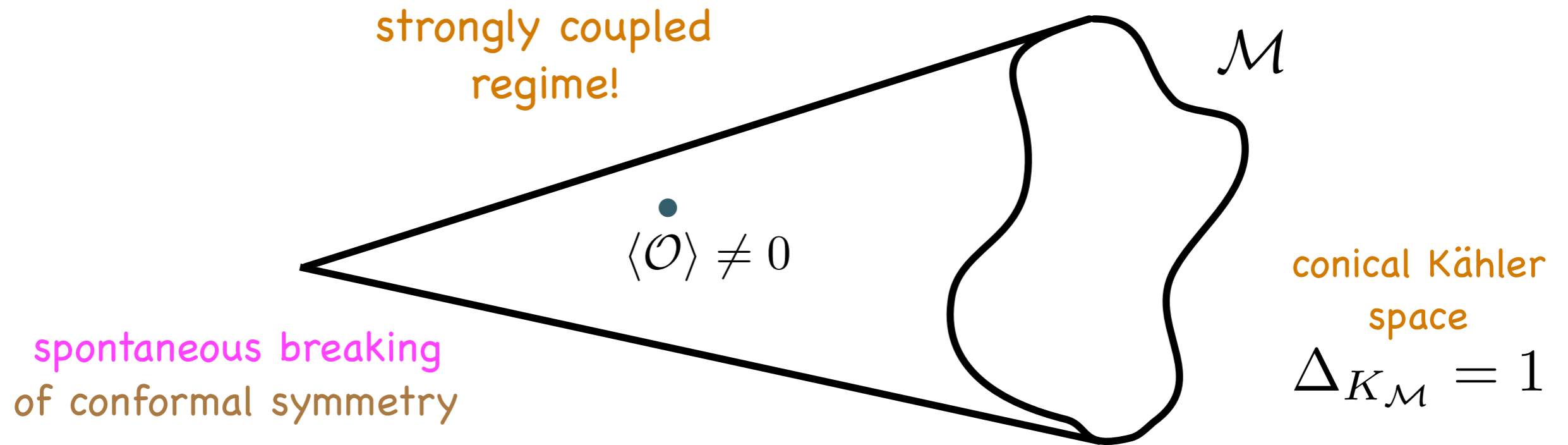


- * flavors
- * unequal ranks $\sim N$
- * monopole operators
- * non-perturbative effects

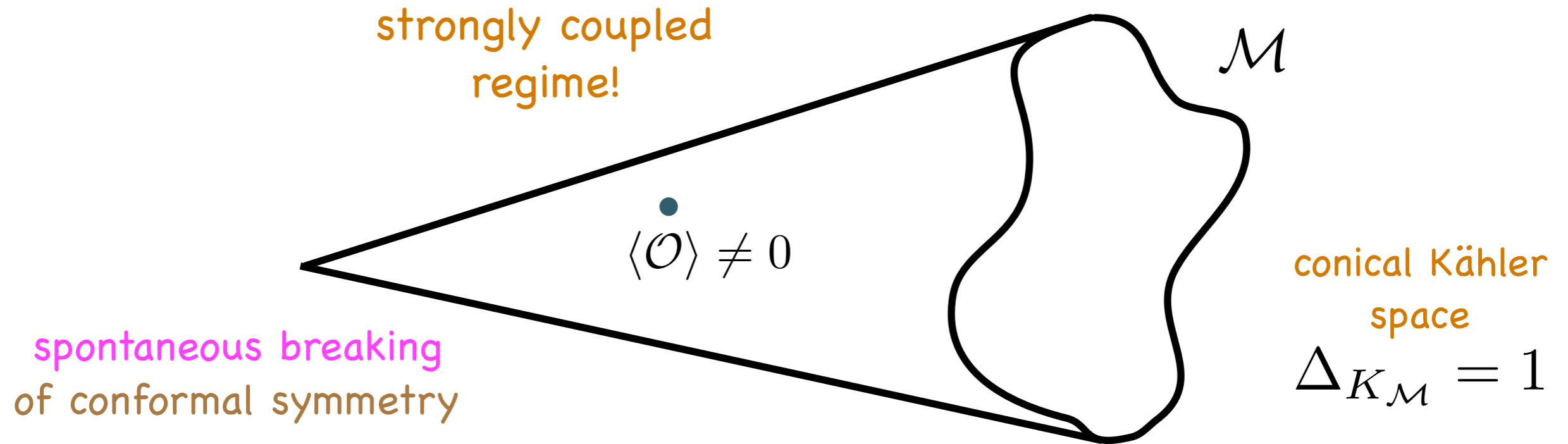
$\mathcal{N} = 2$ SCFT moduli space



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$\mathcal{N} = 2$ SCFT moduli space



📌 Complex/algebraic structure well studied

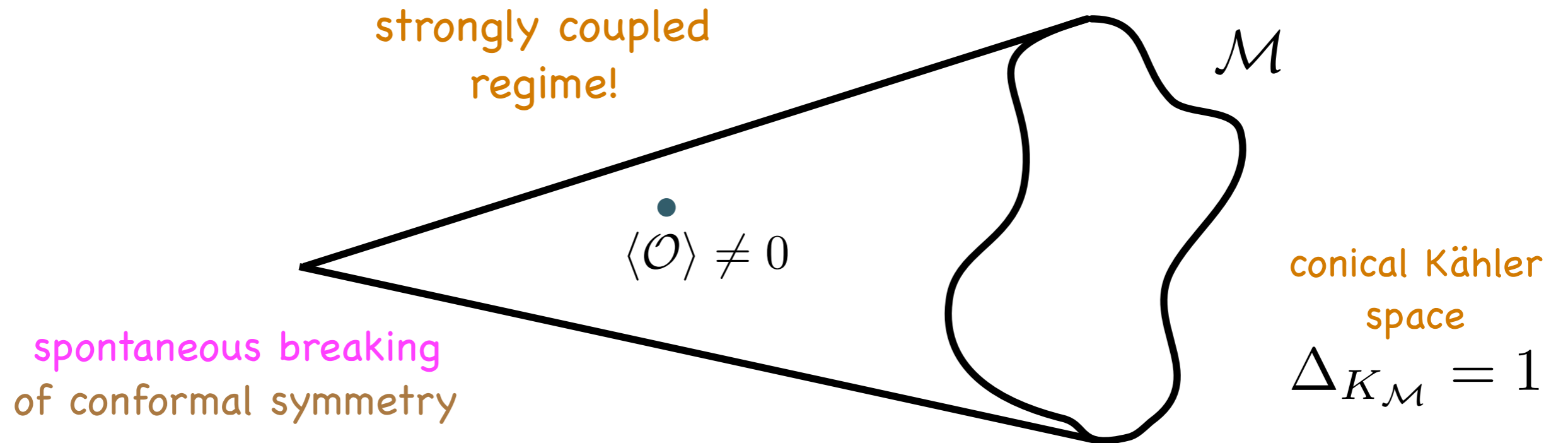
* semi-classical analysis

[De Boer-Hori-Oz '97] [Aharony-Hanany-Intriligator-Seiberg-Strassler '97] [Tong '00] ...

[Martelli-Sparks '08] [Hanany-Zaffaroni '08] [Benini-Closset-Cremonesi '13] ... [Intriligator-Seiberg '13] ...

* chiral rings and Hilbert series [Cremonesi, Hanany, Makkareya, Zaffaroni ...]

$\mathcal{N} = 2$ SCFT moduli space



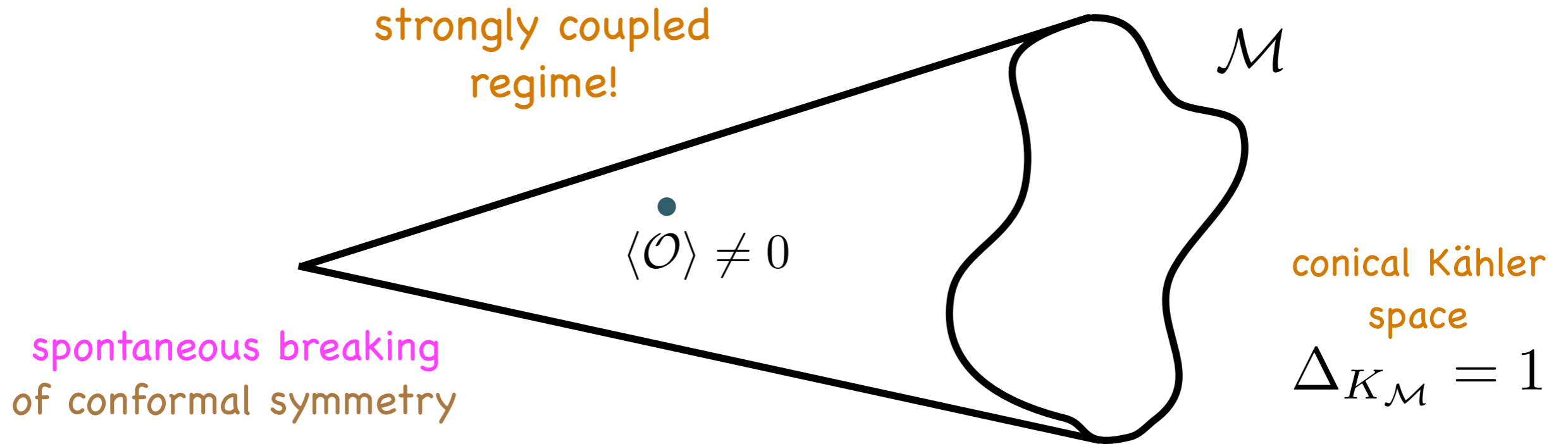
📌 Low energy EFT ?

[De Boer-Hori-Oz '97] [Aharony-Hanany-Intriligator-Seiberg-Strassler '97]
... [Intriligator-Seiberg '13] ...

$$\mathcal{L}_{\text{eff}} = \int d^4\theta K_{\mathcal{M}}(\Phi, \bar{\Phi}) = -g_{i\bar{j}}(\phi, \bar{\phi}) \partial^\mu \phi^i \partial_\mu \bar{\phi}^{\bar{j}} + \dots$$

non-protected quantity

$\mathcal{N} = 2$ SCFT moduli space



📌 Low energy EFT ?

[De Boer-Hori-Oz '97] [Aharony-Hanany-Intriligator-Seiberg-Strassler '97]
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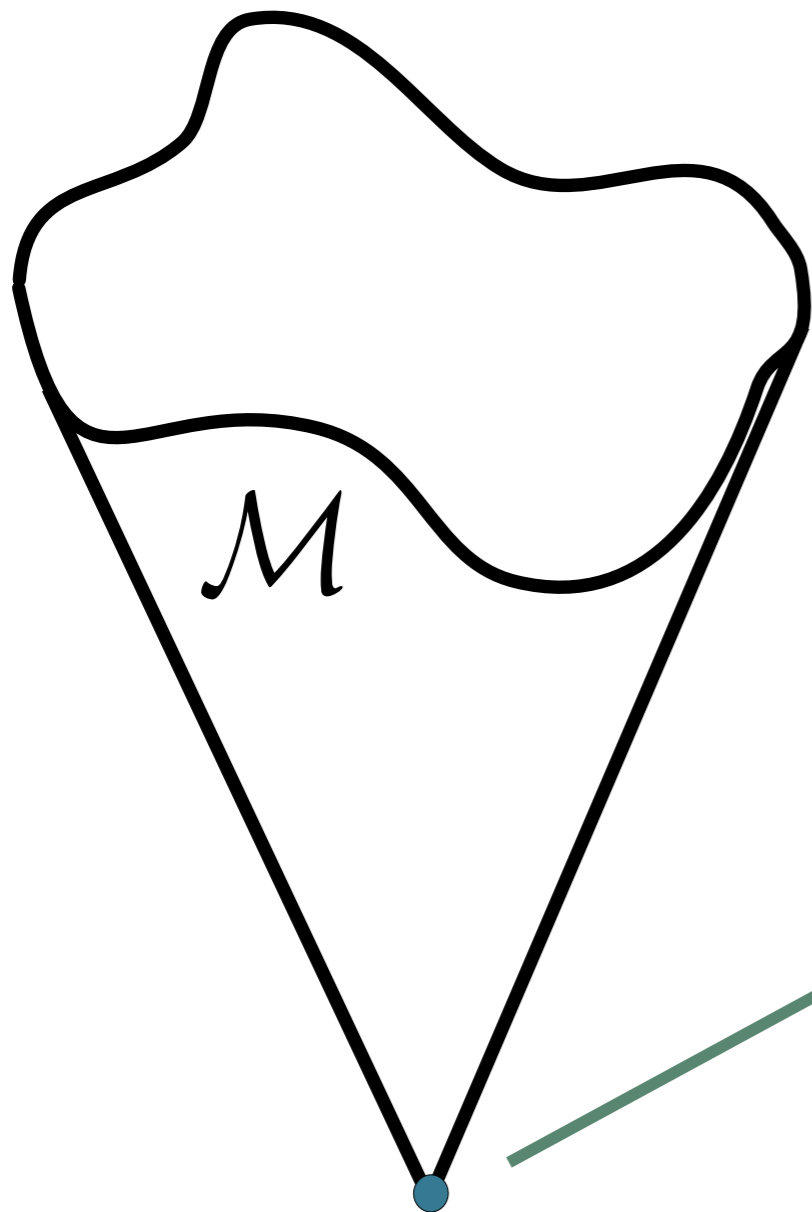
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non-protected quantity

📌 At $N \gg 1$ \longrightarrow holographic EFT from supergravity!

Computation of HEFT

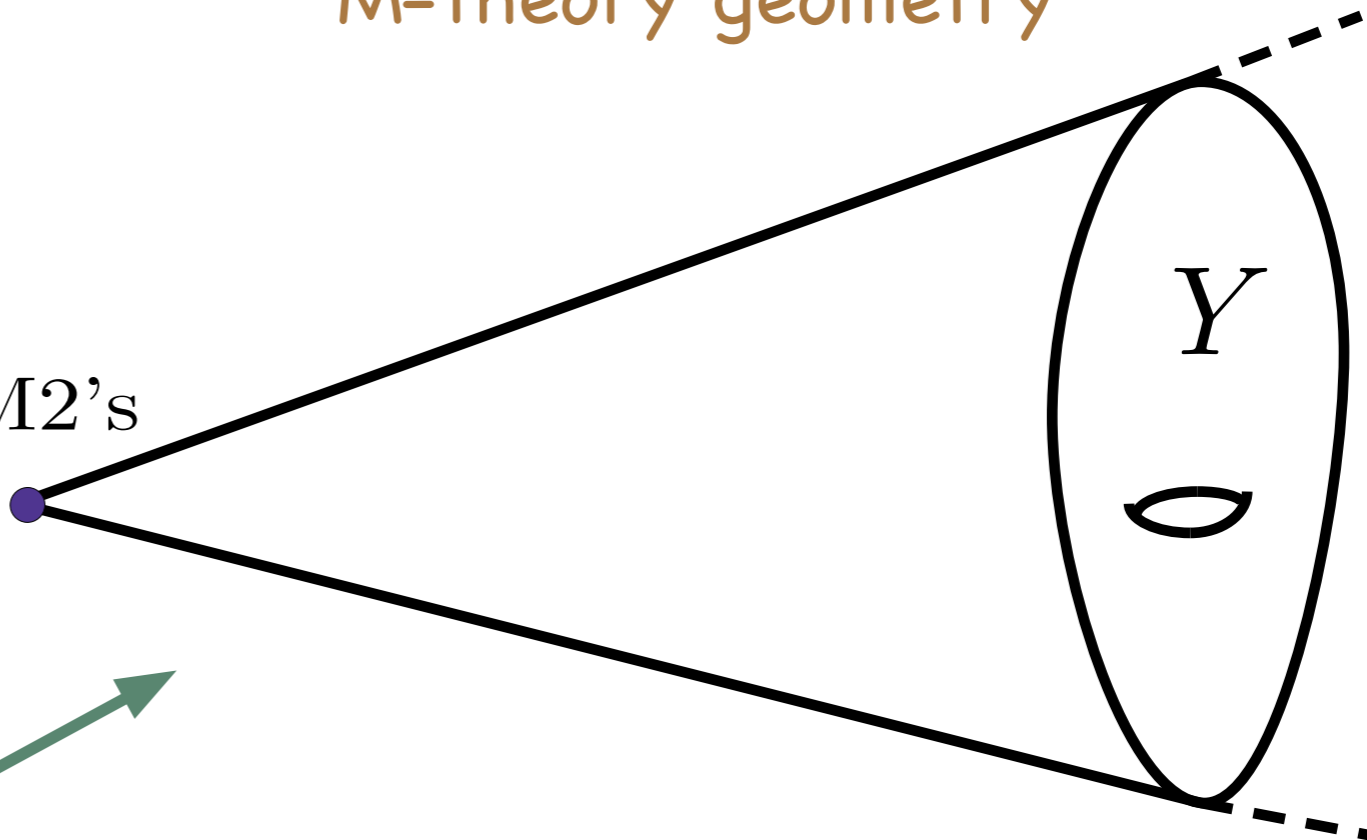
CFT moduli space
(geometric branch)



$\langle \mathcal{O} \rangle = 0$ superconformal vacuum

M-theory geometry

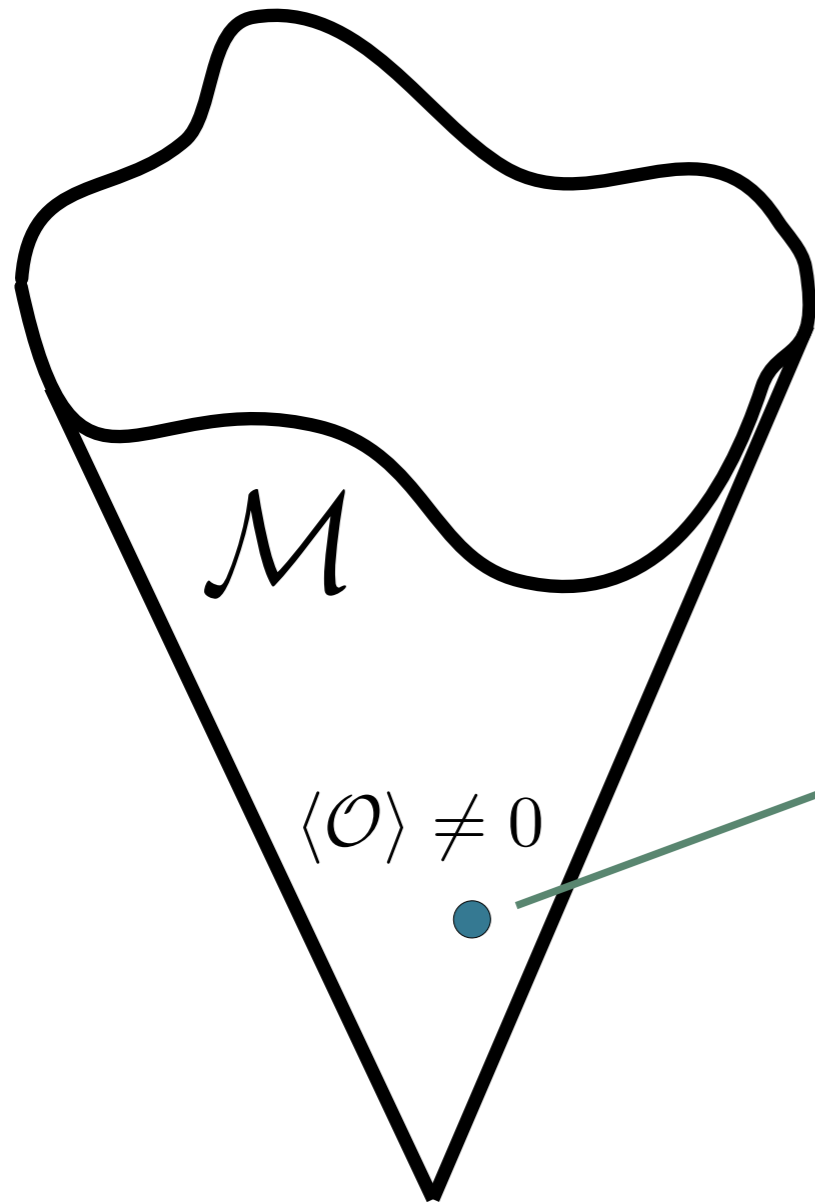
M2's



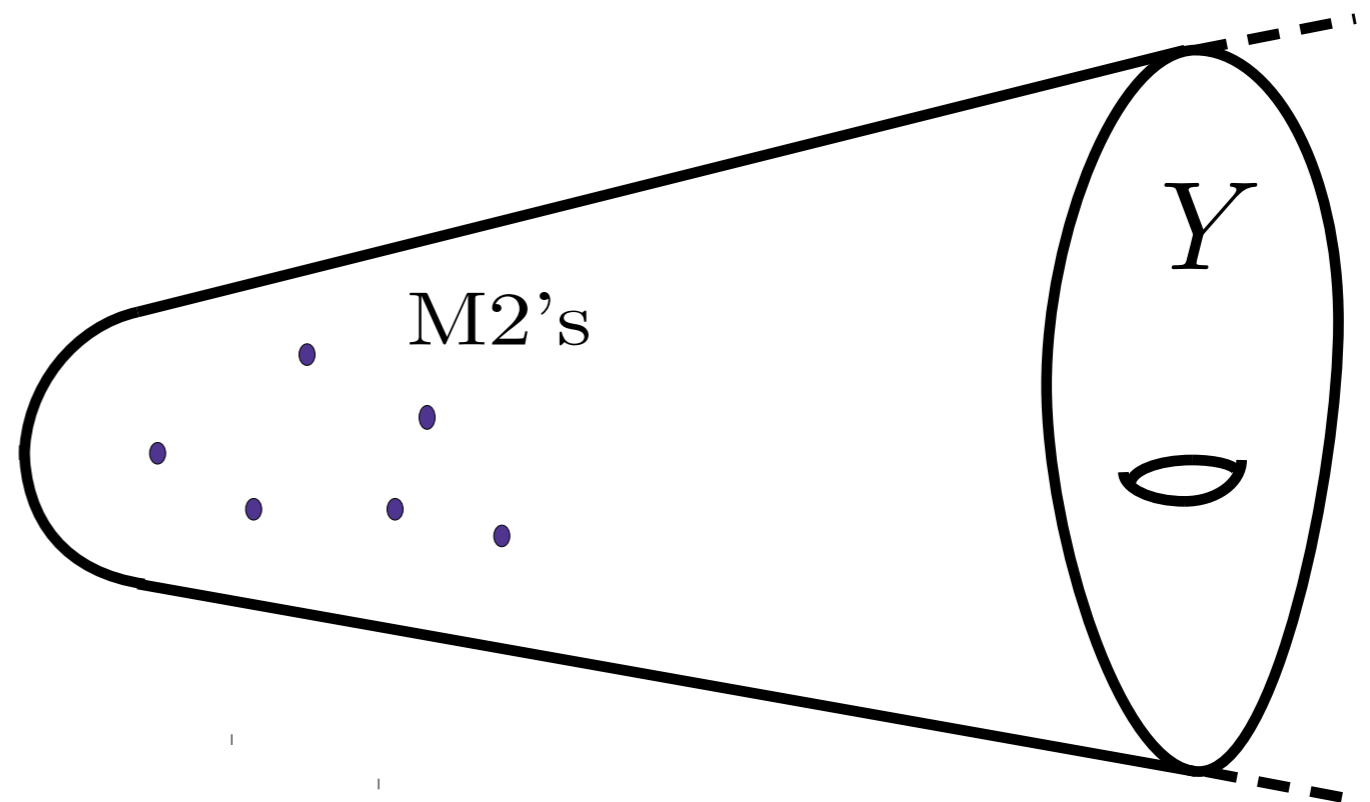
$\text{AdS}_4 \times Y$

Computation of HEFT

CFT moduli space
(geometric branch)



M-theory geometry



Smooth CY geometry + M2-branes:

3d EFT for M-theory
normalizable modes



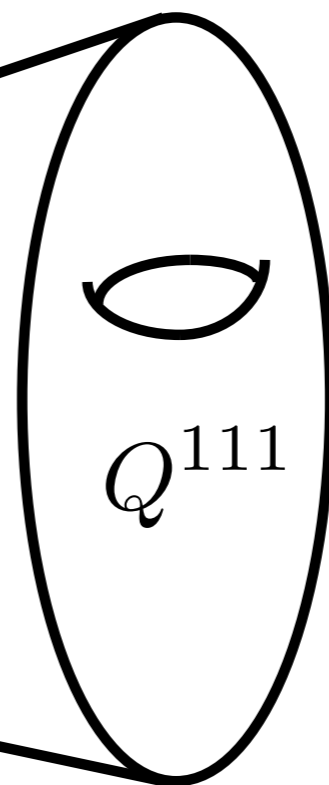
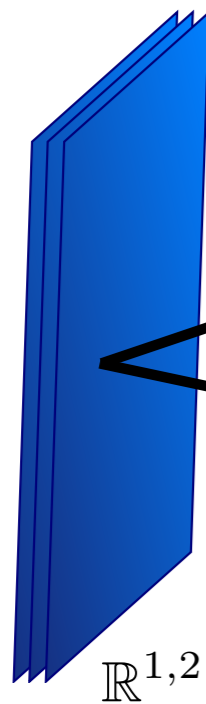
holographic EFT for dual CFT

Example 2:

the Q^{111} model

📌 M-theory origin:

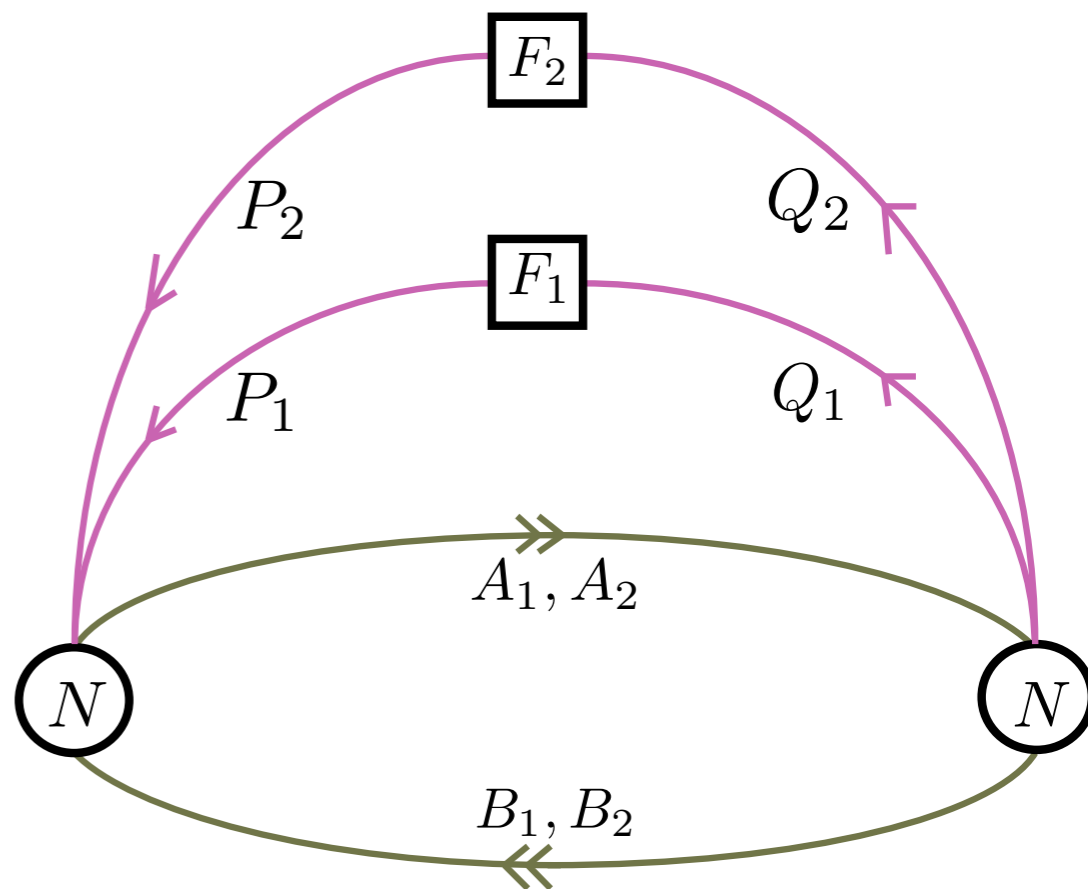
N M2



📌 UV quiver gauge theory:

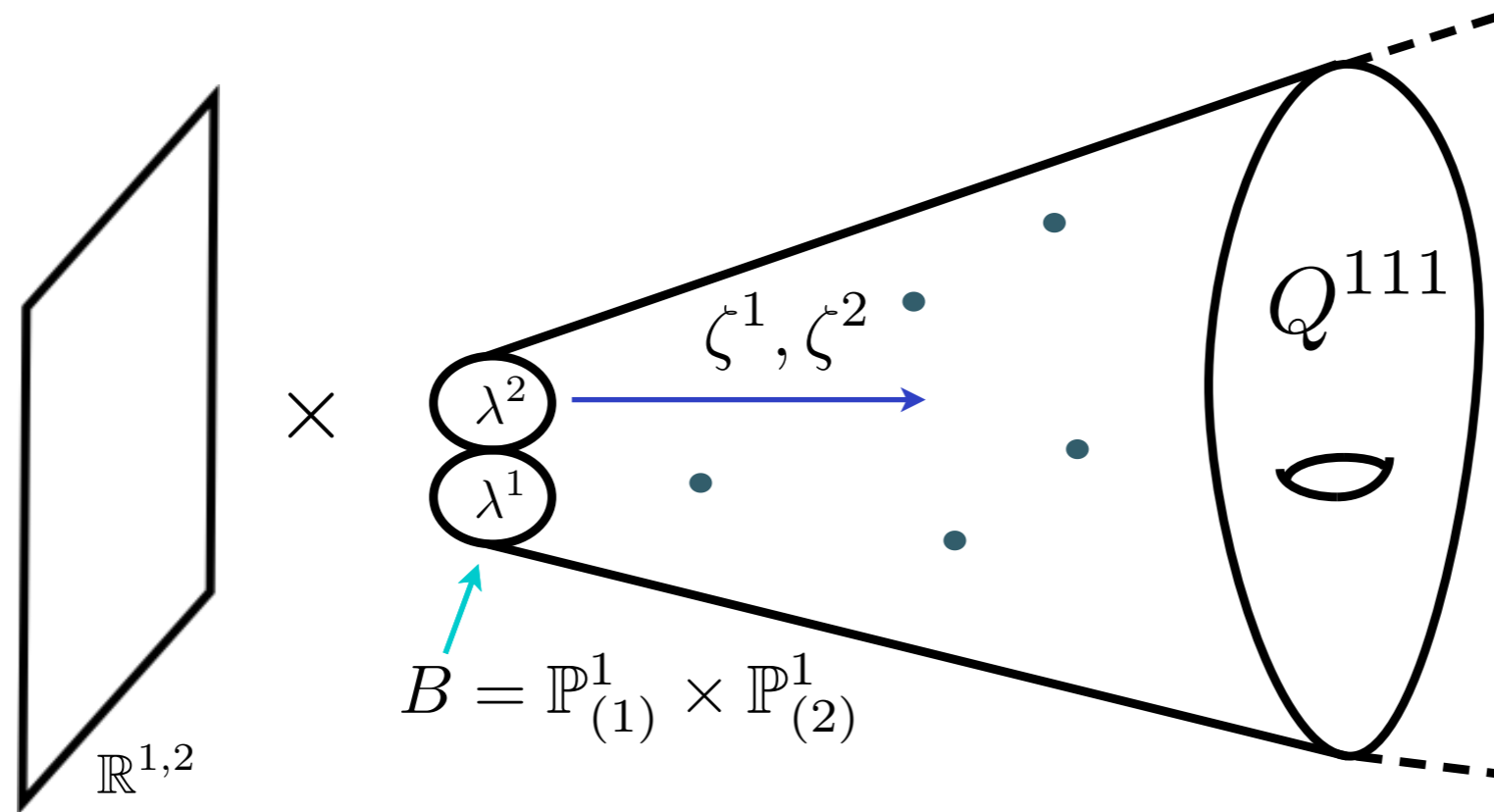
*
$$G = \frac{U(N) \times U(N)}{U(1)_B} \times U(1)_{F_1 - F_2}$$

*
$$W = \text{Tr}(A_1 B_1 A_2 B_2 - A_1 B_2 A_2 B_1) + P_1 A_1 Q_1 + P_2 A_2 Q_2$$



[Benini-Closset-Cremonesi '09]
[Jafferis '09]

HEFT of the Q^{111} model



$$X = \mathcal{L}_B \oplus \mathcal{L}_B$$

$$\mathcal{O}_B(-1, -1)$$

cf. [Cvetič-Gibbons-Lu-Pope '01]

[Benishti-Rodríguez Gómez-Sparks '10]

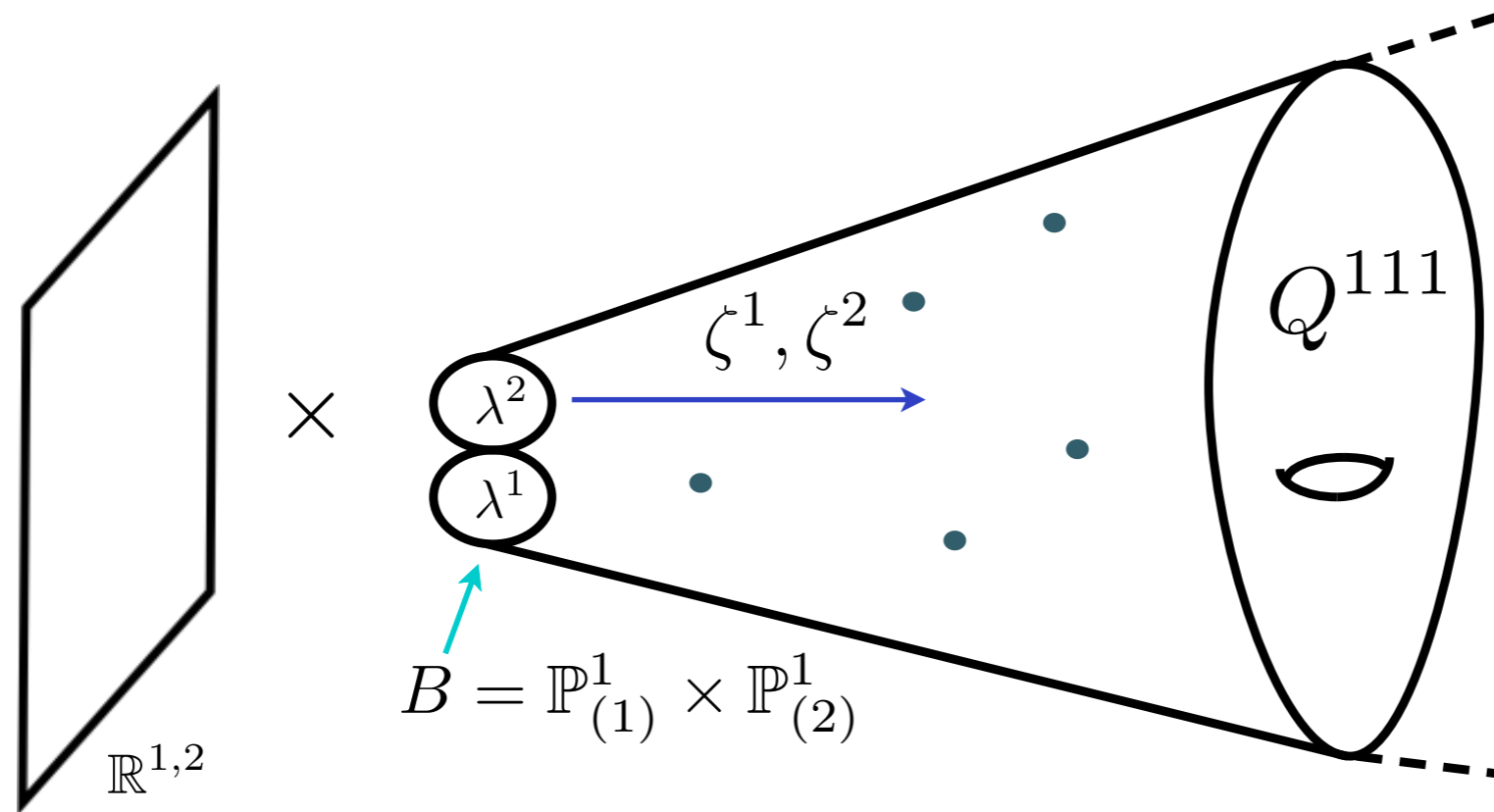
$$z^i = (\lambda^1, \lambda^2, \zeta^1, \zeta^2)$$

$$v_a = \text{vol}(\mathbb{P}_a^1)$$

Moduli	chiral fields
M2-brane positions	$z_I^i = (\zeta_I^1, \zeta_I^2, \lambda_I^1, \lambda_I^2)$
v_1, v_2 + C_6 -axions	ρ_1, ρ_2

$$I = 1, \dots, N$$

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HEFT more easily described in terms of dual vector multiplets V_a :

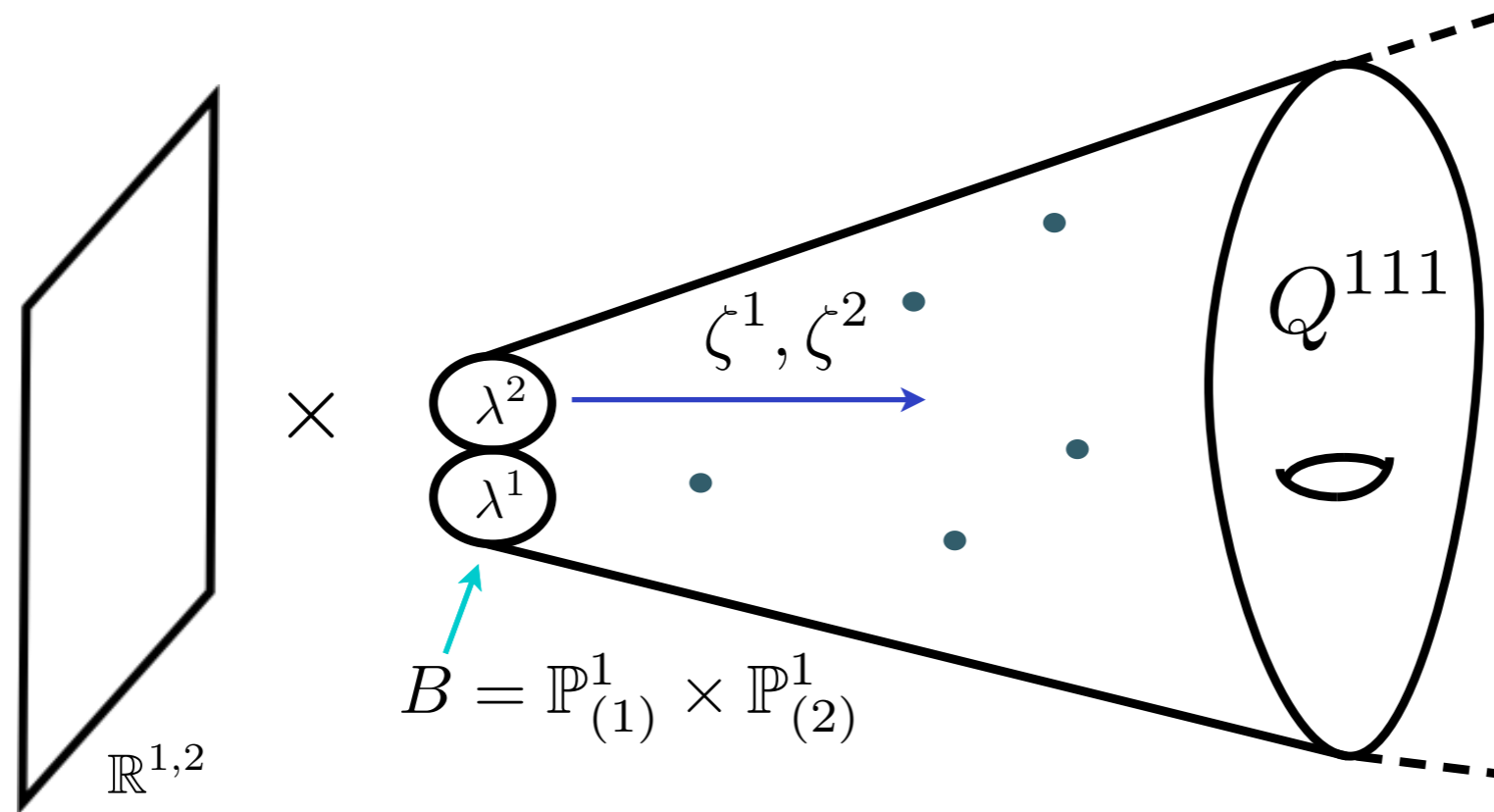
$$* \quad \mathcal{L}_{\text{HEFT}} = \int d^4\theta \mathcal{F}(z, \bar{z}, \Sigma) \quad \text{with}$$

$$\Sigma_a = D\bar{D}V_a = v_a + \dots$$

$$\mathcal{F}(z, \bar{z}, \Sigma) = \sum_{I=1}^N k_X(z_I, \bar{z}_I; \Sigma)$$

$$J_X = i\partial\bar{\partial}k_X$$

HEFT of the Q^{111} model



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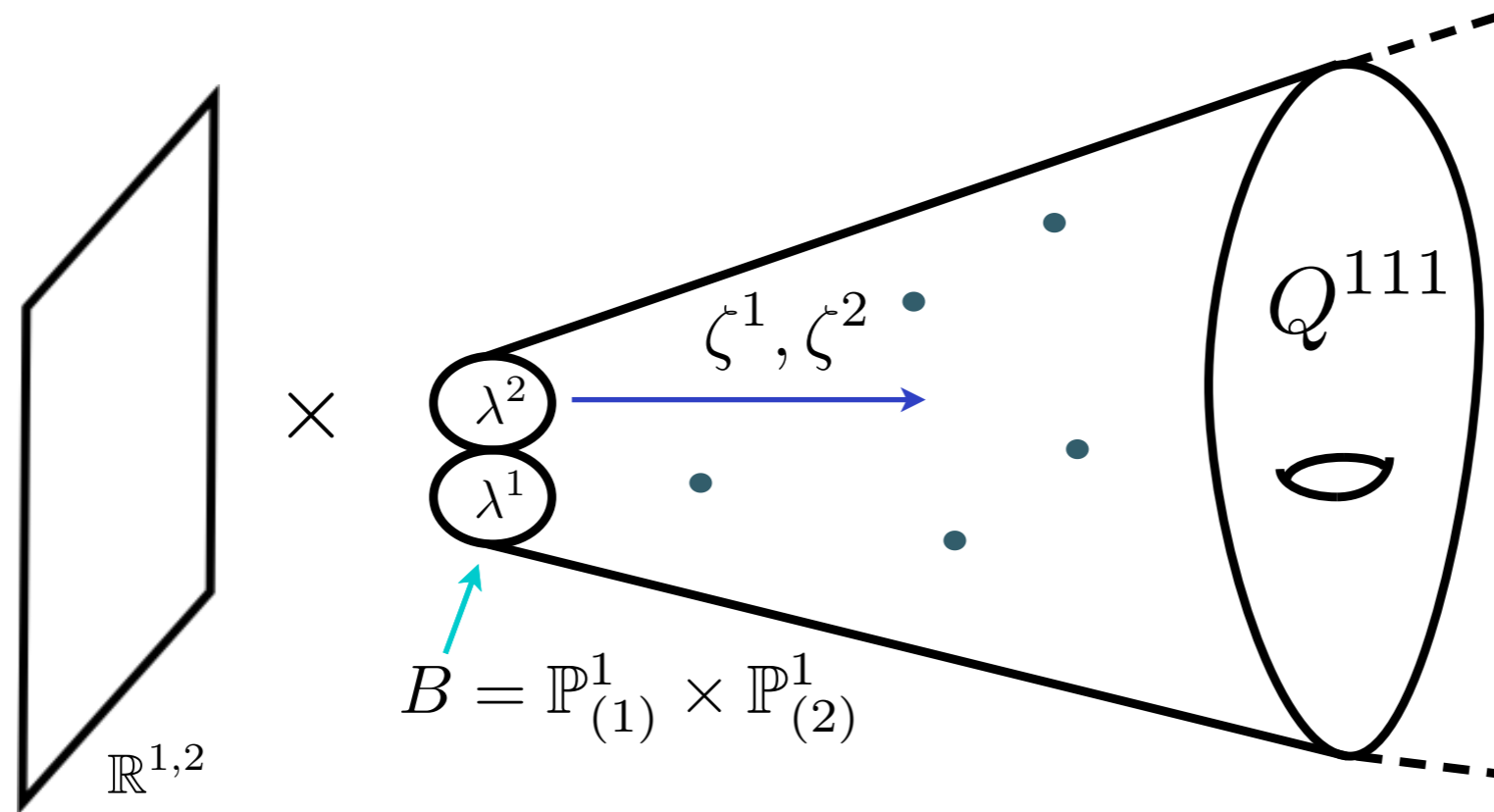
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$$\Sigma_a = D\bar{D}V_a = v_a + \dots$$

Chiral description:
[Hitchin-Karhede-Lindstrom-Rocek '88]
[de Boer-Hori-Oz '97]

$$K_{\mathcal{M}} = \mathcal{F} - \text{Re} \rho^a \Sigma_a \quad \text{with} \quad \text{Re} \rho^a = \frac{\partial \mathcal{F}}{\partial \Sigma_a}$$

HEFT of the Q^{111} model



$$X = \mathcal{L}_B \oplus \mathcal{L}_B$$

$$\mathcal{O}_B(-1, -1)$$

cf. [Cvetič-Gibbons-Lu-Pope '01]
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$$z^i = (\lambda^1, \lambda^2, \zeta^1, \zeta^2)$$

$$v_a = \text{vol}(\mathbb{P}_a^1)$$



Kähler potential:

$$K_{\mathcal{M}} = \sum_{I=1}^N k_0(z_I, \bar{z}_I; v_1, v_2)$$

with $k_0(z, \bar{z}; v_1, v_2) = s + \frac{A_-^2 - v_1 v_2}{A_+ - A_-} \log\left(1 + \frac{s}{A_-}\right) - \frac{A_+^2 - v_1 v_2}{A_+ - A_-} \log\left(1 + \frac{s}{A_+}\right)$

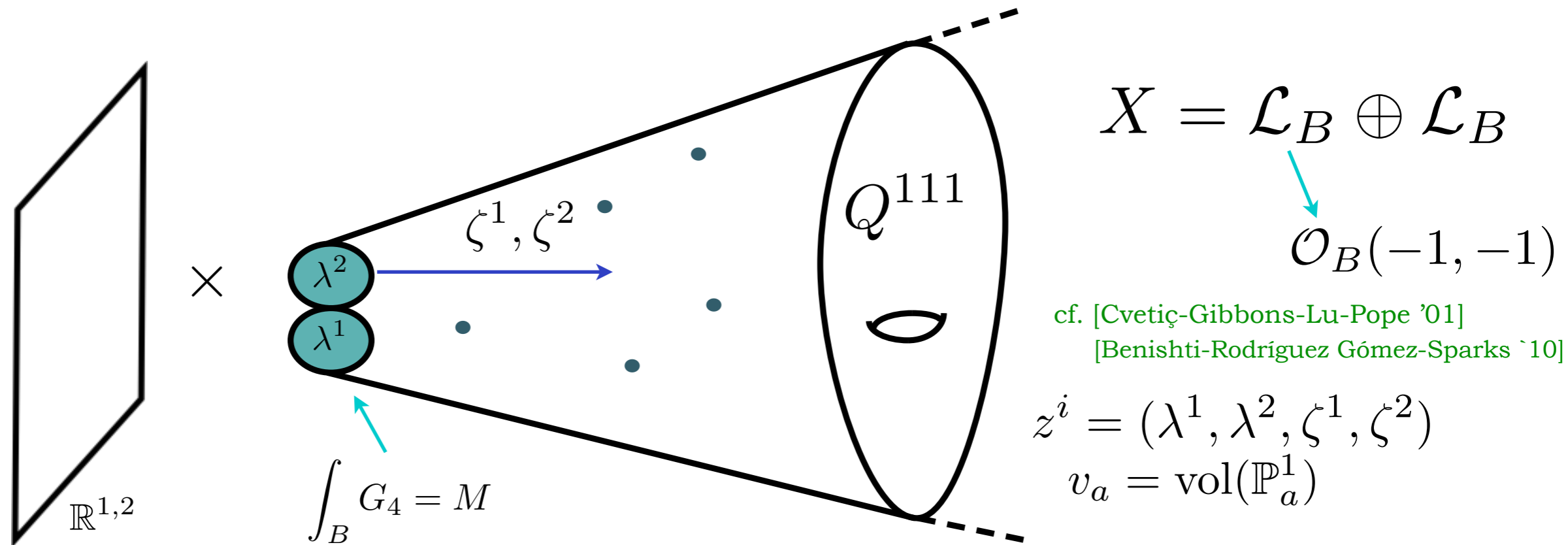
$$* \quad \text{Re} \rho^1 = \sum_{I=1}^N \left[\frac{v_2 - A_-}{A_+ - A_-} \log\left(1 + \frac{s_I}{A_-}\right) - \frac{v_2 - A_+}{A_+ - A_-} \log\left(1 + \frac{s_I}{A_+}\right) + k_{\mathbb{P}^1}(\lambda_I, \bar{\lambda}_I) \right]$$

$$* \quad A_{\pm} = \frac{1}{3} \left(2v_1 + 2v_2 \pm \sqrt{4v_1^2 - 10v_1 v_2 + 4v_2^2} \right)$$

$$* \quad s = (|\zeta_1|^2 + |\zeta_2|^2) e^{K_B(\lambda, \bar{\lambda})}$$

Holographic (large-N)
EFT for dual CFT

HEFT of the Q^{111} model



One can turn on an (explicit) supersymmetric G_4 -flux

$$* K_{\mathcal{M}}^{\text{flux}} = \sum_{I=1}^N k_0(z_I, \bar{z}_I; v) + \frac{1}{2} \int_X k_0(z, \bar{z}; v) (G_4 \wedge G_4)(z, \bar{z}; v)$$

CFT interpretation under study

cf. [Gukov-Vafa-Witten '99]
 [Cvetic-Gibbons-Lu-Pope '01]

[Herzog-Klebanov '01]
 [Martelli-Sparks '09]

Superconformal symmetry

Definite scaling dimensions:

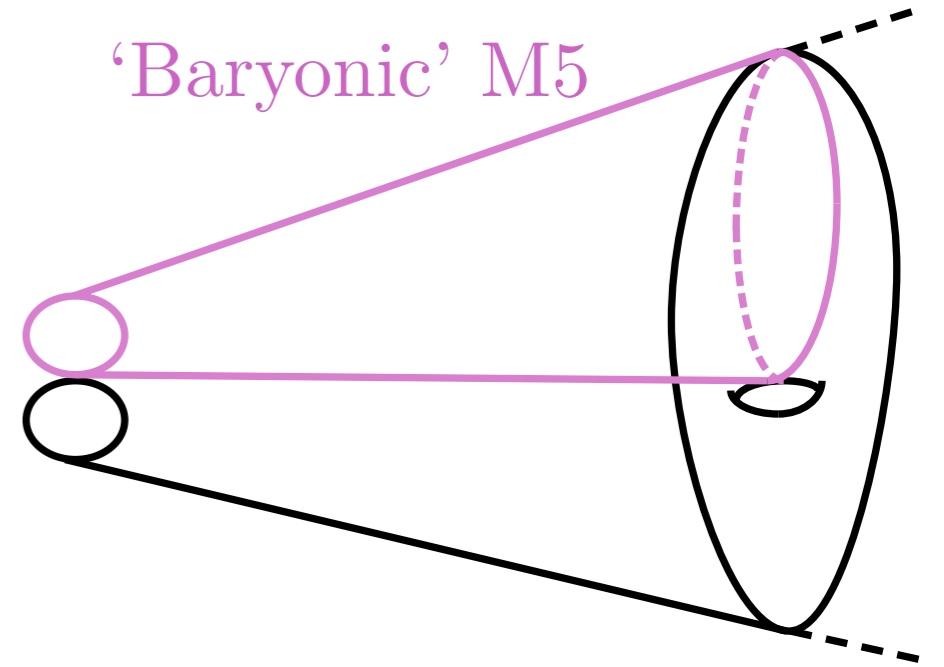
e.g. $\Delta_{e^{-2\pi\rho}} = \frac{N}{3} \longrightarrow$

$\langle B^N \rangle \sim e^{-2\pi\rho}$ have correct $\Delta = \frac{1}{3}N$

[Jafferis, Klebanov, Pufu, Safdi '11]

[Klebanov-Murugan '07]
[Benishti-Rodríguez Gómez-Sparks '10]

'Baryonic' M5

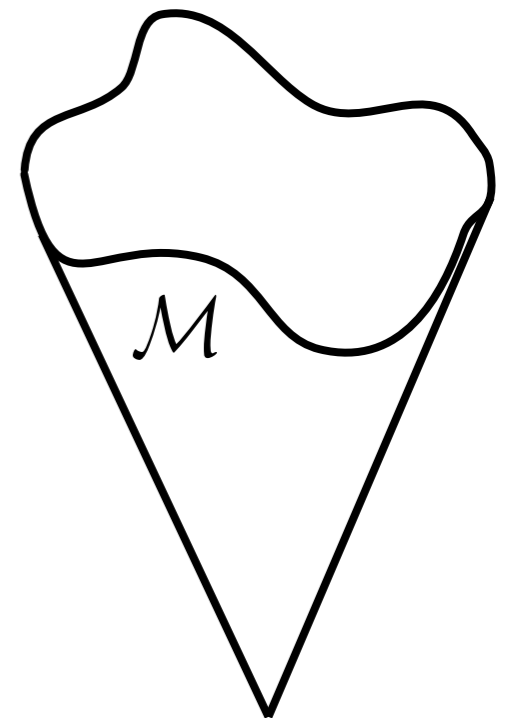


$\Delta[K_{\mathcal{M}}^{\text{flux}}] = 1$

(non-linearly) realised
superconformal symmetry!

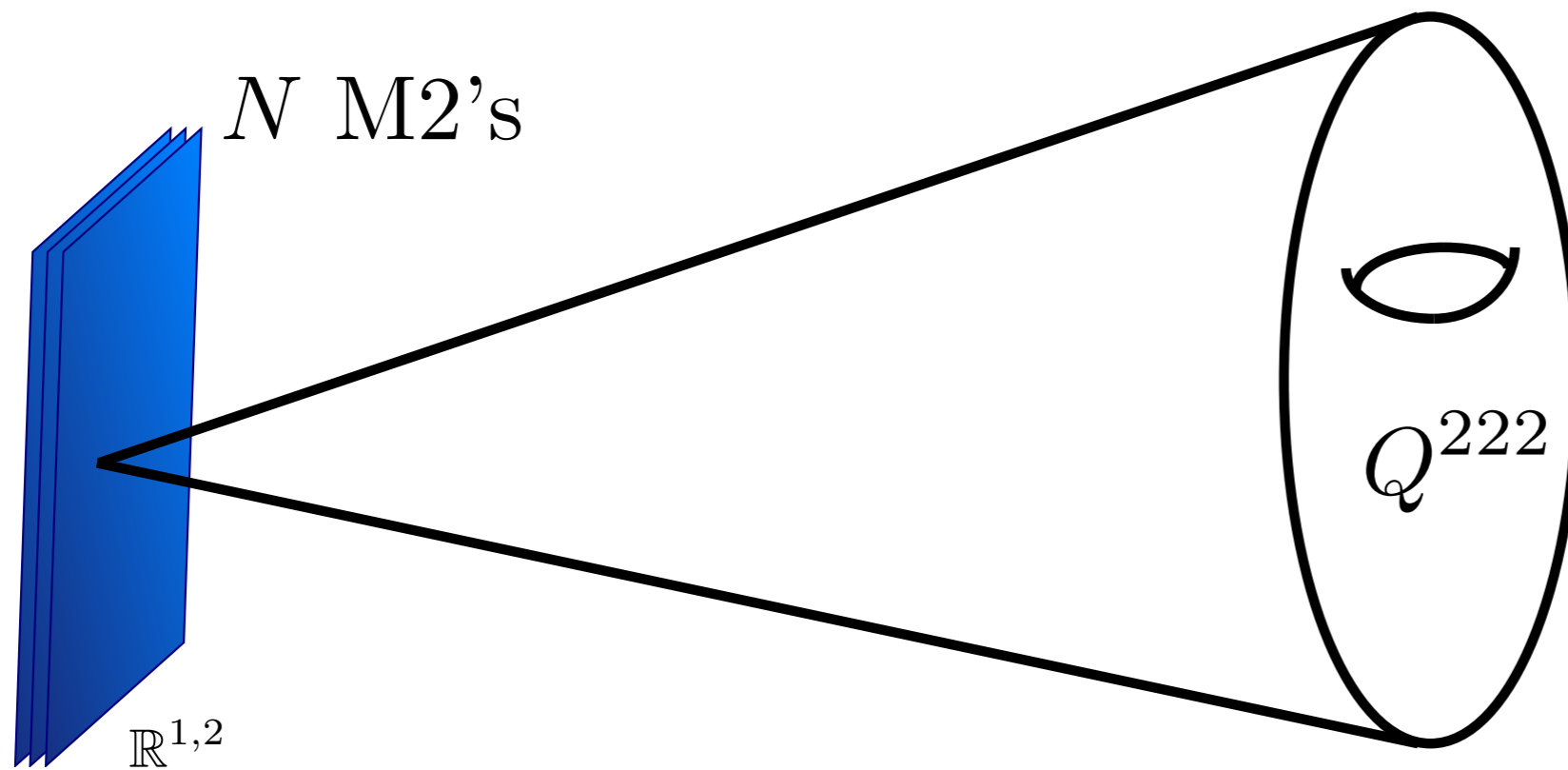


conical Kähler metric
over \mathcal{M}



Non-perturbative (de)stabilisation in
 AdS_4/CFT_3

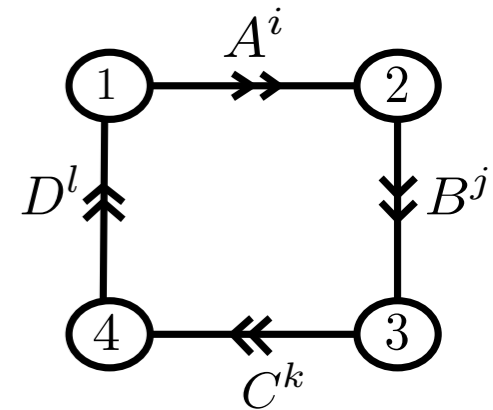
The Q^{222} model



📌 UV quiver gauge theory:

* gauge group:
$$\frac{U(N)_1 \times U(N)_2 \times U(N)_3 \times U(N+2)_4}{U(N)_{B,1} \times U(N)_{B,2}}$$

* superpotential:
$$W = \epsilon_{ik} \epsilon_{jl} \text{Tr}(A^i B^j C^k D^l)$$



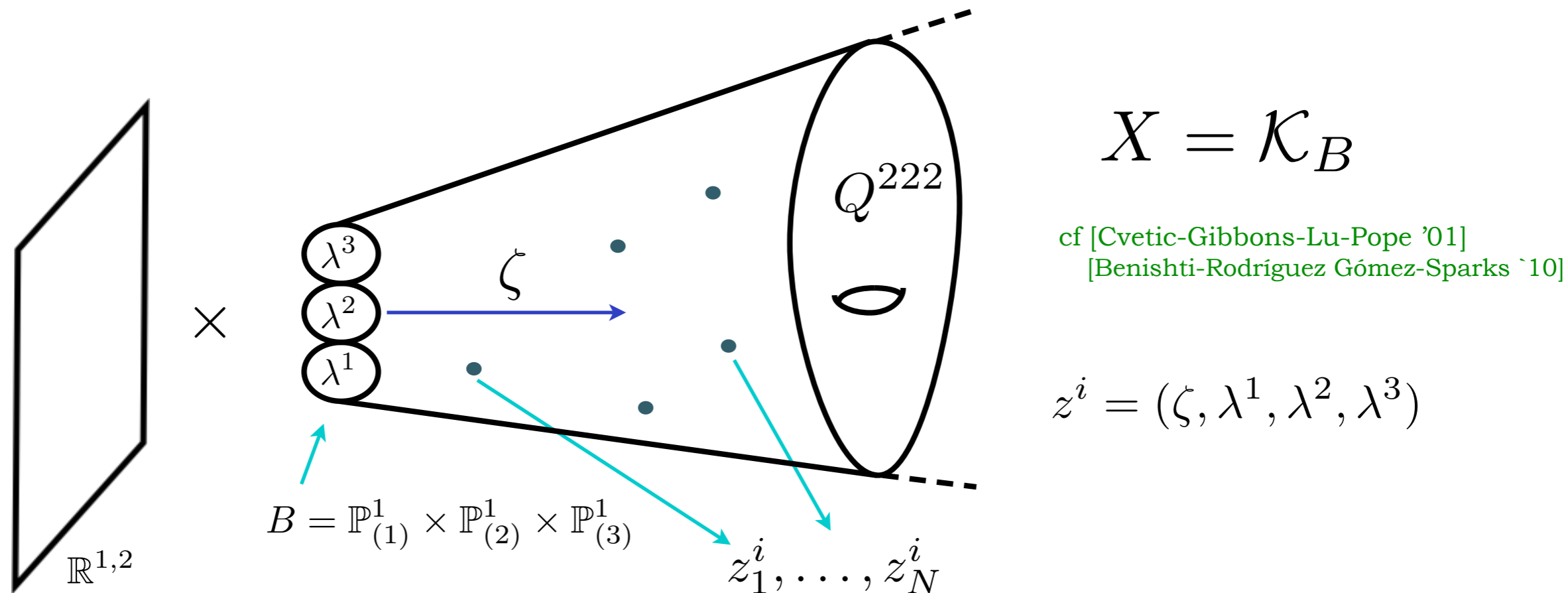
3d version of 4d \mathbb{F}_0 -theory

[Feng-Franco-Hanany-He '10]

'Seiberg dual' of 3d quiver proposed in:

[Closset-Cremonesi '12]

HEFT of the Q^{222} model

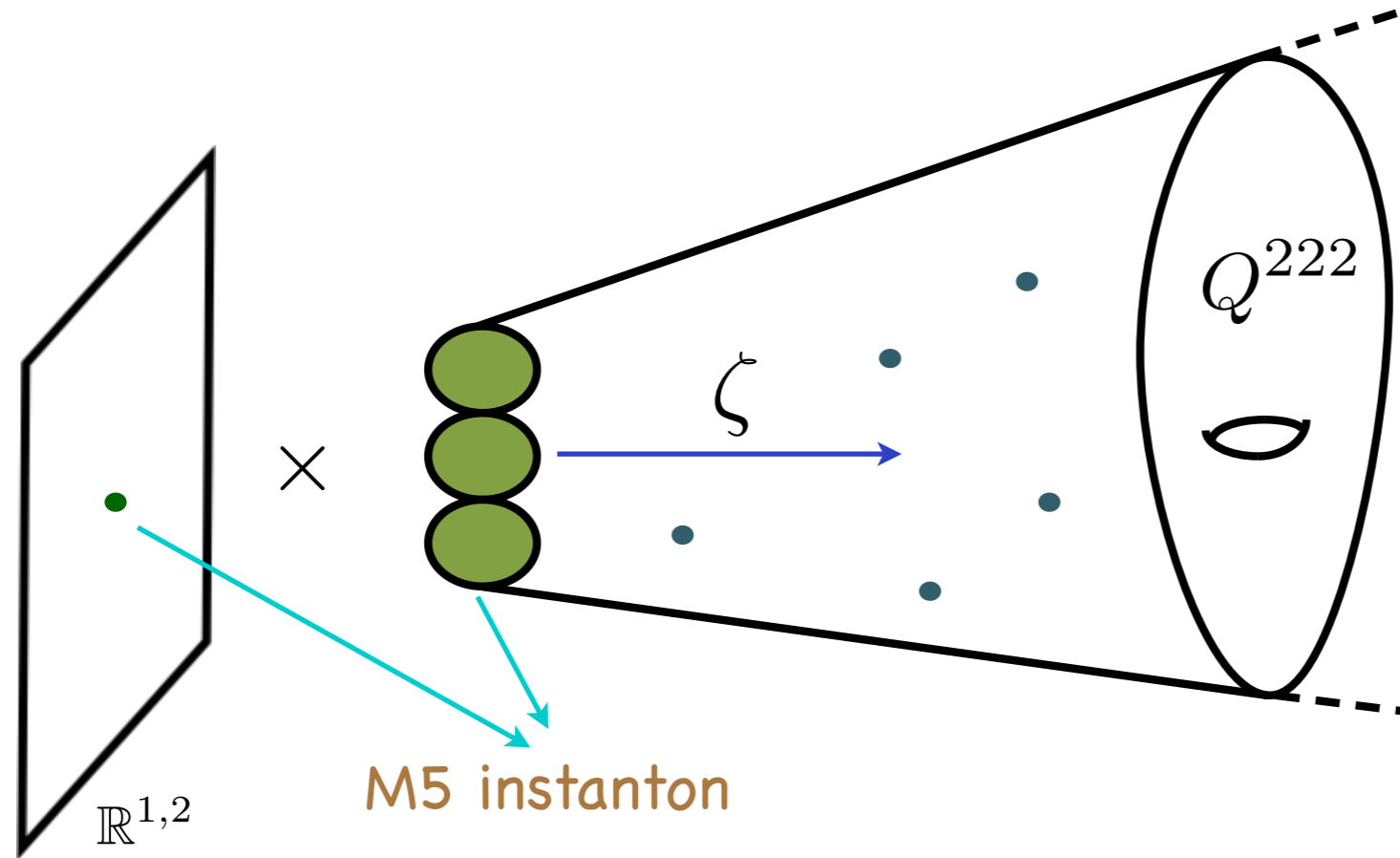


Moduli	chiral fields
M2-brane positons	$z_I^i = (\zeta_I, \lambda_I^1, \lambda_I^2, \lambda_I^3)$
volumes \mathbb{P}^1 's + C_6 -axions	ρ_1, ρ_2, ρ_3

$I = 1, \dots, N$

Explicit **perturbative** HEFT: $K_{\mathcal{M}}(\rho, \bar{\rho}, z_I, \bar{z}_I)$

HEFT of the Q^{222} model



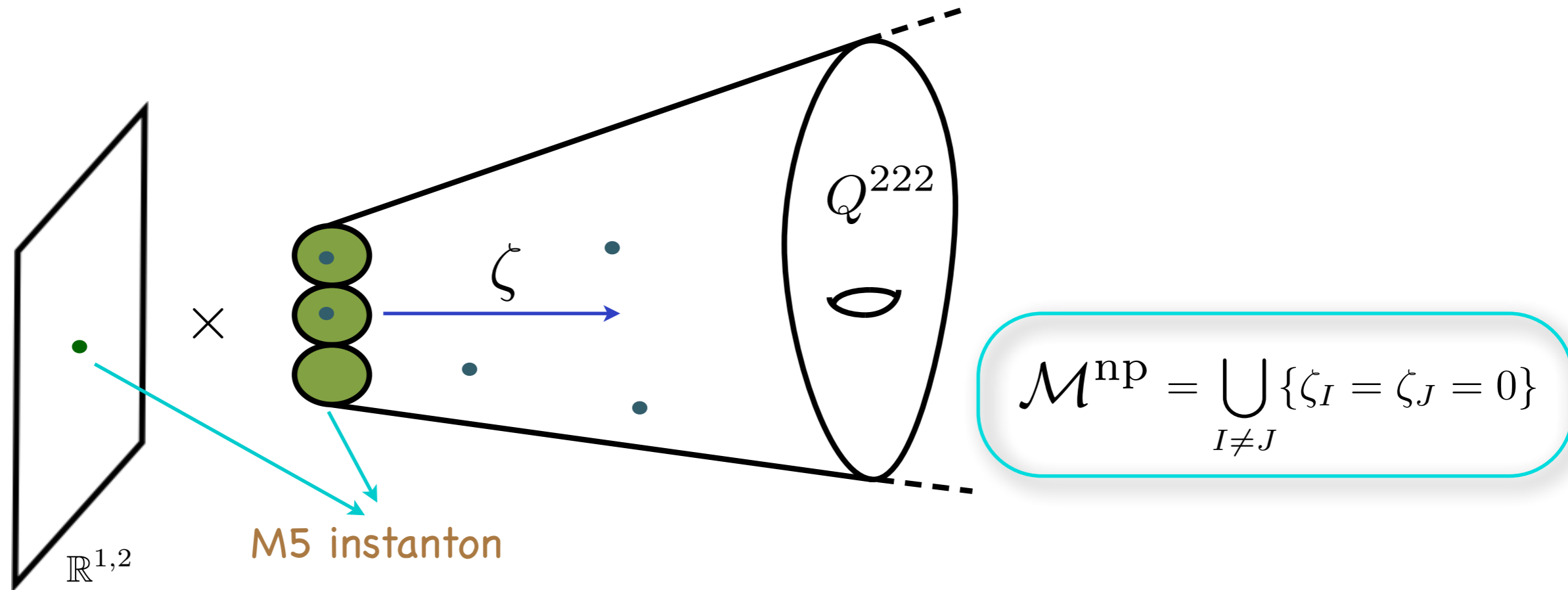
see also [Benishti-Rodríguez Gómez-Sparks `10]

M5-brane instanton generates a **non-perturbative superpotential**

$$W_{\text{np}} = e^{4\pi(\rho_1 + \rho_2 + \rho_3)} \prod_{I=1}^N \zeta_I$$

cf. [Witten `96] [Ganor `96]
 [Katz-Vafa `96] [Diacunescu-Gukov `98]
 [Baumann-Dymarsky-Klebanov-Maldacena-McAllister-Murugan]

HEFT of the Q^{222} model



see also [Benishti-Rodríguez Gómez-Sparks `10]

- M5-brane instanton generates a **non-perturbative superpotential**

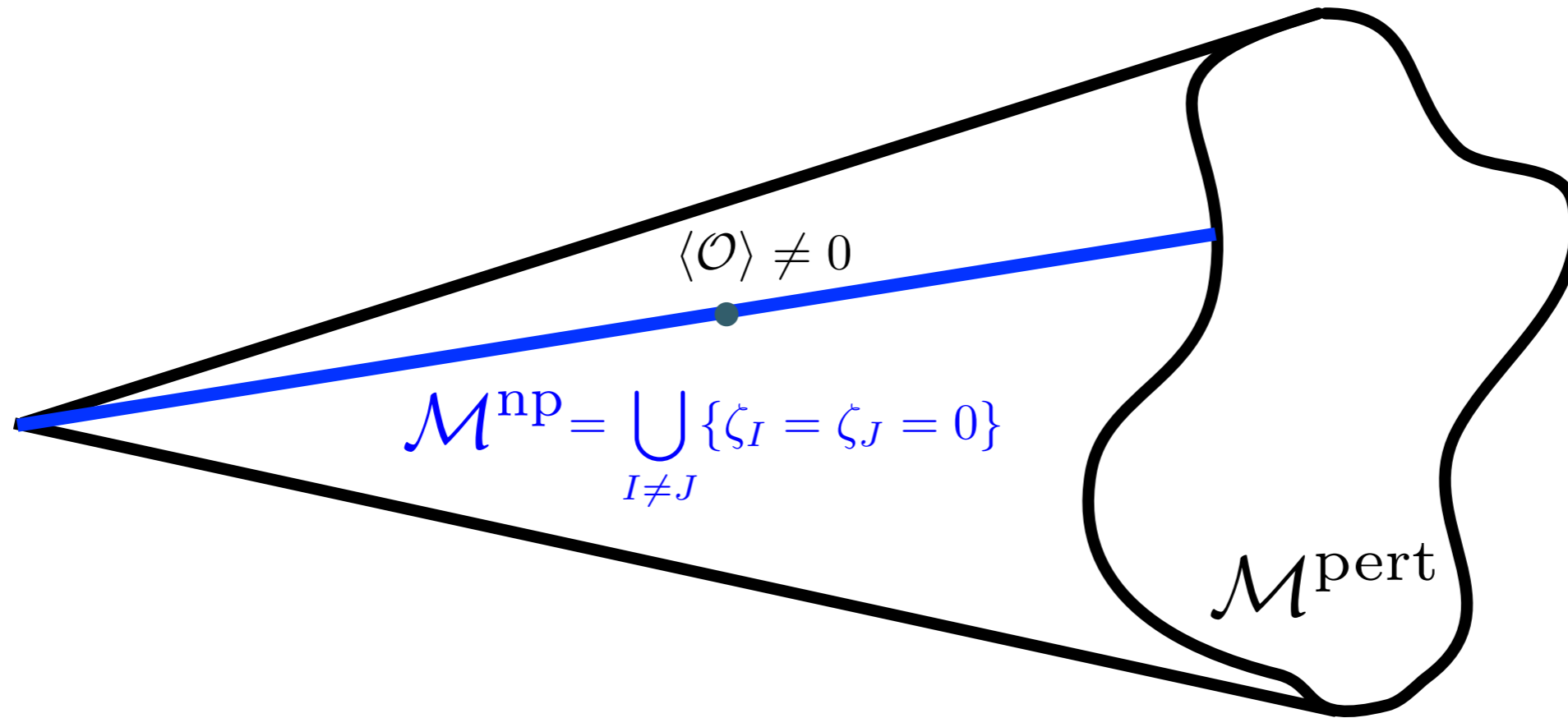
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- Strong coupling counterpart of weakly coupled SU(2) instanton

[Affleck, Harvey, Witten `82] [De Boer-Hori-Oz `97] [Aharony-Hanany-Intriligator-Seiberg-Strassler `97] ...

Complete HEFT & moduli space



* $K(\rho, \bar{\rho}, z, \bar{z})$ perturbative in $1/N \ll 1$

* $W_{\text{np}} = e^{4\pi(\rho_1 + \rho_2 + \rho_3)} \prod_{I=1}^N \zeta_I$ non-perturbative in $1/N \ll 1 \sim O(e^{-cN})$



$$V_{\text{eff}} = K^{A\bar{B}} \partial_A W_{\text{np}} \partial_{\bar{B}} \bar{W}_{\text{np}} \neq 0$$

Summary

- 📌 M-theory derivation of **holographic EFT**'s for 3d $\mathcal{N} = 2$ CFT's
 - * natural parametrization of bulk+brane moduli
 - * general formulas for the Kähler potential of bulk+brane moduli
 - * incorporation of G_4 -fluxes and M5-instantons
- 📌 Explicit formulas for $Q^{111}, Q^{222}, Y^{12}(\mathbb{P}^2)$ from explicit CY metric.

Existence of more efficient computational technics???

Thanks