

Effective comparison of neutrino-mass models

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- 1 Motivation
- 2 The models, their EFTs and spurion analysis
- 3 Individual phenomenology
- 4 Effective comparison of models

Neutrinos have mass

- Neutrinos have mass: clearest evidence for new physics that couples to SM
- But it's extremely tiny, $m_\nu \lesssim 0.1$ eV
 - Suggestive of very large scale (useful for GUTS, leptogenesis), very small couplings (useful for DM), or fine-tuning
- Could well have new physics which gives **small m_ν but larger effects elsewhere** because
 - Tininess of lepton number violating couplings is technically natural
 - Models may involve multiple mass scales

How will we know the true model of neutrino mass?

1. Directly: discovery of a new state (cf. Oleg's and Xabi's talks later this week)
 2. Indirectly: discover a **pattern of deviations from the SM** which points to one specific mechanism
- Indirect approach is less obvious but arguably more promising:
 - Great recent and expected progress in low energy and EW-scale observables: $\mu N \rightarrow eN$, $\mu \rightarrow 3e$, $a_{e,\mu}$, d_e , B decays, m_W, \dots
 - Slower progress on energy frontier

New physics above the EW scale

Focusing exclusively on $\Lambda_{NP} \gg v$, there are two main approaches one can take:

1. An explicit model

- ✓ UV complete
- ✓ Is (somewhat) predictive
- ✗ Small part of theory space
- ✗ **Can we distinguish it?**

Gore Vidal: *'It is not enough to succeed. Others must fail.'*

2. Effective Field Theory

- ✓ (Reasonably) complete coverage of possibilities
- ✓ Computational ease
- ✗ Not UV complete
- ✗ **Many models match onto given Wilson Coefficient(s)**

Distinguishing new physics

- The problem: can't claim uniqueness
- A more useful approach: compare multiple observables (ideally with correlated predictions) in multiple models
- This has been done before, but not enough
Ababda+Biggio+Bordone+Gavela+Hambye '07, Babu+Dev+Janu+Thapa '19,...
- Our work aims to:
 - Show the usefulness of deriving EFTs of models
 - Further develop this approach

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The procedure

1. Pick a model
2. Integrate out heavy states at their mass scale, generate WCs

de Blas+Criado+Perez-Victoria+Santiago '17 (tree-level dim-6),...

3. Run WCs down to scales of observables

Jenkins+Manohar+Trott+Alonso+Stoffer '13, '17;...

4. Compare with established bounds on WCs from observables

Crivellin+Najjari+Rosiek '13, Falkowski+Riva '14, Berthier+Trott '15, Feruglio+Paradisi+Pattori '15,

Falkowski+Gonzalez-Alonso+Mimouni '17, Frigerio+Nardecchi+Serra+Vecchi '18, Calibbi+Marcano+Roy

'21, RC+Frigerio '21,...

Four different neutrino-mass models:

- Type-I seesaw (tree): $n \geq 2$ singlet fermions, $N \sim (1, 1)_0$
- Type-III seesaw (tree): $n \geq 2$ fermion triplets, $\Sigma \sim (1, 3)_0$
- Zee model (loop): two scalars, $H_2 \sim (1, 2)_{1/2}$ and $\delta \sim (1, 1)_1$
- Minimal LQ model (loop): two scalars, $S \sim (3, 1)_{-1/3}$ and $D \sim (3, 2)_{1/6}$ (in SUSY could call them \tilde{d}_R and \tilde{q}_L)
 - Only model with two LQs which induces both m_ν and charged lepton dipoles without y_e -suppression

Wilson Coefficients

| WCs | Seesaw I | Seesaw III | Zee | Leptoquarks |
|-----------------|--|--|--|---|
| c_{ab}^W | $\frac{1}{2}(\epsilon_N^T \mu_N \epsilon_N)_{ab}$ | $\frac{1}{2}(\epsilon_\Sigma^T \mu_\Sigma \epsilon_\Sigma)_{ab}$ | $-2\mu_Z(\epsilon_\delta y_e^\dagger \epsilon_2)_{ab} \mathbf{P}$ $-2\mu_Z(\epsilon_2^T y_e^* \epsilon_\delta)_{ab} \mathbf{P}$ | $3\mu_{DS}(\epsilon_L^T y_d^\dagger \epsilon_D)_{ab} \mathbf{P}$ $+3\mu_{DS}(\epsilon_D^T y_d^* \epsilon_L)_{ab} \mathbf{P}$ |
| c_{ab}^{eB} | $-\frac{g_1}{24}(\epsilon_N^\dagger \epsilon_N y_e^\dagger)_{ab} \mathbf{P}$ | $-\frac{g_1}{8}(\epsilon_\Sigma^\dagger \epsilon_\Sigma y_e^\dagger)_{ab} \mathbf{P}$ | $-\frac{g_1}{3}(\epsilon_\delta^\dagger \epsilon_\delta y_e^\dagger)_{ab} \mathbf{P}$ $+\frac{5g_1}{48}(\epsilon_2^\dagger \epsilon_2 y_e^\dagger)_{ab} \mathbf{P}$ $+\frac{g_1}{24}(y_e^\dagger \epsilon_2 \epsilon_2^\dagger)_{ab} \mathbf{P}$ | $-\frac{5g_1}{4}(\epsilon_L^\dagger y_u^T \epsilon_R)_{ab} \mathbf{L}$ |
| c_{ab}^{eW} | $-\frac{5g_2}{24}(\epsilon_N^\dagger \epsilon_N y_e^\dagger)_{ab} \mathbf{P}$ | $-\frac{3g_2}{8}(\epsilon_\Sigma^\dagger \epsilon_\Sigma y_e^\dagger)_{ab} \mathbf{P}$ | $-\frac{g_2}{6}(\epsilon_\delta^\dagger \epsilon_\delta y_e^\dagger)_{ab} \mathbf{P}$ $+\frac{g_2}{48}(\epsilon_2^\dagger \epsilon_2 y_e^\dagger)_{ab} \mathbf{P}$ | $\frac{3g_2}{4}(\epsilon_L^\dagger y_u^T \epsilon_R)_{ab} \mathbf{L}$ |
| $c_{ab}^{H(1)}$ | $\frac{1}{4}(\epsilon_N^\dagger \epsilon_N)_{ab}$ | $\frac{3}{4}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}$ | $\frac{2g_1^2}{3}(\epsilon_\delta^\dagger \epsilon_\delta)_{ab} \mathbf{L}$ $-\frac{g_1^2}{3}(\epsilon_2^\dagger \epsilon_2)_{ab} \mathbf{L}$ | $-\frac{g_1^2}{3}(\epsilon_D^\dagger \epsilon_D)_{ab} \mathbf{L}$ $-\frac{g_1^2}{6}(\epsilon_L^\dagger \epsilon_L)_{ab} \mathbf{L}$ $-\frac{3}{2}(\epsilon_L^\dagger y_u^T y_u^* \epsilon_L)_{ab} \mathbf{L}$ |
| $c_{ab}^{H(3)}$ | $-\frac{1}{4}(\epsilon_N^\dagger \epsilon_N)_{ab}$ | $\frac{1}{4}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}$ | $\frac{2g_2^2}{3}(\epsilon_\delta^\dagger \epsilon_\delta)_{ab} \mathbf{L}$ | $-\frac{1}{2}g_2^2(\epsilon_L^\dagger \epsilon_L)_{ab} \mathbf{L}$ $-\frac{3}{2}(\epsilon_L^\dagger y_u^T y_u^* \epsilon_L)_{ab} \mathbf{L}$ |
| c_{ab}^{He} | $\frac{1}{2}(y_e \epsilon_N^\dagger \epsilon_N y_e^\dagger)_{ab} \mathbf{L}$ $-\frac{g_1^2}{3}\text{tr}[\epsilon_N^\dagger \epsilon_N] \delta_{ab} \mathbf{L}$ | $\frac{3}{2}(y_e \epsilon_\Sigma^\dagger \epsilon_\Sigma y_e^\dagger)_{ab} \mathbf{L}$ $-g_1^2 \text{tr}[\epsilon_\Sigma^\dagger \epsilon_\Sigma] \delta_{ab} \mathbf{L}$ | $-\frac{g_1^2}{3}(\epsilon_2 \epsilon_2^\dagger)_{ab} \mathbf{L}$ | $3(\epsilon_R y_u^* y_u^T \epsilon_R)_{ab} \mathbf{L}$ $-\frac{g_1^2}{6}(\epsilon_R^\dagger \epsilon_R)_{ab} \mathbf{L}$ |
| c_{ab}^{eH} | $2\lambda(\epsilon_N^\dagger \epsilon_N y_e^\dagger)_{ab} \mathbf{L}$ $+\frac{g_2^2}{3}\text{tr}[\epsilon_N^\dagger \epsilon_N](y_e^\dagger)_{ab} \mathbf{L}$ $-6(c^{W\dagger} c^W y_e)_{ab} \mathbf{L}$ $+8\text{tr}[c^{W\dagger} c^W](y_e^\dagger)_{ab} \mathbf{L}$ | $(\epsilon_\Sigma^\dagger \epsilon_\Sigma y_e^\dagger)_{ab}$ | $\epsilon_\lambda^*(\epsilon_2^\dagger)_{ab}$ | $6(\epsilon_L^\dagger y_u^T y_u^* y_u^T \epsilon_R)_{ab} \mathbf{L}$ $-6\lambda(\epsilon_L^\dagger y_u^T \epsilon_R)_{ab} \mathbf{L}$ |

- Sample of WCs: light (dark) grey for 1-loop leading-log (finite)
- $L \equiv \log(M/v)/(16\pi^2)$, $P \equiv 1/(16\pi^2)$

A brief introduction to spurion analysis

- SM has a $U(3)_l \times U(3)_e \times U(3)_q \times U(3)_u \times U(3)_d$ symmetry, broken by Yukawas but restored if they are 'spurious' fields
- If $l_L \rightarrow V_l l_L$, $e_R \rightarrow V_e e_R$ and $y_e \rightarrow V_e y_e V_l^\dagger$, then

$$\mathcal{L} \supset -\bar{e}_R y_e H^\dagger l_L + h.c. \quad (1)$$

remains invariant under the flavour symmetry

- Treat all new couplings and mass terms this way, enforce that EFT Lagrangian,

$$\mathcal{L} = \sum_i (\sqrt{2}/v)^{d_i-4} c^i Q_i \quad (2)$$

is invariant under symmetry (which may be extended by NP)

- Know how each operator transforms under each symmetry \Rightarrow know how each WC should transform

Spurion analysis in the type-I and type-III seesaw

Initial spurion analysis is very illuminating

- First consider the seesaw mechanisms, with

$$\mathcal{L}_N = \bar{N}_R i \not{\partial} N_R - \left(\bar{N}_R Y_N \tilde{H}^\dagger L + \frac{1}{2} \bar{N}_R M_N N_R^c + h.c. \right), \quad (3)$$

for type-I and $N_R \rightarrow \Sigma_R^A$ for type-III

- Under $U(3)_I \times U(n)_N$ symmetry, have

$$Y_N \rightarrow V_N Y_N V_I^\dagger, \quad M_N \rightarrow V_N M_N V_N^T, \quad (4)$$

- Define dimensionless parameters

$$\epsilon_N \equiv \frac{v}{\sqrt{2}} M_N^{-1} Y_N, \quad \mu_N \equiv \frac{\sqrt{2}}{v} M_N, \quad (5)$$

Spurion analysis in the type-I and type-III seesaw

- All SMEFT operators Q_i are invariant under $U(n)_N$
- The only $U(n)_N$ -invariant combinations at lowest orders in the EFT are

$$\mathcal{O}(M^{-1}) : (\epsilon_N^T \mu_N \epsilon_N)_{\alpha\beta}, \quad \mathcal{O}(M^{-2}) : (\epsilon_N^\dagger \epsilon_N)_{\alpha\beta}, \quad [\mathcal{O}(M^{-1})]^2$$

- So $m_\nu \propto \epsilon_N^T \mu_N \epsilon_N$ and all dim-6 WCs are $c \propto (\epsilon_N^\dagger \epsilon_N)$ or $c \propto m_\nu^2$
- Then setting $m_\nu \propto \epsilon_N^T \mu_N \epsilon_N \rightarrow 0$ implies (for $n = 2, 3$)

$$(\epsilon_N^\dagger \epsilon_N)_{\alpha\beta} \propto \lambda_\alpha \lambda_\beta, \quad (6)$$

$\lambda_\alpha \in \mathbb{R}$, $\alpha = e, \mu, \tau$, i.e. all dim-6 pheno fixed by three parameters

Spurion analysis in the type-I and type-III seesaw

- One-loop dipole WCs are $c_{\alpha\beta}^{eB,eW} \propto (\epsilon_N^\dagger \epsilon_N y_e^\dagger)_{\alpha\beta}$, so $c_{\alpha\alpha}^{eB,eW} \in \mathbb{R} \Rightarrow$ EDM $d_e = 0$ at leading order
- From spurion analysis, find largest imaginary part arises at two-loops,

$$\begin{aligned} |d_e| &\sim \frac{4em_e}{(16\pi^2)^2 v^2} \text{Im}\{[\epsilon_N^\dagger \epsilon_N y_e^\dagger y_e \epsilon_N^\dagger \epsilon_N, \epsilon_N^\dagger \epsilon_N]_{ee}\} \\ &= \frac{em_e(m_\tau^2 - m_\mu^2)}{16\pi^4 v^4} \text{Im}\{(\epsilon_N^\dagger \epsilon_N)_{e\tau} (\epsilon_N^\dagger \epsilon_N)_{\tau\mu} (\epsilon_N^\dagger \epsilon_N)_{\mu e}\} \\ &\lesssim 10^{-37} \text{ e cm} \end{aligned} \tag{7}$$

Spurion analysis in the Zee model

- The Zee Lagrangian is

$$\begin{aligned} \mathcal{L}_{\text{Zee}} = & |D_\mu \delta|^2 + |D_\mu H_2|^2 - M_\delta^2 \delta^\dagger \delta - M_2^2 H_2^\dagger H_2 - M_{\delta 2} \tilde{H}^\dagger H_2 \delta^\dagger \\ & - \lambda_2 (H^\dagger H)(H^\dagger H_2) - \bar{L}_L^c Y_\delta i \sigma_2 l_L \delta - \bar{e}_R Y_2 H_2^\dagger e_R + h.c. + \dots \quad (8) \end{aligned}$$

- Here we have a $U(3)_l \times U(3)_e \times U(1)_\delta \times U(1)_{H_2}$ symmetry, with dimensionless parameters

$$\begin{aligned} \mu_Z &\equiv \frac{\sqrt{2} M_{\delta 2}}{v} \rightarrow \mu_Z e^{i(\phi_\delta - \phi_2)}, & \epsilon_\lambda &\equiv \frac{v \lambda_2}{\sqrt{2} M_2} \rightarrow \epsilon_\lambda e^{-i\phi_2}, \\ \epsilon_\delta &\equiv \frac{v Y_\delta}{\sqrt{2} M_\delta} \rightarrow V_l^* \epsilon_\delta V_l^\dagger e^{-i\phi_\delta}, & \epsilon_2 &\equiv \frac{v Y_2}{\sqrt{2} M_2} \rightarrow V_e \epsilon_2 V_l^\dagger e^{i\phi_2} \end{aligned}$$

Spurion analysis in the Zee model

- Again, we can classify $U(1)_\delta \times U(1)_{H_2}$ -invariant combinations at lowest order

$$\mathcal{O}(M^{-1}) : \mu_Z (\epsilon_\delta)_{\alpha\beta} (\epsilon_2)_{\gamma\delta} , \mu_Z \epsilon_\lambda^* (\epsilon_\delta)_{\alpha\beta} ,$$

$$\mathcal{O}(M^{-2}) : (\epsilon_\delta^*)_{\alpha\beta} (\epsilon_\delta)_{\gamma\delta} , (\epsilon_2^*)_{\alpha\beta} (\epsilon_2)_{\gamma\delta} , \epsilon_\lambda^* \epsilon_\lambda , (\epsilon_2)_{\alpha\beta} \epsilon_\lambda , [\mathcal{O}(M^{-1})]^2$$

- Neutrino mass $m_\nu \propto \mu_Z (\epsilon_\delta y_e^\dagger \epsilon_2)_{\alpha\beta} + ()^T$ since ϵ_δ anti-symmetric
- Small m_ν achieved by $\mu_Z \rightarrow 0$, $\epsilon_\delta \rightarrow 0$, $\epsilon_2 \rightarrow 0$ (all limits conserve lepton number), or by fine-tuning if all non-zero
- See that a) dim-6 WCs can be large while m_ν small, and b) pheno of δ and H_2 are separate: no $\epsilon_\delta \epsilon_2$ terms at dim-6

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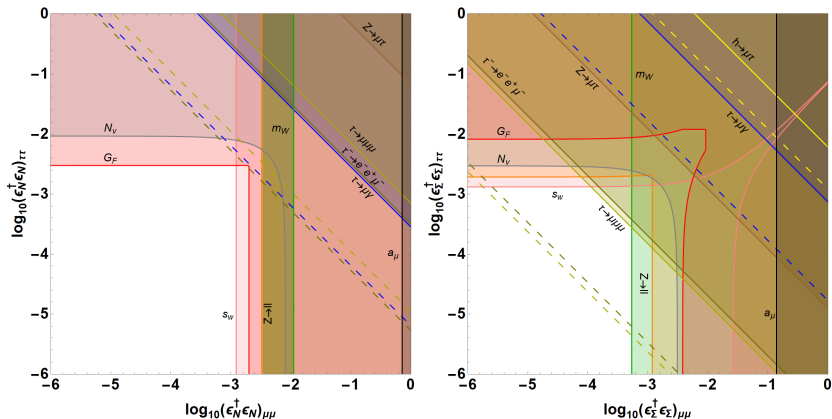
Placed bounds on WCs from various observables (these plus others)

| Observable | Bound | C.L. |
|-------------------------------|---|-------------|
| m_W | $0.23c^G - 0.77c^{HD} \in [-0.6, 13] \times 10^{-4}$ | anom |
| s_w^2 | $c^{HD} - c^G - 1.40c^{HI(1+3)} - 1.62c^{He} \in [-6.1, 9.1] \times 10^{-4}$ | 2σ |
| $G_F^{\mu\tau} / G_F^{e\tau}$ | $c_{\tau ee\tau}^{II} + c_{e\tau\tau e}^{II} - c_{\tau\mu\mu\tau}^{II} - c_{\mu\tau\tau\mu}^{II} + 2c_{\mu\mu\mu}^{HI(3)} - 2c_{ee}^{HI(3)} \in [-1.0, 4.6] \times 10^{-3}$ | 2σ |
| $G_F^{e\tau} / G_F$ | $c_{e\mu\mu e}^{II} + c_{\mu ee\mu}^{II} - c_{e\tau\tau e}^{II} - c_{\tau ee\tau}^{II} + 2c_{\tau\tau\tau}^{HI(3)} - 2c_{\mu\mu\mu}^{HI(3)} \in [-1.9, 4.1] \times 10^{-3}$ | 2σ |
| $G_F^{\mu\tau} / G_F$ | $c_{\mu ee\mu}^{II} + c_{e\mu\mu e}^{II} - c_{\mu\tau\tau\mu}^{II} - c_{\tau\mu\mu\tau}^{II} + 2c_{\tau\tau\tau}^{HI(3)} - 2c_{ee}^{HI(3)} \in [-1.5, 6.0] \times 10^{-3}$ | anom |
| $Z \rightarrow e\mu$ | $\sqrt{ c_{e\mu}^{HI(1)} + c_{e\mu}^{HI(3)} ^2 + c_{e\mu}^{He} ^2 + \frac{1}{2} s_w c_{e\mu}^{eB} + c_w c_{e\mu}^{eW} ^2 + \frac{1}{2} s_w c_{e\mu}^{eB} + c_w c_{e\mu}^{eW} ^2} \lesssim 1.2 \times 10^{-3}$ | 95% |
| $Z \rightarrow e\tau$ | $\sqrt{ c_{e\tau}^{HI(1)} + c_{e\tau}^{HI(3)} ^2 + c_{e\tau}^{He} ^2 + \frac{1}{2} s_w c_{e\tau}^{eB} + c_w c_{e\tau}^{eW} ^2 + \frac{1}{2} s_w c_{e\tau}^{eB} + c_w c_{e\tau}^{eW} ^2} \lesssim 3.1 \times 10^{-3}$ | 95% |
| $Z \rightarrow \mu\tau$ | $\sqrt{ c_{\mu\tau}^{HI(1)} + c_{\mu\tau}^{HI(3)} ^2 + c_{\mu\tau}^{He} ^2 + \frac{1}{2} s_w c_{\mu\tau}^{eB} + c_w c_{\mu\tau}^{eW} ^2 + \frac{1}{2} s_w c_{\mu\tau}^{eB} + c_w c_{\mu\tau}^{eW} ^2} \lesssim 3.5 \times 10^{-3}$ | 95% |
| $Z \rightarrow e^+e^-$ | $1.19(c^G - c^{HD}) + 4.27(c_{ee}^{HI(1)} + c_{ee}^{HI(3)}) - 3.68c_{ee}^{He} \in [-4.2, 2.0] \times 10^{-3}$ | 2σ |
| $Z \rightarrow \mu^+\mu^-$ | $1.19(c^G - c^{HD}) + 4.27(c_{\mu\mu}^{HI(1)} + c_{\mu\mu}^{HI(3)}) - 3.68c_{\mu\mu}^{He} \in [-4.7, 4.3] \times 10^{-3}$ | 2σ |
| $Z \rightarrow \tau^+\tau^-$ | $1.19(c^G - c^{HD}) + 4.27(c_{\tau\tau}^{HI(1)} + c_{\tau\tau}^{HI(3)}) - 3.68c_{\tau\tau}^{He} \in [-2.2, 8.2] \times 10^{-3}$ | 2σ |
| N_ν | $0.58(c^{HD} - c^G) + 11.1c^{He} - 24.8c^{HI(1)} - 0.82c^{HI(3)} \in [-0.019, 0.011]$ | 2σ |
| a_e | $ \text{Re } c_{ee}^{e\gamma, obs} \lesssim 3 \times 10^{-8}$ | anom |
| a_μ | $\text{Re}[c_{\mu\mu}^{e\gamma, obs} + 4.3 \times 10^{-7}(c^G - c^{HD})] \in [-0.5, 4.6] \times 10^{-7}$ | anom |

Bounds derived using LEP, ATLAS, CMS, CDF II, Muon G-2, PDG, Hanneke+ '08, Pich '13, Parker+ '18, Morel+ '20, Aoyama+ '20, de Blas+ '22

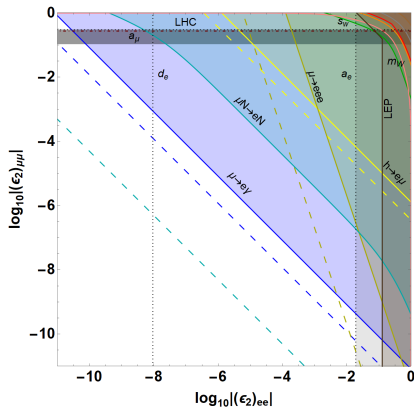
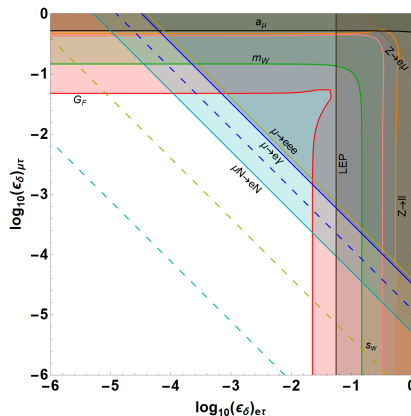
- Having done this once, only have to change it when there's improved experimental data
- Don't include all WCs, but all those obtained at tree or one-loop leading-log in any of the four models
- How to deal with $\geq 2\sigma$ anomalies when imposing 2σ limits?
For a $n\sigma$ anomaly, we allowed a shift of $[n]\sigma$, so as not to rule out NP which negligibly modifies the observable
→ For 4.2σ in a_μ , allowed $a_\mu^{\text{exp}} - 5\sigma \leq a_\mu^{\text{SM}} + \Delta a_\mu \leq a_\mu^{\text{exp}} + 2\sigma$
- Now applied these to each model: looked at two flavours at a time and set couplings to the third to zero

Type-I and type-III seesaw, $\mu - \tau$ sector



- Recall $\epsilon_{N,\Sigma} = (v/\sqrt{2})Y_{N,\Sigma}/M_{N,\Sigma}$, took $M = 10$ TeV for logs
- Have correlated predictions for $n \leq 3$. Flavour conservation (violation) strongest in type-I (type-III) since CLFV induced at loop (tree)
- Type-I gives $\Delta m_W > 0$ but too small, type-III gives $\Delta m_W < 0$

Zee model, $e - \mu$ sector



- ϵ_δ fully determined, for ϵ_2 took $|(\epsilon_2)_{\alpha\beta}| = \sqrt{|(\epsilon_2)_{\alpha\alpha}(\epsilon_2)_{\beta\beta}|}$
- δ interferes with muon decay (thus G_F, m_W, \dots), H_2 does not
- Large $\mu \rightarrow e\gamma$ induced by H_2 from 2-loop Barr-Zee
- Can explain $(g - 2)_\mu$ for $|(\epsilon_2)_{ee}| \lesssim 10^{-10}$

LQ model Lagrangian is

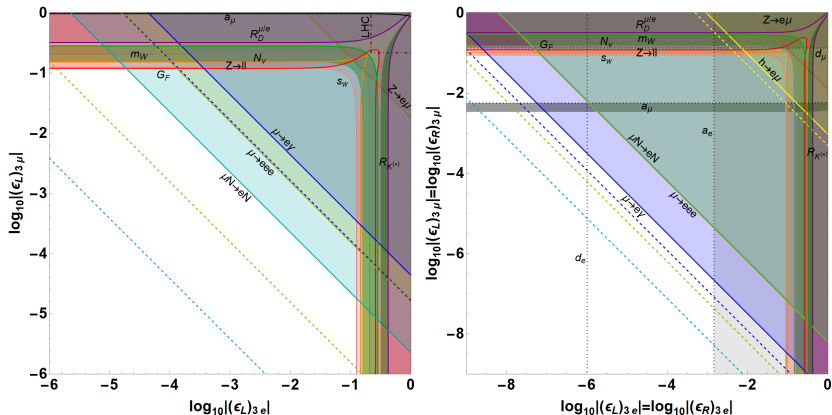
$$\mathcal{L}_{LQ} = |D_\mu S|^2 + |D_\mu D|^2 - V(D, S) \quad (9)$$

$$- (\overline{q_L^c} Y_L i \sigma_2 l_L S^\dagger + \overline{u_R^c} Y_R e_R S^\dagger + \overline{d_R} Y_D D^T i \sigma_2 l_L + h.c.)$$

- Assume LQ couples to only 3rd family quarks in m_d basis:
 - Avoid bounds from pions, kaons etc., focus on lepton sector
 - Captures relevant loops $\propto y_t$
- Y_L is most interesting coupling since
 - It generates interference with muon decay
 - Couples to light quarks via CKM, so induces e.g. $b \rightarrow cl\nu$
 - Combination of Y_L and Y_R gives top-enhanced loops,

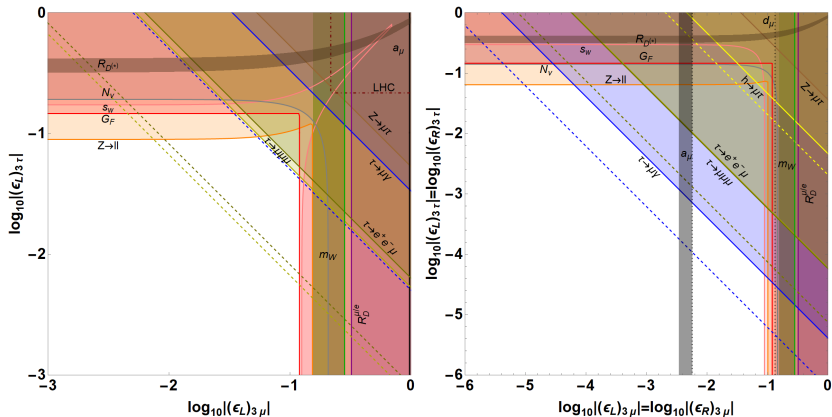
$$\sim N_c y_t^2 \gg g_{1,2}^2$$

LQ model, $e - \mu$ sector



- Correlated observables, $\mu \rightarrow e$ strongest by far, others weak but complementary
- Solutions to m_W and $R_{K^{(*)}}$ anomalies ruled out, but can explain $(g-2)_\mu$ for $|(\epsilon_{L,R})_{ee}| \lesssim 10^{-7}$
- Changing ϵ_R relative to ϵ_L modifies observables depending on dipole

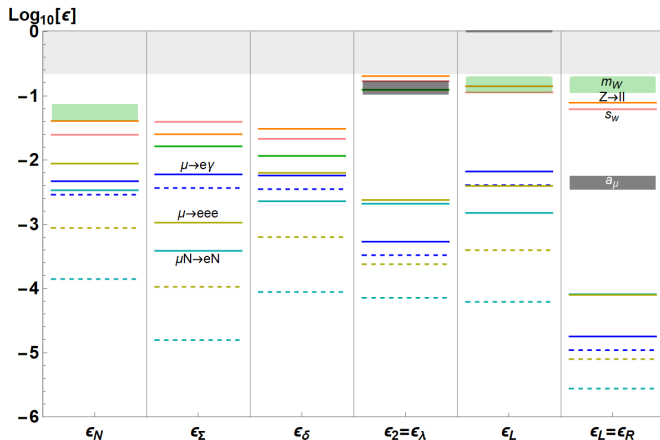
LQ model, $\mu - \tau$ sector



- With only ϵ_L , LFC and LFV bounds similar, y_t -enhancement for $\epsilon_L = \epsilon_R$ makes LFV much stronger
- Solution to $R_{D^{(*)}}$ also ruled-out, $(g-2)_\mu$ explanation persists, even d_μ relevant

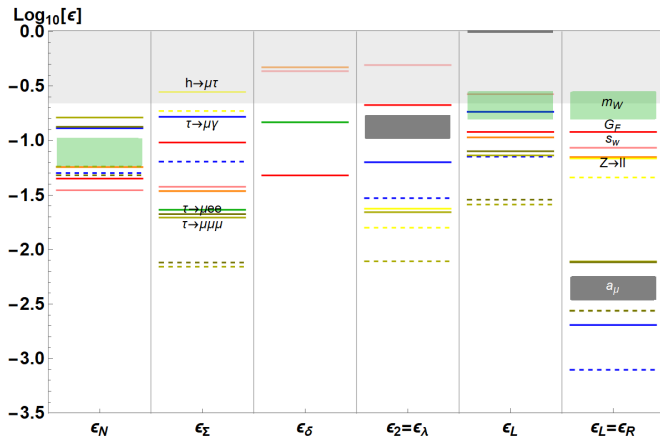
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Comparison: all $\epsilon_{\alpha\beta}$ equal



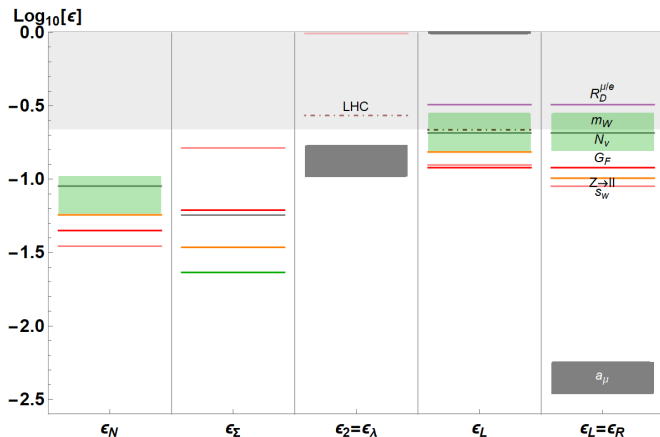
- $\mu \rightarrow e$ always wins: strongest in LQ since no y_μ
- Future $\mu \rightarrow e$ bounds has clear order
- Flavour-conserving bounds more discriminatory

Comparison: no NP coupling to electrons



- $(\epsilon_\delta)_{\mu\tau}$ only \Rightarrow no flavour violation at dim-6
- Bounds from $\tau \rightarrow \mu$ competitive with flavour-conserving ones
- Strong potential to distinguish between models

Comparison: NP couples only to muons



- No ϵ_δ column since $(\epsilon_\delta)_{\mu\mu} = 0$ by antisymmetry
- Can explain $(g - 2)_\mu$ anomalies in Zee and LQ models
- Mainly expect shift in s_W , G_F before m_W , but not in type-III

Conclusions

1. Precision low-energy and EW-scale observables are excellent places to look for evidence of the neutrino mass mechanism
2. EFT is a useful framework: spurion analysis and power-counting is powerful, systematic pheno analysis
 - Strength of bounds obtained reinforces that EFT approach is valid
3. Looking at correlations **within and between models** could be key to discovering mass mechanism if no direct discoveries

Back-up slides

SMEFT operators

| Name | Operator |
|-------------------|--|
| $Q_{W,ab}$ | $(\overline{l_{La}^c} \tilde{H}^*) (\tilde{H}^\dagger l_{Lb})$ |
| $Q_{eB,ab}$ | $(\overline{l_{La}} \sigma_{\mu\nu} e_{Rb}) H B^{\mu\nu}$ |
| $Q_{eW,ab}$ | $(\overline{l_{La}} \sigma_{\mu\nu} e_{Rb}) \sigma^A H W^{A\mu\nu}$ |
| $Q_{Hl,ab}^{(1)}$ | $(\overline{l_{La}} \gamma_\mu l_{Lb}) (H^\dagger i \overleftrightarrow{D}^\mu H)$ |
| $Q_{Hl,ab}^{(3)}$ | $(\overline{l_{La}} \gamma_\mu \sigma^A l_{Lb}) (H^\dagger i \overleftrightarrow{D}^\mu \sigma^A H)$ |
| $Q_{He,ab}$ | $(\overline{e_{Ra}} \gamma_\mu e_{Rb}) (H^\dagger i \overleftrightarrow{D}^\mu H)$ |
| $Q_{eH,ab}$ | $(\overline{l_{La}} H e_{Rb}) (H^\dagger H)$ |
| Q_H | $(H^\dagger H)^3$ |
| Q_{HD} | $(H^\dagger D_\mu H)^* (H^\dagger D^\mu H)$ |
| $Q_{H\Box}$ | $(H^\dagger H) \Box (H^\dagger H)$ |

| Name | Operator |
|-----------------------|--|
| $Q_{ll,ab}$ | $(\overline{l_{La}} \gamma_\mu l_{Lb}) (\overline{l_{Lc}} \gamma^\mu l_{Ld})$ |
| $Q_{le,ab}$ | $(\overline{l_{La}} \gamma_\mu l_{Lb}) (\overline{e_{Rc}} \gamma^\mu e_{Rd})$ |
| $Q_{ee,ab}$ | $(\overline{e_{Ra}} \gamma_\mu e_{Rb}) (\overline{e_{Rc}} \gamma^\mu e_{Rd})$ |
| $Q_{lq,abcd}^{(1)}$ | $(\overline{l_{La}} \gamma_\mu l_{Lb}) (\overline{q_{Lc}} \gamma^\mu q_{Ld})$ |
| $Q_{lq,abcd}^{(3)}$ | $(\overline{l_{La}} \gamma_\mu \sigma^A l_{Lb}) (\overline{q_{Lc}} \gamma^\mu \sigma^A q_{Ld})$ |
| $Q_{qe,abcd}$ | $(\overline{q_{La}} \gamma_\mu q_{Lb}) (\overline{e_{Rc}} \gamma^\mu e_{Rd})$ |
| $Q_{lu,abcd}$ | $(\overline{l_{La}} \gamma_\mu l_{Lb}) (\overline{u_{Rc}} \gamma^\mu u_{Rd})$ |
| $Q_{ld,abcd}$ | $(\overline{l_{La}} \gamma_\mu l_{Lb}) (\overline{d_{Rc}} \gamma^\mu d_{Rd})$ |
| $Q_{eu,abcd}$ | $(\overline{e_{Ra}} \gamma_\mu e_{Rb}) (\overline{u_{Rc}} \gamma^\mu u_{Rd})$ |
| $Q_{ed,abcd}$ | $(\overline{e_{Ra}} \gamma_\mu e_{Rb}) (\overline{d_{Rc}} \gamma^\mu d_{Rd})$ |
| $Q_{lequ,abcd}^{(1)}$ | $(\overline{l_{La}} e_{Rb}) \epsilon (\overline{q_{Lc}} u_{Rd})$ |
| $Q_{lequ,abcd}^{(3)}$ | $(\overline{l_{La}} \sigma_{\mu\nu} e_{Rb}) \epsilon (\overline{q_{Lc}} \sigma^{\mu\nu} u_{Rd})$ |
| $Q_{ledq,abcd}$ | $(\overline{l_{La}} e_{Rb}) (\overline{d_{Rc}} q_{Ld})$ |

Wilson Coefficients 2

| WCs | Seesaw I | Seesaw III | Zee | Leptoquarks |
|------------------------|---|---|--|--|
| c^H | $\frac{4}{3} \lambda g_2^2 \text{tr}[\epsilon_N^\dagger \epsilon_N] L$ $-32 \lambda \text{tr}[c^{W\dagger} c^W] L$ | $-\frac{4}{3} \lambda g_2^2 \text{tr}[\epsilon_\Sigma^\dagger \epsilon_\Sigma] L$ $-32 \lambda \text{tr}[c^{W\dagger} c^W] L$ | $\epsilon_\lambda^* \epsilon_\lambda$ | — |
| $c^{H\Box}$ | $\frac{g_1^2 + 3g_2^2}{6} \text{tr}[\epsilon_N^\dagger \epsilon_N] L$ $+2 \text{tr}[c^{W\dagger} c^W] L$ | $\frac{g_1^2 - g_2^2}{2} \text{tr}[\epsilon_N^\dagger \epsilon_N] L$ $+2 \text{tr}[c^{W\dagger} c^W] L$ | — | — |
| c^{HD} | $\frac{2g_2^2}{3} \text{tr}[\epsilon_N^\dagger \epsilon_N] L$ $+16 \text{tr}[c^{W\dagger} c^W] L$ | $2g_2^2 \text{tr}[\epsilon_N^\dagger \epsilon_N] L$ $+16 \text{tr}[c^{W\dagger} c^W] L$ | — | — |
| c_{abcd}^{\parallel} | $\frac{g_1^2 - g_2^2}{24} (\epsilon_N^\dagger \epsilon_N)_{ab} \delta_{cd} L$ $+ \frac{g_1^2 - g_2^2}{24} \delta_{ab} (\epsilon_N^\dagger \epsilon_N)_{cd} L$ $+ \frac{g_2^2}{12} (\epsilon_N^\dagger \epsilon_N)_{ad} \delta_{cb} L$ $+ \frac{g_2^2}{12} \delta_{ad} (\epsilon_N^\dagger \epsilon_N)_{cb} L$ $+ 2(c^{W\dagger})_{ac} (c^W)_{bd} L$ | $\frac{3g_1^2 + g_2^2}{24} (\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab} \delta_{cd} L$ $+ \frac{3g_1^2 + g_2^2}{24} \delta_{ab} (\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{cd} L$ $- \frac{g_2^2}{12} (\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ad} \delta_{cb} L$ $- \frac{g_2^2}{12} \delta_{ad} (\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{cb} L$ $+ 2(c^{W\dagger})_{ac} (c^W)_{bd} L$ | $(\epsilon_\delta^\dagger)_{ac} (\epsilon_\delta)_{db}$ | $\frac{g_1^2}{6} (\epsilon_D^\dagger \epsilon_D)_{ab} \delta_{cd} L$ $+ \frac{g_1^2}{6} \delta_{ab} (\epsilon_D^\dagger \epsilon_D)_{cd} L$ $+ \frac{g_2^2}{2} (\epsilon_L^\dagger \epsilon_L)_{ad} \delta_{bc} L$ $+ \frac{g_2^2}{2} \delta_{ad} (\epsilon_L^\dagger \epsilon_L)_{cb} L$ $+ \frac{g_1^2 - 3g_2^2}{12} (\epsilon_L^\dagger \epsilon_L)_{ab} \delta_{cd} L$ $+ \frac{g_1^2 - 3g_2^2}{12} \delta_{ab} (\epsilon_L^\dagger \epsilon_L)_{cd} L$ |
| c_{abcd}^{le} | $\frac{g_1^2}{6} (\epsilon_N^\dagger \epsilon_N)_{ab} \delta_{cd} L$ | $\frac{g_1^2}{2} (\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab} \delta_{cd} L$ | $-\frac{1}{2} (\epsilon_2^\dagger)_{ad} (\epsilon_2)_{cb}$ | $\frac{3}{2} (\epsilon_L^\dagger y_u^T \epsilon_R)_{ad} (y_e)_{cb} L$ $+ \frac{3}{2} (y_e^\dagger)_{ad} (\epsilon_R^\dagger y_u^* \epsilon_L)_{cb} L$ $+ \frac{g_1^2}{3} (\epsilon_L^\dagger \epsilon_L)_{ab} \delta_{cd} L$ $+ \frac{2g_1^2}{3} (\epsilon_D^\dagger \epsilon_D)_{ab} \delta_{cd} L$ $+ \frac{2g_1^2}{3} \delta_{ab} (\epsilon_R^\dagger \epsilon_R)_{cd} L$ |
| c_{abcd}^{ee} | — | — | $\frac{g_1^2}{3} (\epsilon_2 \epsilon_2^\dagger)_{ab} \delta_{cd} L$ $+ \frac{g_2^2}{3} \delta_{ab} (\epsilon_2 \epsilon_2^\dagger)_{cd} L$ | $\frac{2g_1^2}{3} (\epsilon_R^\dagger \epsilon_R)_{ab} \delta_{cd} L$ $+ \frac{2g_1^2}{3} \delta_{ab} (\epsilon_R^\dagger \epsilon_R)_{cd} L$ |

Wilson Coefficients 3

| WCs | Seesaw I | Seesaw III | Zee | Leptoquarks |
|--------------------|--|--|--|--|
| $c_{abcd}^{lq(1)}$ | $-\frac{1}{4}(\epsilon_N^\dagger \epsilon_N)_{ab}(y_u^\dagger y_u)_{cd}L$ $-\frac{g_1^2}{36}(\epsilon_N^\dagger \epsilon_N)_{ab}\delta_{cd}L$ | $-\frac{3}{4}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}(y_u^\dagger y_u)_{cd}L$ $-\frac{g_1^2}{12}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}\delta_{cd}L$ | $\frac{2g_1^2}{9}(\epsilon_\delta^\dagger \epsilon_\delta)_{ab}\delta_{cd}L$ $-\frac{g_1^2}{9}(\epsilon_2^\dagger \epsilon_2)_{ab}\delta_{cd}L$ | $\frac{1}{4}(\epsilon_L^\dagger)_{ac}(\epsilon_L)_{db}$ |
| $c_{abcd}^{lq(3)}$ | $-\frac{1}{4}(\epsilon_N^\dagger \epsilon_N)_{ab}(y_u^\dagger y_u)_{cd}L$ $+\frac{g_1^2}{12}(\epsilon_N^\dagger \epsilon_N)_{ab}\delta_{cd}L$ | $\frac{1}{4}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}(y_u^\dagger y_u)_{cd}L$ $-\frac{g_1^2}{12}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}\delta_{cd}L$ | $\frac{2g_1^2}{3}(\epsilon_\delta^\dagger \epsilon_\delta)_{ab}\delta_{cd}L$ | $-\frac{1}{4}(\epsilon_L^\dagger)_{ac}(\epsilon_L)_{db}$ |
| c_{abcd}^{qe} | — | — | $-\frac{g_1^2}{9}\delta_{ab}(\epsilon_2 \epsilon_2^\dagger)_{cd}L$ | $\frac{1}{2}(\epsilon_L^* y_e^T)_{ac}(y_u^T \epsilon_R)_{bd}L$ $+\frac{1}{2}(y_u^\dagger \epsilon_R^*)_{ac}(\epsilon_L y_e^\dagger)_{bd}L$ $+\frac{1}{2}(y_u^\dagger \epsilon_R^*)_{ac}(y_u^T \epsilon_R)_{wd}L$ $-\frac{g_1^2}{3}(\epsilon_L^* \epsilon_L^T)_{ab}\delta_{cd}L$ $-\frac{2g_1^2}{9}\delta_{ab}(\epsilon_R^\dagger \epsilon_R)_{cd}L$ |
| c_{abcd}^{lu} | $\frac{1}{2}(\epsilon_N^\dagger \epsilon_N)_{ab}(y_u y_u^\dagger)_{cd}L$ $-\frac{g_1^2}{9}(\epsilon_N^\dagger \epsilon_N)_{ab}\delta_{cd}L$ | $\frac{3}{2}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}(y_u y_u^\dagger)_{cd}L$ $-\frac{g_1^2}{3}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}\delta_{cd}L$ | $\frac{8g_1^2}{9}(\epsilon_\delta^\dagger \epsilon_\delta)_{ab}\delta_{cd}L$ $-\frac{4g_1^2}{9}(\epsilon_2^\dagger \epsilon_2)_{ab}\delta_{cd}L$ | $\frac{1}{2}(\epsilon_L^\dagger y_u^T)_{ac}(\epsilon_R y_e)_{db}L$ $+\frac{1}{2}(\epsilon_L^\dagger y_u^T)_{ac}(y_u^* \epsilon_L)_{db}L$ $+\frac{1}{2}(y_e^\dagger \epsilon_R^*)_{ac}(y_u^* \epsilon_L)_{db}L$ $-\frac{2g_1^2}{9}(\epsilon_L^\dagger \epsilon_L)_{ab}\delta_{cd}L$ $-\frac{4g_1^2}{9}(\epsilon_D^\dagger \epsilon_D)_{ab}\delta_{cd}L$ $-\frac{g_1^2}{3}\delta_{ab}(\epsilon_R^* \epsilon_R^T)_{cd}L$ |
| c_{abcd}^{ld} | $\frac{g_1^2}{18}(\epsilon_N^\dagger \epsilon_N)_{ab}\delta_{cd}L$ | $\frac{g_1^2}{6}(\epsilon_\Sigma^\dagger \epsilon_\Sigma)_{ab}\delta_{cd}L$ | $-\frac{4g_1^2}{9}(\epsilon_\delta^\dagger \epsilon_\delta)_{ab}\delta_{cd}L$ $+\frac{2g_1^2}{9}(\epsilon_2^\dagger \epsilon_2)_{ab}\delta_{cd}L$ | $-\frac{1}{2}(\epsilon_D^\dagger)_{ad}(\epsilon_D)_{cb}$ |

Wilson Coefficients 4

| WCs | Seesaw I | Seesaw III | Zee | Leptoquarks |
|----------------------|----------|------------|---|---|
| C_{abcd}^{eu} | — | — | $-\frac{4g_1^2}{9}(\epsilon_2\epsilon_2^\dagger)_{ab}\delta_{cd}L$ | $\frac{1}{2}(\epsilon_R^\dagger)_{ac}(\epsilon_R)_{db}$ |
| C_{abcd}^{ed} | — | — | $\frac{2g_1^2}{9}(\epsilon_2\epsilon_2^\dagger)_{ab}\delta_{cd}L$ | $\frac{2g_1^2}{3}\delta_{ab}(\epsilon_D\epsilon_D^\dagger)_{cd}L$ $+\frac{4g_1^2}{9}(\epsilon_R^\dagger\epsilon_R)_{ab}\delta_{cd}L$ |
| $C_{abcd}^{lequ(1)}$ | — | — | $2\text{tr}[y_e^\dagger\epsilon_2](\epsilon_2^\dagger)_{ab}(y_u^\dagger)_{cd}L$ | $-\frac{1}{2}(\epsilon_L^\dagger)_{ac}(\epsilon_R)_{db}$ |
| $C_{abcd}^{lequ(3)}$ | — | — | — | $\frac{1}{8}(\epsilon_L^\dagger)_{ac}(\epsilon_R)_{db}$ |
| C_{abcd}^{ledq} | — | — | $2\text{tr}[y_e^\dagger\epsilon_2](\epsilon_2^\dagger)_{ab}(y_d)_{cd}L$ | $-3(\epsilon_L^\dagger y_u^T \epsilon_R)_{ab}(y_d)_{cd}L$ $-(\epsilon_D^\dagger y_d)_{ad}(\epsilon_D y_e^\dagger)_{cb}L$ $+(\epsilon_L^\dagger y_d^T)_{ac}(\epsilon_L y_e^\dagger)_{db}L$ $+(\epsilon_L^\dagger y_d^T)_{ac}(y_u^T \epsilon_R)_{db}L$ |

One example: c^G

- Important effect is NP interference with muon decay, since this affects measured G_F which is used as an EW input parameter

Fernandez-Martinez+Hernandez-Garcia+Lopez-Pavon '16, Jenkins+Manohar+Stoffer '17,...

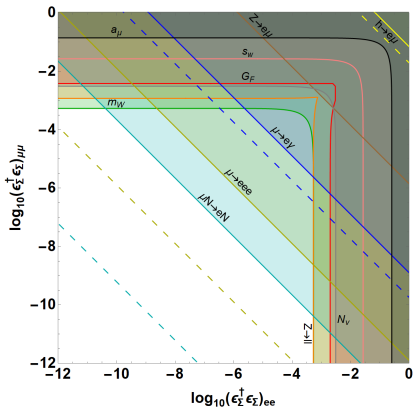
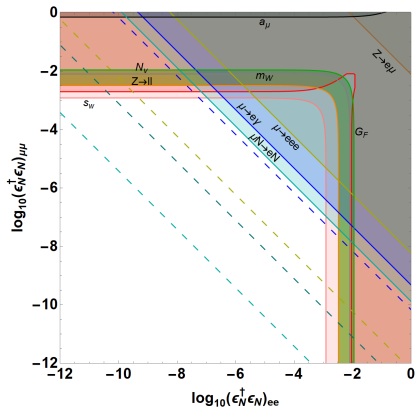
- In EFT at leading-order, the Fermi constant is

$$G_F \simeq \frac{1}{\sqrt{2}V^2}(1 - c^G), \quad c^G \equiv c_{e\mu\mu e}^{ll} + c_{\mu ee\mu}^{ll} - 2c_{ee}^{HI(3)} - 2c_{\mu\mu}^{HI(3)} \quad (10)$$

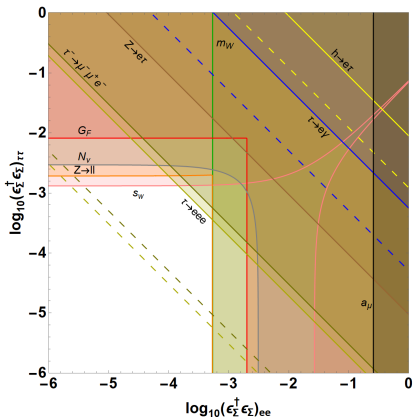
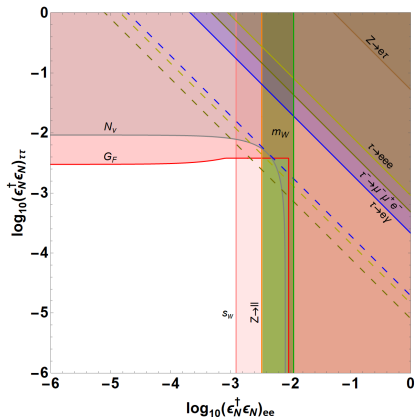
- This (and other effects) enters into EW observables:

$$m_W^2 = \frac{m_Z^2}{2} \left[1 + \left(1 - \frac{2\sqrt{2}\pi\alpha}{G_F m_Z^2} \right)^{1/2} \right], \quad \sin^2 2\theta_w = \frac{2\sqrt{2}\pi\alpha}{G_F m_Z^2}. \quad (11)$$

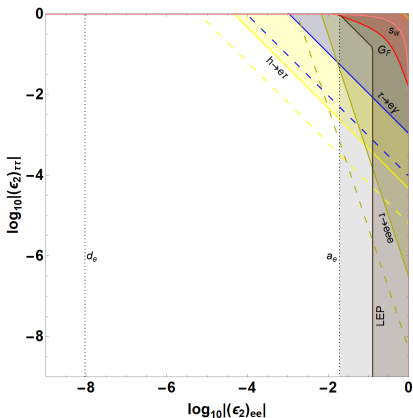
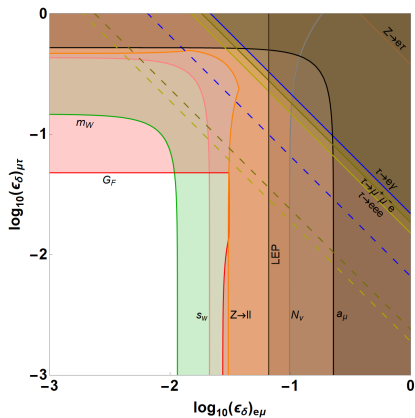
Type-I and type-III seesaw, $e - \mu$ sector



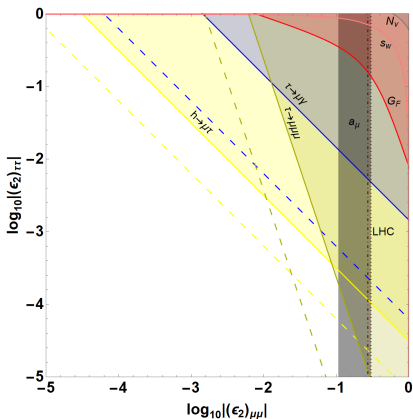
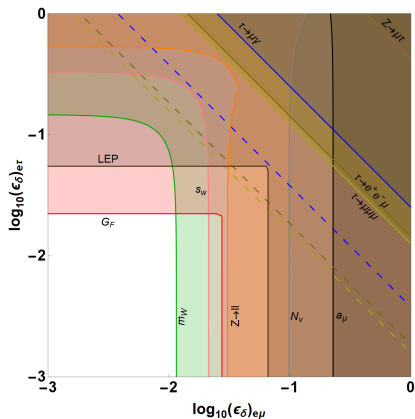
Type-I and type-III seesaw, $e - \tau$ sector



Zee model, $e - \tau$ sector



Zee model, $\mu - \tau$ sector



LQ model, $e - \tau$ sector

