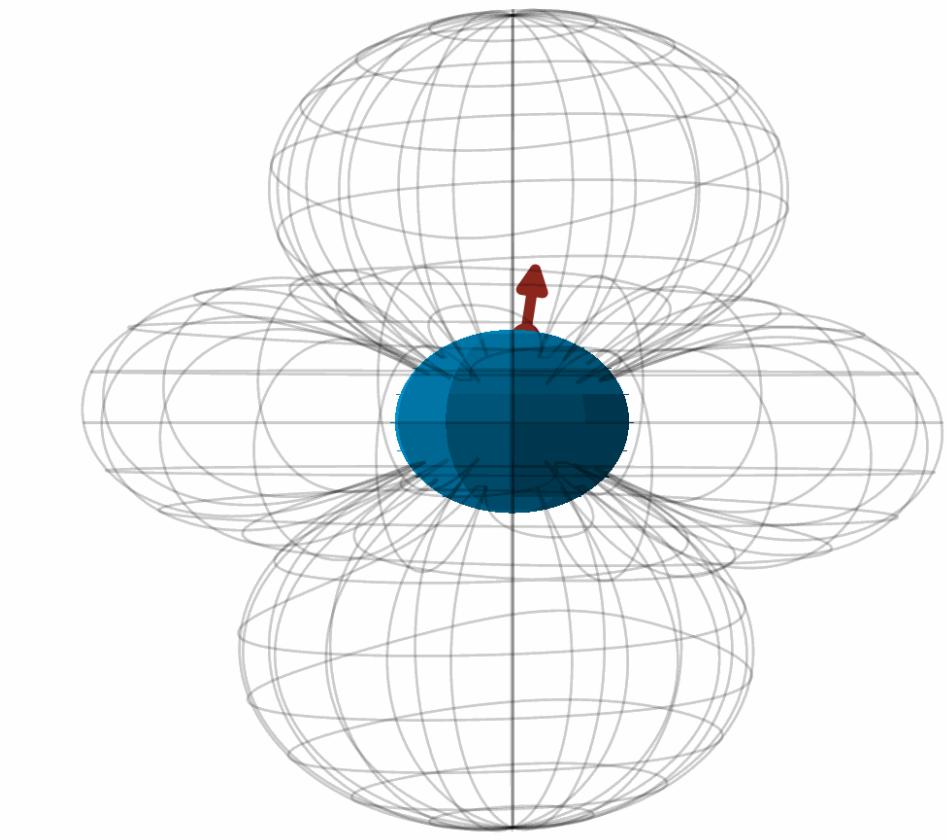


# Neutron Stars as Axion Laboratories

Samuel J. Witte

*28th IFT Xmas Workshop  
Madrid, Spain  
Dec. 15, 2022*



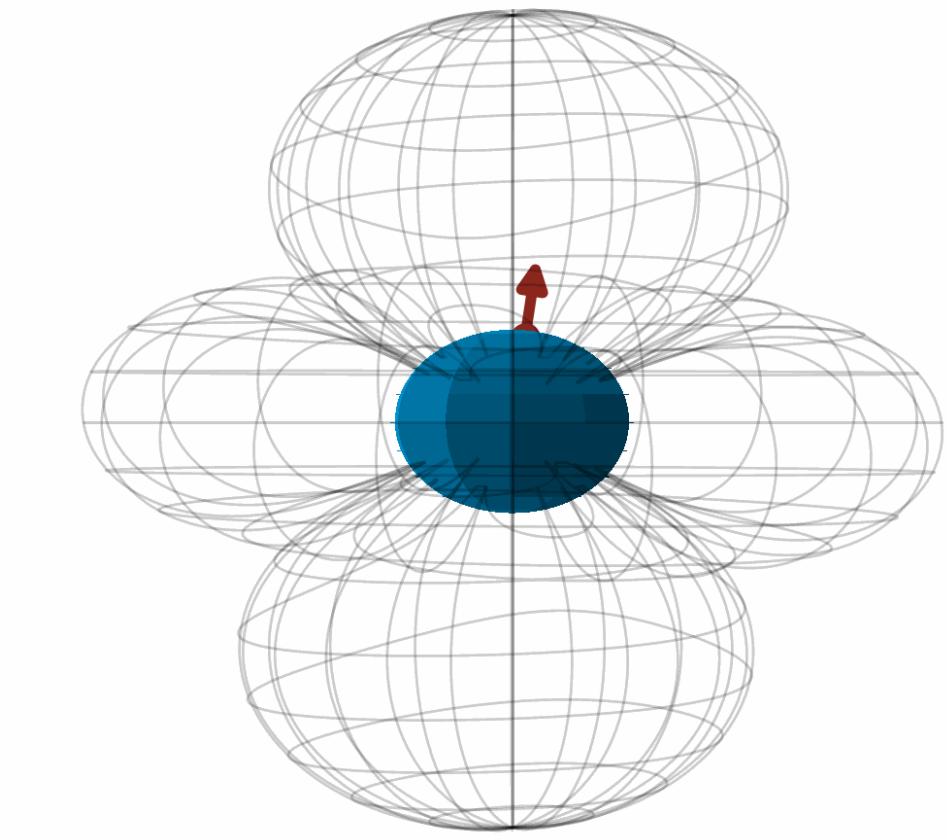
*Axions  
Photons*

Animations available at: [https://github.com/SamWitte/GIF\\_Storage](https://github.com/SamWitte/GIF_Storage)

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**GRAPPA**

GRavitation AstroParticle Physics Amsterdam



UNIVERSITY  
OF AMSTERDAM

# The strong CP problem

*Why does QCD seem to conserve charge-parity (CP) symmetry?*

CP violating term in QCD Lagrangian:

$$\mathcal{L}_{CPV} \supset \bar{\theta} \frac{g_s^2}{32\pi^2} G \tilde{G}$$

Neutron electric dipole moment (eDM)  $\propto \bar{\theta}$

Current limit:  $\bar{\theta} \leq 5 \times 10^{-11}$

Abel et al (2020)

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**Solution:** Introduce goldstone boson  $a$  with parameter  $f_a$  to make theta term dynamical

$$\mathcal{L}_\theta = - \left( \bar{\theta} + \frac{a}{f_a} \right) \frac{g^2}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

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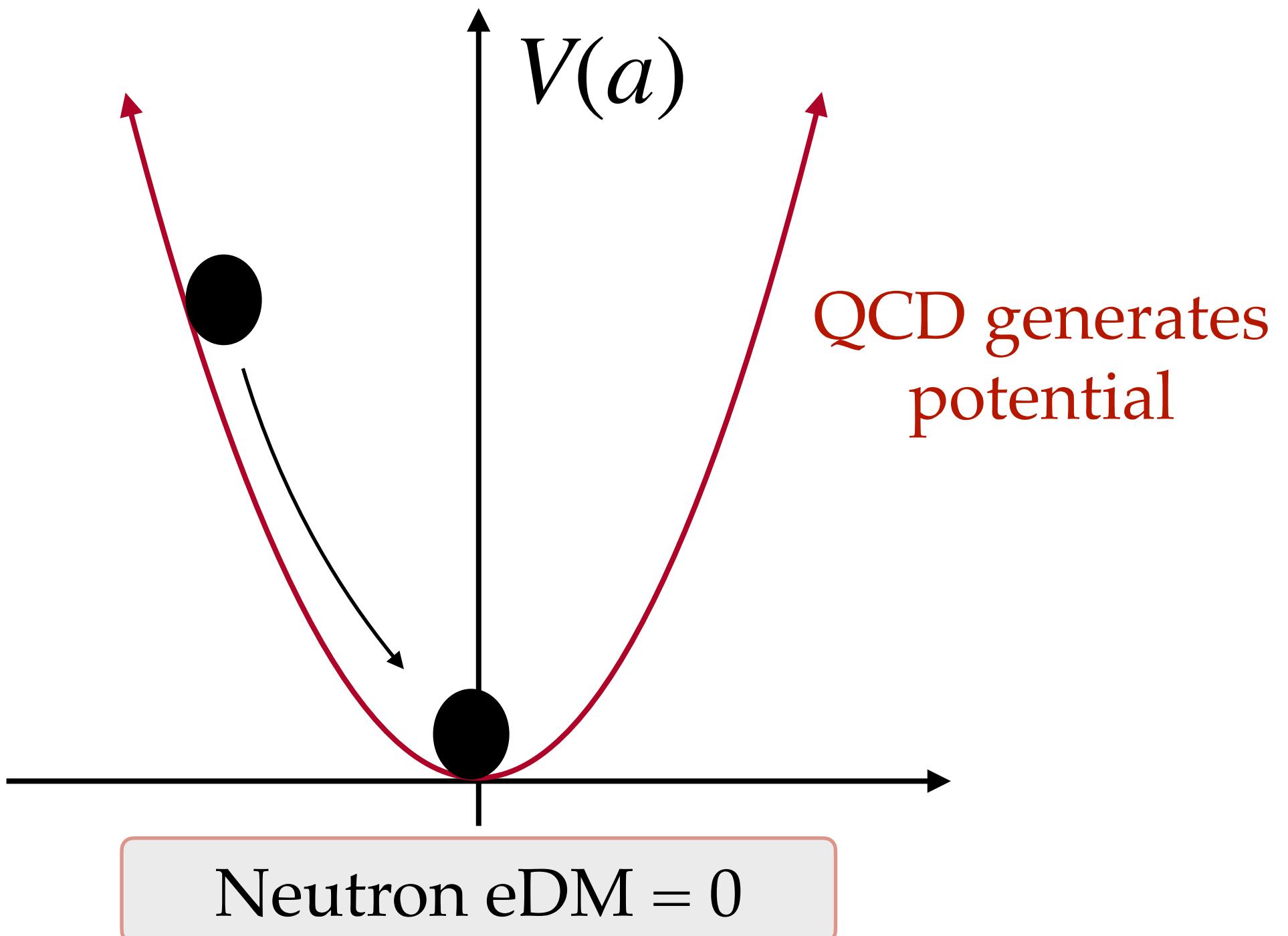
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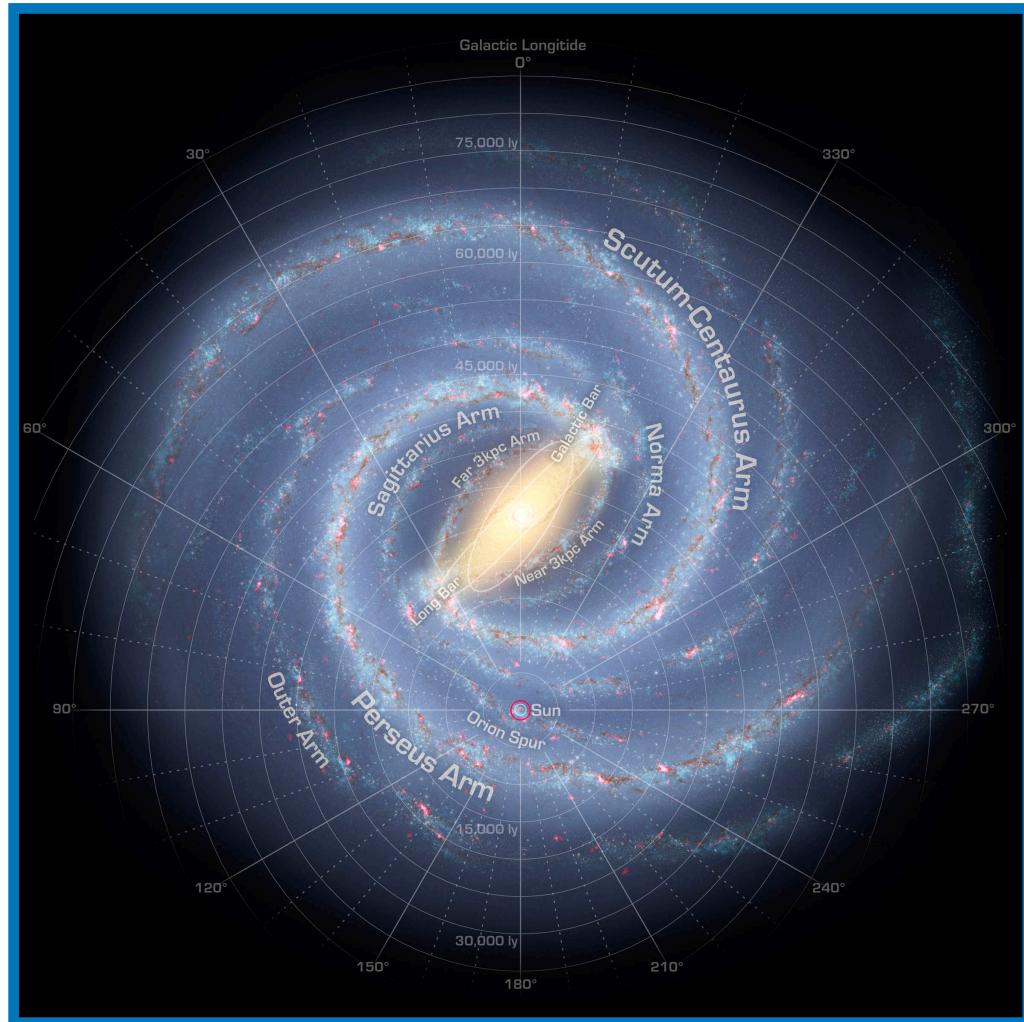
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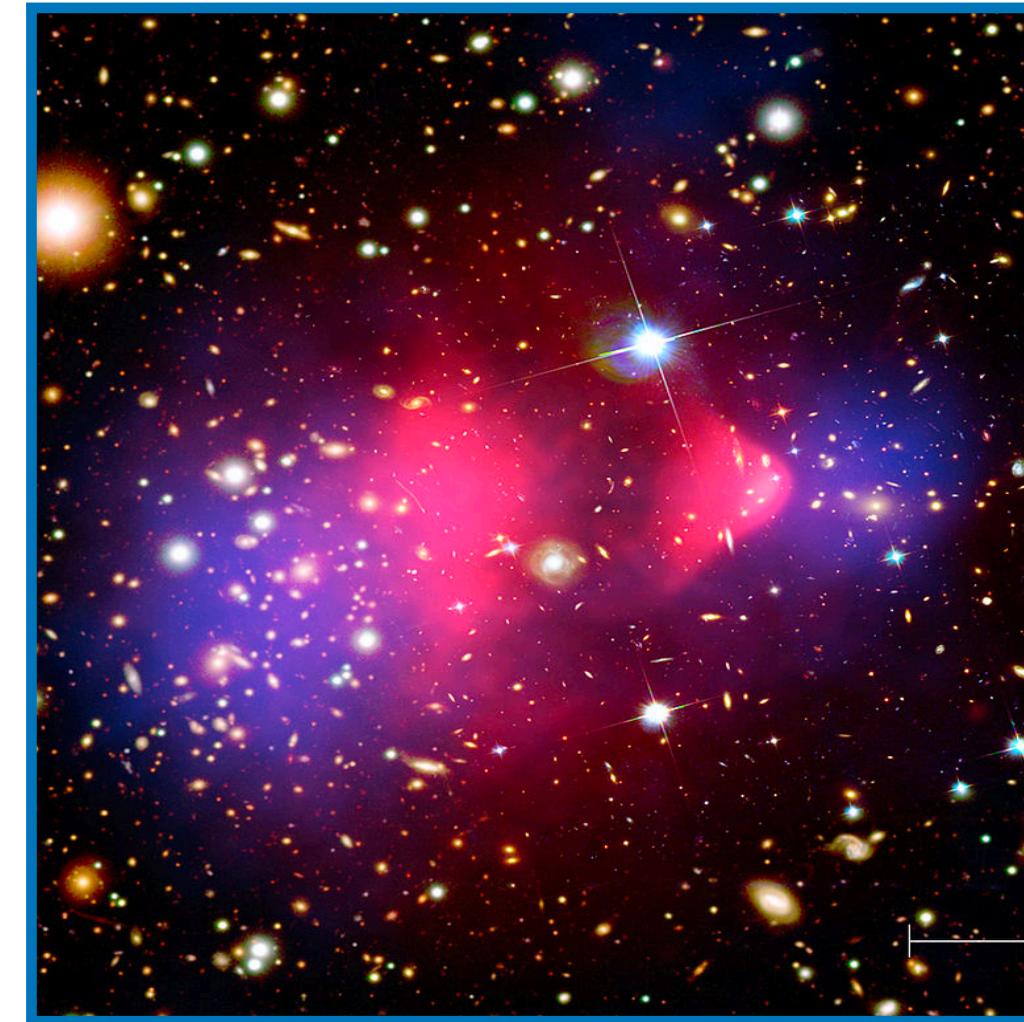
# Evidence for dark matter

*~26% of energy in the Universe today is in a new form of feebly interacting matter*

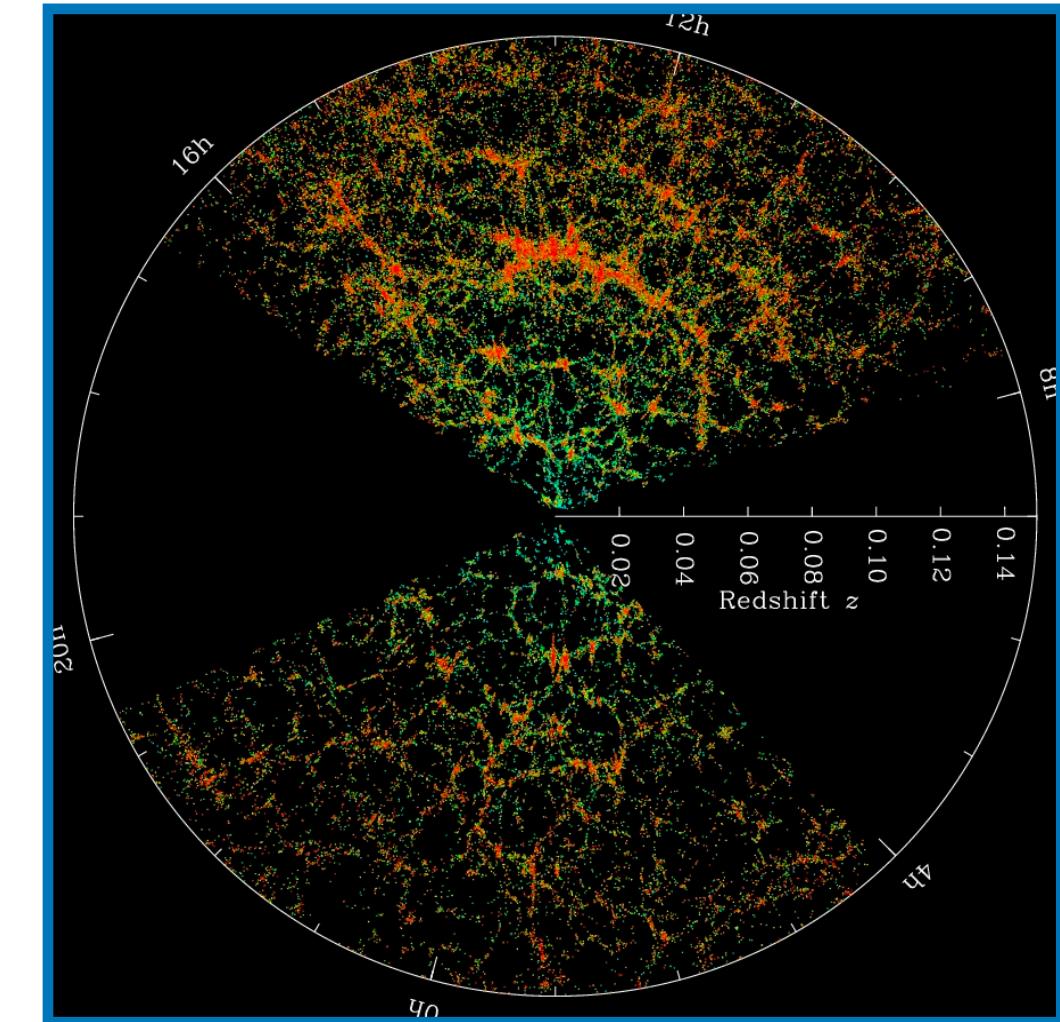
*Galaxy rotation curves*



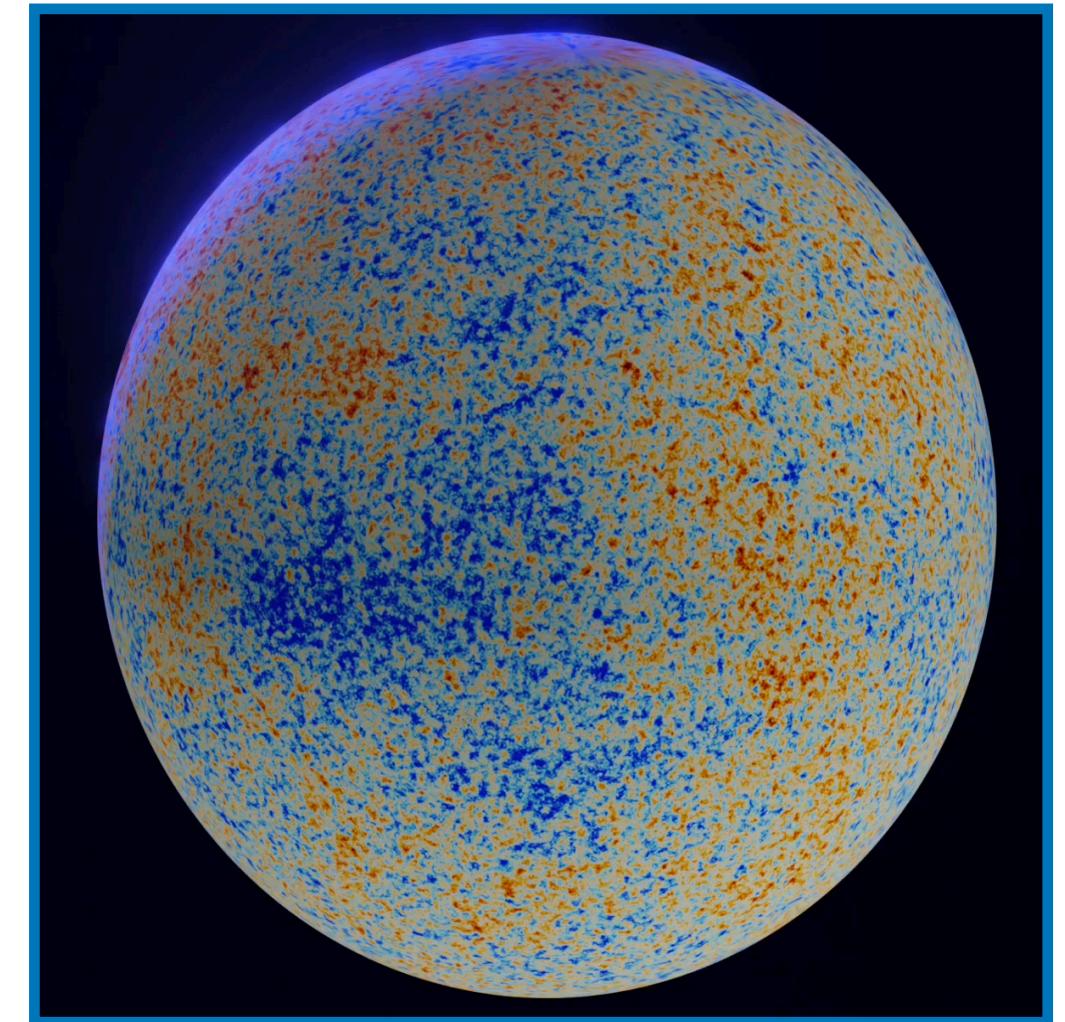
*Merging galaxy clusters*



*Large scale structure*



*Cosmic microwave background*



$\sim kpc$

(Today)

$\sim Mpc$

$\sim 100 Mpc$

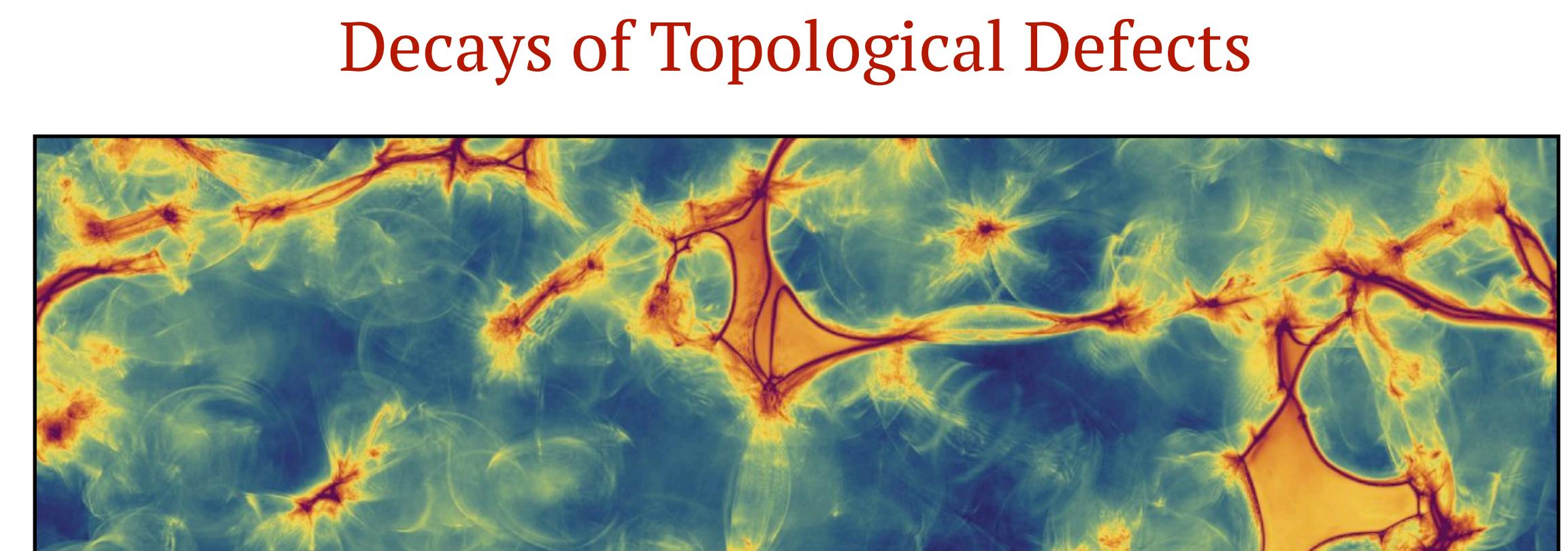
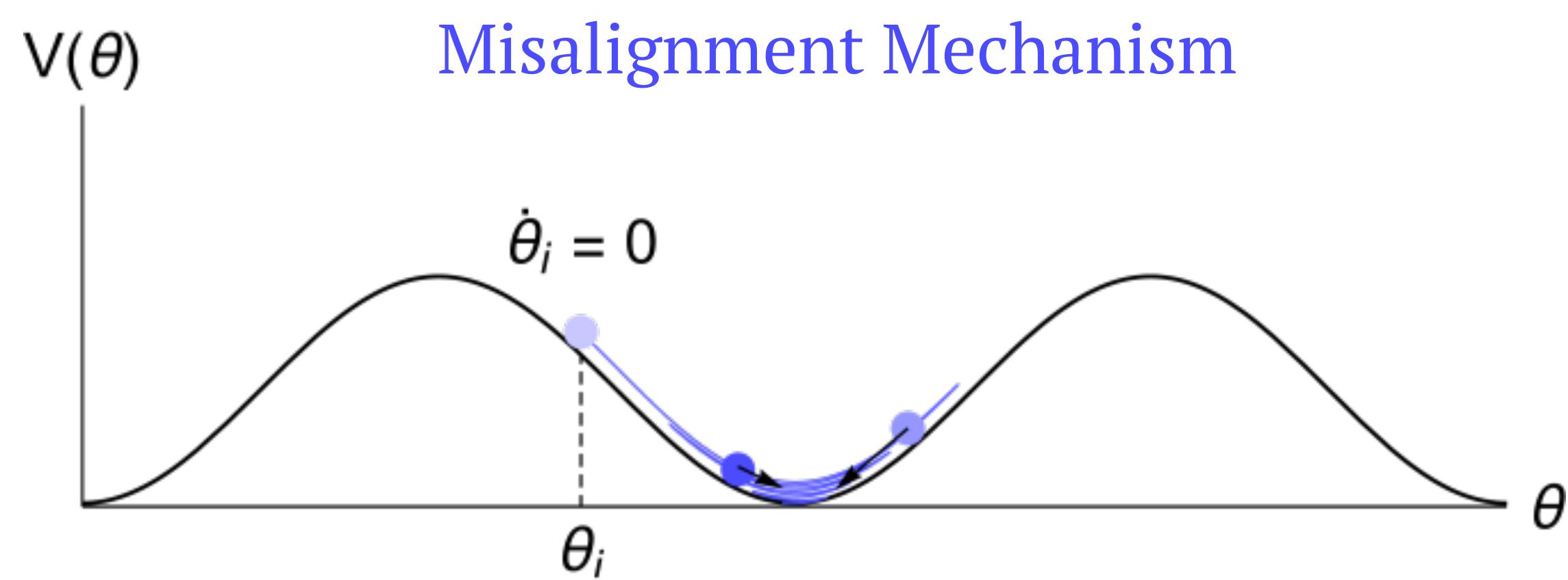
$\sim 10 Gpc$

(370,000 after big bang)

*Characteristic  
Scale*

# Axions as dark matter candidates

- Light axions ( $m_a \ll \mathcal{O}(\text{eV})$ ) are feebly interacting and naturally long-lived
- Can be produced non-thermally in the early Universe



Can easily accommodate observed abundance of dark matter

# Properties of the axion

Axion Mass:

$$m_a \sim \frac{\Lambda_{QCD}^2}{f_a}$$

Axion Couplings:

$$\mathcal{L} \supset \frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

(Term for Strong CP Problem)

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

(Electro-Mag)

$$\sum_f \frac{1}{f_a} \partial_\mu a \bar{f} \gamma^\mu \gamma_5 f$$

(Fermions)

... + other terms

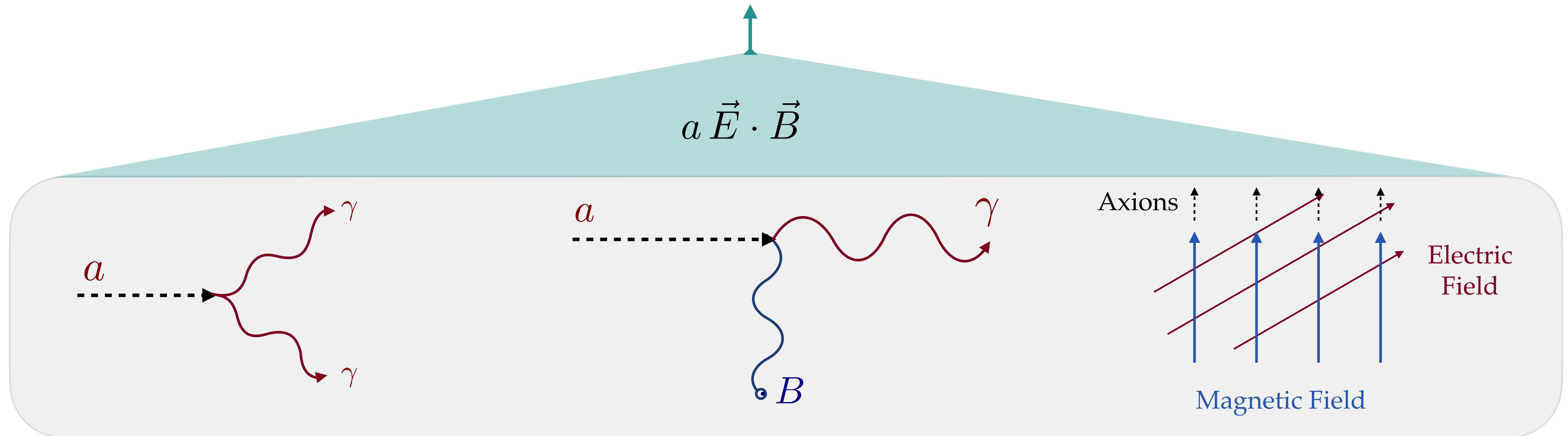
(Slight model dependence  
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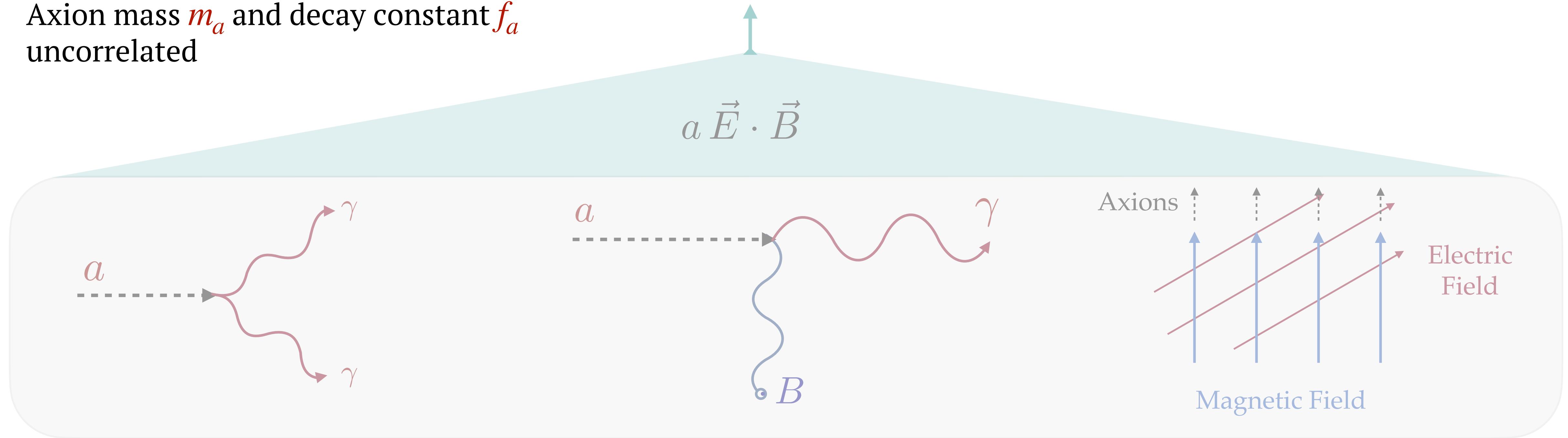


# Axion-like particles (ALPs)

***ALPs do not solve strong CP problem, but naturally emerge in String Theory from compactification***

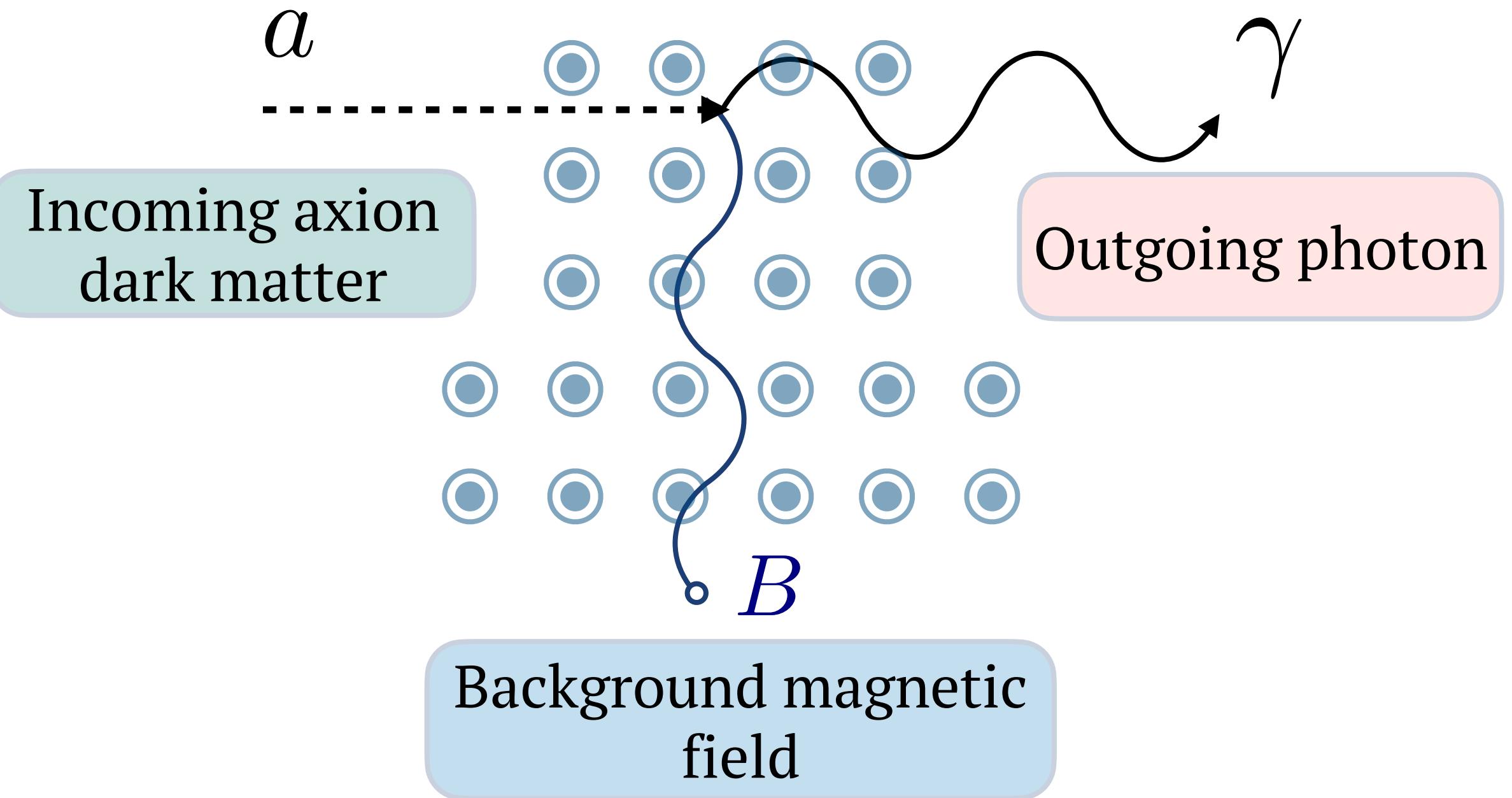
Axion Couplings:  $\mathcal{L} \supset$  No Coupling  $\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$  ... + other terms  
(Electro-Mag)

Axion mass  $m_a$  and decay constant  $f_a$   
uncorrelated



# Axion-photon mixing

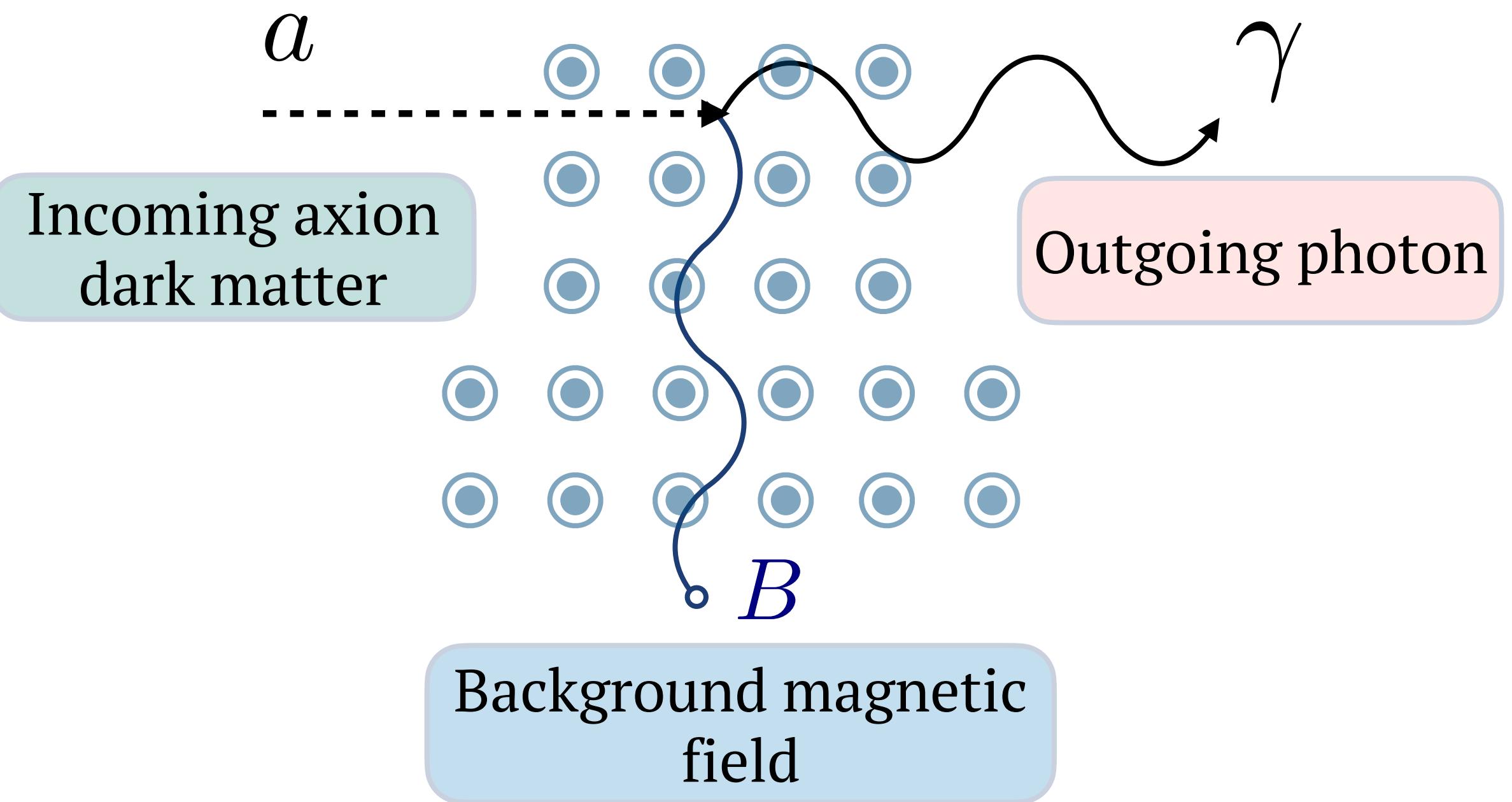
$$\mathcal{L} \sim g_{a\gamma\gamma} [a] E \cdot B$$



# Axion-photon mixing

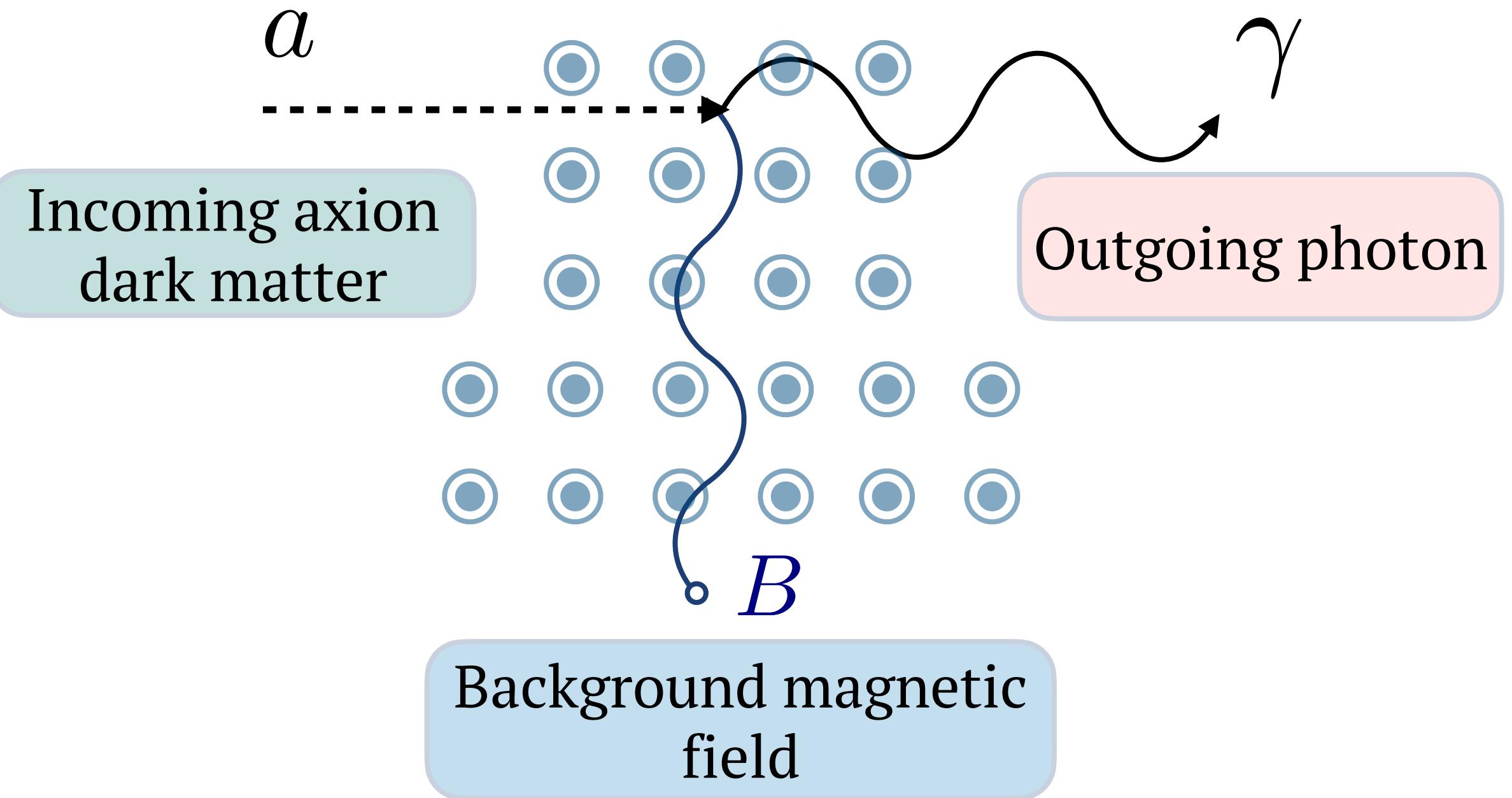
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$$p_{a \rightarrow \gamma} \sim g_{a\gamma\gamma}^2 B^2 \times (\text{Length})^2$$



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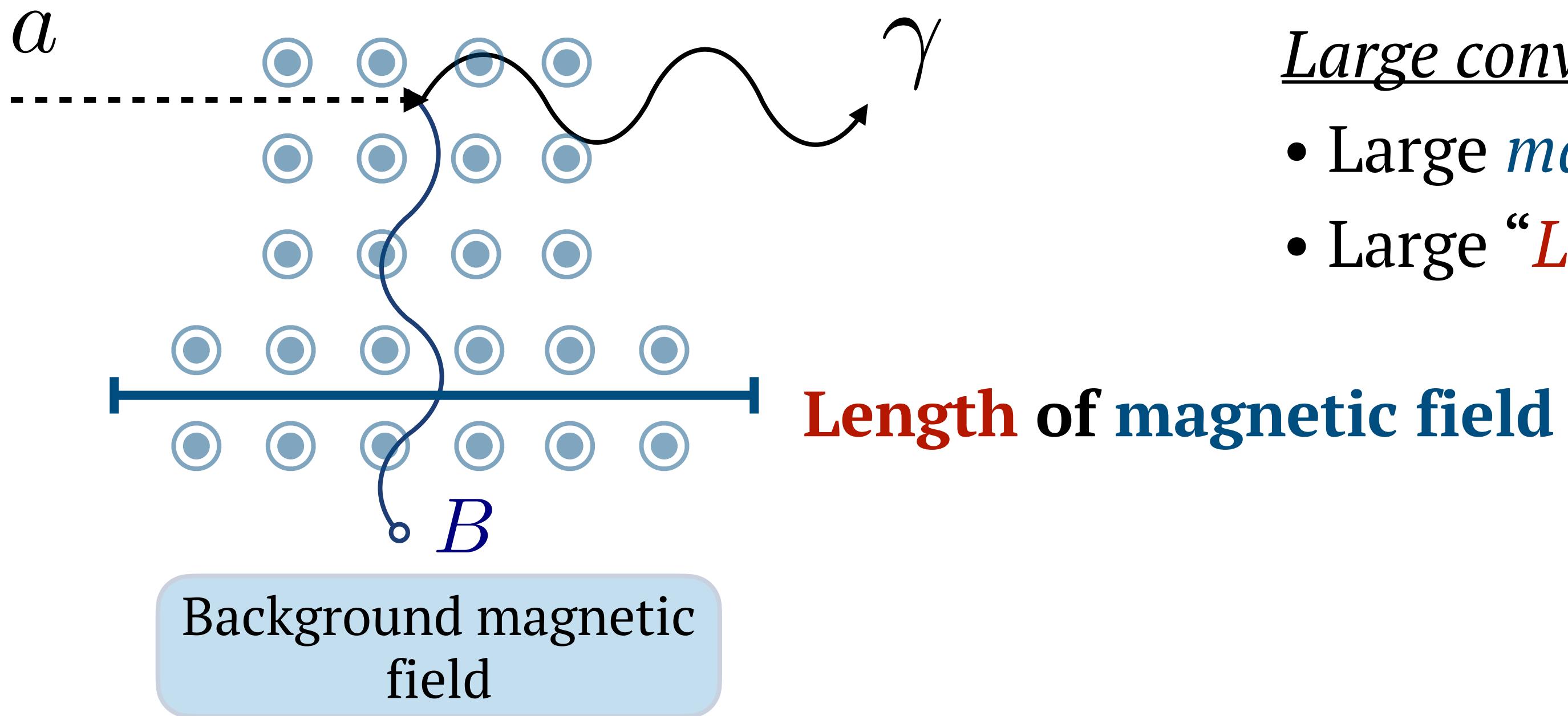
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Large conversion probabilities require:

- Large *magnetic fields*
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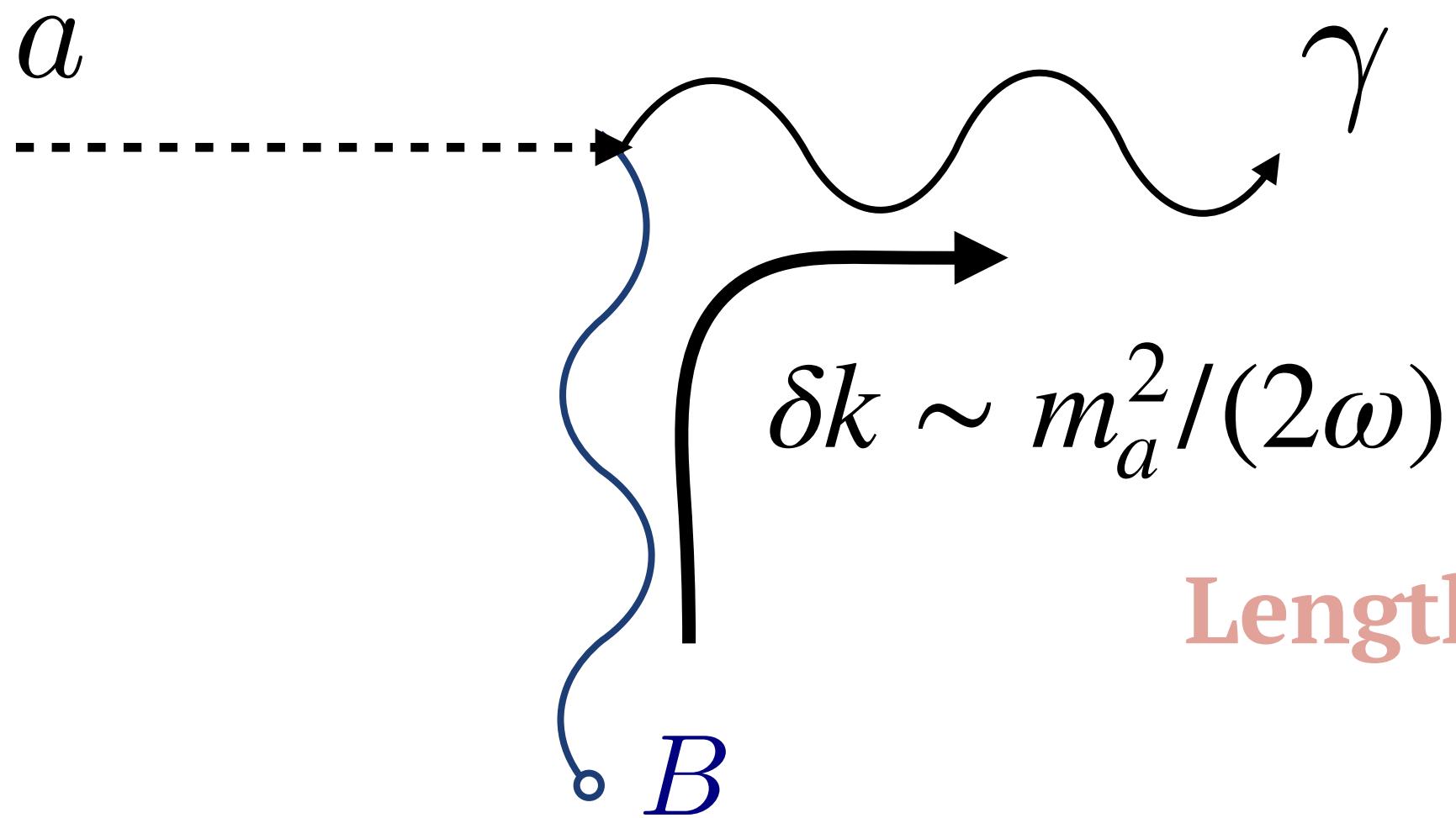
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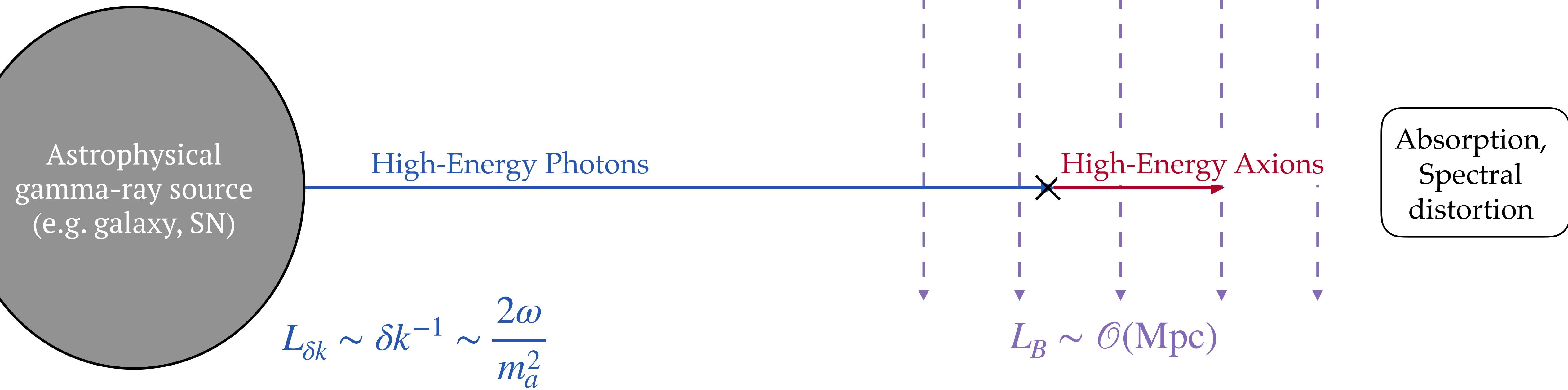
**Length set by momentum transfer from magnetic field**

$$L_{\delta k} \sim \delta k^{-1}$$

# Axion-photon mixing

Galactic/Cluster Magnetic Field

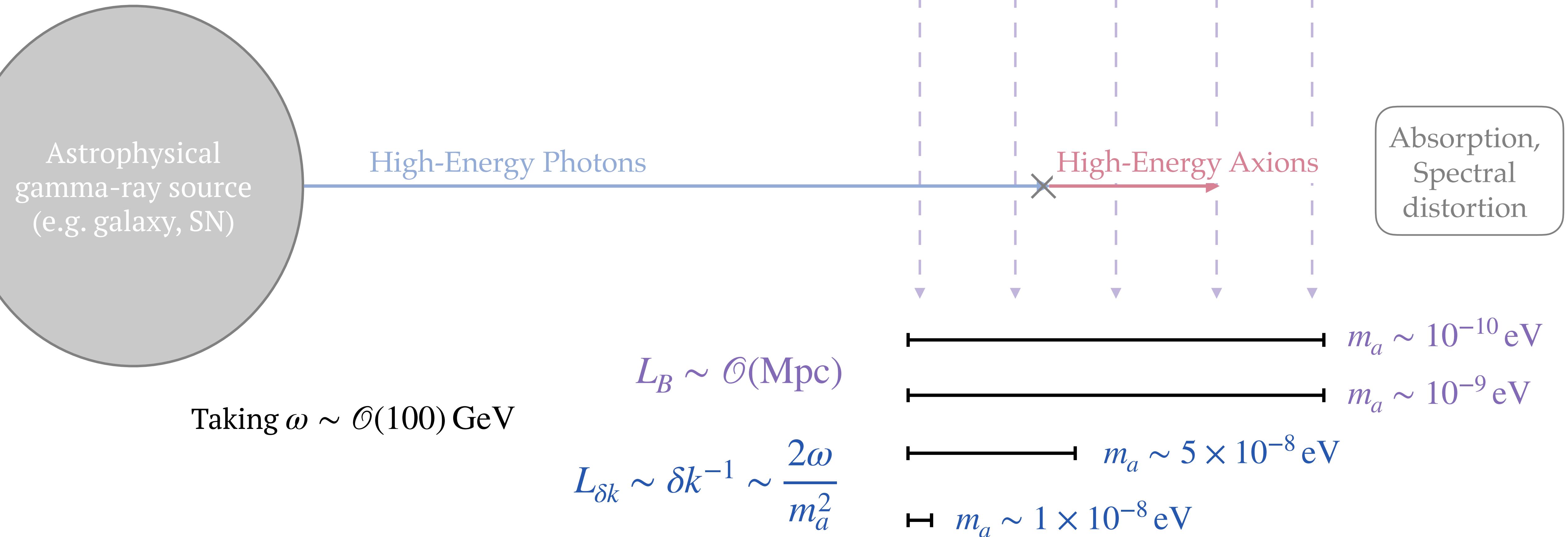
***High-energy indirect axion searches***



# Axion-photon mixing

Galactic/Cluster Magnetic Field

***High-energy indirect axion searches***



# Axion parameter space

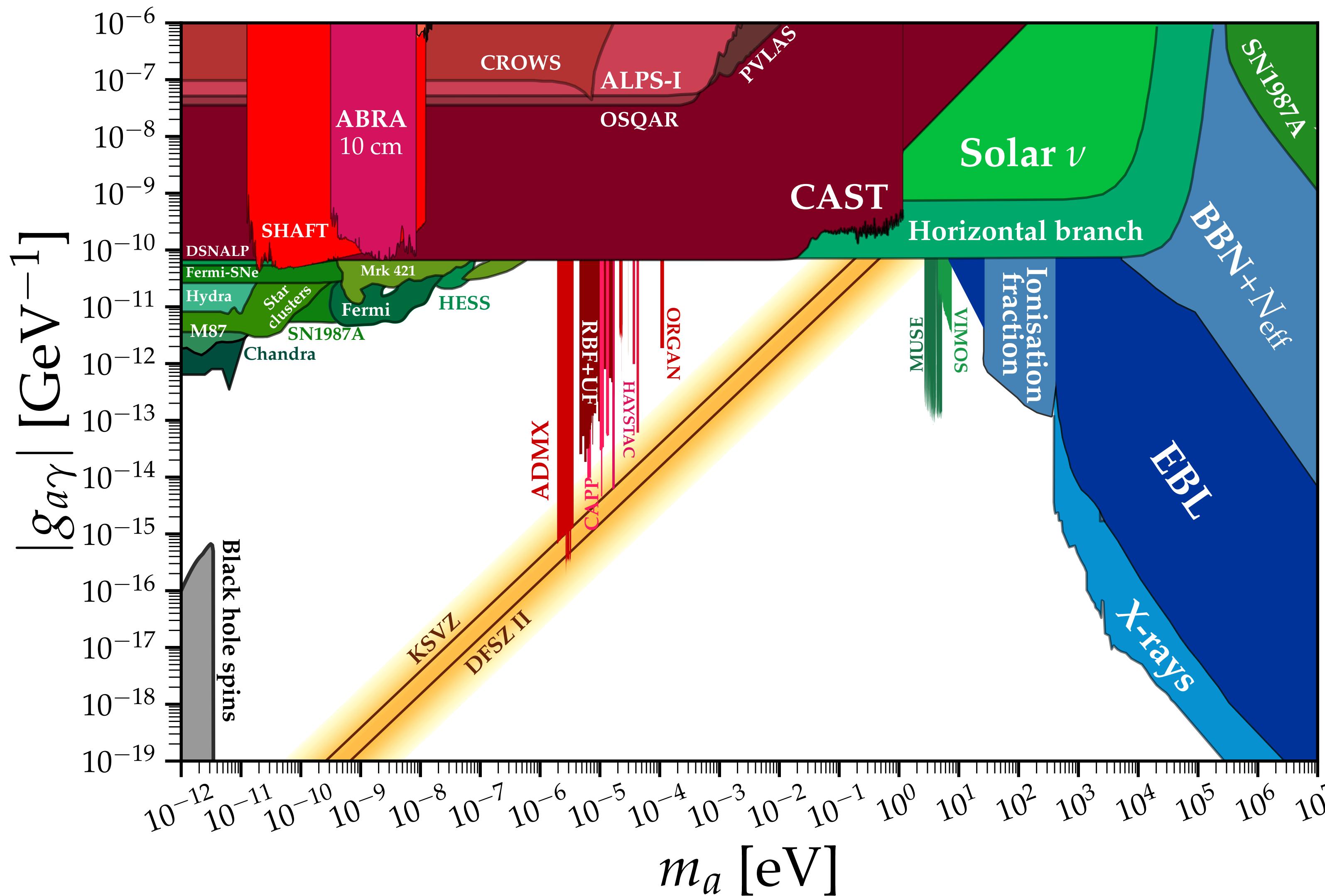


Image credit: Ciaran O'hare  
(Slightly out of date – c. 2021)

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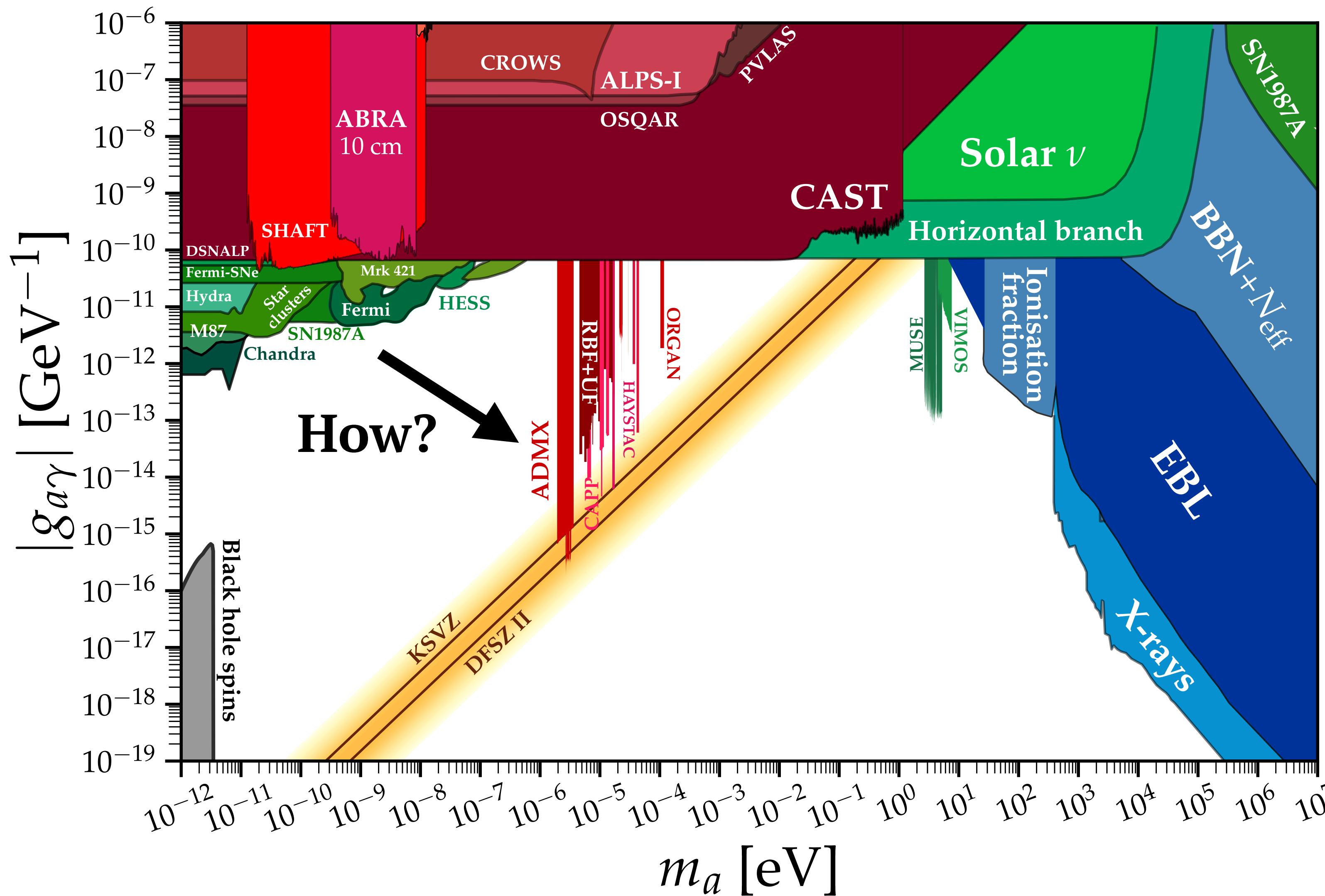
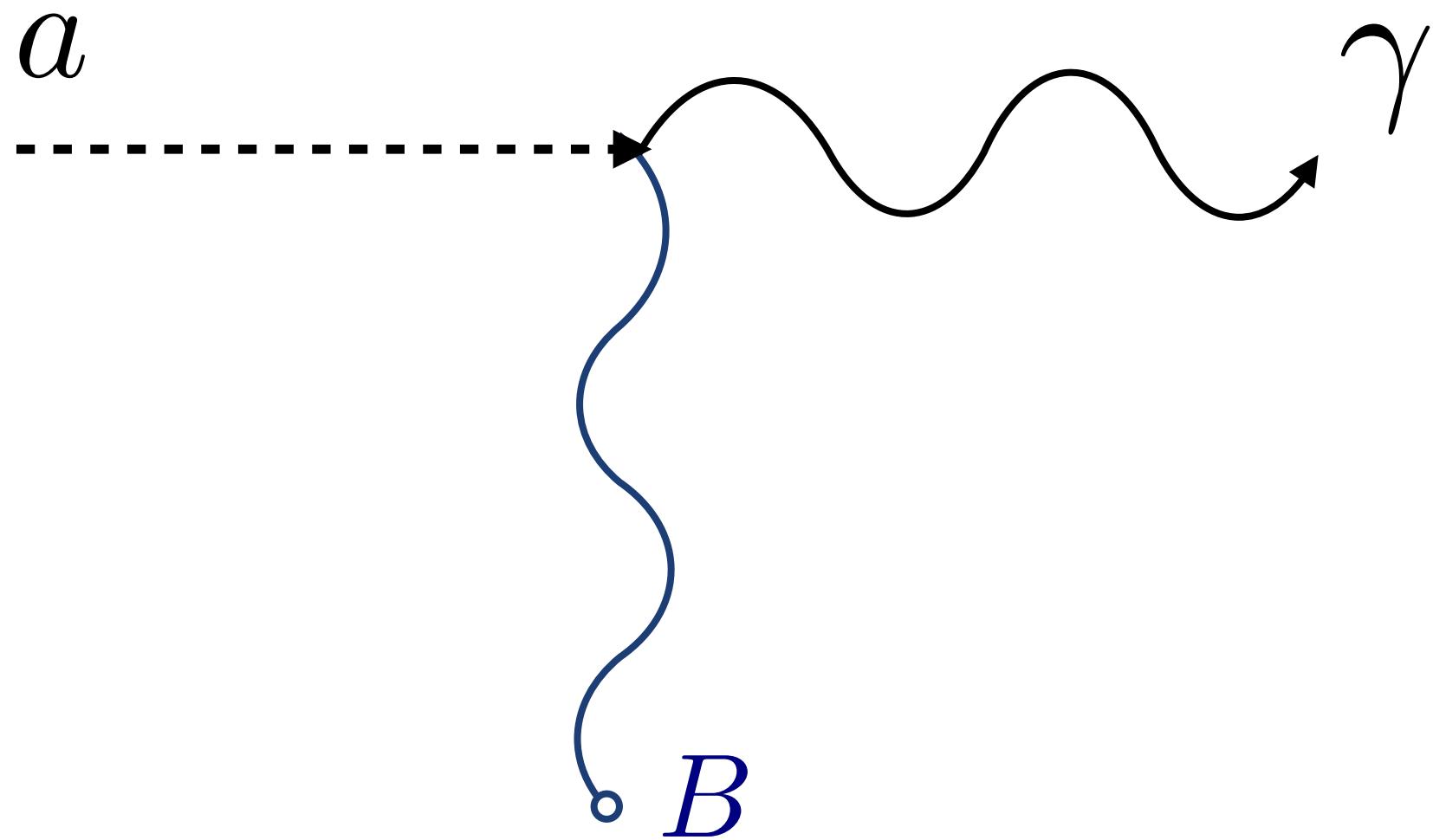


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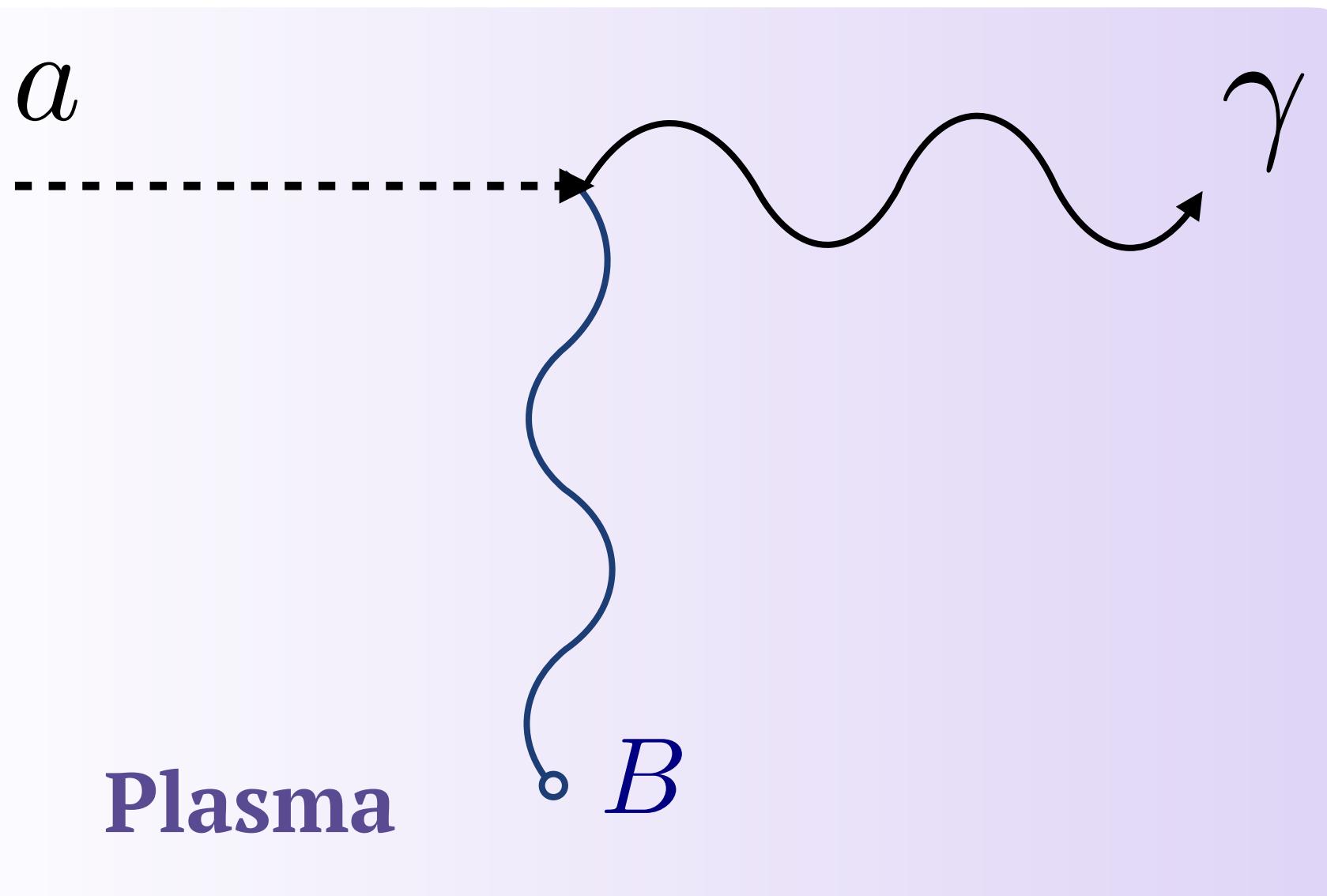
Momentum mismatch in **vacuum**

$$\delta k \sim \sqrt{\omega^2 - m_a^2} - \omega$$

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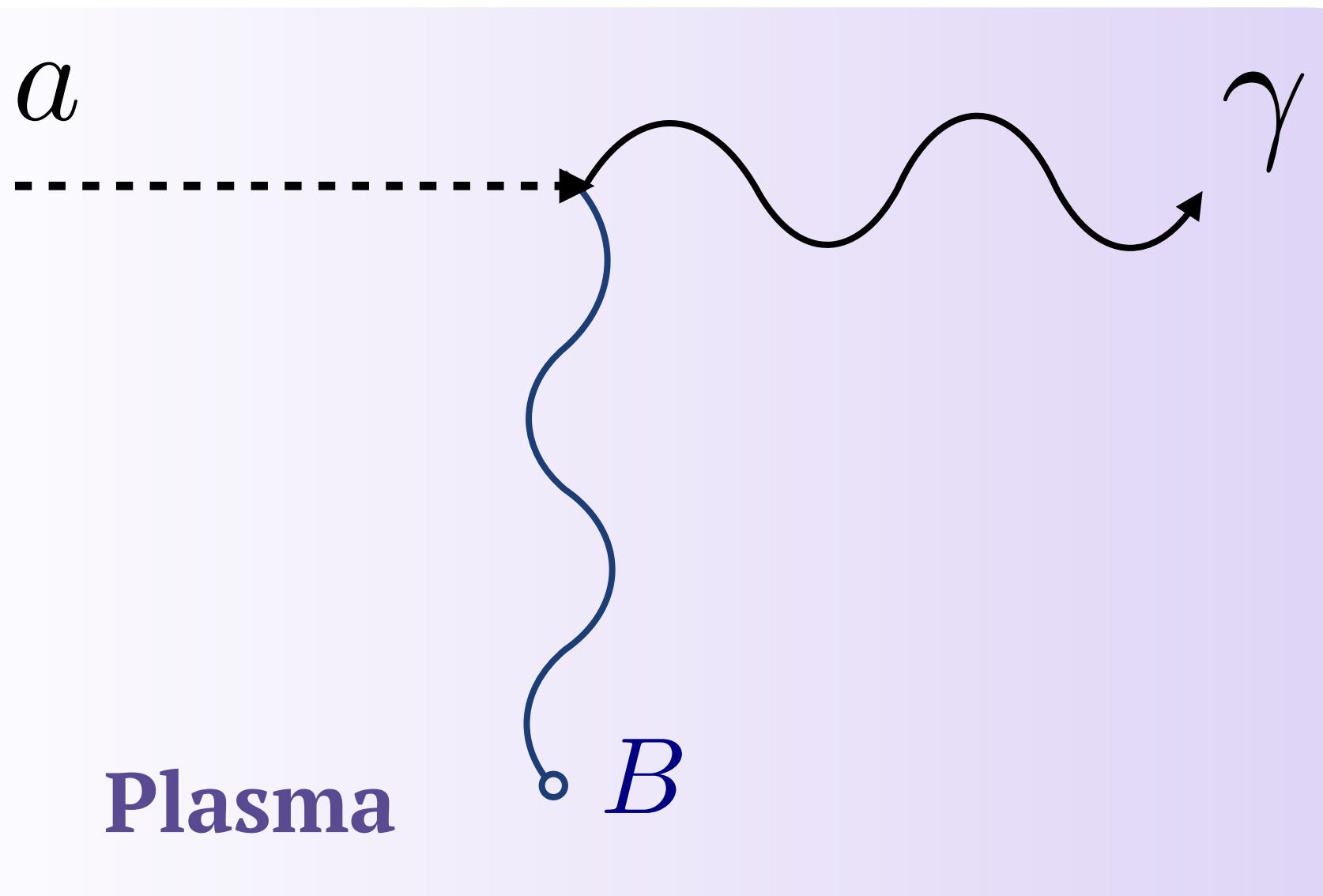
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Momentum mismatch in plasma

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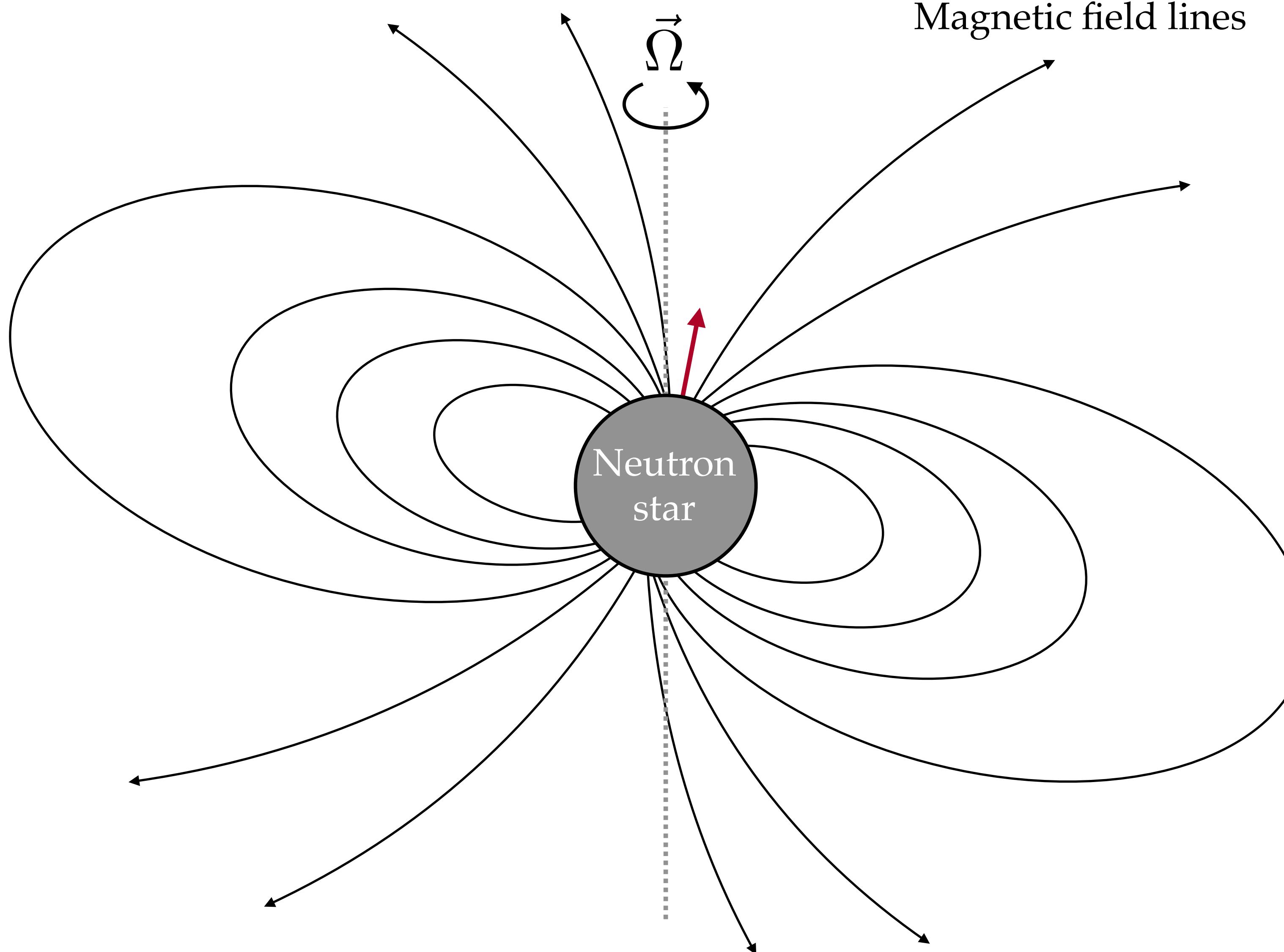
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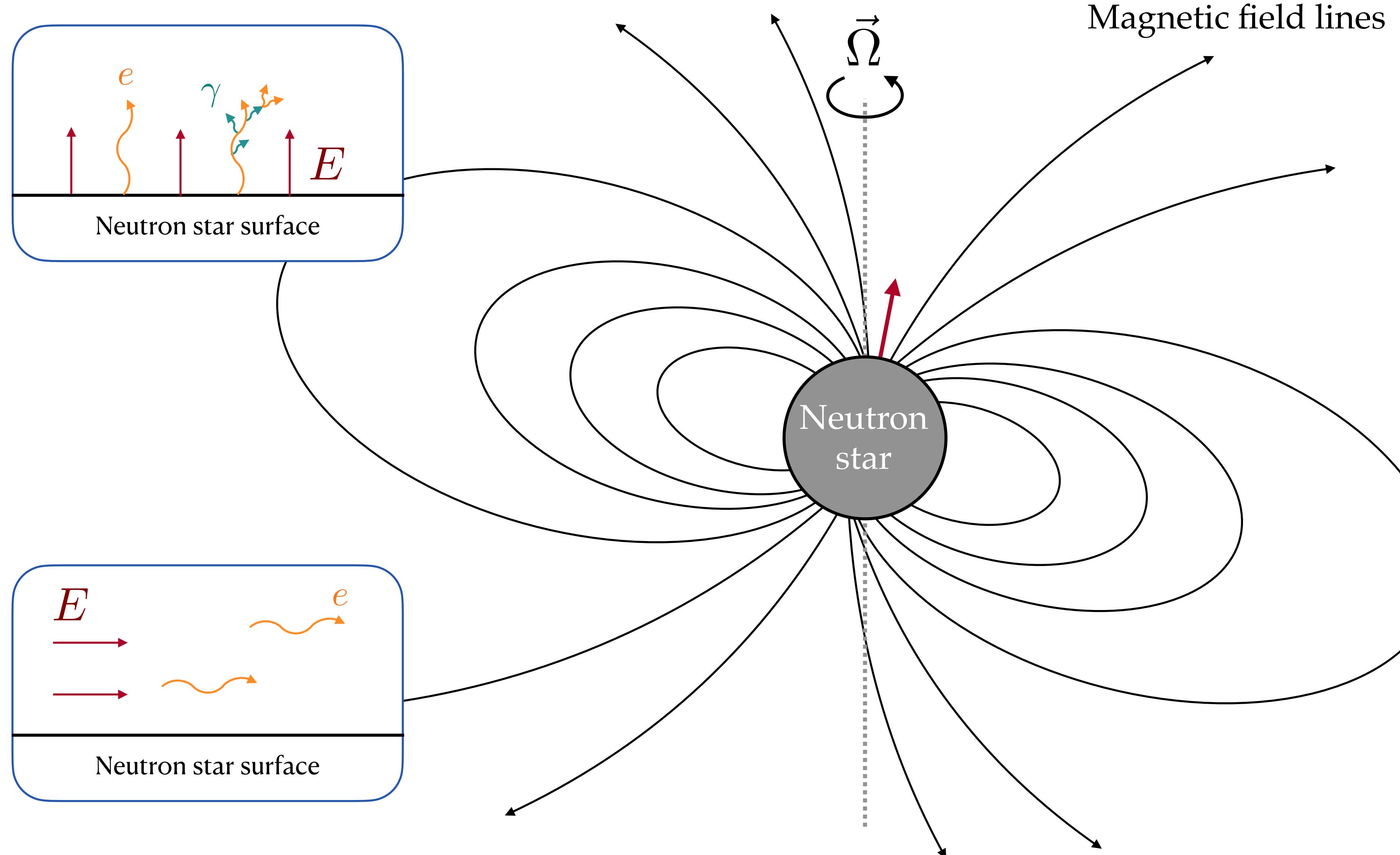
*Ideal environments: Large coherent magnetic fields and spatially varying plasmas*

# Neutron star magnetospheres



$$|\vec{B}| \lesssim 10^{15} \text{ G}$$
$$r_{NS} \sim 10 \text{ km}$$

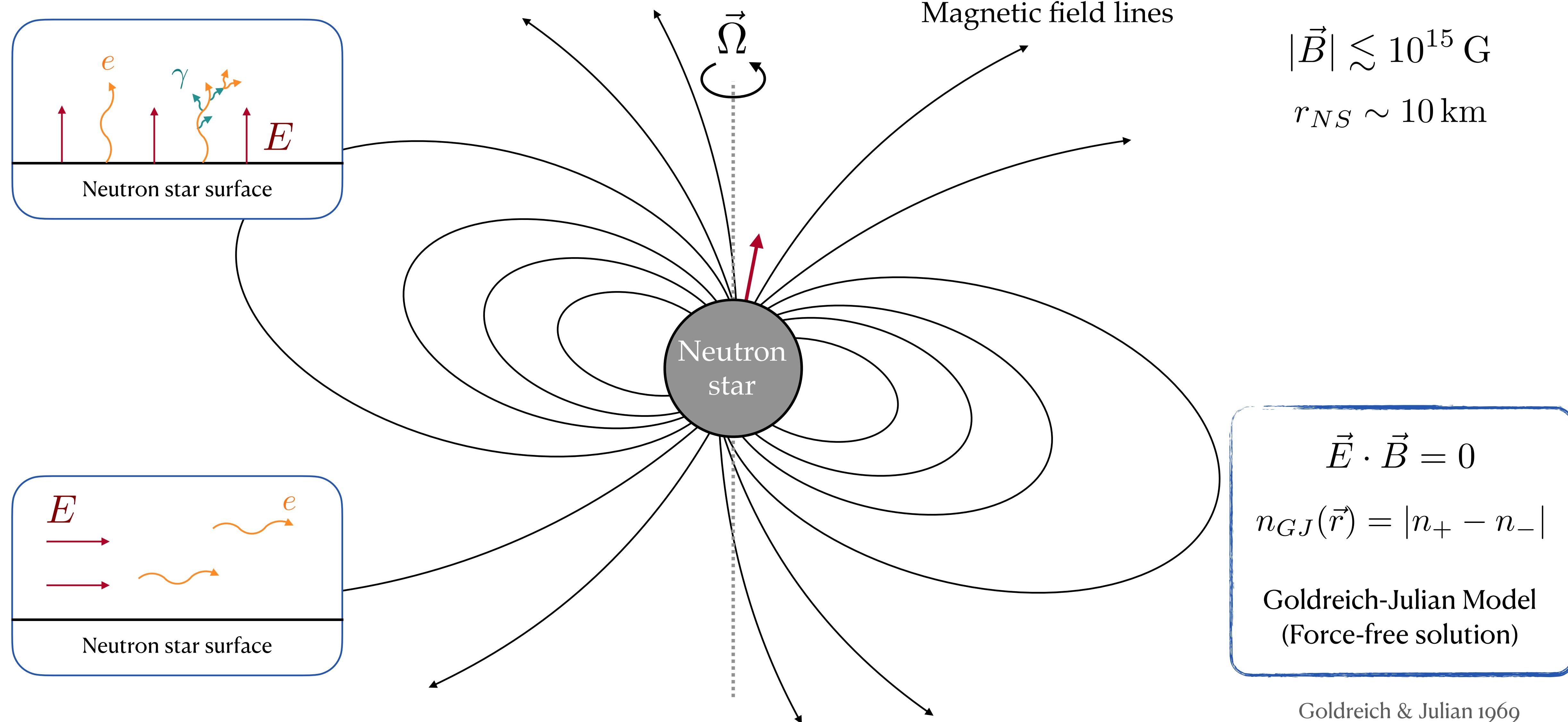
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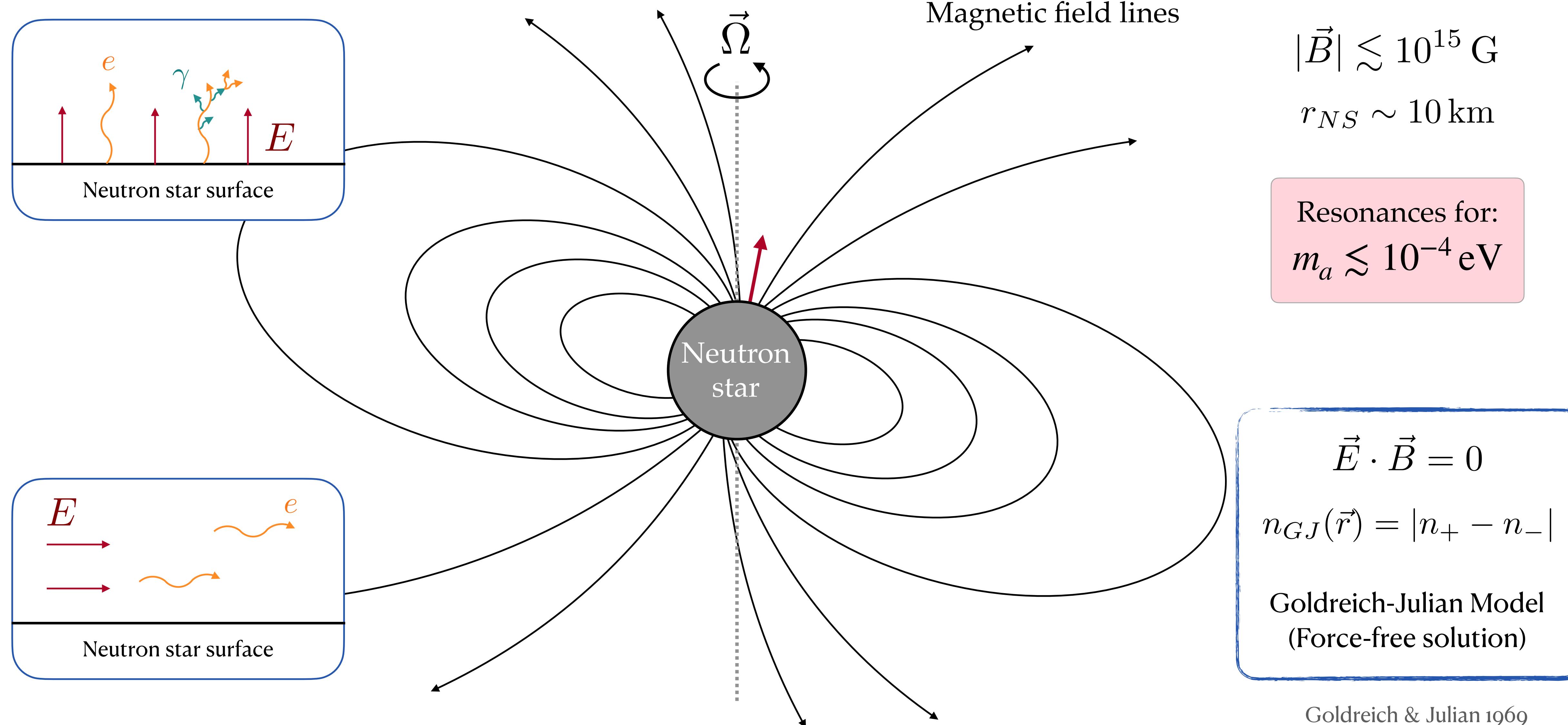
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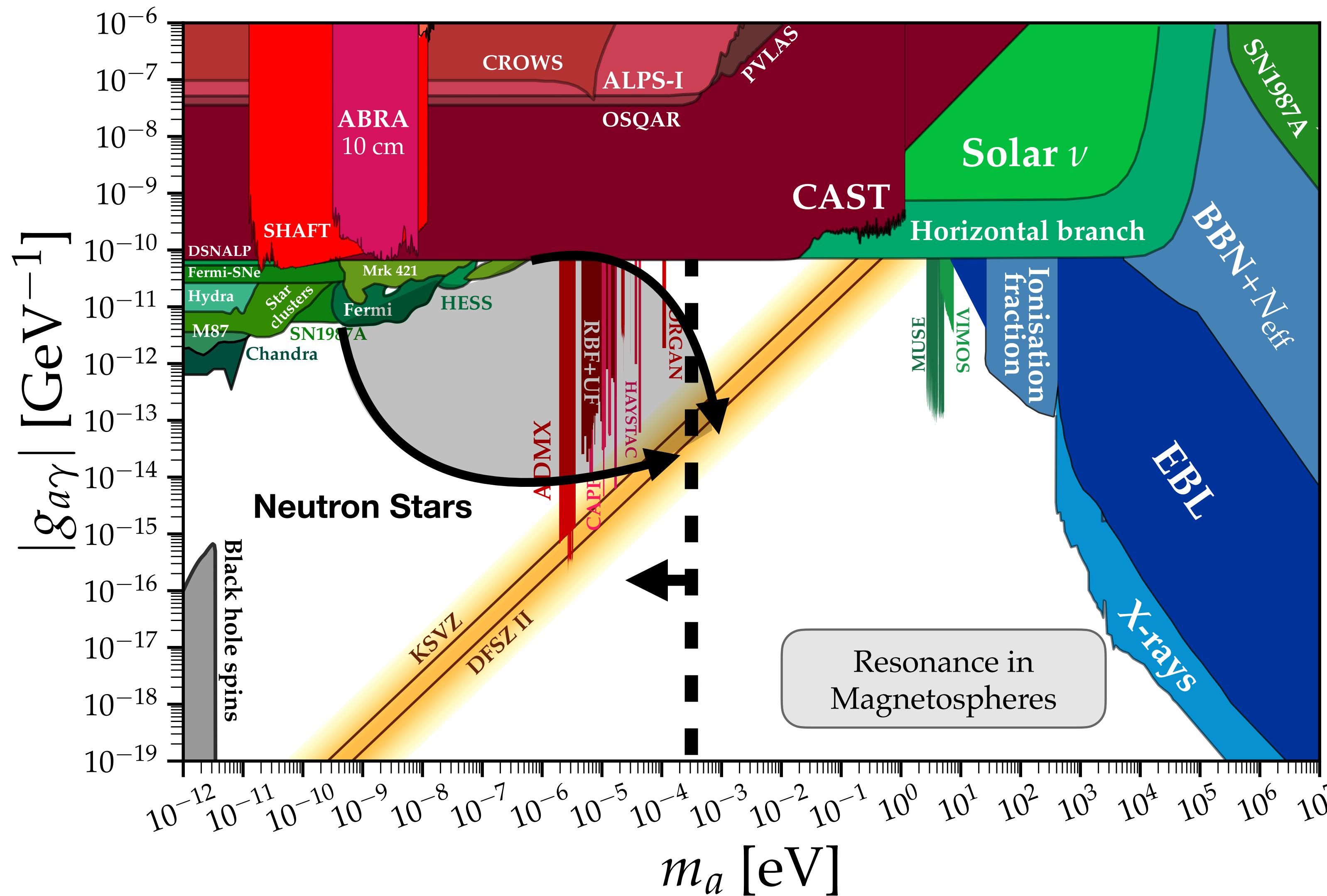
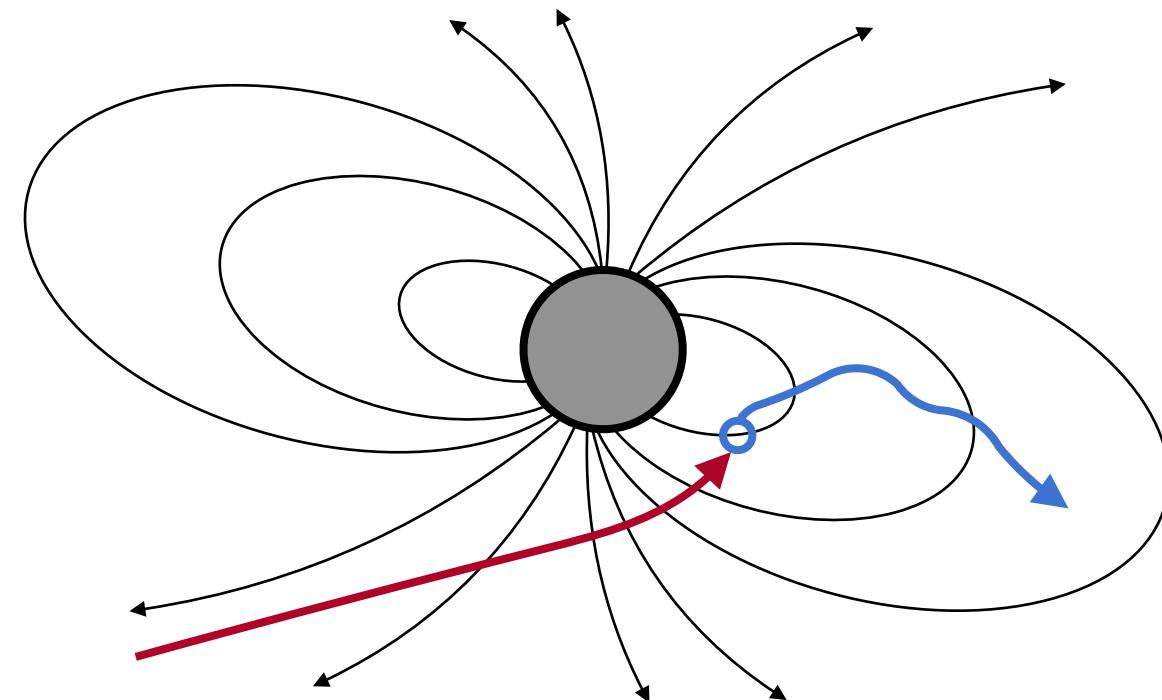


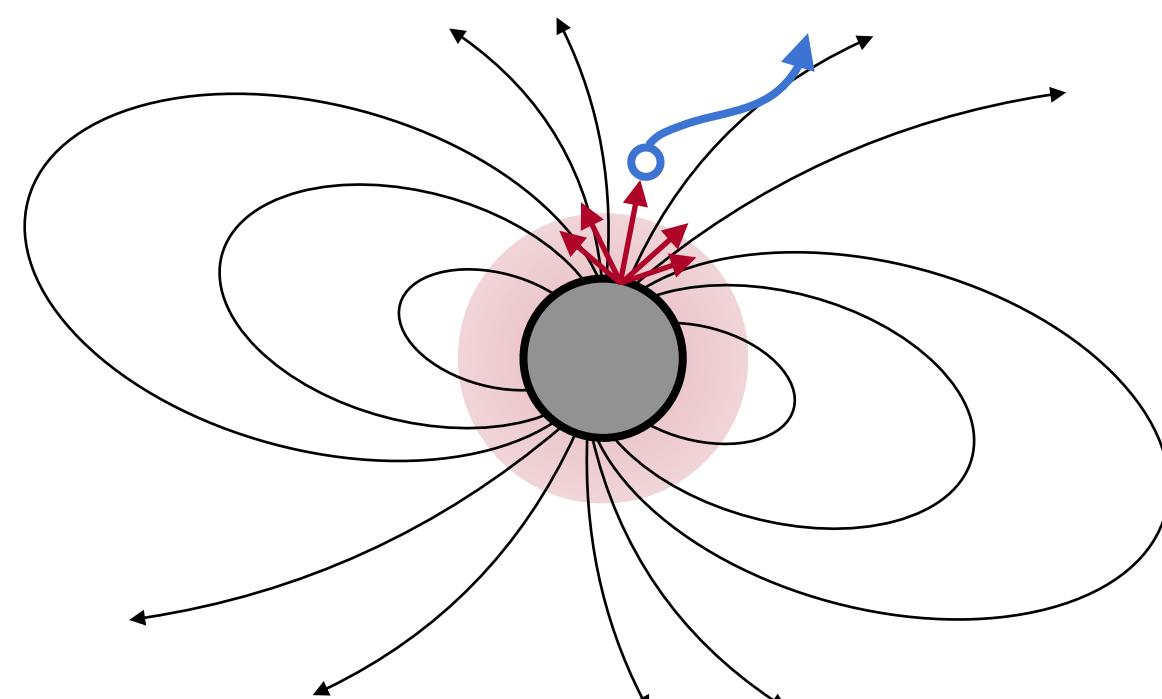
Image credit: Ciaran O'hare

# Neutron stars as axion labs



## Part 1: Resonant production of radio photons from axion dark matter

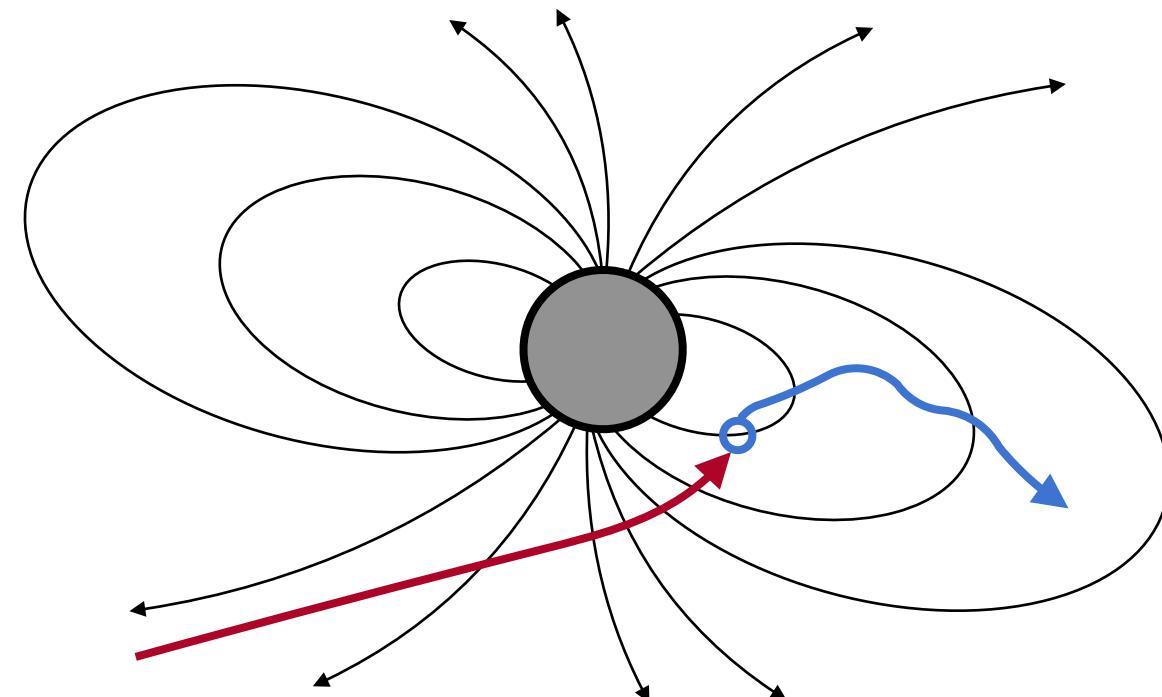
See e.g.: Pshirkov & Popov (2009), Hook et al. (2018), Safdi et al. (2018), Battye et al. (2019, 2021), SJW et al. (2021, 2022), Foster, SJW et al (2022), Thejmsland, McDonald, SJW (To appear), SJW et al (To appear), McDonald & SJW (To appear),...



## Part 2: Axion production from pulsar pair cascades

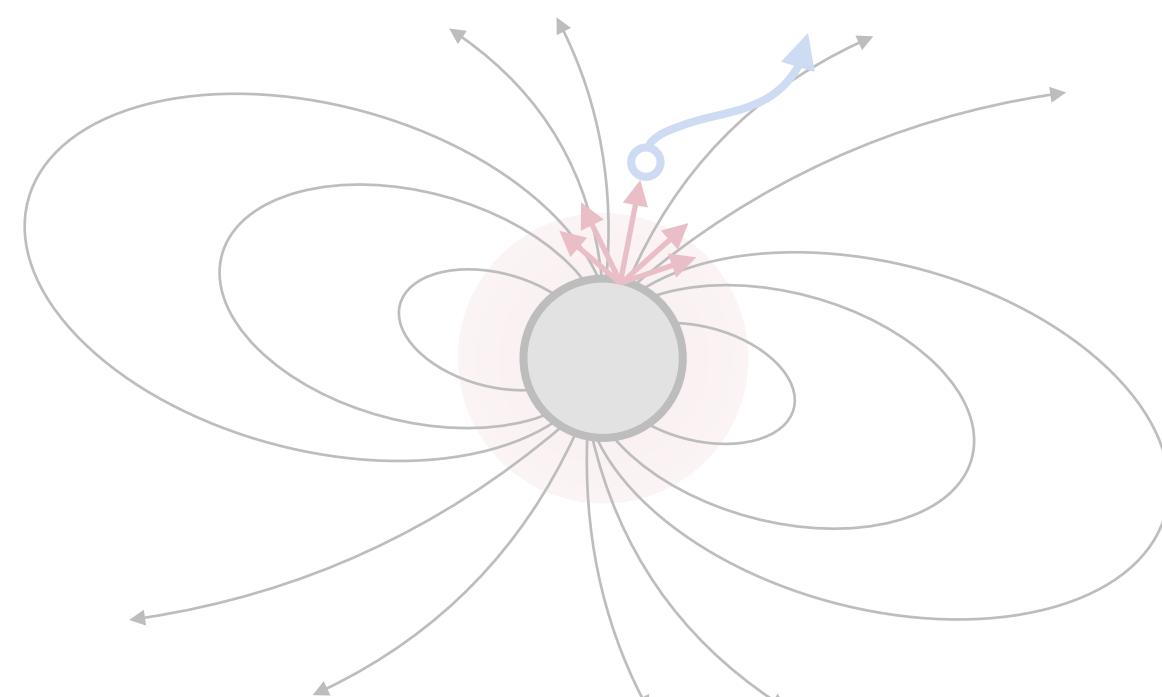
Prabhu (2021), Noordhuis, Prabhu, SJW, Cruz, Chen, Weniger (2022), Noordhuis, Prabhu, SJW, Weniger (Appearing soon), Caputo, Philippov, SJW (Appearing soon)

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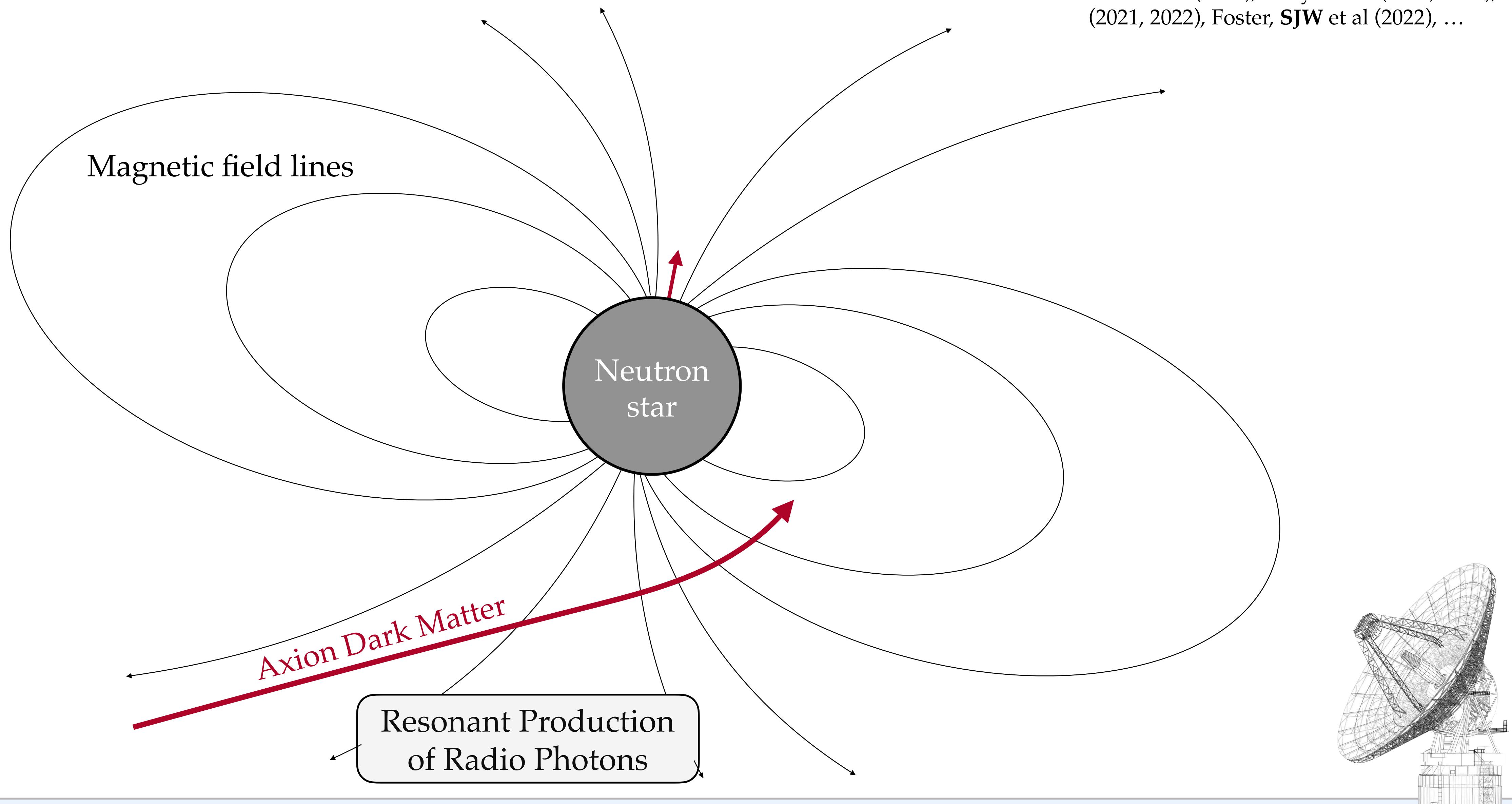


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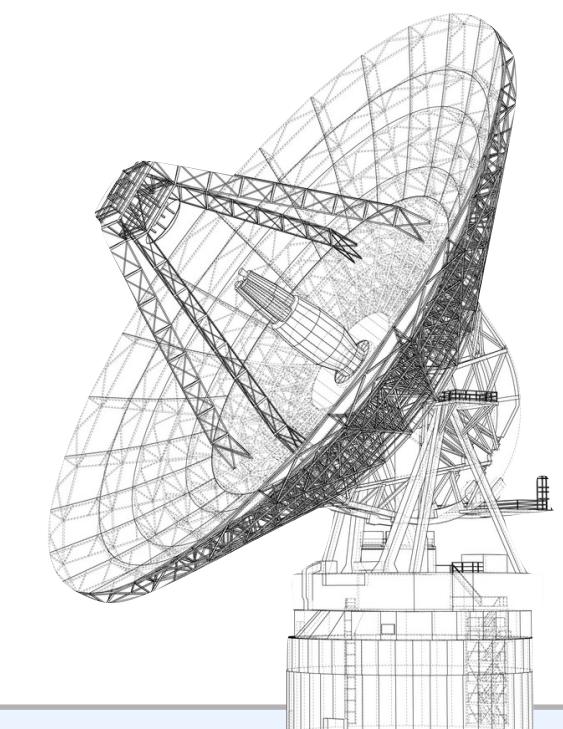
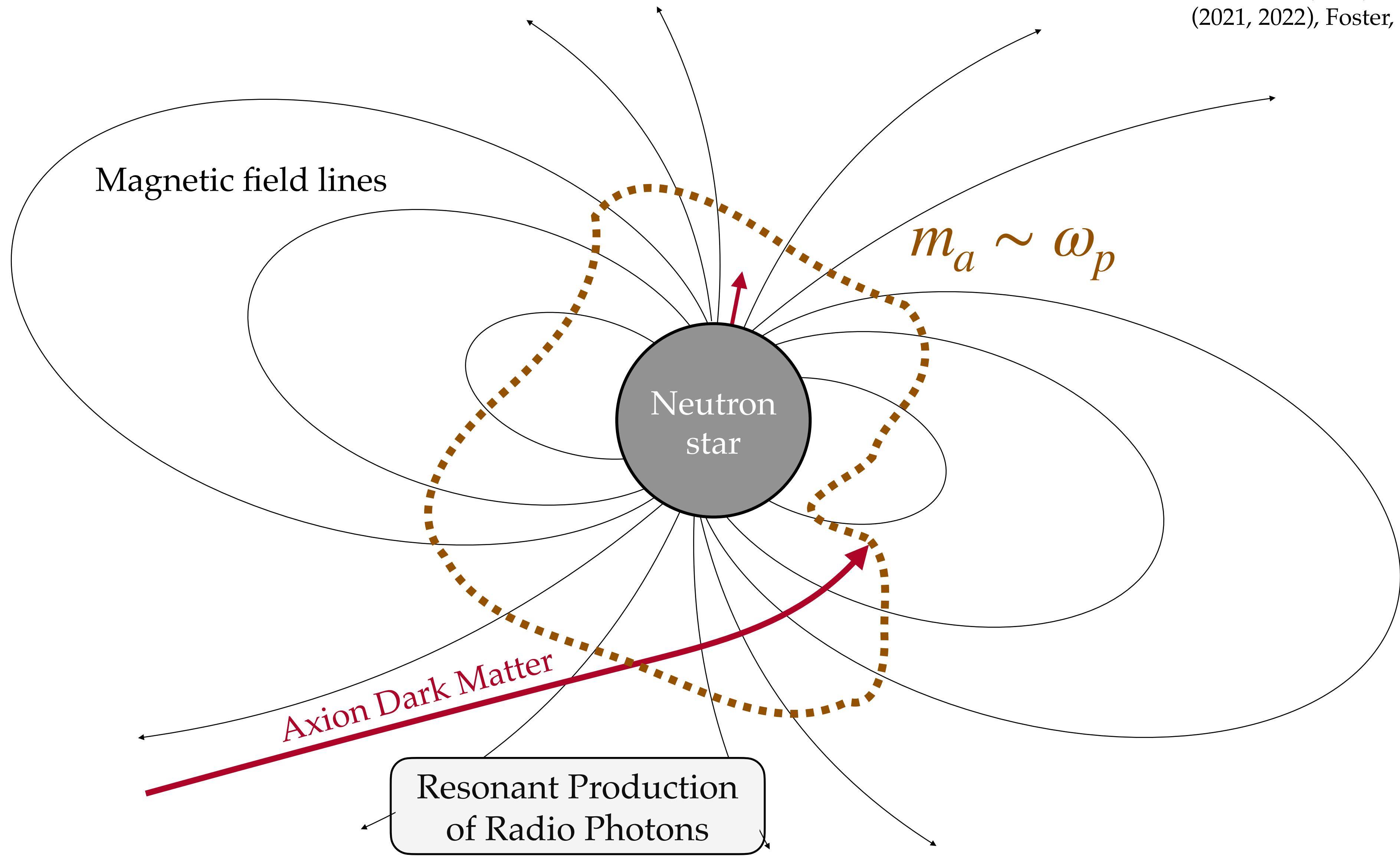
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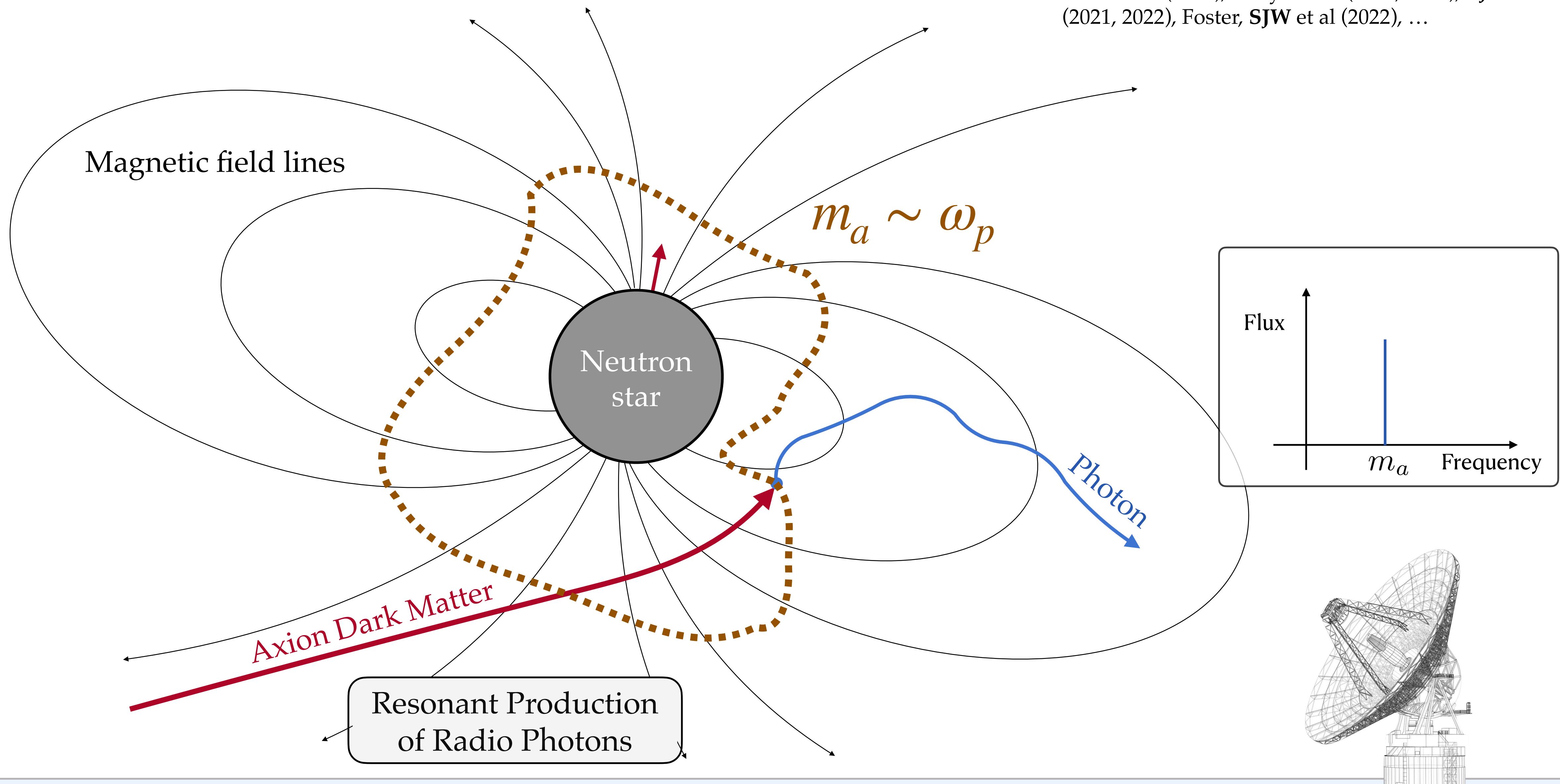
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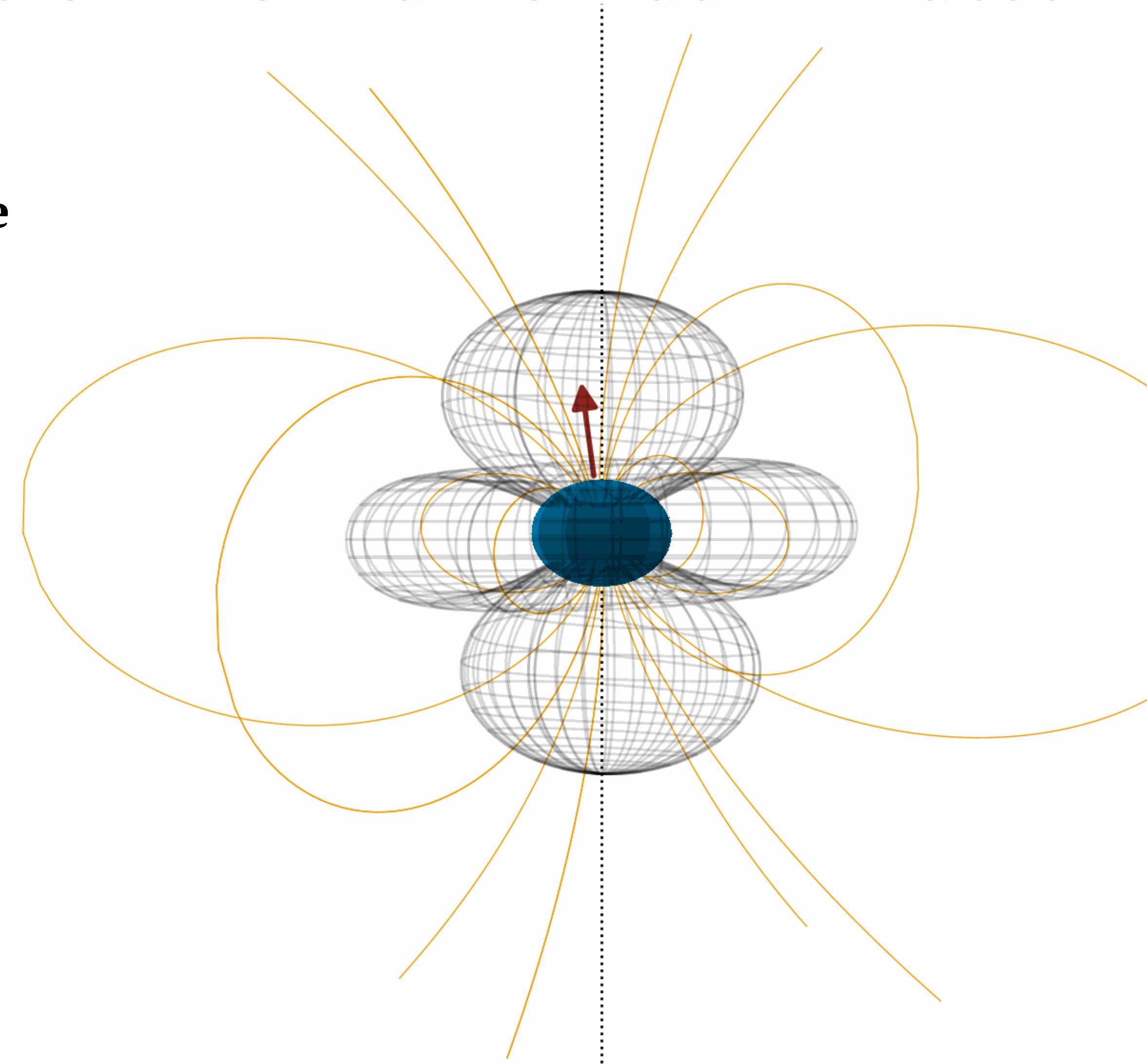
# Photon production from axion dark matter

**Step 1: Define plasma  
structure of magnetosphere**

## Resonant Conversion

Location:  $m_a \sim \omega_p$

Efficiency:  $(\partial\omega_p)^{-1}$



Animations available at: [https://github.com/SamWitte/GIF\\_Storage](https://github.com/SamWitte/GIF_Storage)

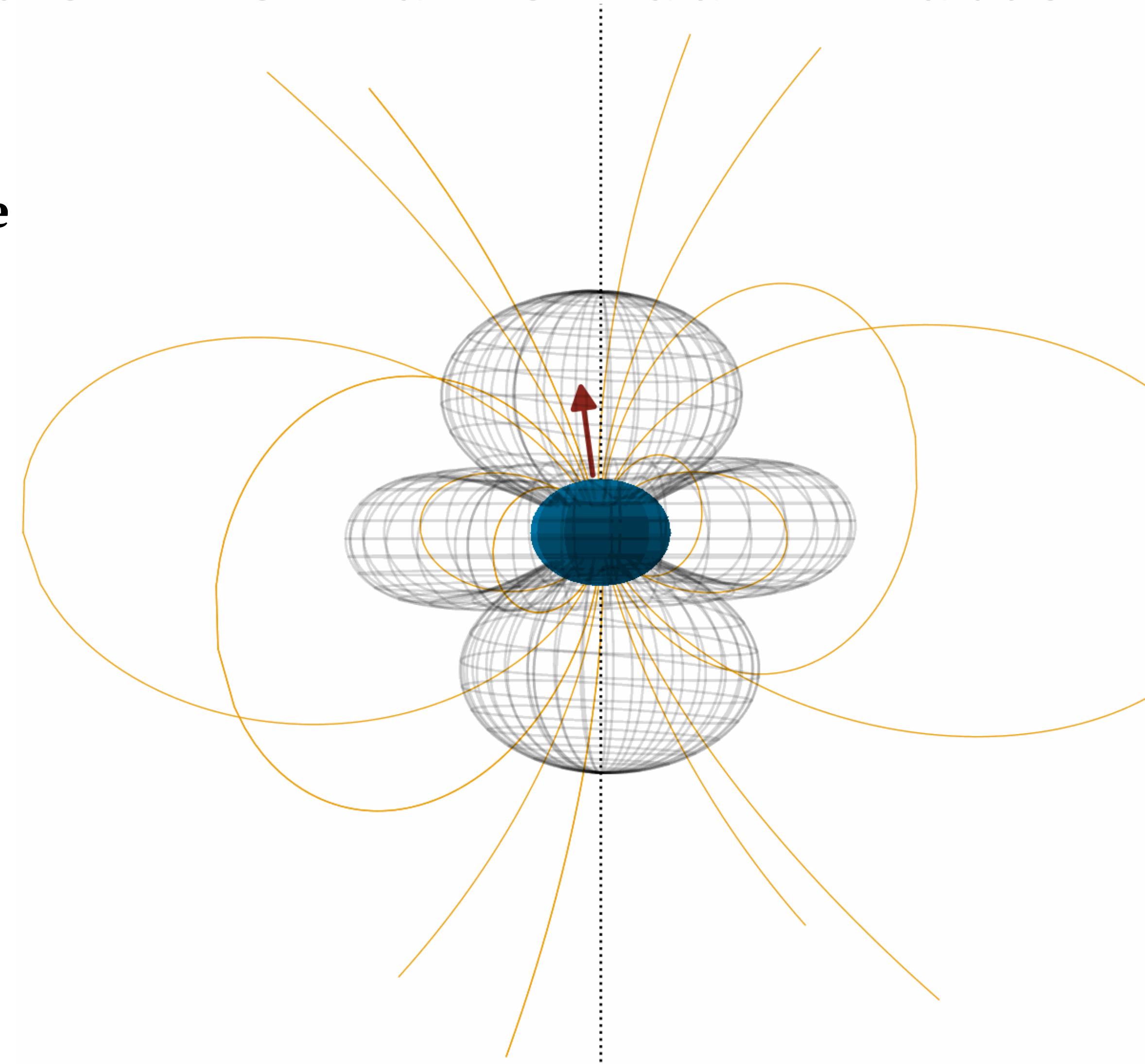
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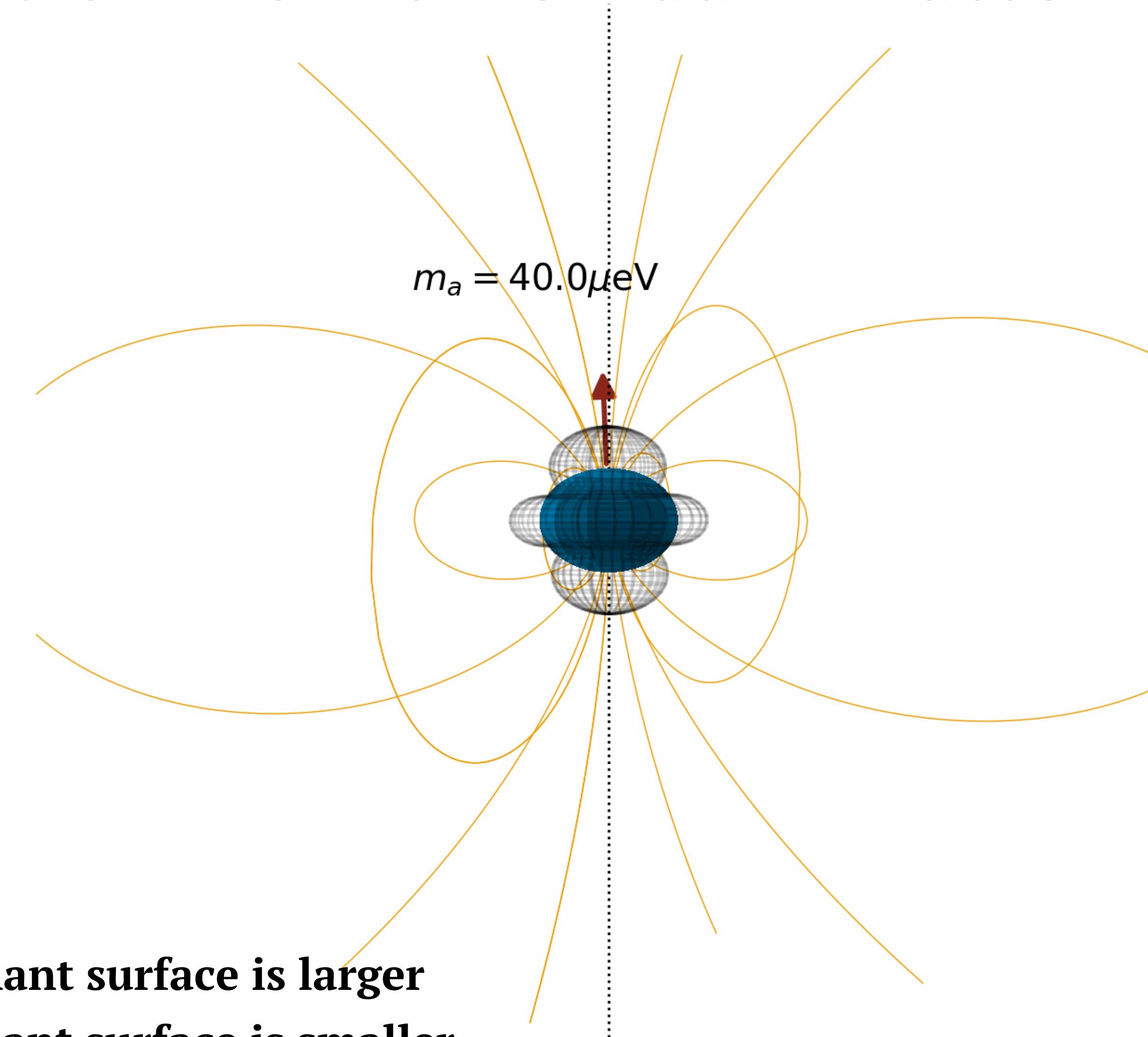
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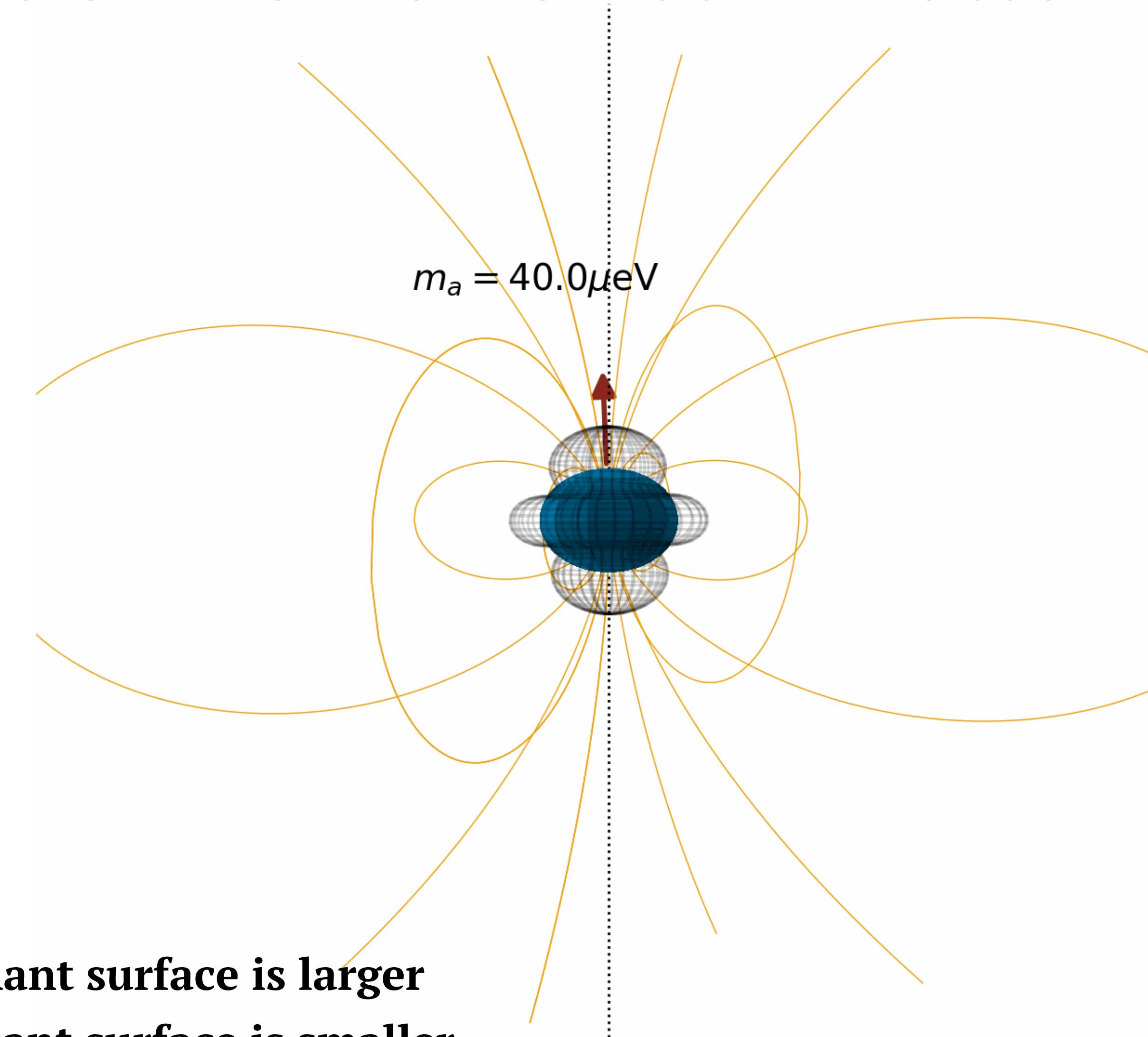


**Smaller axion mass → resonant surface is larger**

**Larger axion mass → resonant surface is smaller**

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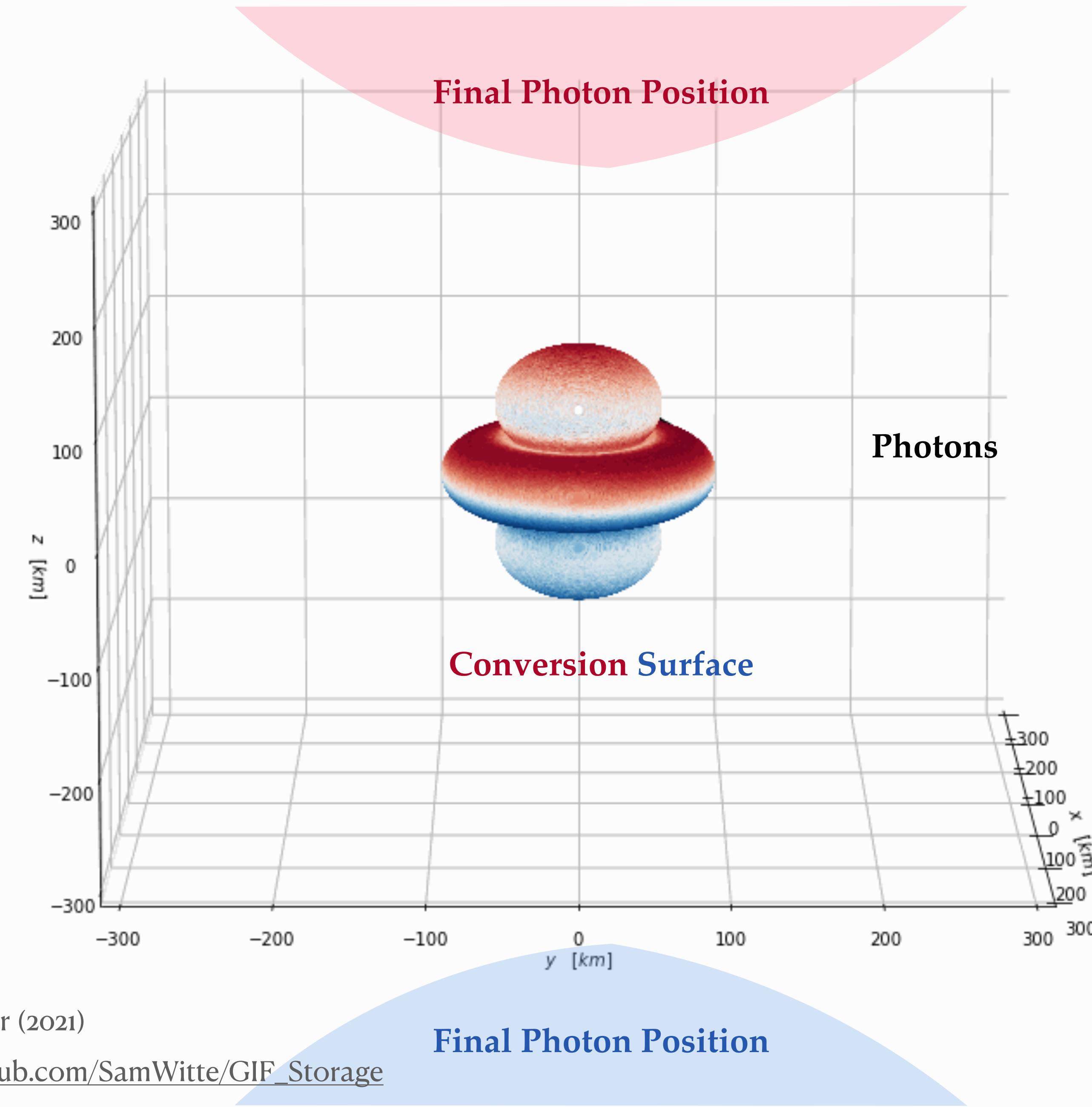
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# Ray tracing

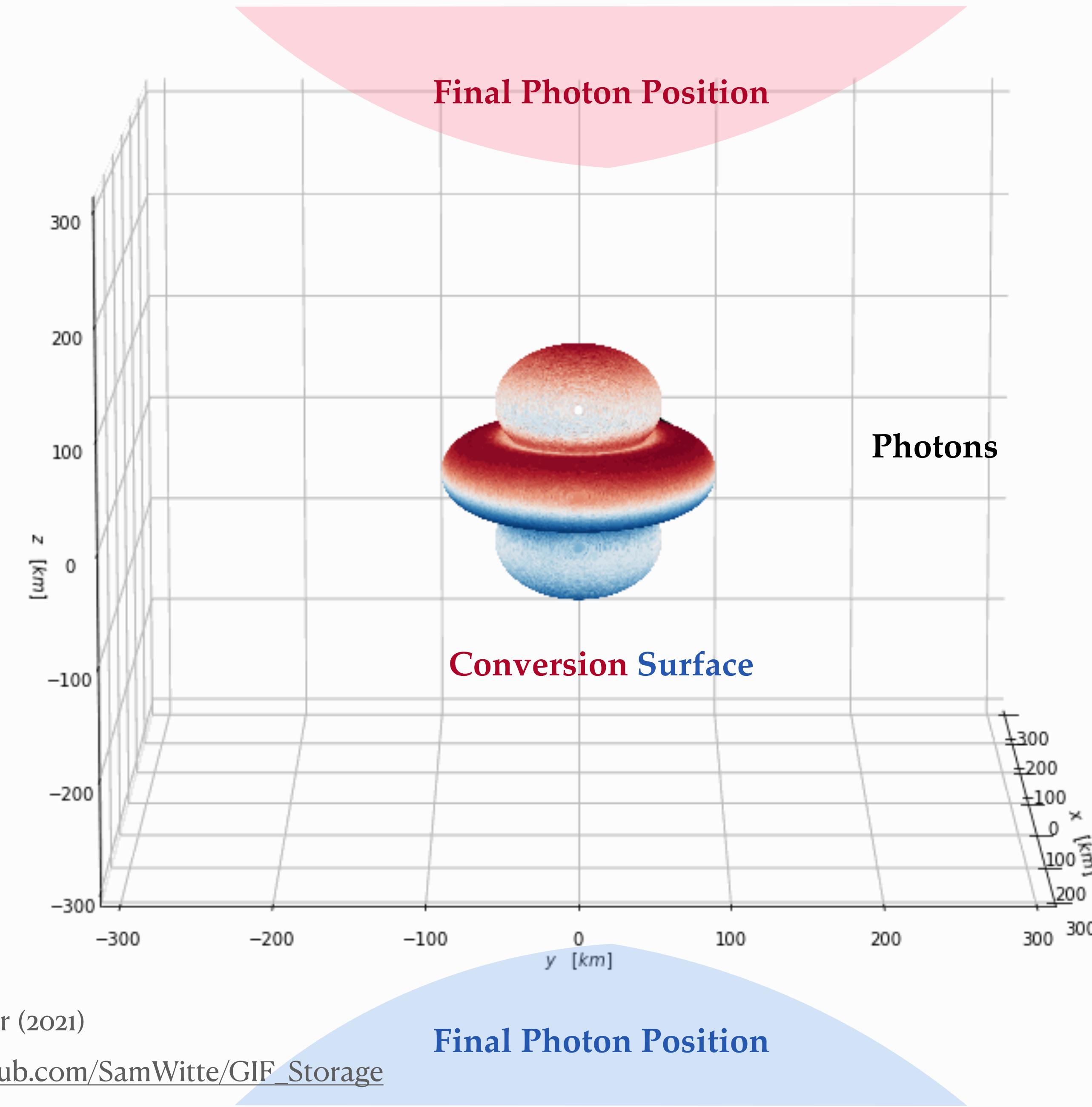
## Step 2: Axion phase space to photon flux



- Ray tracing allows for:**
- Accurate mapping of radio flux
  - Back-reaction on axion phase space
  - Line broadening effects
  - Path-dependent absorption

# Ray tracing

## Step 2: Axion phase space to photon flux

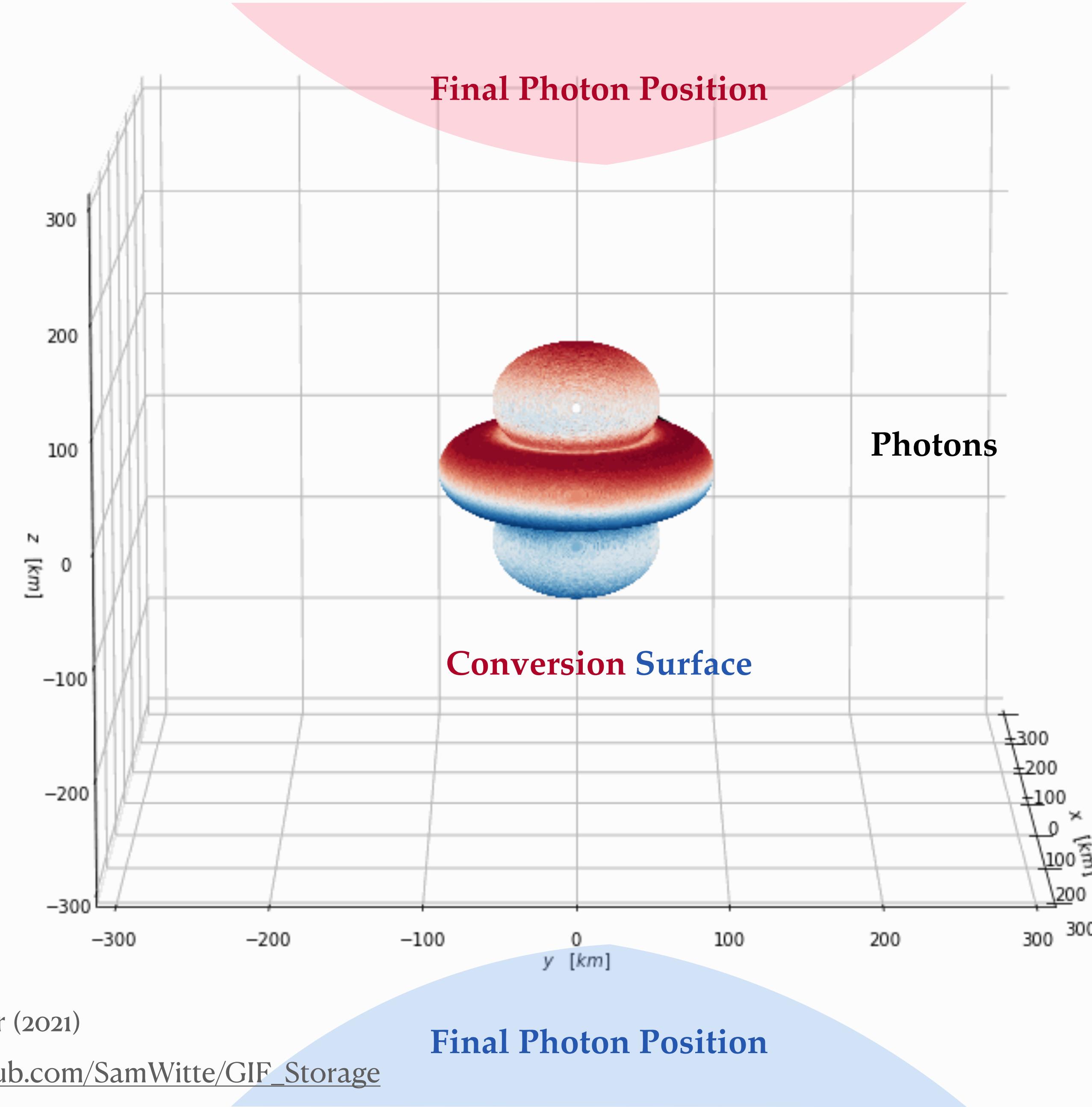


**Ray tracing allows for:**

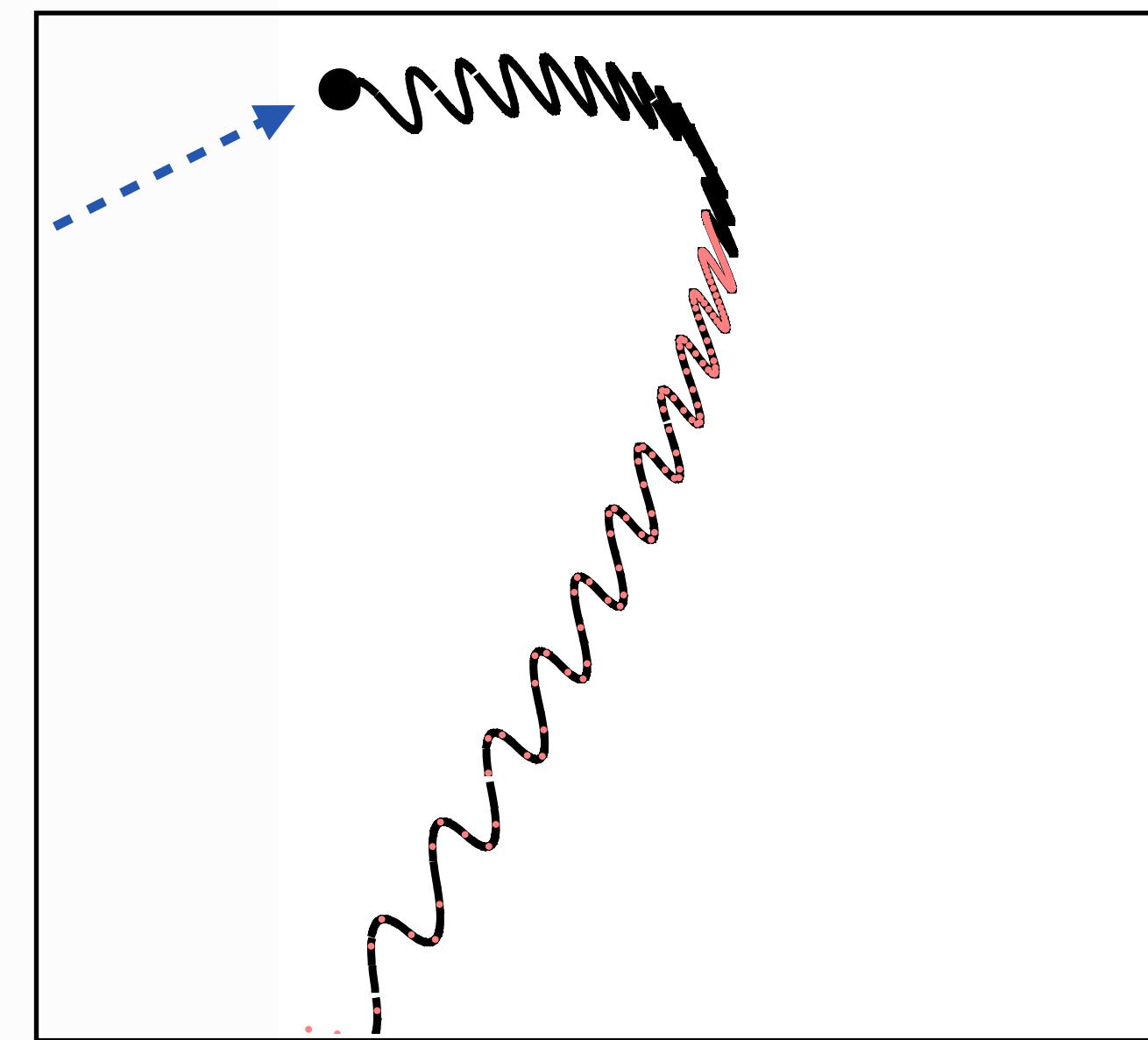
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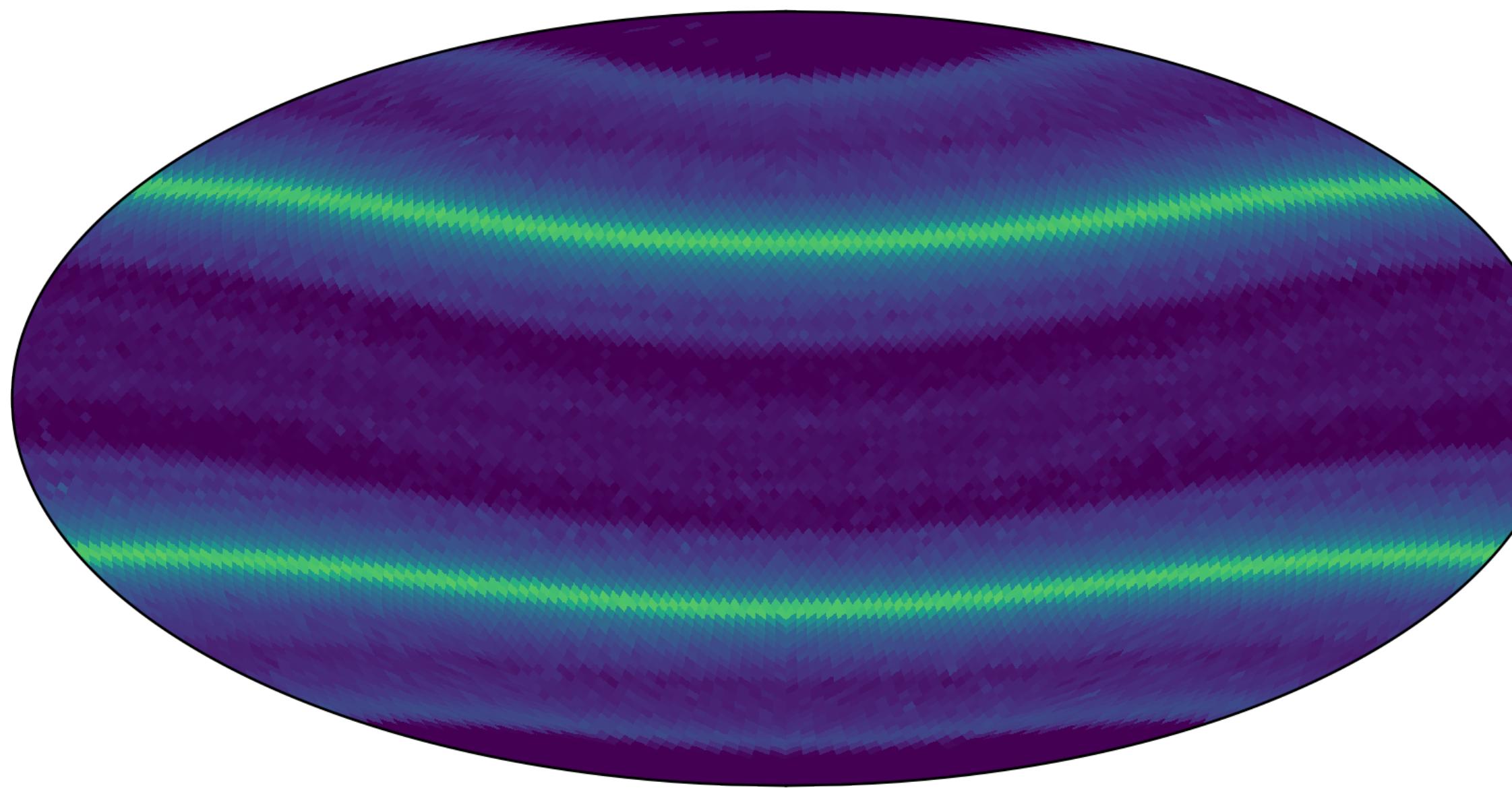
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~ 500 meters

# Radio signal from isolated neutron star

*Projected sky flux as viewed from neutron star*



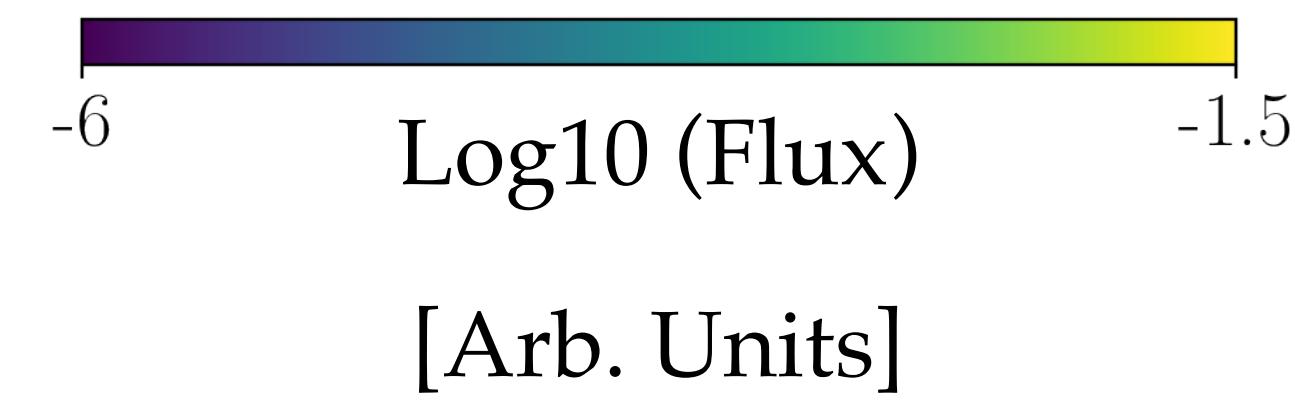
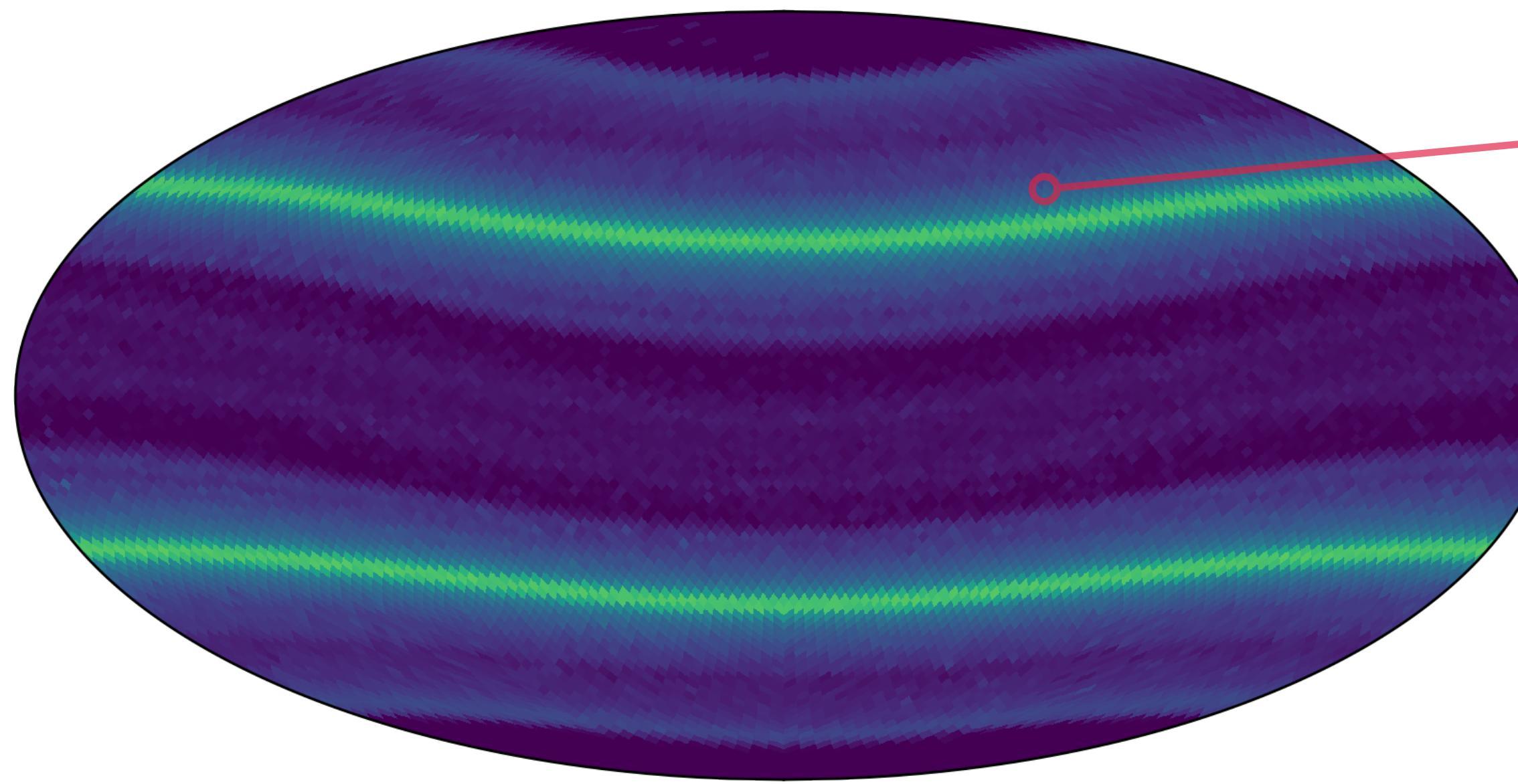
-6                    -1.5  
Log10 (Flux)

[Arb. Units]

SJW, Noordhuis, Edwards, Weniger (2021)

# Radio signal from isolated neutron star

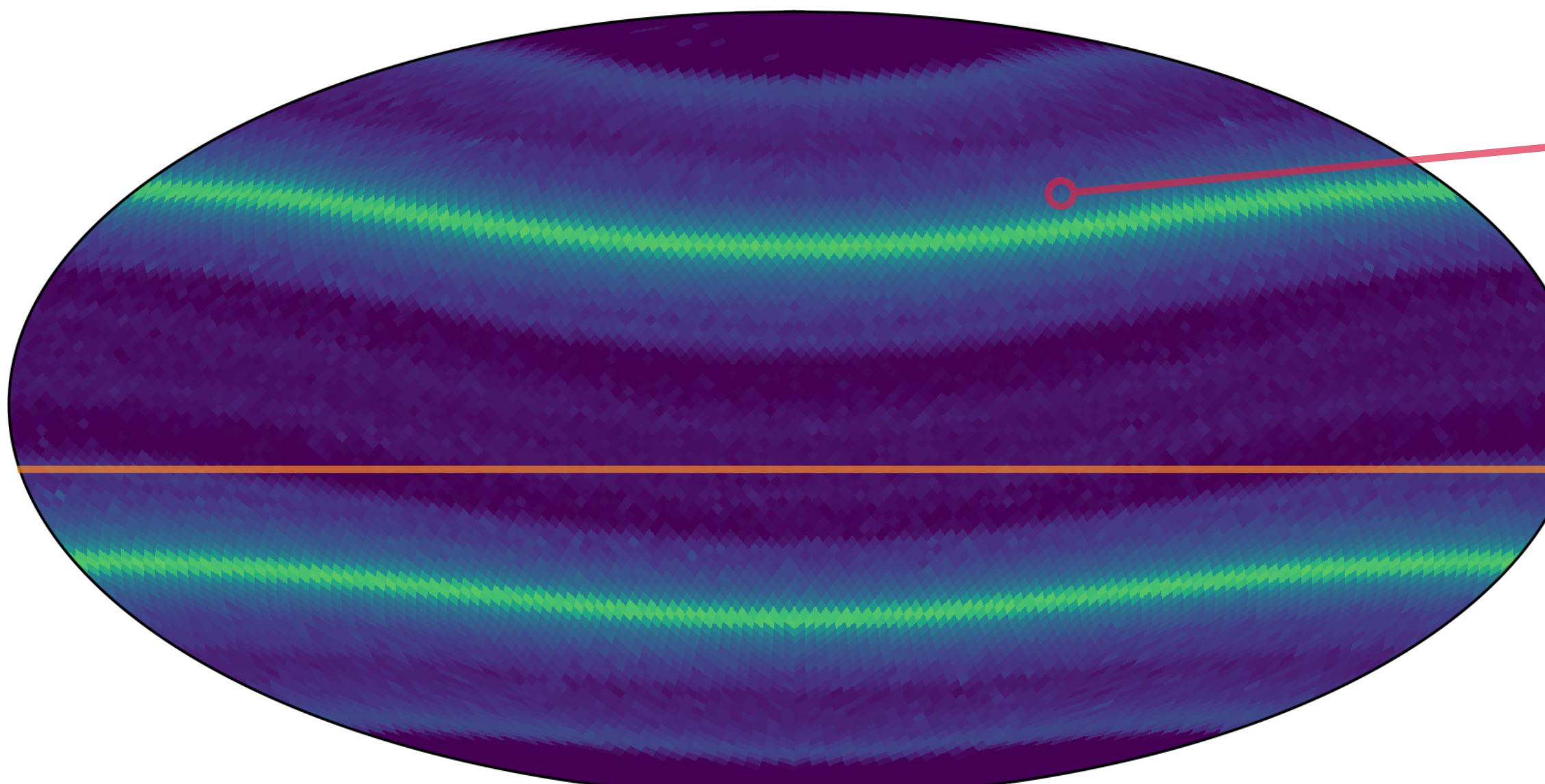
*Projected sky flux as viewed from neutron star*



SJW, Noordhuis, Edwards, Weniger (2021)

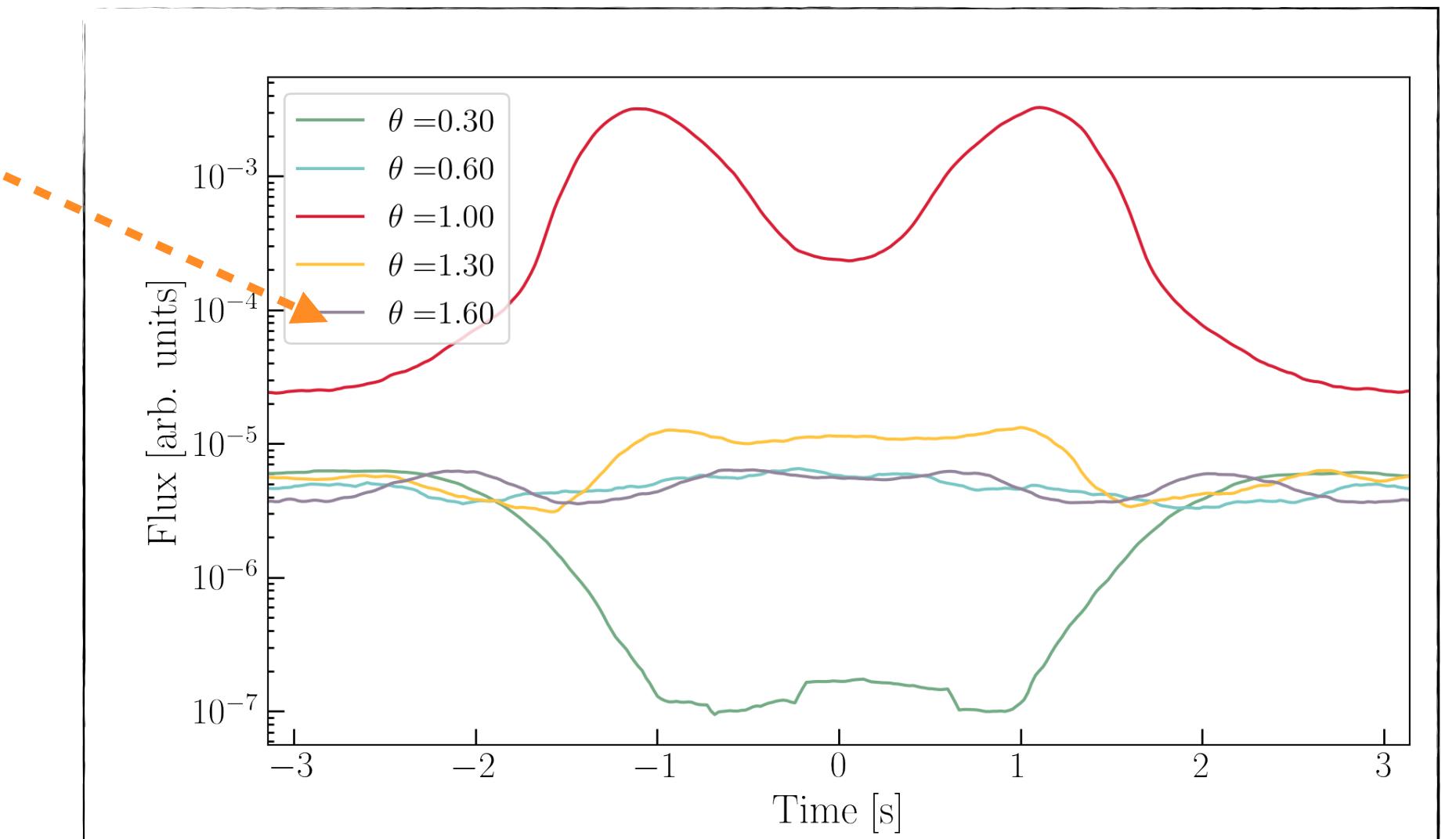
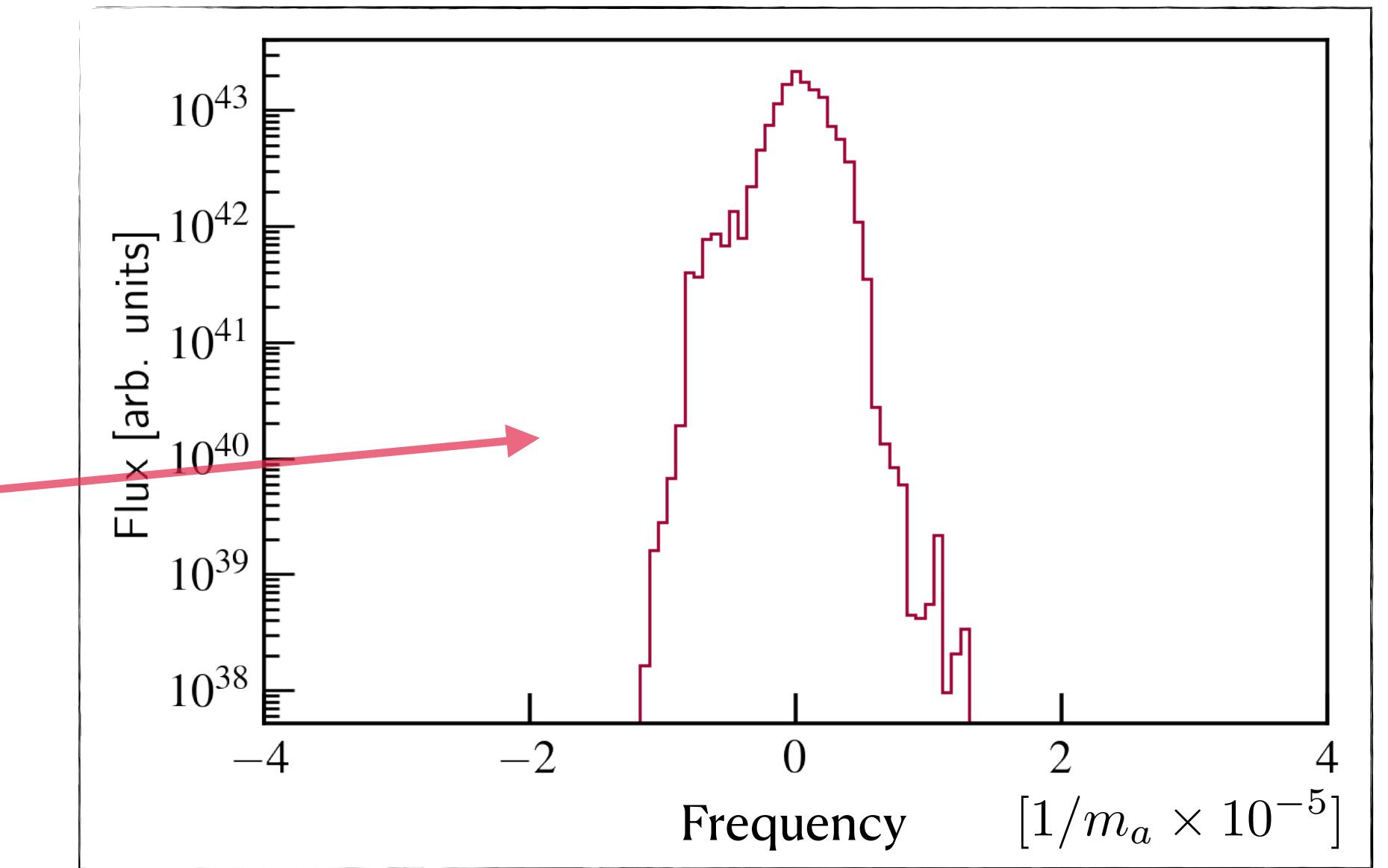
# Radio signal from isolated neutron star

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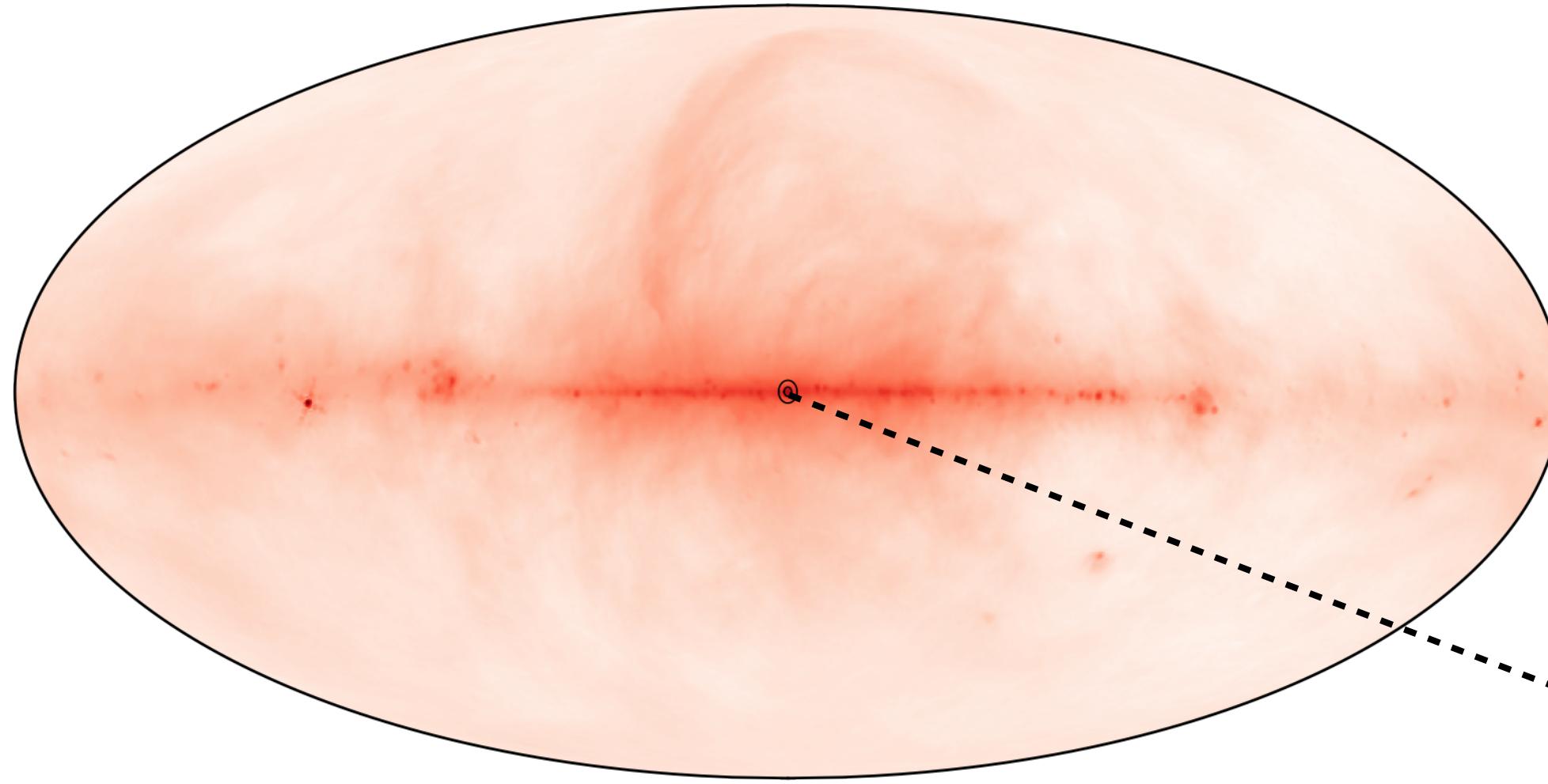


Log10 (Flux)  
[Arb. Units]

SJW, Noordhuis, Edwards, Weniger (2021)

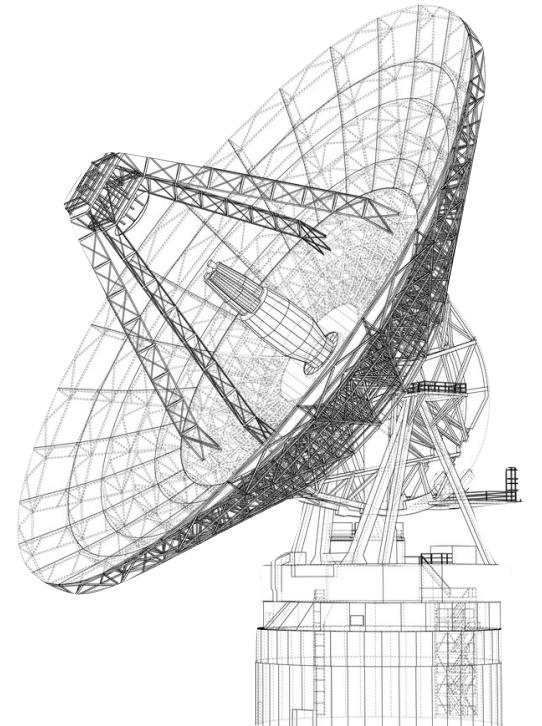


# Observing the galactic center with the Green Bank Telescope



## Survey Details:

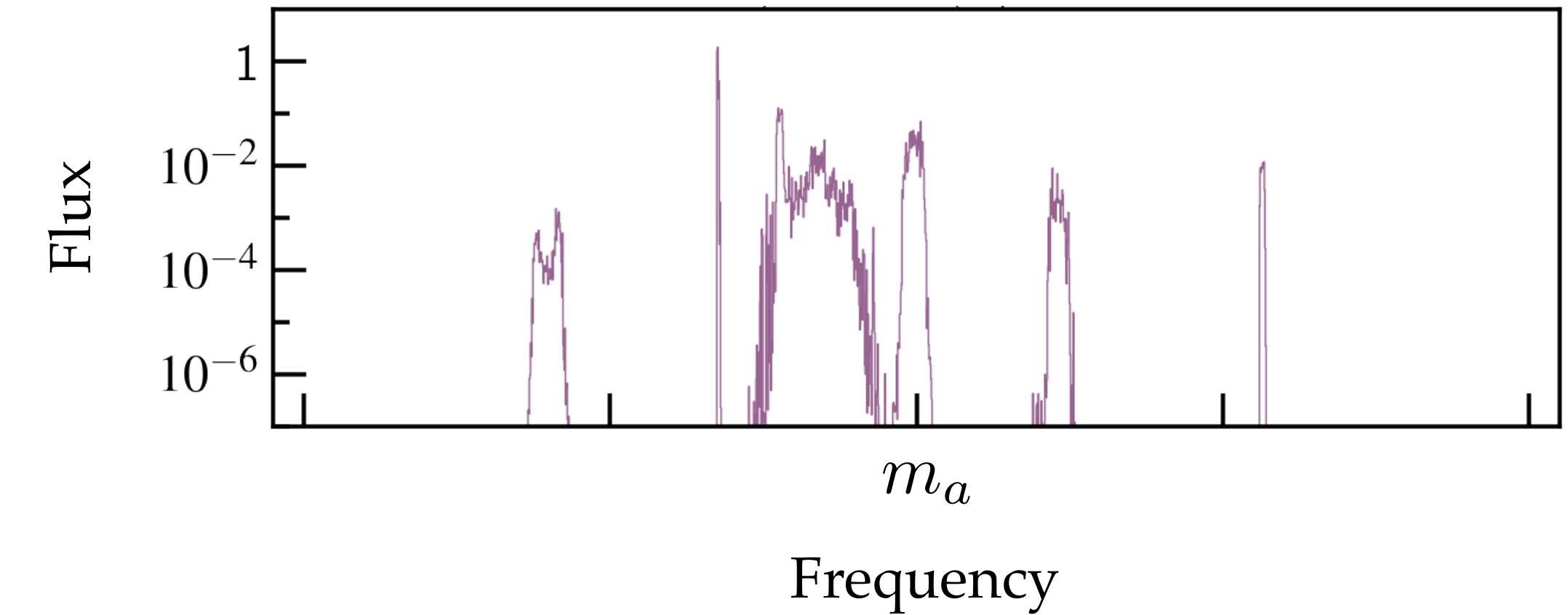
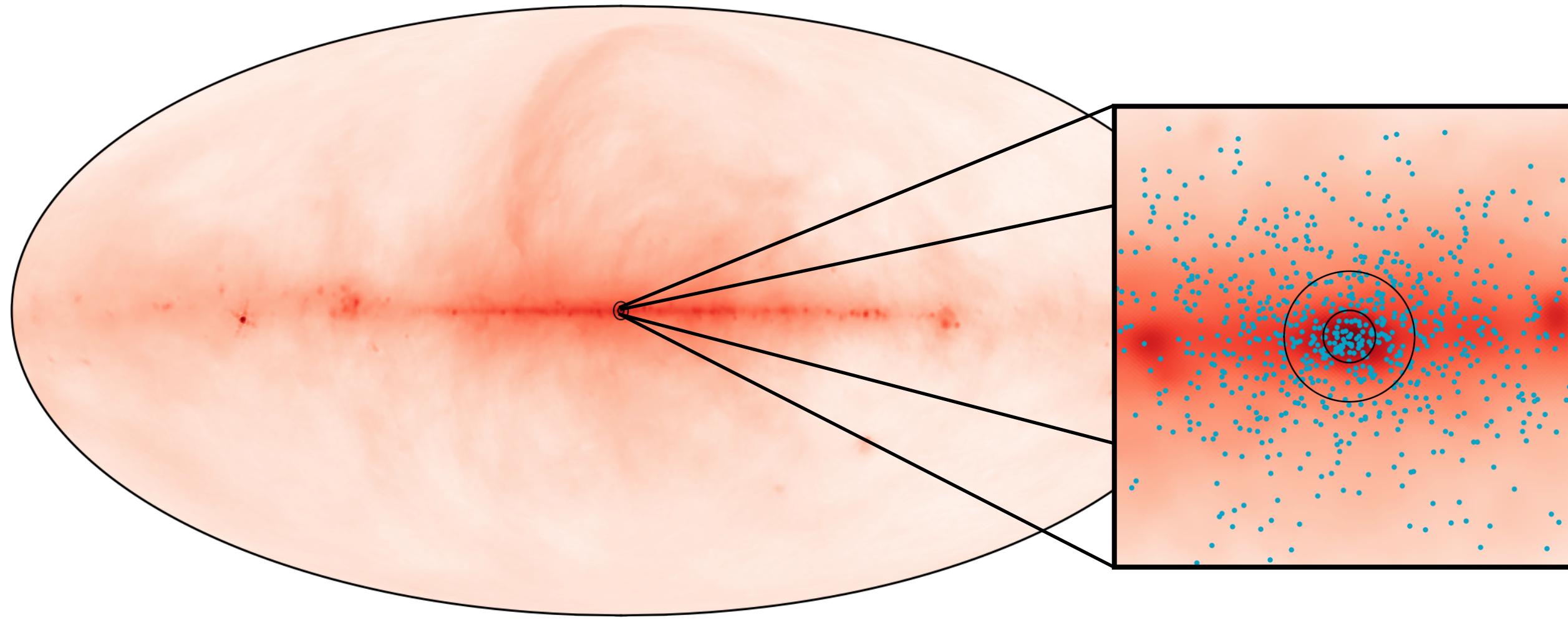
- **Telescope:** Green Bank Telescope, 100m Single Dish
- **Observation Frequency:** 4–8 GHz [C band]
- **Observation Target:** Milky Way Galactic Center [inner ~ few pcs]  
*(need high dark matter densities)*
- **Observation Time:** ~4.6 hours
- **Observation Strategy:** On/off target



*Data courtesy of the Breakthrough Listen Initiative*

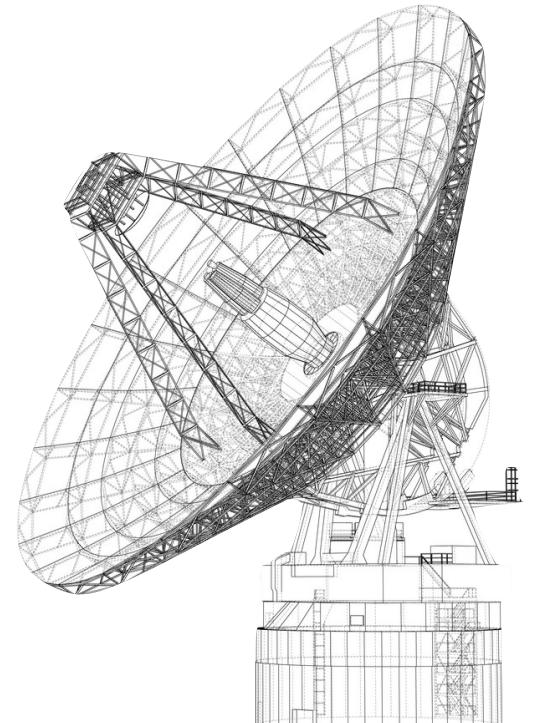
Foster, SJW, Lawson, Linden, Gajjar, Weniger, Safdi (2022)

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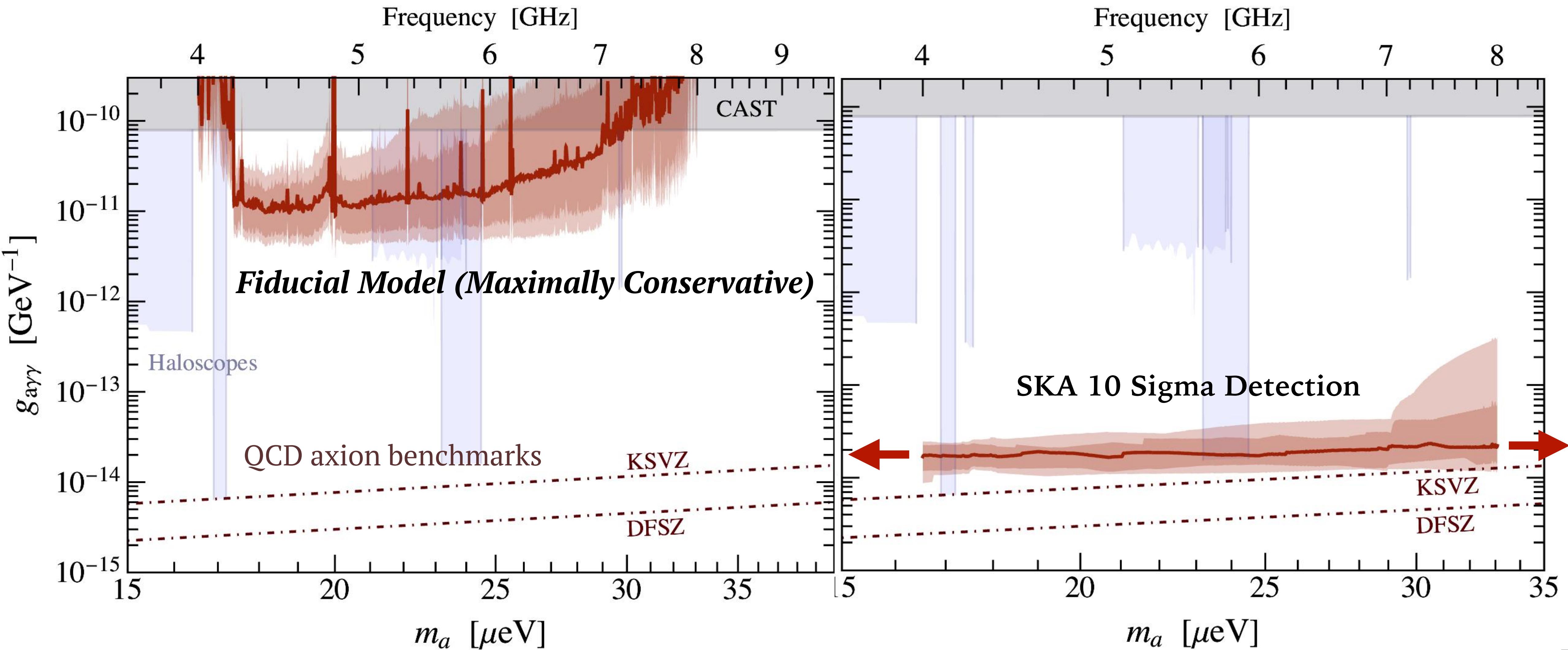
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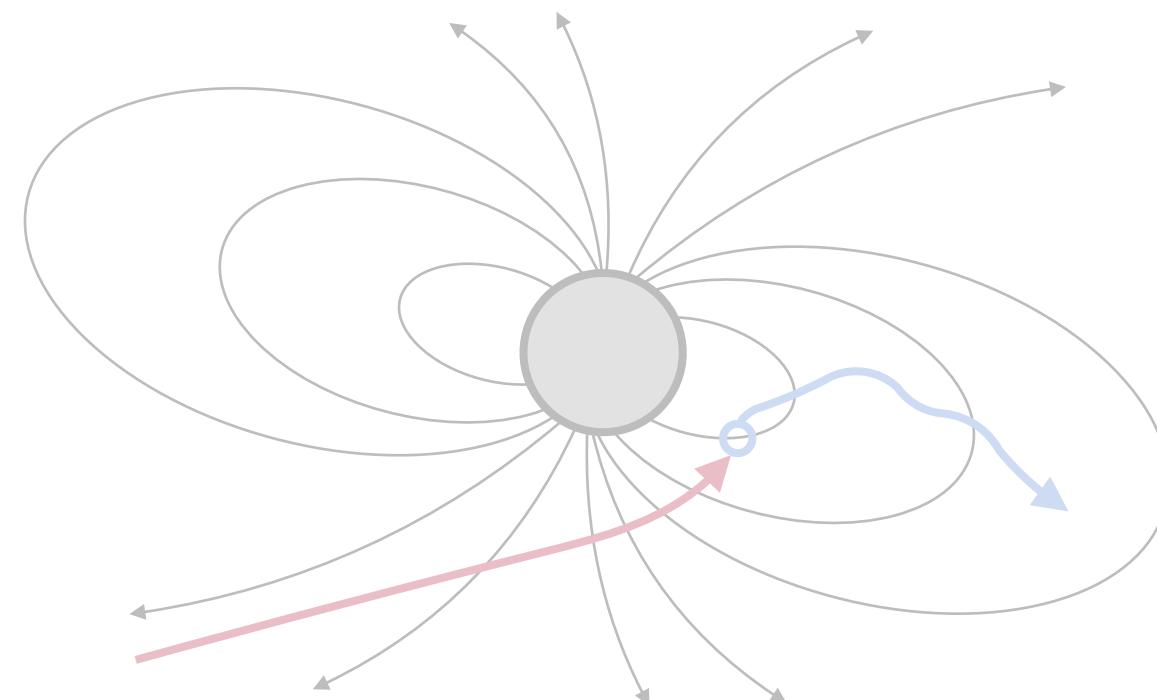
Data courtesy of the Breakthrough Listen Initiative

Foster, SJW, Lawson, Linden, Gajjar, Weniger, Safdi (2022)

# Searching for axions in the galactic center

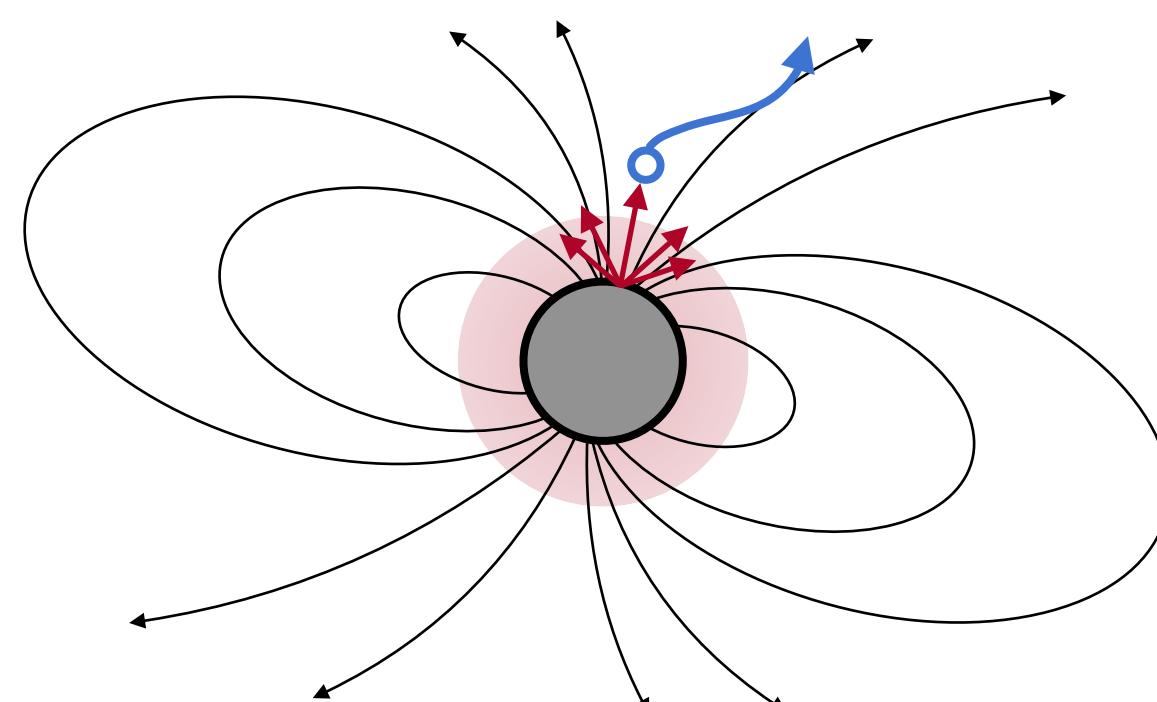


# Neutron stars as axion labs



## Part 1: Resonant production of radio photons from axion dark matter

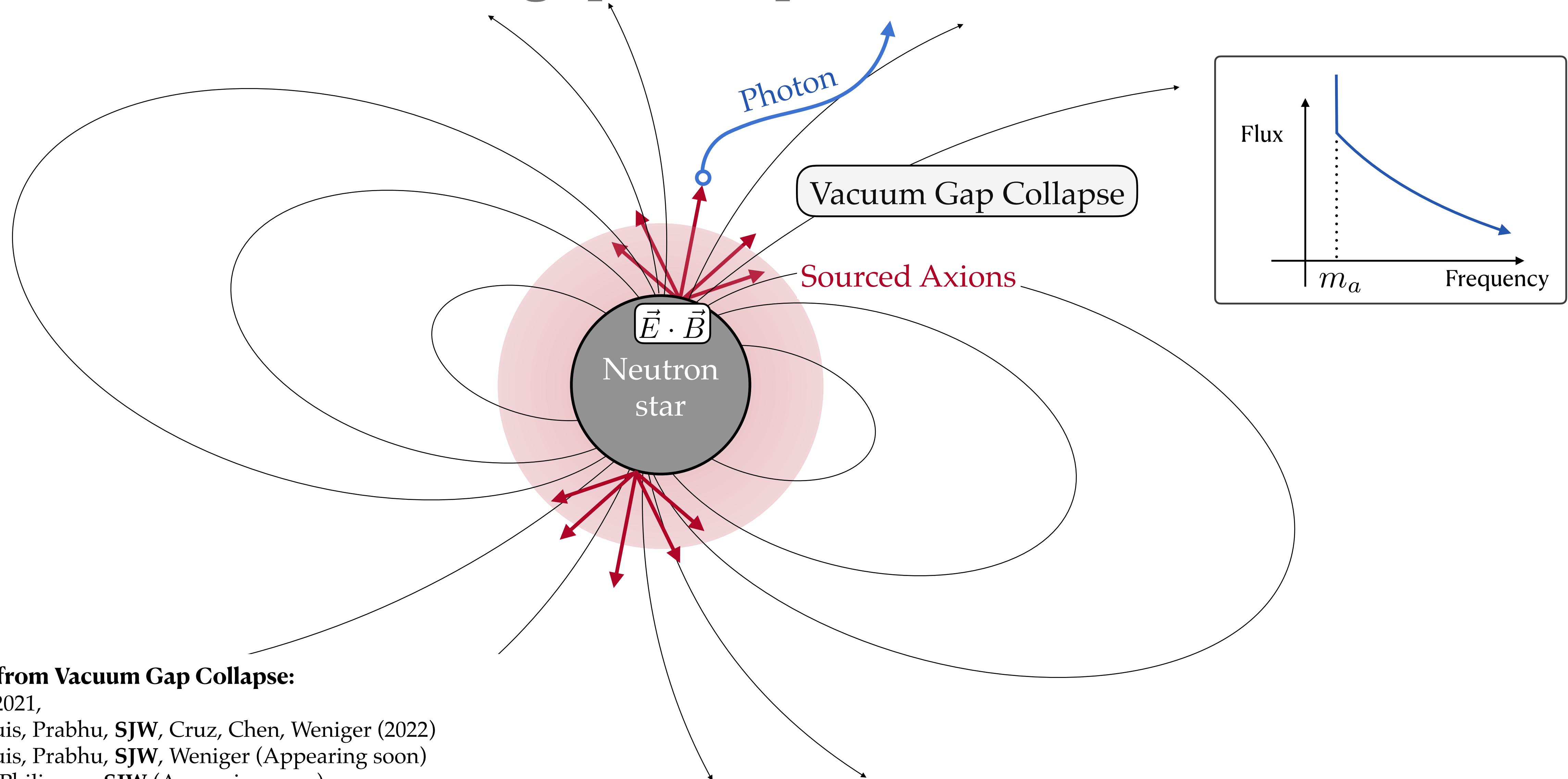
See e.g.: Pshirkov & Popov (2009), Hook et al. (2018), Safdi et al. (2018), Battye et al. (2019, 2021), SJW et al. (2021, 2022), Foster, SJW et al (2022), Thejmsland, McDonald, SJW (To appear), SJW et al (To appear), McDonald & SJW (To appear),...



## Part 2: Sourcing axions from the vacuum gap collapse

Prabhu (2021), Noordhuis, Prabhu, SJW, Cruz, Chen, Weniger (2022), Noordhuis, Prabhu, SJW, Weniger (Appearing soon), Caputo, Philippov, SJW (Appearing soon)

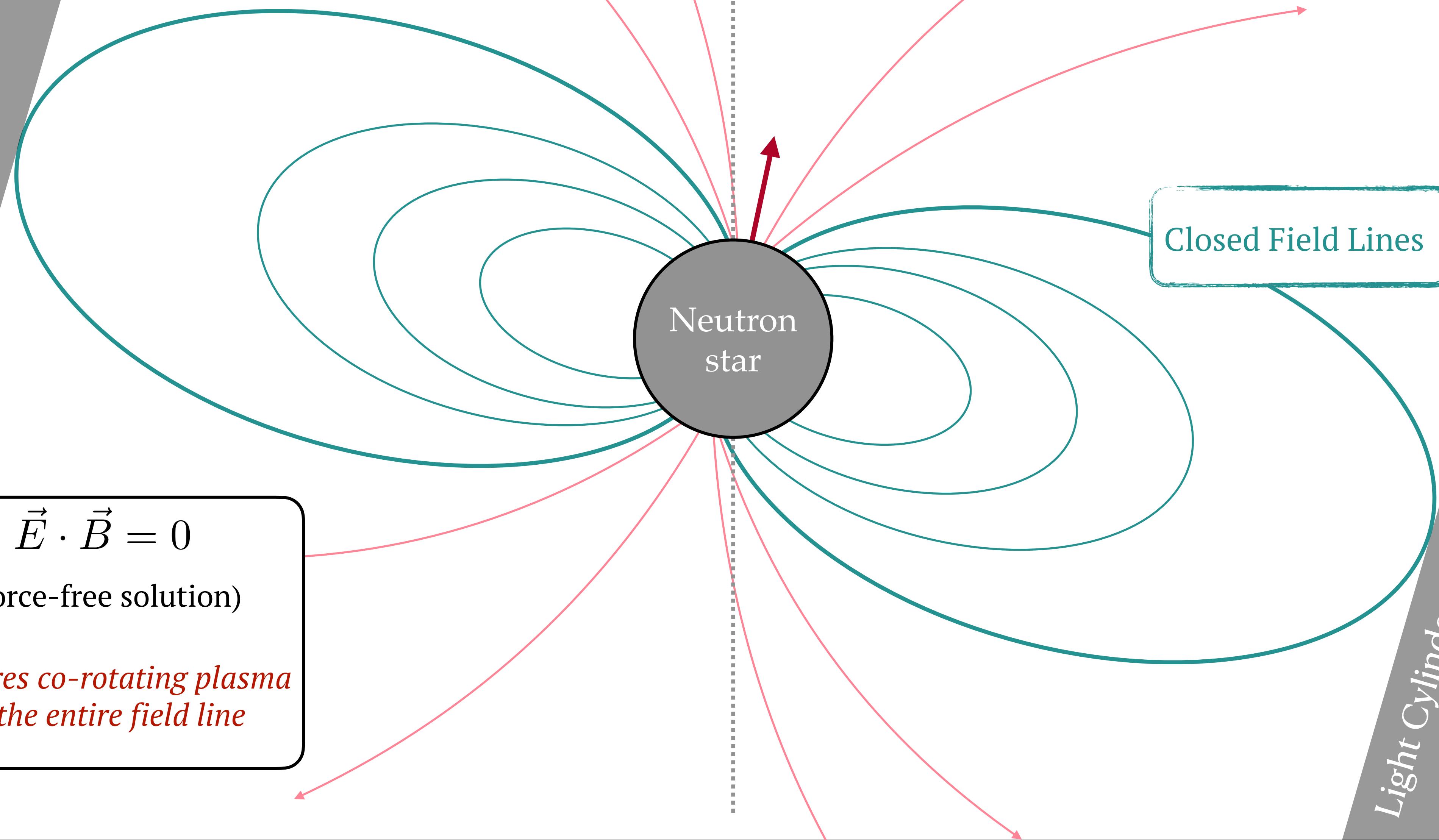
# Axions from vacuum gap collapse



$$\vec{E} \cdot \vec{B} = 0$$

(Force-free solution)

*Requires co-rotating plasma  
along the entire field line*



Open Field Lines

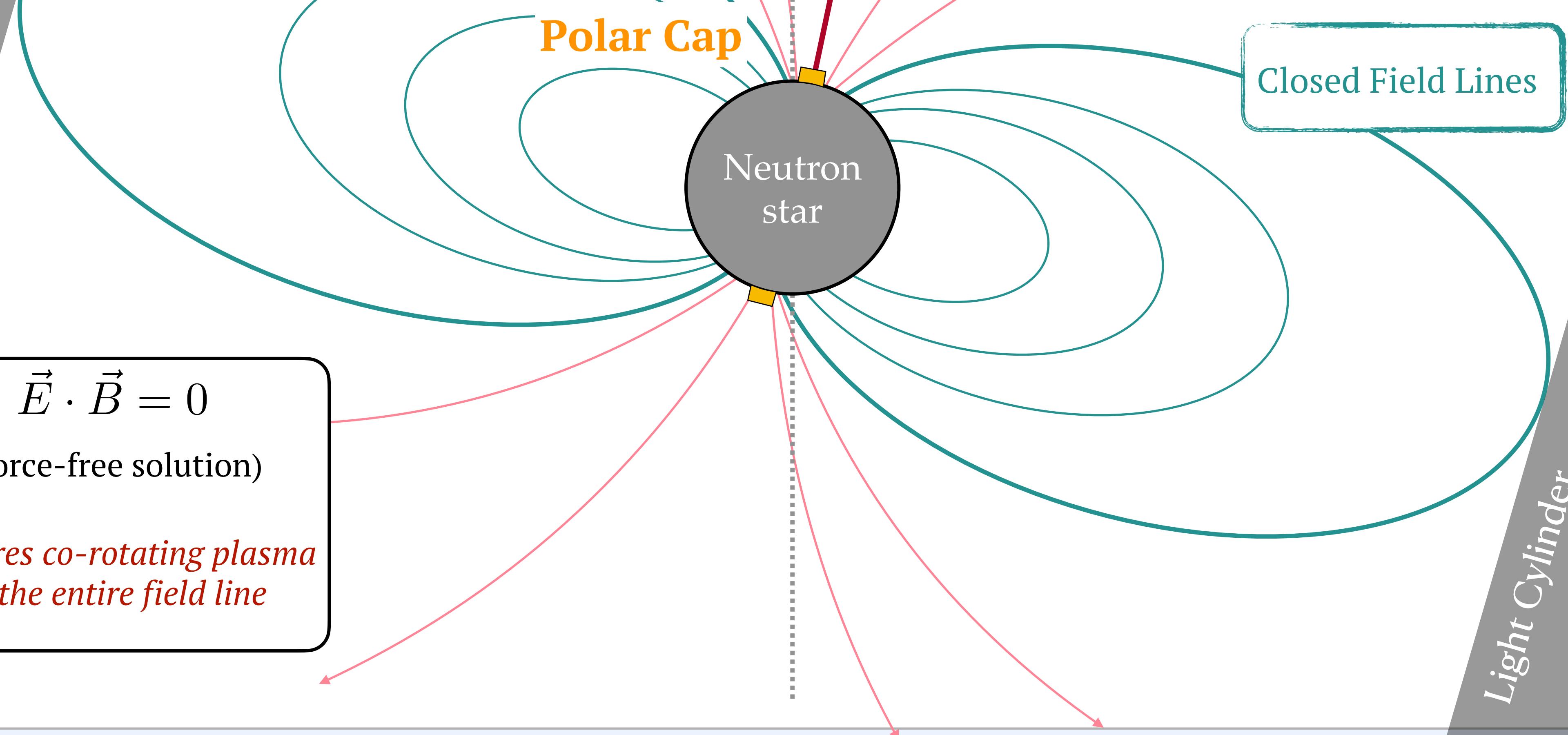
Closed Field Lines

Light Cylinder

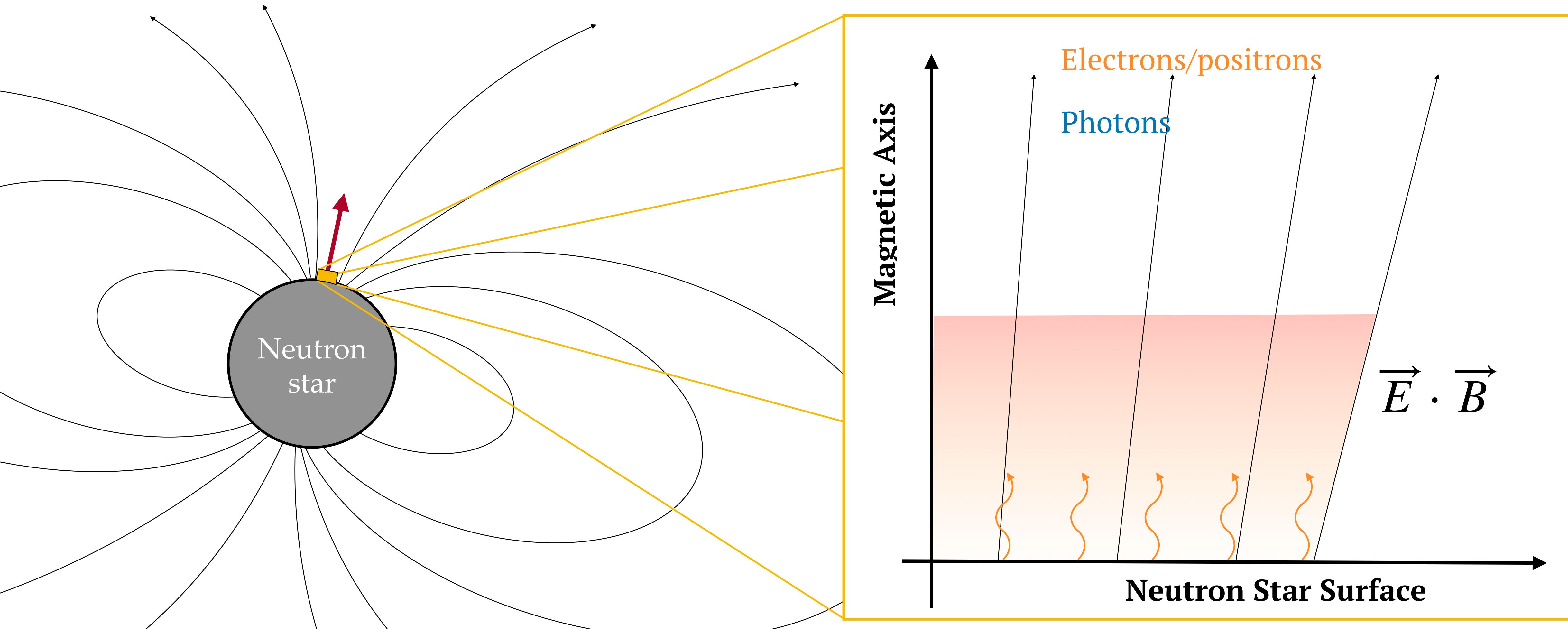
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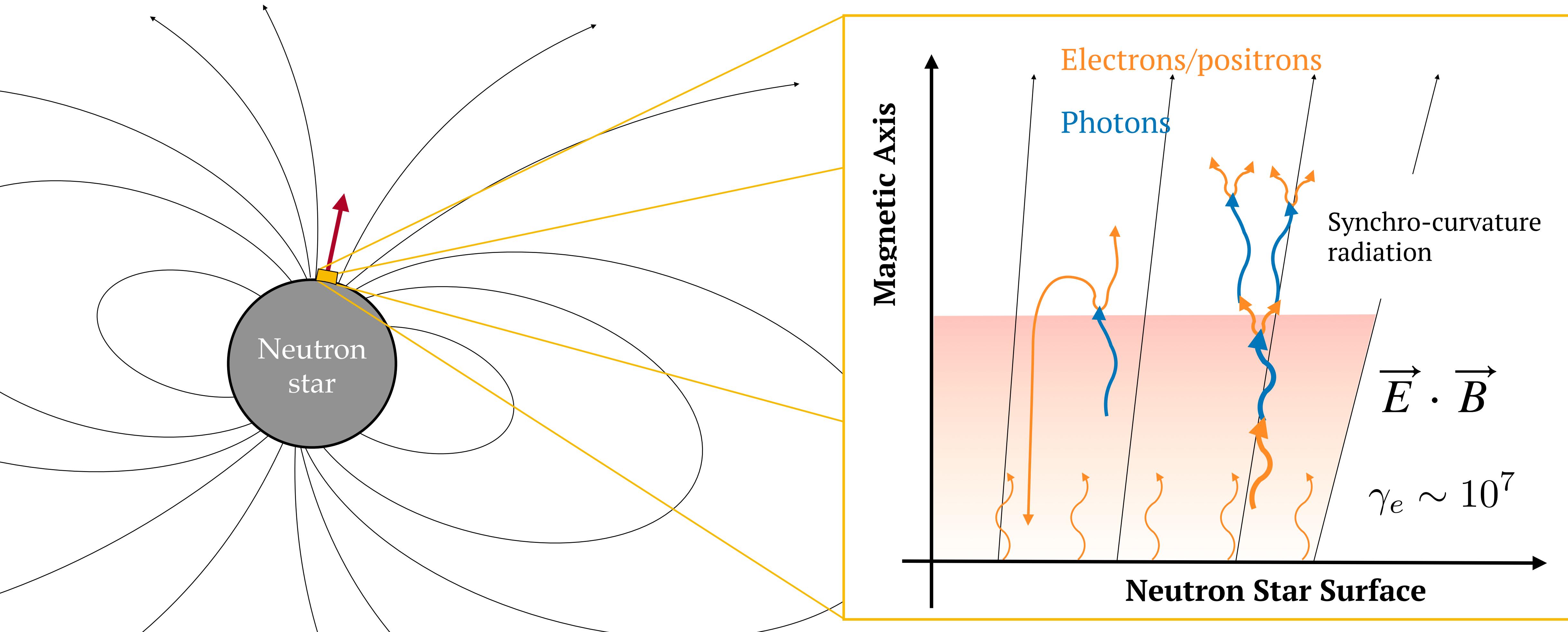
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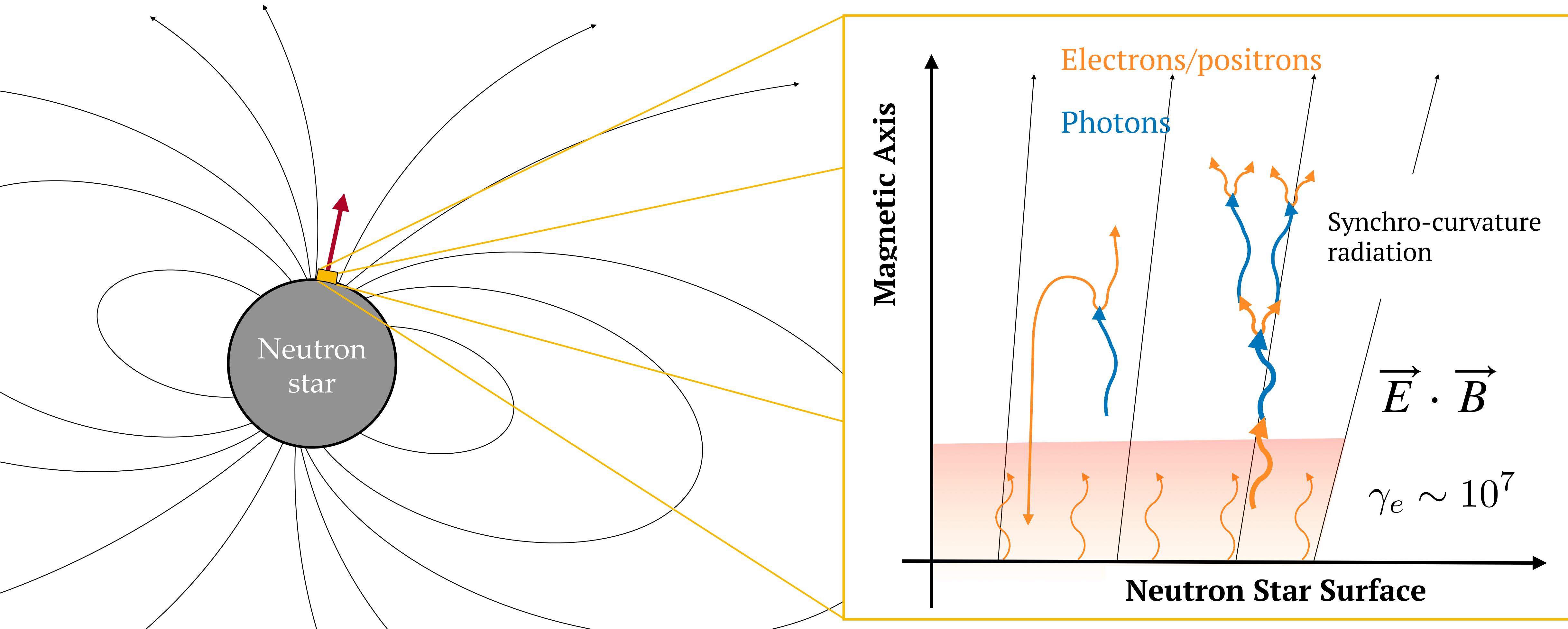
# Axions from vacuum gap collapse



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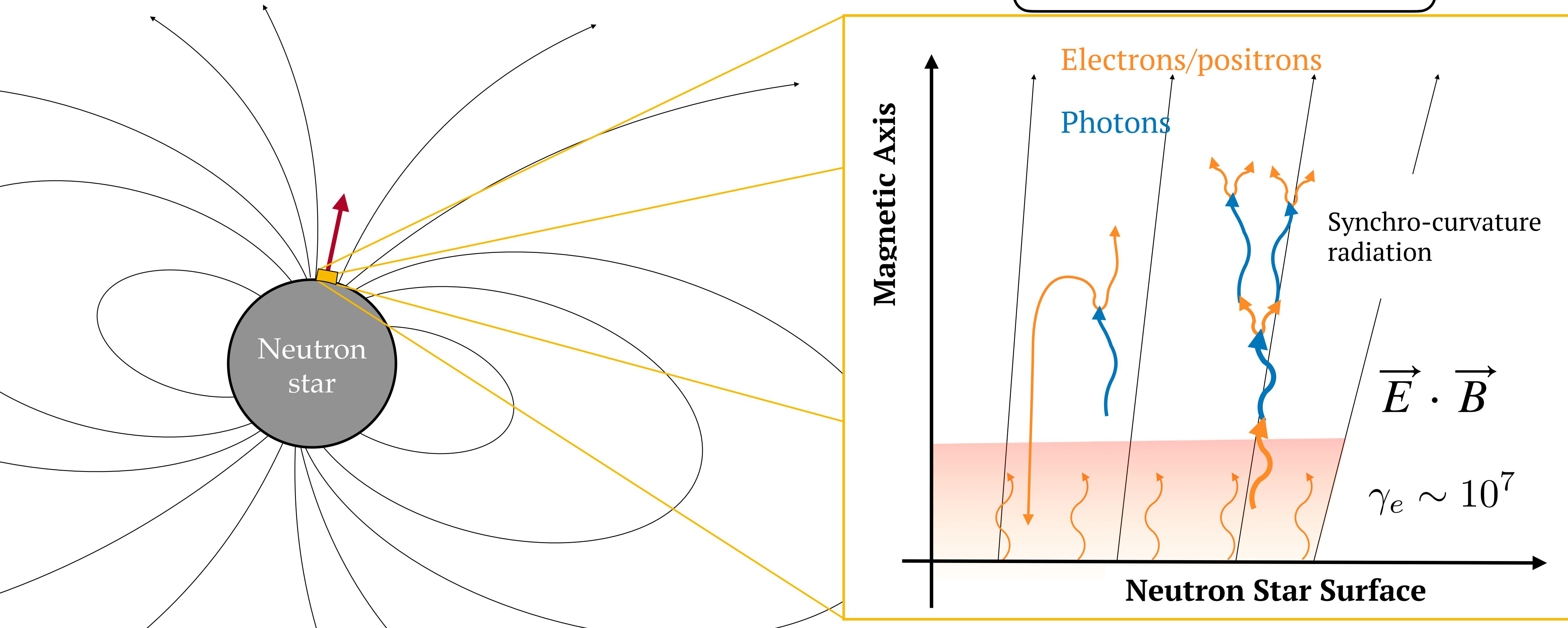
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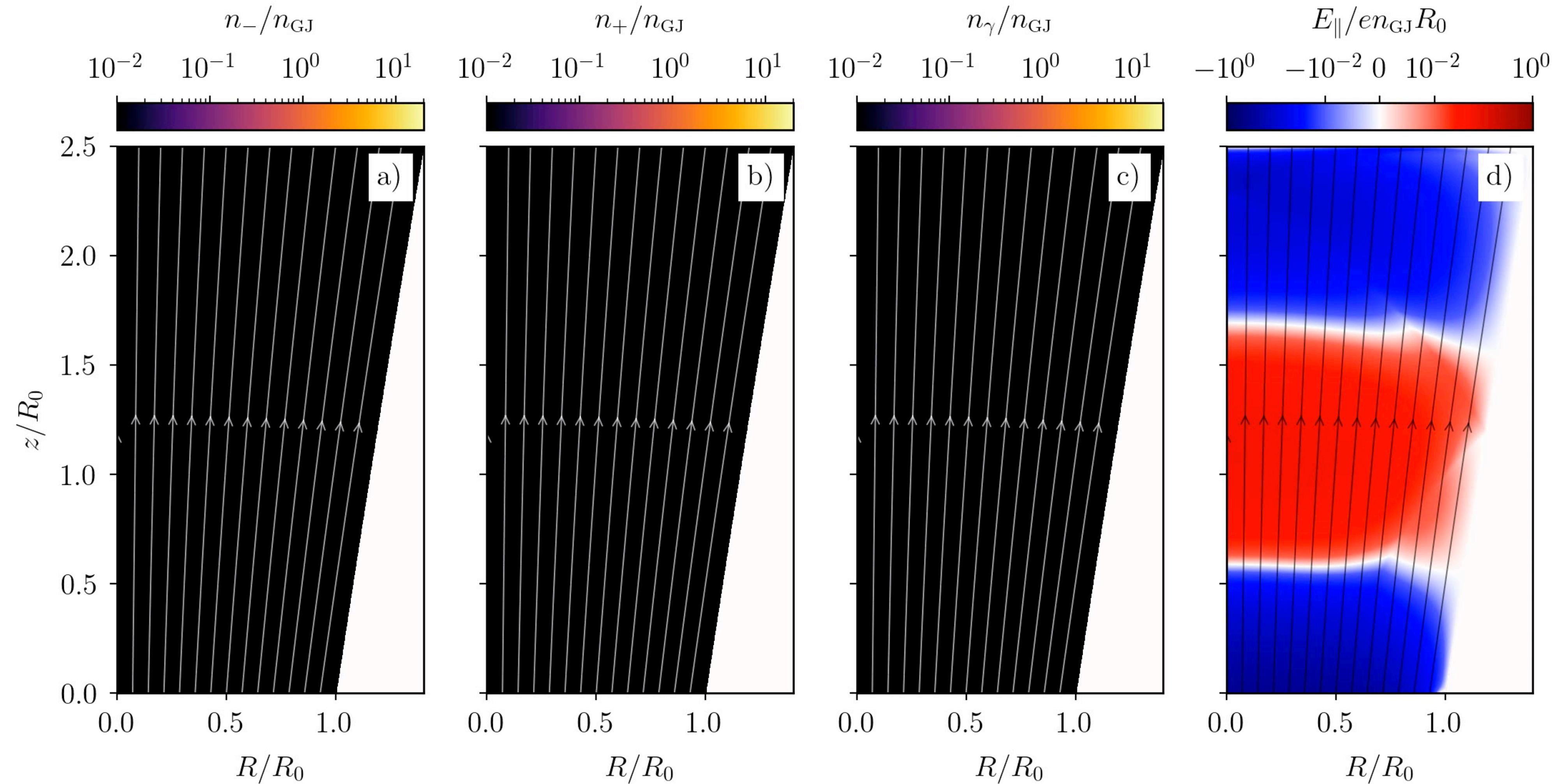
Axion spectra

$$\dot{N}_a(\vec{k}) \propto |FT(g_{a\gamma\gamma} \vec{E} \cdot \vec{B})|^2$$



# Vacuum gap collapse

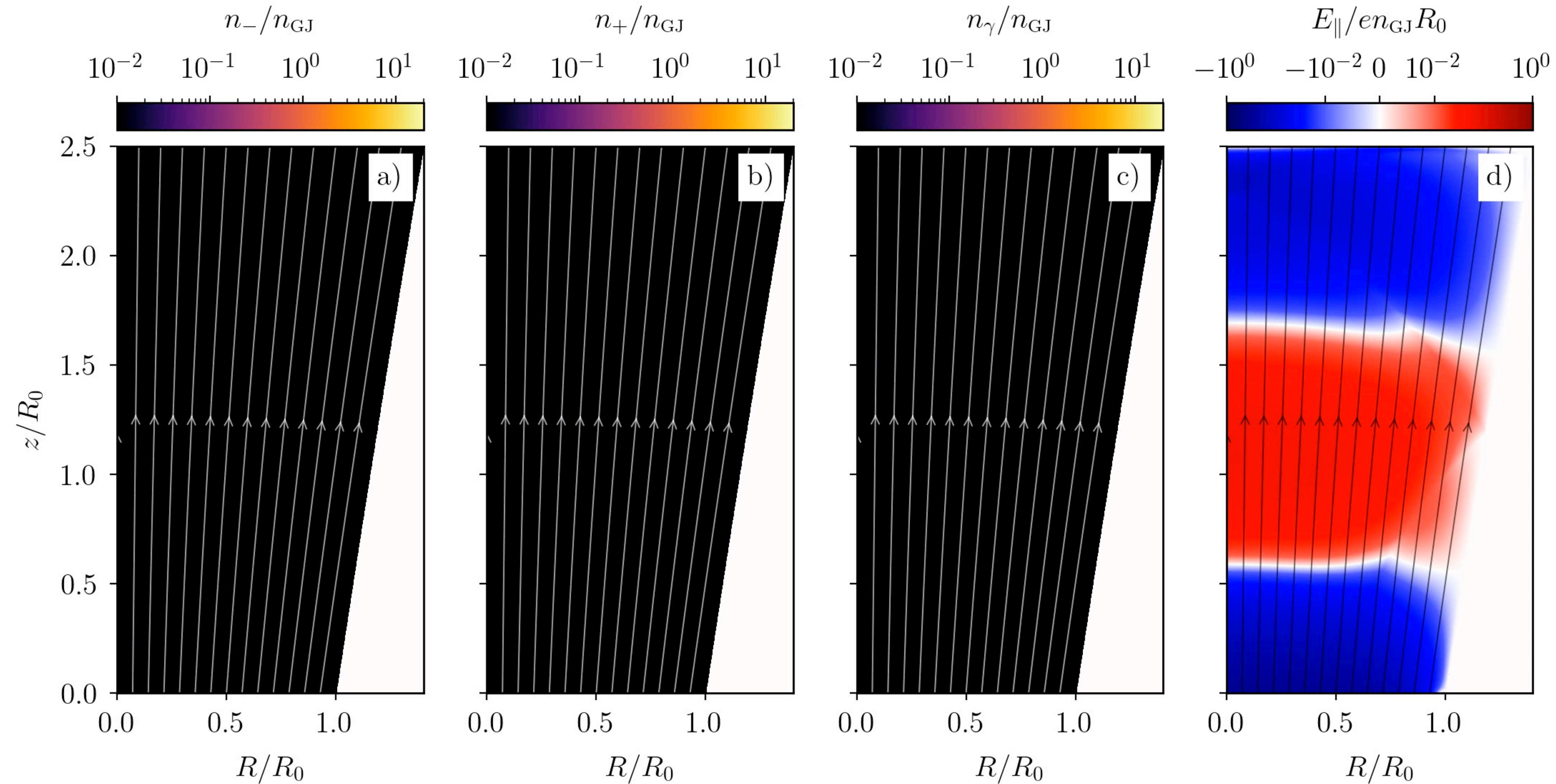
$$tc/R_0 = 2.50$$



Simulations courtesy of F. Cruz and A. Chen

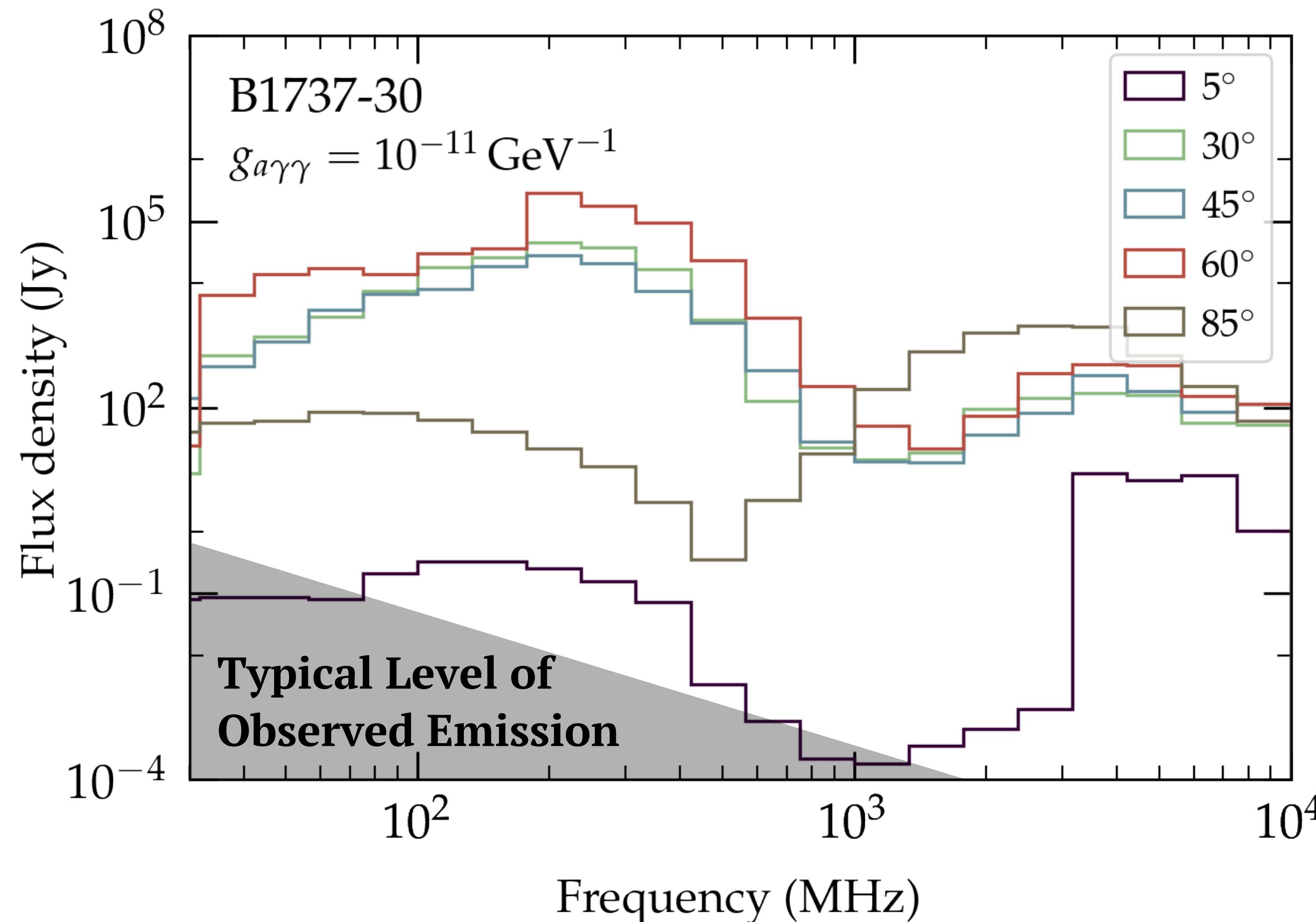
# Vacuum gap collapse

$$tc/R_0 = 2.50$$

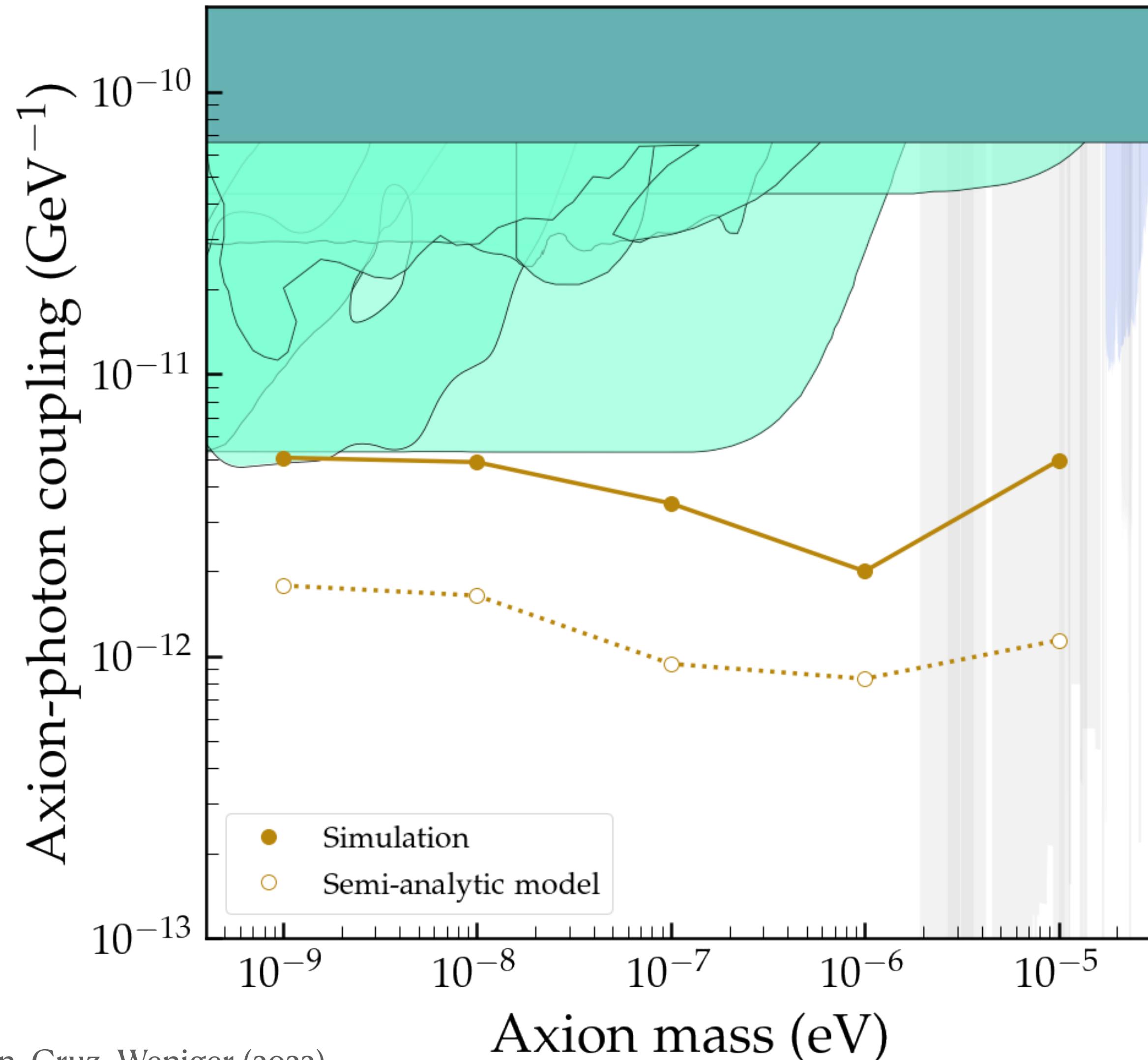


Simulations courtesy of F. Cruz and A. Chen

# Radio Spectrum



# Constraints



## Current search:

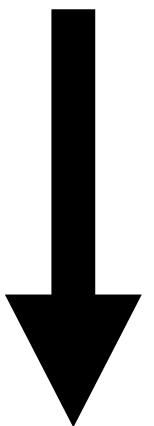
- Uses only 27 well-studied pulsars!

## Future outlook:

- Wider frequency observations
- Full population in ATNF pulsar catalogue
- 3D PIC simulations

If there exists an axion with a mass

$$10^{-8}\text{eV} \lesssim m_a \lesssim 10^{-5}\text{eV}$$

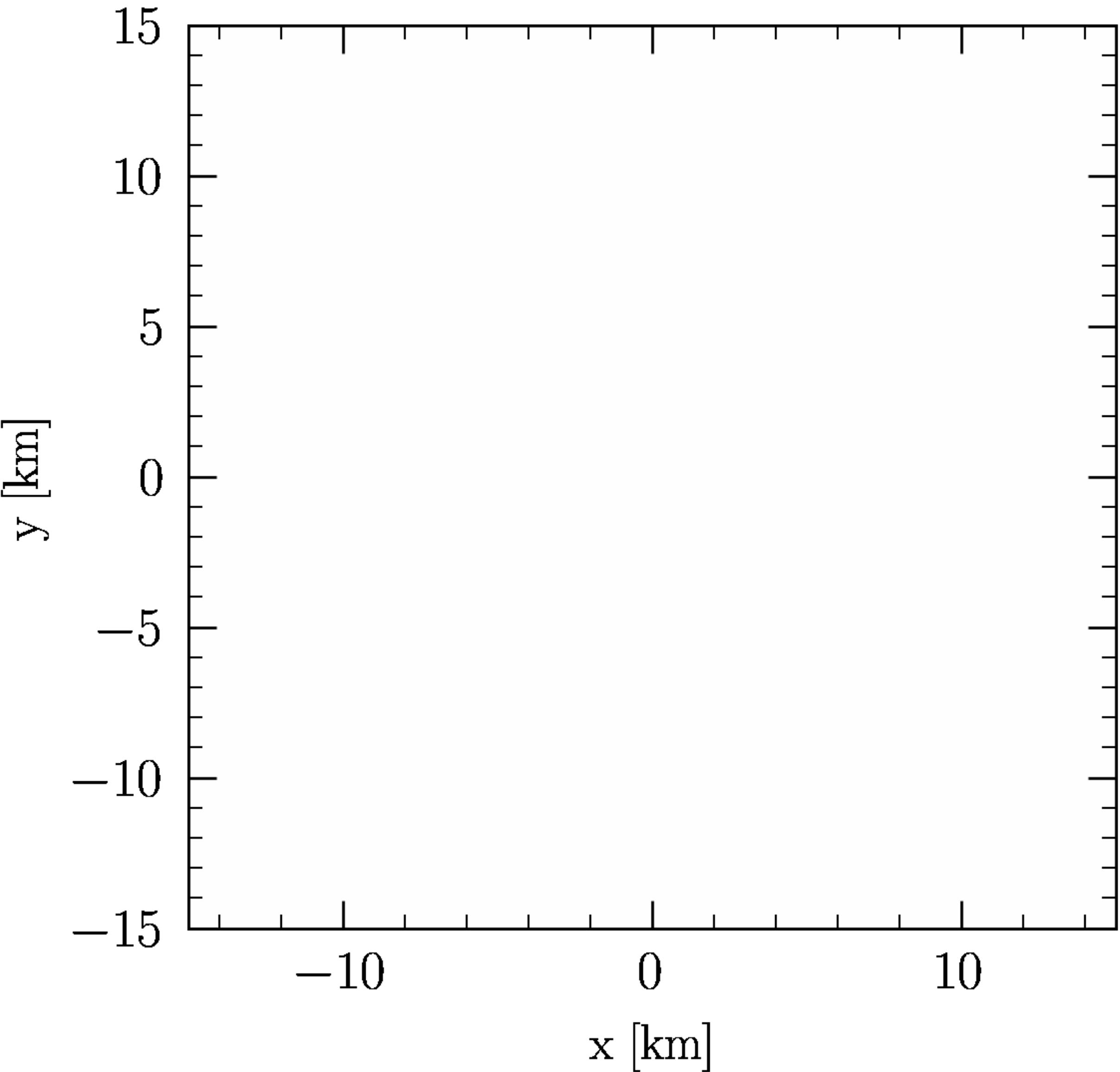


All pulsars are surrounded by extremely  
dense clouds of axions.

# Axion clouds

For these masses, most energy goes into gravitationally bound states...

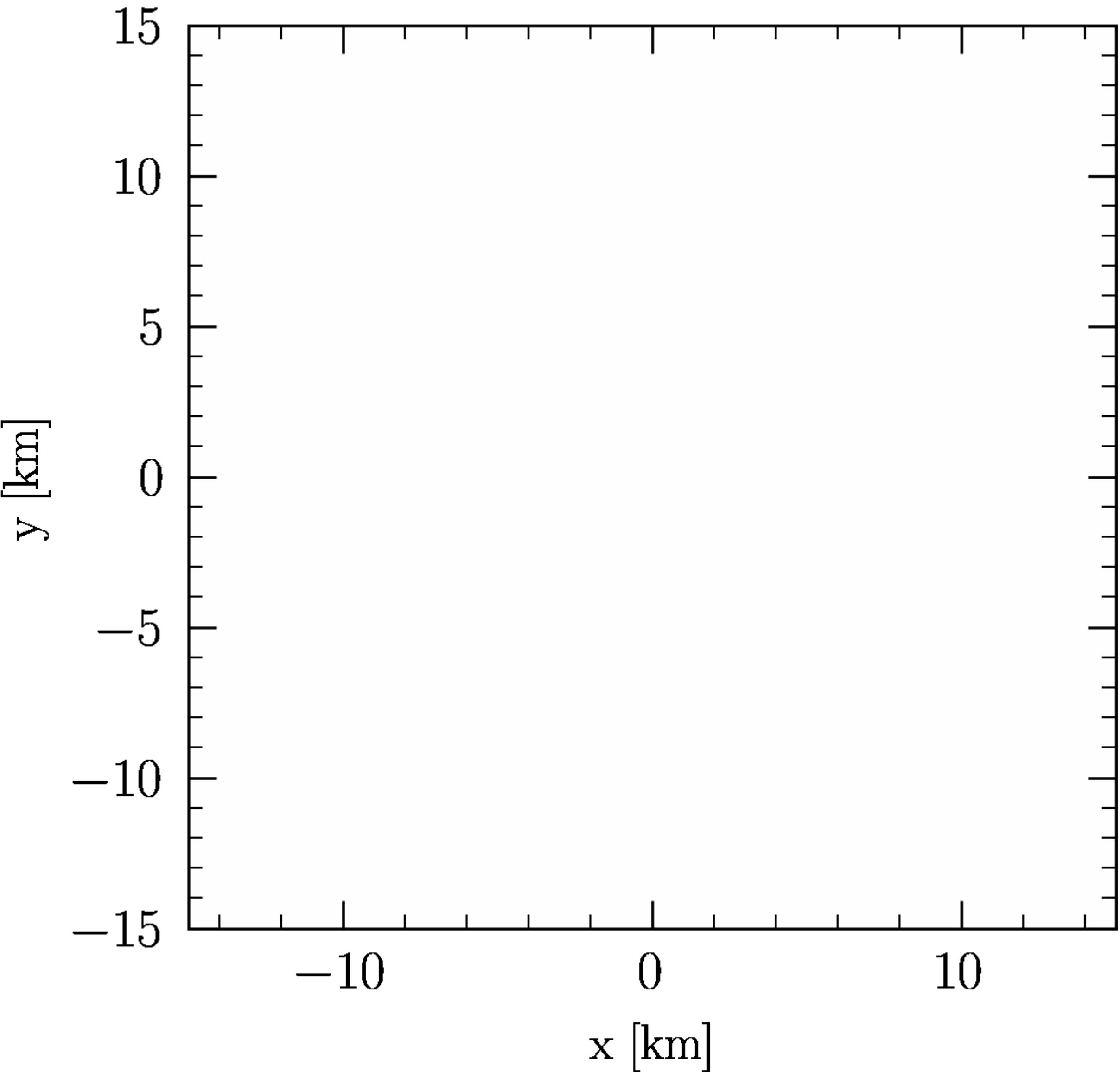
Can accumulate for  $\sim$ kyr timescales



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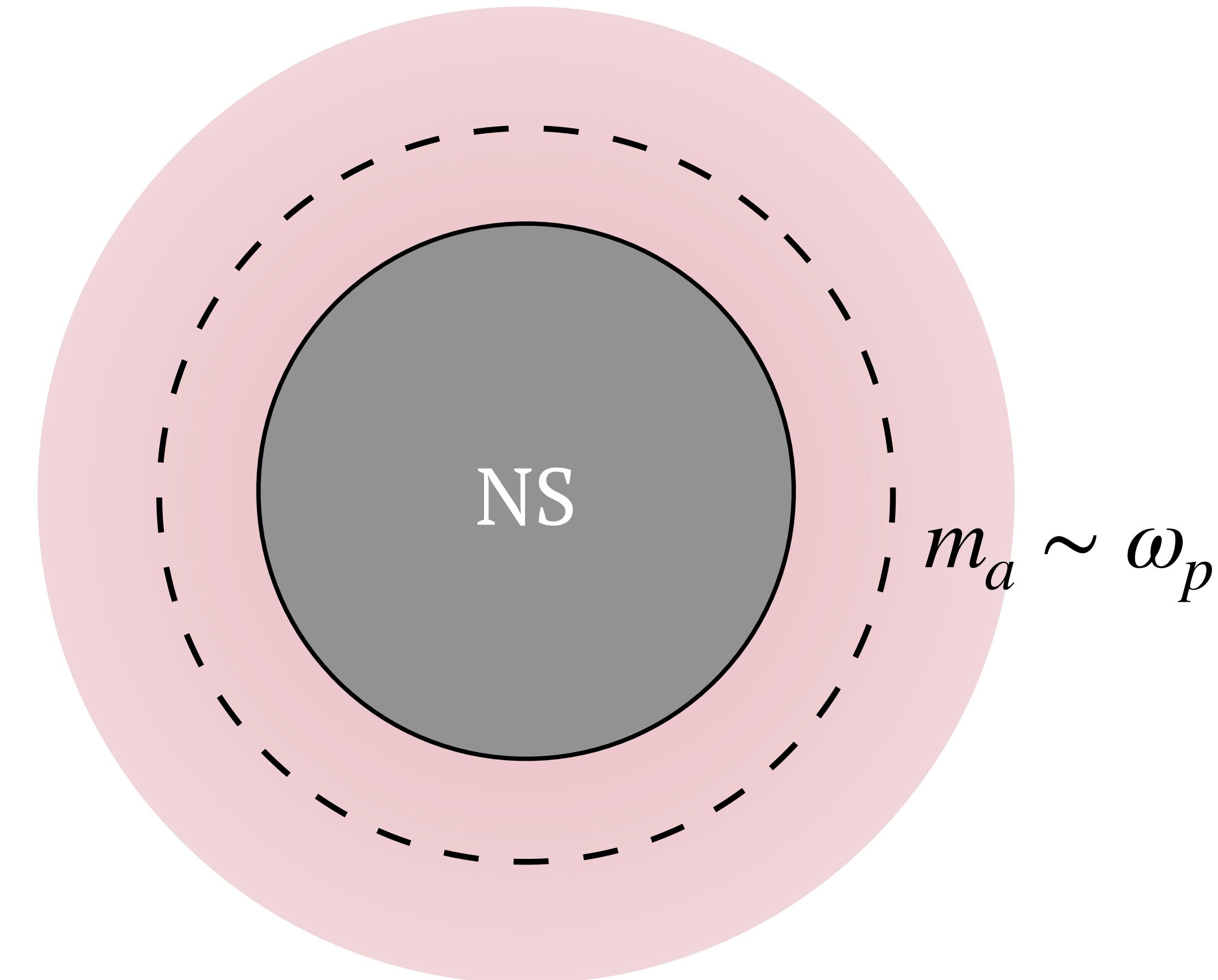
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# Quenching of bound state growth

Emission from resonant conversion:

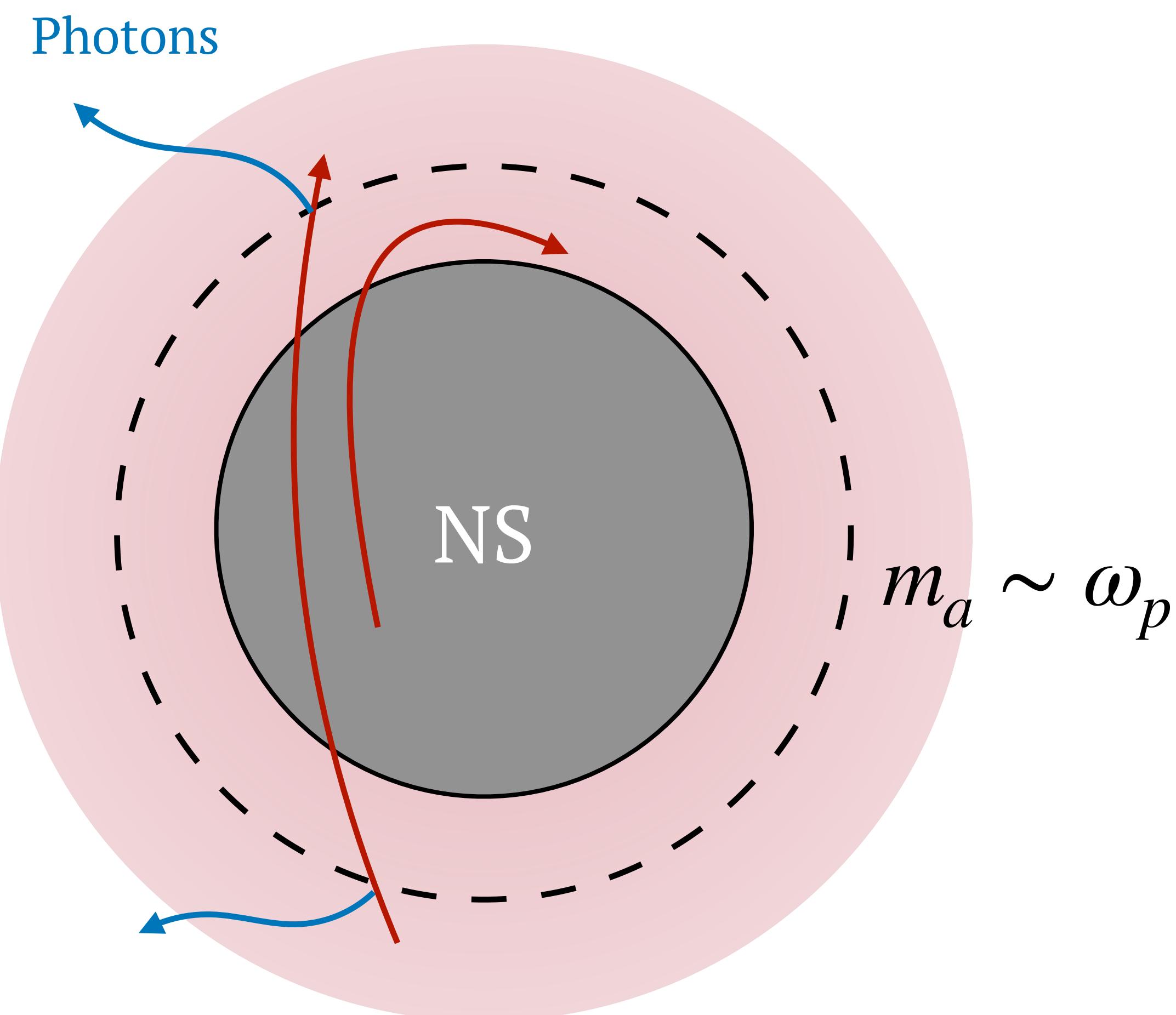
Noordhuis, Prabhu, Weniger, **SJW** (To appear)



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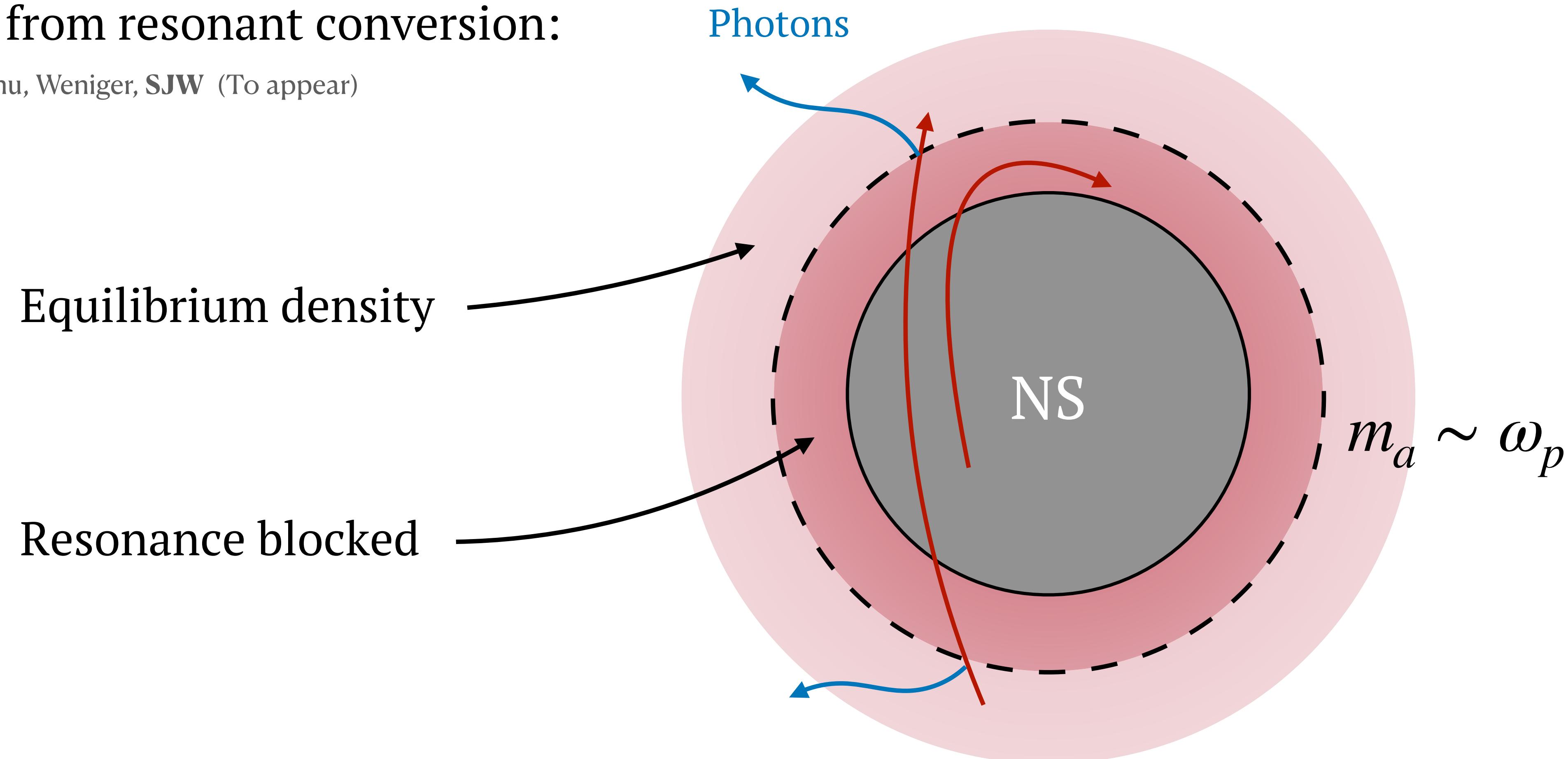
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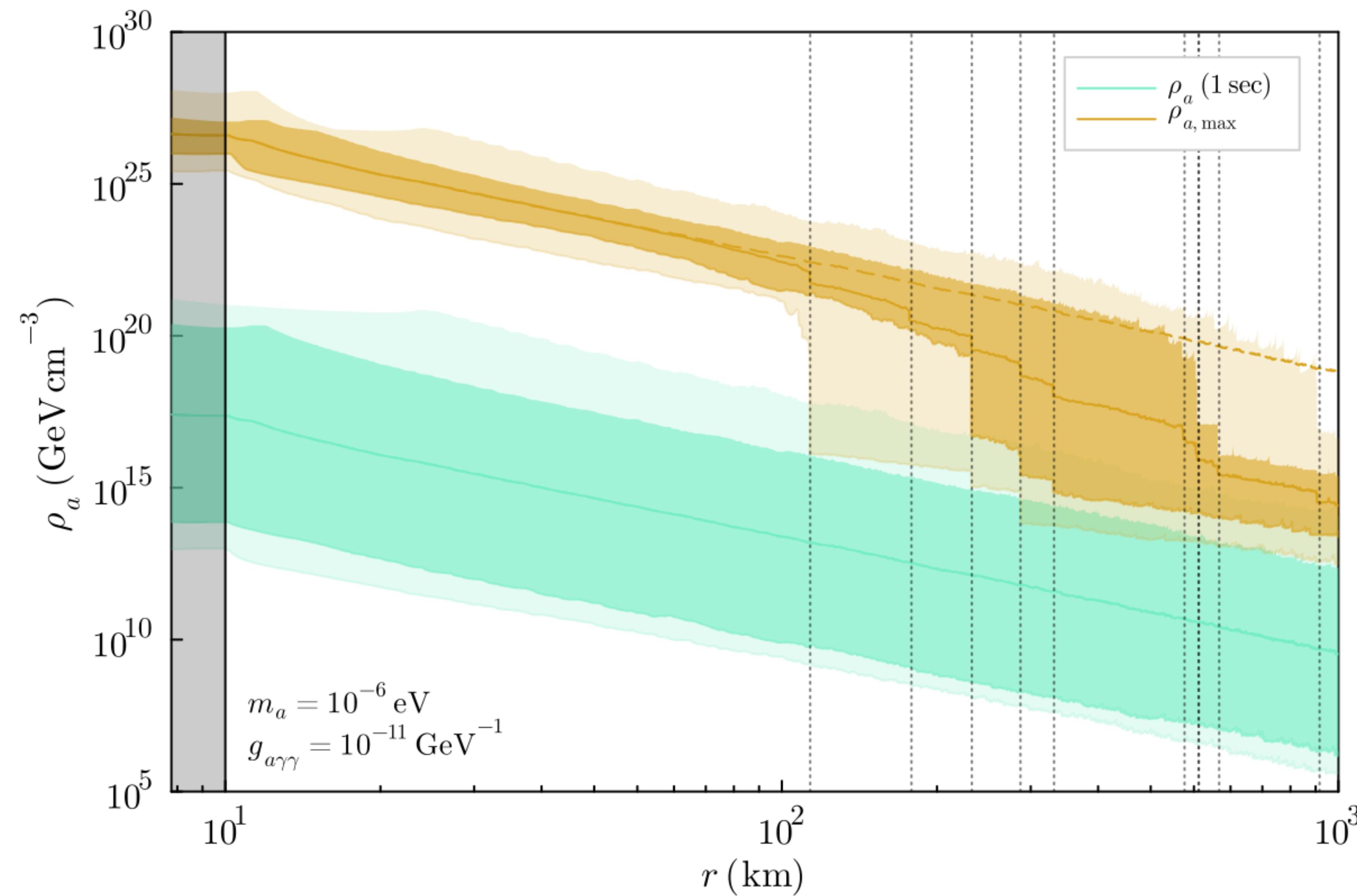
# Quenching of bound state growth

Emission from resonant conversion:

Noordhuis, Prabhu, Weniger, **SJW** (To appear)



# Bound state profiles



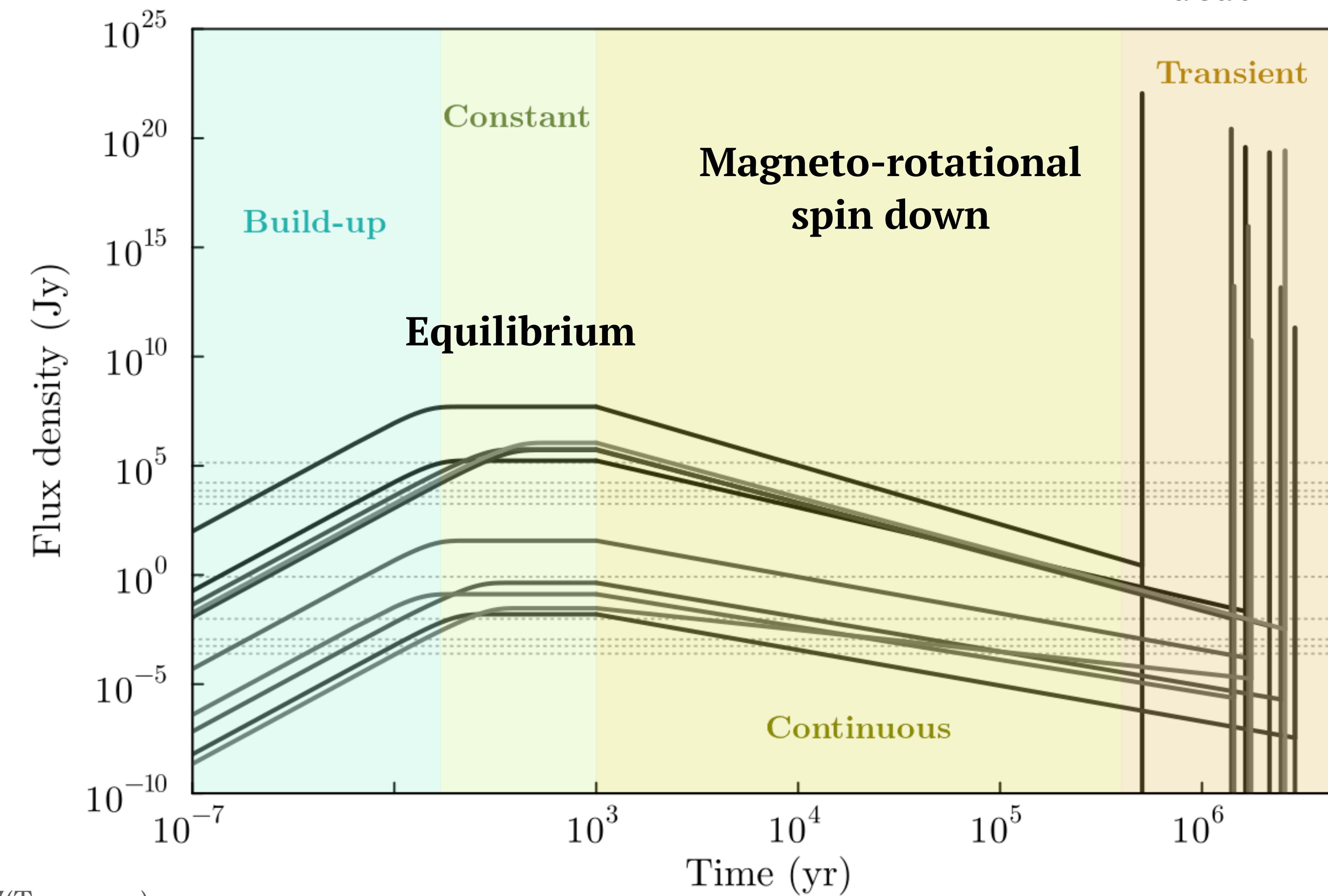
Noordhuis, Prabhu, Weniger, SJW (To appear)

# Evolution of bound cloud

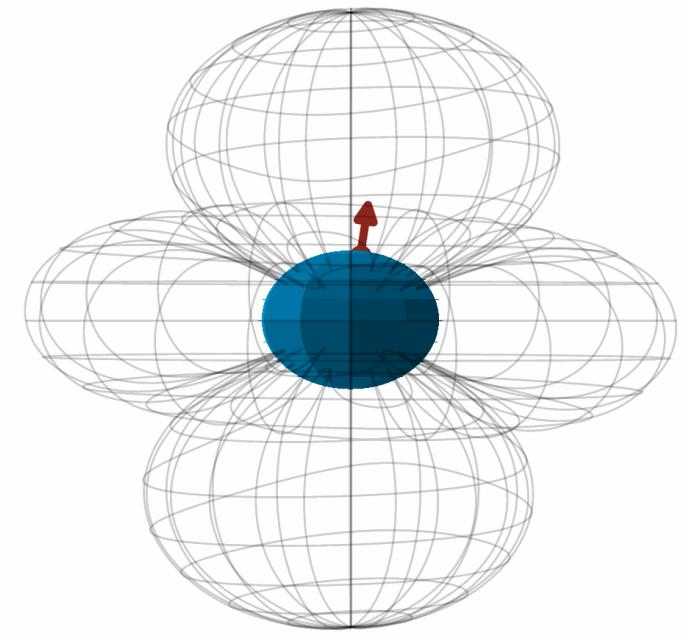
Charge  
separation at  
death

$$m_a = 10^{-6} \text{ eV}$$

$$g_{a\gamma\gamma} = 10^{-11} \text{ GeV}^{-1}$$

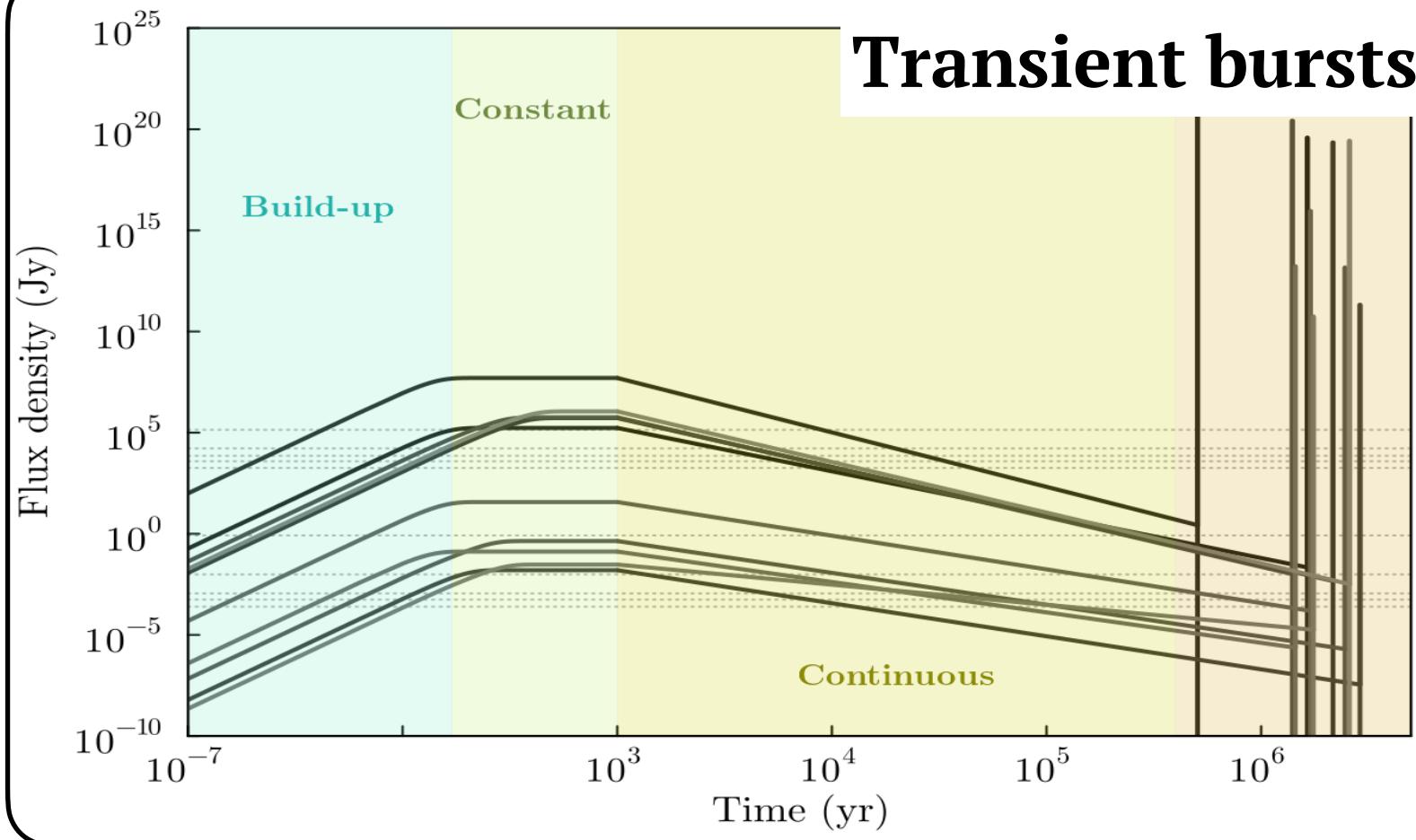
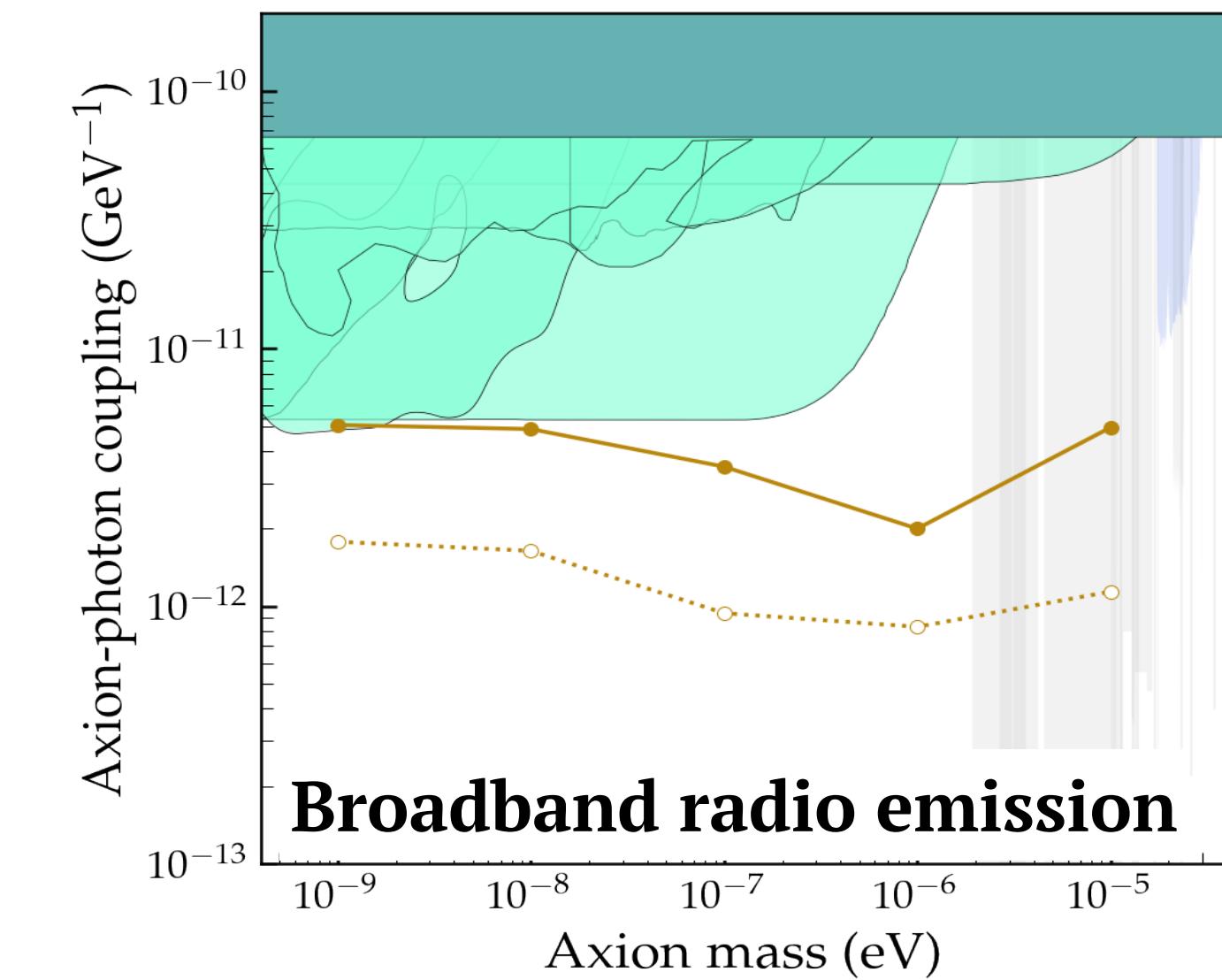


# Take-Home Message

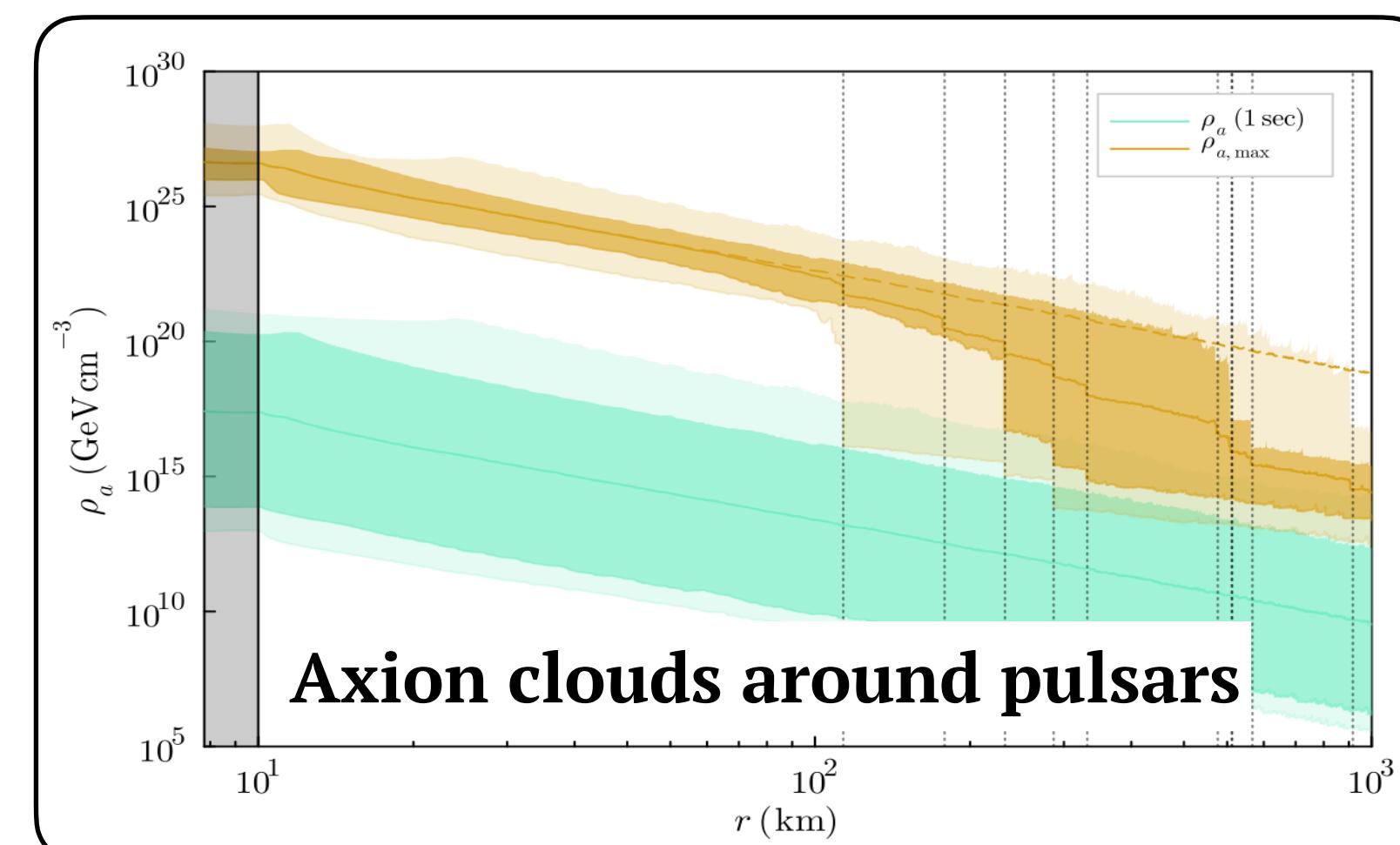


Spectral lines from axion dark matter

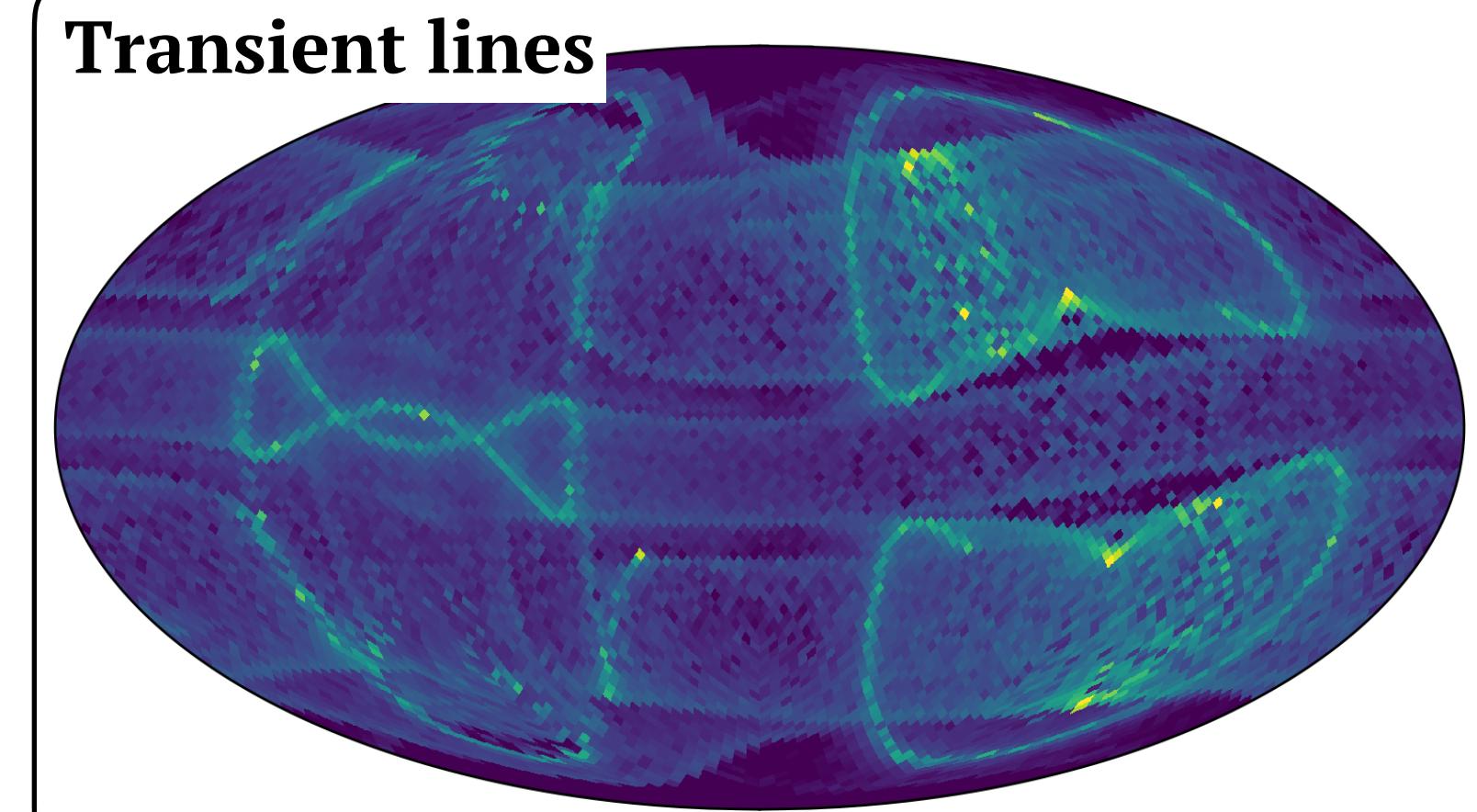
*Neutron stars are incredible axion laboratories, with rich and powerful signatures*



Transient bursts

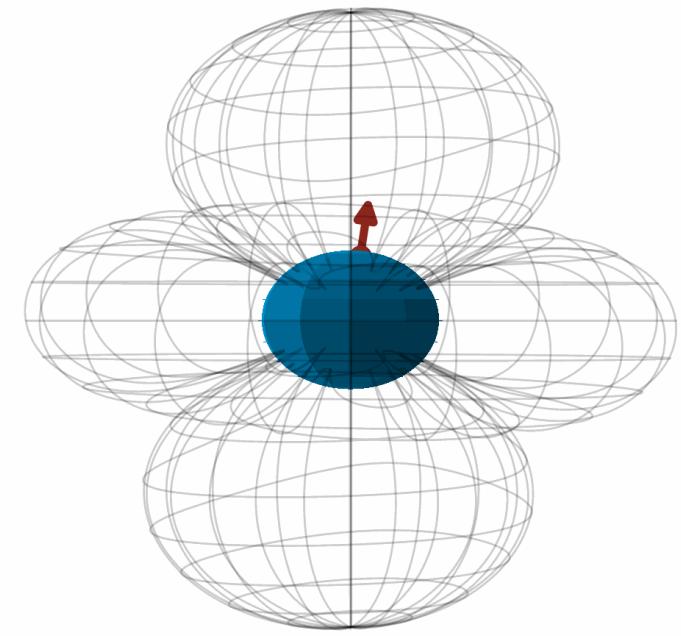


Axion clouds around pulsars



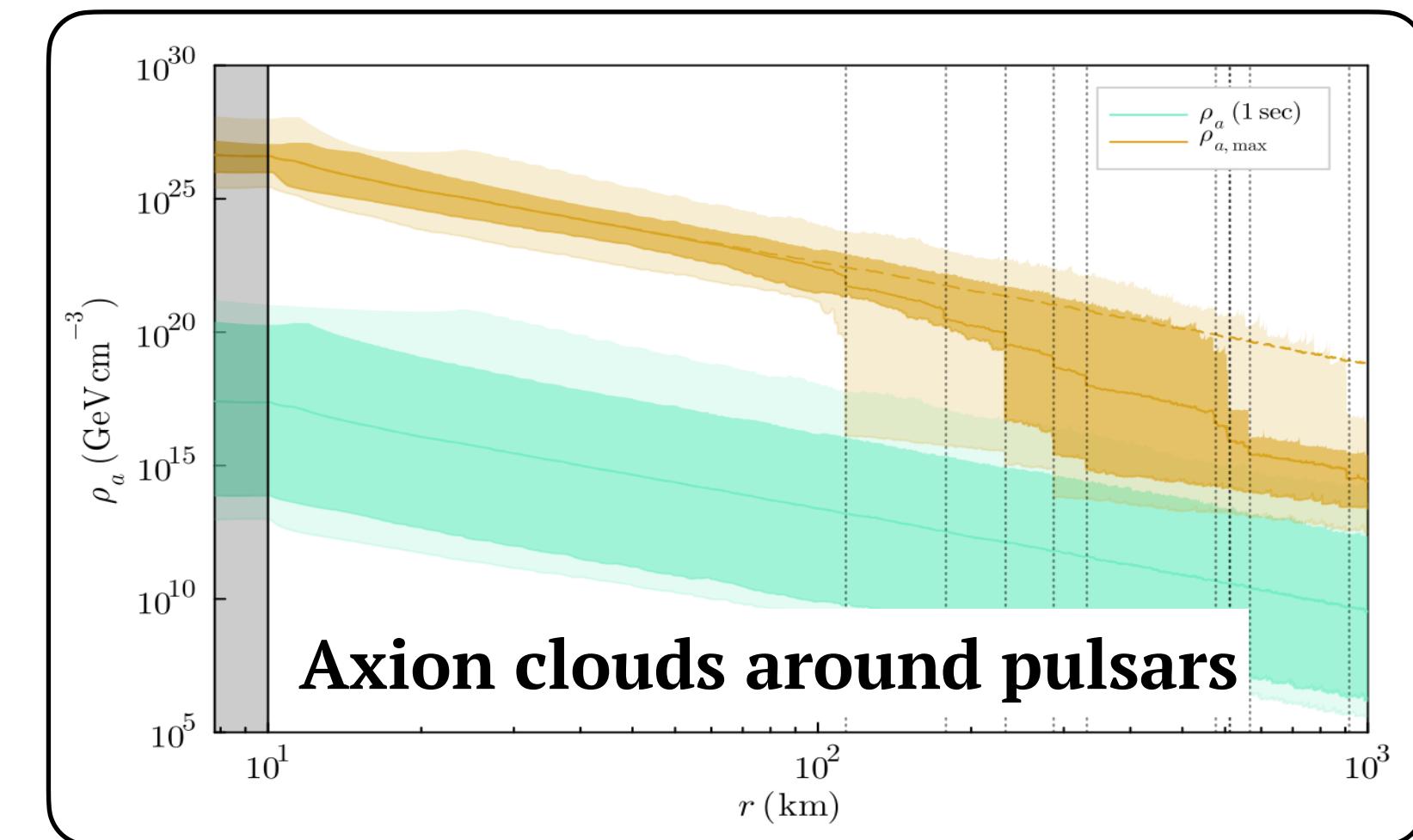
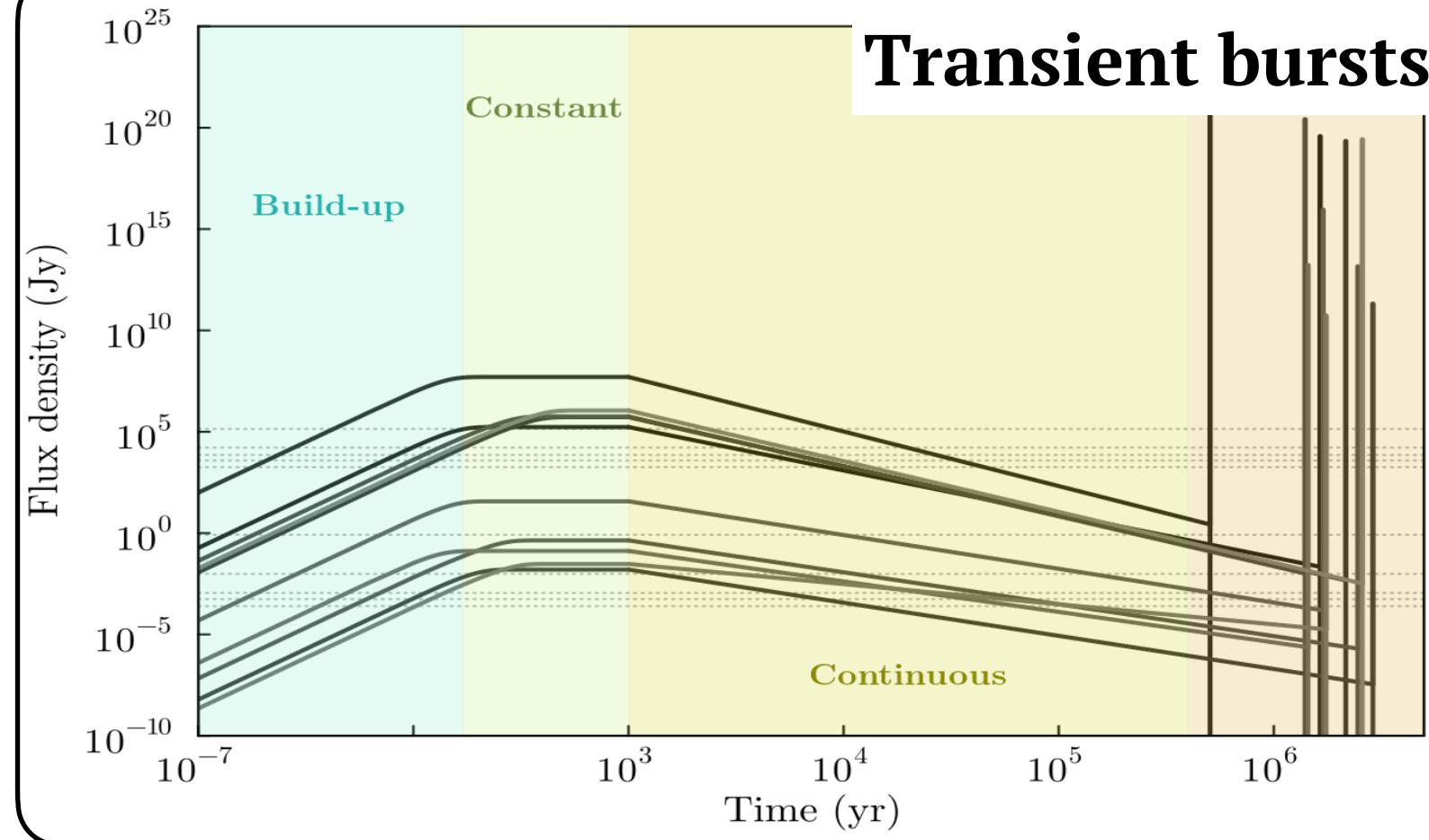
Transient lines

# Take-Home Message

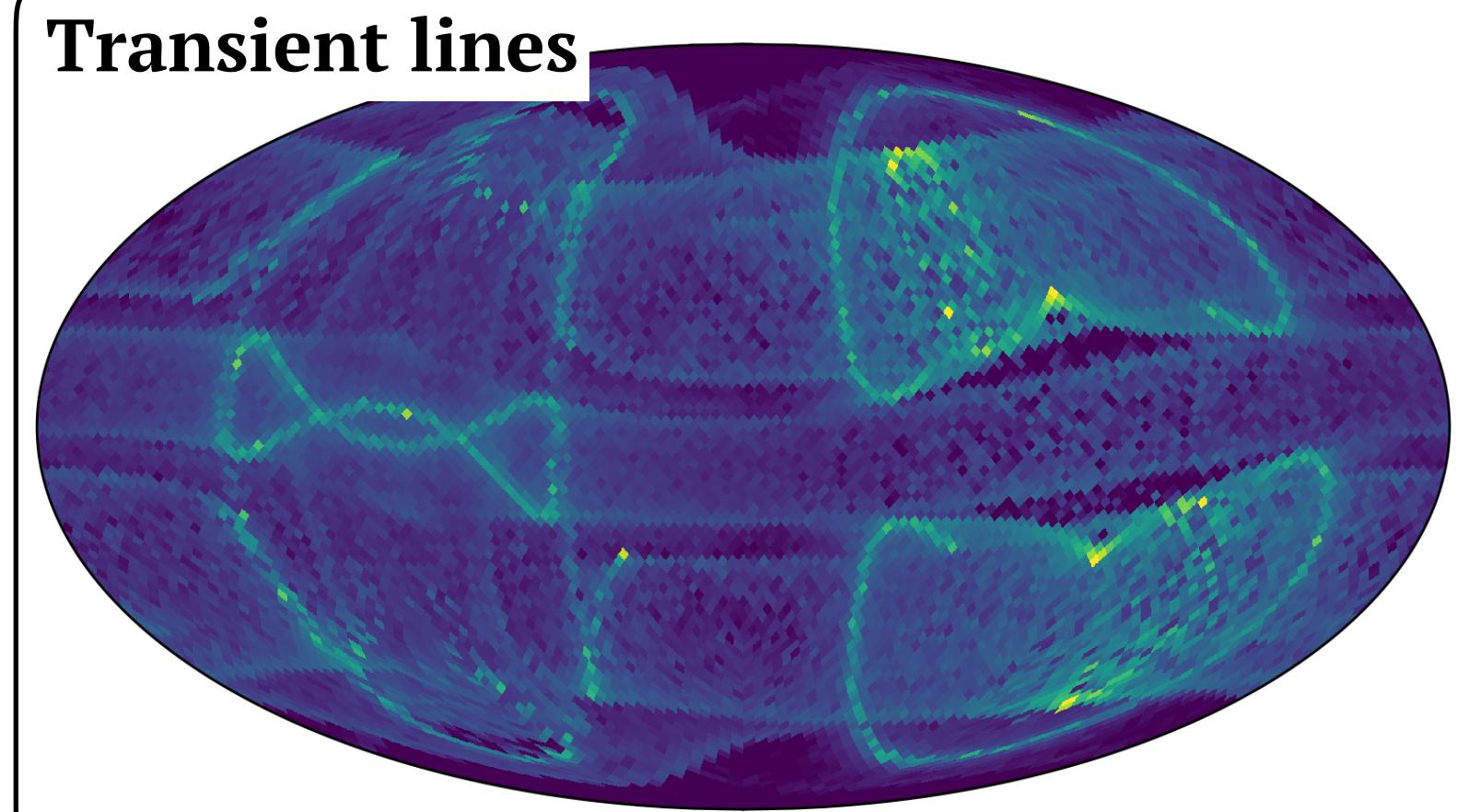
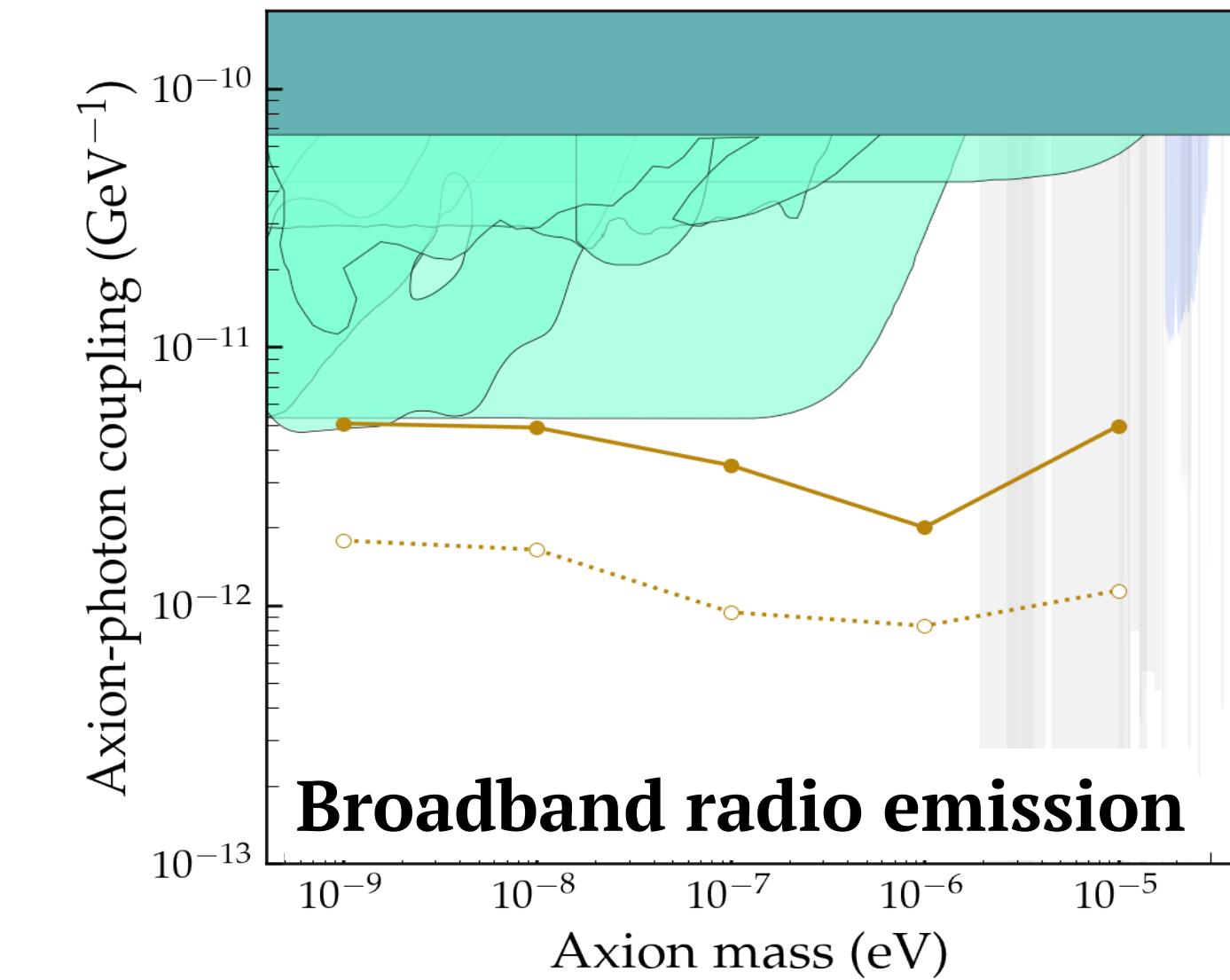


Spectral lines from axion dark matter

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Samuel J. Witte (GRAPPA / Amsterdam)



Transient lines