

# Imprints of parity violation from gravitational waves V modes

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# Outline

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1. Importance of  $pnG$  to detect  $P$ -violation in the early-universe.
2. Current probes of  $P$ -violation.
3. Anisotropies in circular-polarized SGWB to probe  $P$ -violation.

# Role of pnG, scalar sector

$$\langle X_{\mathbf{k}_1} \dots X_{\mathbf{k}_n} \rangle_{\text{odd}} = \langle X_{\mathbf{k}_1} \dots X_{\mathbf{k}_n} \rangle - P(\langle X_{\mathbf{k}_1} \dots X_{\mathbf{k}_n} \rangle)$$

$$X = \zeta, \gamma^\lambda$$

- Assuming **homogeneity and isotropy**, not all primordial correlators matter.

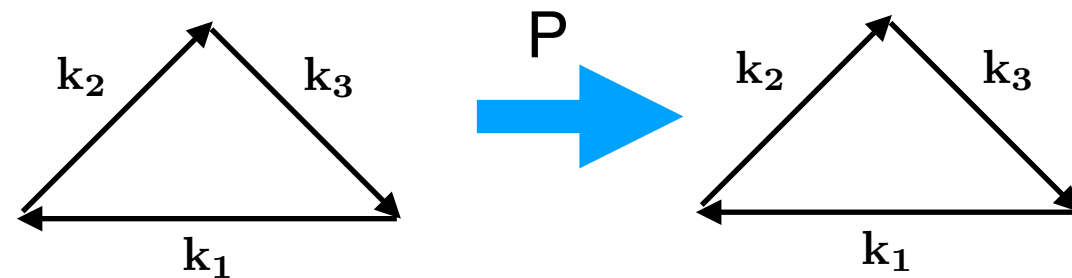
## - POWER SPECTRUM AND BISPECTRUM:

- Need only **magnitude of momenta**.

$$P(\langle \zeta_{k_1} \zeta_{k_2} \rangle) = \langle \zeta_{k_1} \zeta_{k_2} \rangle$$

$$P(\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle) = \langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle$$

$$\langle \zeta \zeta \rangle_{\text{odd}} = \langle \zeta \zeta \zeta \rangle_{\text{odd}} = 0$$

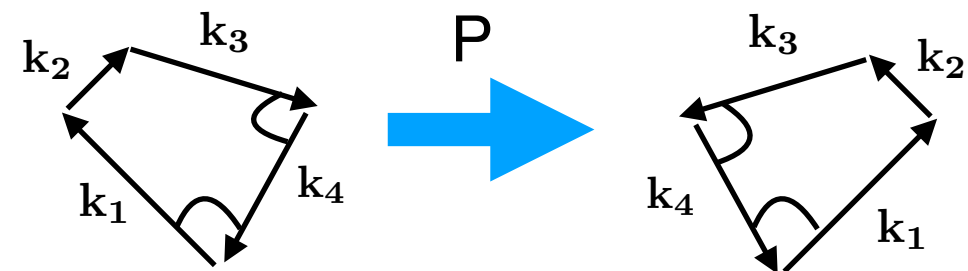


## - TRISPECTRUM:

- Need **magnitude of momenta + 2 angles**.

$$P(\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \zeta_{k_4} \rangle) \neq \langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \zeta_{k_4} \rangle$$

$$\langle \zeta \zeta \zeta \zeta \rangle_{\text{odd, NG}} \neq 0$$



# Role of pnG, tensor sector

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- Tensor perturbations possess 2 polarization states, **R- and L-handed**:  $P(\gamma_{\mathbf{k}}^R) = \gamma_{-\mathbf{k}}^L$

## - POWER SPECTRUM:

$$P(\langle \gamma_{\mathbf{k}}^R \gamma_{\mathbf{k}}^R \rangle) = \langle \gamma_{\mathbf{k}}^L \gamma_{\mathbf{k}}^L \rangle$$

$$\langle \gamma_{\mathbf{k}} \gamma_{\mathbf{k}} \rangle|_{\text{odd}} = \langle \gamma_{\mathbf{k}}^R \gamma_{\mathbf{k}}^R \rangle - \langle \gamma_{\mathbf{k}}^L \gamma_{\mathbf{k}}^L \rangle$$

- Issue: **tensor perturbations not detected yet.**

( $r < 0.032$ , *Tristram et. al. 2022*)

- **tensor perturbations detected  $\rightarrow$  S/N  $\sim r$  (CMB):**  
(e.g. *Gerbino et. al. 2016*) **challenging to observe.**

## - TENSOR AND SCALAR-TENSOR BISPECTRA: $\langle \zeta \zeta \gamma \rangle_{\text{odd}}, \langle \zeta \gamma \gamma \rangle_{\text{odd}}, \langle \gamma \gamma \gamma \rangle_{\text{odd}}$

e.g.  $\langle \zeta \zeta \gamma \rangle|_{\text{odd}} = \langle \zeta_{k_1} \zeta_{k_2} \gamma_{k_3}^R \rangle - \langle \zeta_{k_1} \zeta_{k_2} \gamma_{k_3}^L \rangle$

- **Tensor perturbations detected  $\rightarrow$  S/N  $\approx r$  (CMB).**  
(e.g. *Shiraishi 2019*)

**pnG PLAY A FUNDAMENTAL ROLE in detecting P-violation!**

# Current probes of P-violation

## CMB (2D):

- **POWER SPECTRUM:**  $\langle \gamma_k \gamma_k \rangle |_{\text{odd}} \longrightarrow \langle TB \rangle, \langle EB \rangle$   
(e.g. Gerbino et. al. 2016)

**Challenging:**

$$S/N \sim r$$

**No detection of B modes**

- **BISPECTRUM:**  $\langle \gamma_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle |_{\text{odd}} \longrightarrow \langle BTT \rangle$   
(e.g. Shiraishi, Liguori, Fergusson 2015; Bartolo, **Orlando**, Shiraishi 2017; Shiraishi 2019)

**No detection of B modes**

- **TRISPECTRUM:**  $\langle \zeta_{\mathbf{k}_1} \zeta_{\mathbf{k}_2} \zeta_{\mathbf{k}_3} \zeta_{\mathbf{k}_4} \rangle |_{\text{odd}} \longrightarrow \langle TTTT \rangle$   
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**Cosmic variance**

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**Cosmic variance**

## Large Scale Structures:

Galaxy shear (2D):

- POWER SPECTRUM:  $\langle \gamma_k \gamma_k \rangle |_{\text{odd}} \longrightarrow \langle EB \rangle$   
(e.g. Biagetti, **Orlando** 2020)

**Challenging:**

$$S/N \sim r$$

**No detection of B modes**

Large scale overdensity-field (3D):

- TRISPECTRUM:  $\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \zeta_{k_4} \rangle |_{\text{odd}} \longrightarrow \langle \delta\delta\delta\delta \rangle$

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**Recent OBSERVATION  
in BOSS!**

Seen in Oliver Philcox's talk

# First ever claimed detection

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- The **cosmic birefringence** signal recently claimed (*e.g.*  $3.6\sigma$  in *Eskilt, Komatsu 2022*) **cannot be explained by inflation!** The associated  $r \sim 10^2$  is above the CMB constraint: **overproduction of  $B$  modes** (*e.g.* *Fujita et. al. 2022*).
- **First ever claimed detection of P-violation** that can be associated to inflation ( $3\sigma$  in *Philcox 2022*;  $7\sigma$  in *Hou et. al. 2022*).
- If confirmed, **smoking-gun for beyond single-field slow-roll models!**



# Future: V modes from SGWB direct detection

Previous talks:

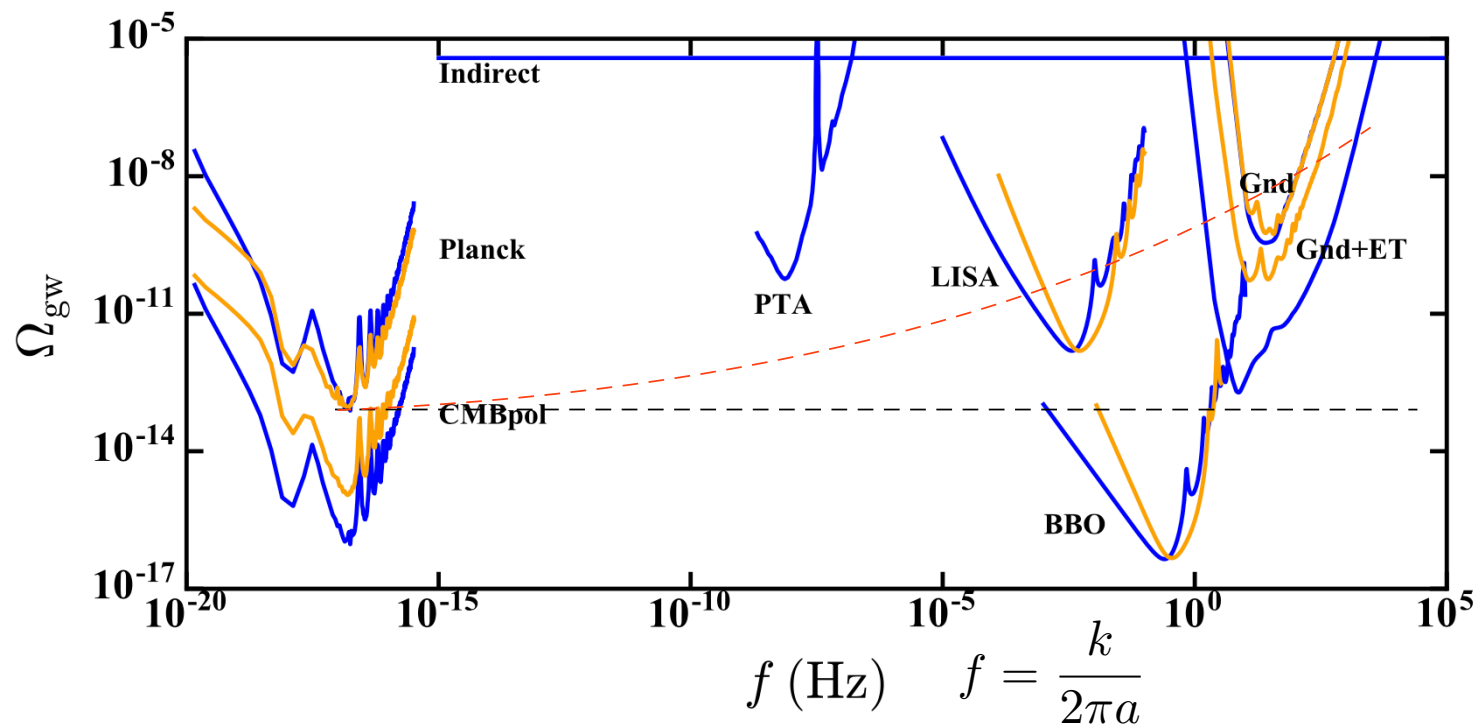
Unpolarised GWs (I modes):

$$\Omega_{\text{GW}}^I(k) \propto \langle \gamma_k^R \gamma_k^R \rangle + \langle \gamma_k^L \gamma_k^L \rangle$$

Circular polarised GWs (V modes):

$$\Omega_{\text{GW}}^V(k) \propto \langle \gamma_k^R \gamma_k^R \rangle - \langle \gamma_k^L \gamma_k^L \rangle$$

**P-violation!**



----- Growth-mechanism  
(2030-2040):  
LISA  
Taiji  
Einstein Telescope  
Cosmic Explorer

..... (2040-2050):  
BBO  
DECIGO

Courtesy of Smith, Caldwell 2016

# SGWB V modes

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$$\Omega_{\text{GW}}^V(k, \hat{n}) = \bar{\Omega}_{\text{GW}}^V(k) + \delta_{\text{GW}}^V(k, \hat{n})$$

# SGWB V modes monopole

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$$\Omega_{\text{GW}}^V(k, \hat{n}) = \overline{\Omega}_{\text{GW}}^V(k) + \delta_{\text{GW}}^V(k, \hat{n})$$

(e. g. *Seto, Taruya 2008; Smith, Caldwell 2016; Domcke et. al. 2019; Orlando, Pieroni, Ricciardone 2020; Seto 2020*)

$$\overline{\Omega}_{\text{GW}}^V(k) \propto \langle \gamma_k^R \gamma_k^R \rangle - \langle \gamma_k^L \gamma_k^L \rangle$$

$k_{\text{GW}} \gg k_{\text{CMB}} \longrightarrow r_{\text{GW}}$  evades CMB constraint  $\longrightarrow$  Hope to measure the parity-odd tensor power spectrum

# Recent: SGWB V modes anisotropies

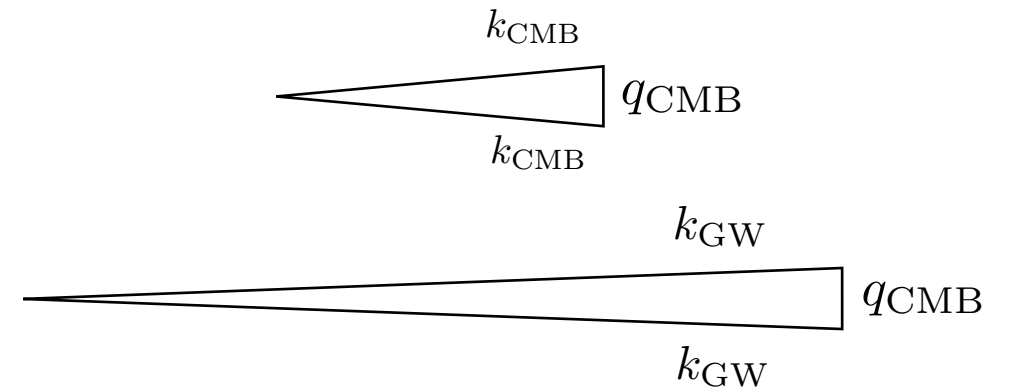
$$\Omega_{\text{GW}}^V(k, \hat{n}) = \bar{\Omega}_{\text{GW}}^V(k) + \delta_{\text{GW}}^V(k, \hat{n})$$

- New: study **V modes intrinsic anisotropies** (G. Orlando 2022, arXiv:2206.14173)

- Previous talks:  $\Omega_{\text{GW}}^I(k, \hat{n}) = \bar{\Omega}_{\text{GW}}^I(k) + \delta_{\text{GW}}^I(k, \hat{n})$

$$\delta_{\text{GW}}^I(\hat{n}) \sim f_{\text{NL}}^{ttt, sq}, f_{\text{NL}}^{tts, sq}$$

$$f_{\text{NL}}^{tts, sq} = f_{\text{NL}}^{RRs, sq} + f_{\text{NL}}^{LLs, sq}$$



(e.g. Adshead et. al. 2021; Malhotra et. al. 2021; Dimastrogiovanni et. al. 2021-2022)

- I modes  $\rightarrow$  V modes:

$$\begin{aligned} \delta_{\text{GW}}^V(\hat{n}) &\sim f_{\text{NL}}^{RRR, sq} - f_{\text{NL}}^{LLL, sq} \\ &\sim f_{\text{NL}}^{RRs, sq} - f_{\text{NL}}^{LLs, sq} \end{aligned}$$

**Sourced by  $\langle tts \rangle_{\text{odd}}$  and  $\langle ttt \rangle_{\text{odd}}$  ultra-squeezed bispectra**

# A non-linear probe of parity violation

- V modes angular power-spectrum:

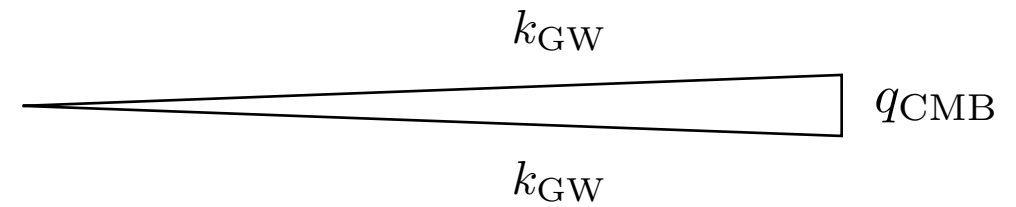
$$C_\ell^{VV} = \frac{1}{2\ell + 1} \sum_m \langle \delta_{\text{GW},\ell m}^V \delta_{\text{GW},\ell m}^{*V} \rangle$$

$$C_0^{VV}(k) \sim [\mathcal{A}_t^R(k) - \mathcal{A}_t^L(k)]^2$$

$$C_\ell^{VV}(k)|_{\langle tts \rangle} \sim \int dq \dots \mathcal{A}_s(q) [\mathcal{A}_t^R(k) f_{\text{NL}}^{\text{RRS}}(k, q) - \mathcal{A}_t^L(k) f_{\text{NL}}^{\text{LLS}}(k, q)]^2 \quad \ell \geq 1$$

$$C_\ell^{VV}(k)|_{\langle ttt \rangle} \sim \int dq \left\{ \mathcal{A}_t^R(q) \left[ \mathcal{A}_t^R(k) f_{\text{NL}}^{\text{RRR,ttt}}(k, q) - \mathcal{A}_t^L(k) f_{\text{NL}}^{\text{LRR,ttt}}(k, q) \right]^2 + \right. \\ \left. + \mathcal{A}_t^L(q) \left[ \mathcal{A}_t^L(k) f_{\text{NL}}^{\text{LLL,ttt}}(k, q) - \mathcal{A}_t^R(k) f_{\text{NL}}^{\text{RLL,ttt}}(k, q) \right]^2 \right\}$$

$\mathcal{A} :=$  power-spectra amplitudes



- V modes anisotropies sourced by:

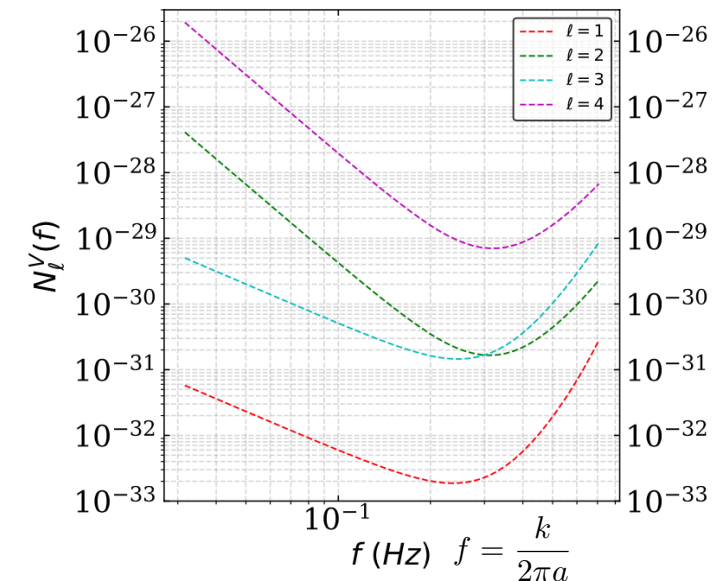
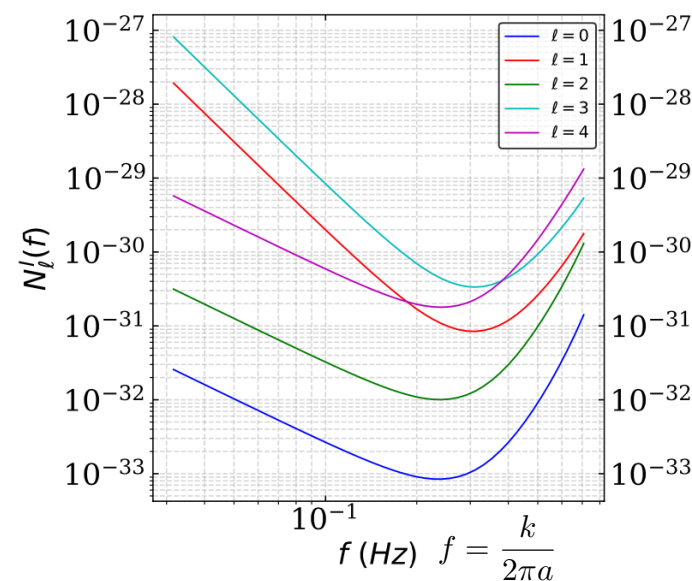
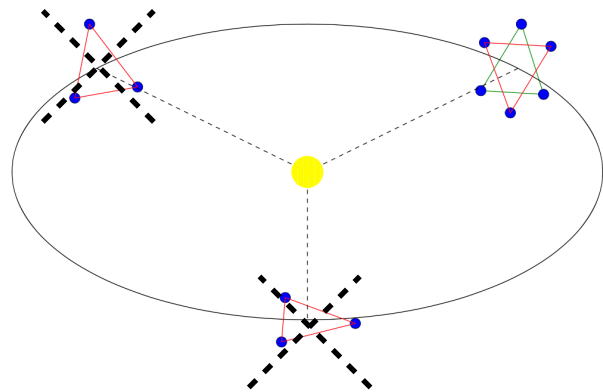
-  $\langle tts \rangle_{\text{even}}$  and  $\langle ttt \rangle_{\text{even}}$  +  $\langle tt \rangle_{\text{odd}}$  ( **V modes monopole  $\neq 0$**  )

-  $\langle tts \rangle_{\text{odd}}$  and  $\langle ttt \rangle_{\text{odd}}$  +  $\langle tt \rangle_{\text{even}}$  ( **V modes monopole = 0** )

# Detection prospects

- Main difference with I modes case: in **V modes** channel there is **no contamination** from **astrophysical** GW backgrounds and **negligible** from **induced** anisotropies.
- Noise curves obtained with well-established pipeline (*Alonso et. al. 2020*).

- **BBO/DECIGO-like experiment, early-stage.**



- Fisher-forecast on **parity-odd**  $\langle \text{tts} \rangle$ :

(from **G. Orlando 2022**)

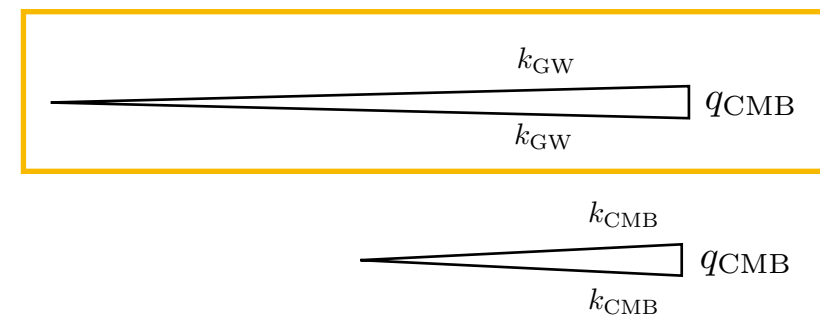
$$f_{\text{NL}}^{\text{tts,odd}} \Big|_{5\text{yrs}}^{\text{GW}} \sim 10^3 \times \left( \frac{0.01}{r_{\text{GW}}} \right)$$

(Orlando 2022)

VS

$$f_{\text{NL}}^{\text{tts,odd}} \Big|_{\text{B-mode, } \ell_{\text{max}}=100}^{\text{CMB}} \sim 10^4$$

(Bartolo, Orlando, Shiraishi 2017)



Message:  $r_{\text{GW}} \gtrsim 10^{-3}$  **competitive** (not only complementary) with **CMB experiments!**

# Take home message

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- **PnG important** to detect **P-violation** in the early-universe (scalar and tensor sectors).
- **Anisotropies in SGWB circular polarization** can probe **P-violation** in tensor and tensor-scalar **pnG** on **configurations inaccessible to large-scale experiments**.
- In the future, **gravitational-wave experiments** will probe parity-odd  $\langle tts \rangle$  with a **sensitivity competitive** with **CMB experiments**.

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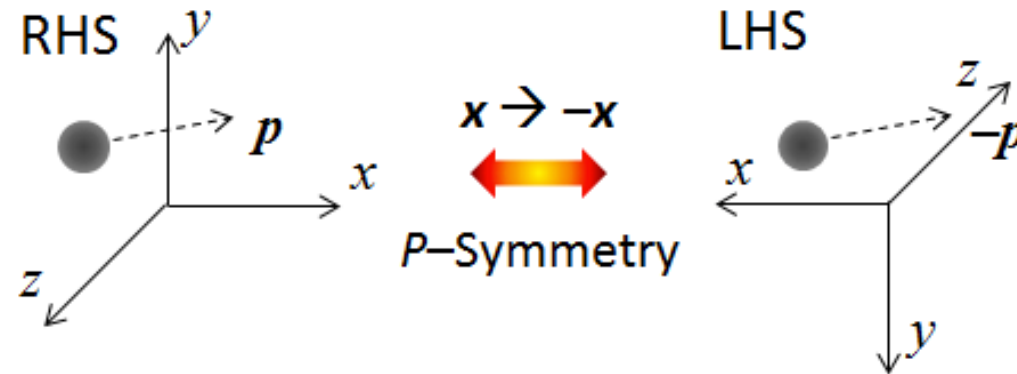
THANK YOU!

**BACK-UP SLIDES**



# Motivation for studying P-violation in early-universe

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- **Standard** modelling (slow-roll): inflation is **P-invariant**

## THEORETICAL:

- P-violating early-universe processes **explain the baryonic asymmetry**  
(see e.g. Carroll 1998; Alexander et. al. 2004)

## OBSERVATIONAL:

- **Recent evidence for primordial P-violation** in LSS from BOSS galaxy survey  
( $3\sigma$  in Philcox 2022;  $7\sigma$  in Hou et. al. 2022)

# P-violation modelling

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- **Modified gravity models (higher derivatives):**

- Hořava–Lifshitz gravity, 3 deriv. (e.g. Wang 2017)
- Chern-Simons gravitational term coupled to a scalar field, 4 deriv. (e.g. Bartolo, **Orlando** 2017)
- Higher-order chiral scalar-tensor theories, > 4 deriv. (e.g. Bartolo, Caloni, **Orlando**, Ricciardone 2020)

$$\Delta\mathcal{L}_{\text{CS}}^{\text{gravit}} = f(\phi) \epsilon^{\mu\nu\rho\sigma} R_{\mu\nu}{}^{\kappa\lambda} R_{\rho\sigma\kappa\lambda}$$

- **Gauge field-axion Chern-Simons couplings** (e.g. Dimastrogiovanni, Fasiello, Fujita 2016)

$$\Delta\mathcal{L}_{\text{CS}}^{\text{gauge}} \propto \phi \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^a F_{\rho\sigma,a} \quad a \in \mathcal{G} = U(1), SU(2), \dots$$

- **Modified gravity + Gauge-field coupling** (e.g. Mirzaghali, Komatsu, Lozanov, Watanabe 2020)

- **Effective field theory, cosmological bootstrap:**

- Write all the operators that break P and are compatible with certain assumed symmetries (e.g. Bordin, Cabass 2020; Cabass, Pajer, Stefanyszyn, Supel 2021)

# SGWB V modes monopole

$$\Omega_{\text{GW}}^V(k, \hat{n}) = \overline{\Omega}_{\text{GW}}^V(k) + \delta_{\text{GW}}^V(k, \hat{n})$$

$$\overline{\Omega}_{\text{GW}}^V(k) \propto \langle \gamma_k^R \gamma_k^R \rangle - \langle \gamma_k^L \gamma_k^L \rangle$$

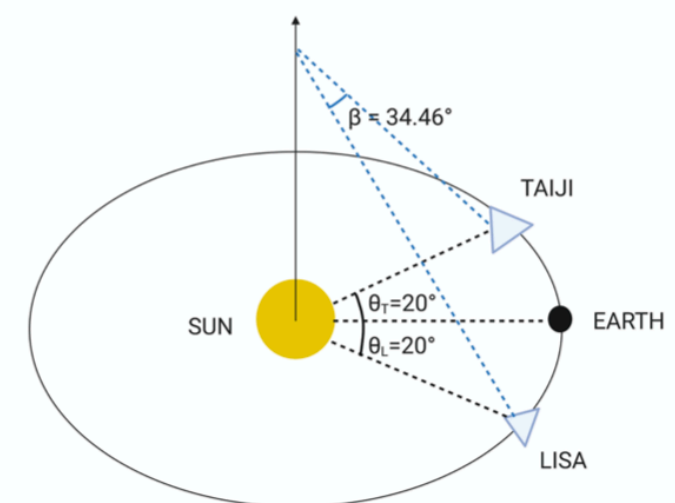
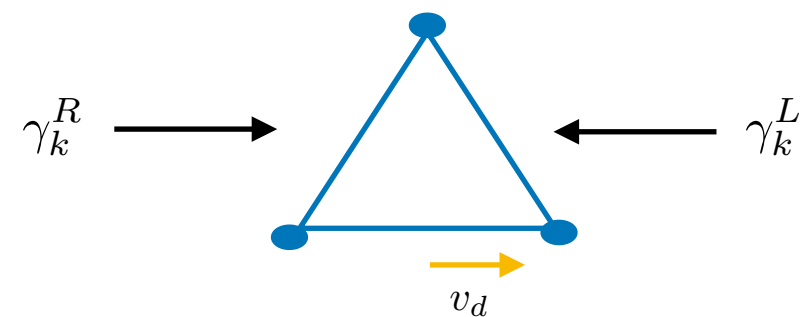
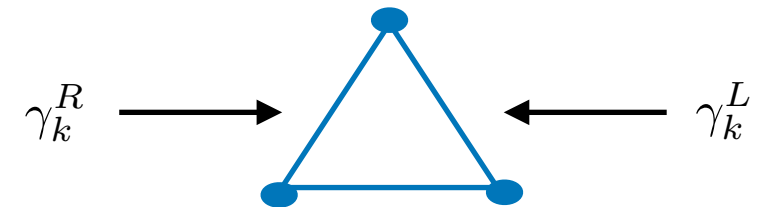
- Coplanar detectors insensitive to V-mode monopole

1. **Dipolar anisotropy** in the GW background **induced** by the detector-SGWB relative motion  
(Domcke et. al. 2019)

2. **Network of detectors:**

- network of ground-based interferometers  
(e.g. Seto, Taruya 2008; Smith, Caldwell 2016)
- network of space-based interferometers  
(e. g. **Orlando**, Pieroni, Ricciardone, 2020; Seto 2020)

$S/N$  : **space-net**  $\gg$  **dipolar**  $\gg$  **ground-net**



# Next steps

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- Role of **advanced state of BBO/DECIGO** missions and their network
- Role of **forthcoming experiments** (LISA, Taiji, ET, CE, PTA)
- Role of **cross-correlations**:

$$\langle V_{\text{GW}} - T_{\text{CMB}} \rangle, \langle V_{\text{GW}} - E_{\text{CMB}} \rangle, \langle V_{\text{GW}} - B_{\text{CMB}} \rangle, \langle V_{\text{GW}} - \mu_{\text{CMB}} \rangle, \dots$$

- Role of **different polarisation states**:  $Q_{\text{GW}}, U_{\text{GW}}$  modes