

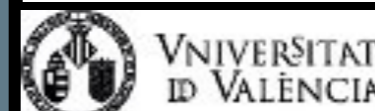
# Searching for Neutrinos through Cosmology

Olga Mena

IFIC-CSIC/UV Valencia (Spain)



in**v**isiblesPlus  
elusi**v**es  
neutrinos, dark matter & dark energy physics



# Today's menu

## Antipasto

- The classical cosmic pizza
- The neutrino slice
- Neutrino decoupling in the early universe
- Other cosmic pizzas for tasting

## Main course

- Number of neutrinos and Big-Bang Nucleosynthesis
- Number of neutrinos and Cosmic Microwave Background Radiation
- Neutrino masses and Cosmic Microwave Background Radiation
- Neutrino masses and structure formation in the universe
- The Dark Justice League game:  $\Sigma m_\nu$  versus  $w(z)$

## Doggy Bag

- Take home messages

# $\Lambda$ CDM Pizza

$\Omega_i$

Heavy elements

$\Omega_{\text{Heavy Elements}} = 0.0003$



Dark energy

$\Omega_{\Lambda} = 0.7$

Neutrinos!

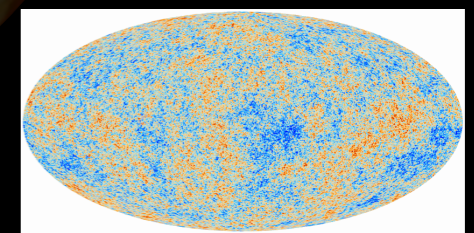
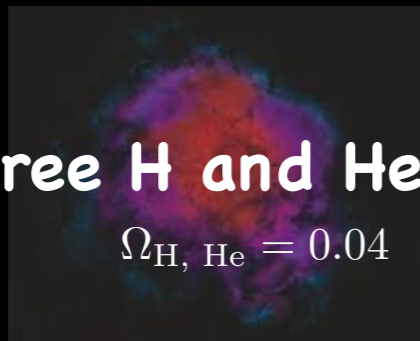
Stars

$\Omega_{\text{Stars}} = 0.005$



Free H and He

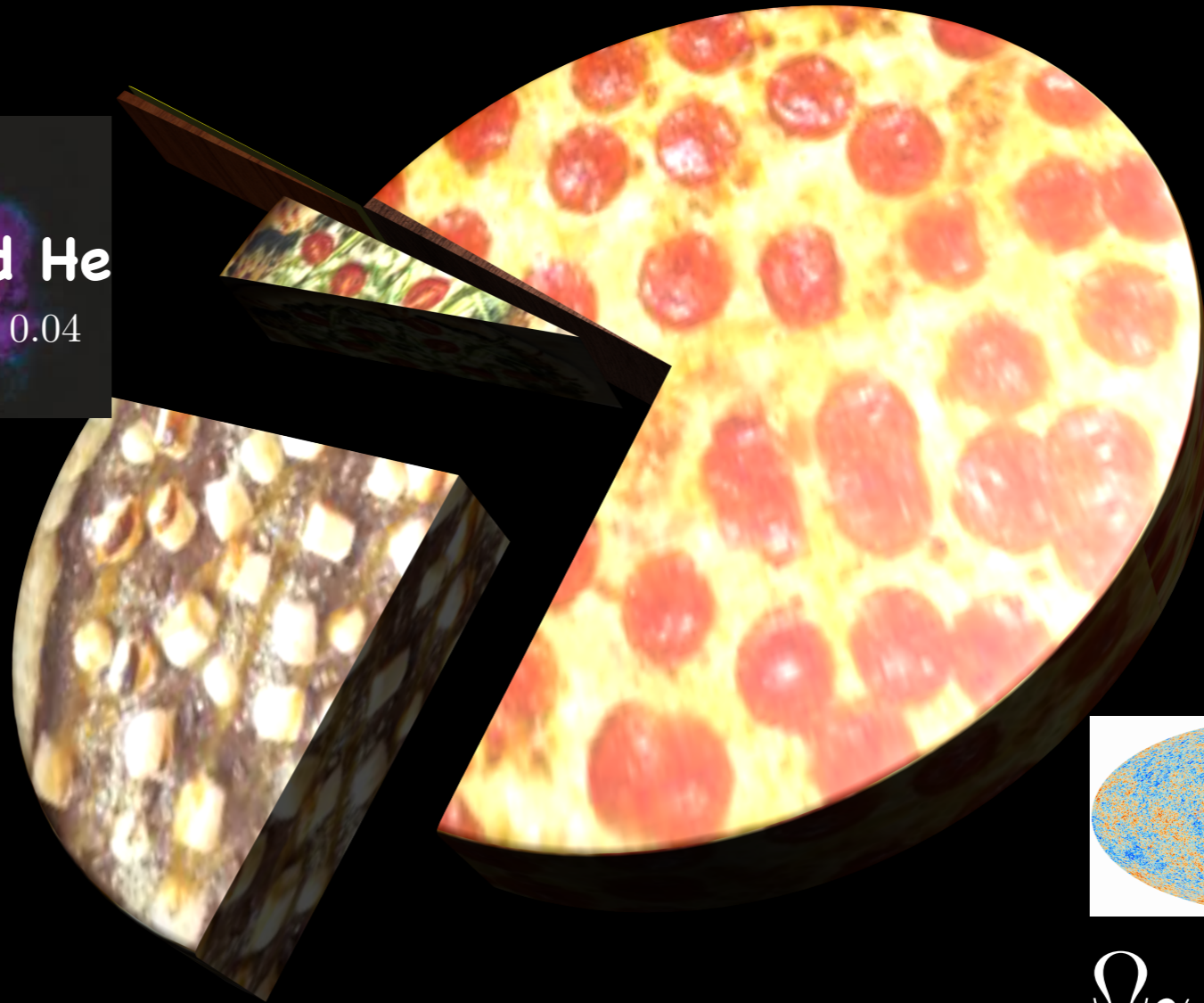
$\Omega_{\text{H, He}} = 0.04$



$\Omega_{\gamma} \sim 10^{-5}$

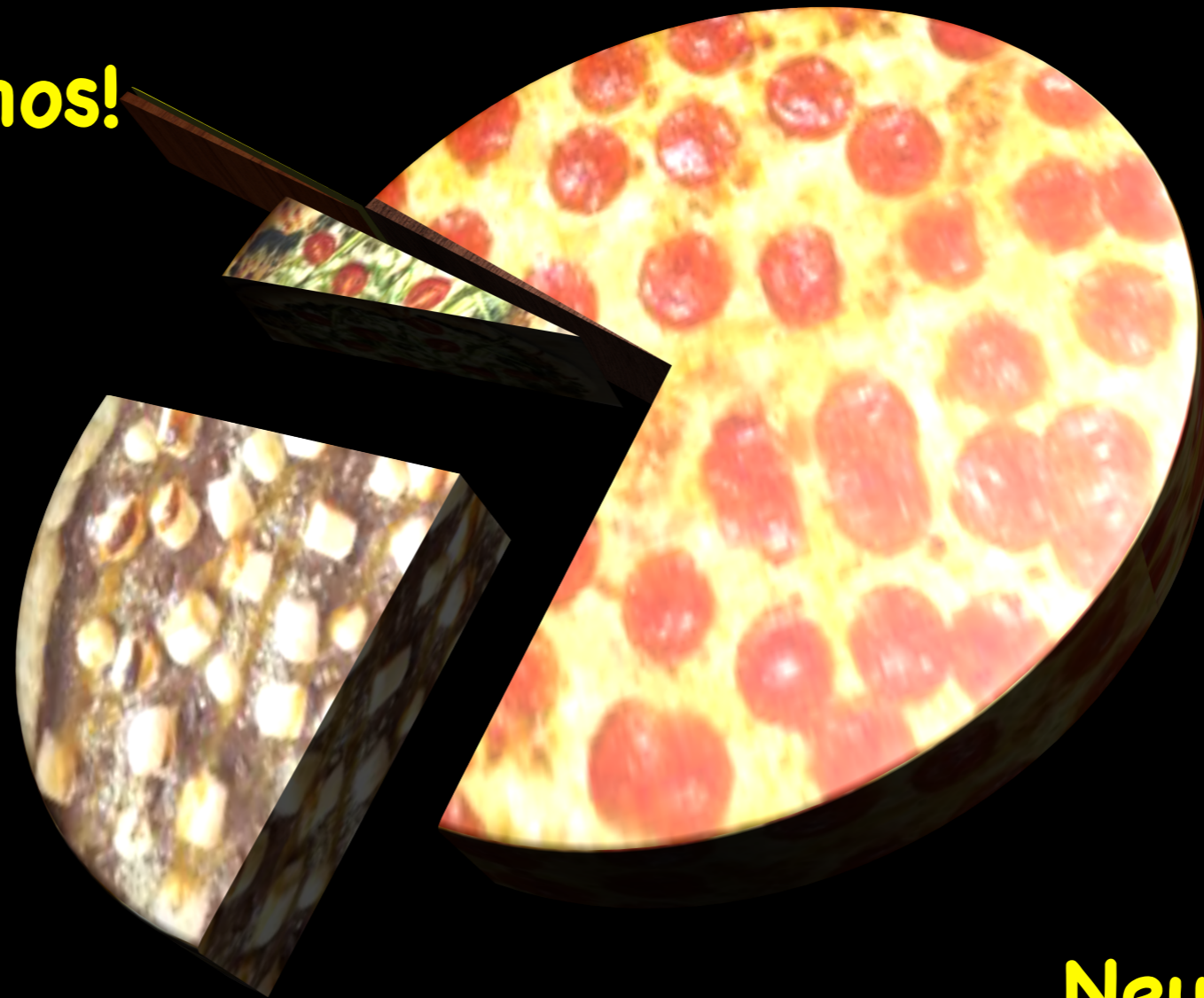
Cold Dark matter

$\Omega_{\text{CDM}} = 0.25$



How large is the **MASSIVE** neutrino contribution?

**Neutrinos!**



**Cosmology tells us**

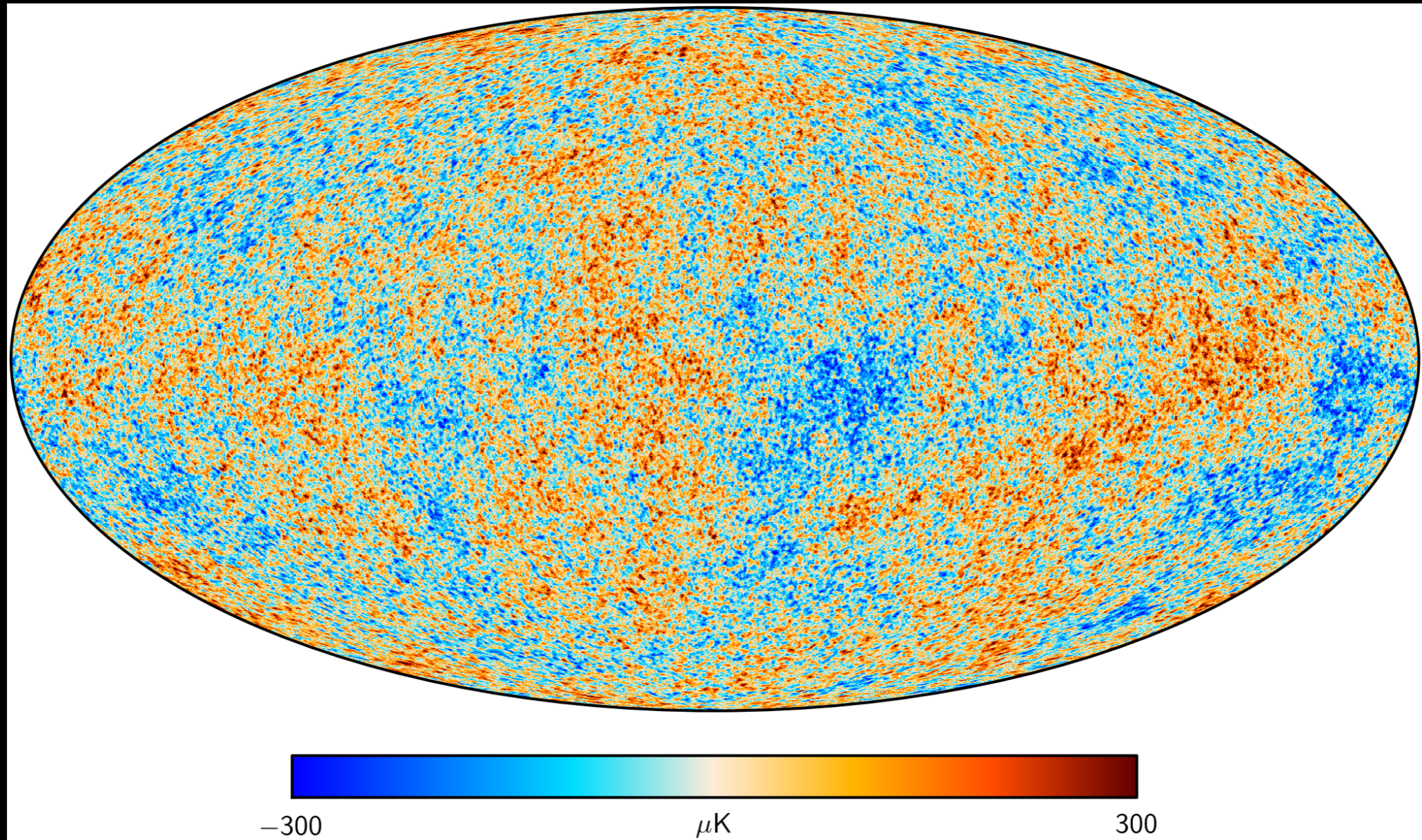
$$\Omega_\nu \lesssim 0.0024 \text{ 95\% CL}$$

**Neutrino**

**oscillations tell us**

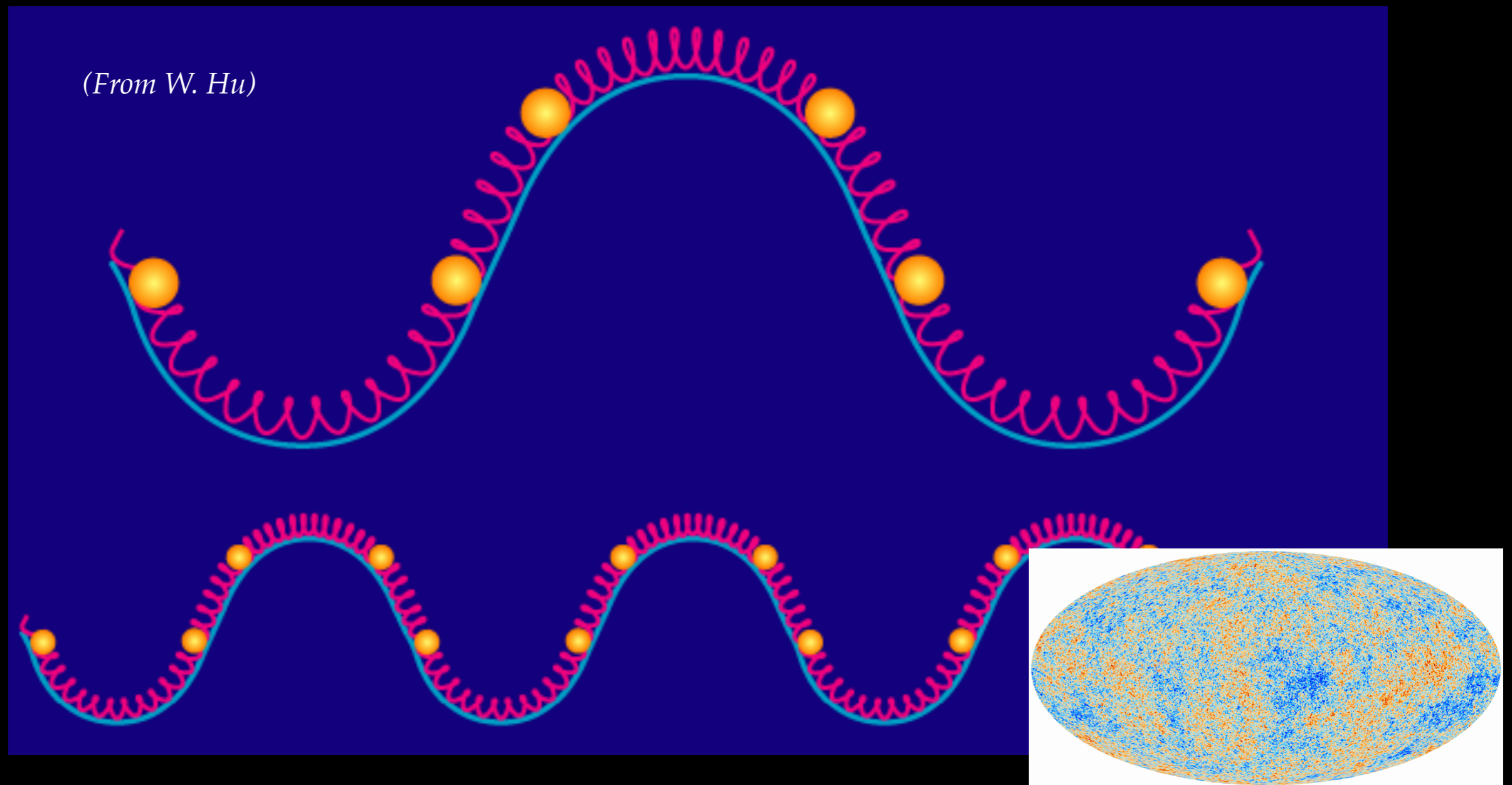
$$\Omega_\nu \gtrsim 0.0012 \text{ 95\% CL}$$

I guess all you know about dark matter/what about dark radiation?  
But radiation is visible, and it has a mean  $T \approx 2.725$  K!



This map is just telling us how the CMB temperature fluctuations vary with the angular size of patches in the sky...

The CMB fluctuations are due to the acoustic oscillations in the baryon-photon fluid before recombination.

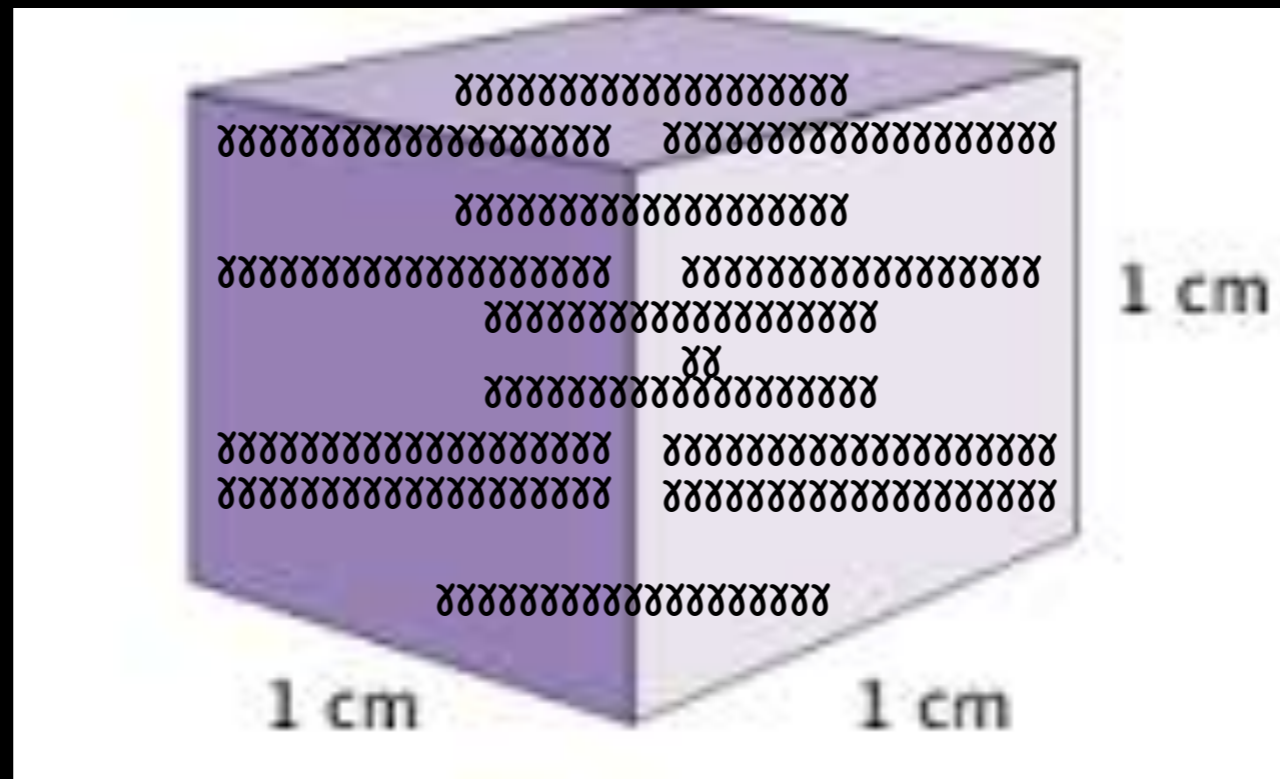


Potential wells  $\longrightarrow$  High density  $\longrightarrow$  COLD SPOTS in CMB maps  
Potential hills  $\longrightarrow$  Low density  $\longrightarrow$  HOT SPOTS in CMB maps

I guess all you know about dark matter/what about dark radiation?

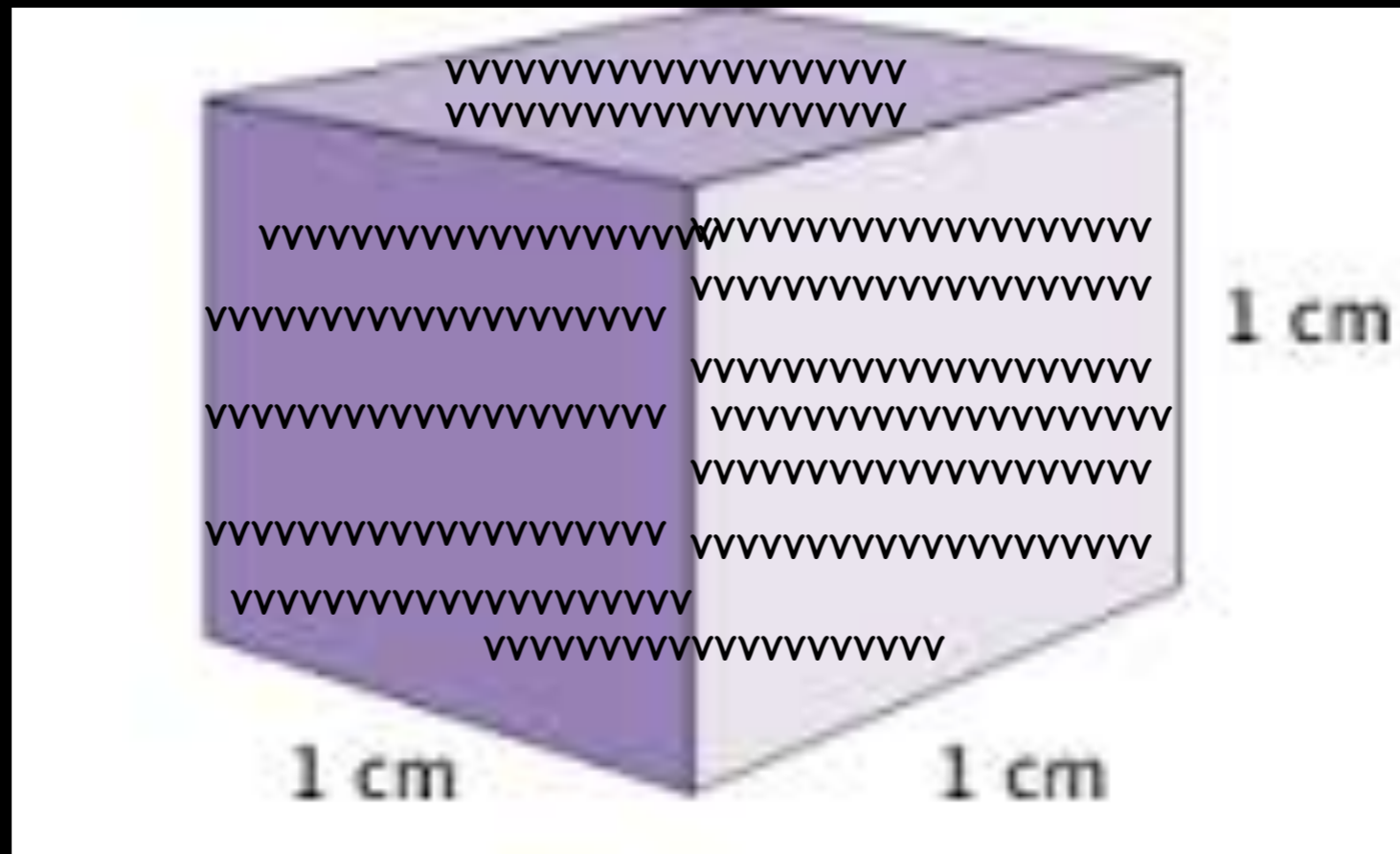
But radiation is visible!

410 photons/cm<sup>3</sup>



According to standard cosmology, there is a cosmic neutrino background, equivalent to the CMB photon background, albeit slightly colder  $T \approx 1.94$  K

**340 neutrinos/cm<sup>3</sup>**

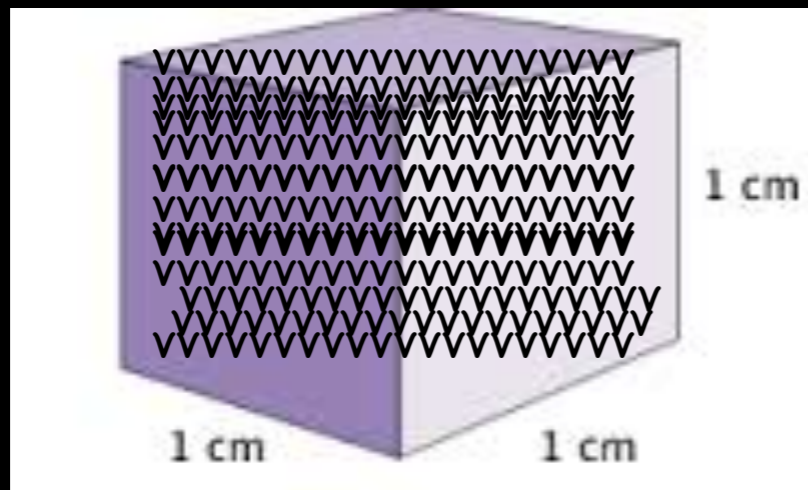


This cosmic relic neutrino background has never been detected directly.



The universe is filled with a dense flux of "relic neutrinos" created in the Big Bang.  
This makes neutrinos the most abundant KNOWN form of...

**340 neutrinos/cm<sup>3</sup>**



**HOT dark matter!**

According to **standard cosmology**, there are three active Dirac or Majorana neutrinos, which decouple from the thermal bath when their scattering rate is smaller than the expansion rate of the universe:

$$\Gamma_\nu \lesssim H$$

- Neutrinos only interact via weak interactions, with a rate:

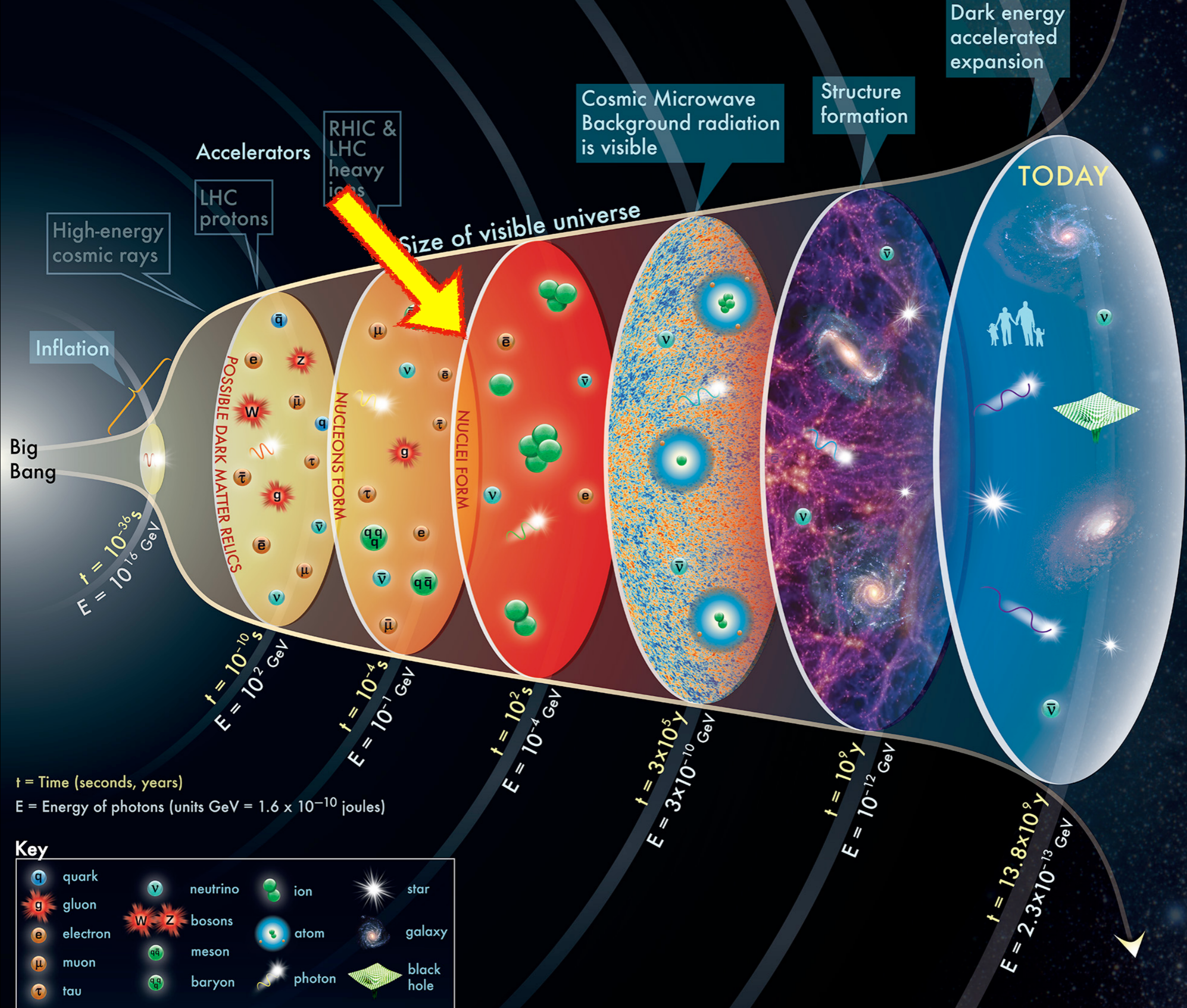
$$\Gamma_\nu = n\sigma v \simeq T^3 G_F^2 T^2 \sim G_F^2 T^5$$

- While the expansion rate of the universe is given by the Hubble factor:

$$H^2 = \frac{8\pi G}{3} \rho \sim T^4 / m_{pl}^2$$

$$\Gamma_\nu / H \sim \left( \frac{T}{1 \text{ MeV}} \right)^3$$

- **Therefore neutrinos decouple from the thermal bath around 1 MeV.**



$t$  = Time (seconds, years)  
 $E$  = Energy of photons (units GeV =  $1.6 \times 10^{-10}$  joules)

**Key**

quark	neutrino	ion	star
gluon	bosons	atom	galaxy
electron	meson	photon	black hole
muon	baryon		
tau			

The concept for the above figure originated in a 1986 paper by Michael Turner.

Event	Time	Redshift	Temperature
Baryogenesis	?	?	?
EW phase transition	$2 \times 10^{-11} s$	$10^{15}$	$100 GeV$
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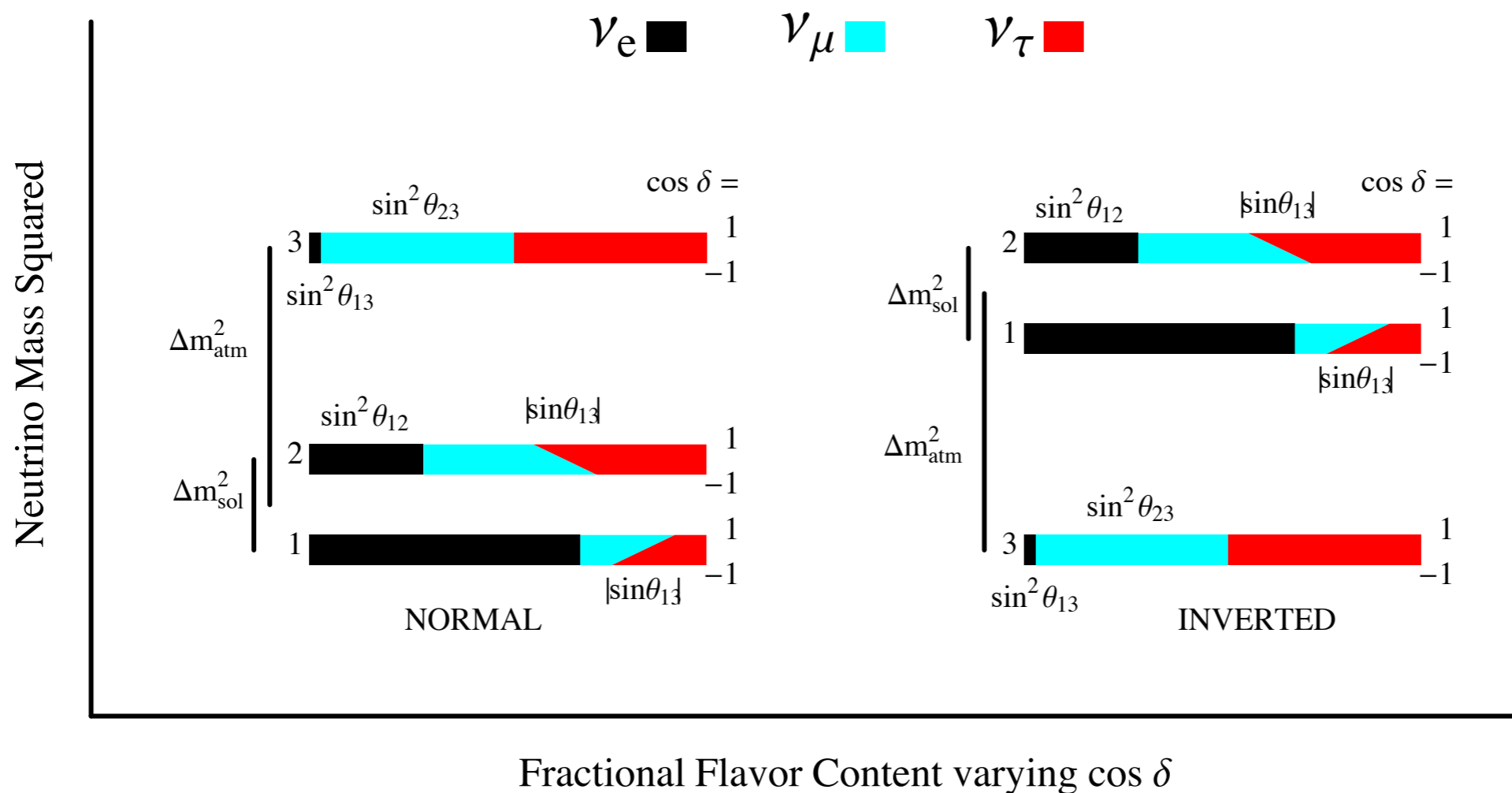


According to **neutrino oscillation physics**, we know that there are at least two Dirac or Majorana **massive** neutrinos:

$$\Delta m_{12}^2 = (7.05 - 8.14) \times 10^{-5} \text{eV}^2$$

$$\Delta m_{13}^2 = (2.41 - 2.60) \times 10^{-3} \text{eV}^2$$

$$\Delta m_{13}^2 = -(2.31 - 2.51) \times 10^{-3} \text{eV}^2$$



(Mena, Parke, PRD'04)

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We are sure then that **two neutrinos have a mass above:**

$$\sqrt{\Delta m_{12}^2} \simeq 0.008 \text{ eV}$$

and that **at least one of these neutrinos has a mass larger than**

$$\sqrt{|\Delta m_{13}^2|} \simeq 0.05 \text{ eV}$$

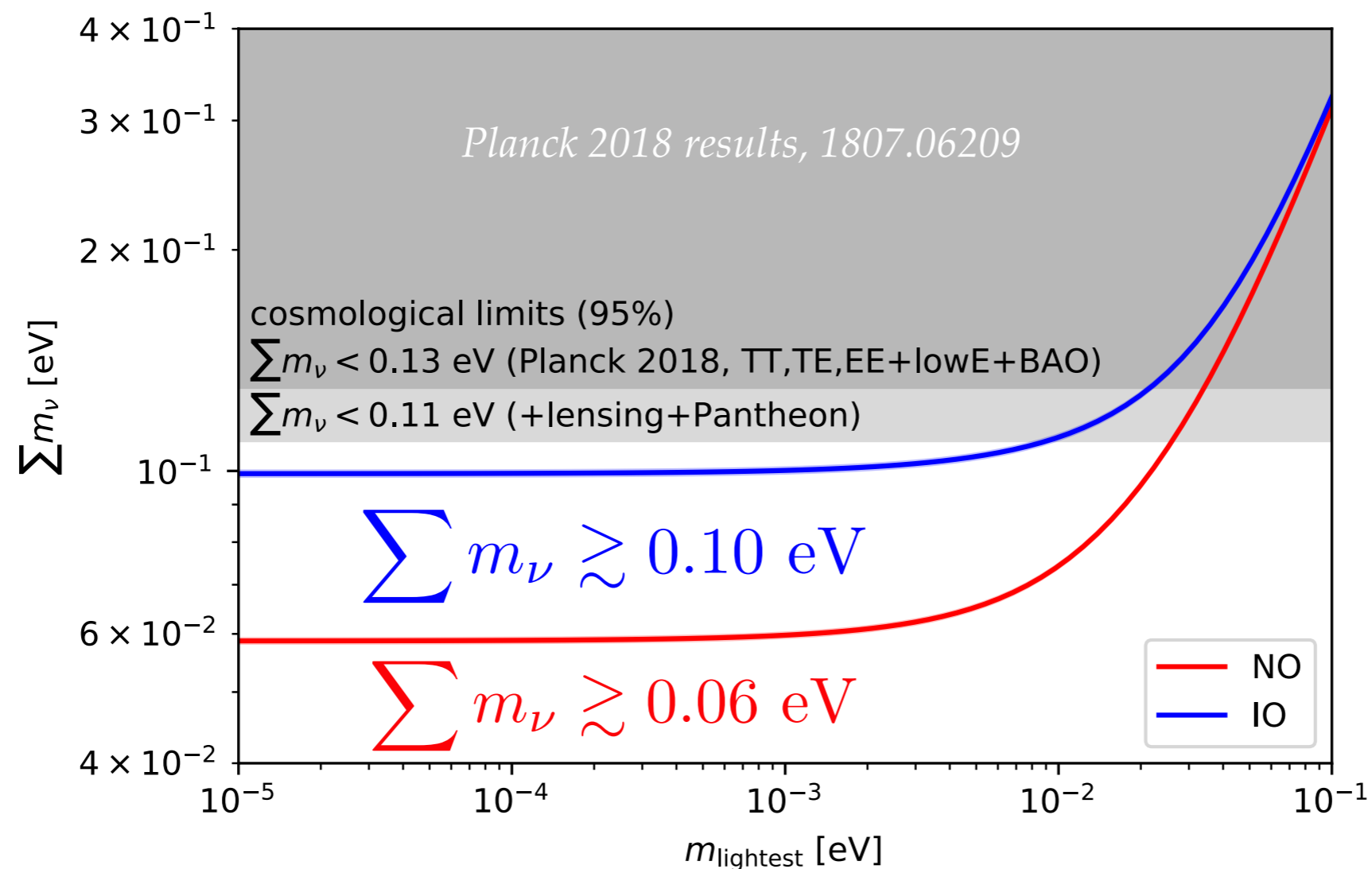
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which translates into a lower bound on the total neutrino mass, depending on the ordering:





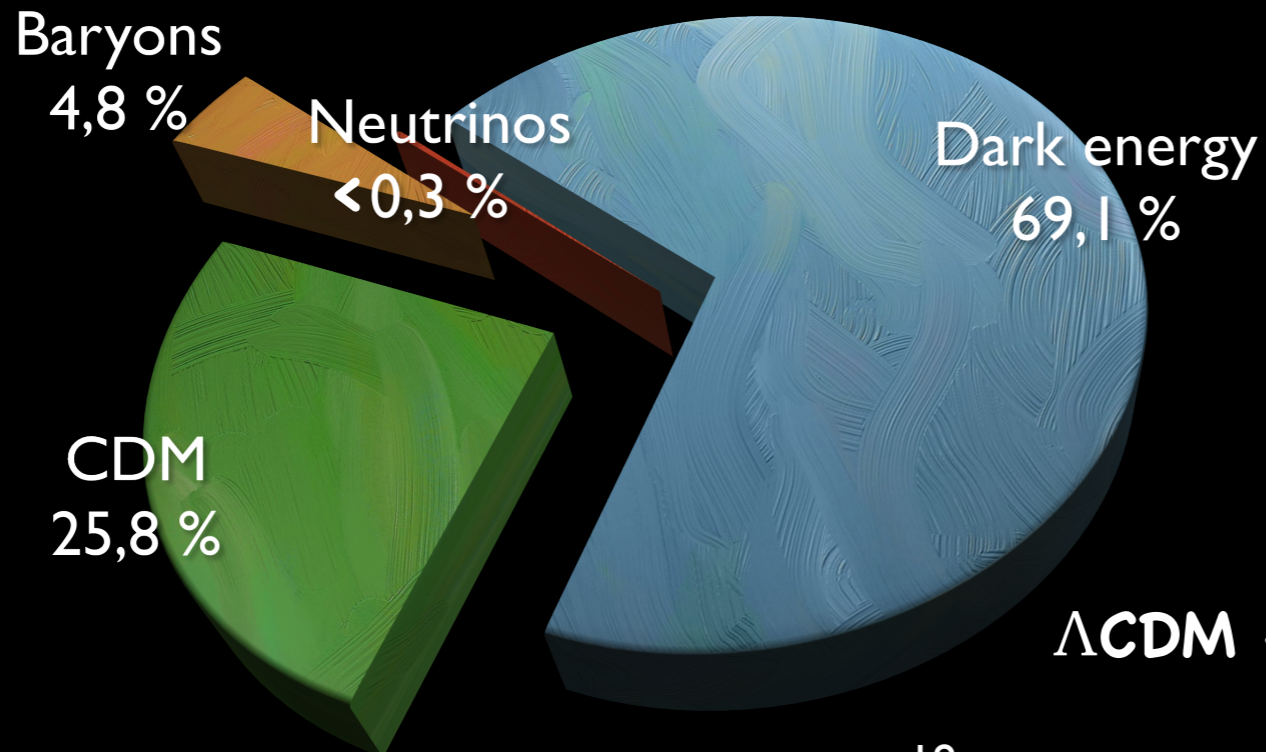
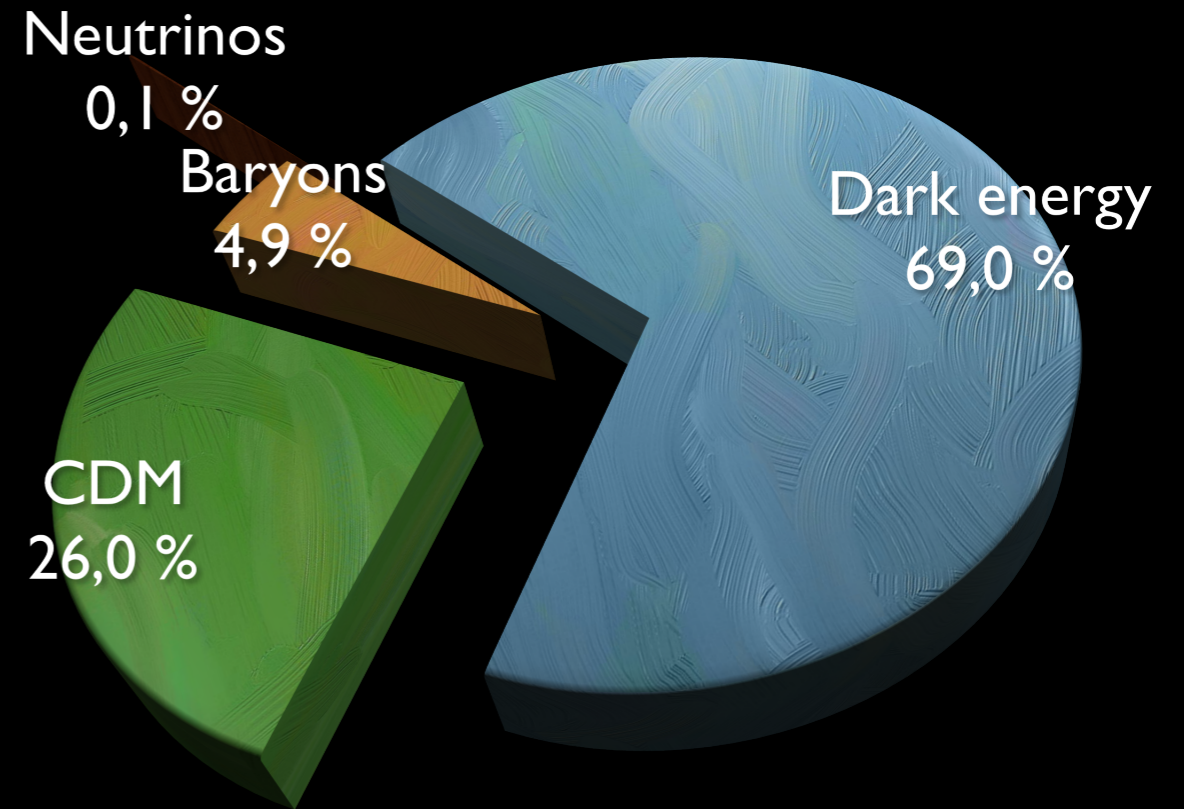
# Planck 2018 Cosmic Pizzas



# Planck 2018 Cosmic Pizzas

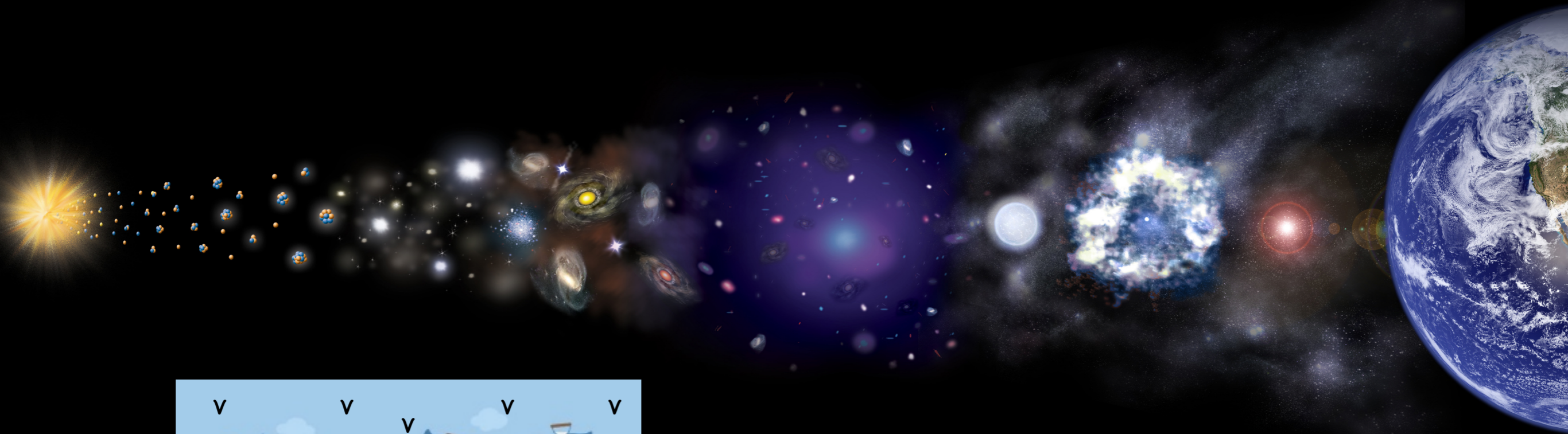
Planck 2018 results, 1807.06209

$$\Lambda\text{CDM} + \Sigma m_{\nu, \text{fiducial}} = 0.06 \text{ eV}$$



$$\Lambda\text{CDM} + \Sigma m_{\nu, \text{fiducial}} < 0.12 \text{ eV @95\% CL}$$

To hunt and bound their abundances and their masses, we need to look at several epochs in our universe's evolution:



and it's as challenging as trapping time!

Are you willing to join me in the  
Cosmo neutrino hunting trip?



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# Number of neutrinos: $N_{\text{eff}}$

The total radiation in the universe can be written as:

$$\Omega_r h^2 = \left( 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right) \Omega_\gamma h^2$$

$N_{\text{eff}} = 3.046$  standard scenario: electron, muon and tau neutrinos

$N_{\text{eff}} < 3.046$  (less neutrinos): Neutrino decays ?

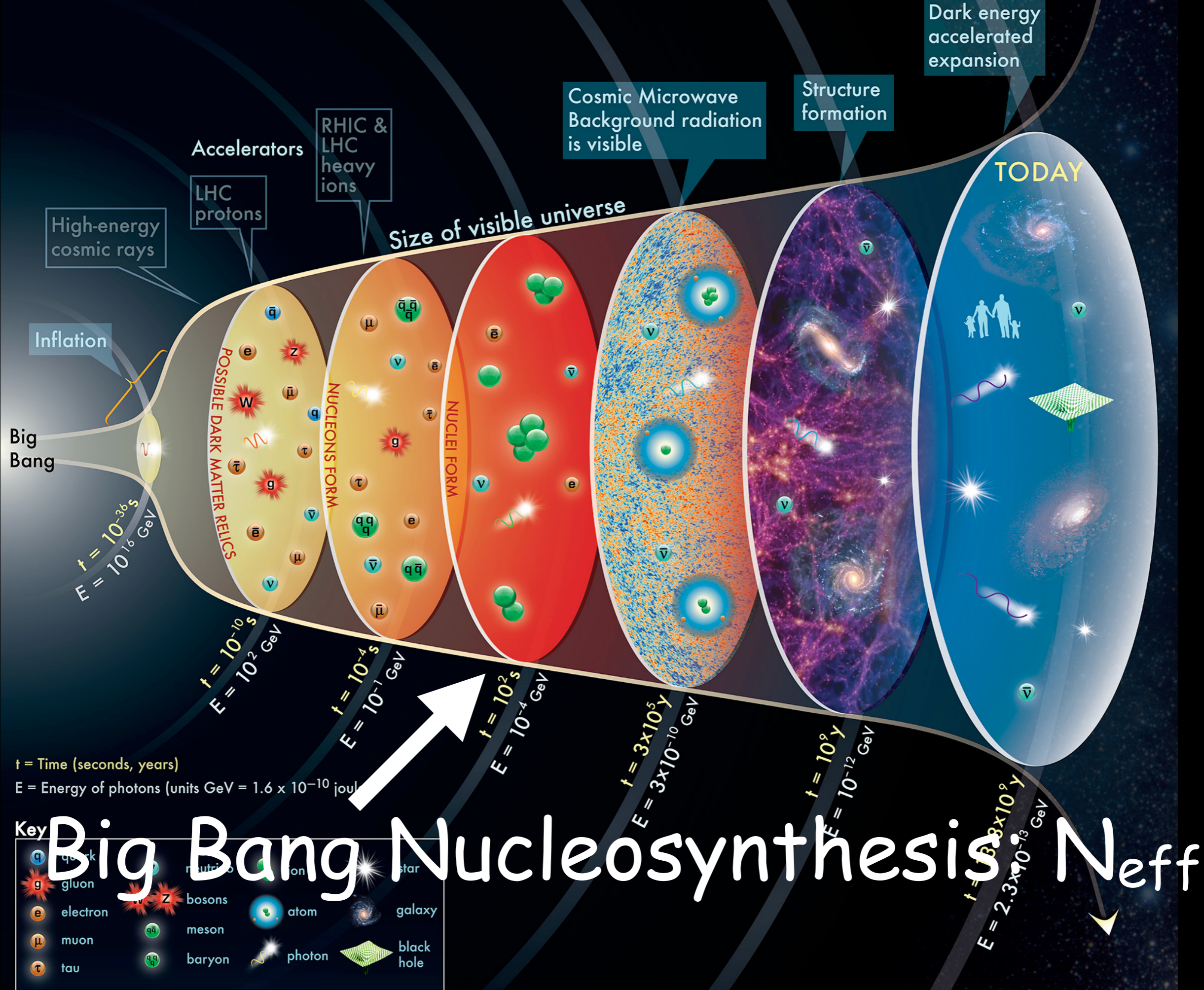
$N_{\text{eff}} > 3.046$  (more neutrinos): Sterile neutrino species ?

*But...if they are sterile, and do not interact with other particles, how cosmologists measure them?*



*That's the dark side of the GRAVITATIONAL FORCE...*





Event	Time	Redshift	Temperature
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# Big Bang Nucleosynthesis: $N_{\text{eff}}$

BBN theory predicts the abundances of D,  $^3\text{He}$ ,  $^4\text{He}$  and  $^7\text{Li}$  which are fixed by  $t \approx 180$  s. They are observed at late times: low metallicity sites with little evolution are “ideal”.

# Big Bang Nucleosynthesis: $N_{\text{eff}}$

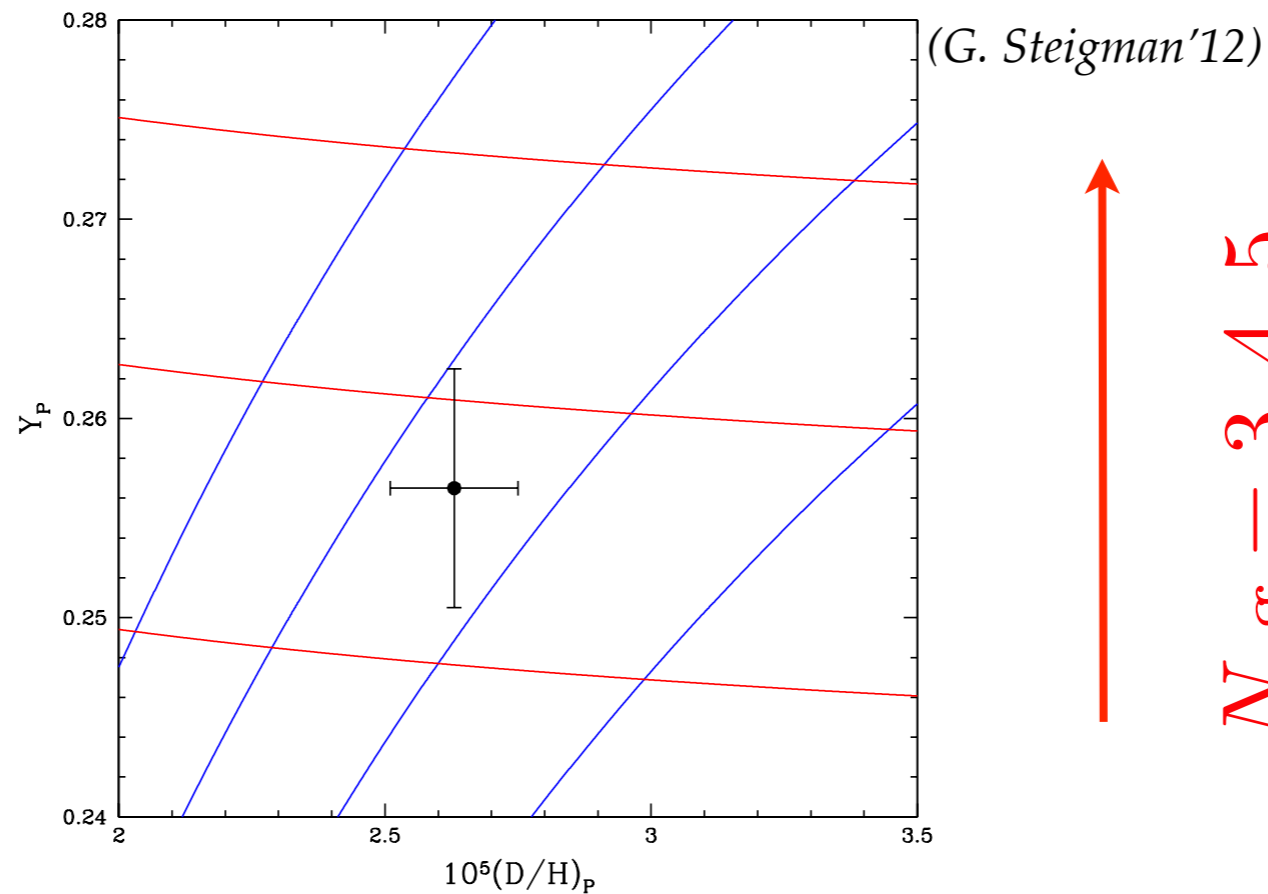
$N_{\text{eff}}$  changes the freeze out temperature of weak interactions:

$$\Gamma_{n \leftrightarrow p} \sim H$$

**MORE NEUTRINOS:**

Higher  $N_{\text{eff}}$ : larger expansion rate & freeze out temperature, **MORE HELIUM 4**

$$n/p \simeq e^{-\frac{m_n - m_p}{T_{\text{freeze}}}} \quad Y_p = \frac{2(n/p)}{1 + n/p}$$



# Today's menu

## Antipasto

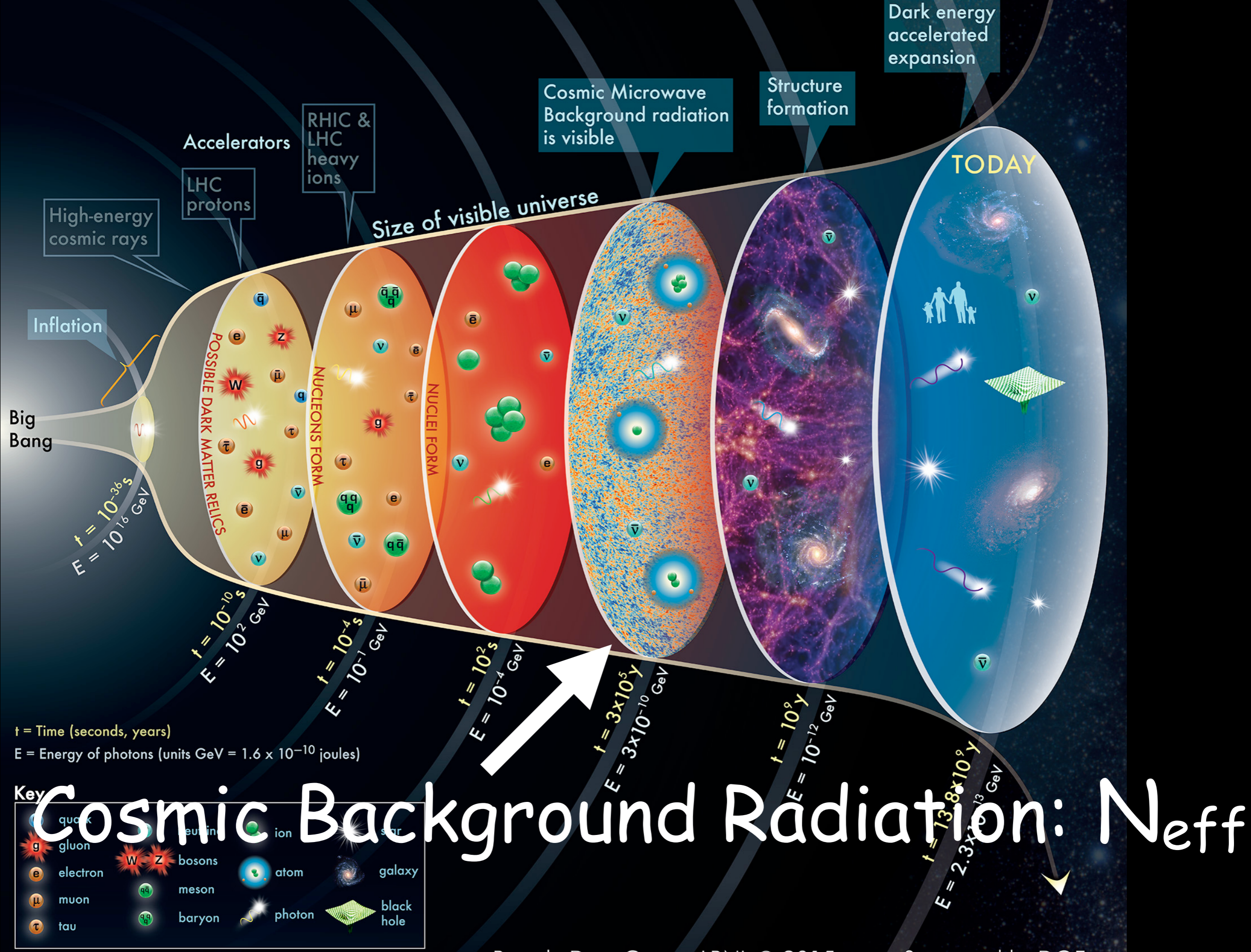
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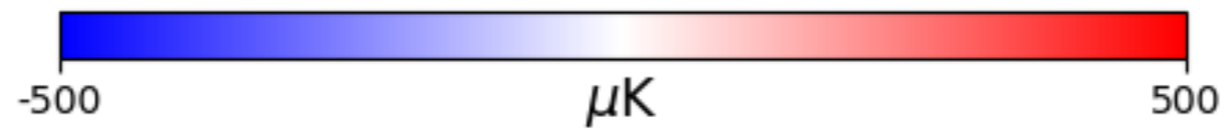
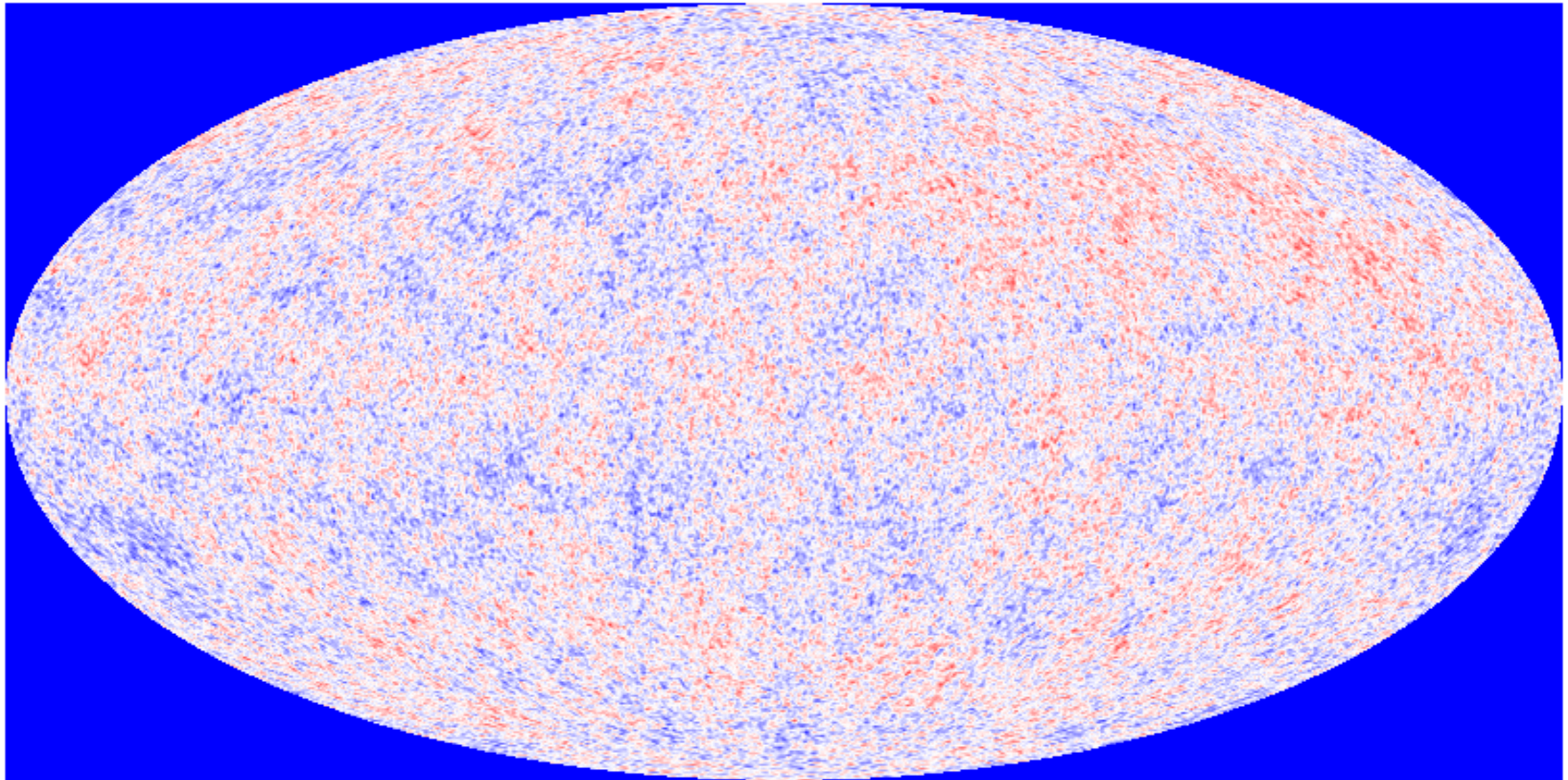
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Also known as "photon decoupling", as photons started freely travel through the universe without interacting with matter and the CMB is "frozen"

# CMB: $N_{\text{eff}}$

67.31\_0.02222\_0.1197\_0.078\_3.089\_0.9655\_3.046\_0 map



# CMB: $N_{\text{eff}}$

Spherical harmonics decomposition:

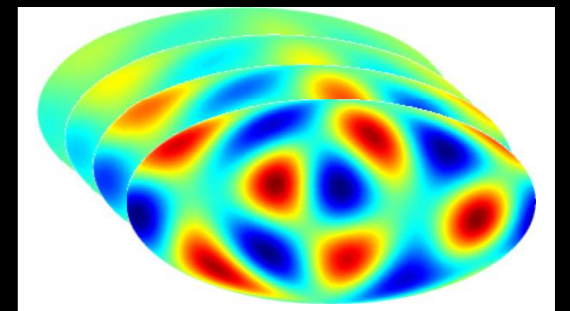
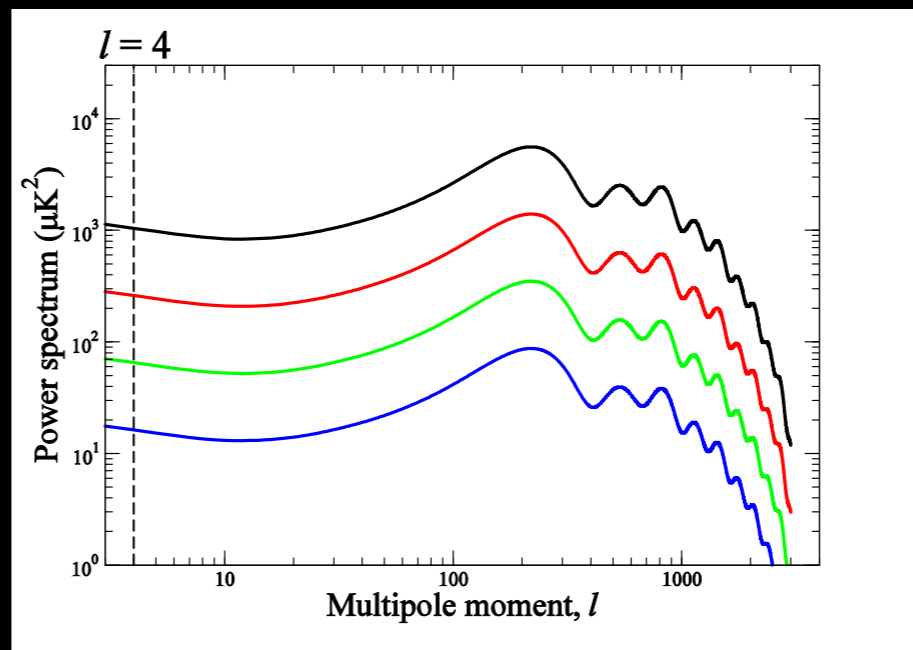
$$T(\hat{n}) = \sum_{\ell=0}^{\ell_{\text{max}}} \sum_{m=-\ell}^{\ell} a_{\ell m} Y_{\ell m}(\hat{n})$$

With expansion coefficients:

$$a_{\ell m} = \int_{4\pi} T(\hat{n}) Y_{\ell m}^*(\hat{n}) d\Omega$$

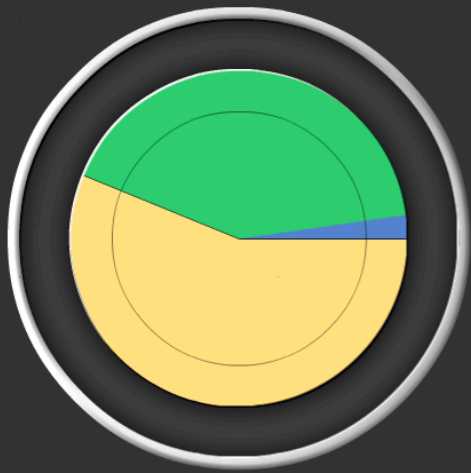
The angular power spectrum measures the amplitude as a function of the wavelength:

$$C_{\ell} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell m}|^2$$



# CMB: Neff

## CMB Analyzer



Universe Content

Atoms

100 %

Cold Dark Matter

74 %

Dark Energy

4 %

### Additional Properties

Hubble Constant

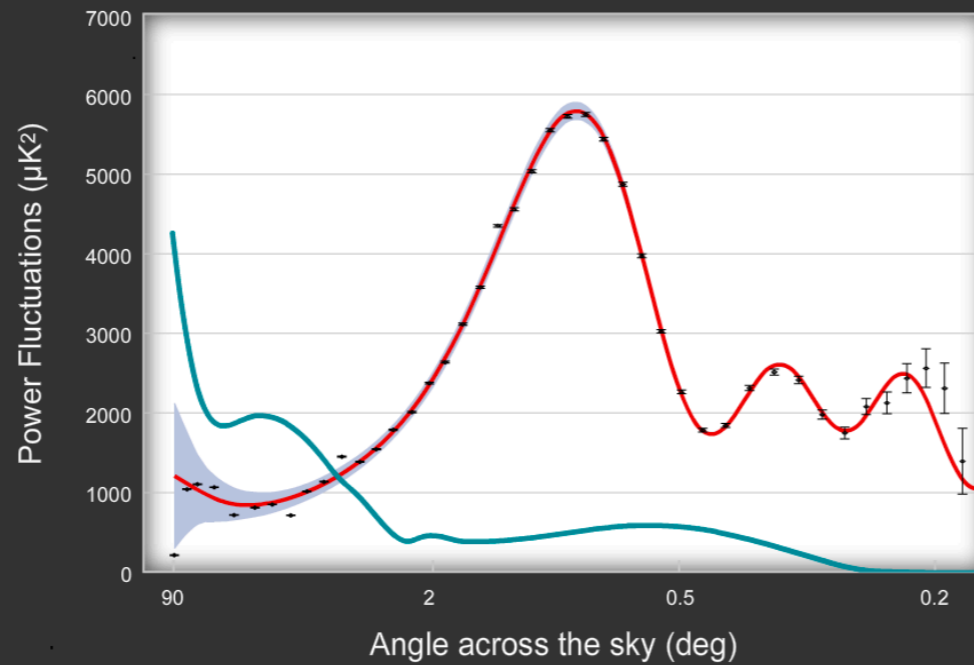
84

Reionization redshift

22

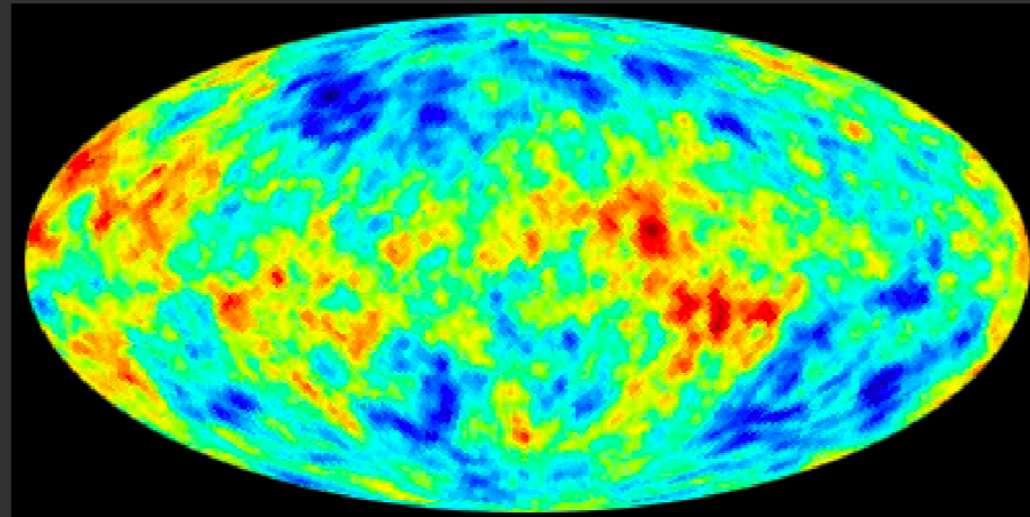
Spectral Index

0.8



**Pie Chart:** Graphically shows the composition of your universe. The wedges compare the amount of each component; the size of the pie compares the total composition (matter + dark matter + dark energy) with the critical density (black circle).

- A universe at critical density is geometrically flat and probably infinite.
- A universe can have more or less than the critical density.
- Flatness - the term we use for closeness to critical density.



**Age:** 6.9 billion years

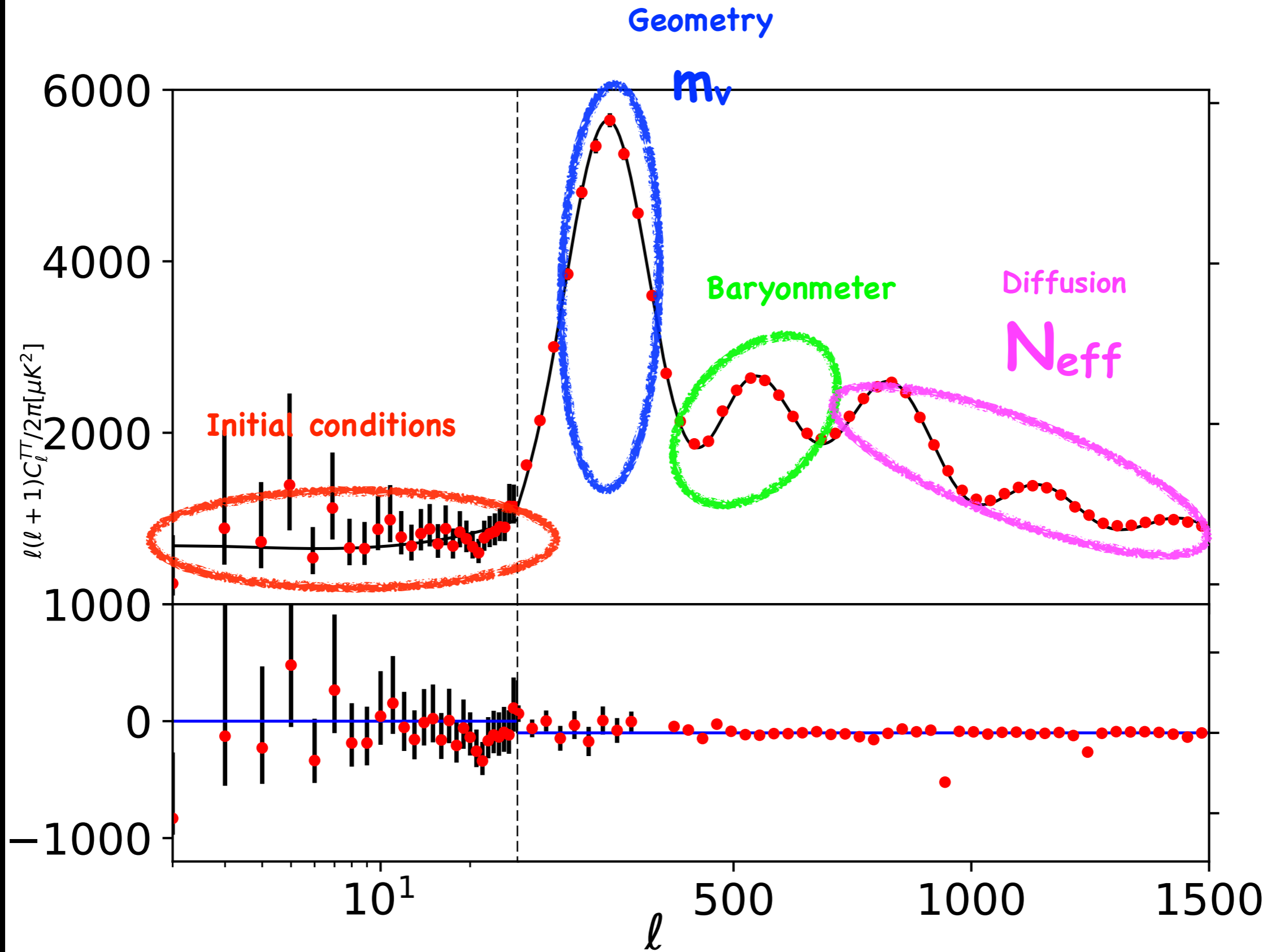
**Flatness:** 1.7

ANSWER

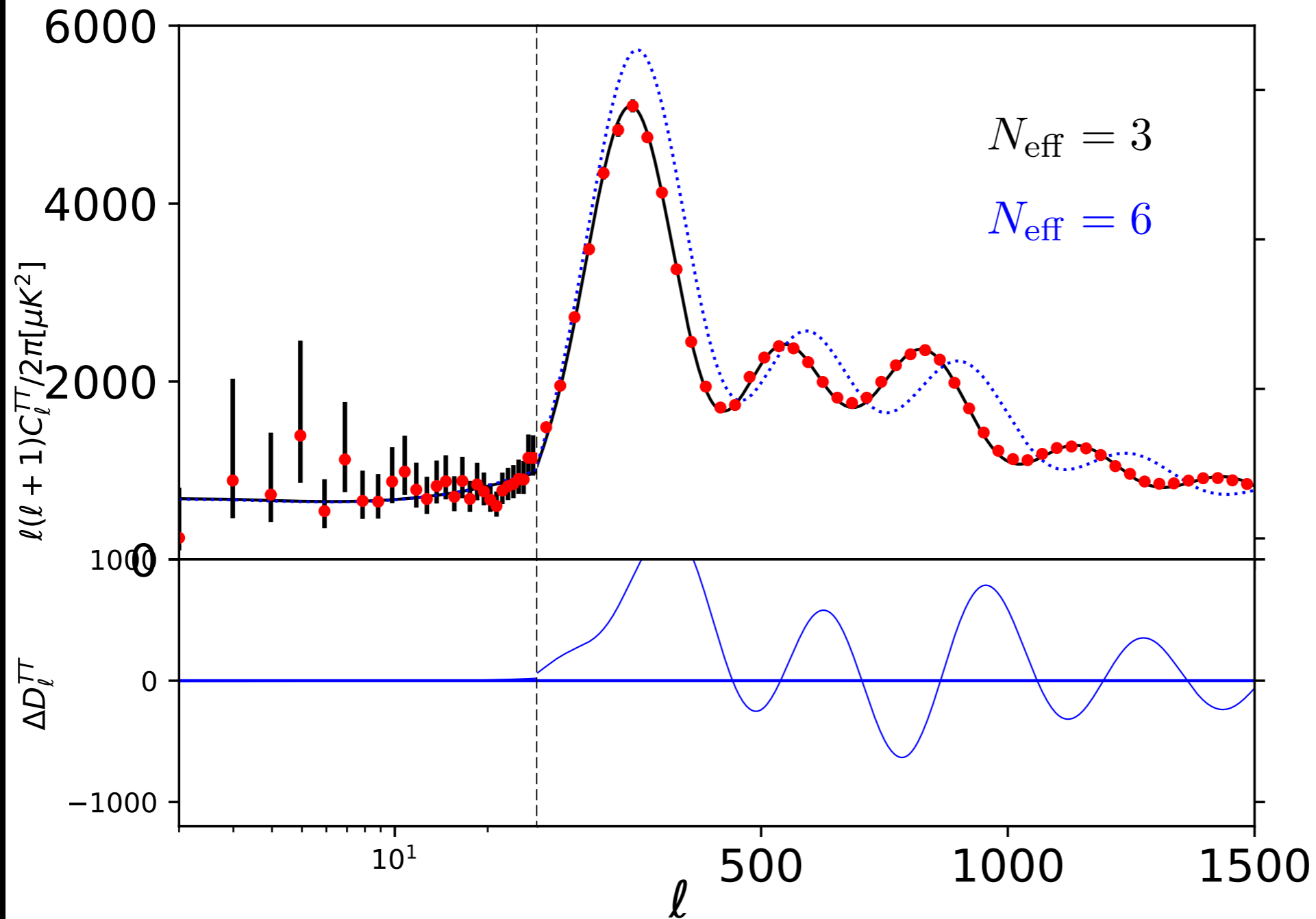
RESET



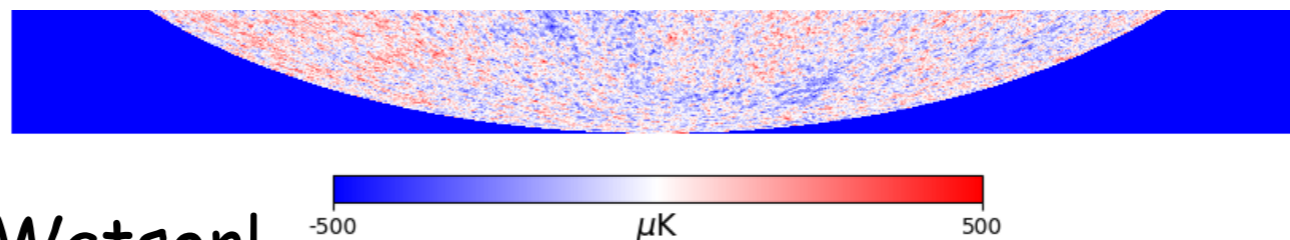
# CMB: a lot to learn about...



# CMB: $N_{\text{eff}}$



Elementary, my dear Watson!



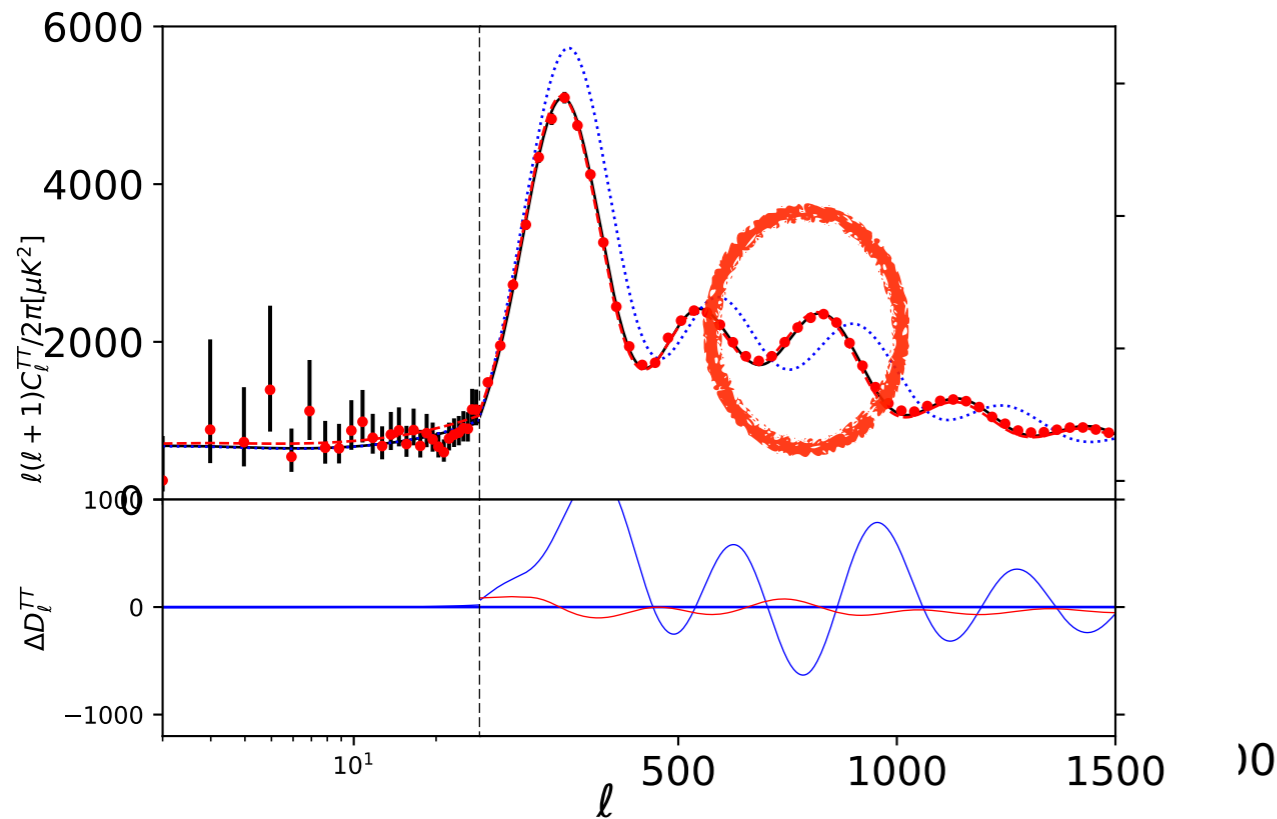
# CMB: $N_{\text{eff}}$

$$N_{\text{eff}} = 6 \quad N_{\text{eff}} = 3 \quad N_{\text{eff}} = 6$$

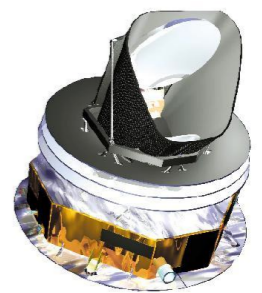
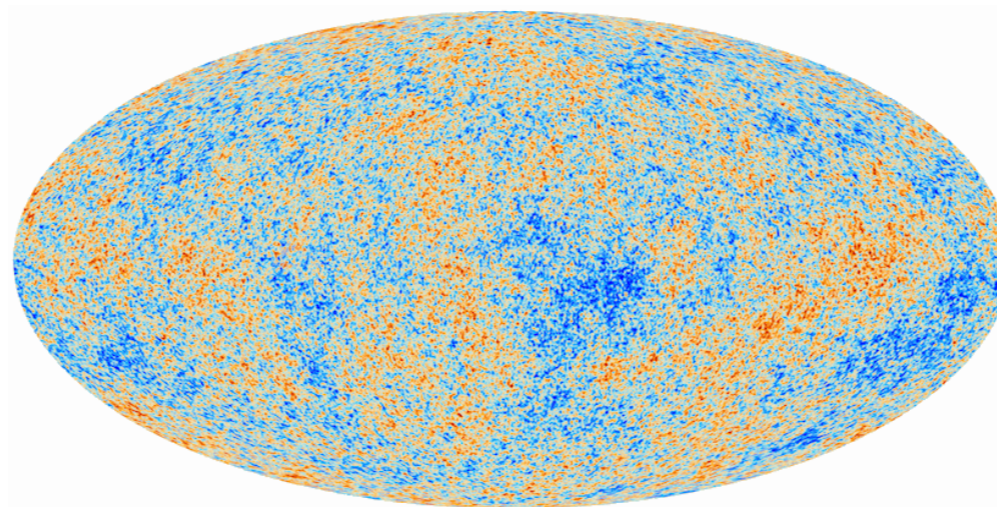
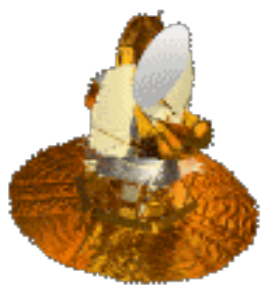
$$(\omega_b, \omega_m, h, A_s, n_s, \tau, N_{\text{eff}})$$

**Warning!**

It is elementary, Sherlock Holmes!



Only effect at  $\ell < 1000$  that can not be mimicked by others: anisotropic stress, around 3<sup>rd</sup> peak



Neutrinos are free-streaming particles propagating at the speed of light, faster than the sound speed in the photon fluid, suppressing the oscillation amplitude of CMB modes that entered the horizon in the radiation epoch.

# CMB: $N_{\text{eff}}$

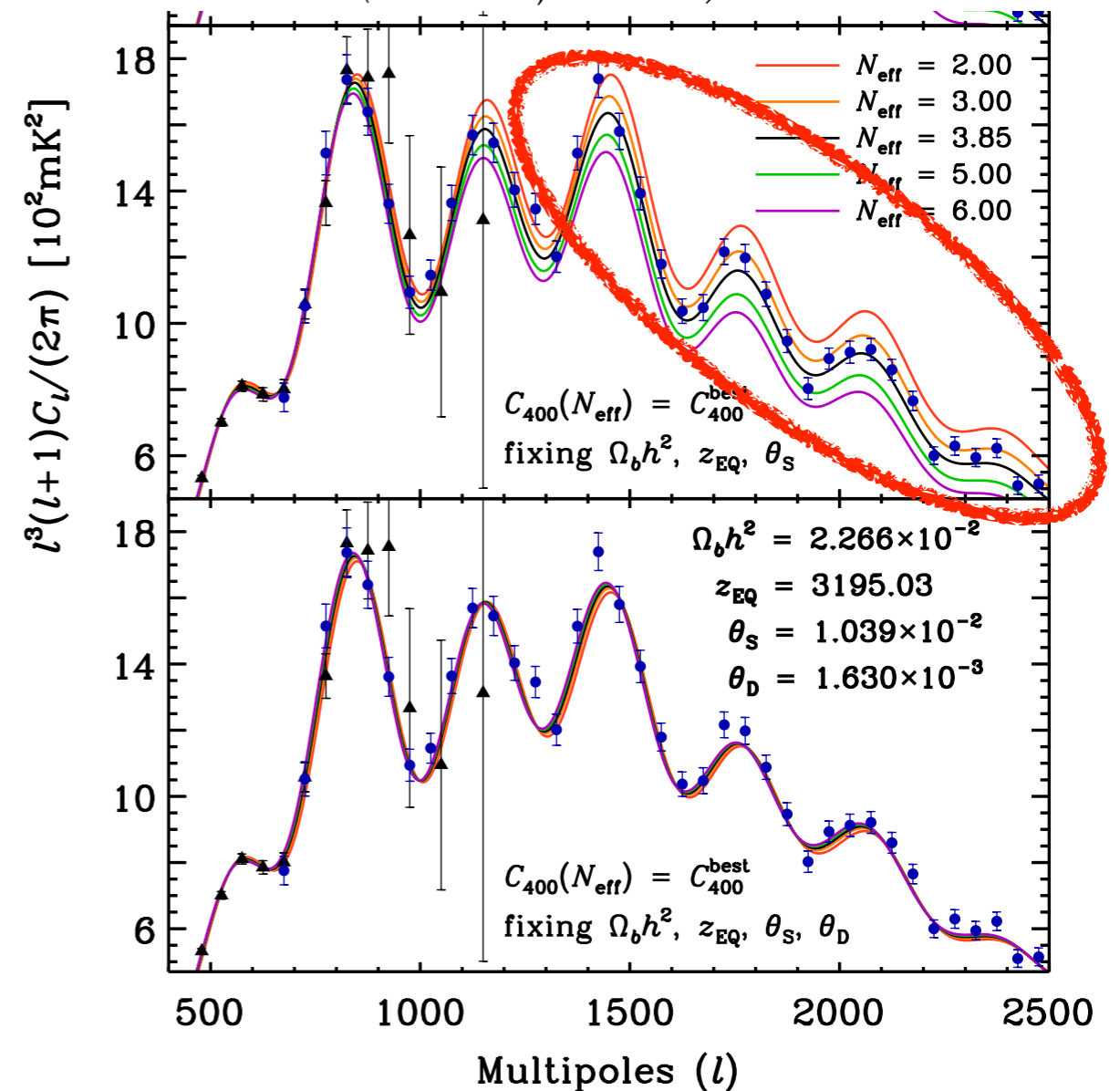
@Cosmic Microwave Background in the damping tail, measured by SPT, ACT & Planck:

Higher  $N_{\text{eff}}$  will increase the expansion rate AND the damping at high multipoles.



$$r_d^2 \propto \int_0^{a_*} \frac{da}{a^3 \sigma_T n_e H}$$

(Hou et al, PRD'13)



# $N_{\text{eff}}$

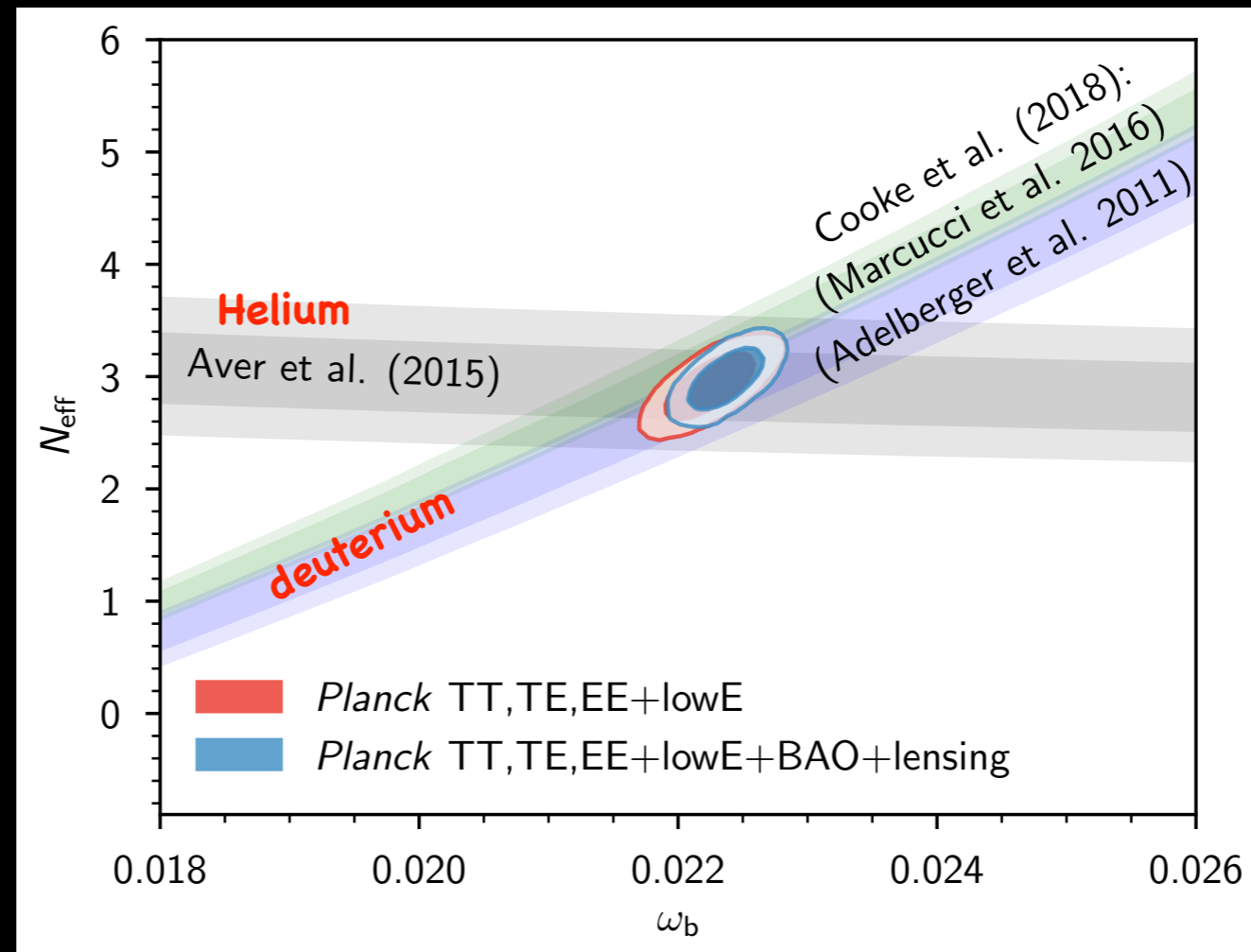
- Planck 2018 CMB temperature polarization and lensing potential data:

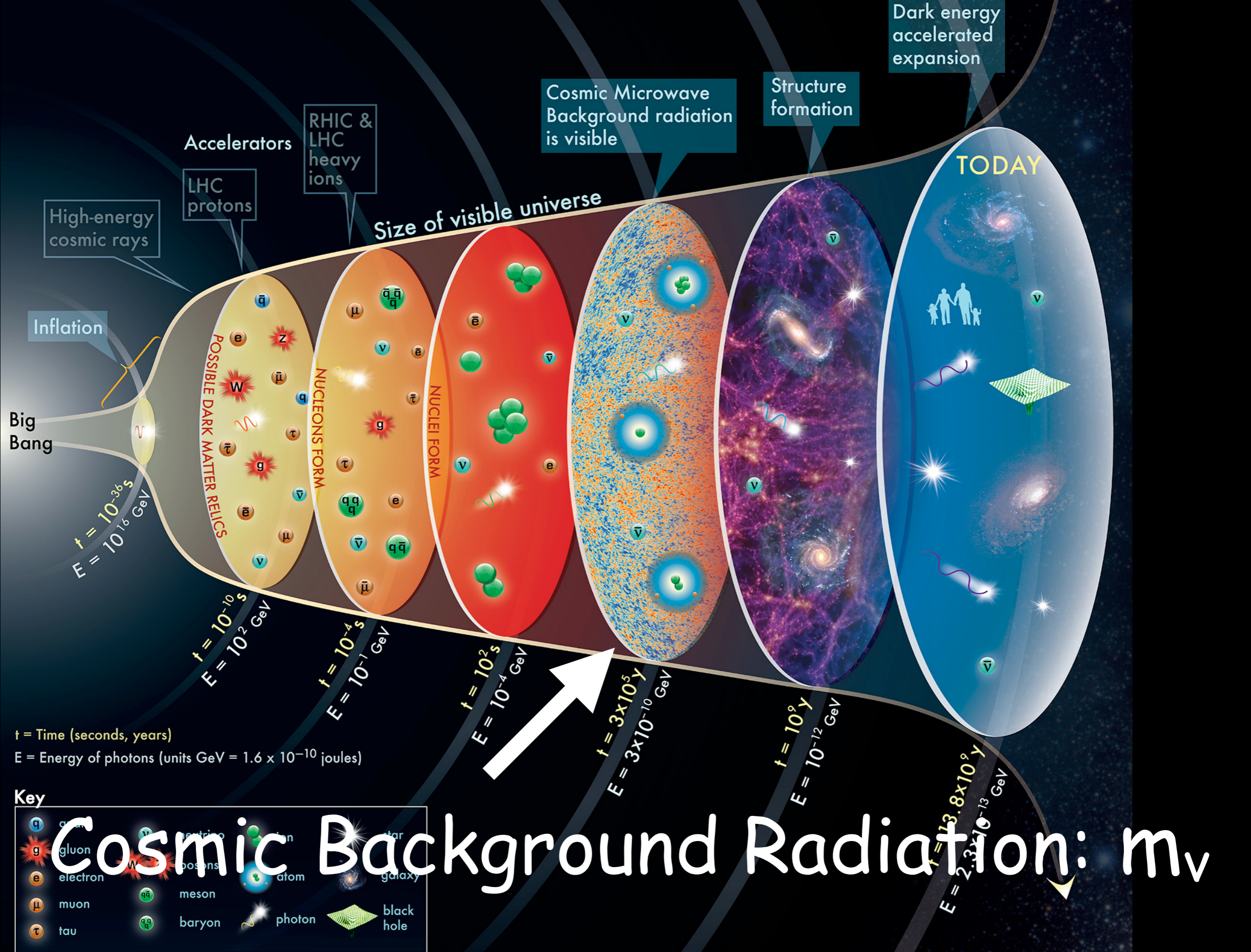
$$N_{\text{eff}} = 2.89^{+0.36}_{-0.38} \text{ 95\%CL}$$

- If we add large scale structure information in the BAO shape form:

$$N_{\text{eff}} = 2.99^{+0.34}_{-0.33} \text{ 95\%CL}$$

- Perfectly consistent with BBN estimates:





The concept for the above figure originated in a 1986 paper by Michael Turner.

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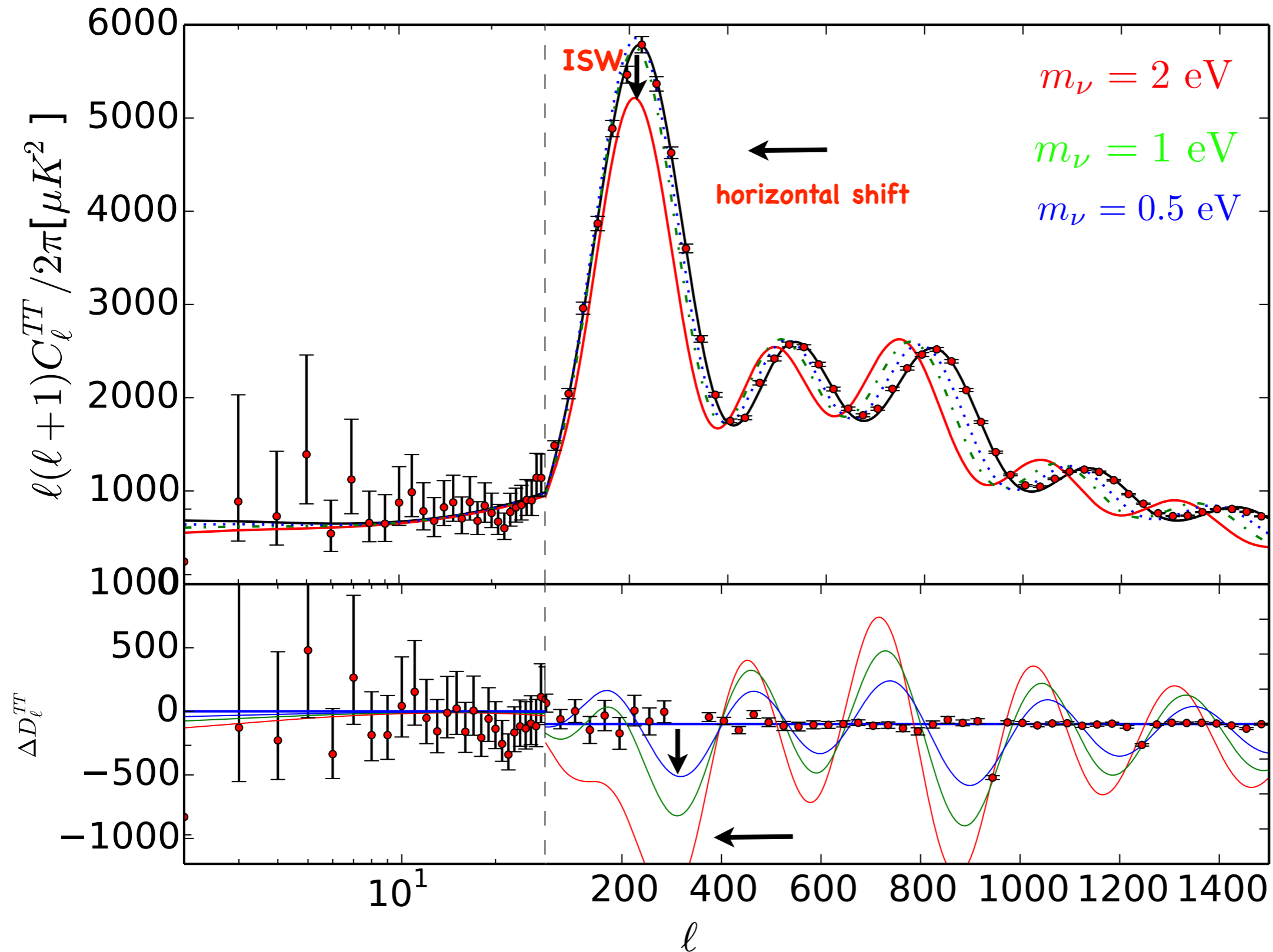
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- Take home messages

# CMB: $\Sigma m_\nu$

@ CMB: Early Integrated Sachs Wolfe effect (ISW).

Shift in the angular position of the peaks.



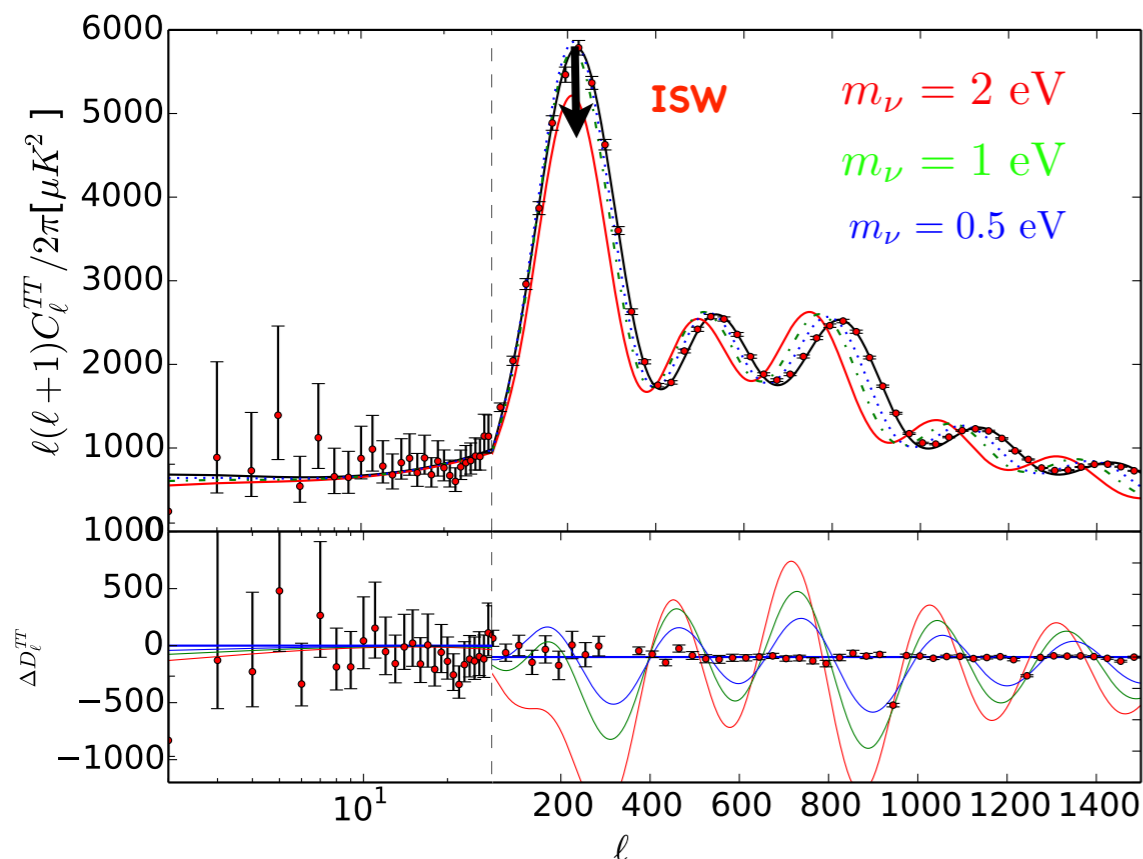


# CMB: $\Sigma m_\nu$

@ CMB: Early Integrated Sachs Wolfe effect (ISW)

$$\Theta(\hat{n}) = \frac{\delta T}{T}(\hat{n}) \simeq \Theta_0 + \Psi + \hat{n}(\hat{v}_e - v) + \int \dot{\Psi} + \dot{\Phi} d\eta$$

In matter domination, the gravitational potential is constant: **NO ISW effect!**  
 The transition **from the relativistic to the non relativistic neutrino regime** gets imprinted in the decays of the gravitational potentials near the recombination period, **contributing to the ISW effect!**



This early ISW effect leads to a depletion of:

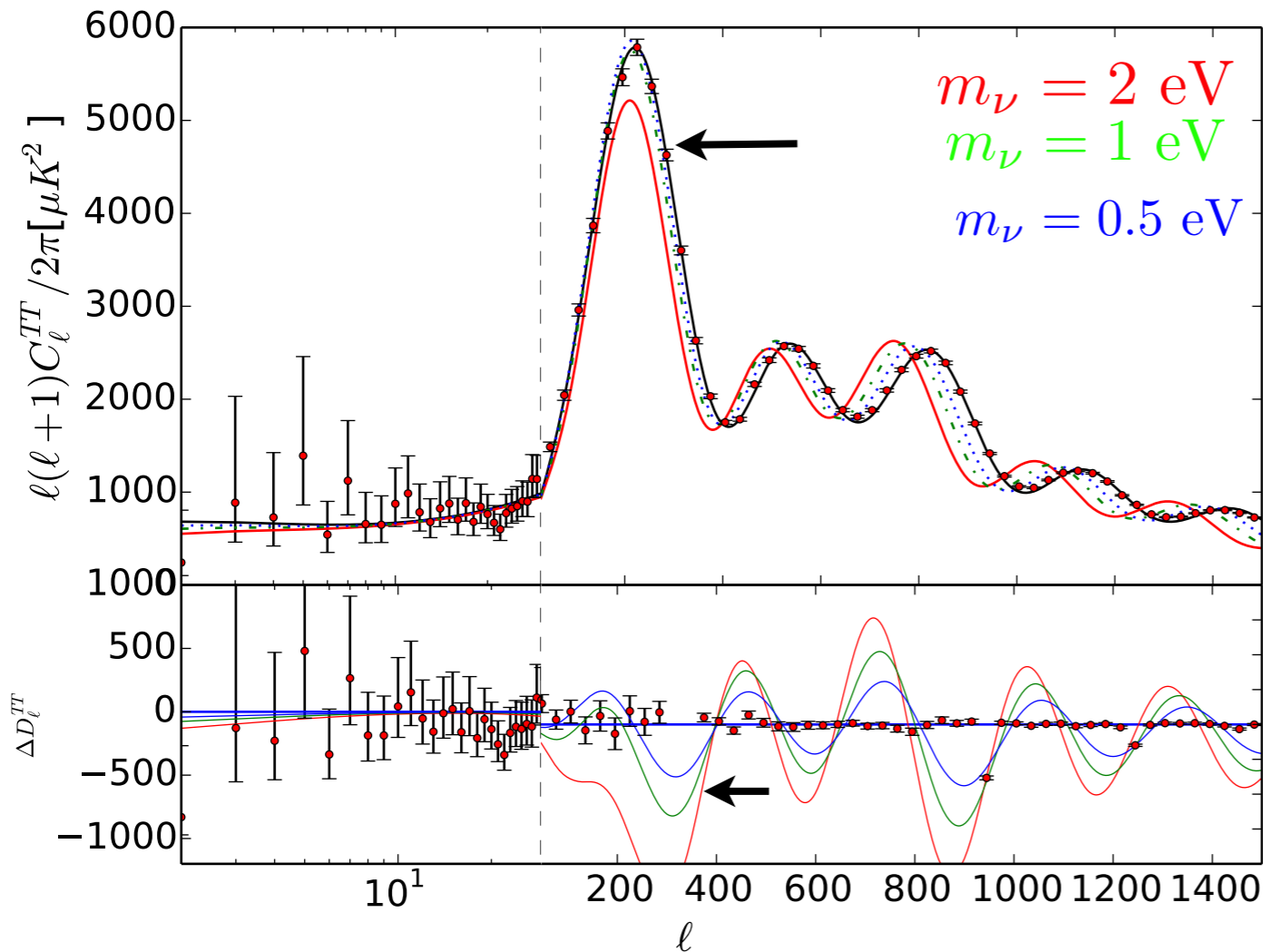
$$\frac{\Delta C_\ell}{C_\ell} = -\left(\sum m_\nu / 0.1 \text{ eV}\right)\%$$

on multipoles:

$$20 < \ell < 200$$

# CMB: $\Sigma m_\nu$

@ CMB: Early Integrated Sachs Wolfe effect (ISW).  
**Shift in the angular position of the peaks.**



$$\theta_s = \frac{r_s}{D_A}$$

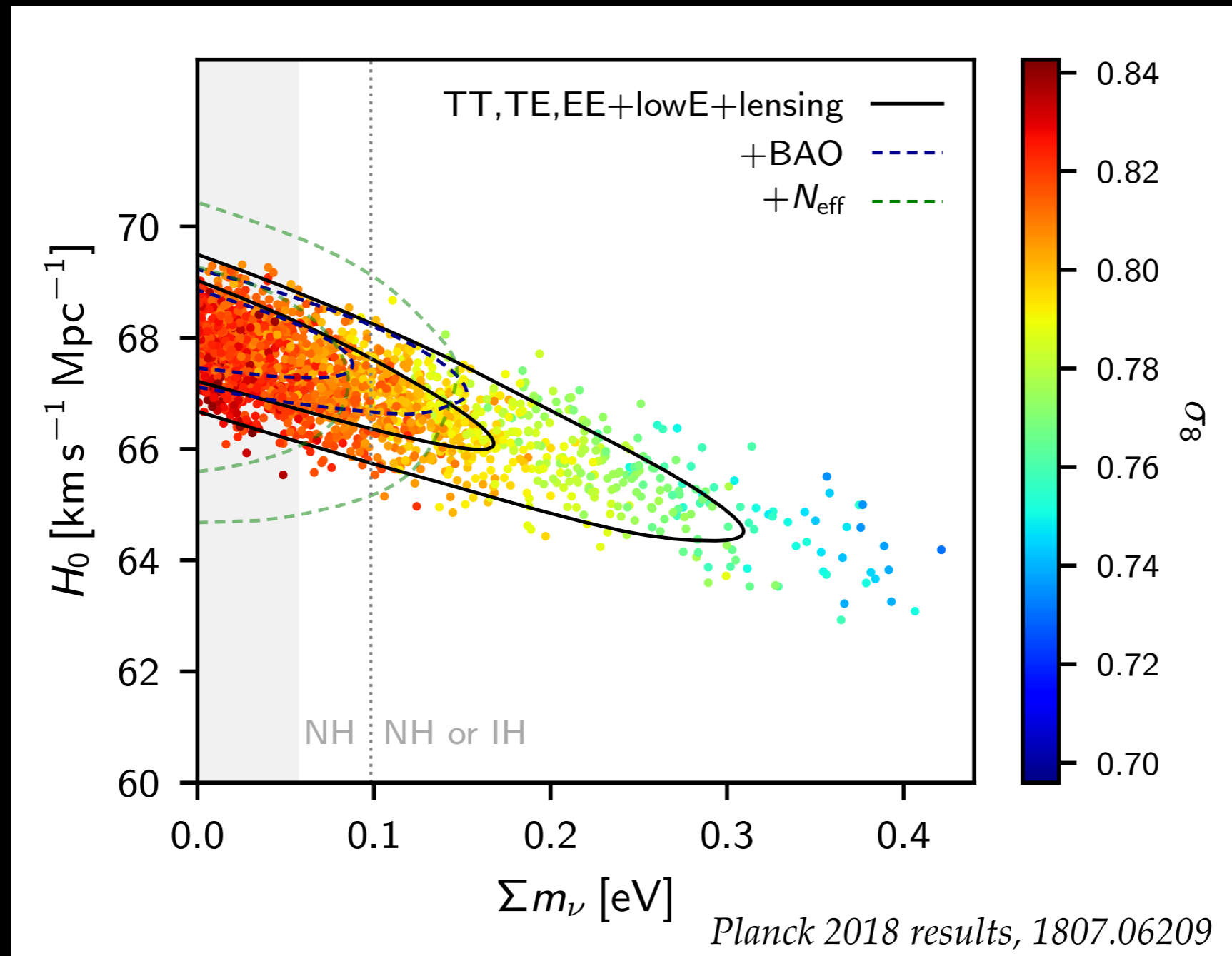
$$r_s = \int_0^{t(z_d)} c_s (1+z) dt = \frac{2}{3k_{\text{eq}}} \sqrt{\frac{6}{R_{\text{eq}}}} \ln \frac{\sqrt{1+R_d} + \sqrt{R_d + R_{\text{eq}}}}{1 + \sqrt{R_{\text{eq}}}}$$

$$D_A = \int_0^{z_{\text{rec}}} \frac{dz}{H(z)}$$

The higher the neutrino mass, the lower the angular diameter distance.

Peaks shift to lower multipoles. But this effect can be compensated with a lower Hubble constant:

**Strong degeneracy between  $\Sigma m_\nu$  and the Hubble constant  $H_0$ !**



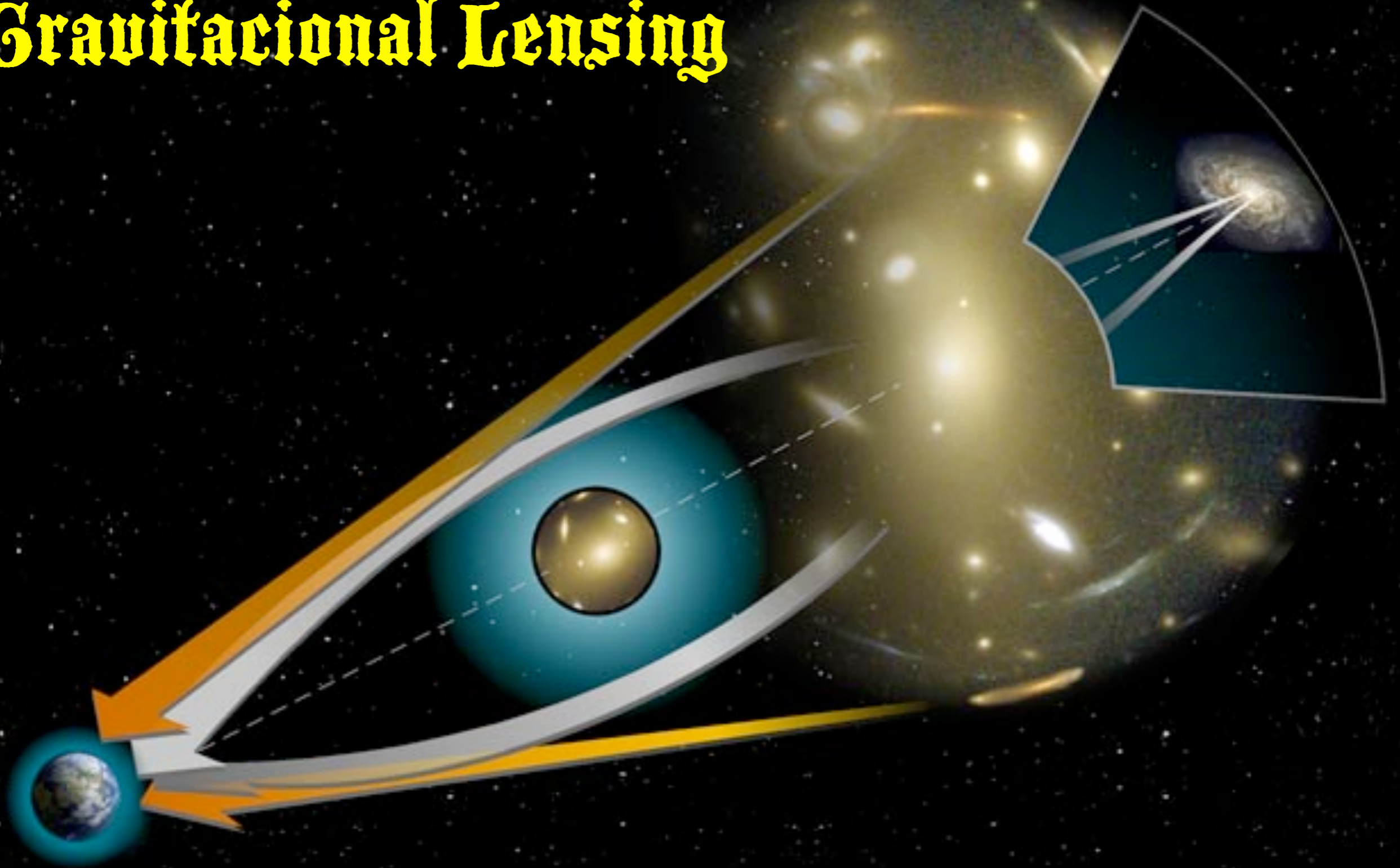
**Strong degeneracy between  $\Sigma m_\nu$  and the Hubble constant  $H_0$ !**

# CMB: $\Sigma m_\nu$

@ CMB: Early Integrated Sachs Wolfe effect (ISW).  
Shift in the angular position of the peaks.

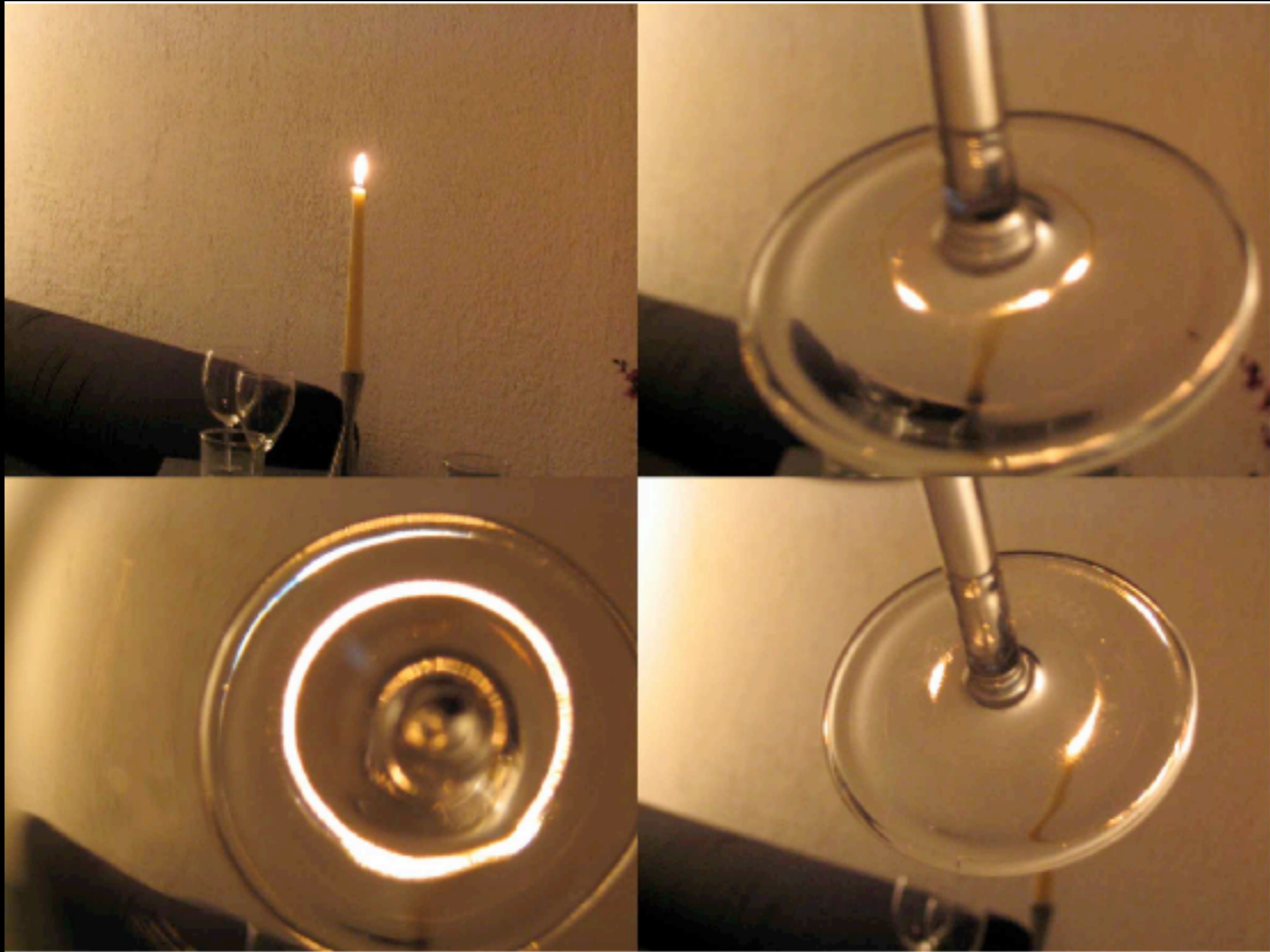


# Gravitational Lensing



Einstein's relativity predicts that the presence of a massive body will curve space time, distorting the light trajectory. The shape of the background objects will change/multiplied by the presence of intervening galaxies.

# Gravitational Lensing



Einstein rings: Perfect alignment

Syzygy!

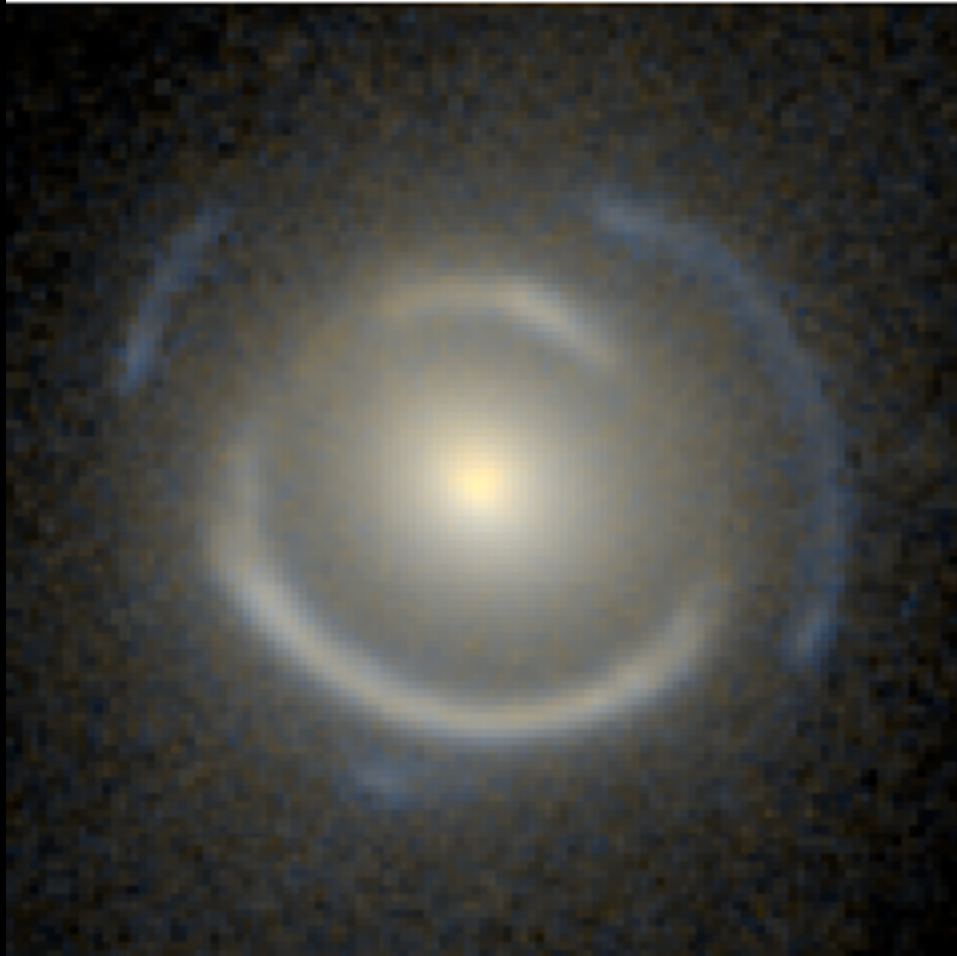
Lensing Galaxy



This movie shows a spiral galaxy acting as a lense of a background quasar (Quasi-stellar radio source) moving behind the galaxy. When the alignment source-lens-observer is perfect, we see the formation of the Einstein ring!

# Gravitational Lensing

SDSSJ0946+1006



**Double Einstein ring! 3 perfectly aligned galaxies (probably less than 100 cases in all the universe, and we have observed one!)**



# CMB Lensing: $\Sigma m_\nu$

Lensing remaps the CMB fluctuations:

$$\Theta_{\text{lensed}}(\hat{n}) = \Theta(\hat{n} + \nabla\phi(\hat{n}))$$

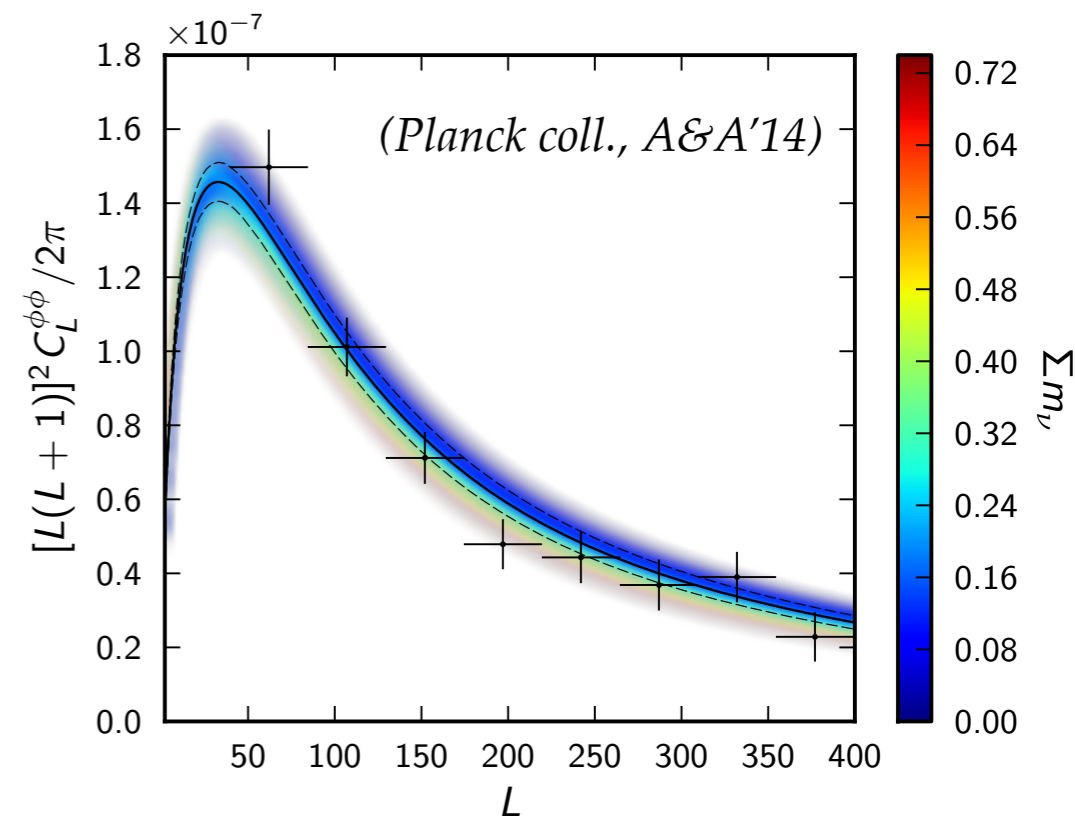
Lensing potential  $\phi$  is a measure of the integrated mass distribution back to the last scattering surface

$$\phi(\hat{n}) = -2 \int_0^{z_{\text{rec}}} \frac{dz}{H(z)} \underbrace{\Psi(z, D(z)\hat{n})}_{\text{Matter distribution}} \underbrace{\left( \frac{D(z_{\text{rec}}) - D(z)}{D(z_{\text{rec}})D(z)} \right)}_{\text{Geometry}}$$

$$C_L^{\phi\phi} = \frac{8\pi^2}{L^3} \int_0^{z_{\text{rec}}} \frac{dz}{H(z)} D(z) \left( \frac{D(z_{\text{rec}}) - D(z)}{D(z_{\text{rec}})D(z)} \right)^2 P_\Psi(z, k = L/D(z))$$

Neutrino free-streaming implies less clustering on small scales, **reducing therefore CMB lensing!**

(Kaplinghat et al PRL'03, Lesgourgues et al, PRD'06)



Planck TTTEEE+lowT+lowE+lensing

$$\Sigma m_\nu < 0.24 \text{ eV } 95\% \text{ CL}$$

# Today's menu

## Antipasto

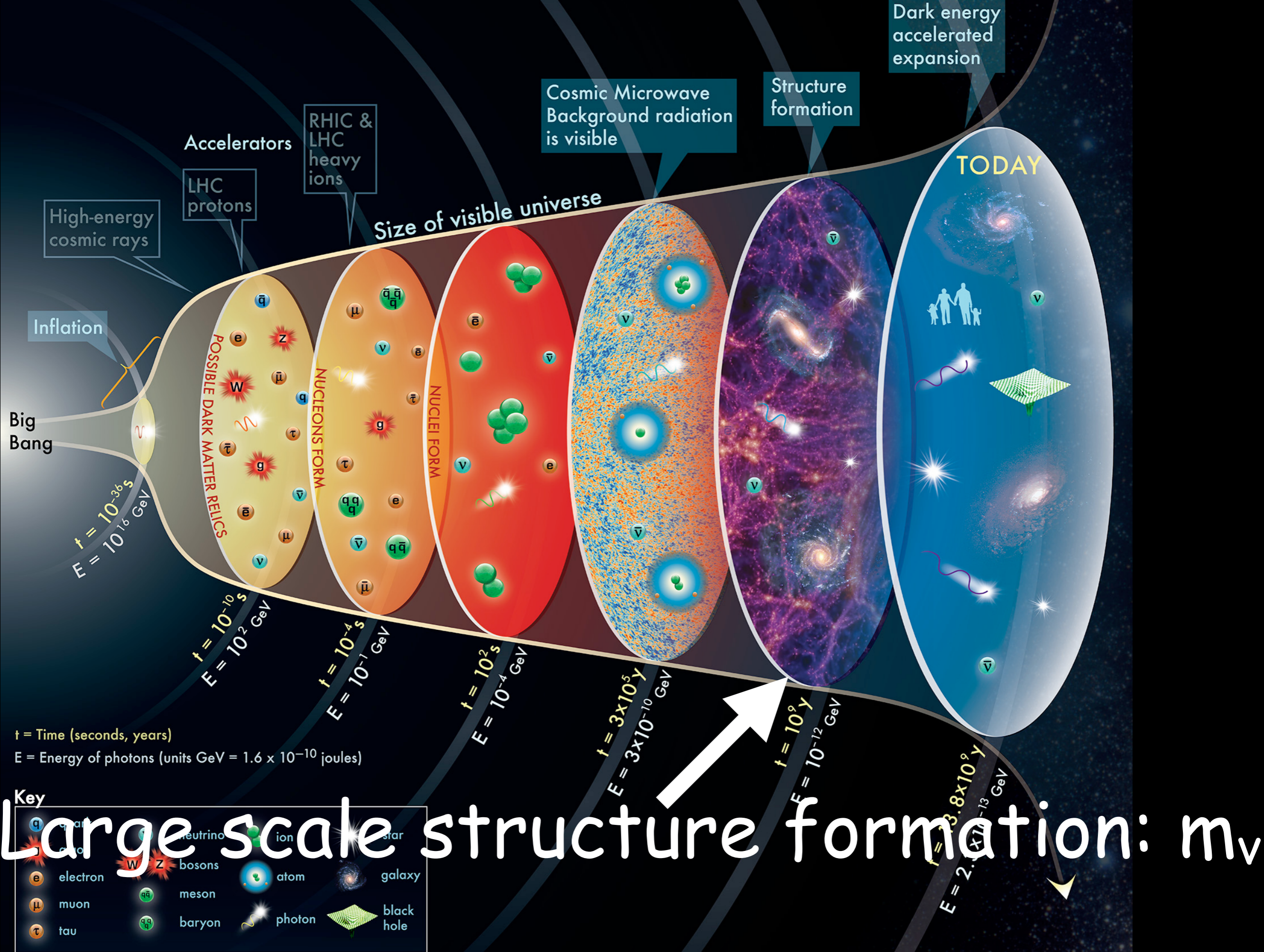
- The classical cosmic pizza
- The neutrino slice
- Neutrino decoupling in the early universe
- Other cosmic pizzas for tasting

## Main course

- Number of neutrinos and Big-Bang Nucleosynthesis
- Number of neutrinos and Cosmic Microwave Background Radiation
- Neutrino masses and Cosmic Microwave Background Radiation
- ● Neutrino masses and structure formation in the universe
- The Dark Justice League game:  $\Sigma m_\nu$  versus  $w(z)$

## Doggy Bag

- Take home messages



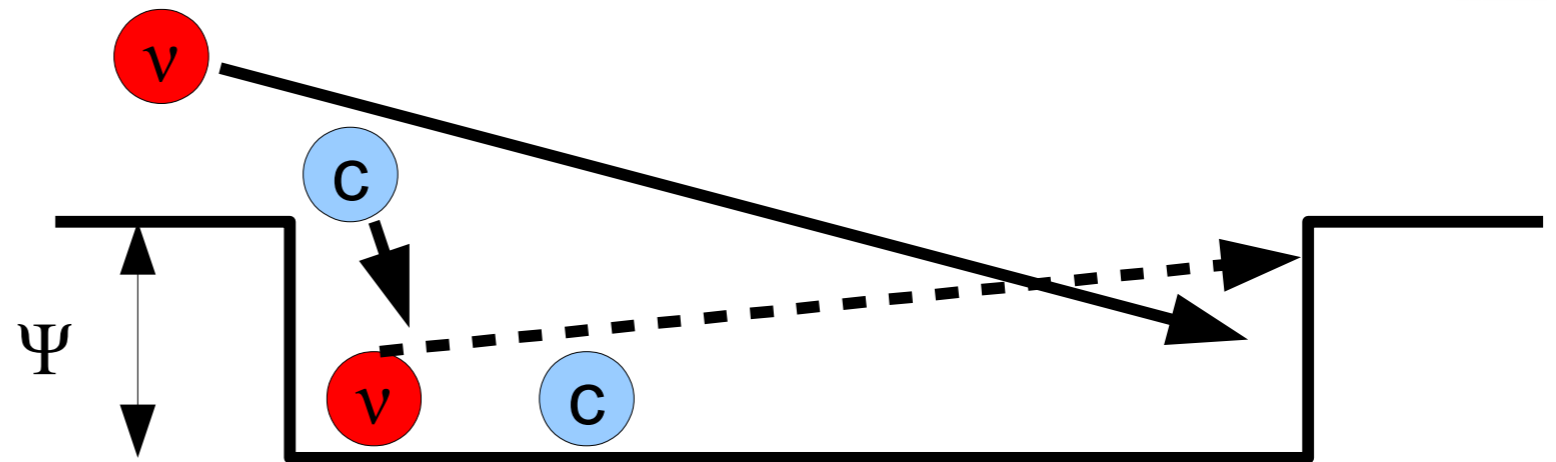
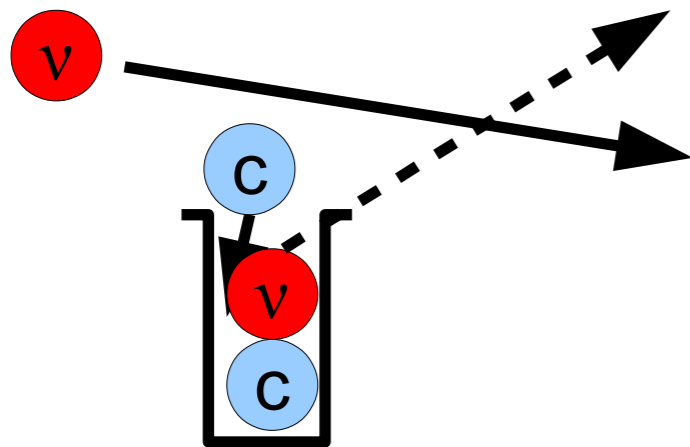
The concept for the above figure originated in a 1986 paper by Michael Turner.

# Large scale structure: $m_\nu$

Neutrino masses suppress structure formation on scales larger than their free streaming scale when they turn non relativistic. (*Bond et al PRL'80*)

Neutrinos with eV or sub-eV masses are **HOT** relics with **LARGE** thermal velocities!

Cold dark matter instead has zero velocity and therefore it clusters at any scale!



$$\lambda \ll \lambda_{fs,\nu} \rightarrow k \gg k_{fs,\nu}$$

$$\lambda \gg \lambda_{fs,\nu} \rightarrow k \ll k_{fs,\nu}$$



# Large scale structure: $m_\nu$

Growth equation for a single uncoupled fluid, linear regime, with constant sound speed:

$$\ddot{\delta} + \underbrace{2 \frac{\dot{a}}{a} \dot{\delta}}_{\text{Hubble drag}} - \underbrace{c_s^2 k^2 \frac{\delta}{a^2}}_{\text{Pressure}} = \underbrace{4\pi G \rho \delta}_{\text{Gravity}}$$

**Jeans scale:**

$$k_J \equiv \sqrt{\frac{4\pi G \rho}{c_s^2 (1+z)^2}}$$

$k > k_J$  no growth can occur

$k < k_J$  density perturbations growth

**Neutrino free streaming scale:**

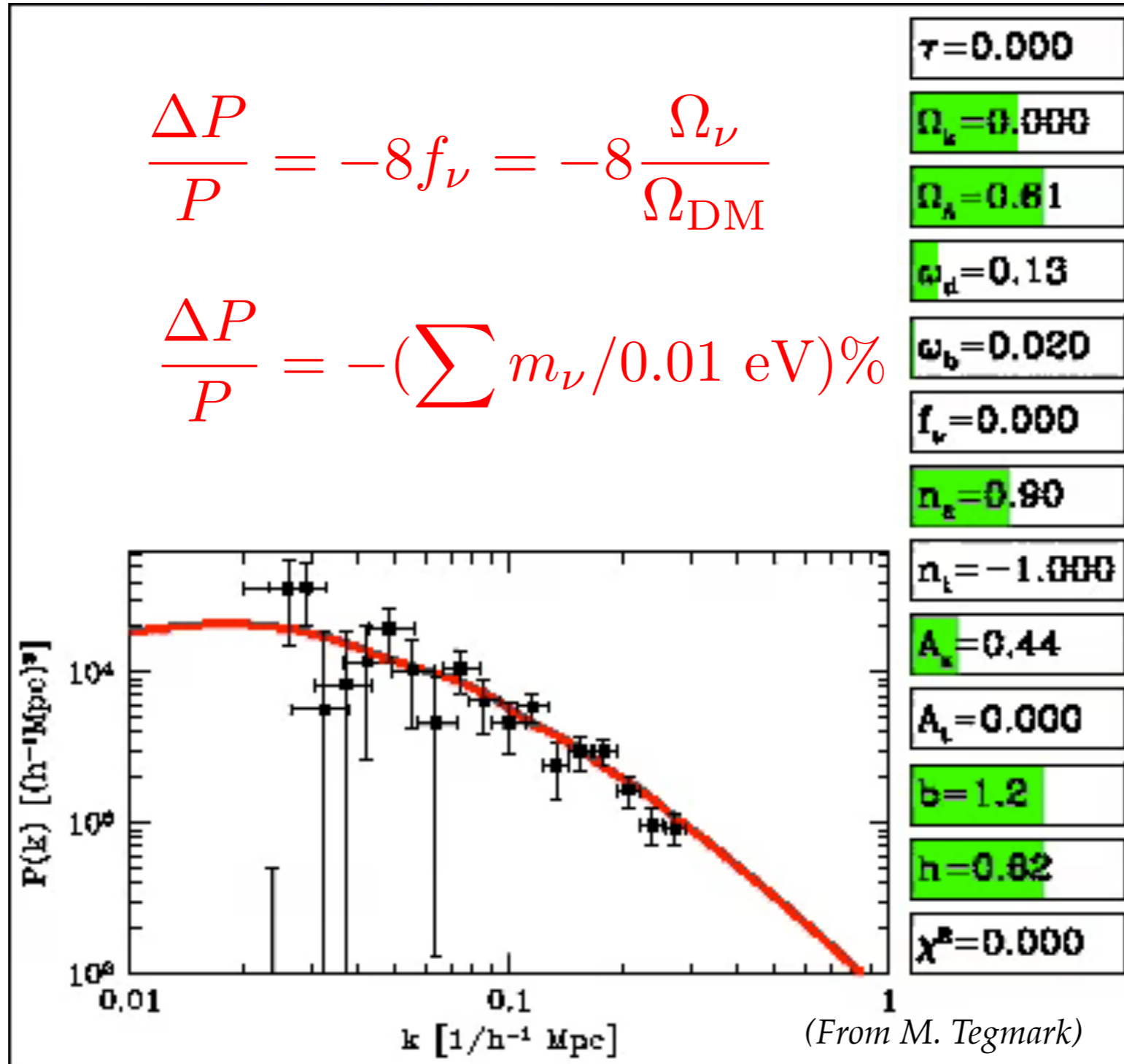
$$k_{fs,\nu}(z) \equiv \sqrt{\frac{3}{2}} \frac{H(z)}{(1+z)\sigma_{\nu,\nu}(z)}$$

# Large scale structure: $m_\nu$

Matter power spectrum suppression:

$$\frac{\Delta P}{P} = -8f_\nu = -8 \frac{\Omega_\nu}{\Omega_{DM}}$$

$$\frac{\Delta P}{P} = -(\sum m_\nu / 0.01 \text{ eV})\%$$



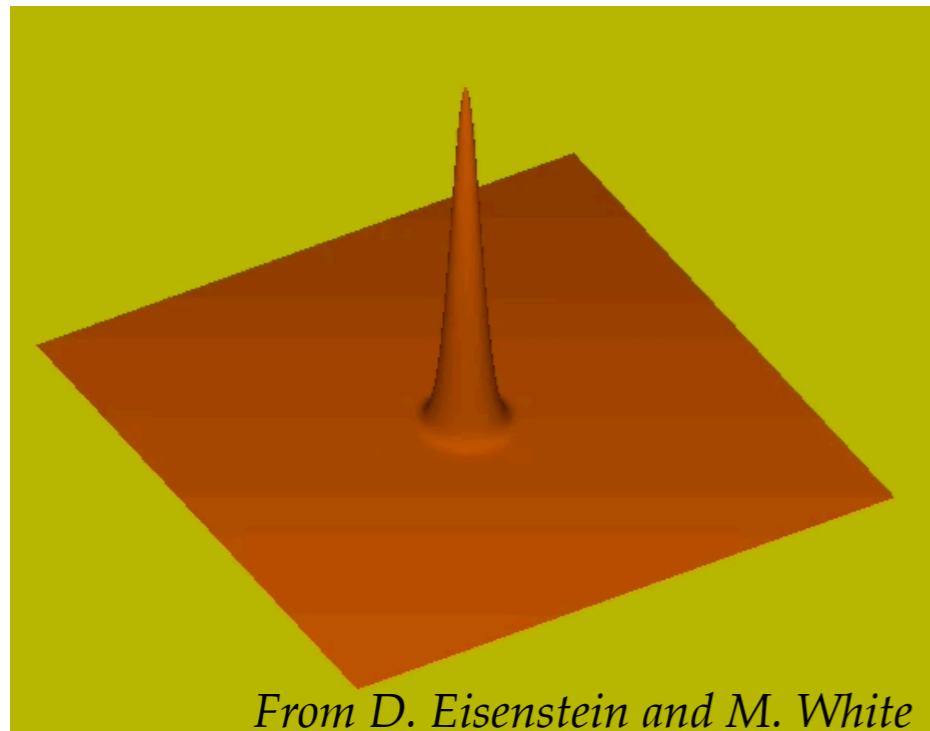
↑ Small scales

# Baryon Acoustic Oscillations

Photons and baryons in the early universe behave as a tightly coupled fluid, resembling acoustic waves, generated as the baryon-photon fluid is attracted and falls onto the overdensities:

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The time when the baryons are “released” from the drag of the photons is known as the drag epoch. From then on photons expand freely while the acoustic waves “freeze in” the baryons at a scale given by the size of the horizon at the drag epoch:



$$r_s = 147.09 \pm 0.26 \text{ Mpc}$$

(Planck 2018 results)



# Baryon Acoustic Oscillations

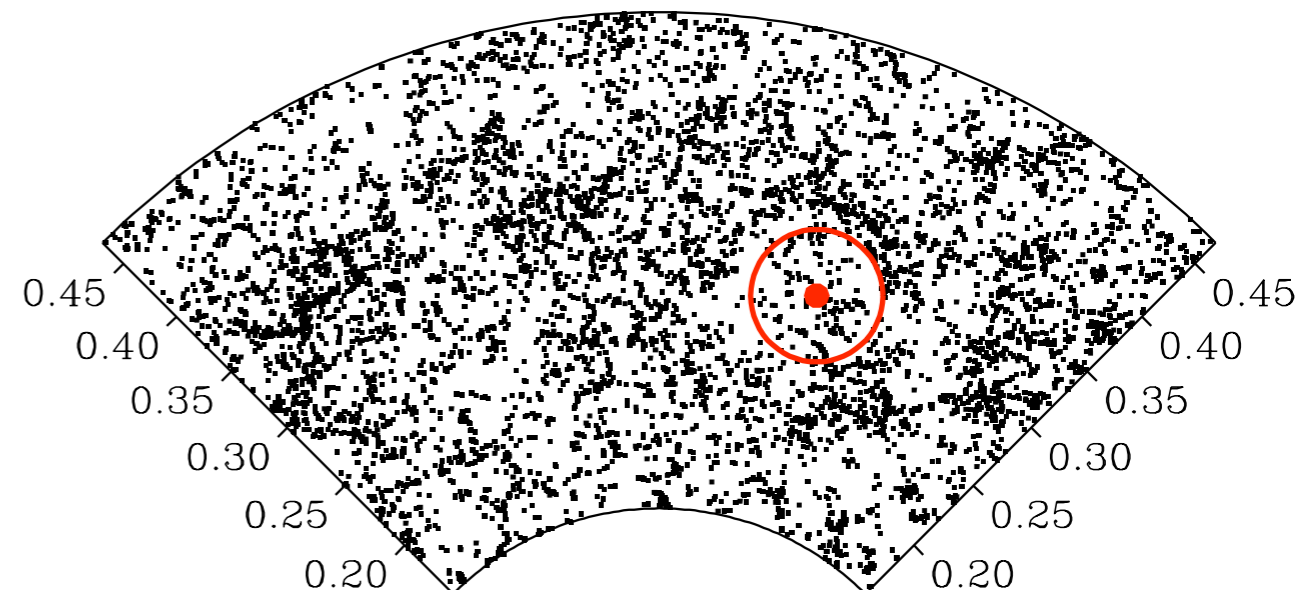
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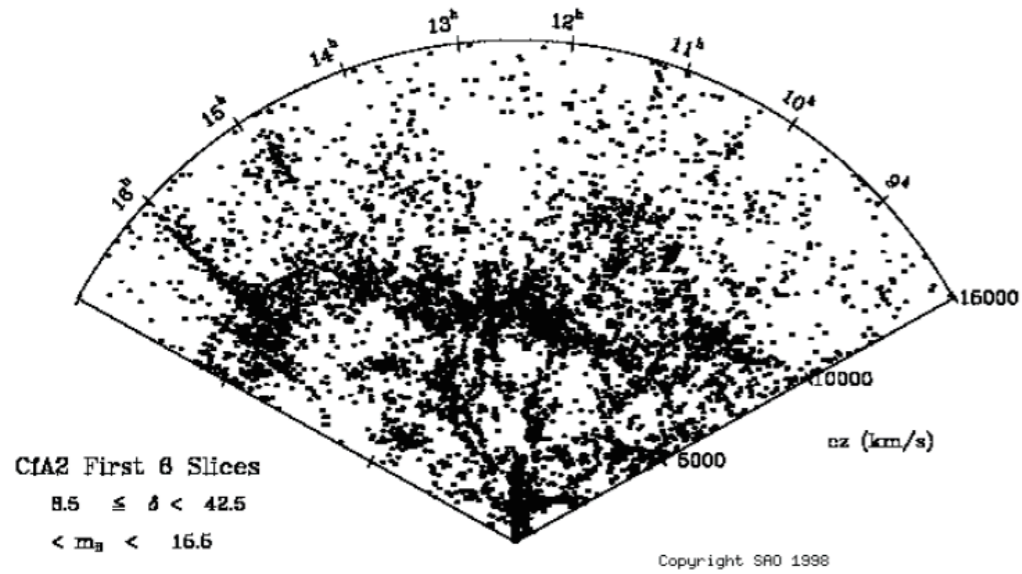
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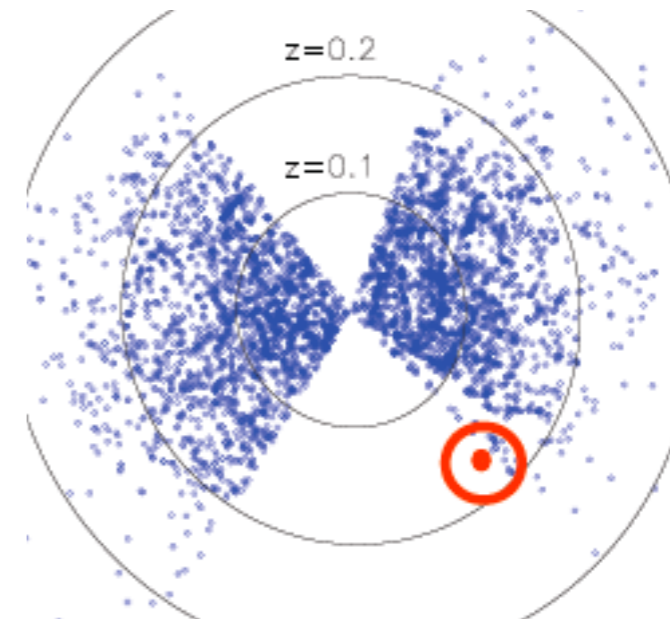
There should be a small excess  
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function around 150 Mpc!



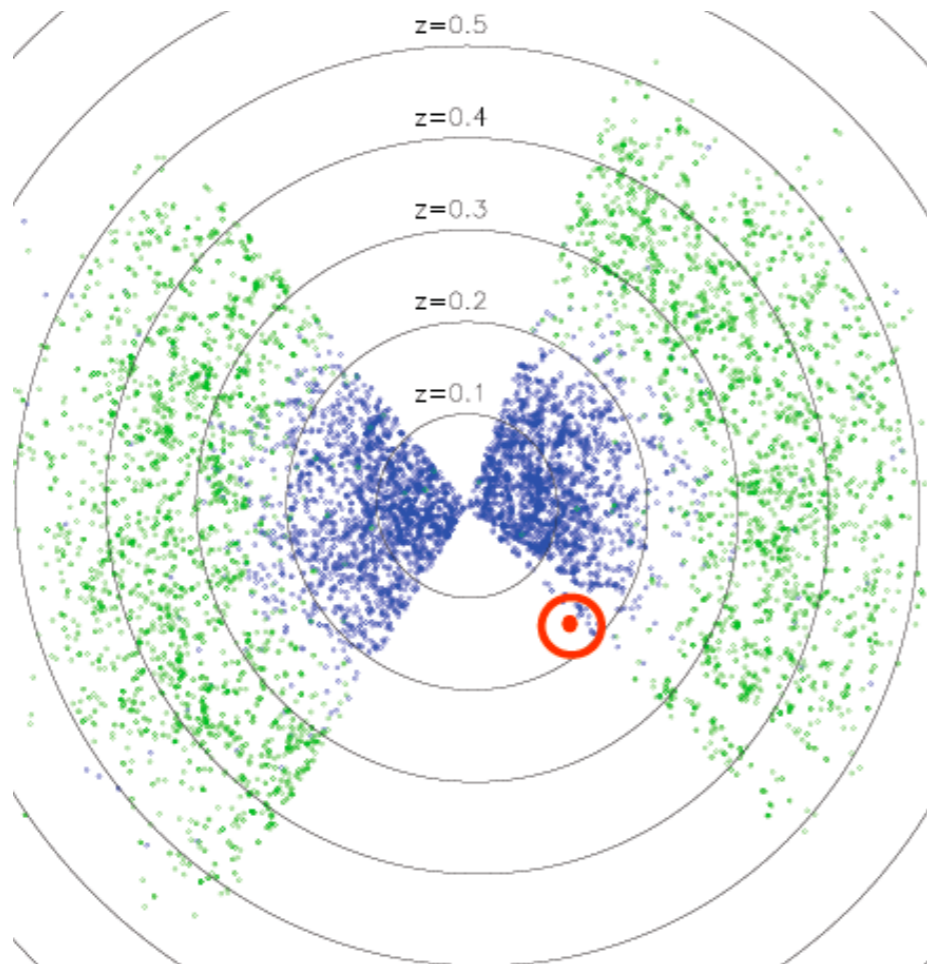
# 80's: Tiny surveys Baryon Acoustic Oscillations



BAO scale



2000: Main galaxies @SDSS.  
Big number, but small volume

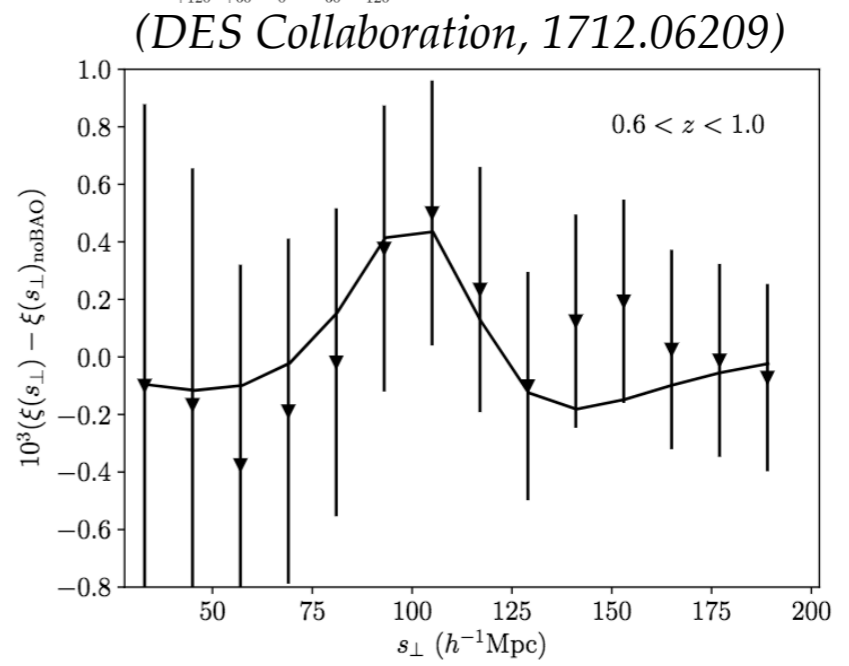
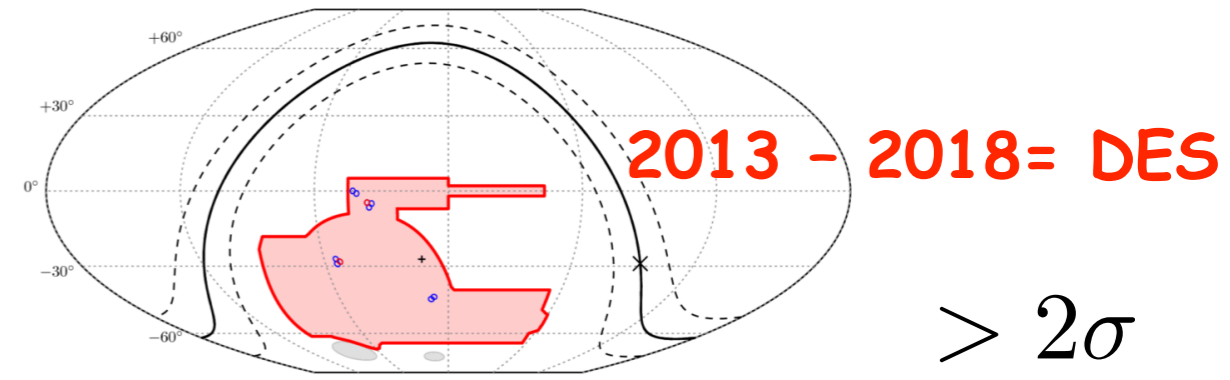
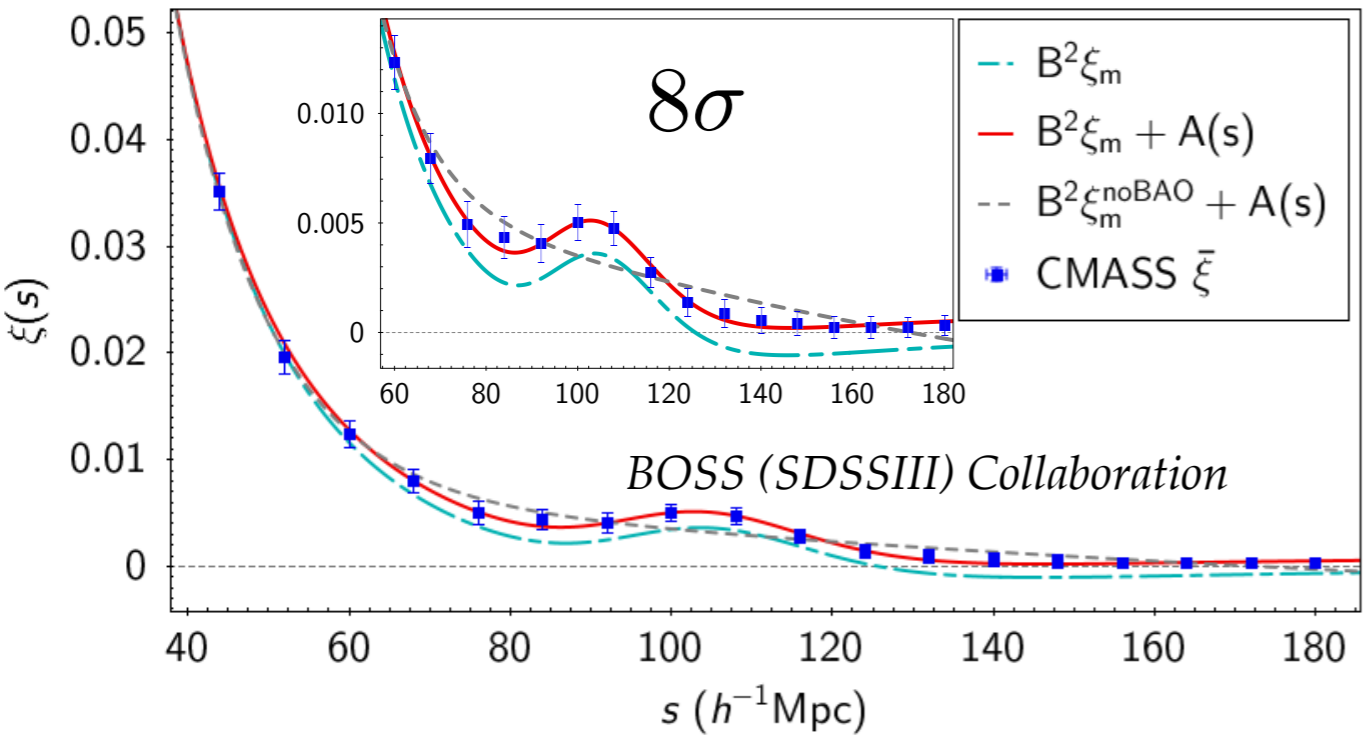
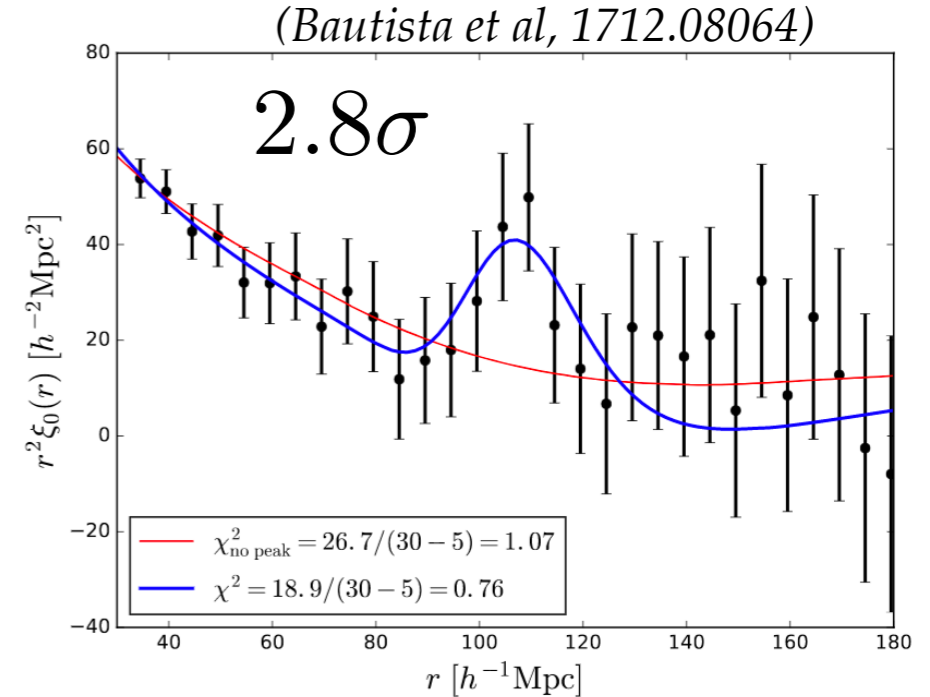
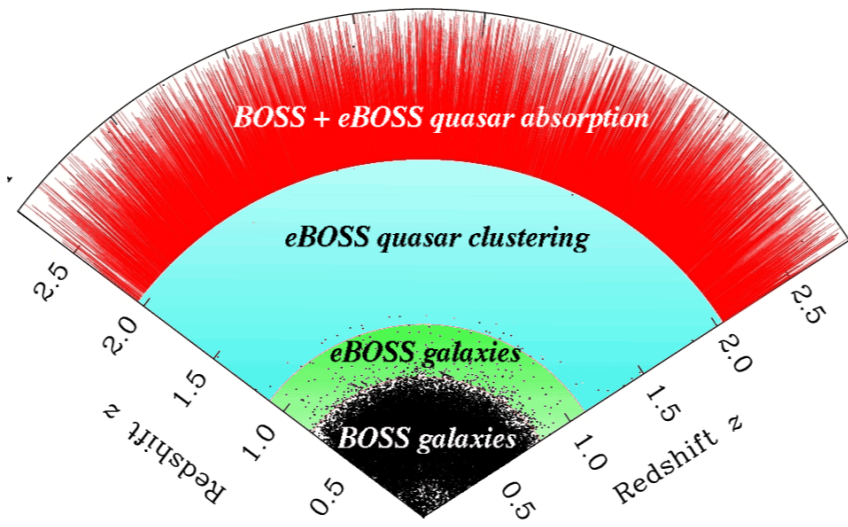
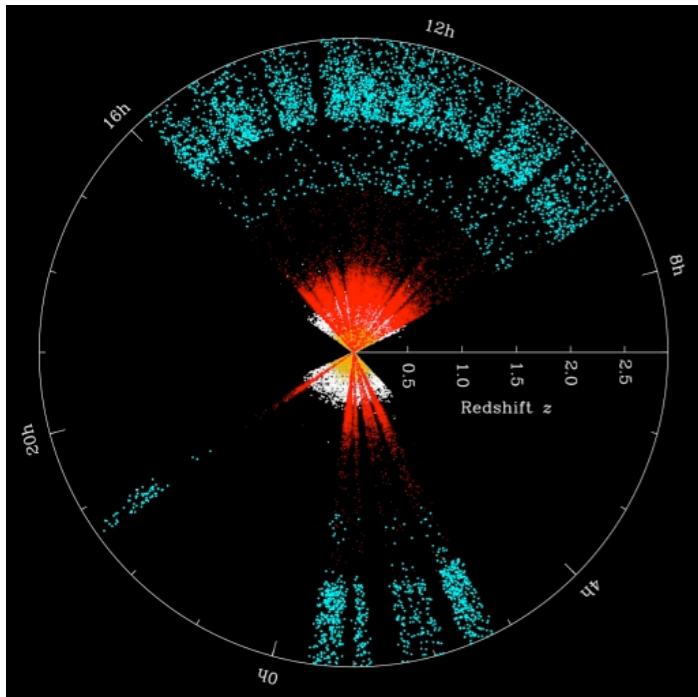


2005: Luminous Red Galaxies @ SDSS.  
Big Volume: first detection of the BAO signature

# Baryon Acoustic Oscillations

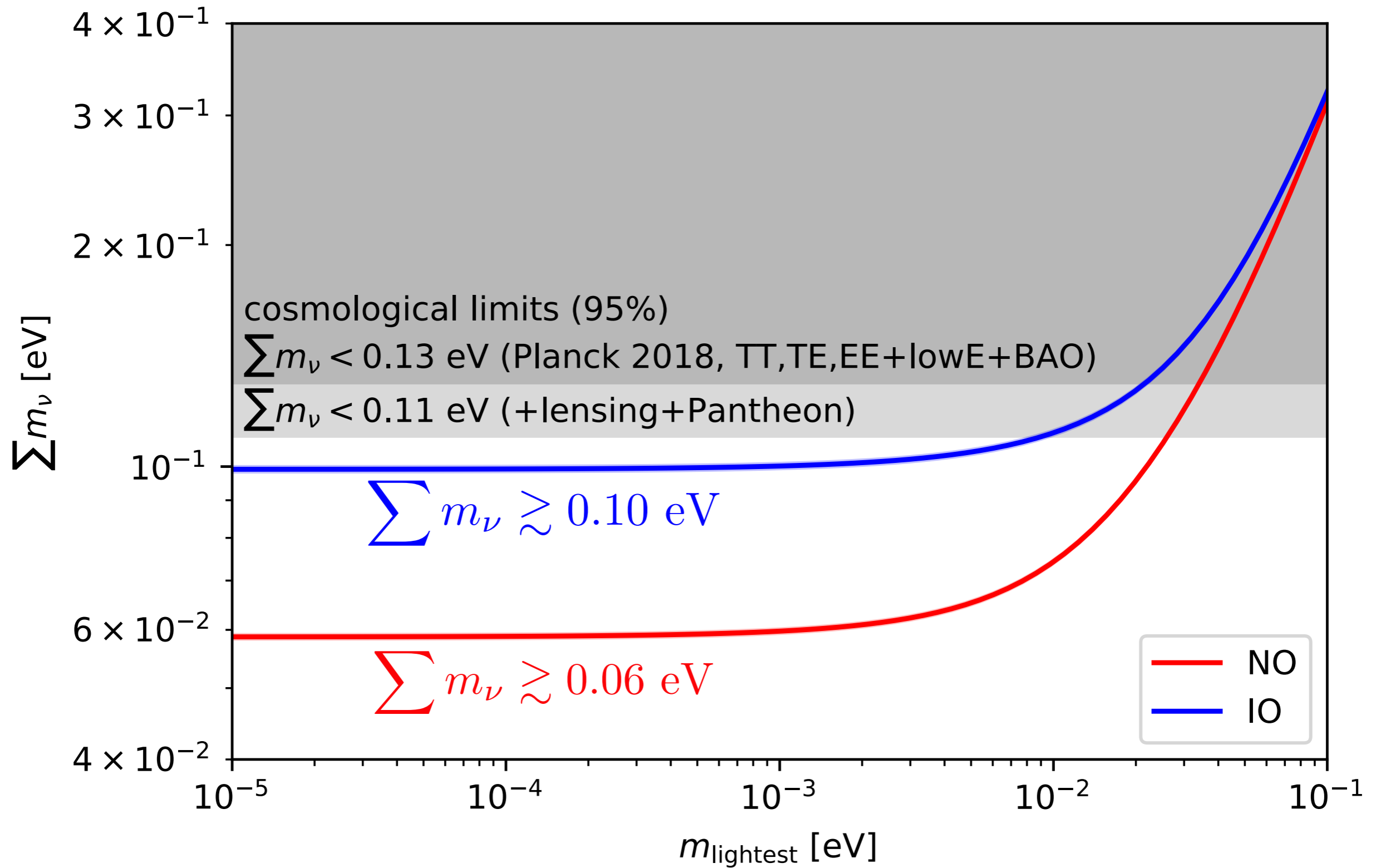
2009-2014= SDSS III

2014 - 2020= SDSS IV eBOSS



# $\Sigma m_\nu$

Planck 2018 results, 1807.06209



Planck TTTEEE+lowT+lowE+lensing

$$\Sigma m_\nu < 0.24 \text{ eV } 95\% \text{CL}$$

+ BAO

$$\Sigma m_\nu < 0.12 \text{ eV } 95\% \text{CL}$$

+ BAO + SNIa

$$\Sigma m_\nu < 0.11 \text{ eV } 95\% \text{CL}$$

+ BAO + SNIa +  $H_0 = 73.45 \pm 1.66 \text{ km/s/Mpc}$

*Riess et al, APJ'18*

$$\Sigma m_\nu < 0.0970 \text{ eV } 95\% \text{CL}$$

## Planck TTTEEE+lowT+lowE+lensing

$$\sum m_\nu < 0.26 \text{ eV} \quad N_{\text{eff}} = 2.90 \pm 0.37 \text{ 95\%CL}$$

+ BAO

$$\sum m_\nu < 0.12 \text{ eV} \quad N_{\text{eff}} = 2.96^{+0.34}_{-0.33} \text{ 95\%CL}$$

+ BAO + SNIa

$$\sum m_\nu < 0.11 \text{ eV} \quad N_{\text{eff}} = 2.98^{+0.35}_{-0.33} \text{ 95\%CL}$$

+ BAO + SNIa +  $H_0=73.45 \pm 1.66 \text{ km/s/Mpc}$  + w + nrun

$$\sum m_\nu < 0.16 \text{ eV} \quad N_{\text{eff}} = 3.11^{+0.38}_{+0.38} \text{ 95\%CL}$$

# Today's menu

## Antipasto

- The classical cosmic pizza
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## Main course

- Number of neutrinos and Big-Bang Nucleosynthesis
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- ● The Dark Justice League game:  $\Sigma m_\nu$  versus  $w(z)$

## Doggy Bag

- Take home messages

The 3-Neutrino representative,

$$\Omega_\nu$$

Madame Dark energy  $\Omega_\Lambda$

Mr Inflation

The radiation  
member,  
 $N_{\text{eff}}$

Lady Cold Dark matter,  
 $\Omega_{\text{cdm}}$







## The Dark JUSTICE GAME:

The 3-Neutrino representative  $\Sigma m_\nu$

versus

the Dark energy equation of state  $w(z)$

## GAME RULES:

1. Choose your favourite cosmological model for dark energy
2. Derive cosmological bounds on  $\Sigma m_\nu$  within that model, discarding neutrino oscillations (i.e. using just with the prior  $\Sigma m_\nu > 0$ )
3. Are cosmological bounds consistent with oscillation data?

**YES!**

**GREAT! You just won the game!**

Your model is not ruled out (yet!)

Go to 1.

**NO!**

(i.e.  $\Sigma m_\nu < 0.06$  eV or  $\Sigma m_\nu < 0.1$  eV)

**Write a paper**

**GAME OVER...after referral process**

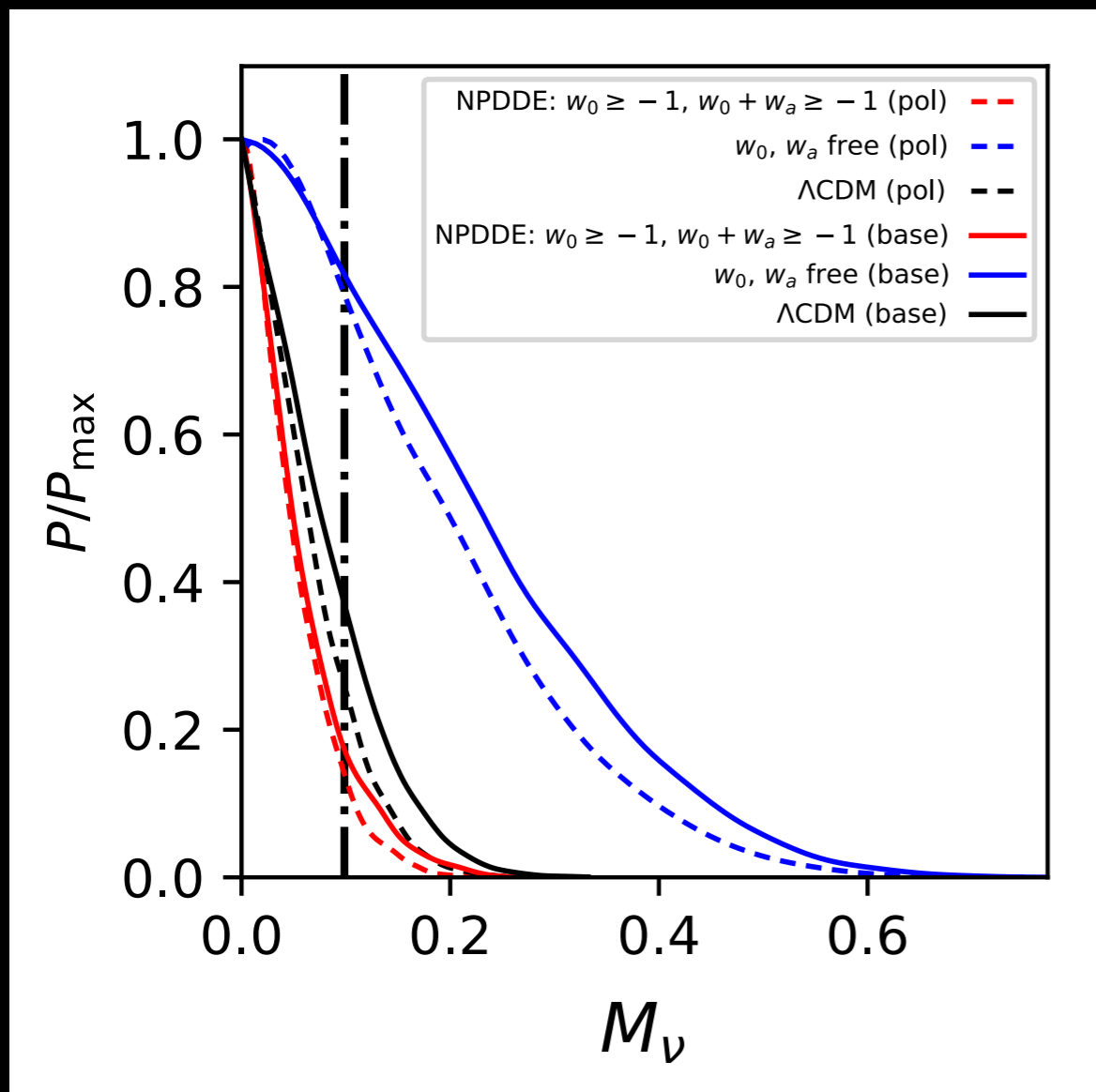
# The Dark Justice Game

$$w(z) = w_0 + w_a \frac{z}{1+z}$$

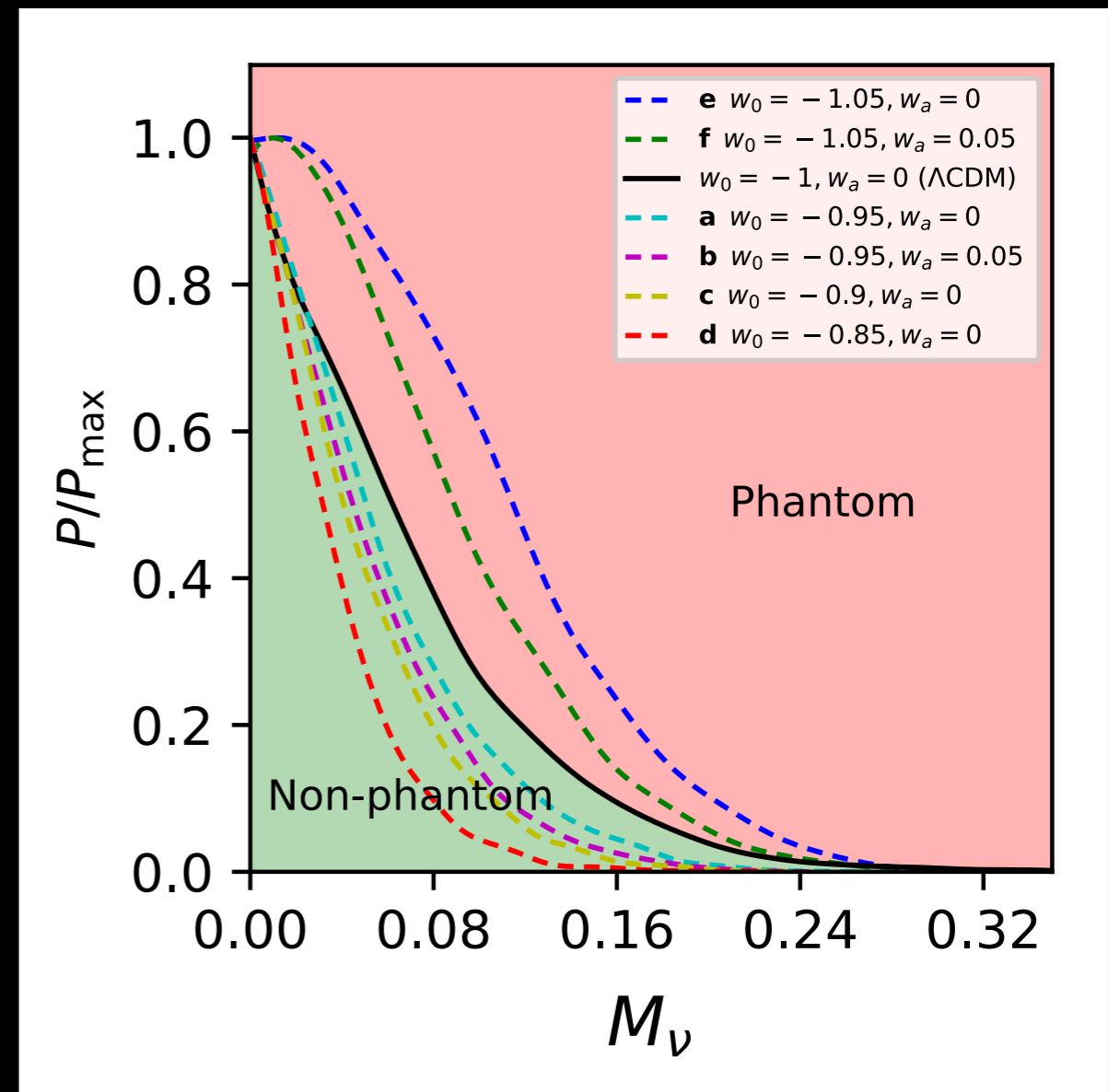
*Chevalier & Polarsky'01 & Linder'03*

$$w_0 \geq -1 \quad w_0 + w_a \geq -1$$

**NON-PHANTOM REGION**



?



*Vagnozzi et al PRD'18*

*Choudury & Choubey, JCAP'18*

PHANTOM



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- ● Take home messages

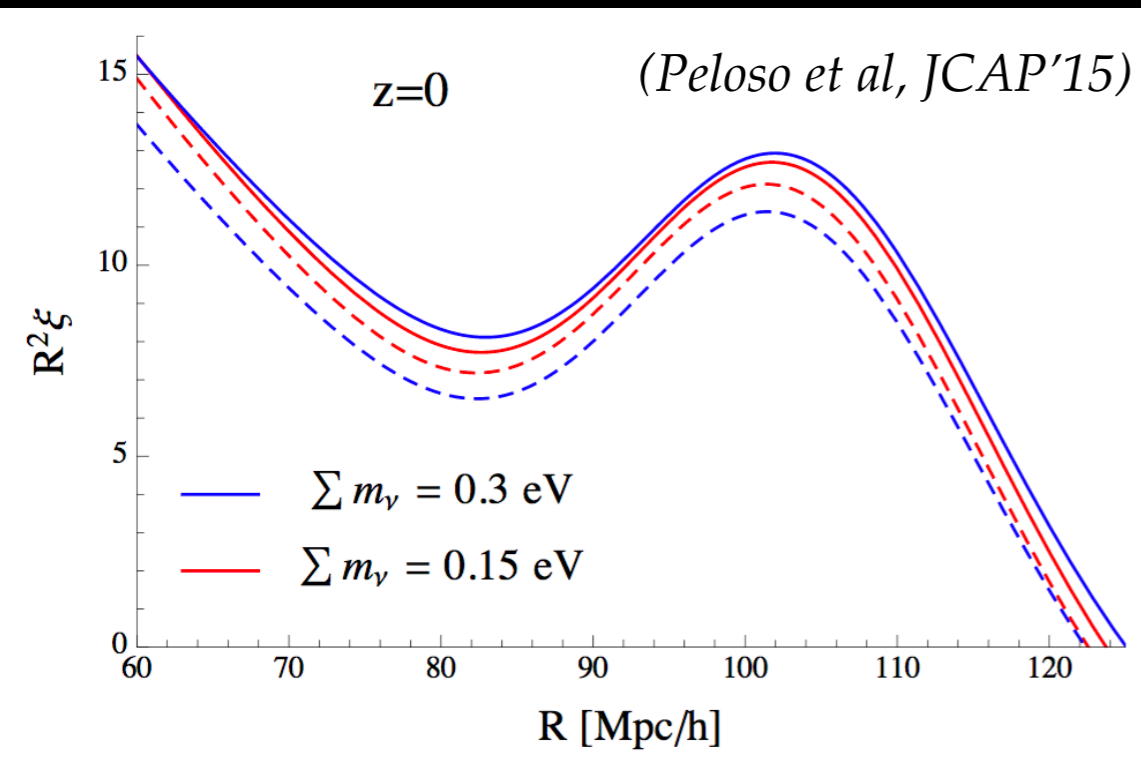
# The "Take Home" messages



- $\nu$  masses & abundances leave key signatures in cosmological observables.
- **NO** hints so far for neutrino masses or extra dark radiation species!
- $N_{\text{eff}}$  @BBN: Light element abundances ( $^4\text{He}$ ) abundances.
- $N_{\text{eff}}$  @CMB: damping tail
- $N_{\text{eff}} = 2.99^{+0.34}_{-0.33}$ , (95% CL) from 2018 Planck TTTEEE+lensing, perfectly consistent with BBN.
- Cosmology provides currently the tightest bounds to neutrino masses.
- $\nu$  masses@CMB: Early ISW, gravitational lensing
- $\nu$  masses@LSS: Free streaming reduces clustering at small scales
- $\Sigma m_\nu < 0.12$  eV (95%CL) from 2018 Planck TTTEEE+lensing plus BAO data
- For non-phantom (physical) dynamical dark energy,  $\Sigma m_\nu$  bounds get tighter!



# What we know: Massive neutrinos cosmological signatures



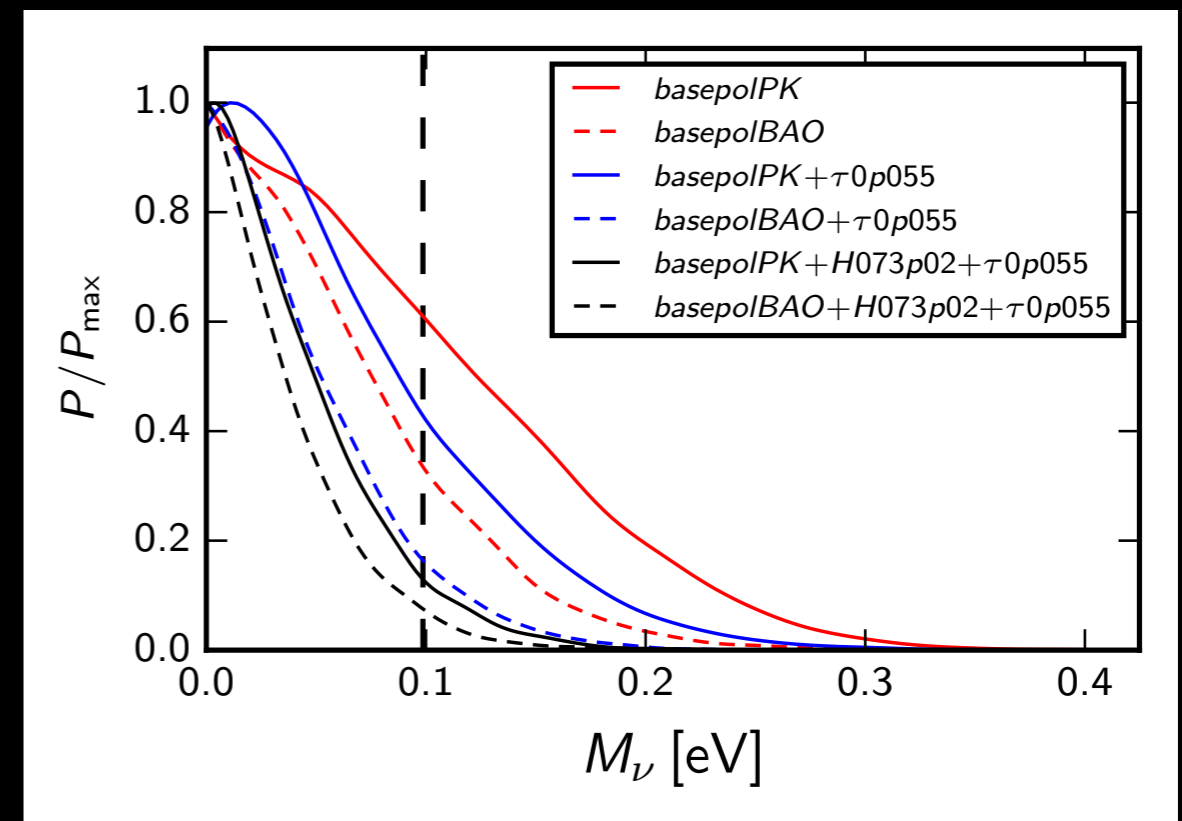
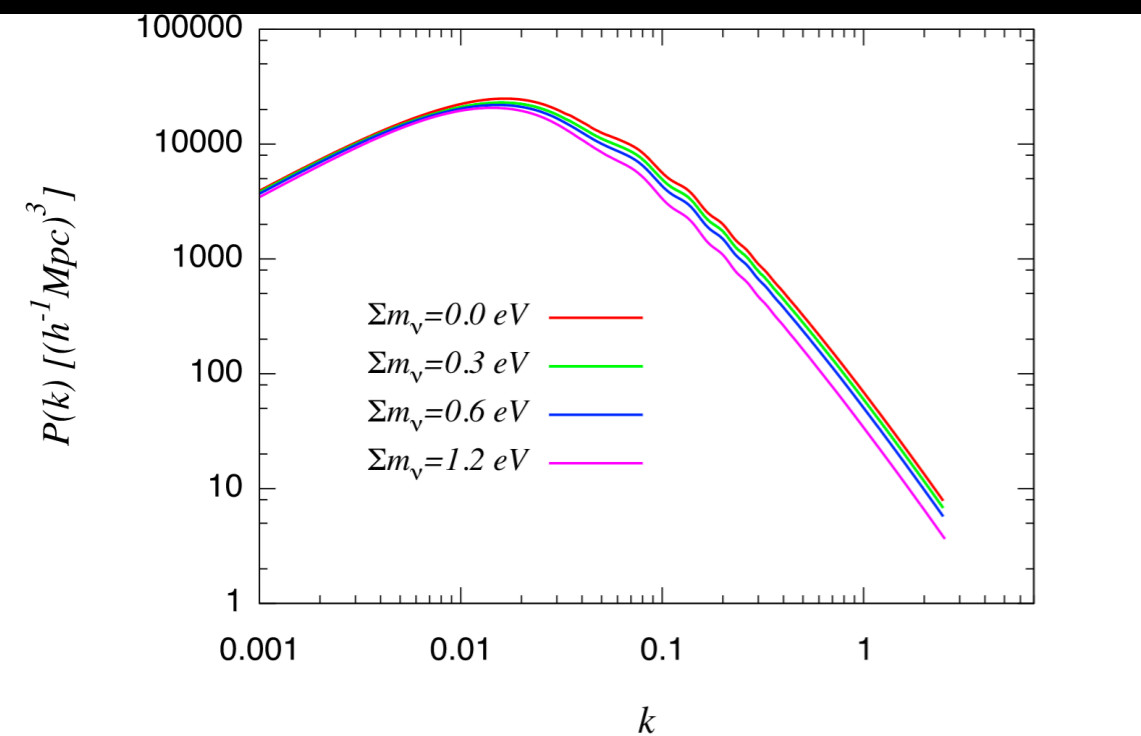
Large scale structure measurements can be interpreted either in the geometrical or shape forms

2 point correlation function

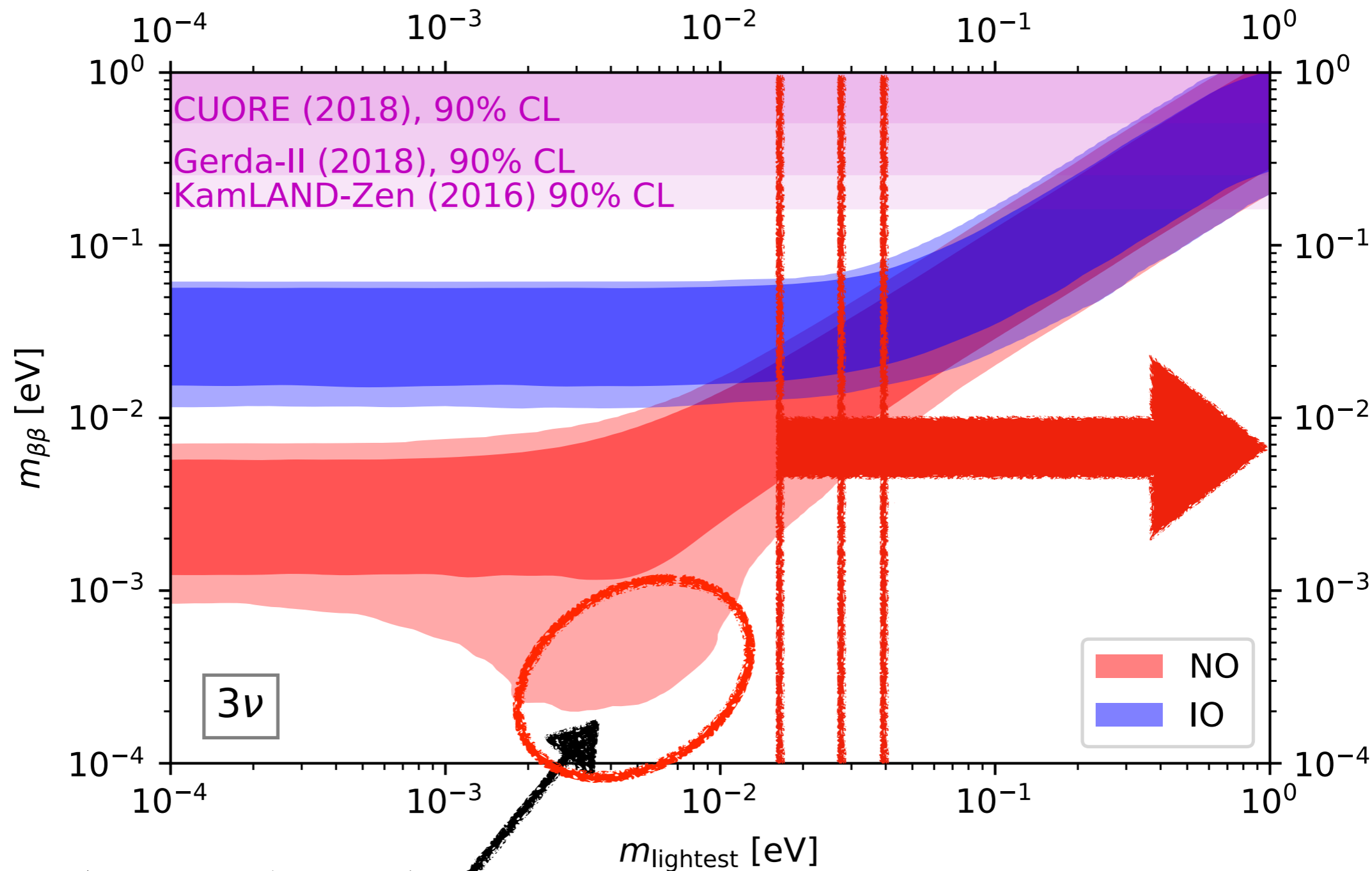
Fourier Transform

Matter power spectrum

BAO information more powerful



# What we know

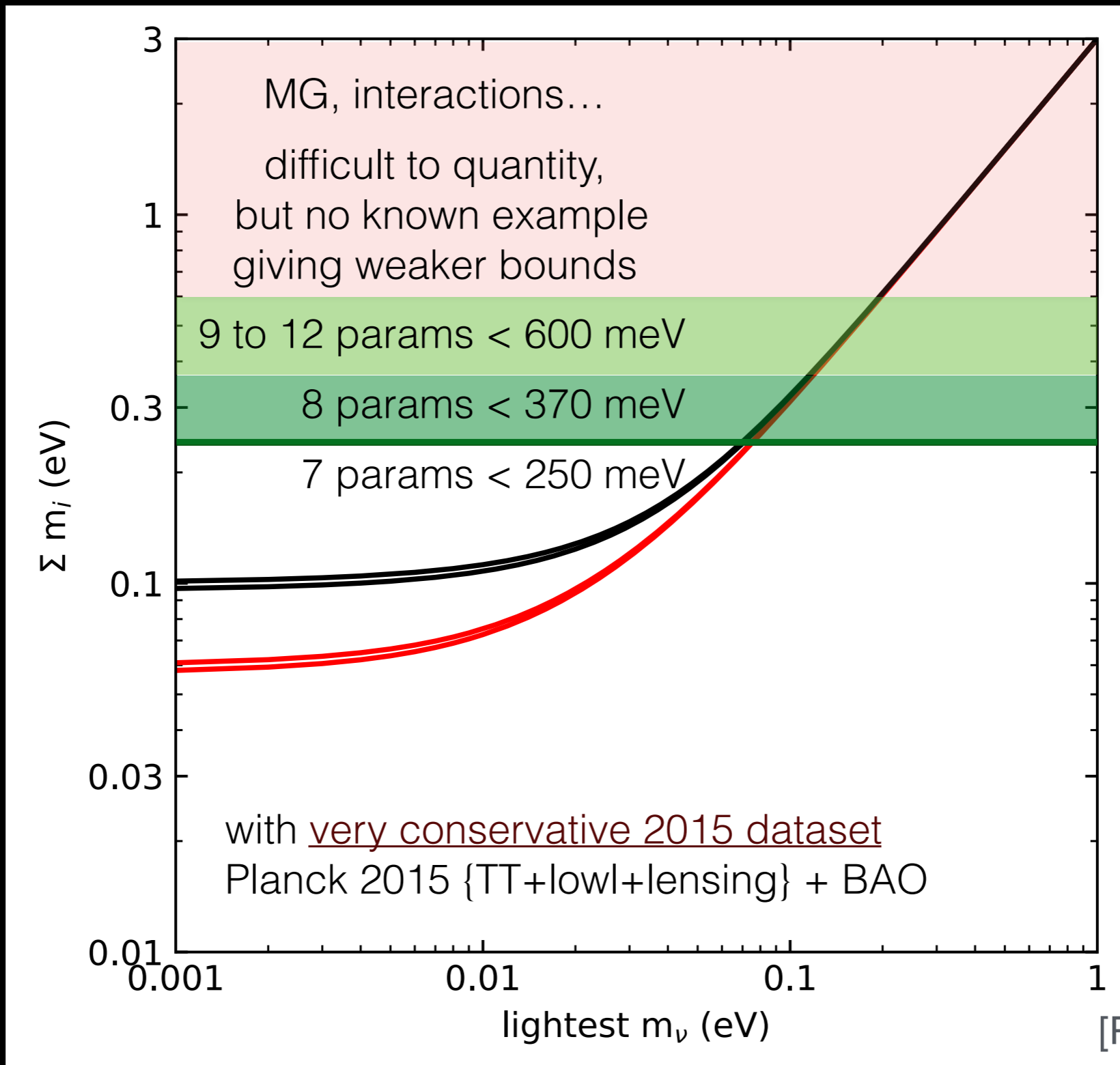


(Agostini et al, PRD'17)

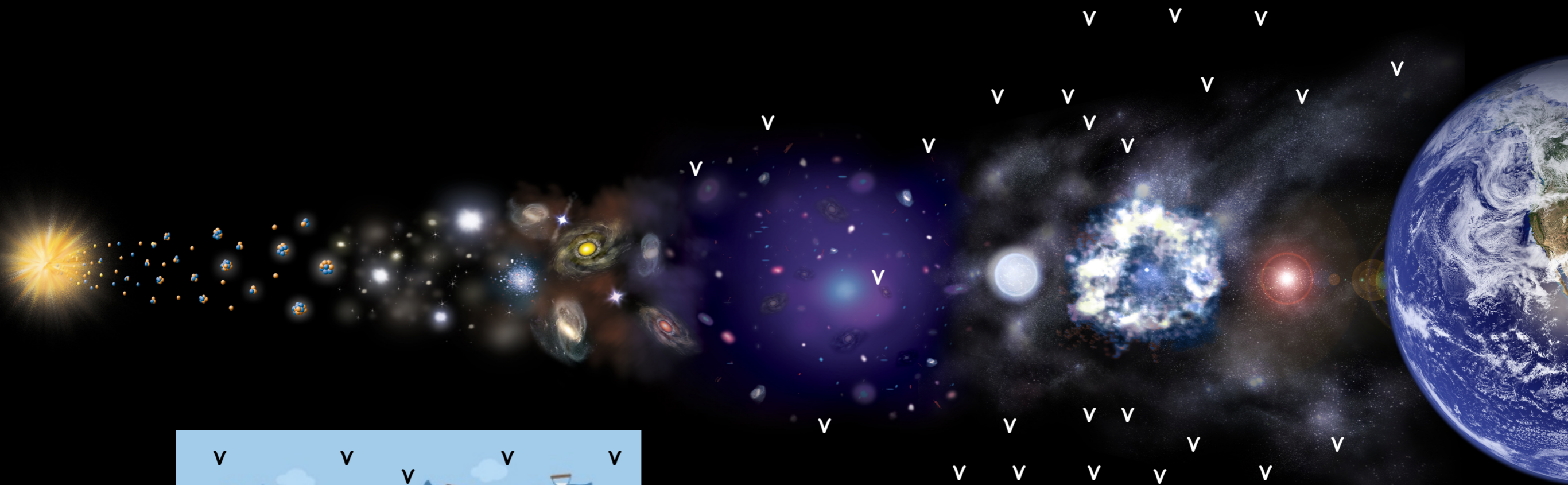
$m_{\beta\beta} < 2 \cdot 10^{-4}$  would require  
some fine tuning in the Majorana phases



# What we know



# BACKUP SLIDES



in**v**isiblesPlus  
elusi**v**es  
neutrinos, dark matter & dark energy physics



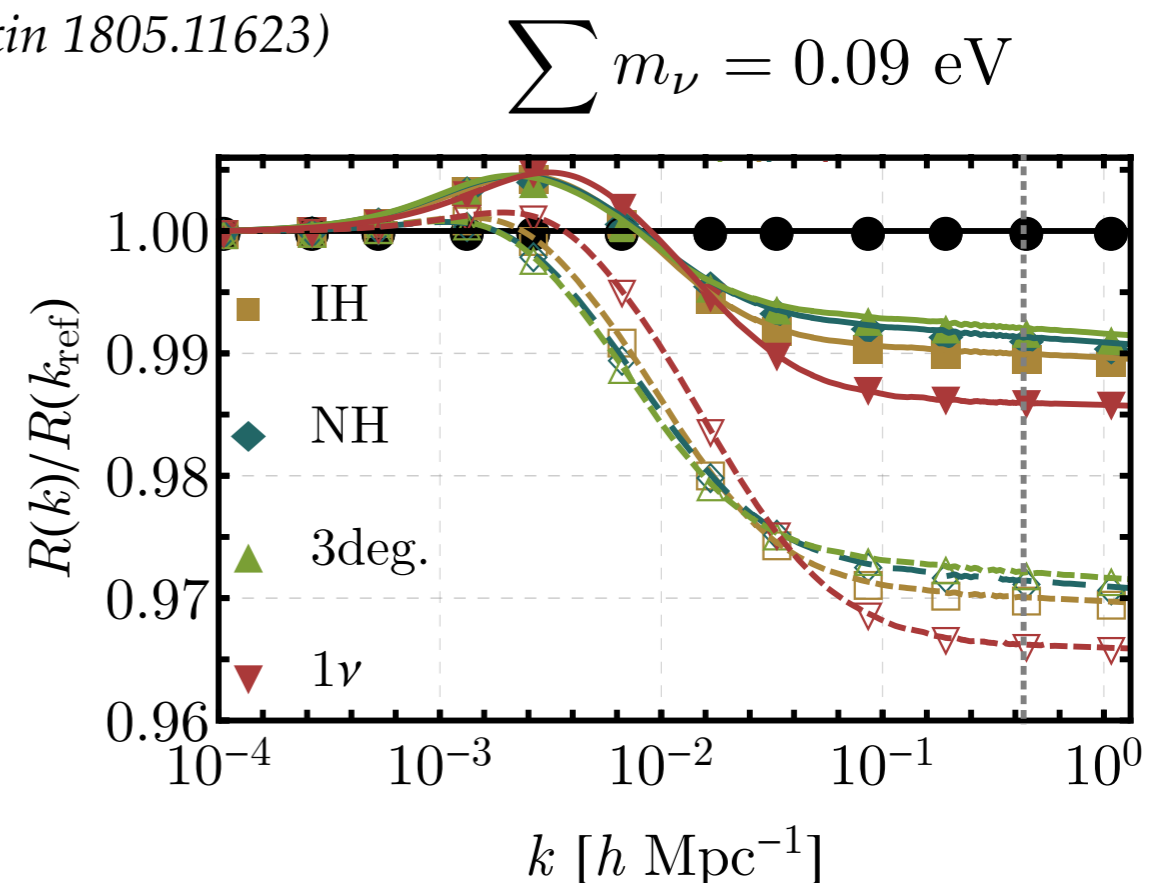
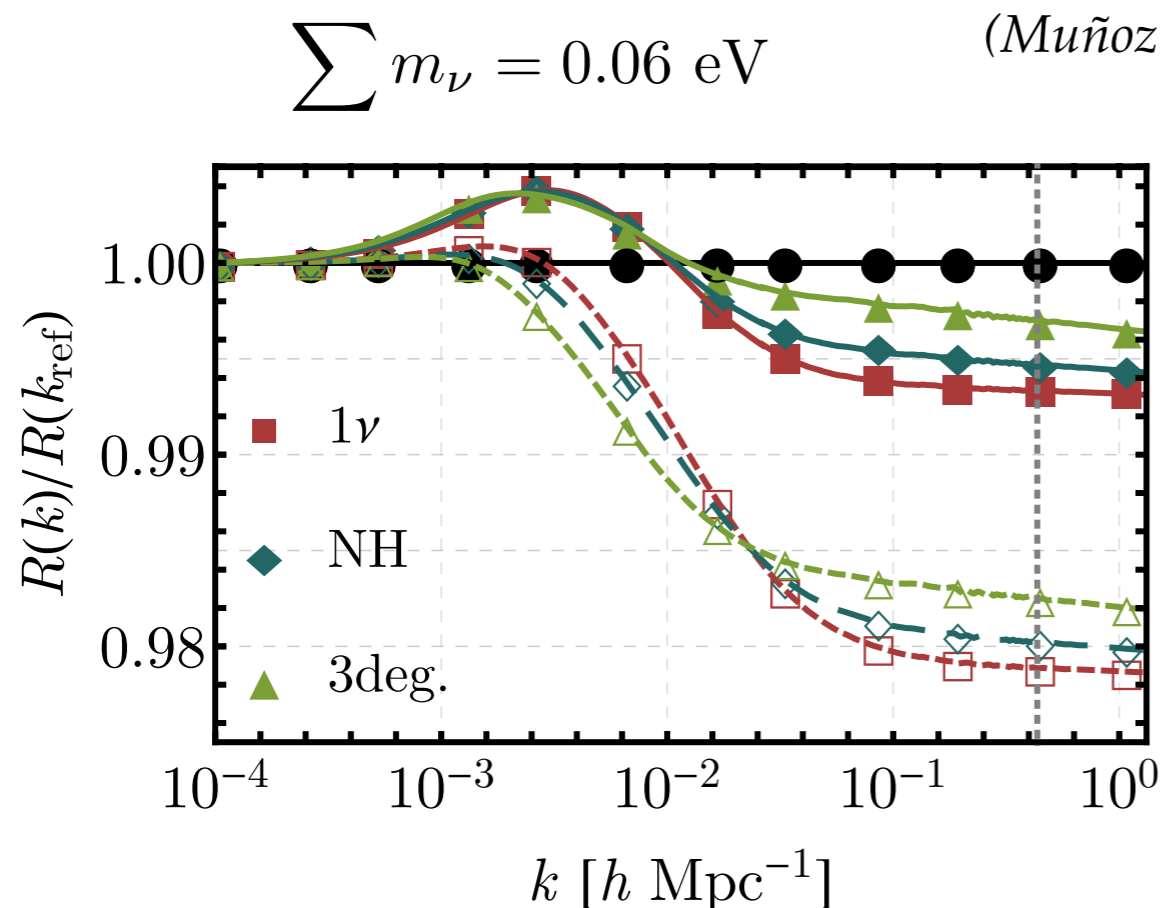
# What we know: Massive neutrinos cosmological signatures

@LSS: Caveats, BIAS!

$$P_{gg}(k, z) = \textit{bias}^2 P(k, z)$$

Galaxies are **biased** tracers of the underlying matter density field! *(Kaiser, APJ'84)*

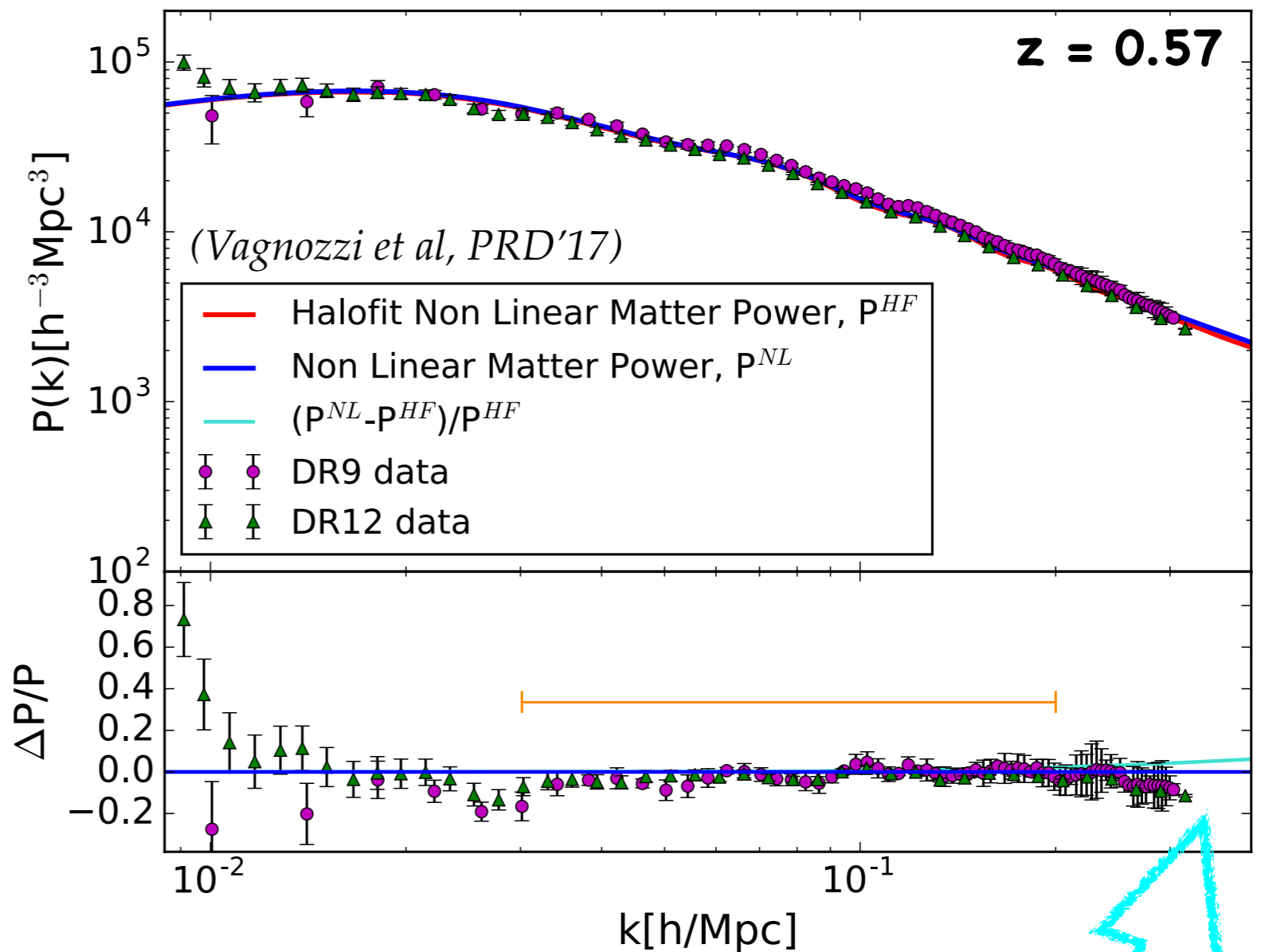
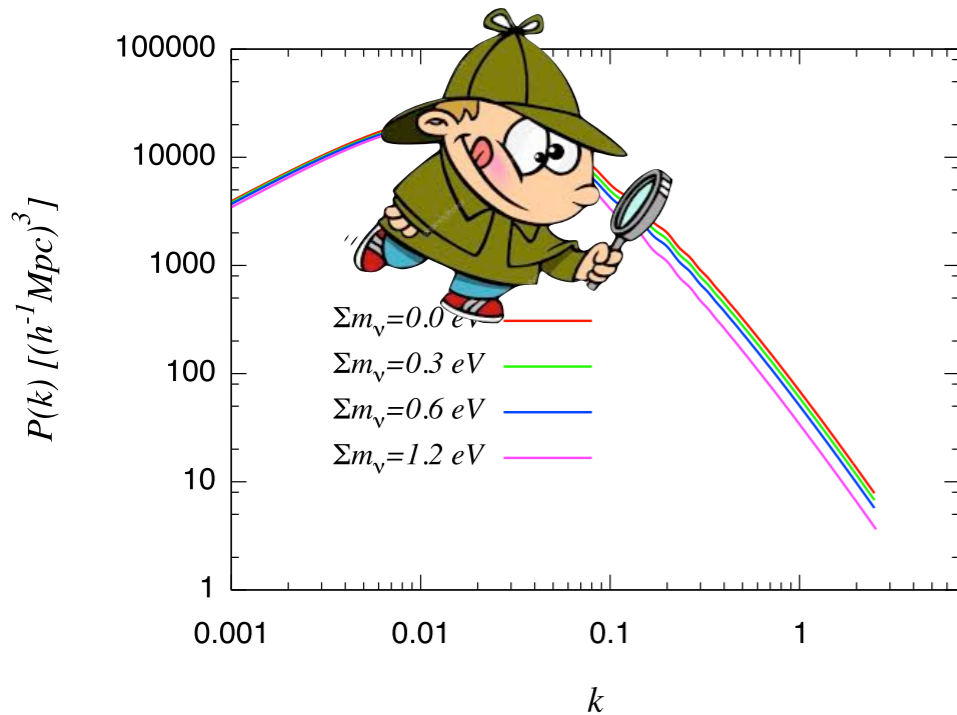
Neutrinos themselves induce a scale-dependent bias *(LoVerde & Zaldarriaga; Castorina et al)*



# What we know: Massive neutrinos cosmological signatures

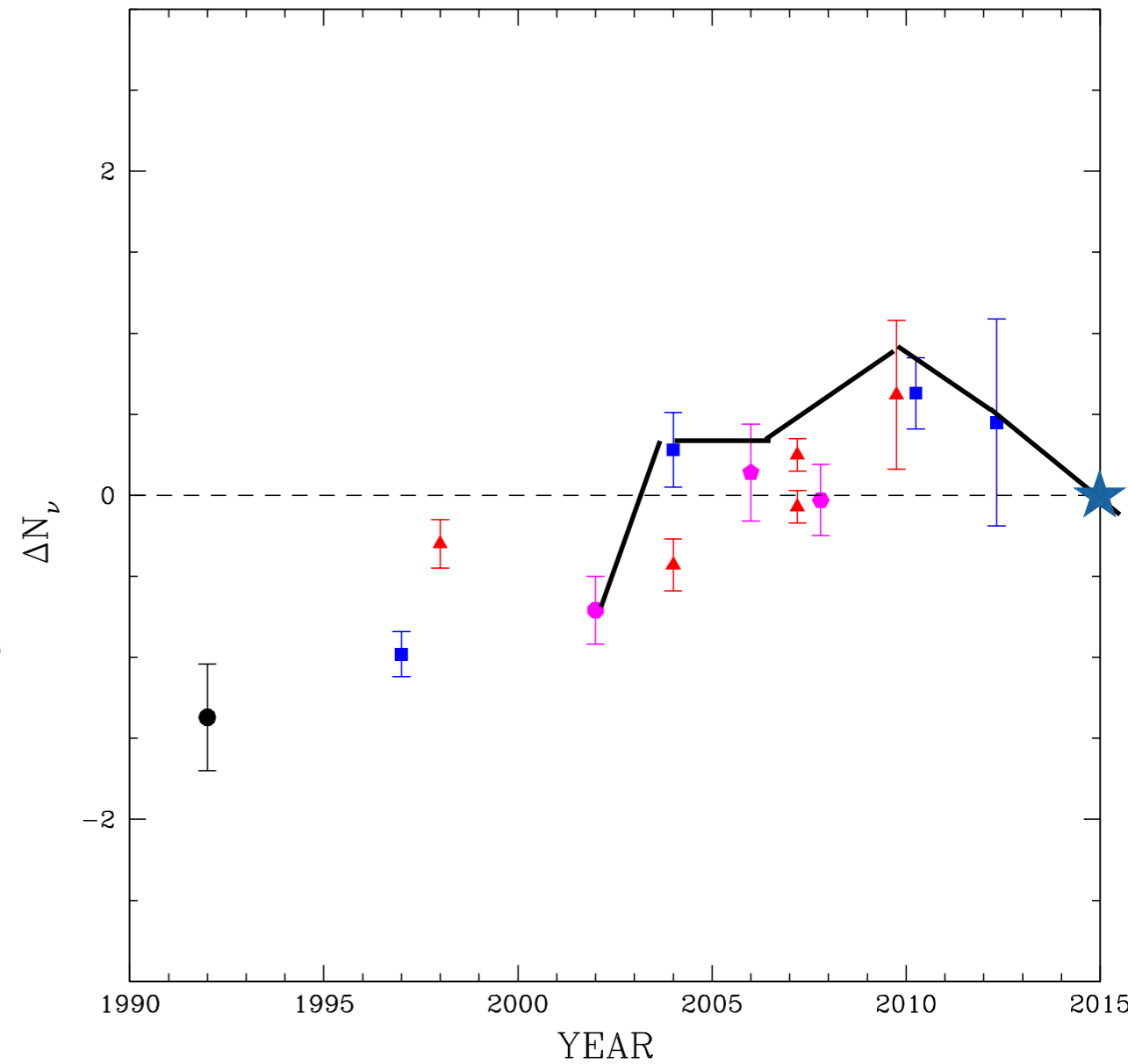
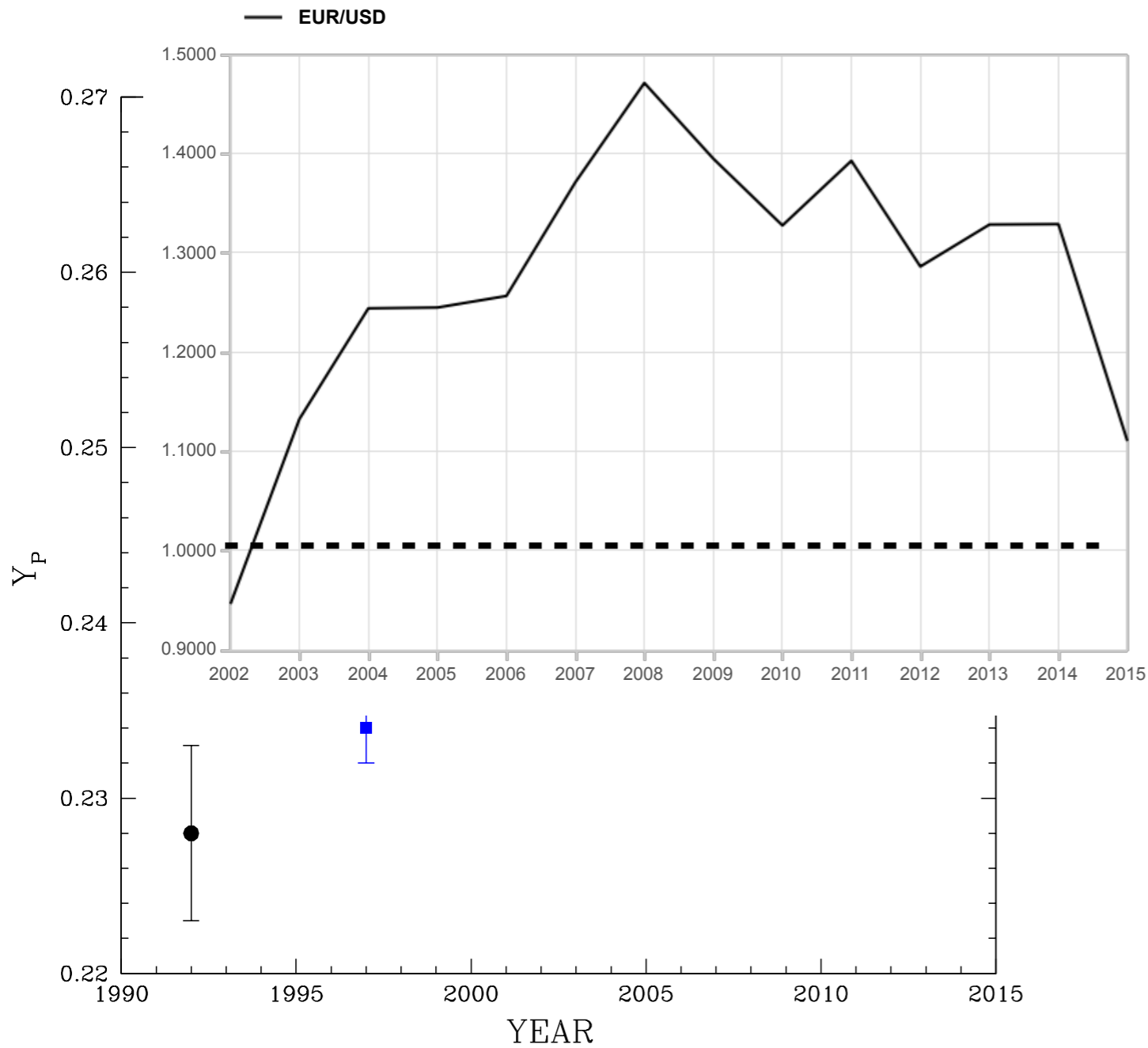
@LSS: Caveats, NON-LINEARITIES

Beyond a given scale  $k_{nl}$ , linear perturbation theory breaks down!



# Big Bang Nucleosynthesis: $N_{\text{eff}}$

Chronology, over some years, of the published observational determinations of  $Y_{\text{p}}$ :  
the extracted value of  $\Delta N_{\text{eff}}$  mirrors the helium fraction  $Y_{\text{p}}$ .



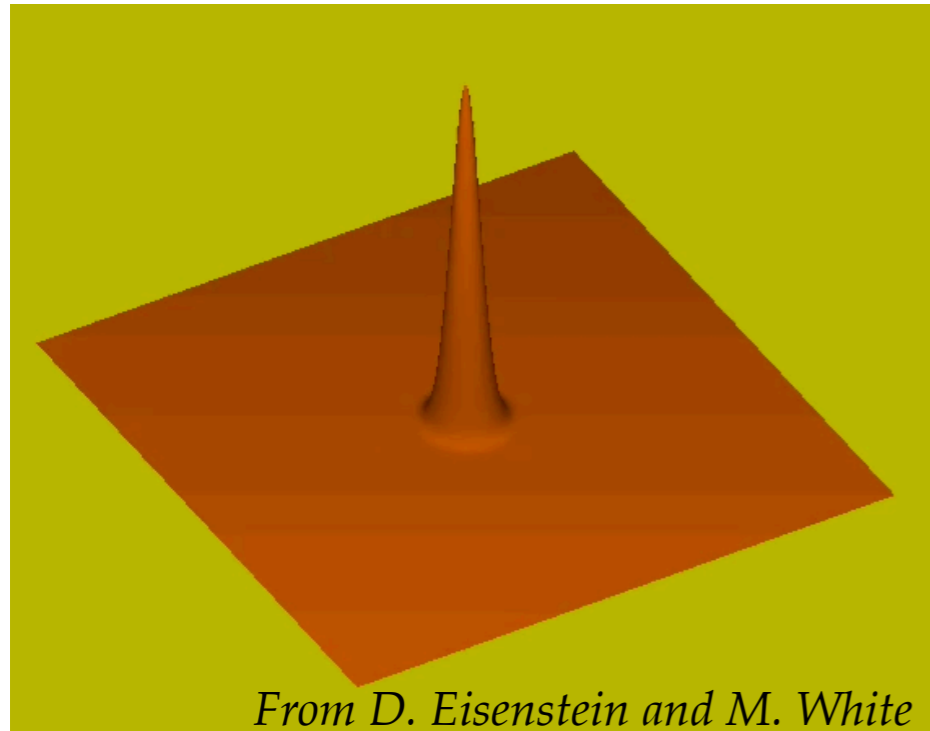
(G. Steigman'12)

# Baryon Acoustic Oscillations

Photons and baryons in the early universe behave as a tightly coupled fluid, resembling acoustic waves, generated as the baryon-photon fluid is attracted and falls onto the overdensities:

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The time when the baryons are “released” from the drag of the photons is known as the drag epoch. From then on photons expand freely while the acoustic waves “freeze in” the baryons at a scale given by the size of the horizon at the drag epoch:



From D. Eisenstein and M. White

$$R \equiv 3\rho_b/4\rho_\gamma$$

$$r_s = \int_0^{t(z_d)} c_s (1+z) dt = \frac{2}{3k_{\text{eq}}} \sqrt{\frac{6}{R_{\text{eq}}}} \ln \frac{\sqrt{1+R_d} + \sqrt{R_d+R_{\text{eq}}}}{1+\sqrt{R_{\text{eq}}}}$$

$$r_s = 147.09 \pm 0.26 \text{ Mpc} \quad (\text{Planck 2018 results})$$

# Baryon Acoustic Oscillations

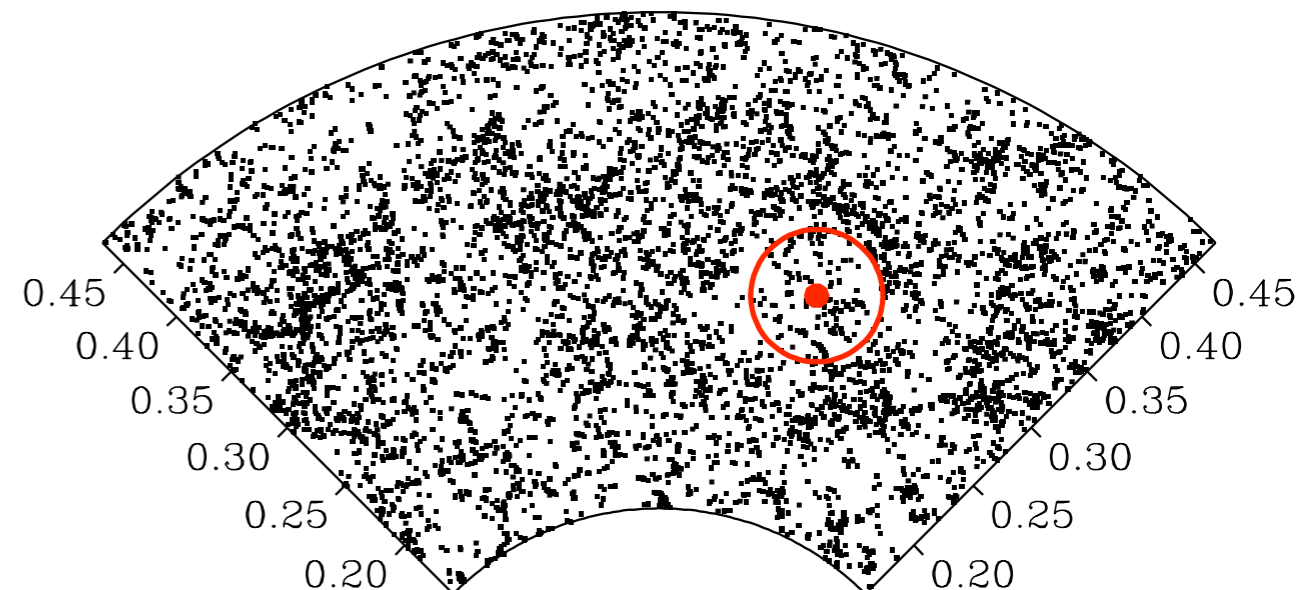
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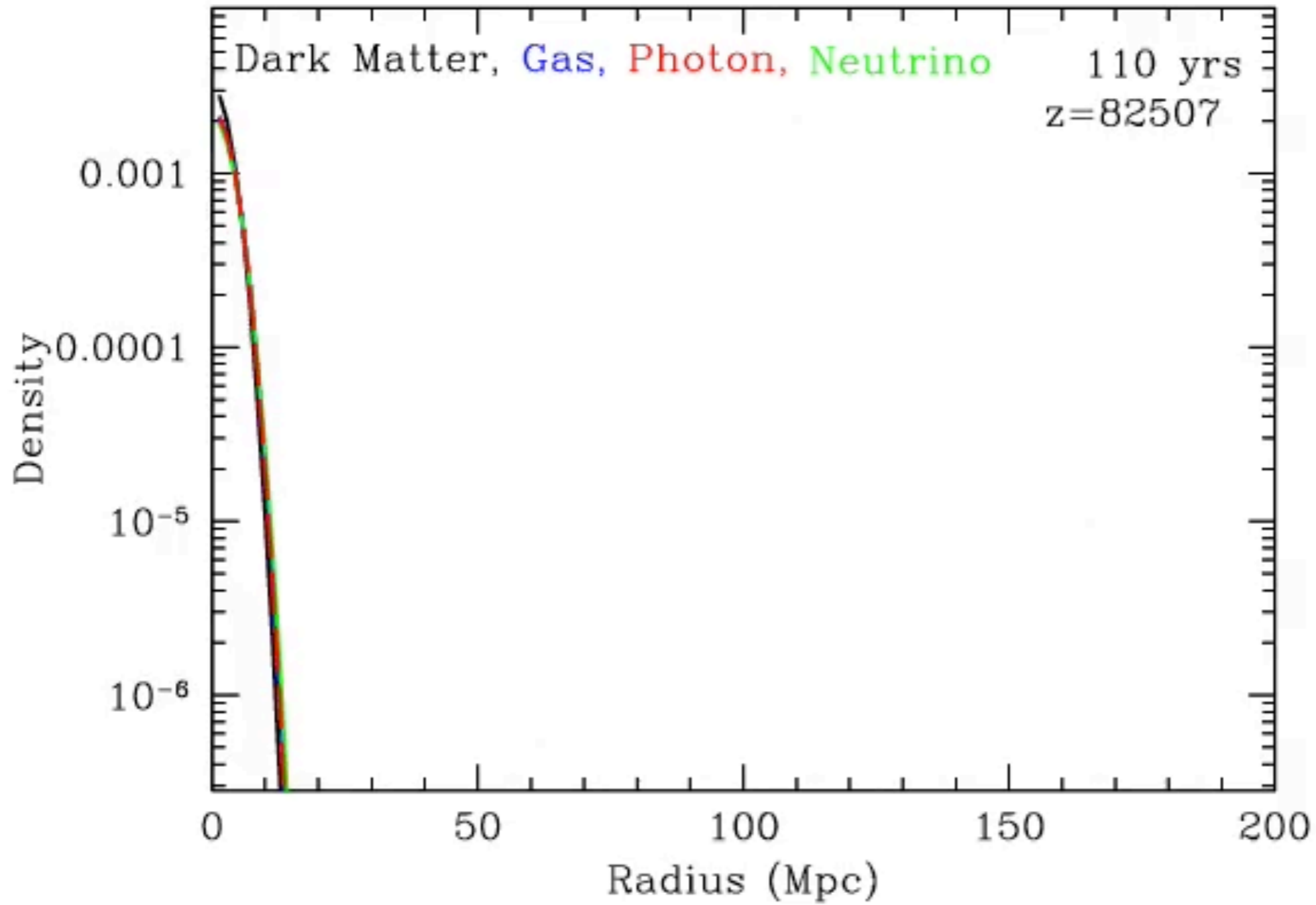
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There should be a small excess  
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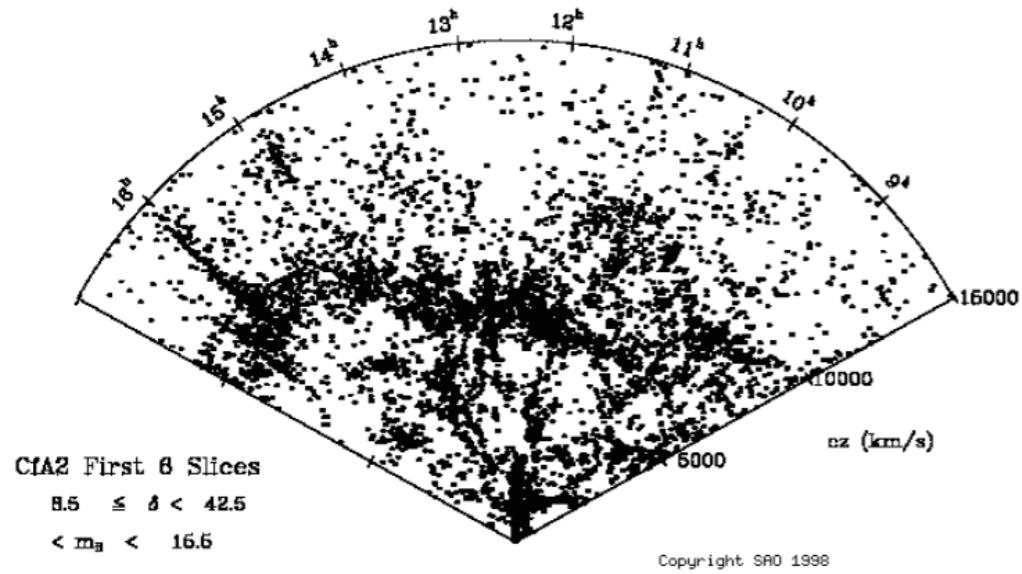
# Baryon Acoustic Oscillations



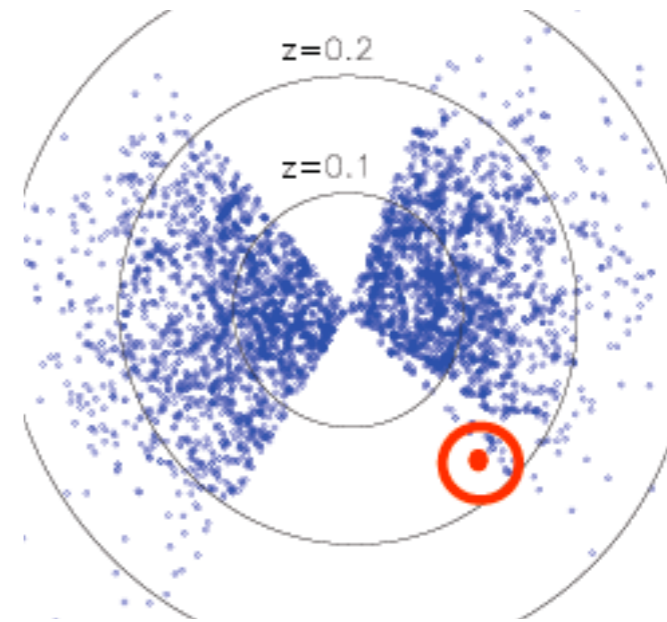
*From D. Eisenstein and M. White*



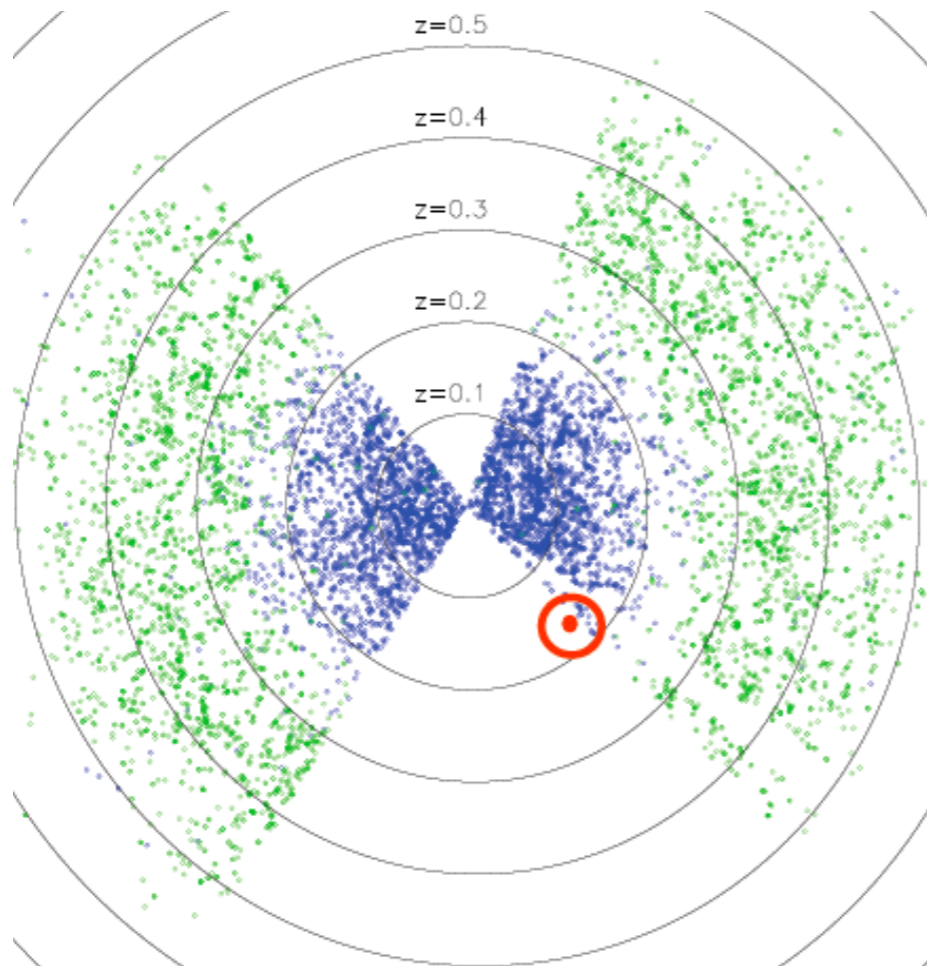
# 80's: Tiny surveys Baryon Acoustic Oscillations



BAO scale



2000: Main galaxies @SDSS.  
 Big number, but small volume

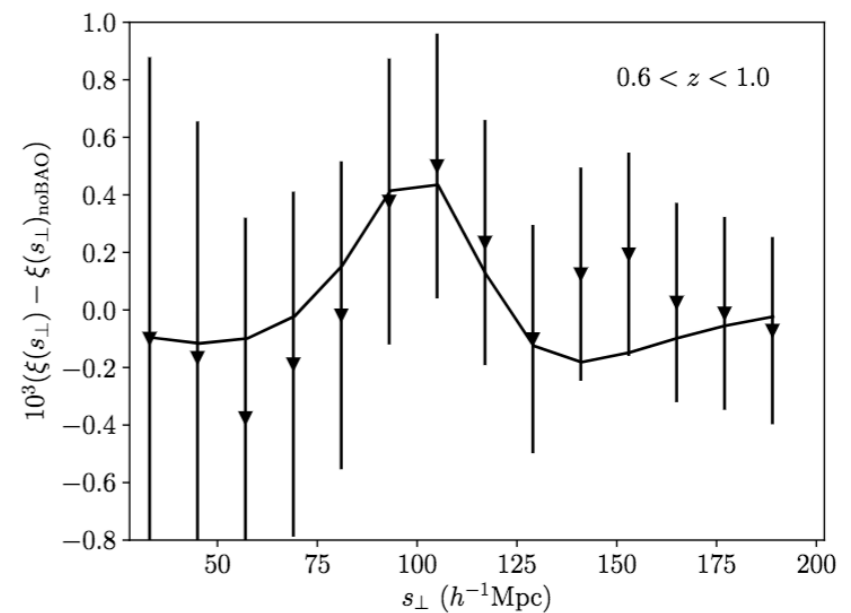
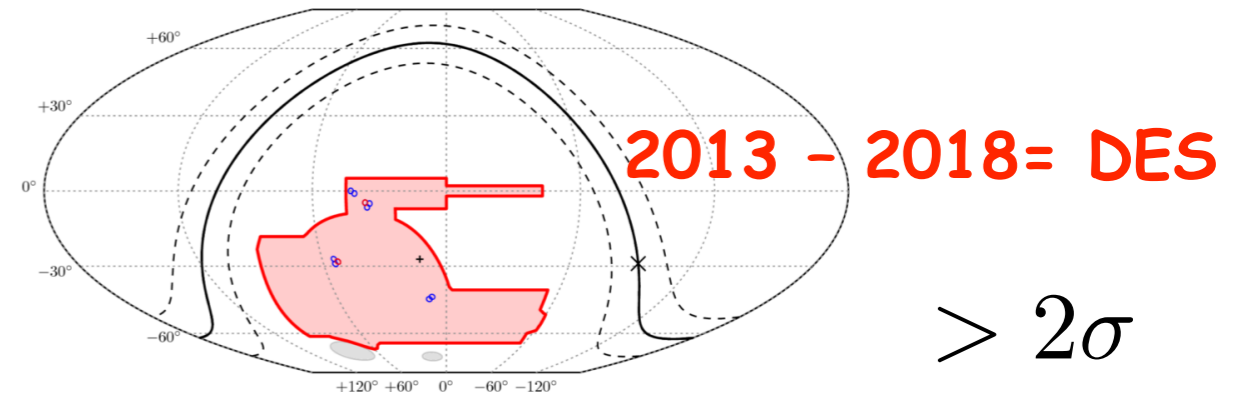
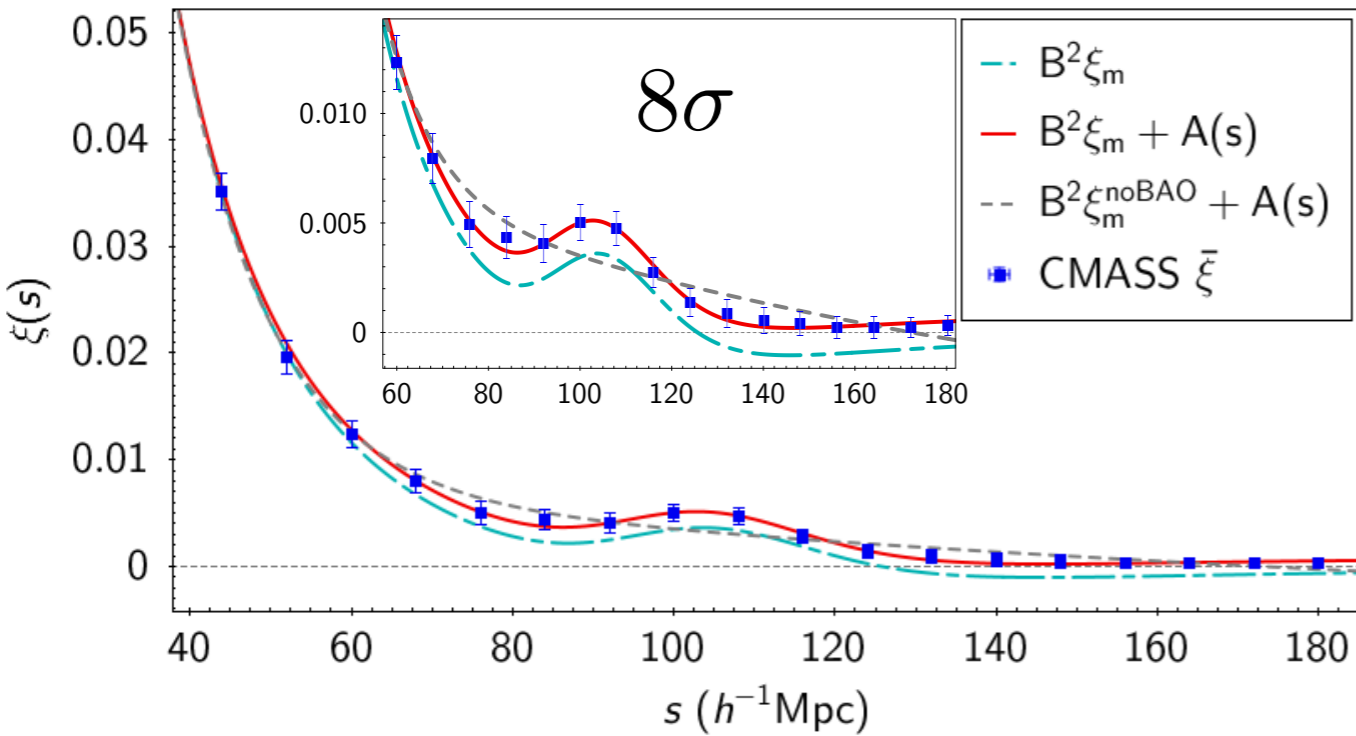
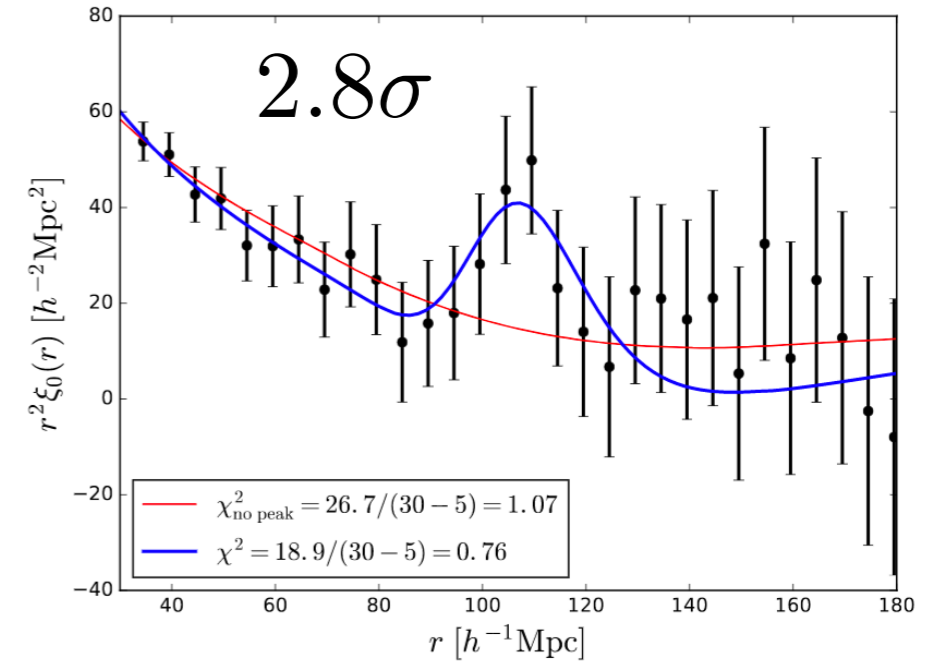
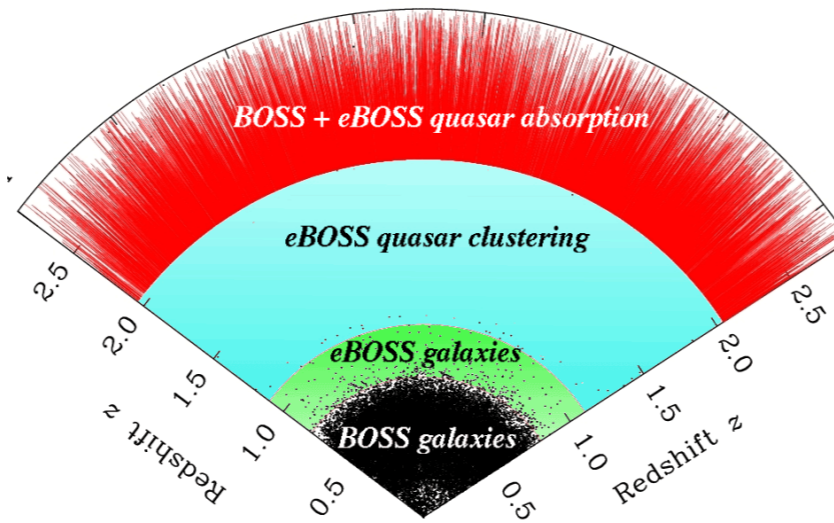
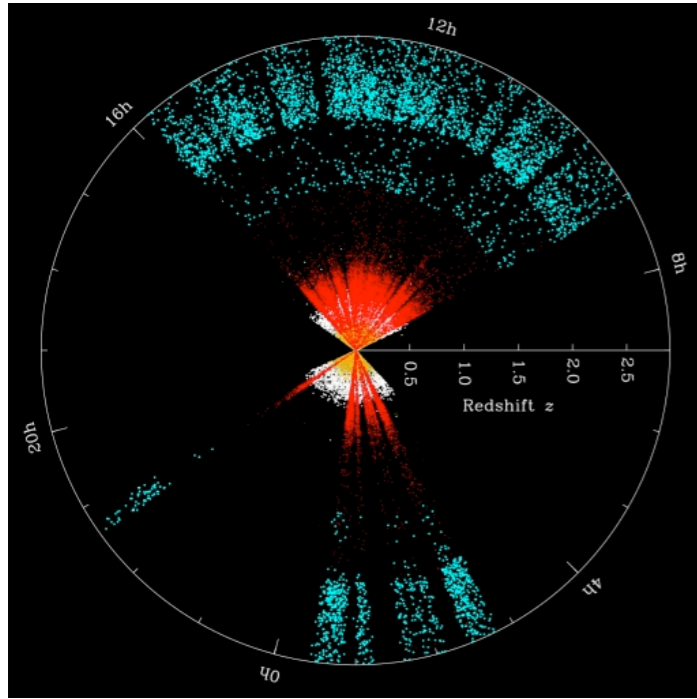


2005: Luminous Red Galaxies @ SDSS.  
 Big Volume: first detection of the BAO signature

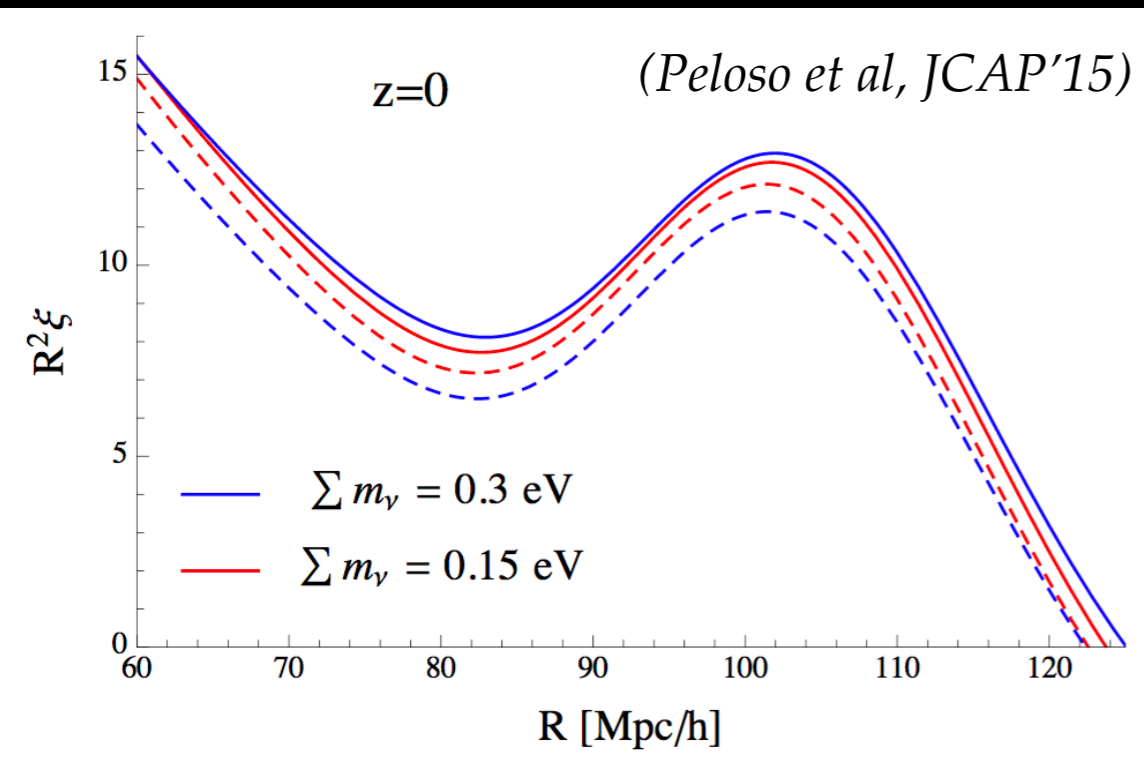
# Baryon Acoustic Oscillations

2009-2014= SDSS III

2014 - 2020= SDSS IV eBOSS



# Large scale structure and $m_\nu$



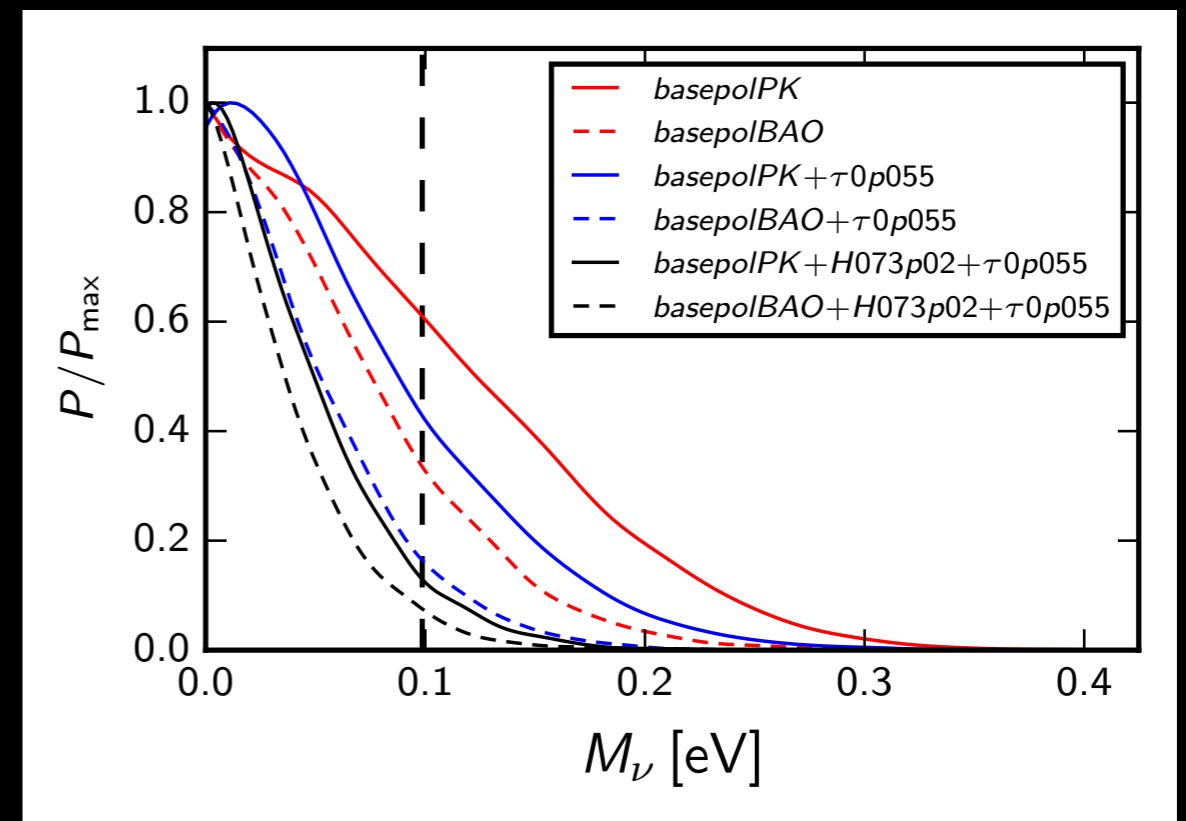
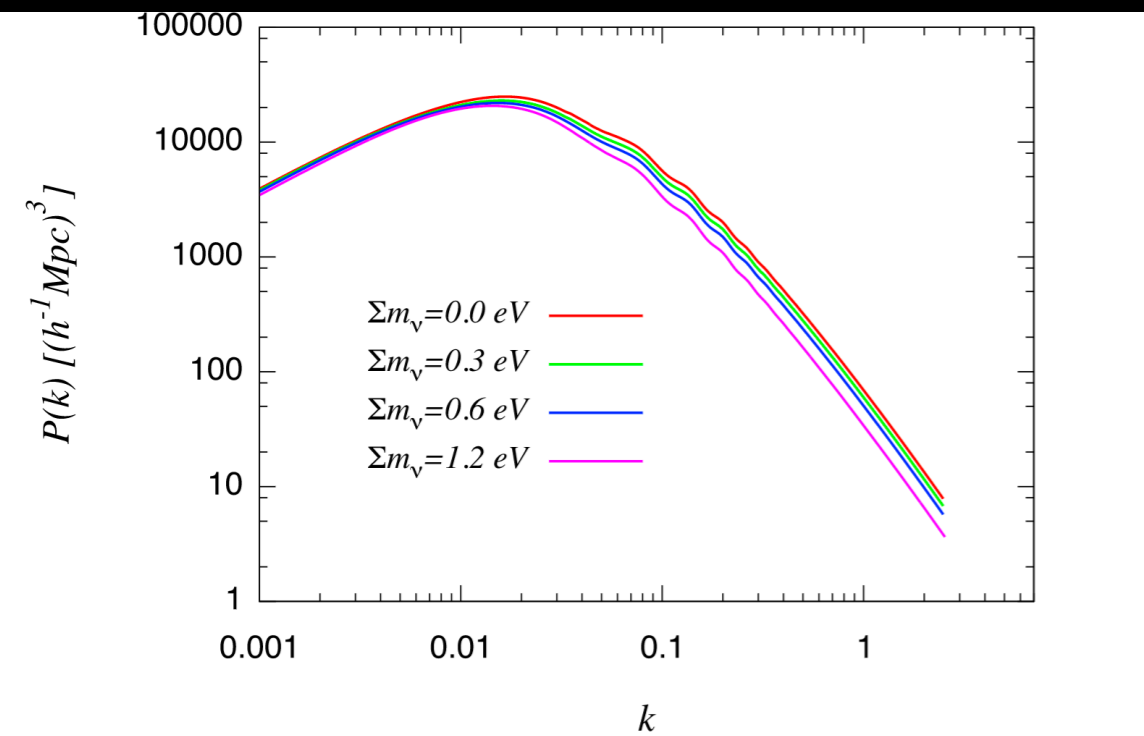
Large scale structure measurements can be interpreted either in the geometrical or shape forms

2 point correlation function

Fourier Transform

Matter power spectrum

BAO information still more powerful



One can look for  
(*sterile*) neutrinos in  
something not so  
shiny and bright....

# DARK MATTER

COLD dark matter  
HOT dark matter  
WARM dark matter

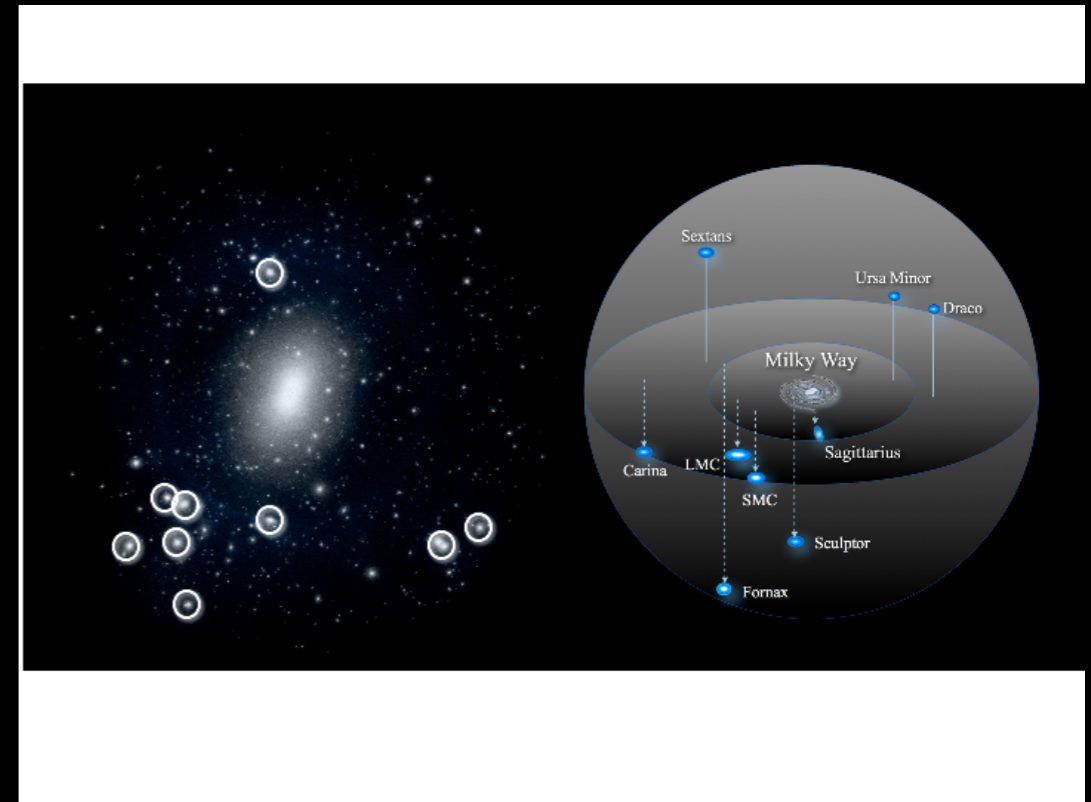
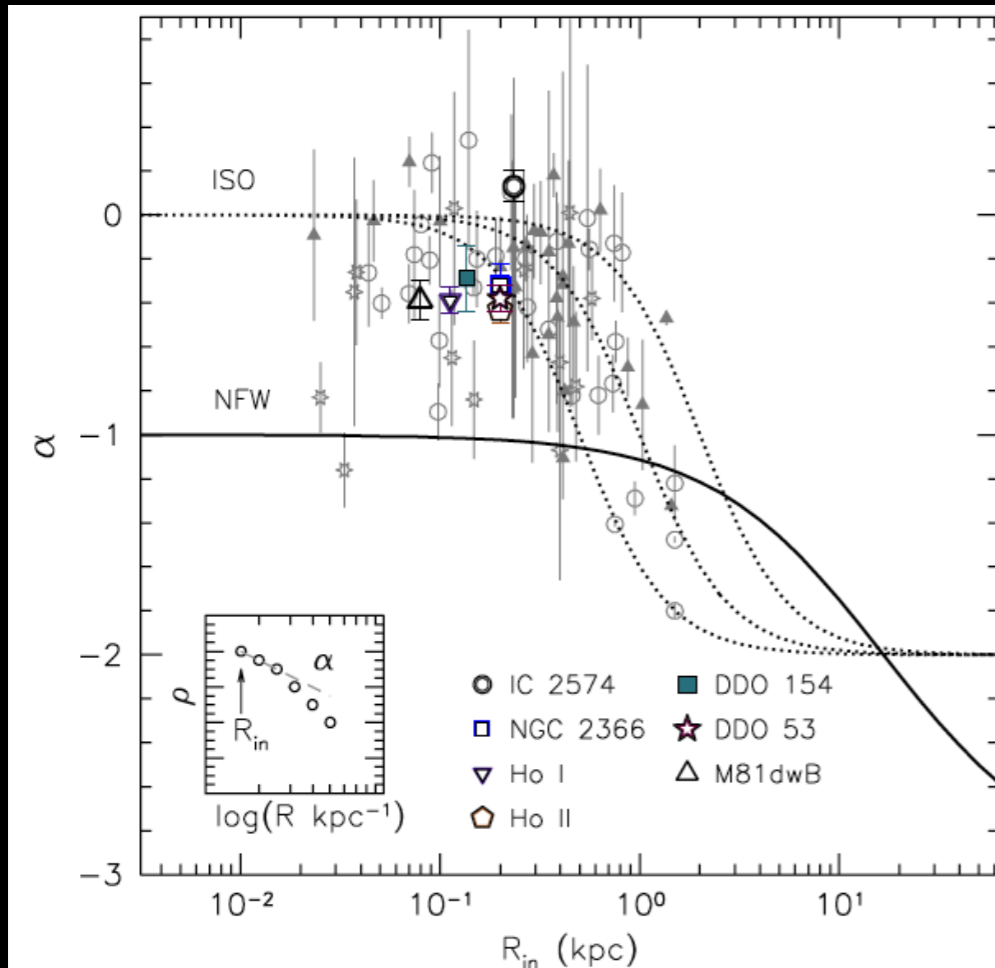
CDM  
HDM  
WDM



CREATED BY

JOSEPH MALLOZZA

# Small scale crisis of $\Lambda$ CDM@galactic and sub-galactic scales

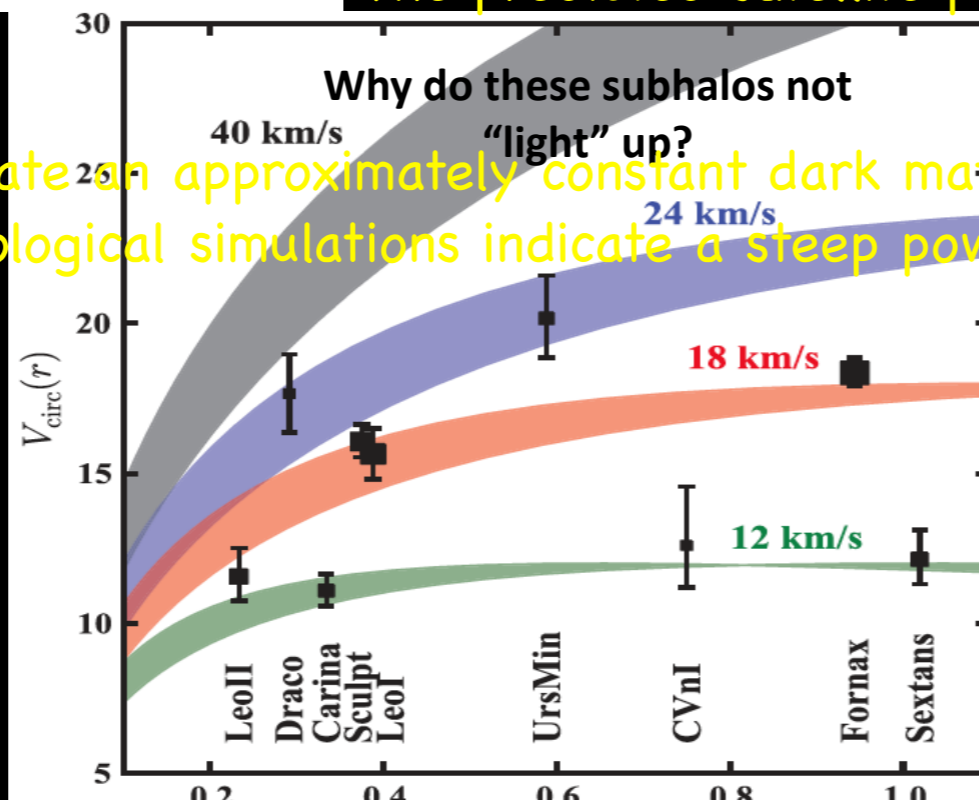


## Missing satellite problem

The predicted satellite population far exceeds the observed one

## Core/Cusp problem

Observations seem to indicate an approximately constant dark matter density in the inner parts of galaxies (core), while cosmological simulations indicate a steep power-law-like behaviour (cusp)



## Too big to fail (TBTFF) problem

Massive dark subhalos are too dense to match data.

Expected 10 subhalos in the Milky Way with  $v > 30$  km/s, only 3 known!

(Boylan et al, MNRAS'11)

# Sterile keV (0.01 $m_e$ ) neutrino as a warm dark matter candidate?

A controversial unidentified line has been detected at with a significance  $> 3\sigma$  in two independent samples of X-ray clusters with XMM-Newton.

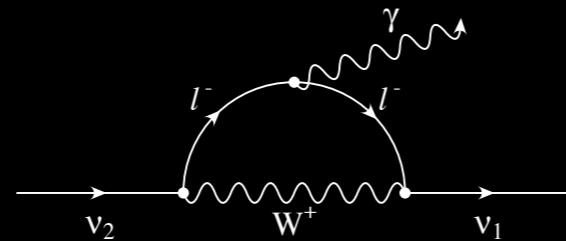


It is independently seen by the same group in the Perseus Cluster with Chandra data.



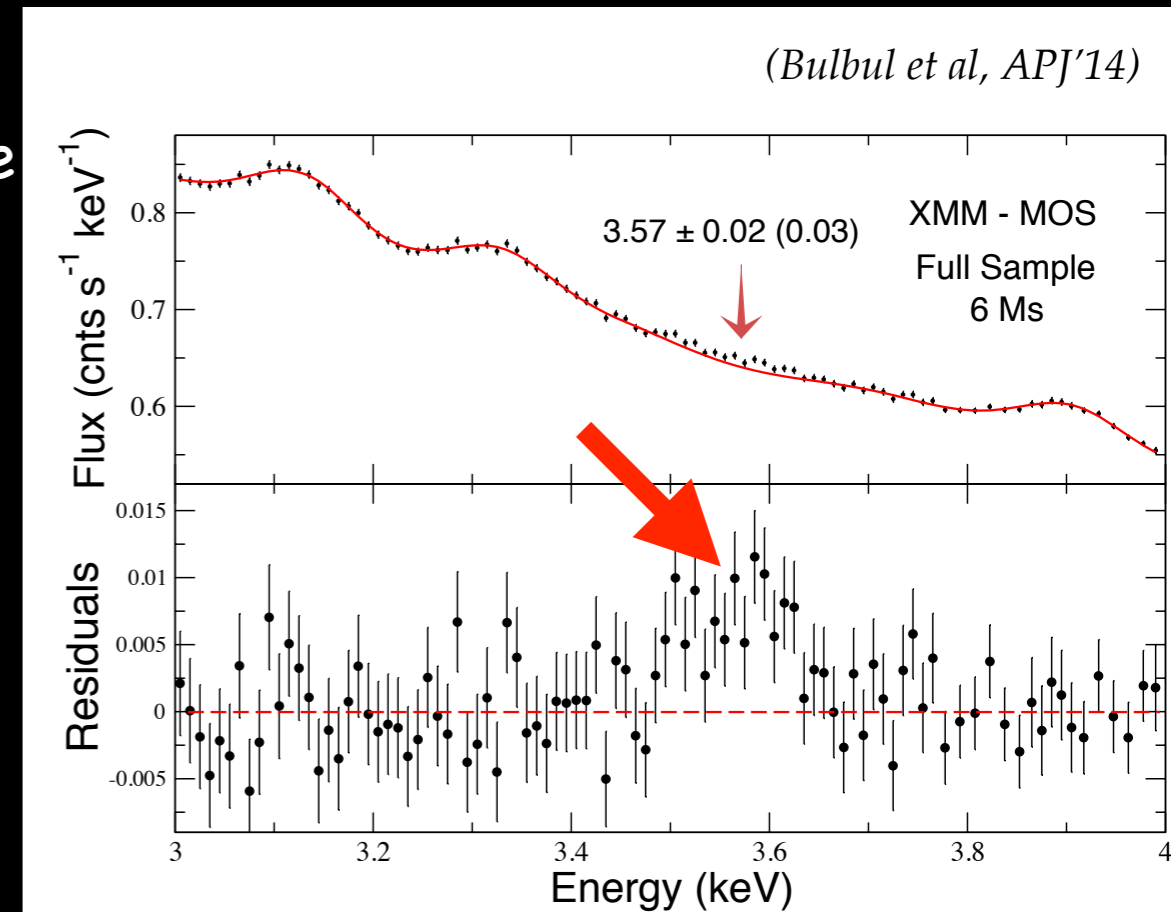
(Bulbul et al, APJ'14)

An independent group finds a line at the same energy toward Andromeda and Perseus with XMM-Newton, with a combined statistical evidence of  $4.4\sigma$ . (Boyarsky et al, PRL'14)



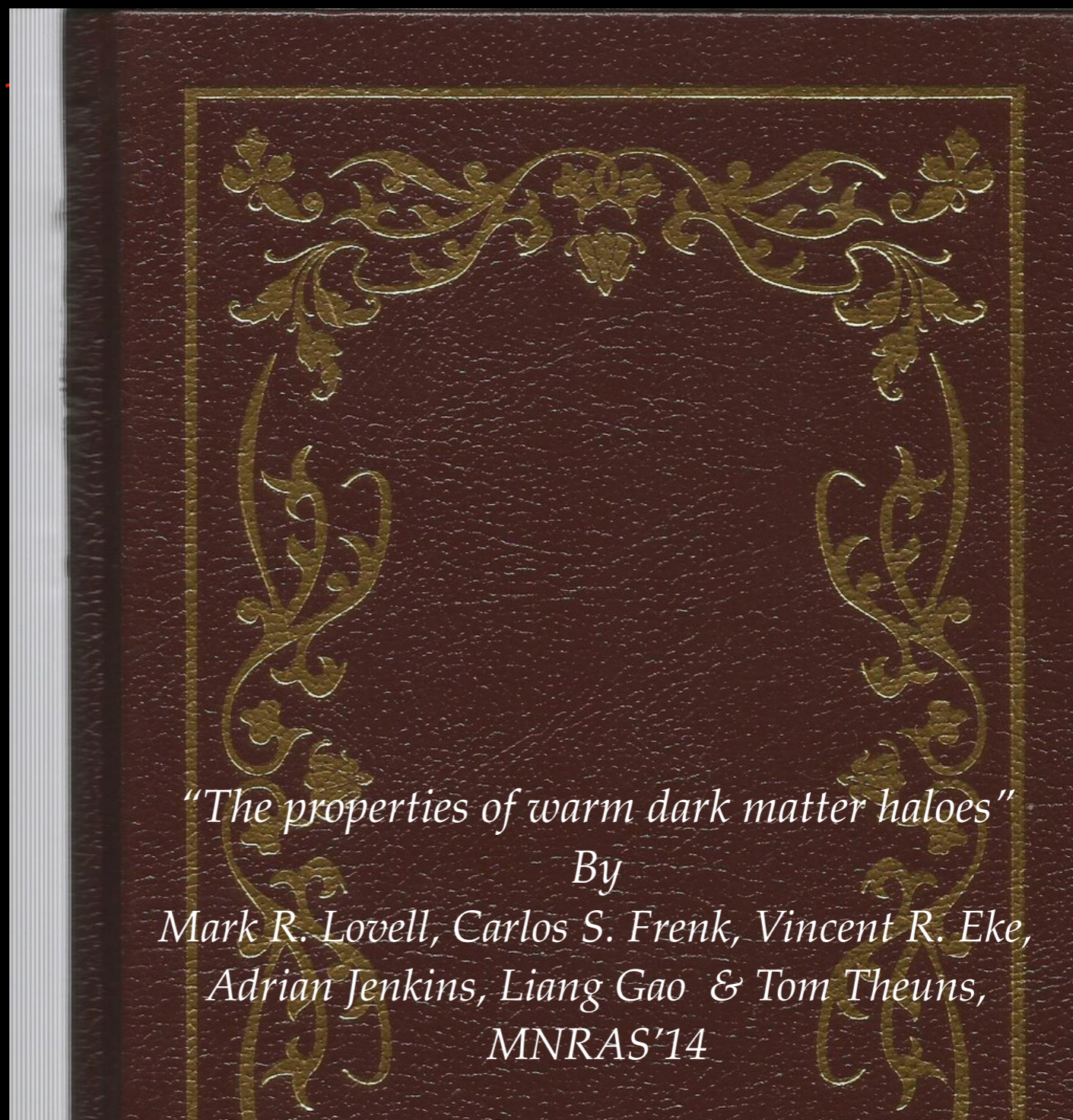
$$\nu_s \rightarrow \nu_\alpha + \gamma$$

$$m_s = 2E = 7.1 \text{ keV}$$



## Sterile keV ( $0.01 m_e$ ) neutrino as a **warm** dark matter candidate?

**WDM** leads to an identical large scale structure pattern than CDM, but very different subhaloes abundance, structure and dynamics: the free streaming of a keV sterile neutrino will reduce power at the small scales, delaying structure formation and lowering the haloes concentration.

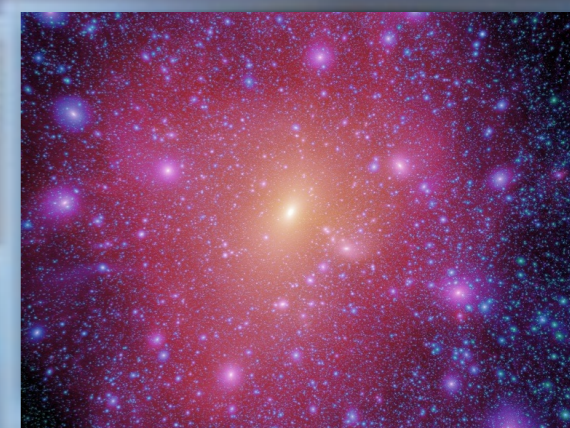




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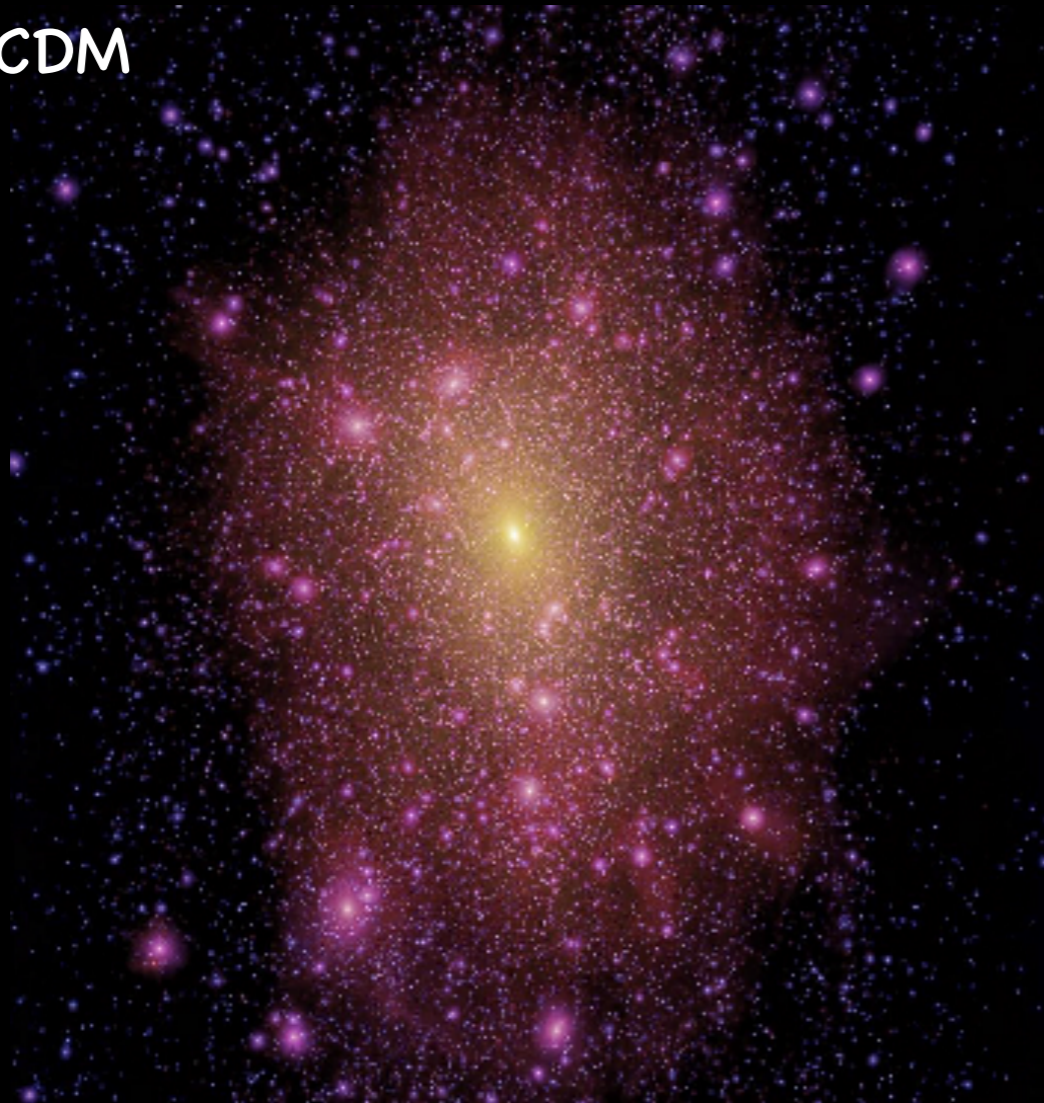
Simulations have shown that WDM can solve/alleviate the small scale crisis of  $\Lambda$ CDM



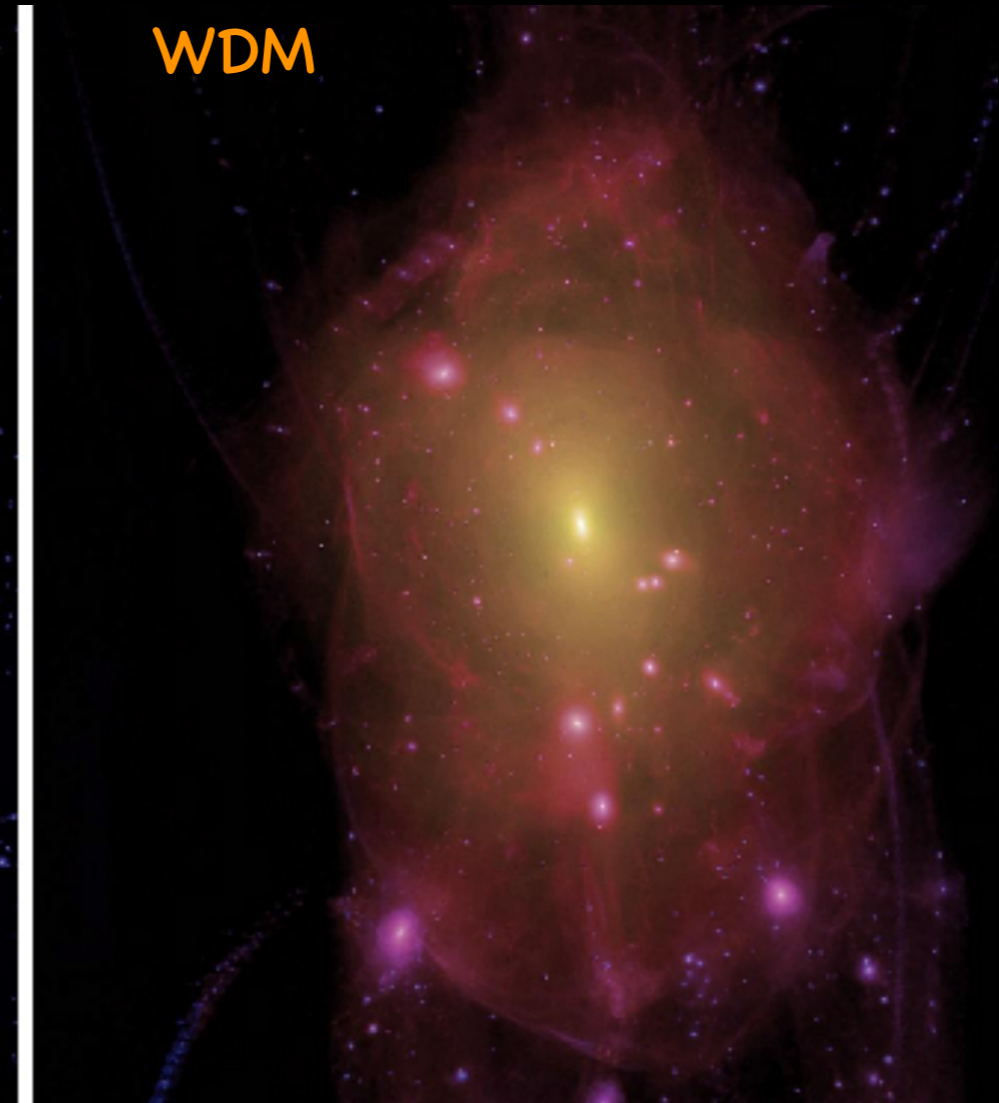
# Sterile keV ( $0.01 m_e$ ) neutrino as a warm dark matter candidate?

WDM could reconcile theory with observations!

CDM



WDM



*"The Haloes of Bright Satellite Galaxies in a Warm Dark Matter Universe", Mark R. Lovell, Vincent R. Eke, Carlos S. Frenk, Liang Gao, Adrian Jenkins, Jie Wang, D.M. White, Alexey Boyarsky & Oleg Ruchayskiy MNRAS'12*

*"The properties of warm dark matter haloes", Mark R. Lovell, Carlos S. Frenk, Vincent R. Eke, Adrian Jenkins, Liang Gao & Tom Theuns, MNRAS'14*

Backup material

- The entropy density is:  $s \equiv \frac{\rho + p}{T}$

¿How are related the photon and the neutrino temperatures?

- Electron positron annihilation takes place **AFTER** neutrino decoupling.
- In an expanding universe the entropy density per comoving volume is conserved:

- Boson's entropy contribution:
- Fermion's entropy contribution:

$$2\pi^2 T^3 / 45$$

$$7/8 \times 2\pi^2 T^3 / 45$$

- Before electron/positron annihilation= electrons ( $g=2$ ), positrons ( $g=2$ ), neutrinos (3), antineutrinos (3) and photons ( $g=2$ ) therefore:

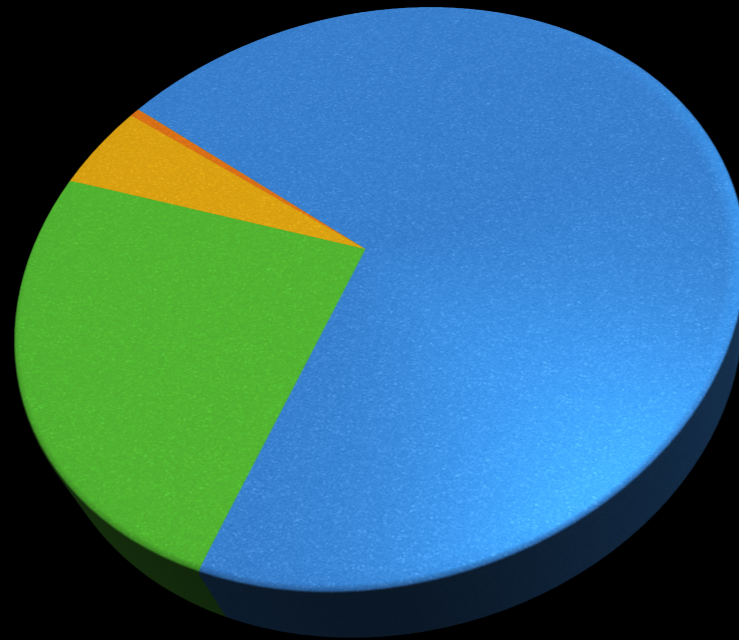
$$s(a_1) = 2\pi^2 T_1^3 / 45 (2 + 7/8(2 + 2 + 3 + 3))$$

- After, only neutrinos, antineutrinos and photons but at different temperature!

$$s(a_2) = 2\pi^2 / 45 (2T_\gamma^3 + 7/8(3 + 3)T_\nu^3)$$

$$s(a_1)a_1^3 = s(a_2)a_2^3 \quad a_1 T_1 = a_2 T_\nu \quad \longrightarrow \quad \left(\frac{T_\nu}{T_\gamma}\right) = \left(\frac{4}{11}\right)^{1/3}$$

# Summary's Dessert Cosmic Cake



**Sterile neutrino masses and abundances leave key signatures in cosmological observables.**

**Abundances ( $N_{\text{eff}}$ ) : via Cosmic Microwave Background measurements damping tail & Big Bang Nucleosynthesis light element abundances,  $N_{\text{eff}} < 3.41$  (@95%CL).**

**Masses: neutrino free-streaming nature induce a small-scale suppression matter power spectrum,  $m_{\nu, \text{eff}} < 0.7$  eV ( $< 0.0000014 m_e$ ) (@95%CL).**

**No current cosmological evidence for sterile neutrinos or dark radiation.**

**Warm Dark Matter sterile keV neutrinos: alleviate/solve mostly all the small scale problems of the standard Cold Dark Matter scenario, still a very interesting option!**

# Massive neutrinos cosmological signatures: $m_\nu$

Growth equation for a single uncoupled fluid, linear regime, with constant sound speed:

$$\ddot{\delta} + \underbrace{2\frac{\dot{a}}{a}\dot{\delta}}_{\text{Hubble drag}} - \underbrace{c_s^2 k^2 \frac{\delta}{a^2}}_{\text{Pressure}} = \underbrace{4\pi G\rho\delta}_{\text{Gravity}}$$

Jeans scale:

$$k_J \equiv \sqrt{\frac{4\pi G\rho}{c_s^2(1+z)^2}}$$

$k > k_J$  no growth can occur

$k < k_J$  density perturbations growth

Neutrino free streaming scale:

$$k_{fs,\nu}(z) \equiv \sqrt{\frac{3}{2}} \frac{H(z)}{(1+z)\sigma_{\nu,\nu}(z)}$$

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# $N_{\text{eff}}$ dark radiation species cosmological signatures

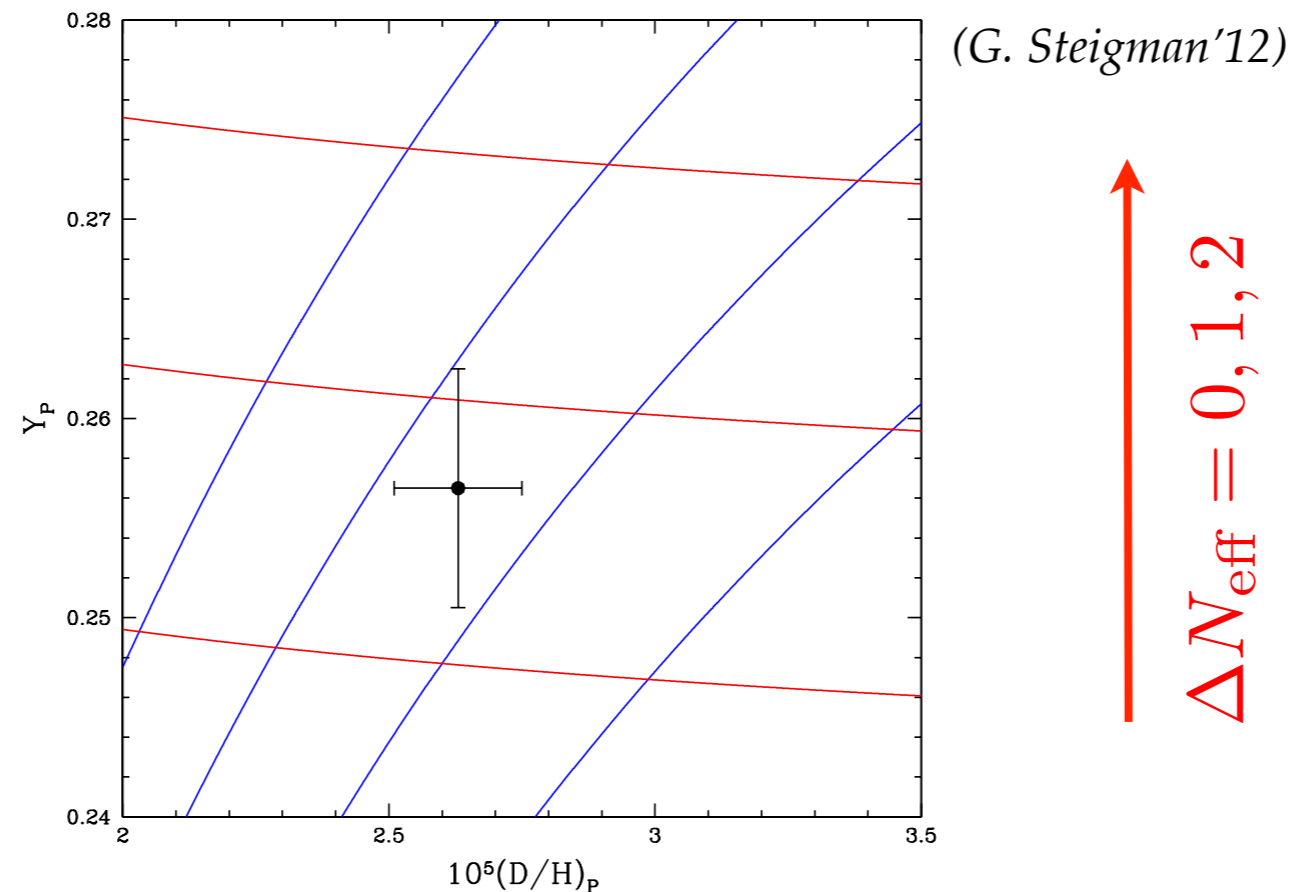
$N_{\text{eff}}$  changes the freeze out temperature of weak interactions:

$$\Gamma_{n \leftrightarrow p} \sim H$$

$$\Omega_r h^2 = \left( 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right) \Omega_\gamma h^2$$

Higher  $N_{\text{eff}}$ , Higher expansion rate, higher freeze out temperature, higher  $^4\text{He}$  fraction:

$$n/p \simeq e^{-\frac{m_n - m_p}{T_{\text{freeze}}}} \quad Y_p = \frac{2(n/p)}{1 + n/p}$$





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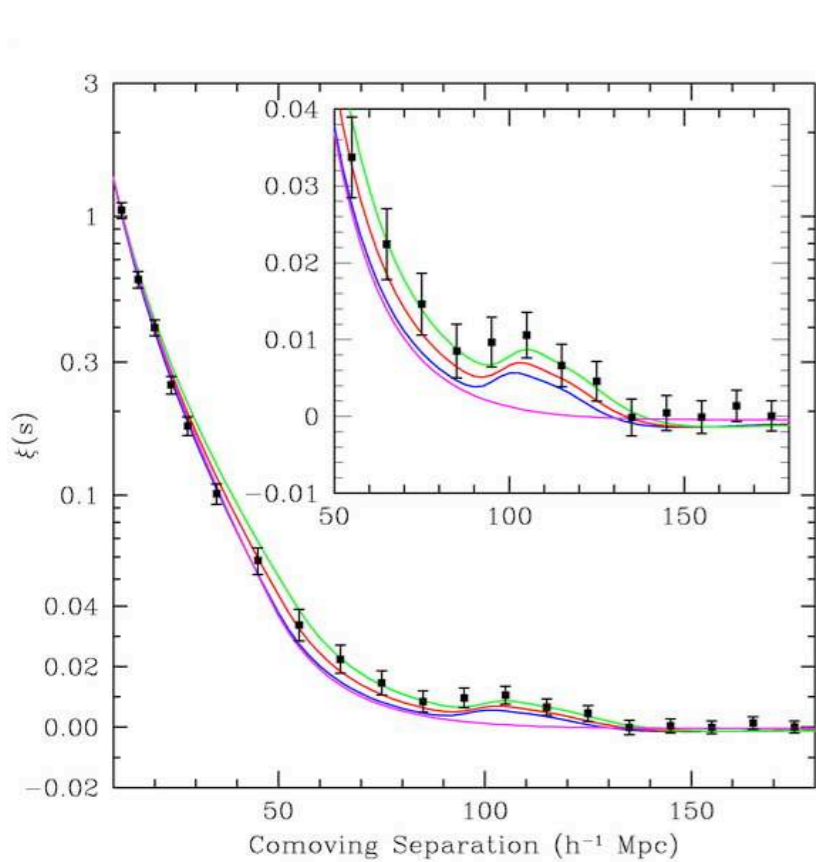
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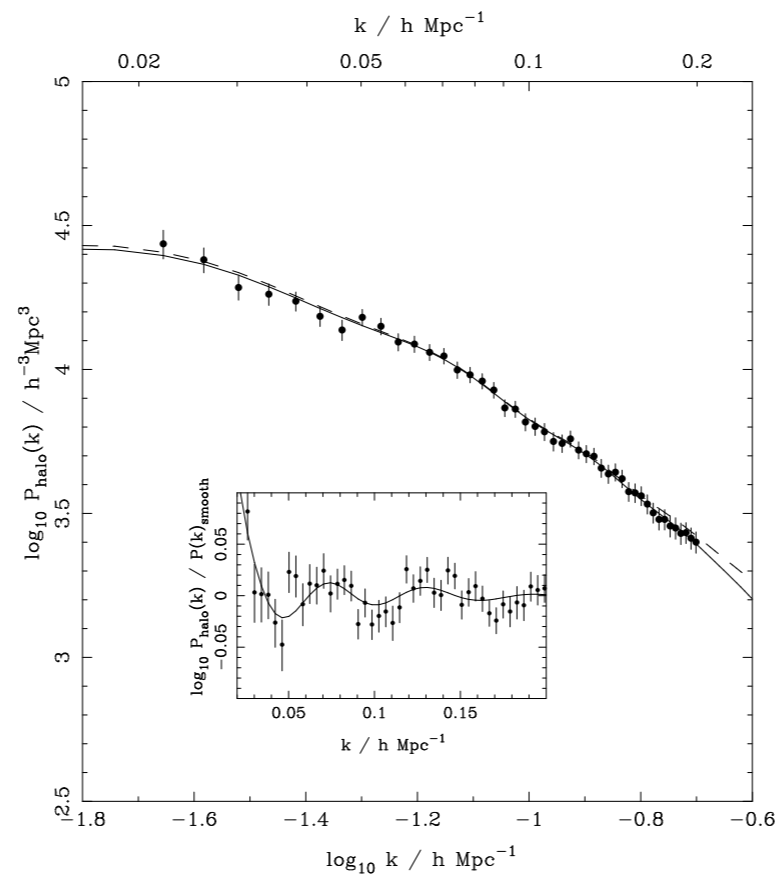
Los catálogos de galaxias miden la función de correlación:

$$\xi(\vec{r}) \equiv \langle \delta(\vec{x}) \delta(\vec{x} + \vec{r}) \rangle_{\text{Volume}} \quad \langle \tilde{\delta}(\vec{k}) \tilde{\delta}(\vec{k}') \rangle_{\text{Volume}} = (2\pi)^3 P(k) \delta^3(\vec{k} - \vec{k}')$$

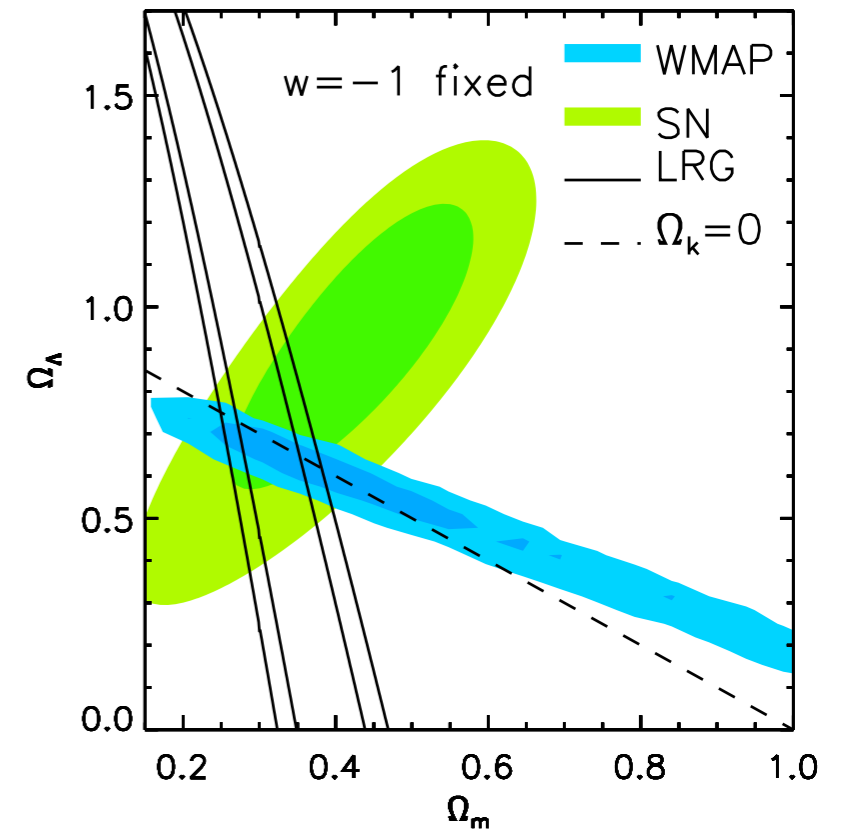
$$\delta(\vec{x}) \equiv \frac{\rho(\vec{x}) - \bar{\rho}(\vec{x})}{\bar{\rho}(\vec{x})} \quad \tilde{\delta}(\vec{k}) \equiv \int d^3\vec{r} e^{i\vec{k}\vec{r}} \delta(\vec{r})$$



Eisenstein et al'05



Reid et al'09



SSDS 2005: Primera detección de la señal BAO (3.4s) (47000 LRGs, 4000 deg<sup>2</sup> , z=0.35)

SDSS II 2009: 110 000 LRGs, 8000 deg<sup>2</sup> , z=0.35.