

# DARK MATTER COMPLEMENTARITY: A CASE STUDY

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*Prof. Katelin Schutz, McGill University*

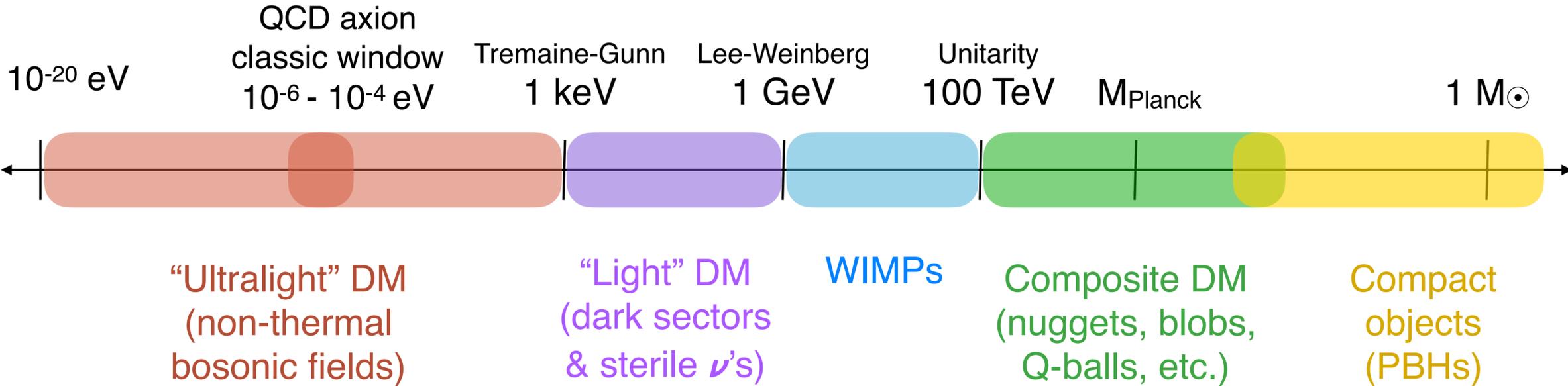
*Canada Research Chair in Astrophysics beyond the Standard Model*

*Xmas 2023 @ IFT*

**WHAT IS THE DARK  
MATTER?**

# DARK MATTER MASS

(not to scale)

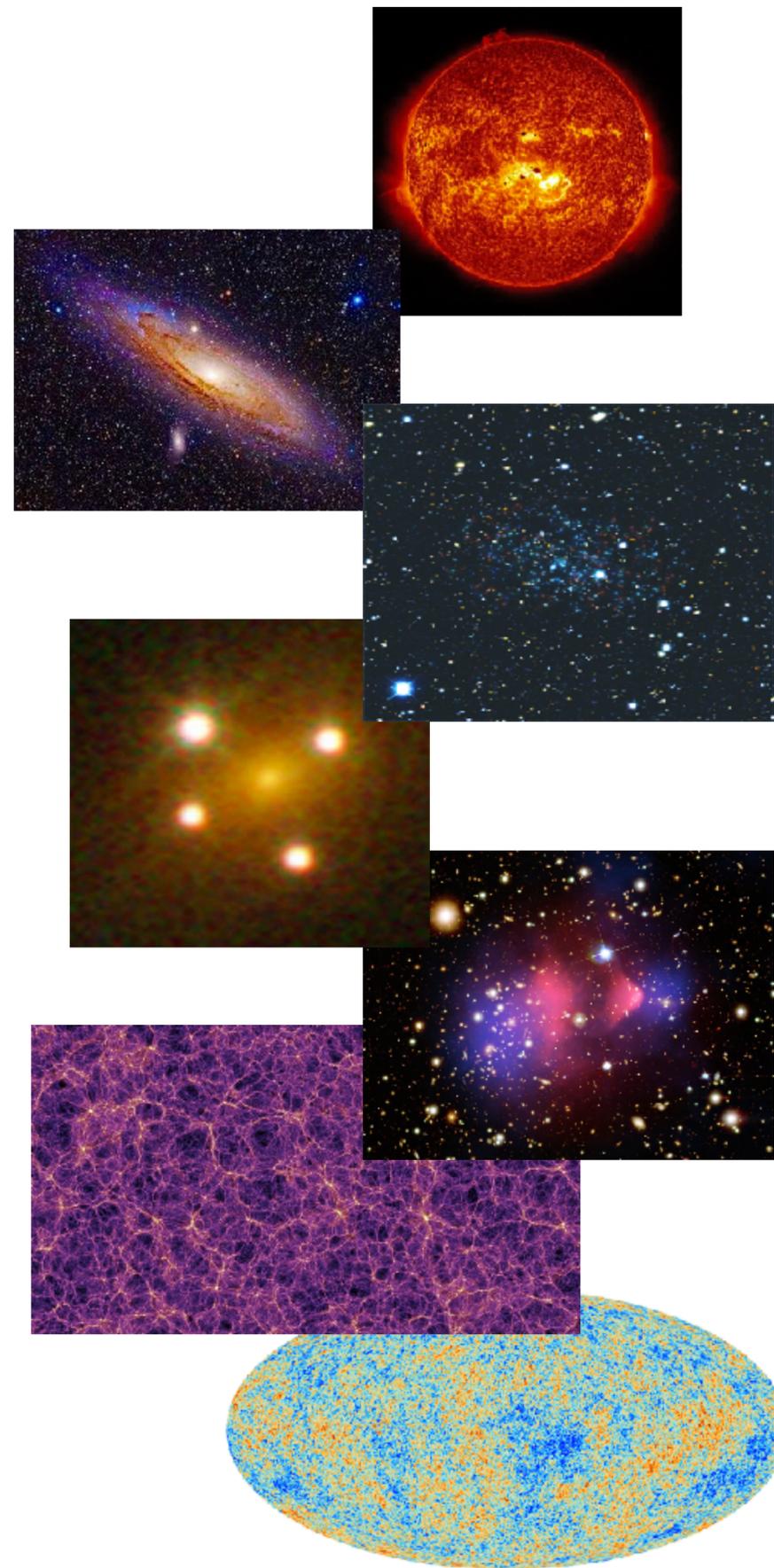


➤ Many possibilities spanning 90+ orders of magnitude!

**A DIVERSITY OF THEORIES REQUIRES  
THAT WE EXPLORE A DIVERSITY OF  
APPROACHES AND SYSTEMS!**

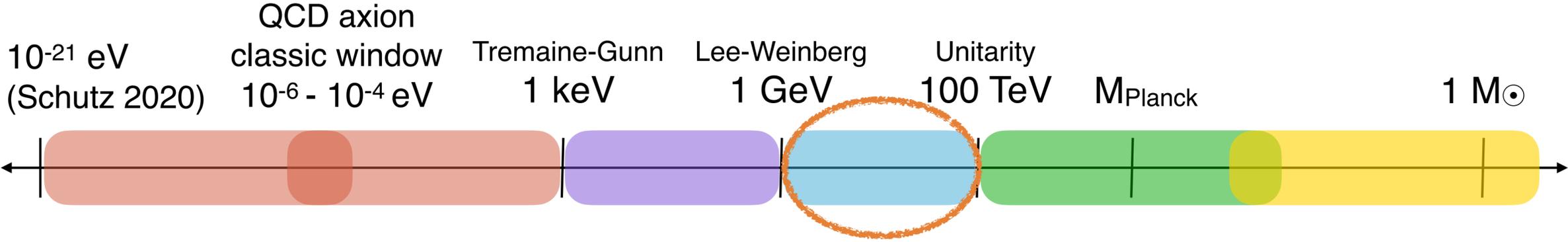
# APPROACH/PHILOSOPHY

- Use any/all available astrophysical systems that can tell us about dark matter
- 20 orders of magnitude in length and 18 orders of magnitude in time
- Consider this information in a holistic, self-consistent way (“complementarity” of different probes)



# DARK MATTER MASS

(not to scale)



“Ultralight” DM  
(non-thermal  
bosonic fields)

“Light” DM  
(dark sectors  
& sterile  $\nu$ 's)

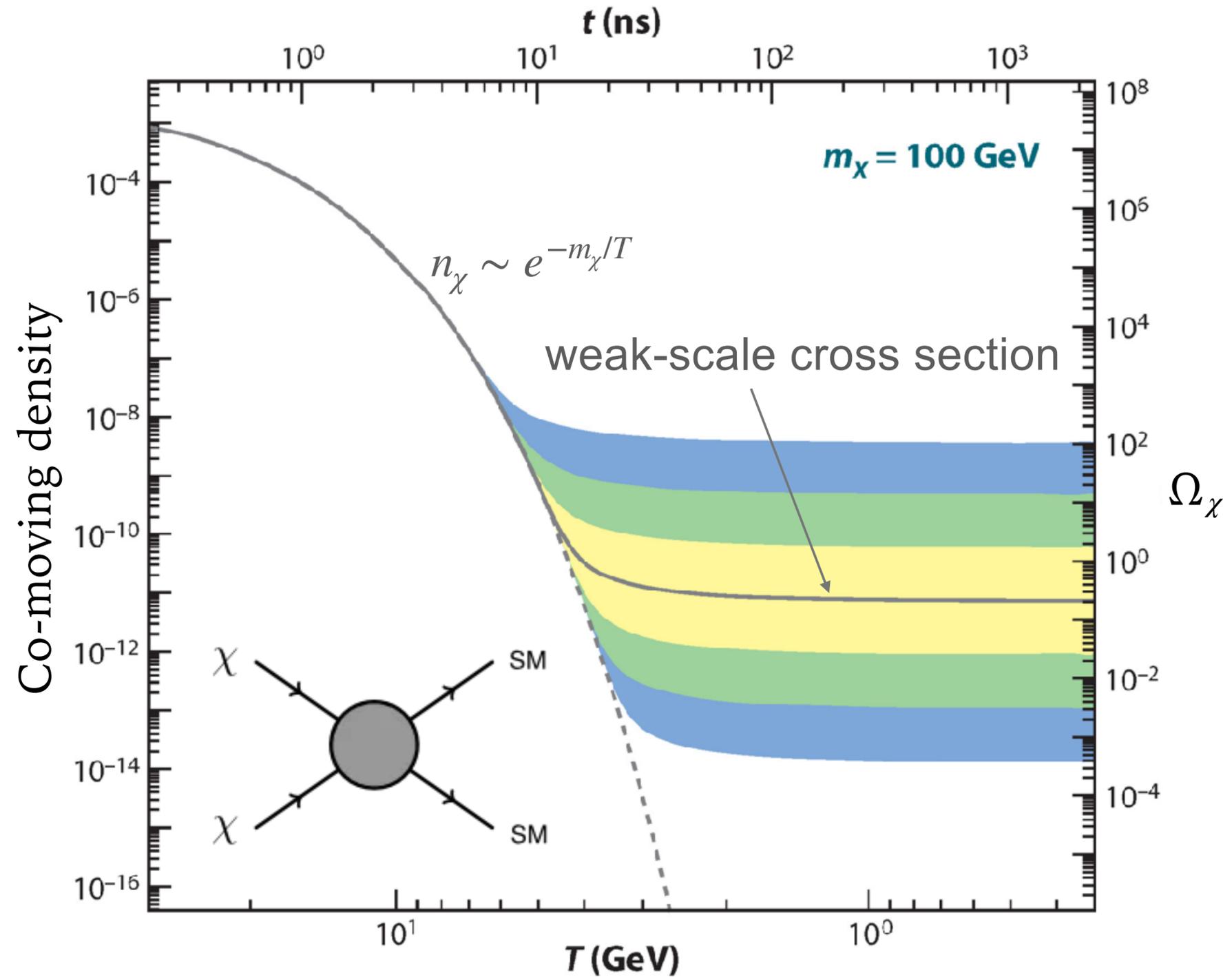
WIMPs

Composite DM  
(nuggets, blobs,  
Q-balls, etc.)

Compact  
objects  
(PBHs)

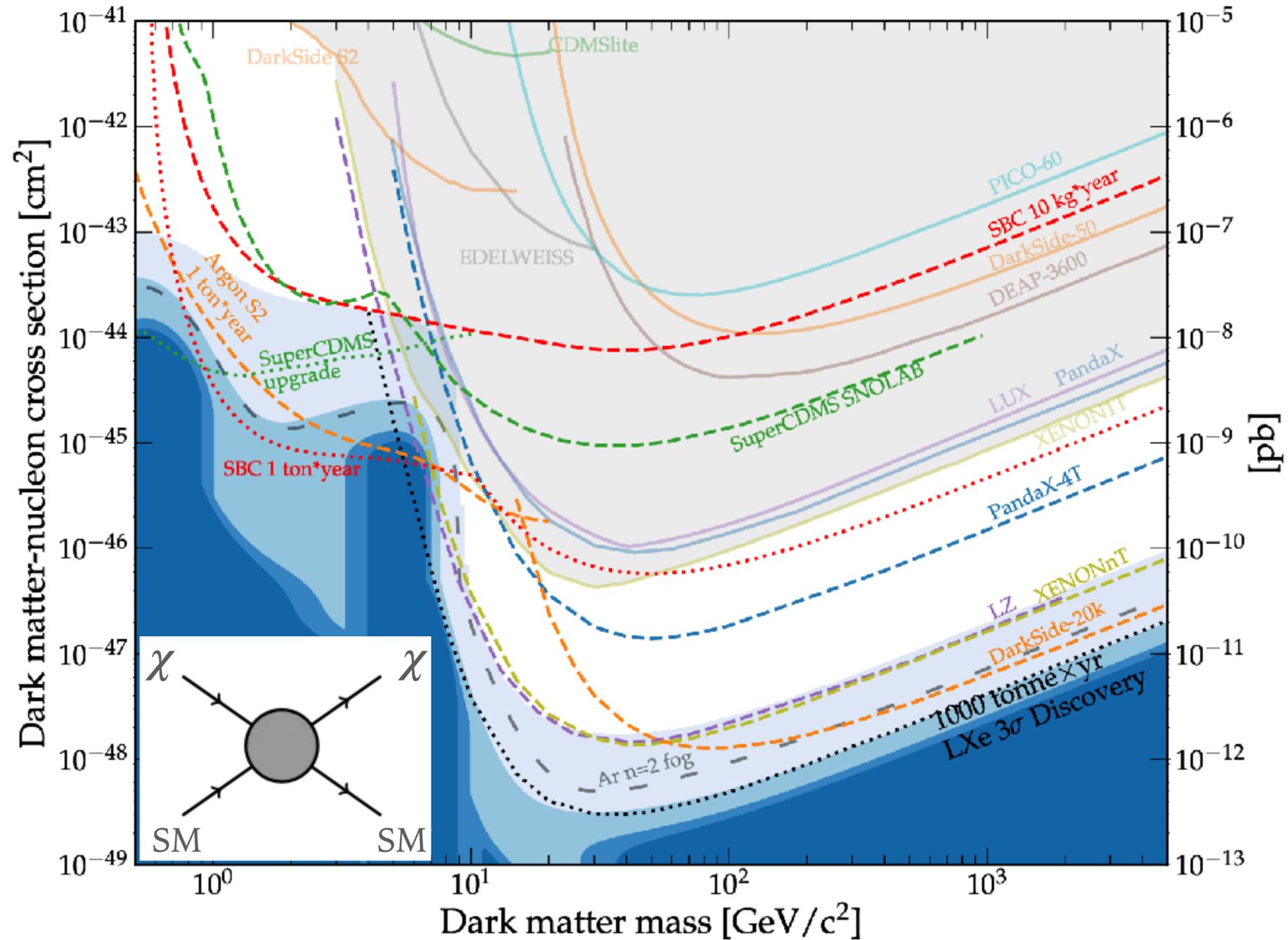
What is the status?  
(Already a need for  
complementarity)

# THERMAL DARK MATTER CANDIDATE: WIMPS (FREEZE-OUT)

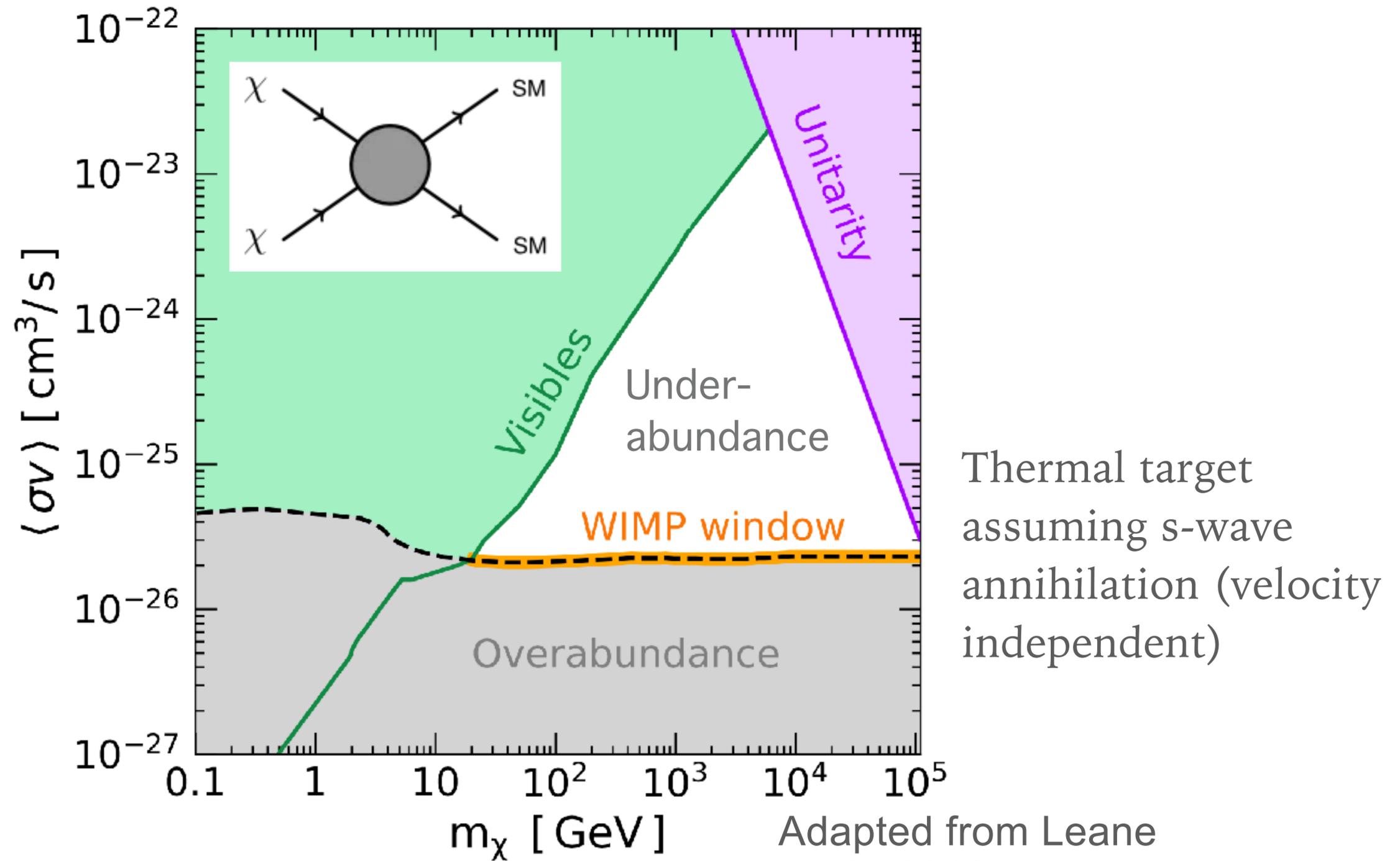


Adapted from Jonathan Feng

# WIMP DIRECT DETECTION (MODEL DEPENDENT)



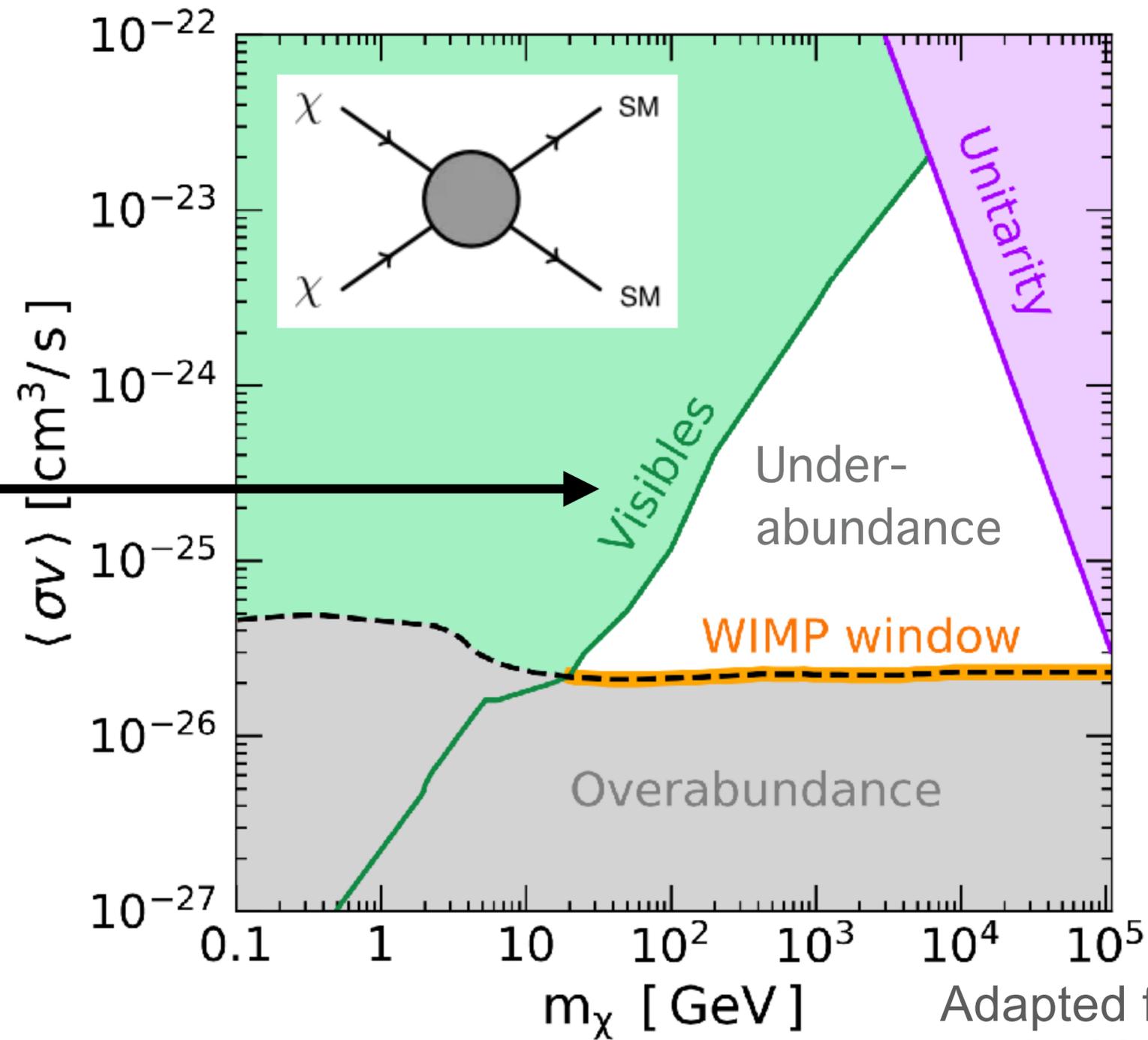
# WIMP (THERMAL FREEZE-OUT) INDIRECT DETECTION WINDOW



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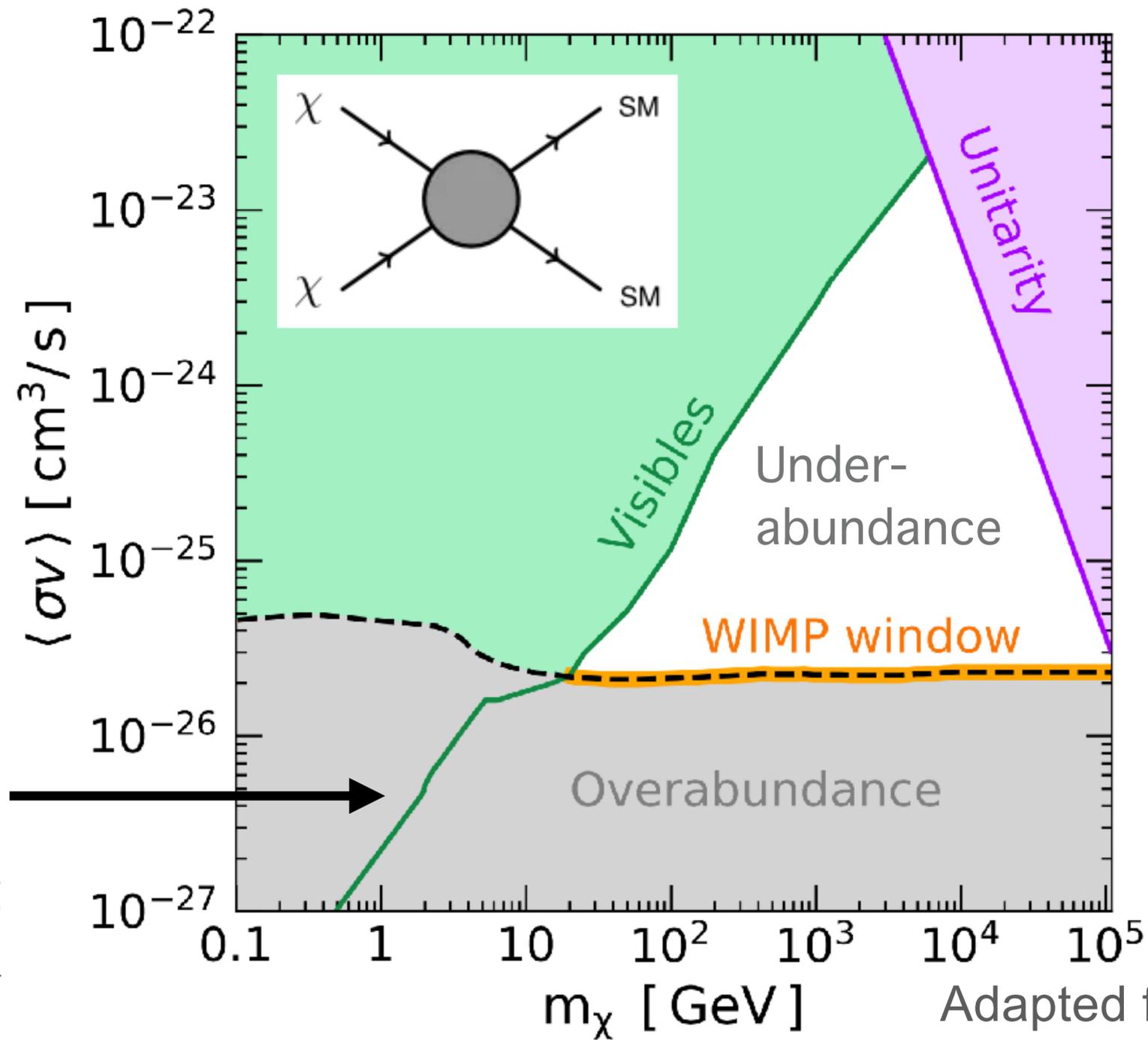


Visible byproducts cascade and can be observed in gamma rays with Fermi



Adapted from Leane et al. (2018)

# WIMP (THERMAL FREEZE-OUT) INDIRECT DETECTION WINDOW

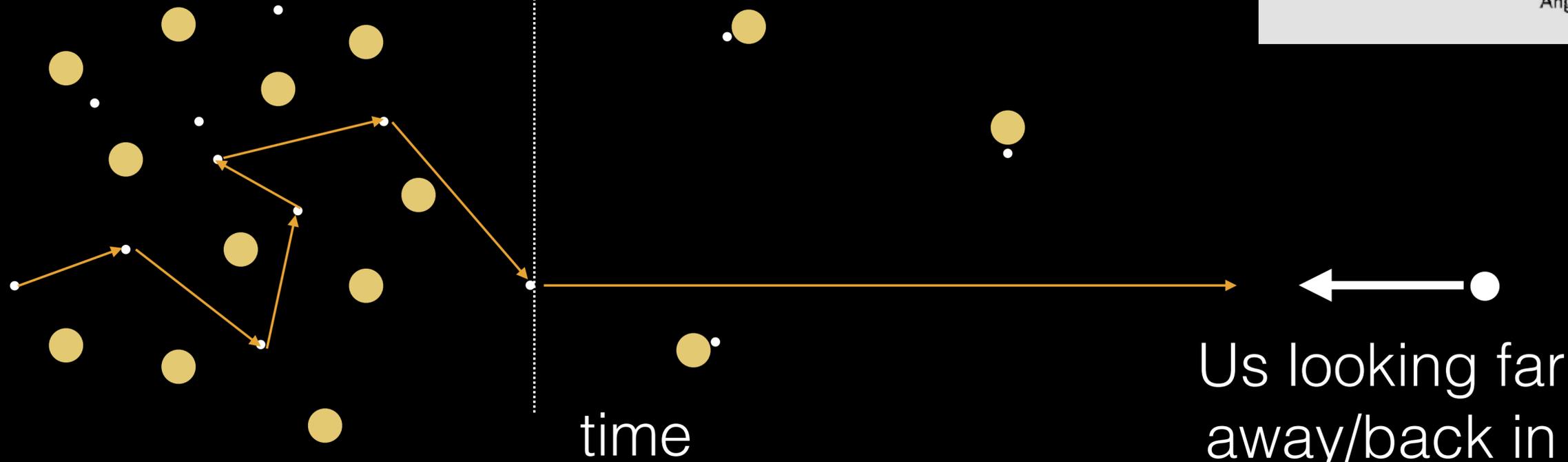


Low-mass bounds are driven by CMB constraint assuming s-wave cross section

Adapted from Leane et al. (2018)

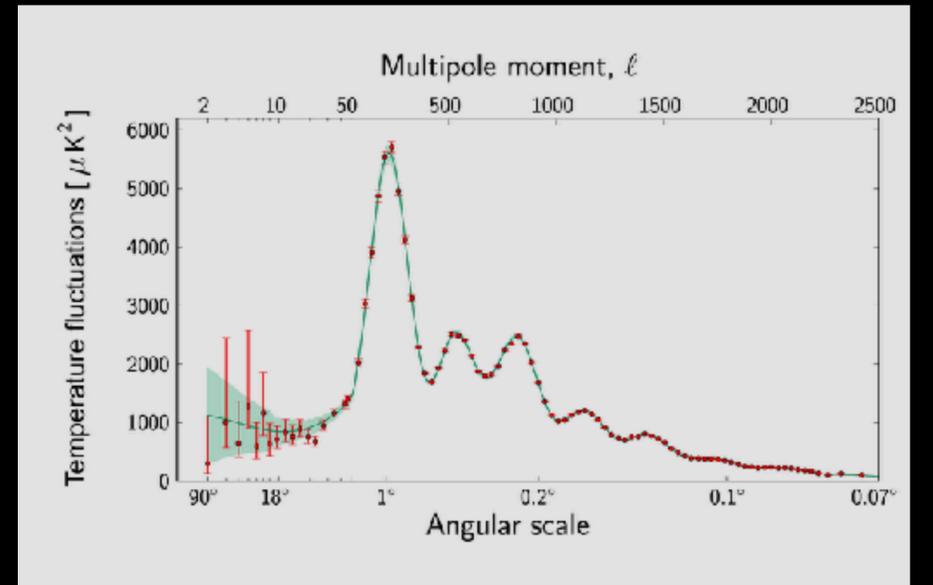
Too hot for atoms  
to form (plasma)  
Not transparent

Cool enough for  
atoms to exist  
Transparent



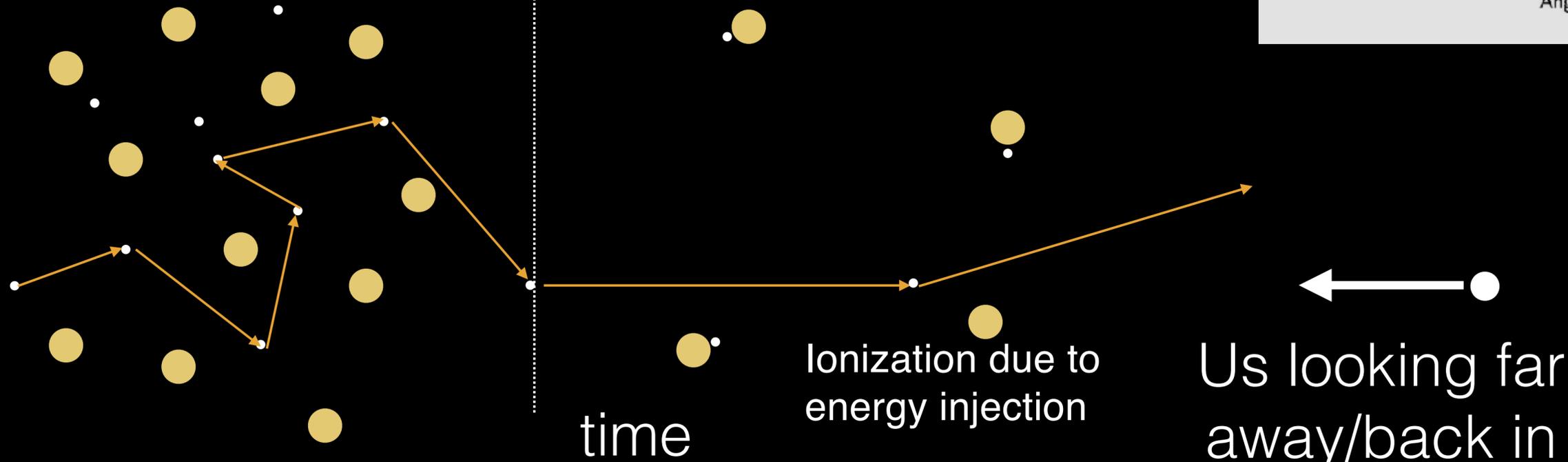
Smaller  
Denser  
Hotter

Larger  
Less dense  
Cooler



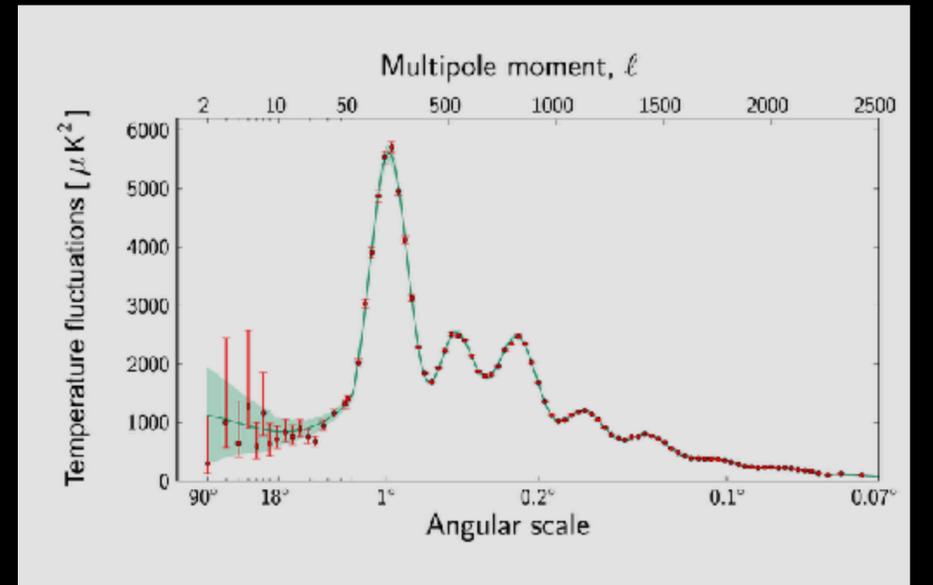
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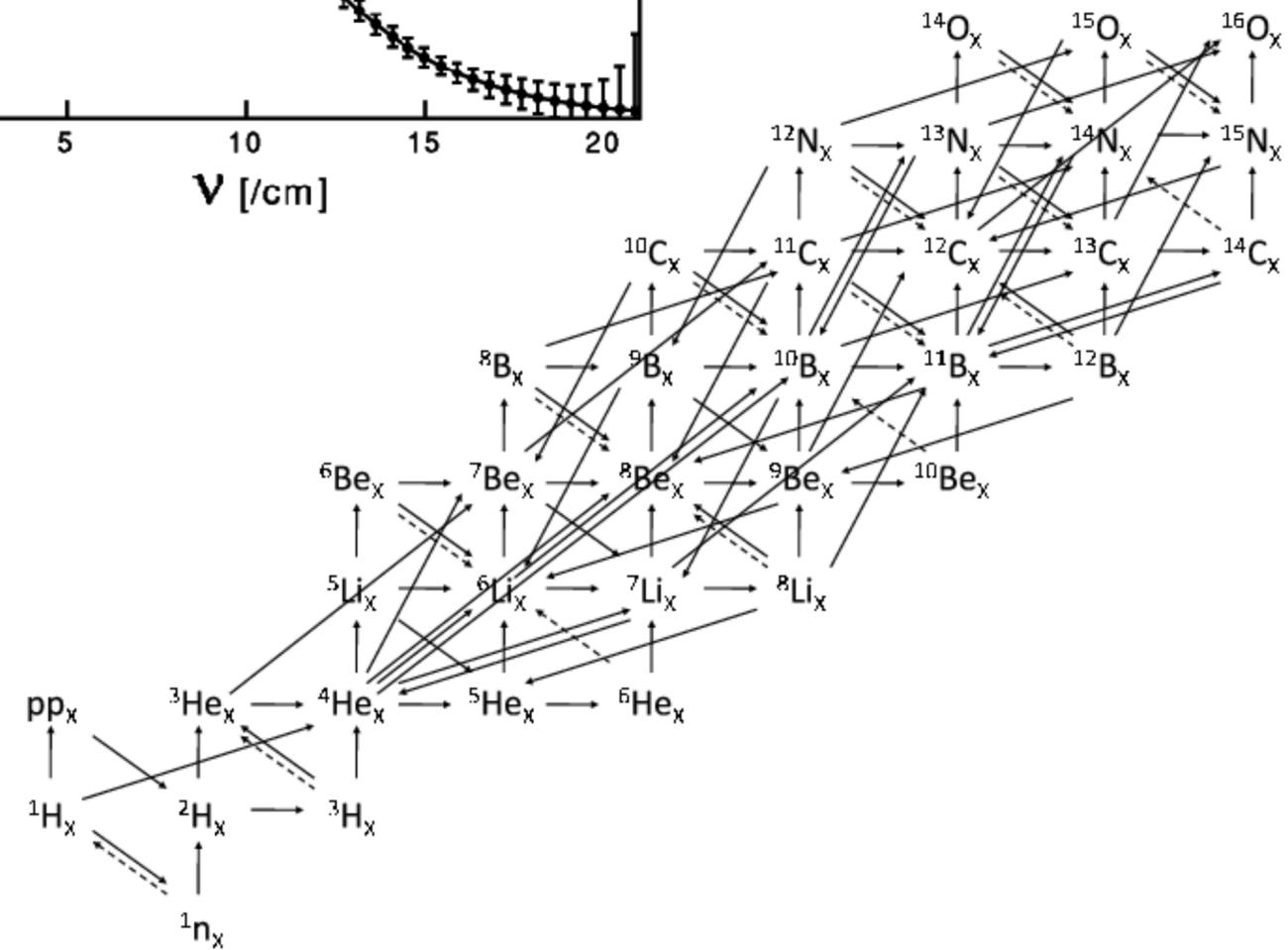
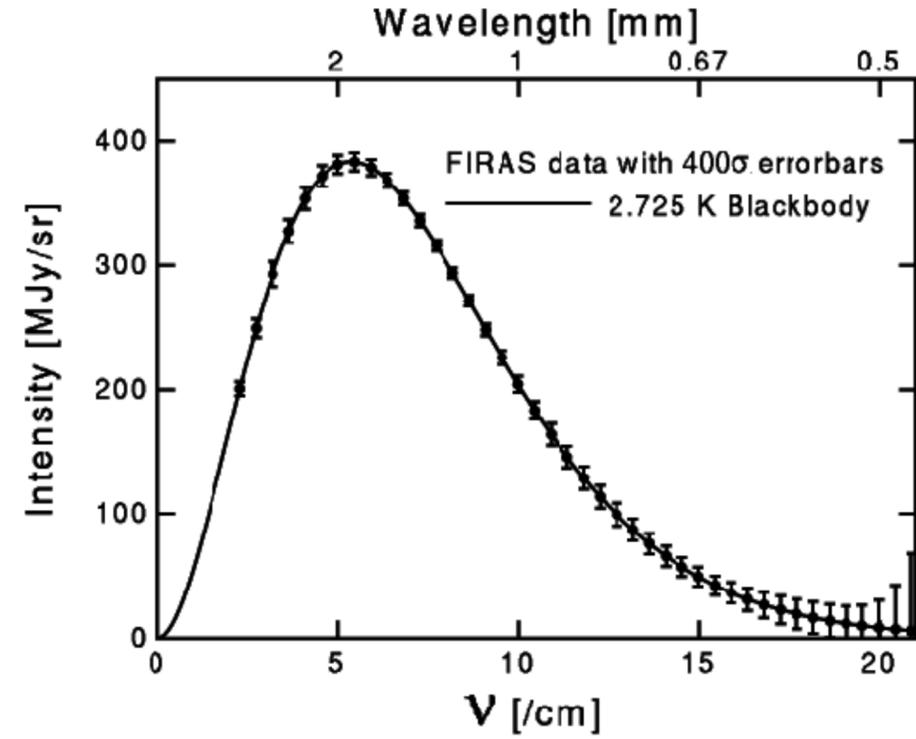
Smaller  
Denser  
Hotter

Larger  
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# EARLY UNIVERSE IS EXTREMELY SENSITIVE TO ENERGY INJECTION

- If one part per billion of the dark matter annihilates, that would ionize whole universe post-recombination
- Before recombination, energy injection would cause CMB spectrum to deviate from blackbody measured by FIRAS at ppm level
- Big Bang Nucleosynthesis also is very sensitive to energy injection which causes photodissociation of light elements, messes up flow chart of nuclear processes



**THE UPSHOT: YOU CAN ESSENTIALLY TREAT  
THE UNIVERSE AS A CALORIMETER, SO DARK  
MATTER CAN'T BE A WIMP\* BELOW  $\sim 10$  GEV**

**\*UNLESS ANNIHILATION IS STRONGLY VELOCITY DEPENDENT**

# LEE-WEINBERG BOUND

---

- For dark matter masses above mass scale of mediators ( $\sim 100$  GeV if they are electroweak)

$$\sigma \sim \frac{\alpha^2}{m_\chi}$$

- Below mediator mass scale,

$$\sigma \sim \frac{\alpha^2 m_\chi^2}{m_V^4}$$

which saturates perturbative cross section needed for relic dark matter density at  $\sim$ GeV masses if mediator is W or Z,  
**new mediator is required for sub-GeV thermal dark matter!**

# LEE-WEINBERG BOUND

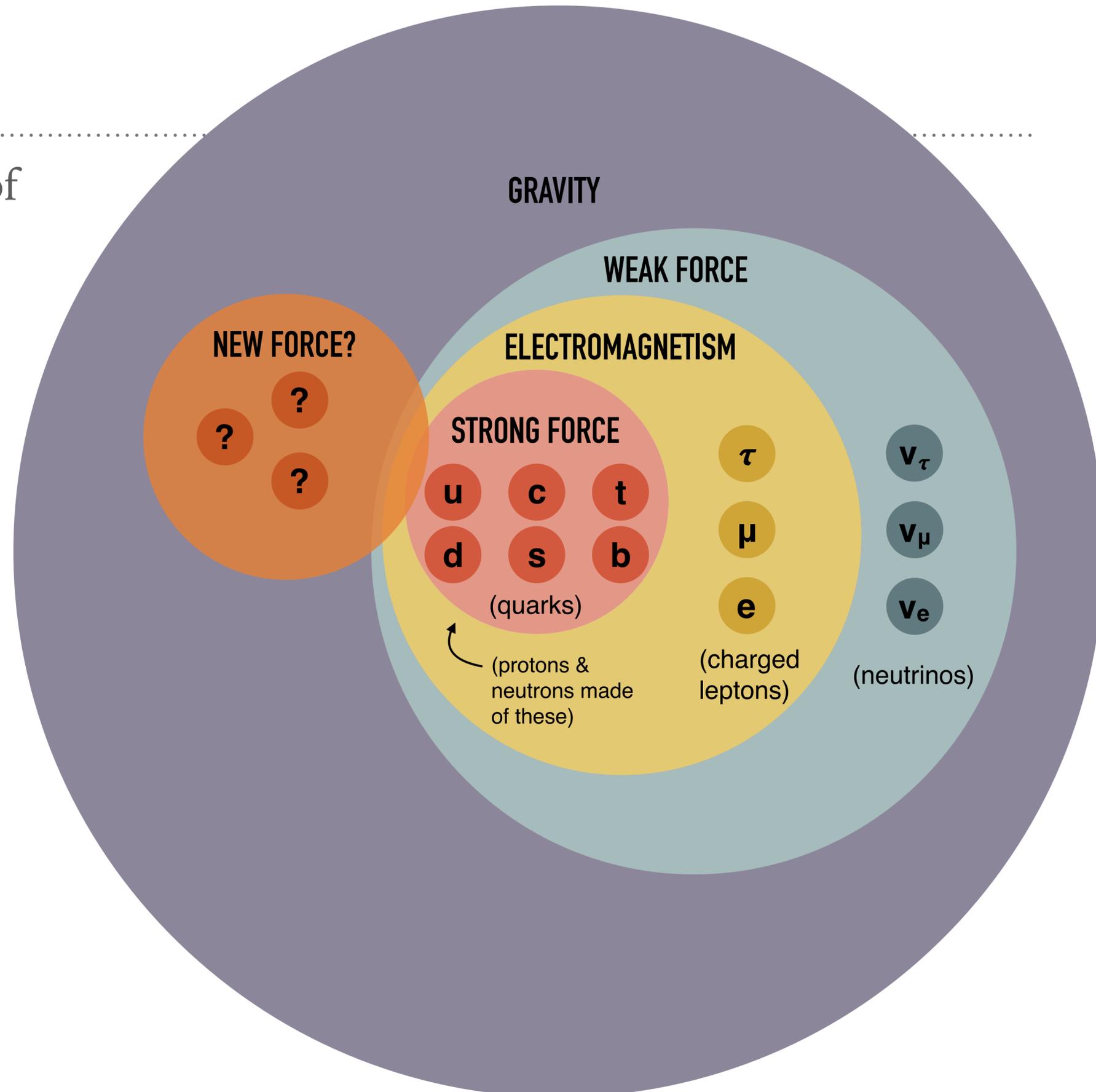
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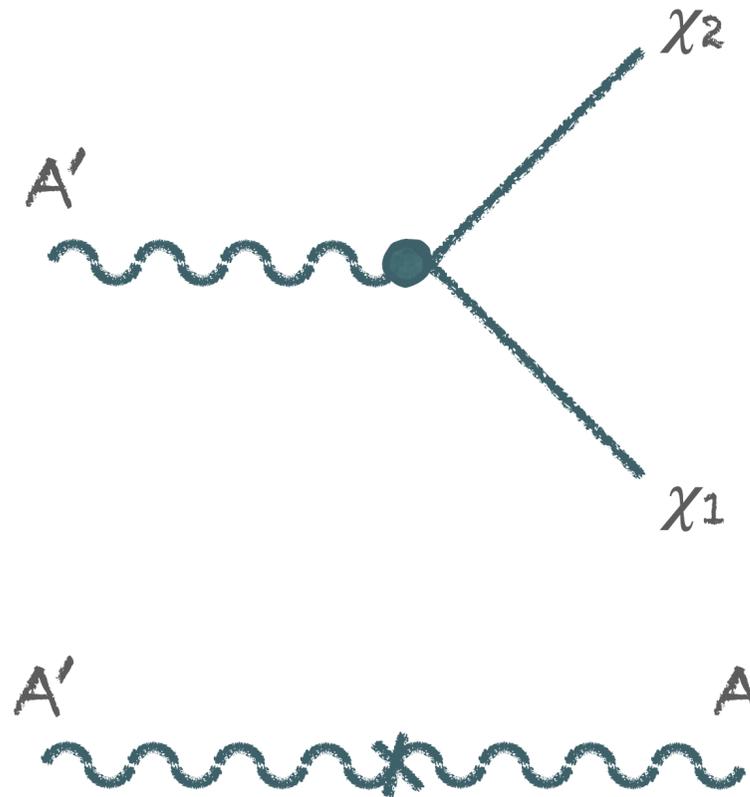
**PRESERVING THE SUCCESSES OF  
FREEZE-OUT AT LOWER DARK MATTER  
MASSES WITH DARK SECTORS**

# PSEUDO-DIRAC DARK MATTER

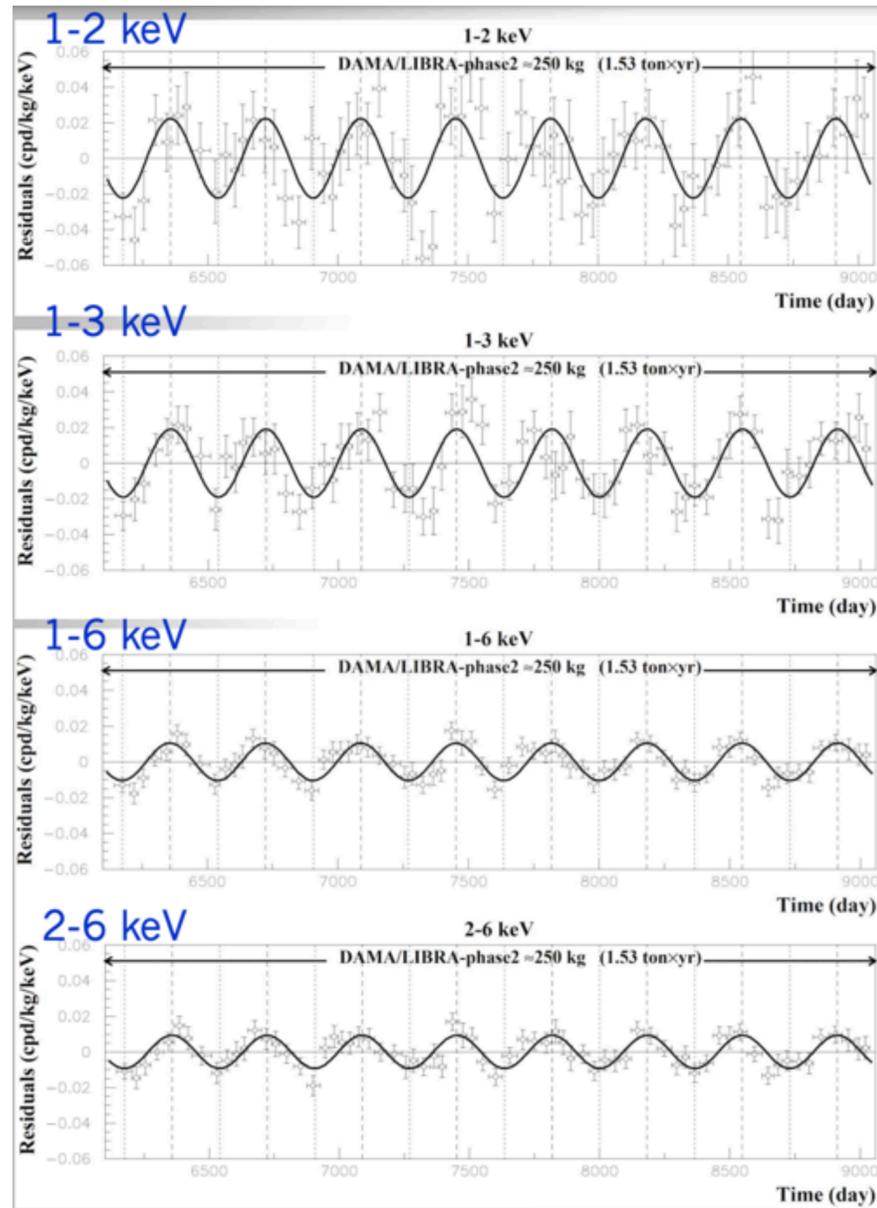
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- If dark matter is charged under a new gauge group, e.g. dark U(1), with a massive gauge boson (dark photon with mass coming from some symmetry breaking), Dirac dark matter multiplet will naturally split into multiple mass states  $\chi_1$  and  $\chi_2$  with small Majorana mass splitting  $\delta = m_2 - m_1$
- Majorana states don't carry conserved charge and couplings are off-diagonal (i.e. no state appears twice in vertex)  
Arkani-Hamed, Finkbeiner, Slatyer, Weiner  
“A theory of dark matter” (~2000 citations)

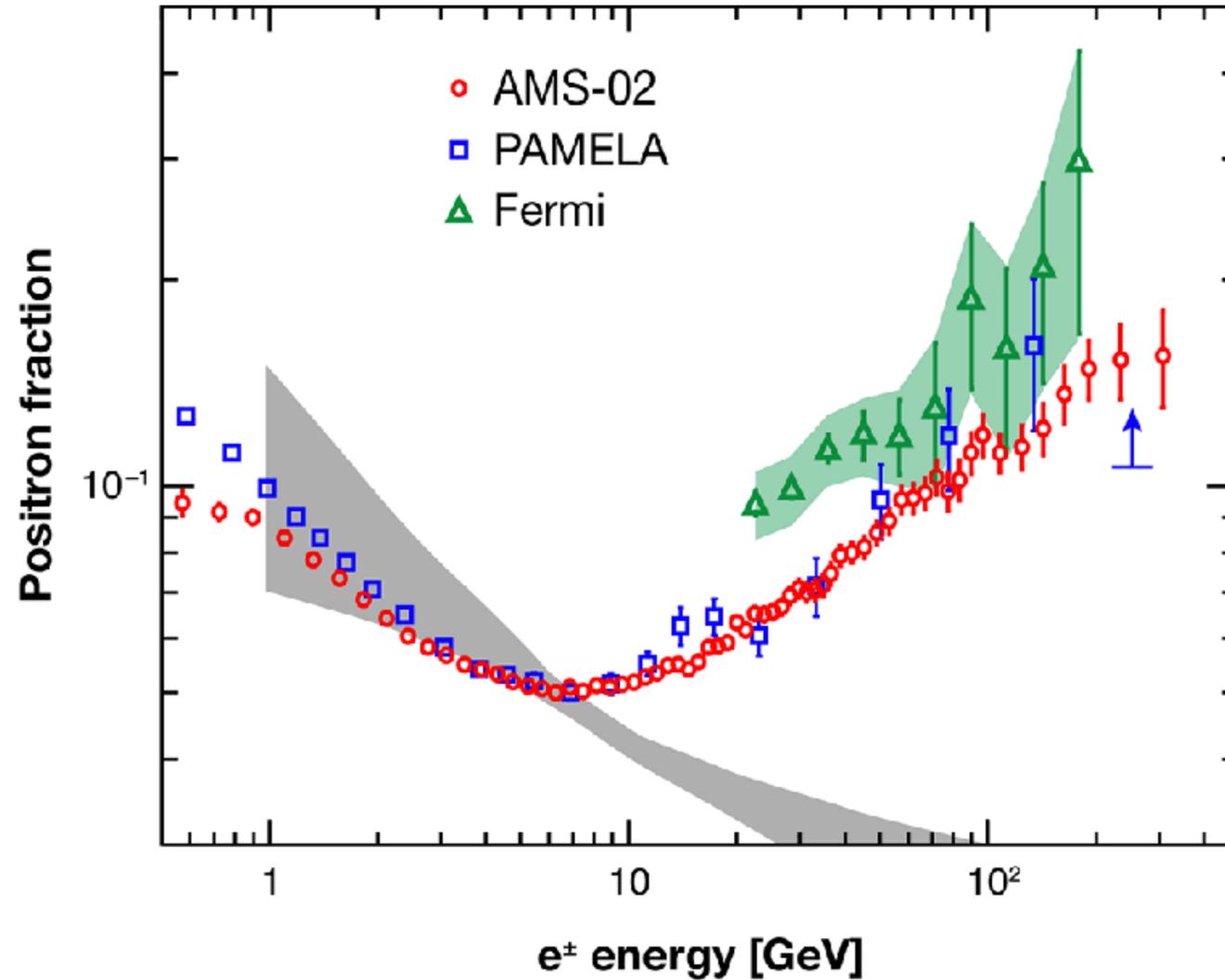
$$\mathcal{L} \supset \frac{\kappa}{2} F'_{\mu\nu} F^{\mu\nu} + ig_\chi A'_\mu \chi_2 \gamma^\mu \chi_1$$



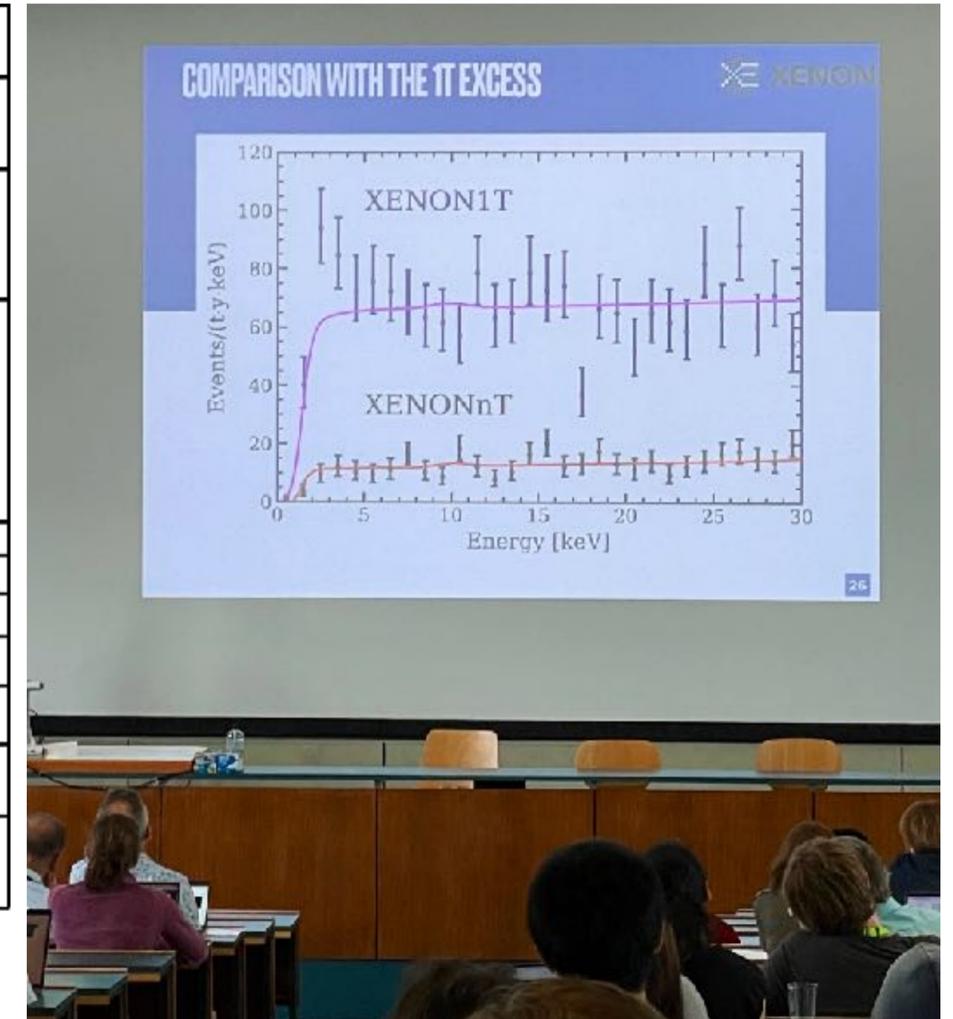
# PSEUDO-DIRAC DARK MATTER IS OFTEN INVOKED WHEN THERE ARE ANOMALIES



DAMA/LIBRA annual modulation  
e.g. Tucker-Smith & Weiner (2001)  
~1000 citations

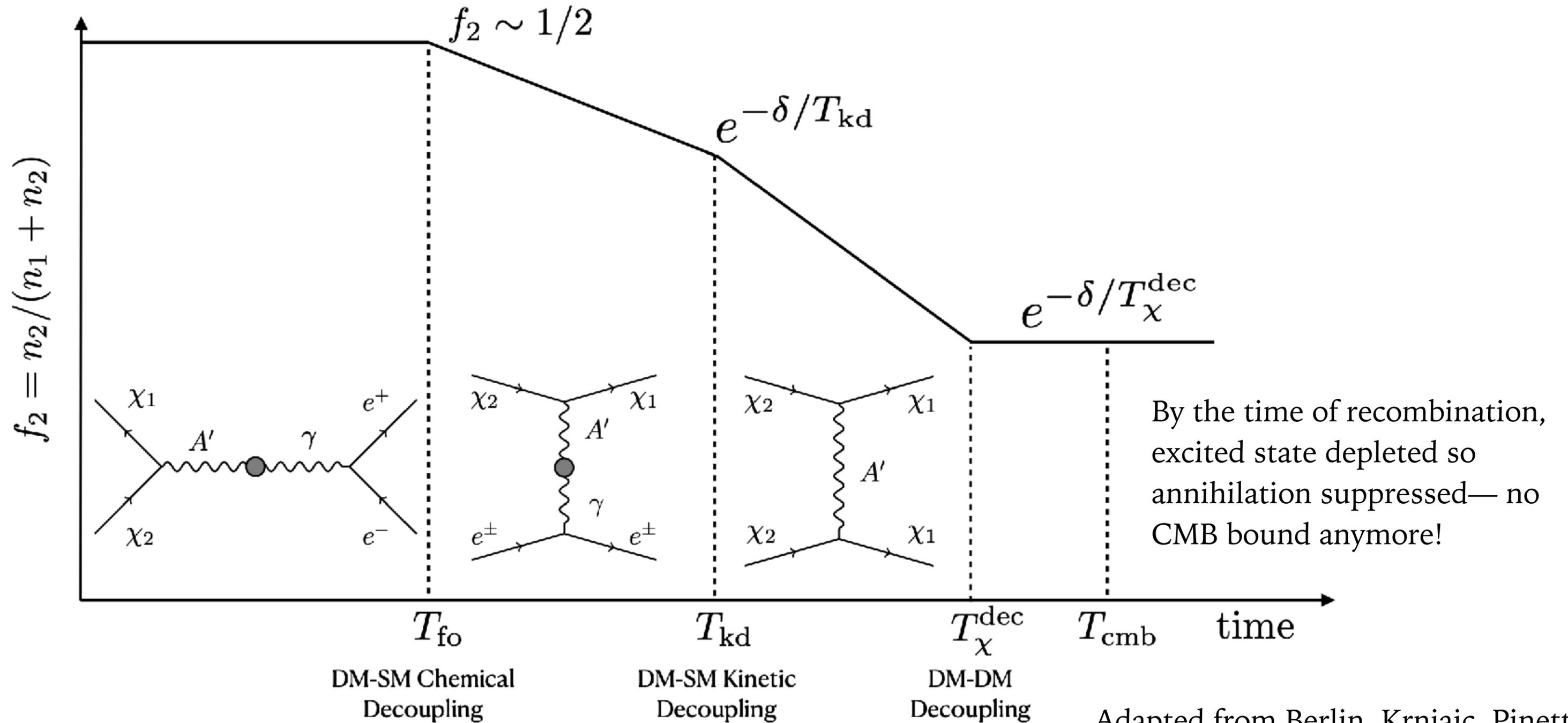


Rising positron fraction at high energies  
e.g. Arkani-Hamed et al. (2008)  
~2000 citations



XENON1T excess (photo I took at  
IDM during XENONnT talk)  
e.g. Baryakhtar et al. (2020)  
An et al. (2020)  
~100 citations

# FREEZE-OUT OF PSEUDO-DIRAC DARK MATTER



Adapted from Berlin, Krnjaic, Pinetti

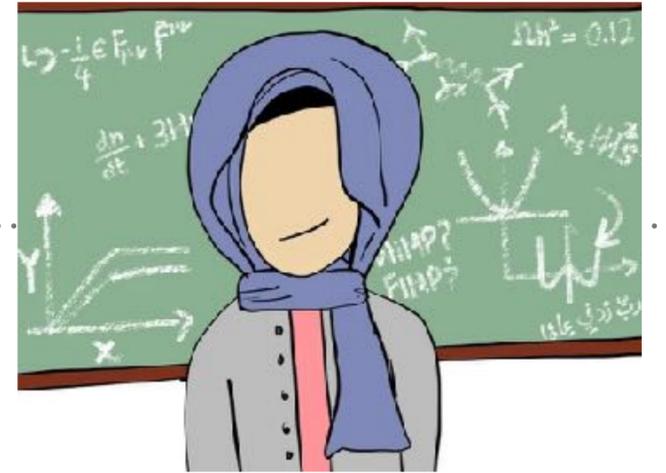
**HAS THE PARAMETER SPACE FOR THIS WELL-STUDIED MODEL BEEN MAPPED SYSTEMATICALLY?**

**HAVE OBSERVABLES BEEN TREATED HOLISTICALLY WITH COMPLEMENTARITY IN MIND?**

# NO! PLAN FOR REST OF TALK

---

- Discuss a few regions of pseudo-Dirac dark matter parameter space where the thermal history and observables have not been well-characterized:
  - If the mediator is close to twice the dark matter mass, freeze-out is resonant which substantially changes allowed couplings, mass splittings (Brahma, Heeba, **KS** 2308.01960)
  - Dark matter could scatter exothermically/endothermically, altering the structure of small galaxies (O'Neil, Vogelsberger, Heeba, **KS**, et al. *MNRAS* 2023)
  - If the couplings are very small, freeze-in thermal history is possible and excited state becomes cosmologically metastable, decaying at late times (Heeba, Lin, **KS** *PRD* 2023)



Dr. Saniya Heeba



Nirmalya Brahma

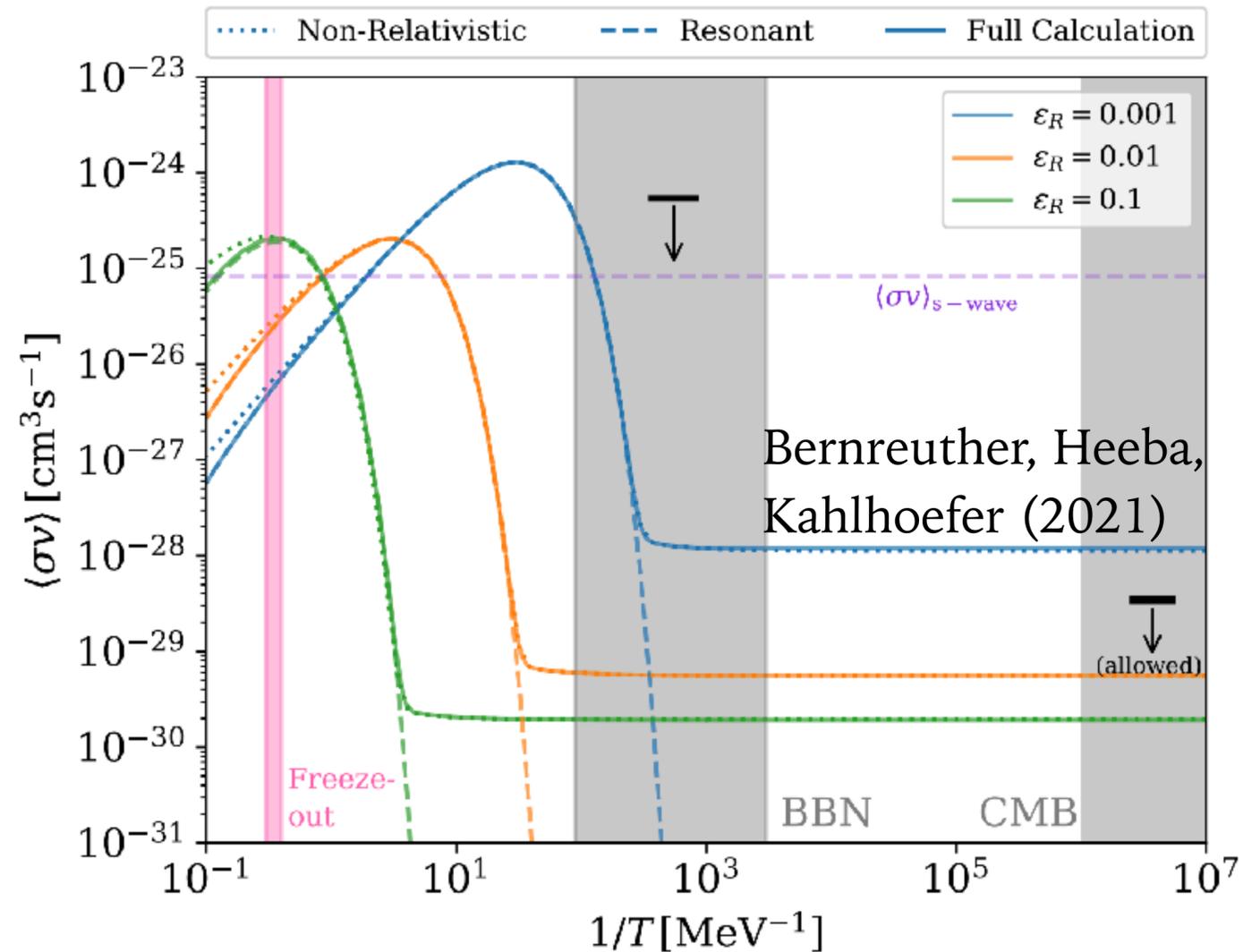


Stephanie O'Neil

# **RESONANT INELASTIC DARK MATTER**

# IS IT POSSIBLE TO HAVE SMALL MASS SPLITTINGS CONSISTENT WITH THE CMB?

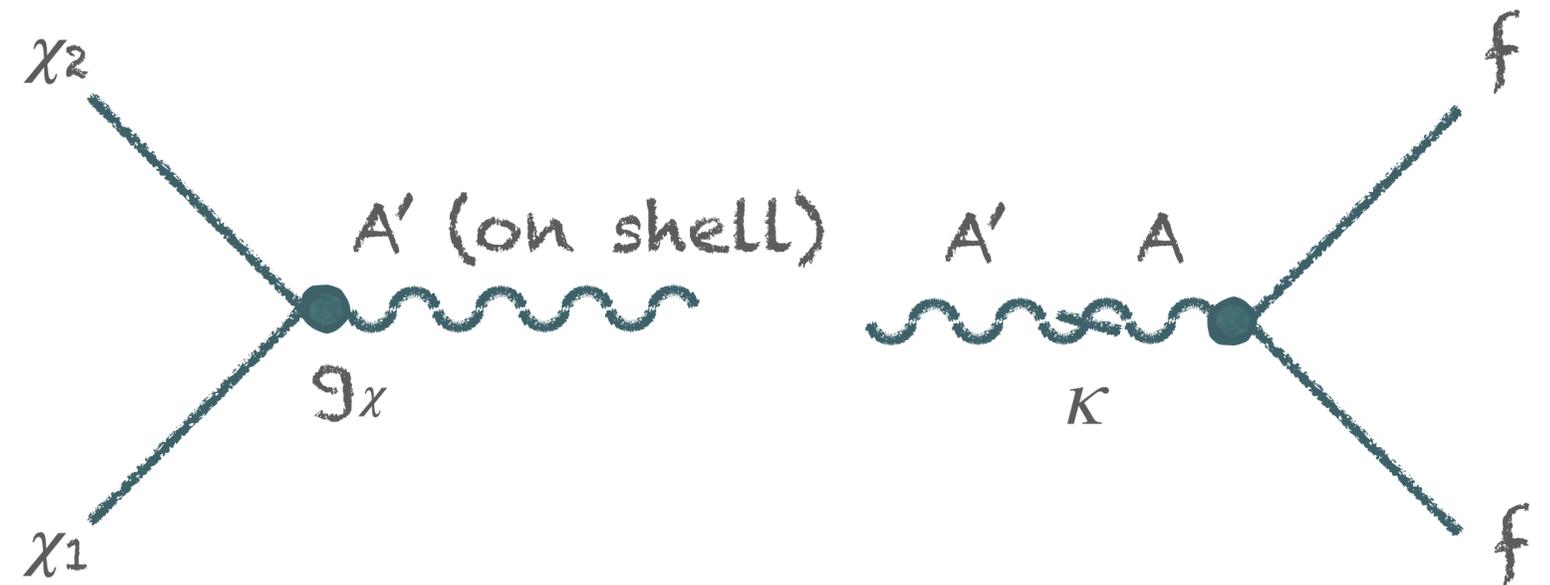
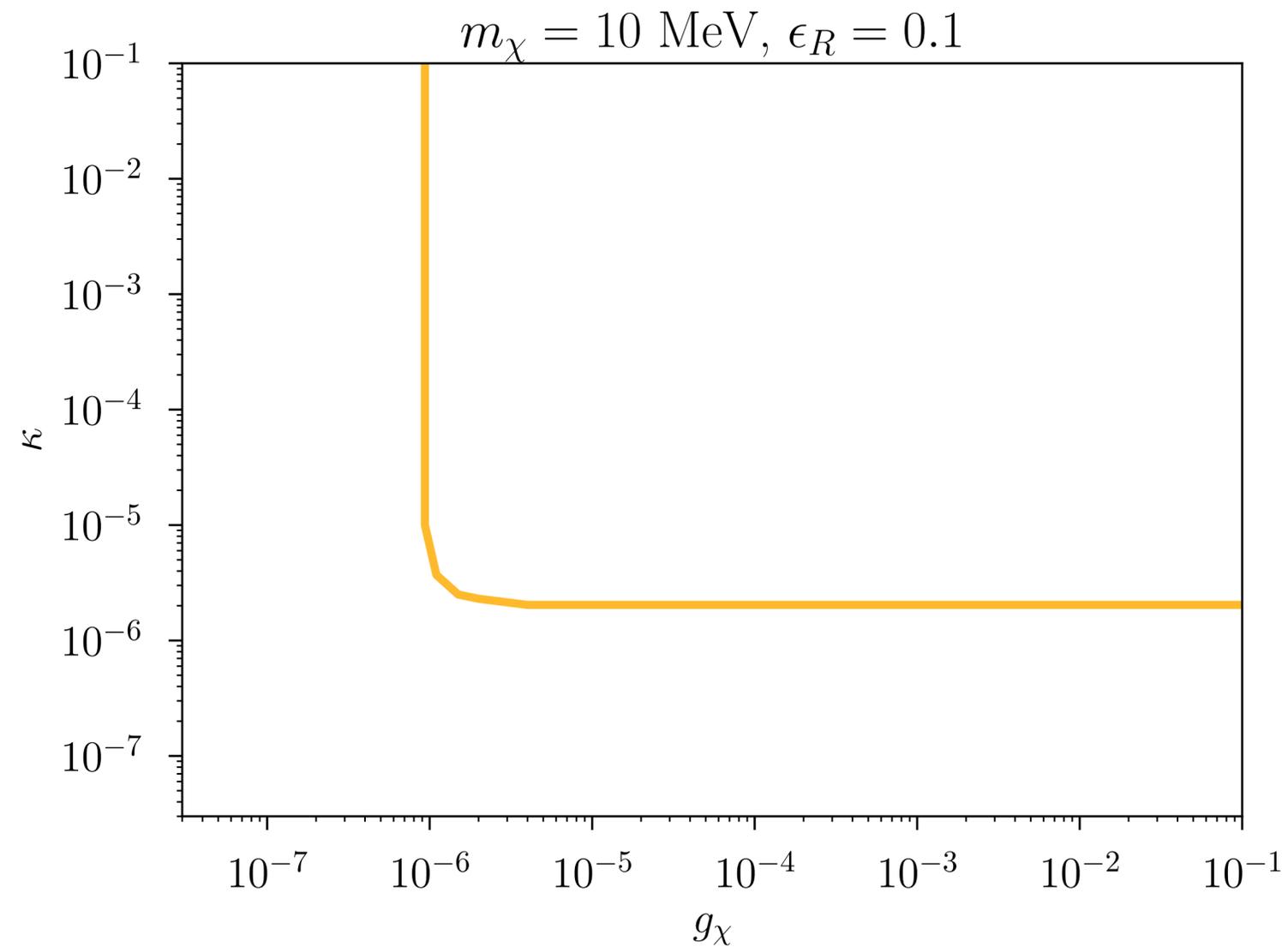
- Usually by the time of recombination, if the mass splitting isn't much bigger than an eV then the excited state won't be very thermally depleted
- If the excited state is around, then small amount of it will annihilate with ground state and mess up the CMB... unless! What if there is a strong velocity dependence to annihilation so it happens a lot during freeze-out but not at late times?
- If mediator is resonant with around twice the mass of the dark matter, a lot of dark matter can be produced on resonance for *very* small couplings so that annihilation is very inefficient off resonance
- But... we can't be too resonant! Otherwise that delays the dark matter annihilation into an era when cosmic calorimetry is relevant



$$\epsilon_R = \frac{m_{A'}^2 - 4m_\chi^2}{4m_\chi^2} = \frac{m_{A'}^2 - s_{\min.}}{s_{\min.}}$$

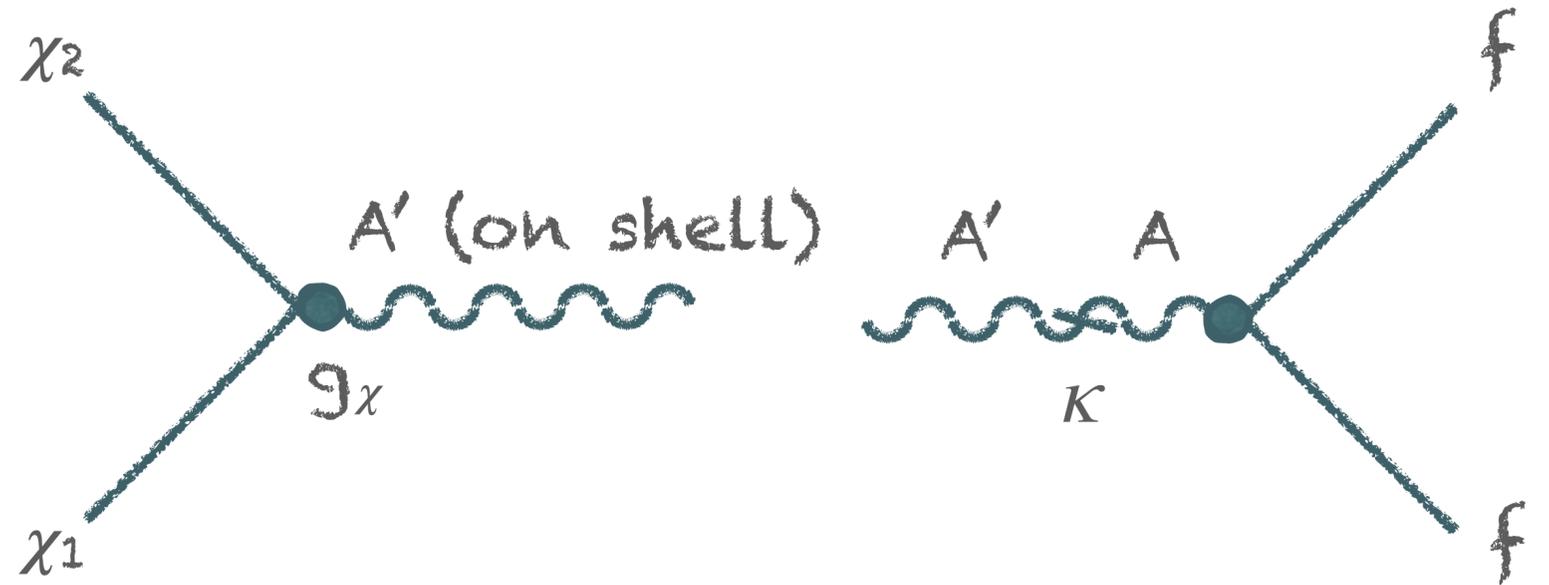
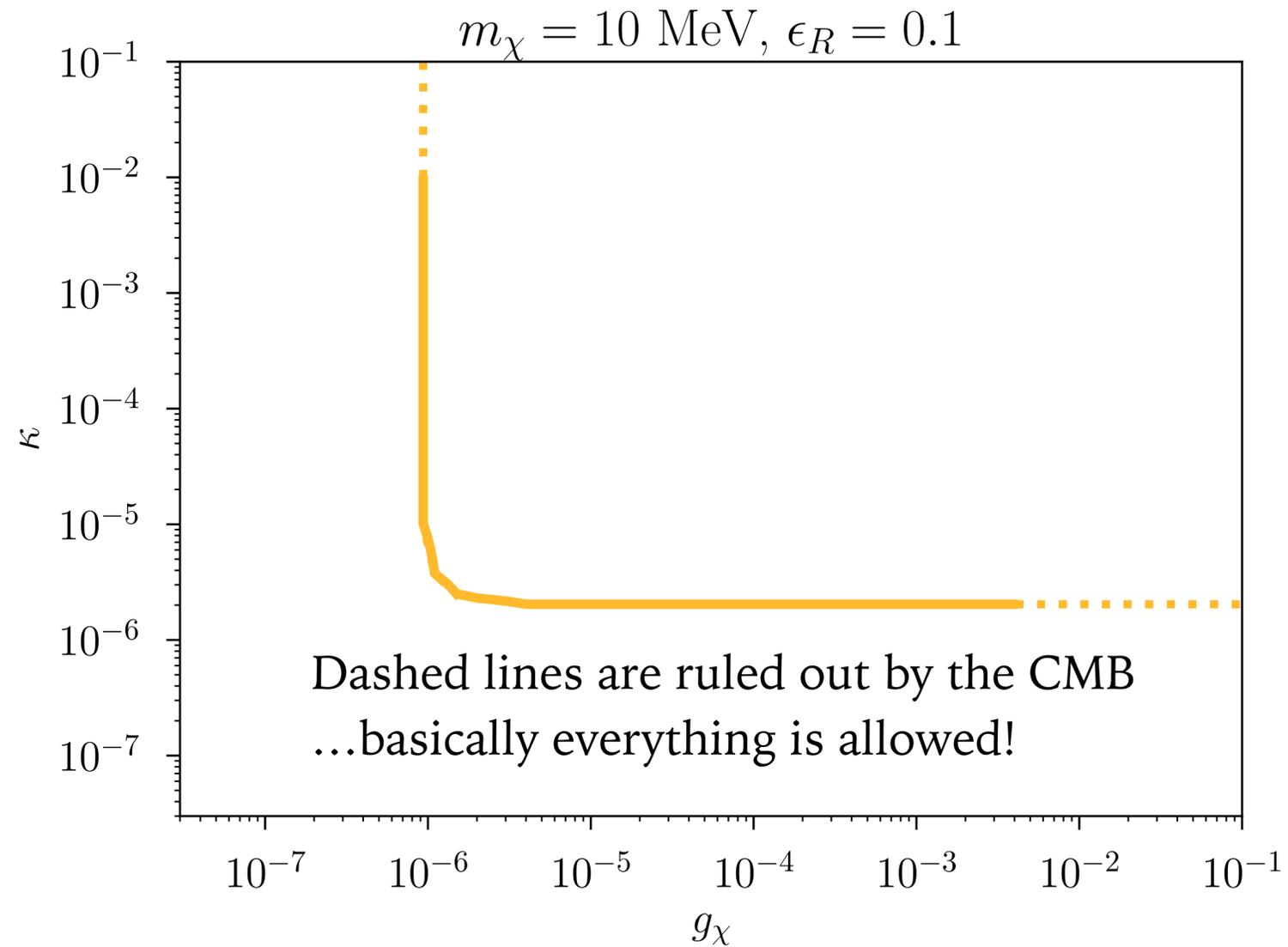
Too much fine-tuning is ruled out by cosmology!

# PARAMETER SPACE SETTING THE RELIC ABUNDANCE



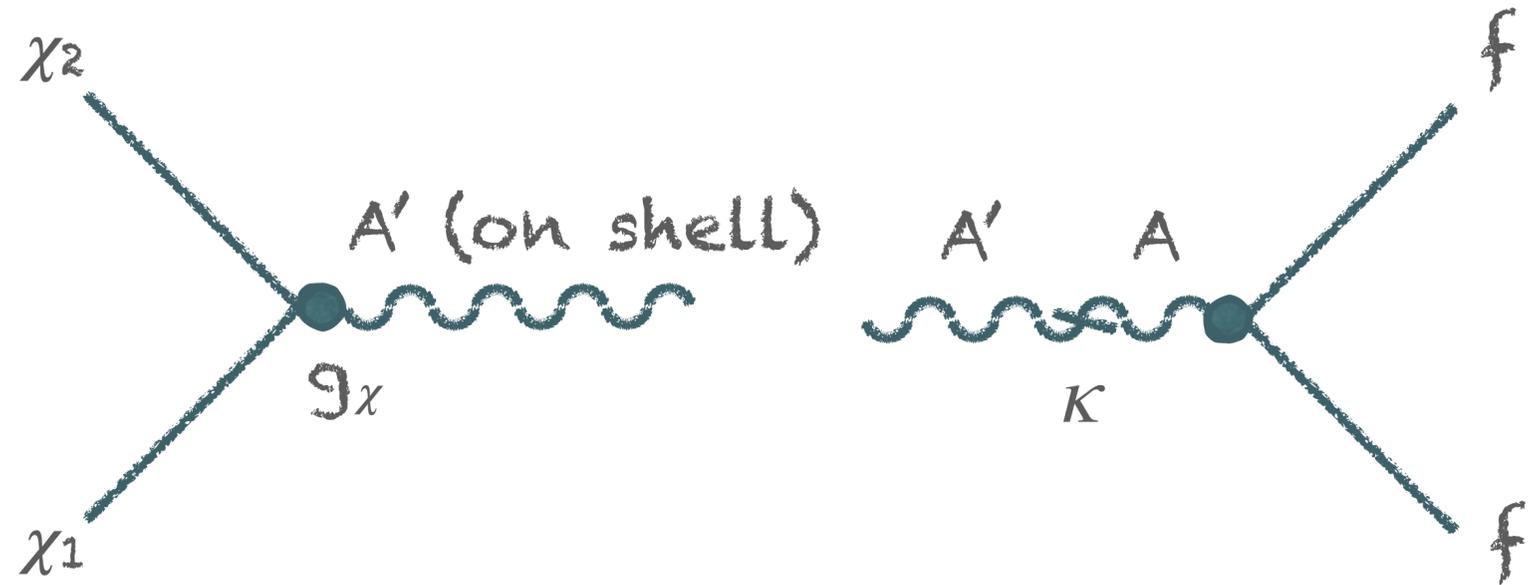
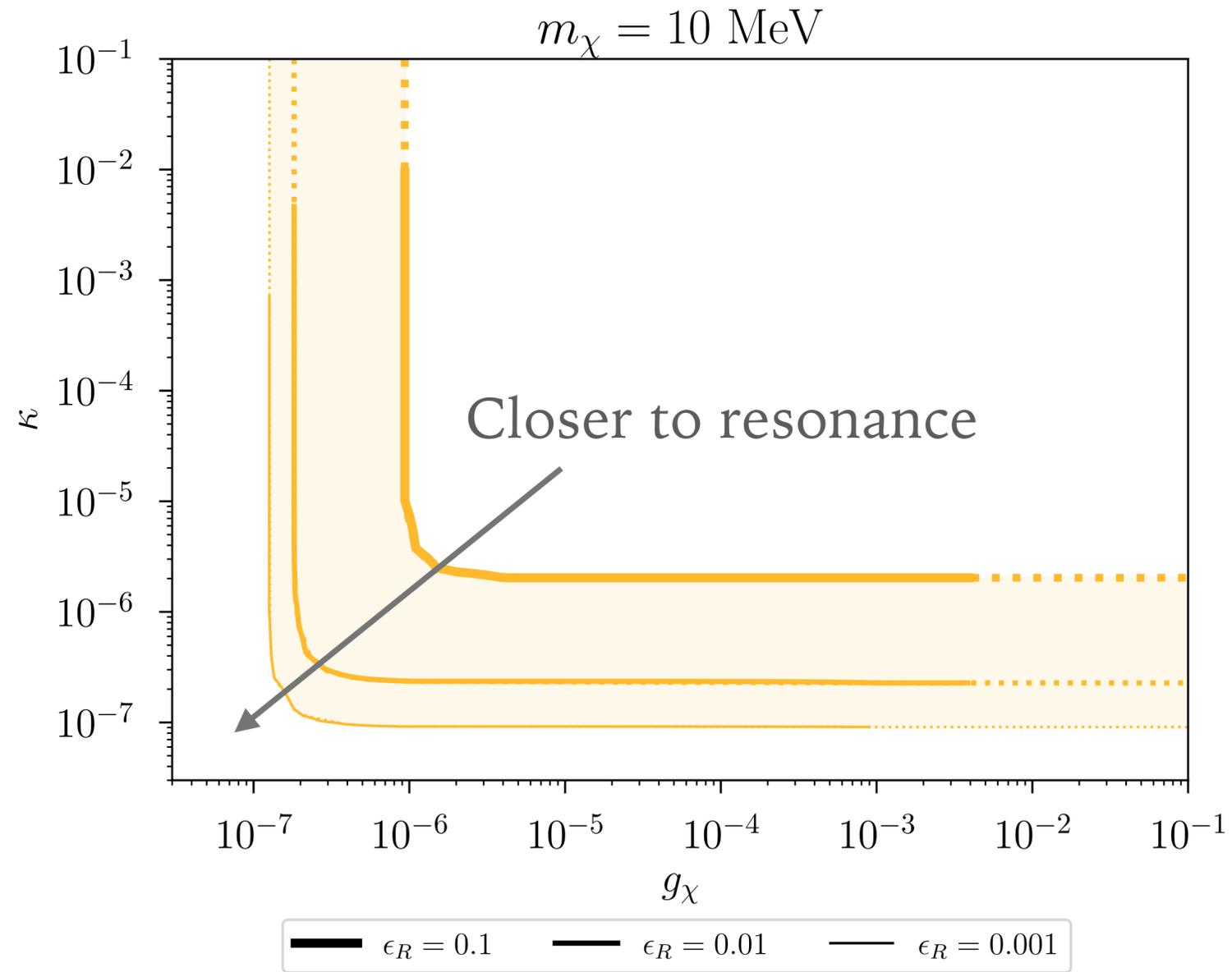
Whichever step is slower controls the rate, so relic abundance only depends on one coupling or the other

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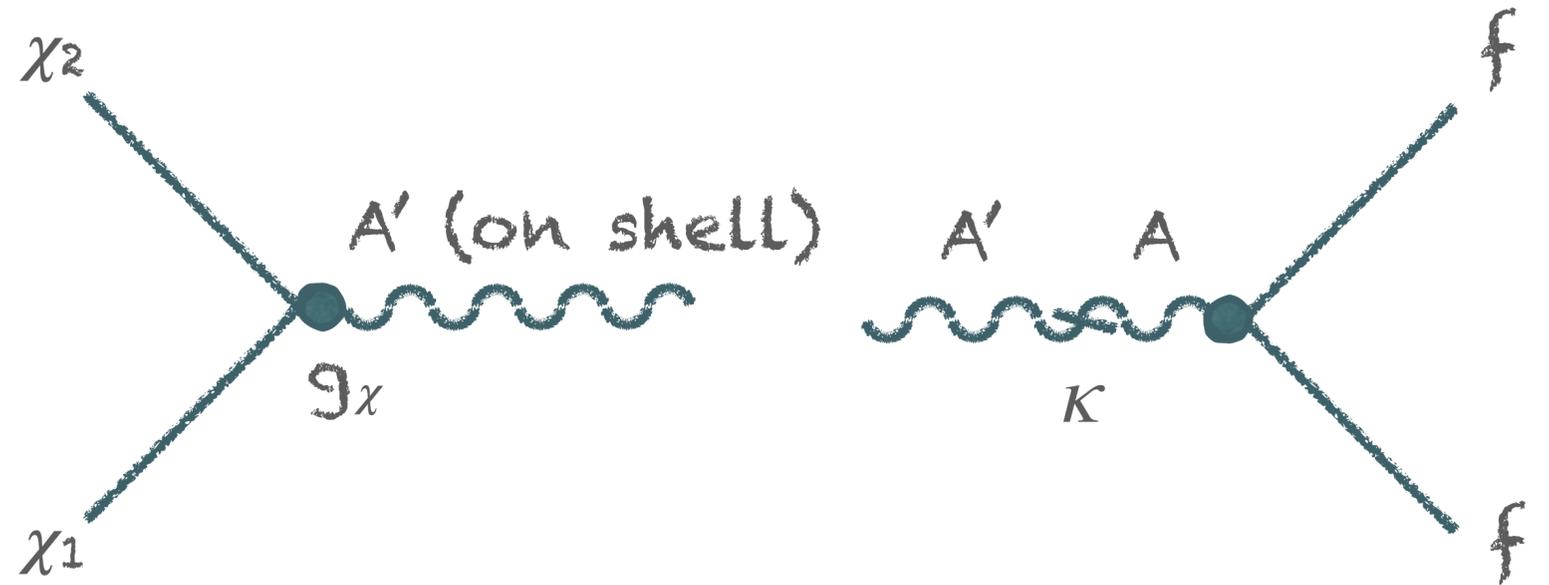
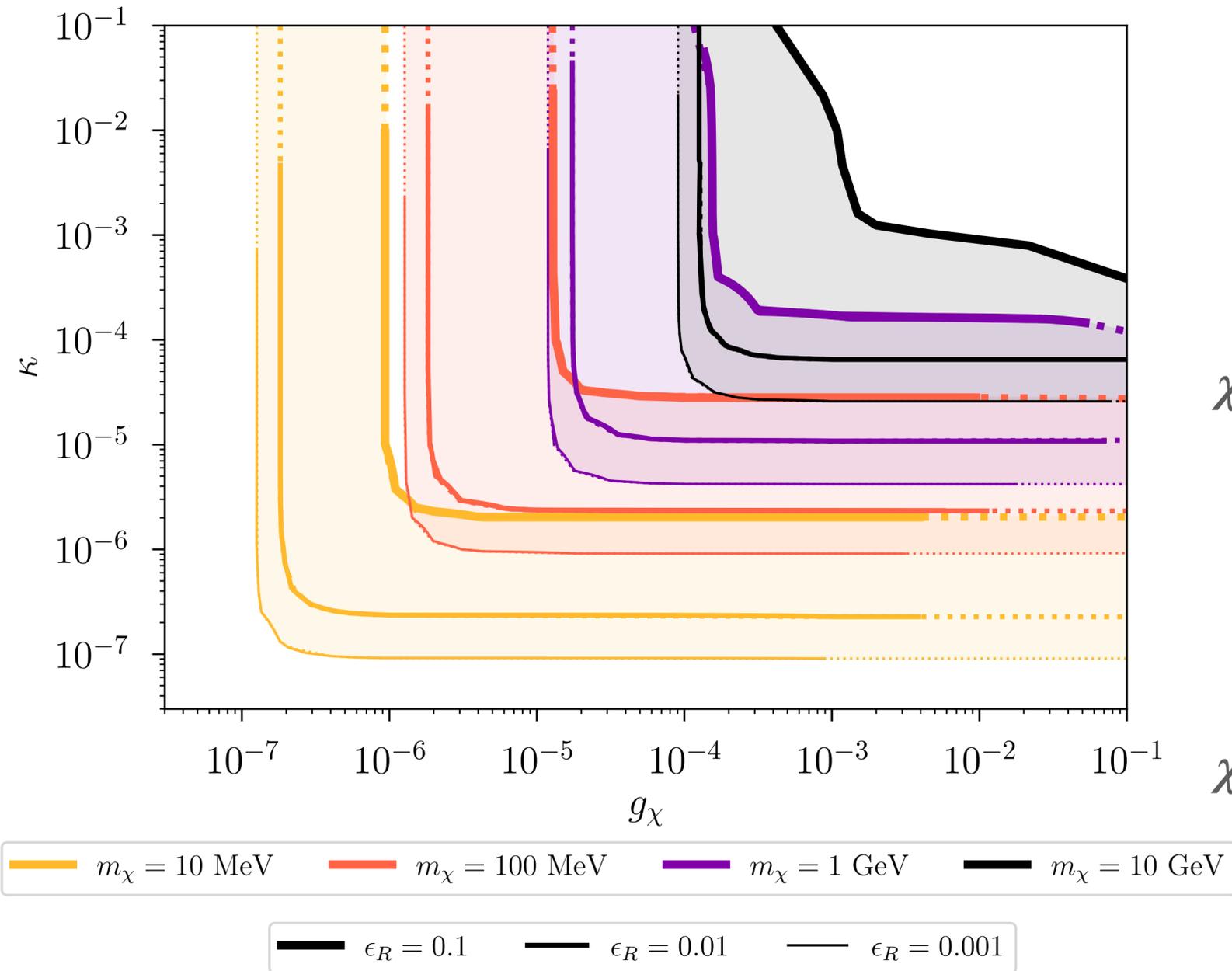


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Brahma, Heeba, **KS 2308.01960**

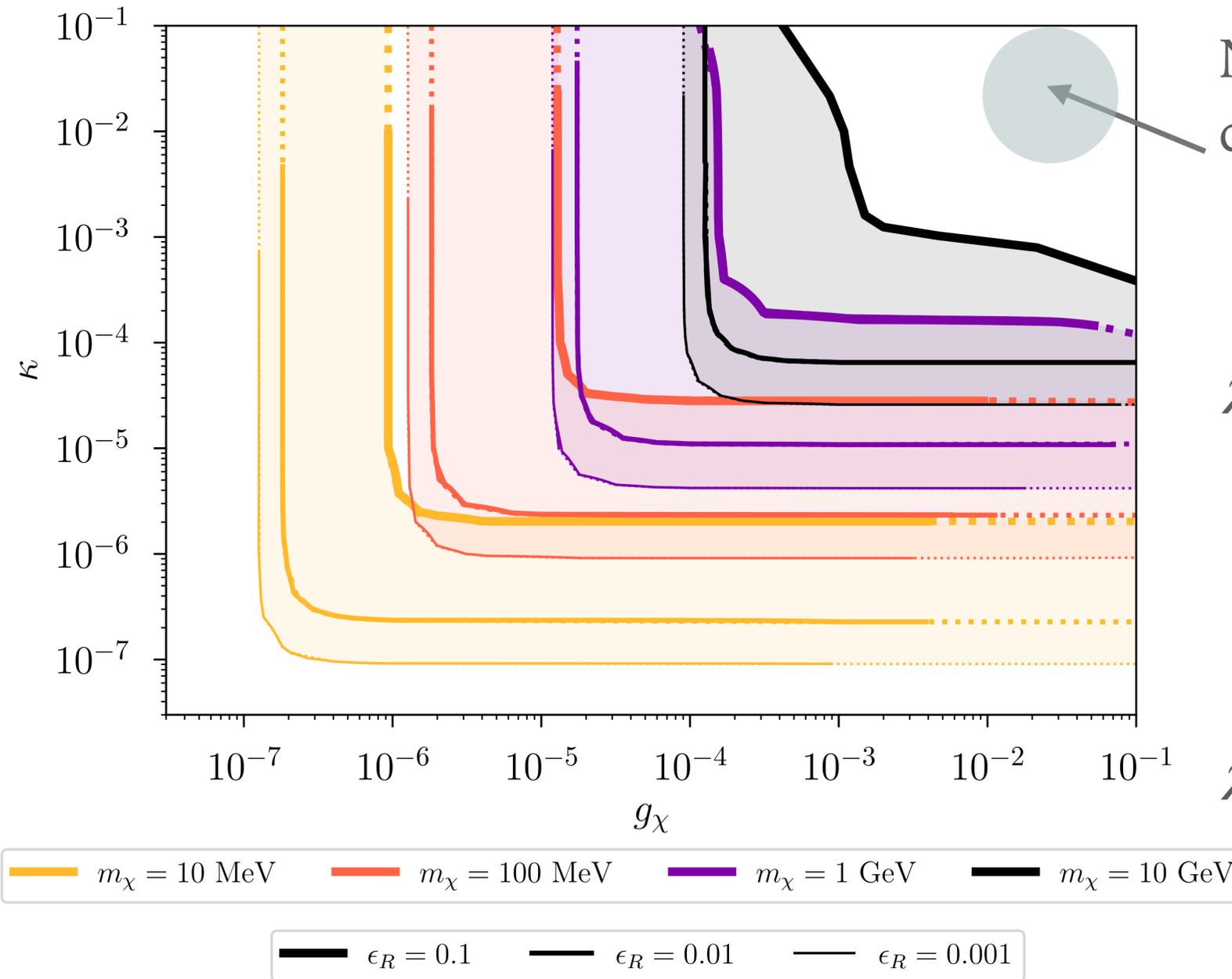
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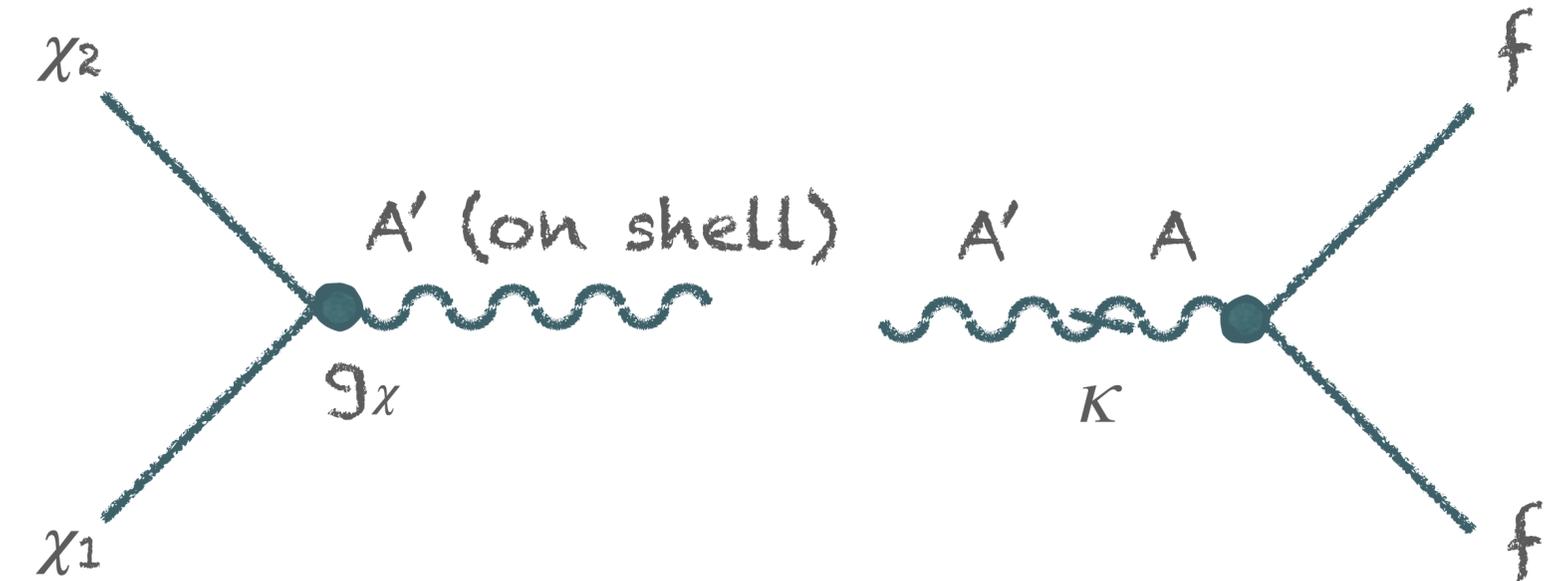


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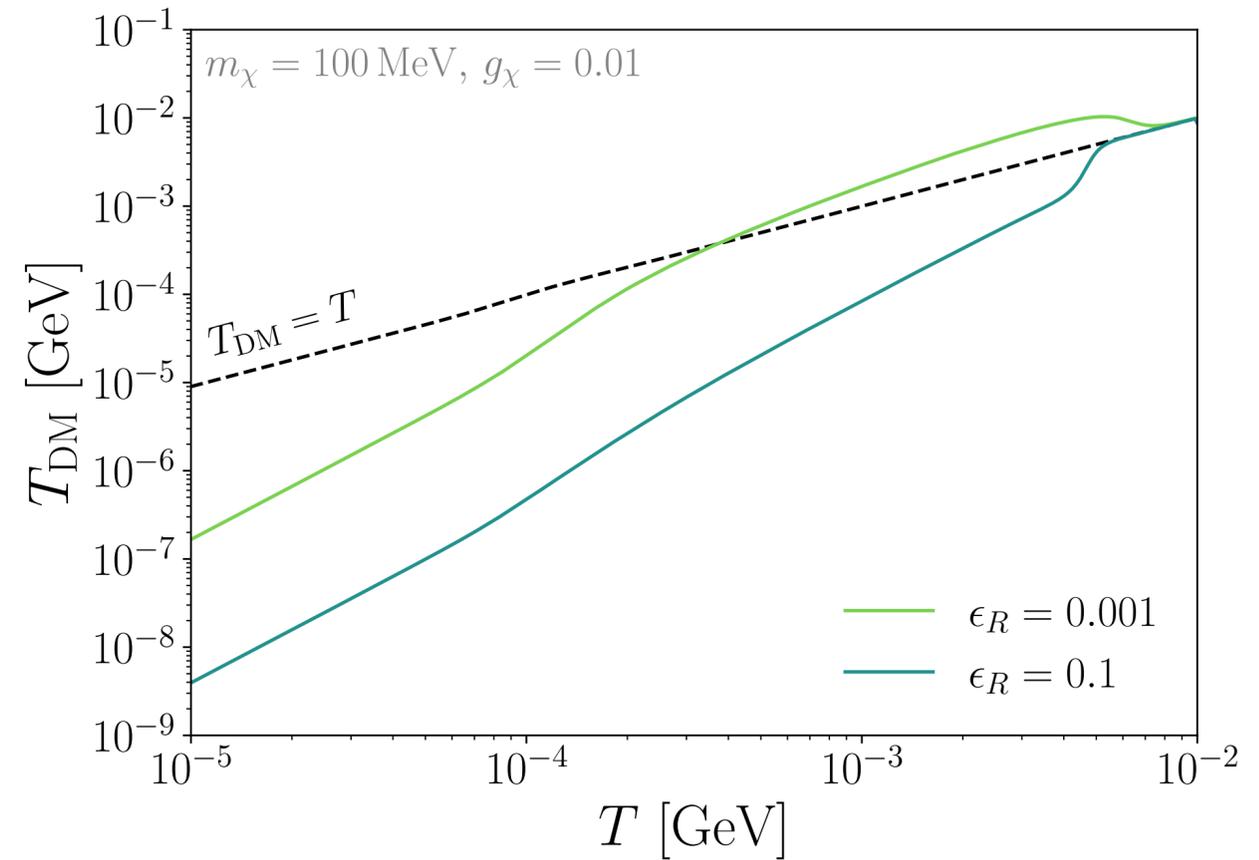
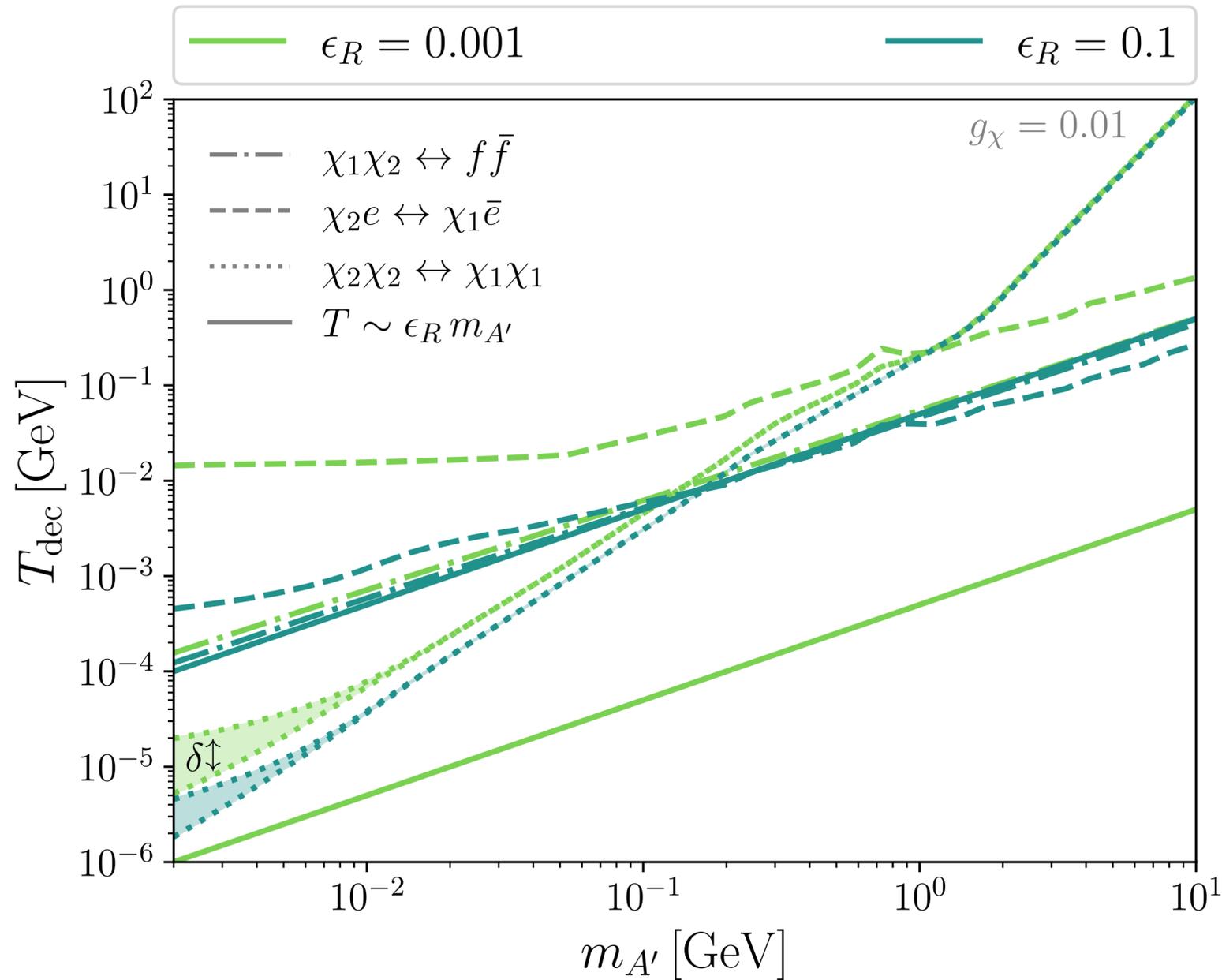


Non-resonant freeze-out cross sections live here



Whichever step is slower controls the rate, so relic abundance only depends on one coupling or the other

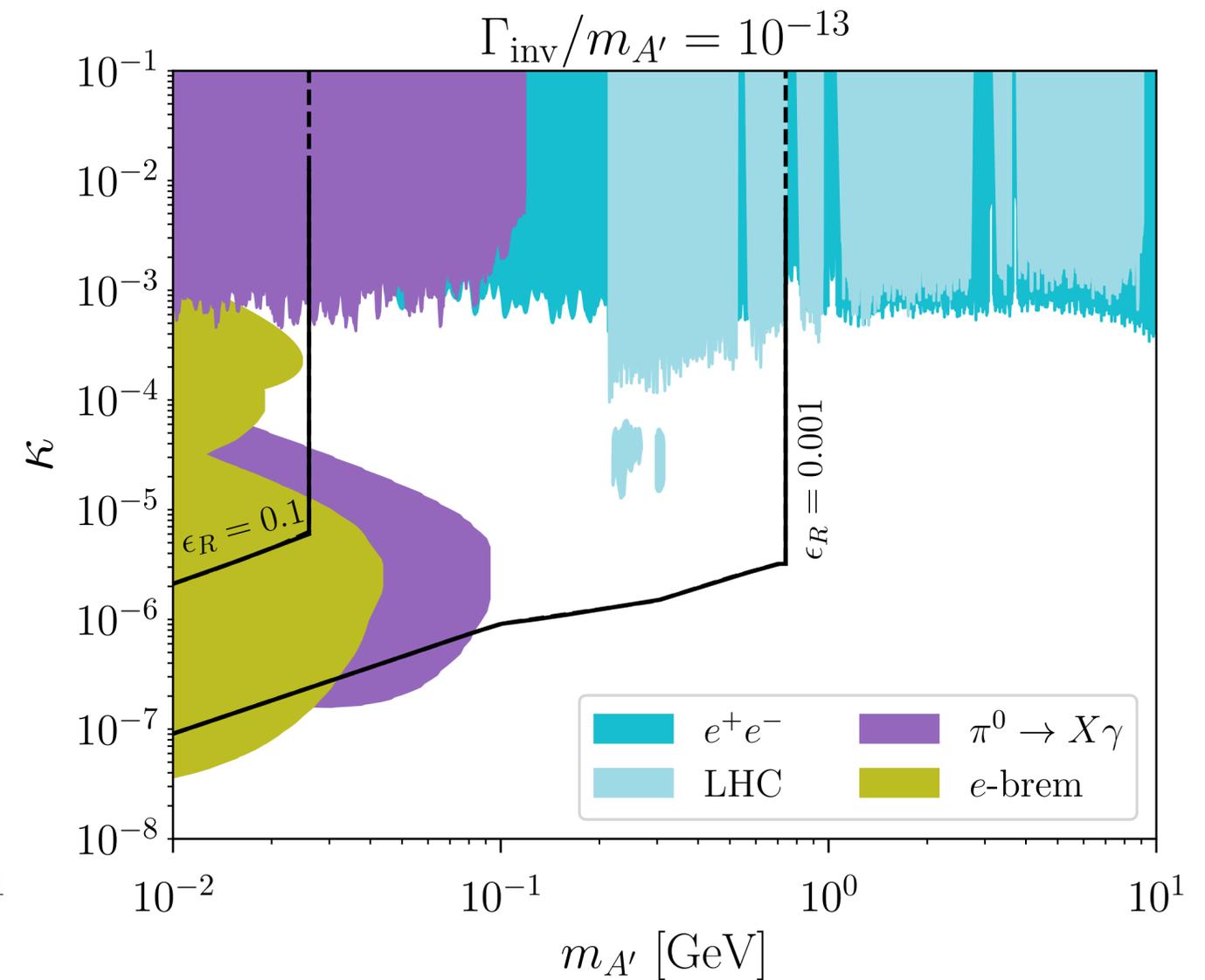
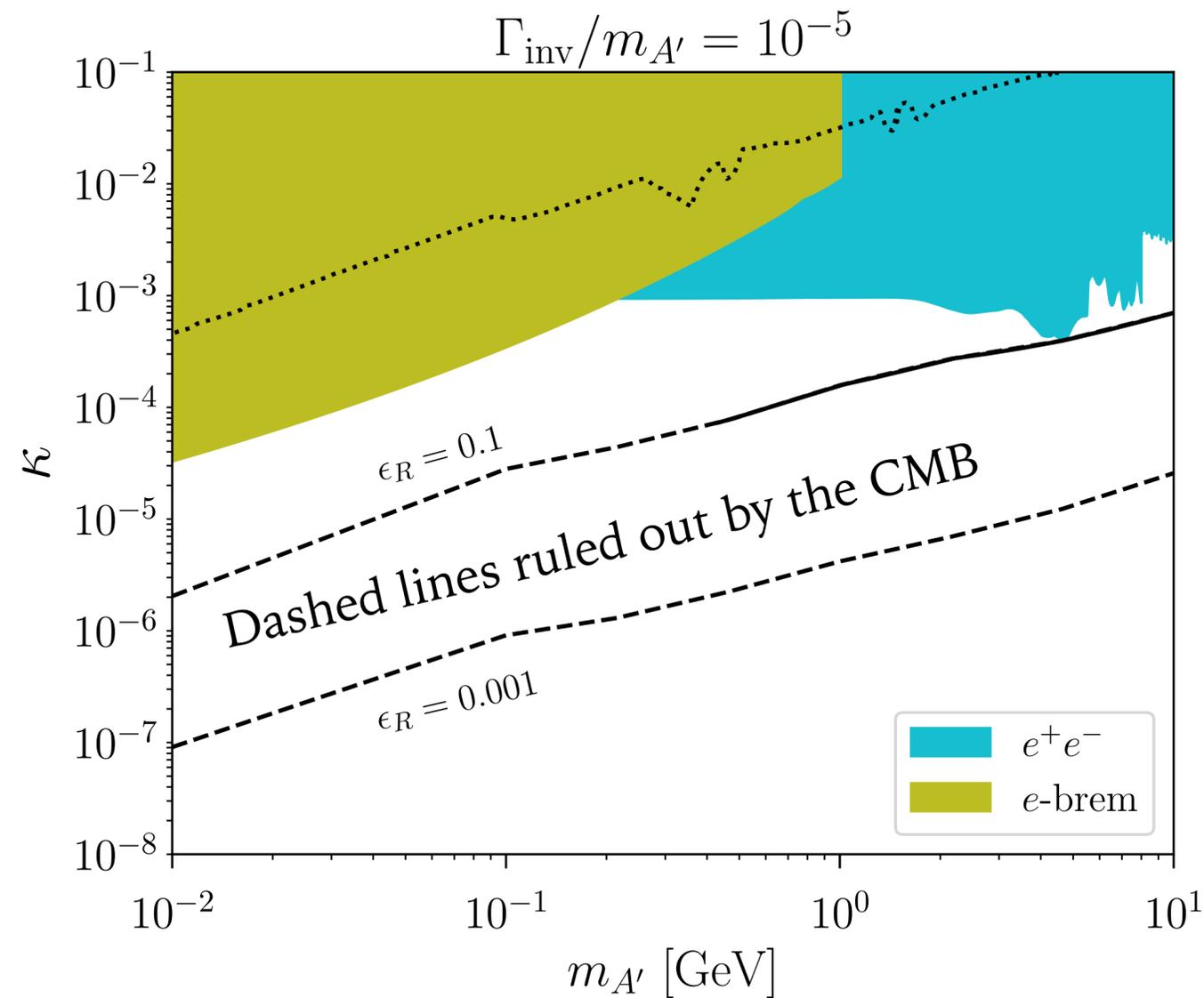
# UNUSUAL THERMAL HISTORY FOR RESONANT DARK MATTER



- The couplings can be so tiny that the dark matter kinetically decouples from the SM before it's done annihilating, temperature evolves very differently from SM temperature!
- Have to solve full coupled Boltzmann equations (not just one for dark matter density) to capture full behavior

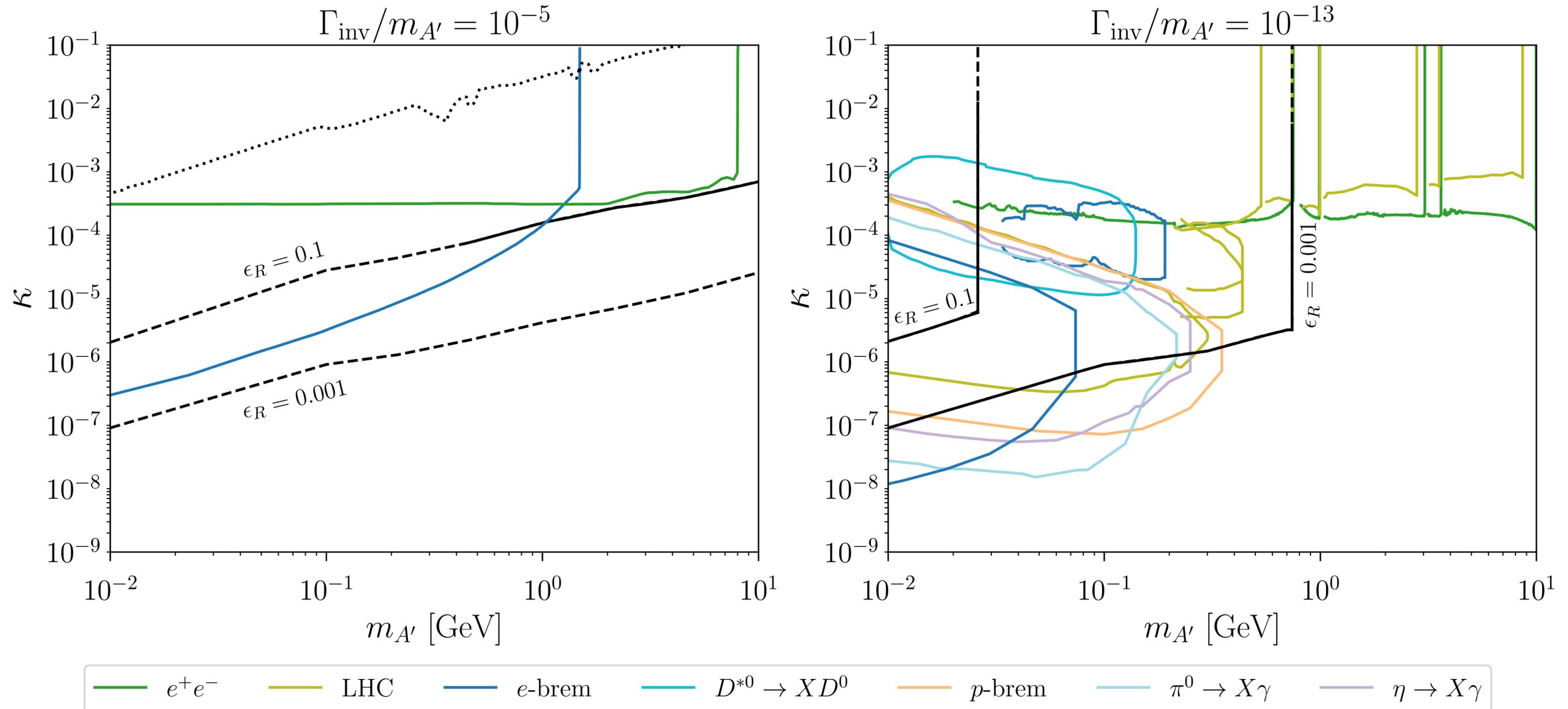
# TERRESTRIAL CONSEQUENCES OF THERMAL HISTORY

Limits computed with DarkCast,  
Ilten et al. (2018)

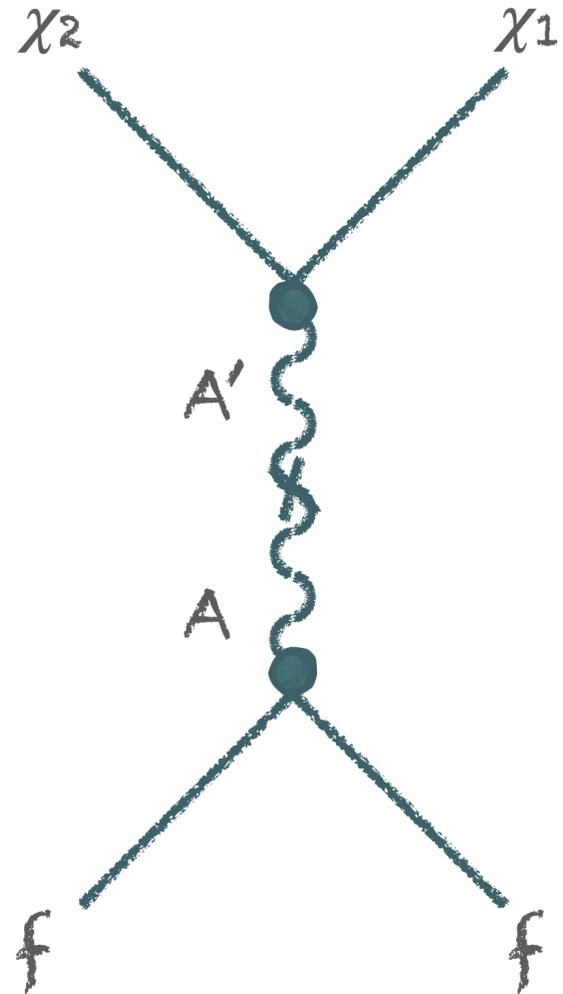


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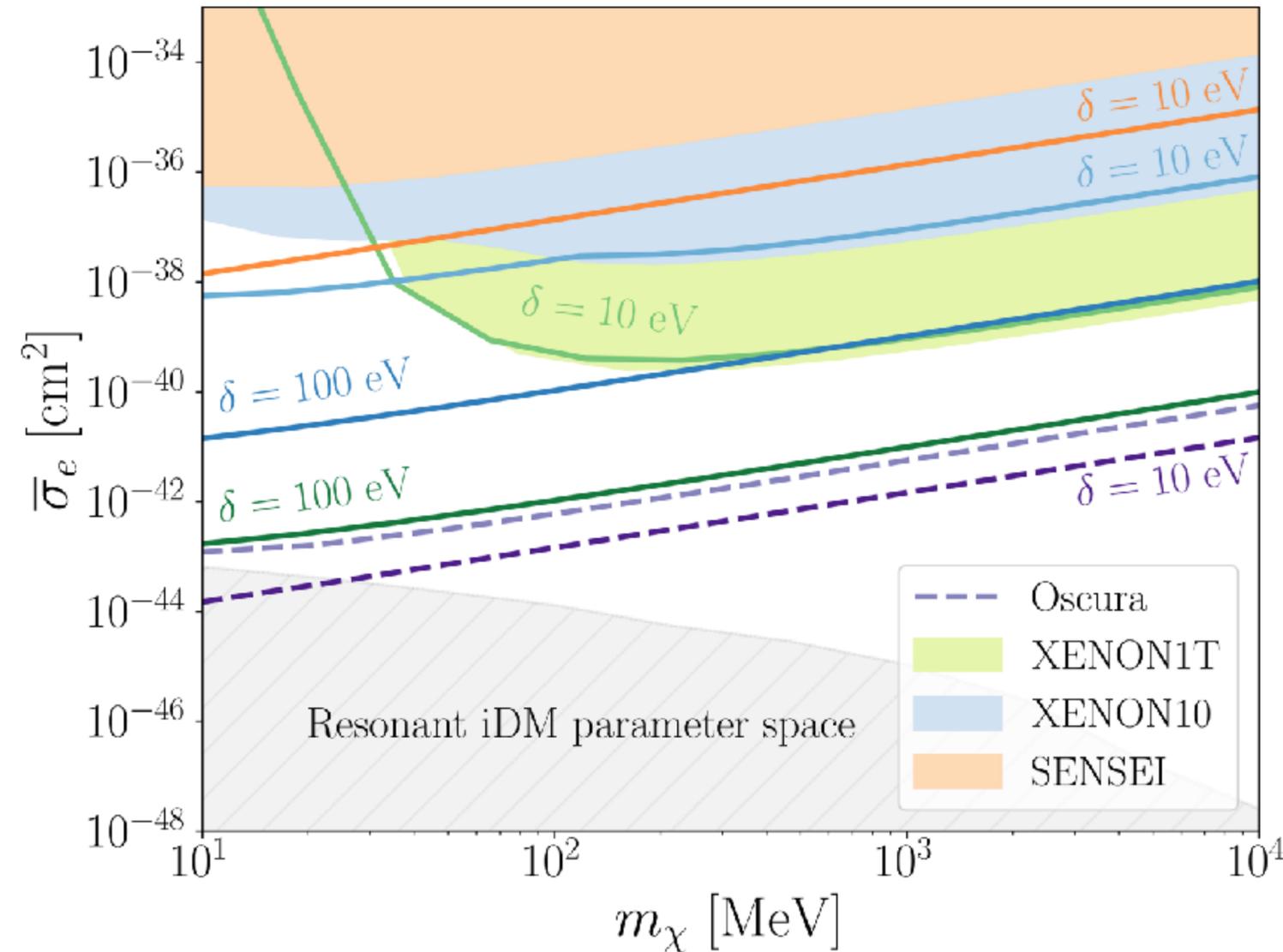
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# SIGNATURES OF THE COSMOLOGICALLY PRESENT EXCITED STATE



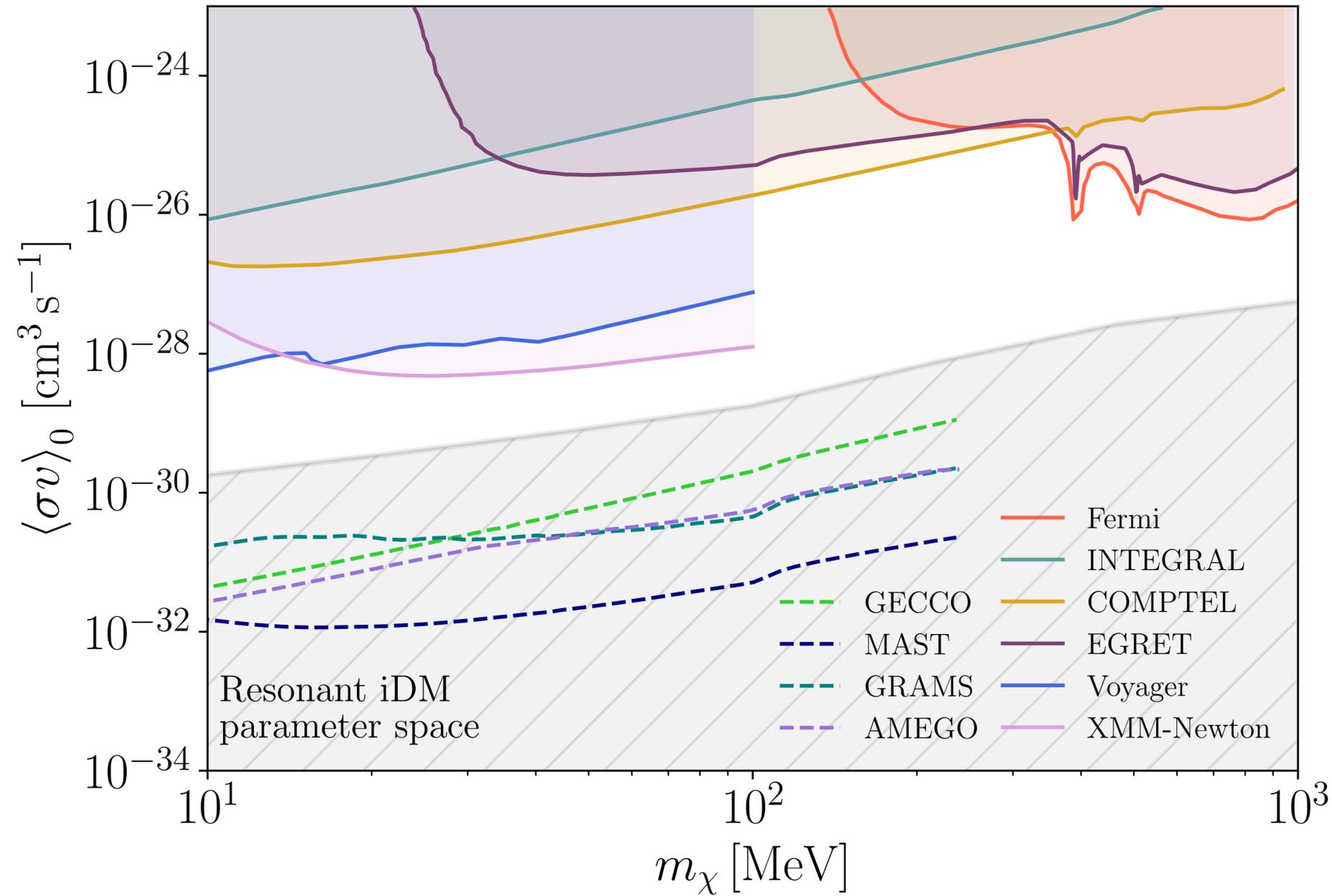
Relic excited state is unique to this case (usually it's very depleted) and can deposit energy differently in direct detection



Reach extends to lower DM masses because mass splitting overcomes Milky Way kinematics... still hard to target due to small couplings but not crazy

Brahma, Heeba, **KS 2308.01960**

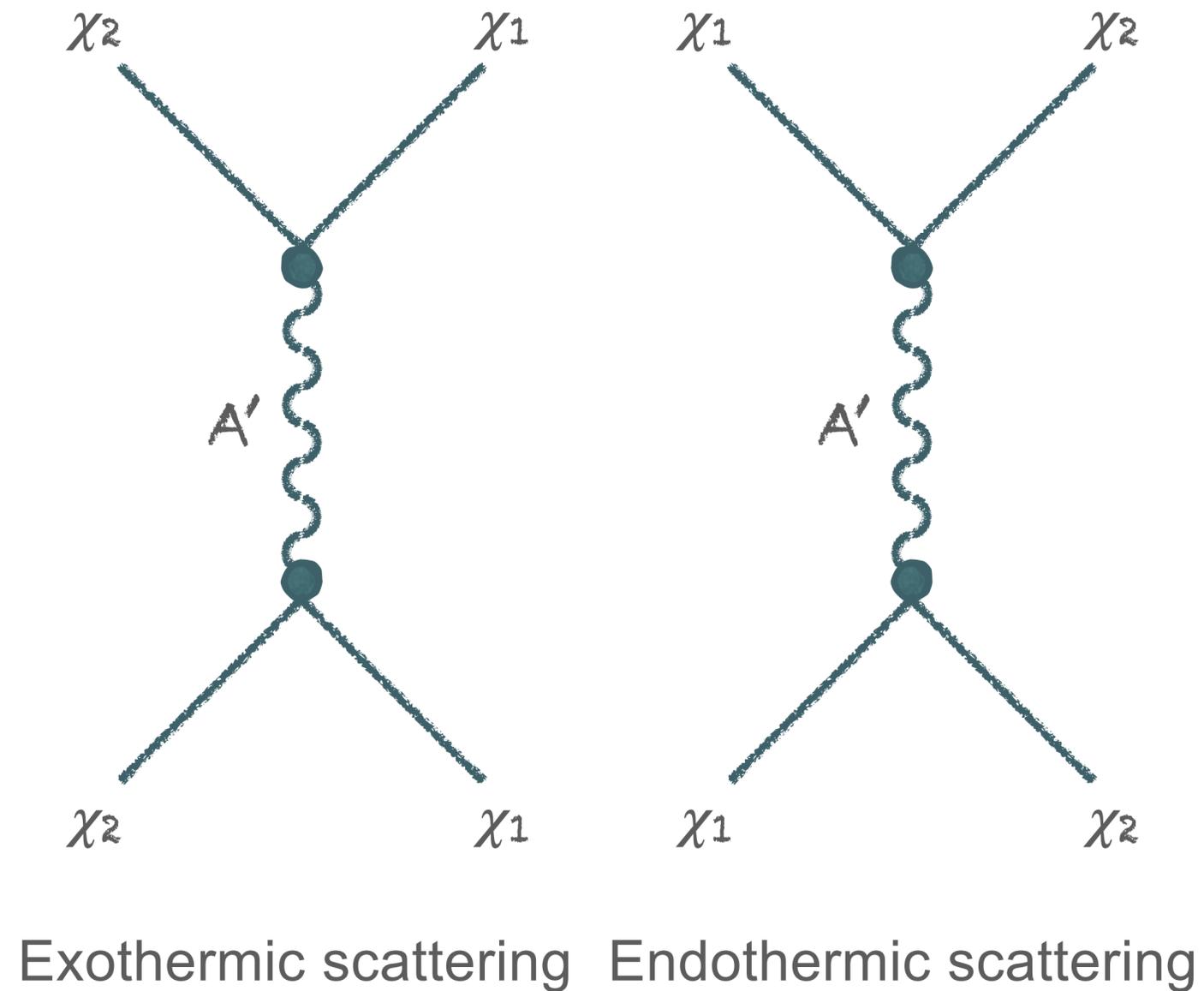
# SIGNATURES OF THE COSMOLOGICALLY PRESENT EXCITED STATE



This candidate would have escaped detection in indirect searches so far but not necessarily for much longer!

# ASTROPHYSICAL SCATTERING SIGNATURES (SET BY DARK GAUGE COUPLING)

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- Relic excited state can be collisionally de-excited and populate the ground state
- Mass splitting could be below kinematic threshold for upscattering in a typical galactic environment, re-populating excited state
- These scattering channels convert between kinetic and mass energy, providing a way to heat and cool dark matter depending on the parameters and astrophysical environment
- Can we get exotic dark matter distributions (very dense clumps, disks, etc) from this kind of energy transfer?

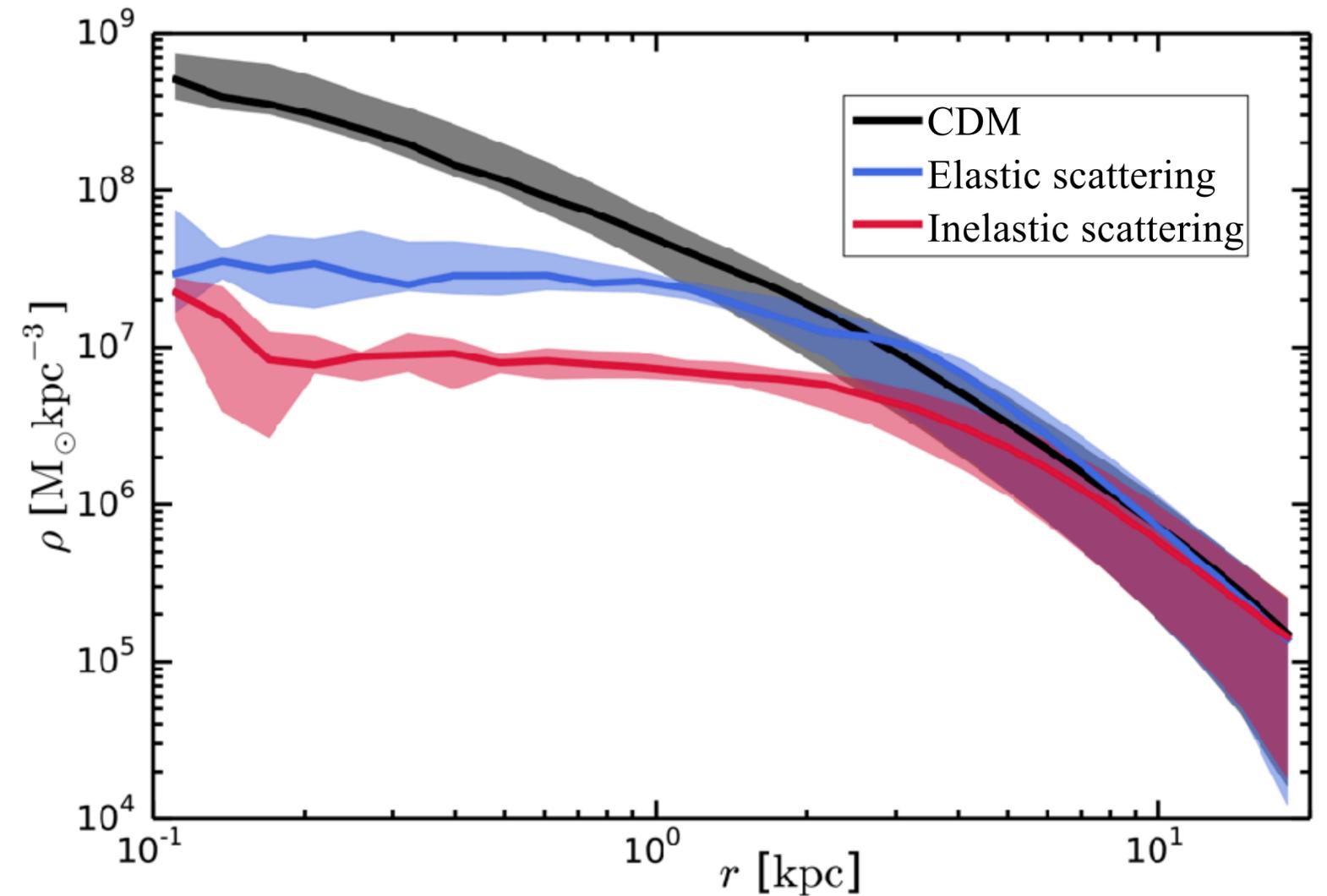
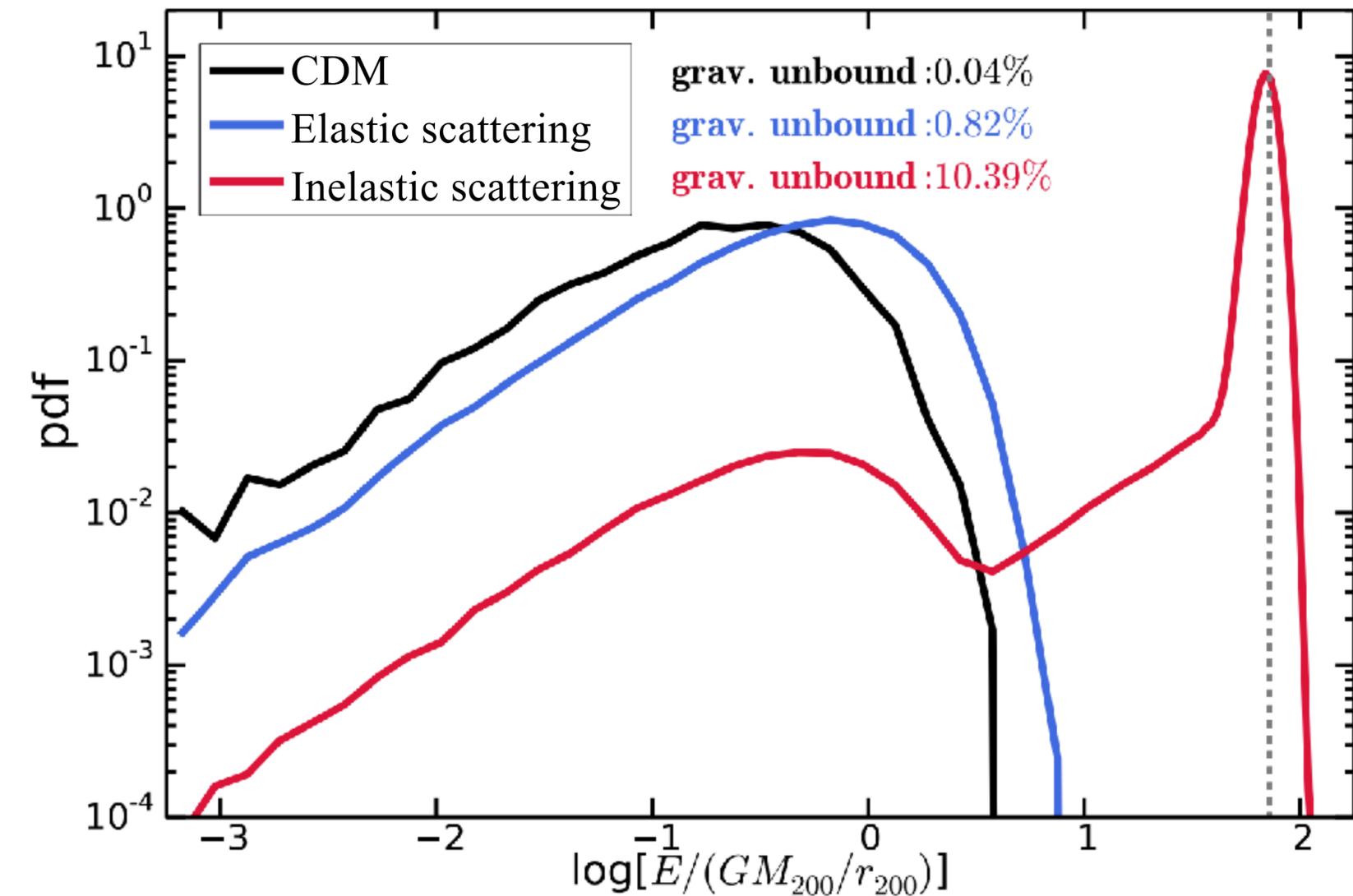
# WHAT HAPPENS TO GALAXY HALOS IF ONLY EXOTHERMIC SCATTERING IS POSSIBLE?



Vogelsberger, Zavala, **KS**, Slatyer MNRAS (2019)

Based on lighter mediator regime where Sommerfeld enhancement is possible, cross sections from **KS** & Slatyer (2015)

# DARK MATTER PARTICLES GET KICKED OUT OF THEIR HALOS, DENSITIES SMEARED



Vogelsberger, Zavala, KS, Slatyer MNRAS (2019)

# WHAT HAPPENS TO GALAXY HALOS IF YOU ADD BOTH EXO- AND ENDOTHERMIC SCATTERING?

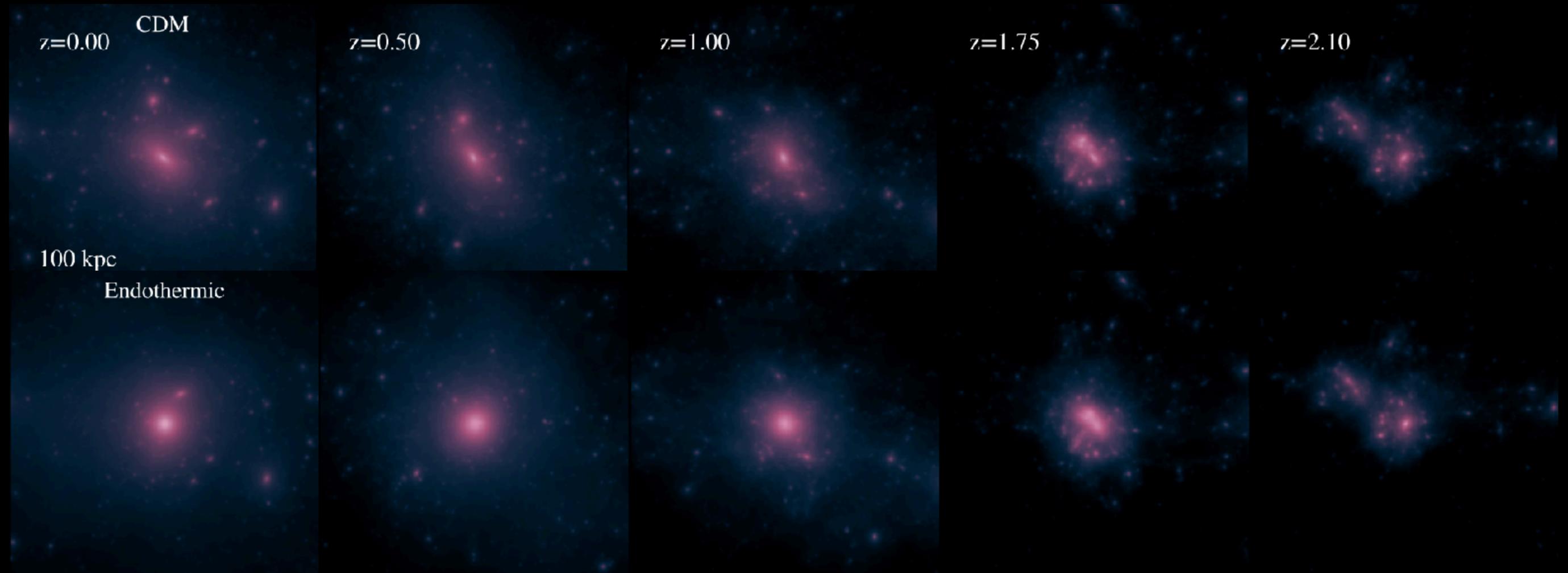


Stephanie O'Neil and Saniya Heeba

O'Neil, Vogelsberger, Heeba, KS et al. MNRAS (2022)

Simulations done in the Born regime of scattering

# WHAT HAPPENS TO GALAXY HALOS IF YOU ADD ENDOTHERMIC SCATTERING?



O'Neil, Vogelsberger, Heeba, KS et al. MNRAS (2022)

**... MOST OF THE "ACTION" HAPPENS AFTER FORMATION OF HEAVIER HALOS (LATER IN BOTTOM-UP STRUCTURE FORMATION) DUE TO KINETIC BARRIER TO UPSCATTERING!**

# THE UPSHOT: INELASTIC SCATTERING COULD COMPLETELY CHANGE HOW DWARF GALAXIES LOOK

Vogelsberger, Zavala, KS, Slatyer MNRAS (2019)

O'Neil, Vogelsberger, Heeba, KS et al. MNRAS (2022)

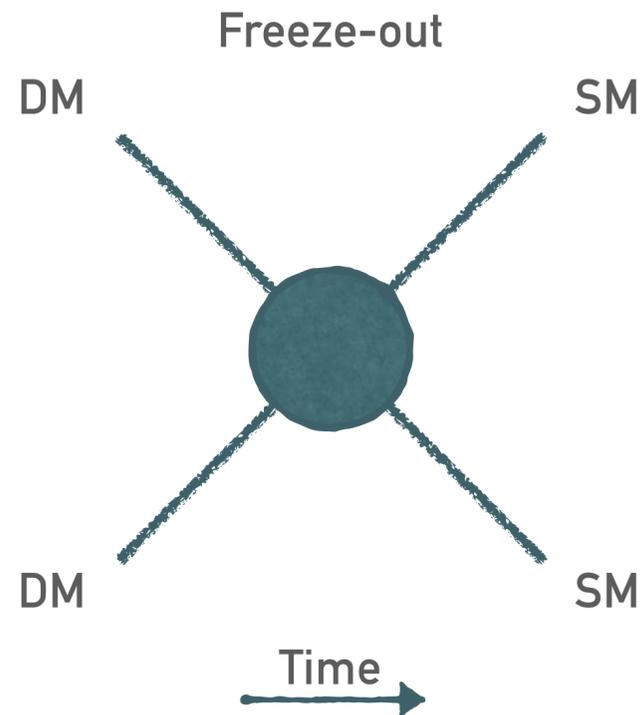


Cartoon by Dr. Saniya Heeba

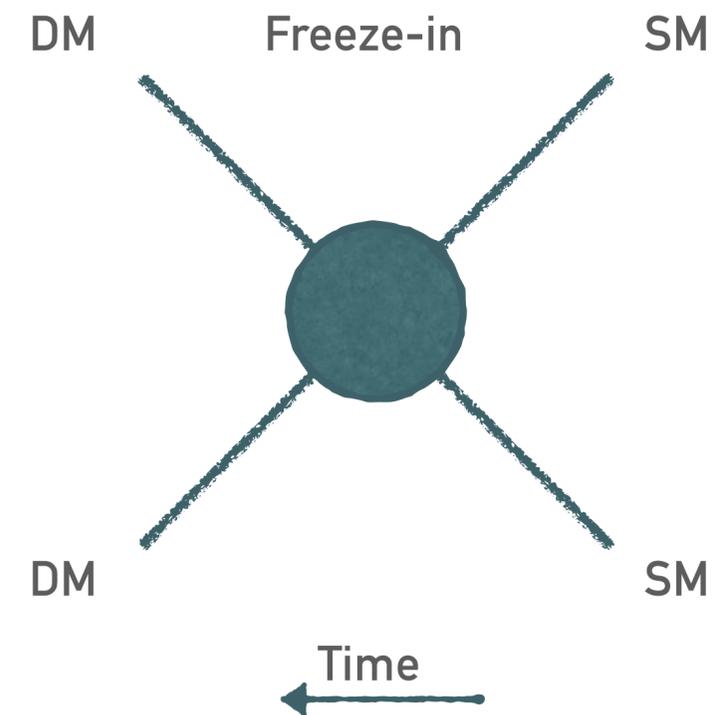
# INELASTIC FREEZE-IN

# FREEZE-OUT VS. FREEZE-IN

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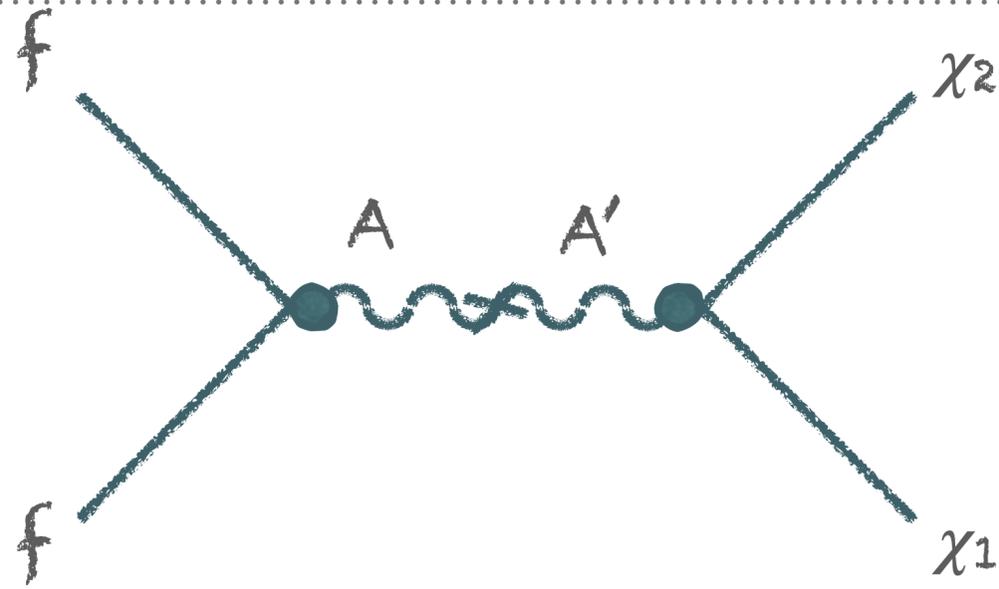


- DM is part of thermal bath, has high thermal initial abundance
- Independent of initial conditions due to thermalization
- DM abundance depleted by DM annihilation to SM
- Relatively large coupling means there are direct and indirect detection observables

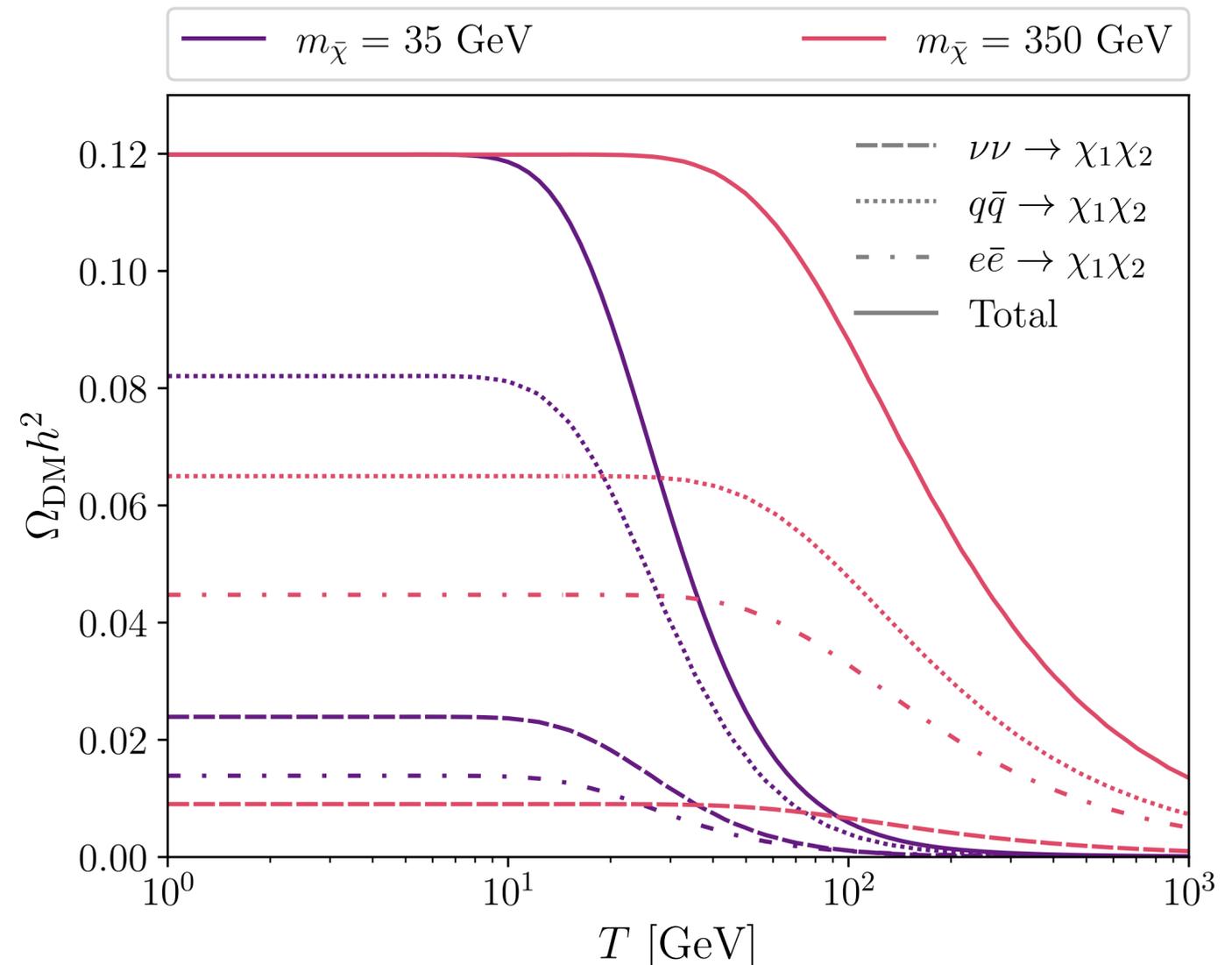
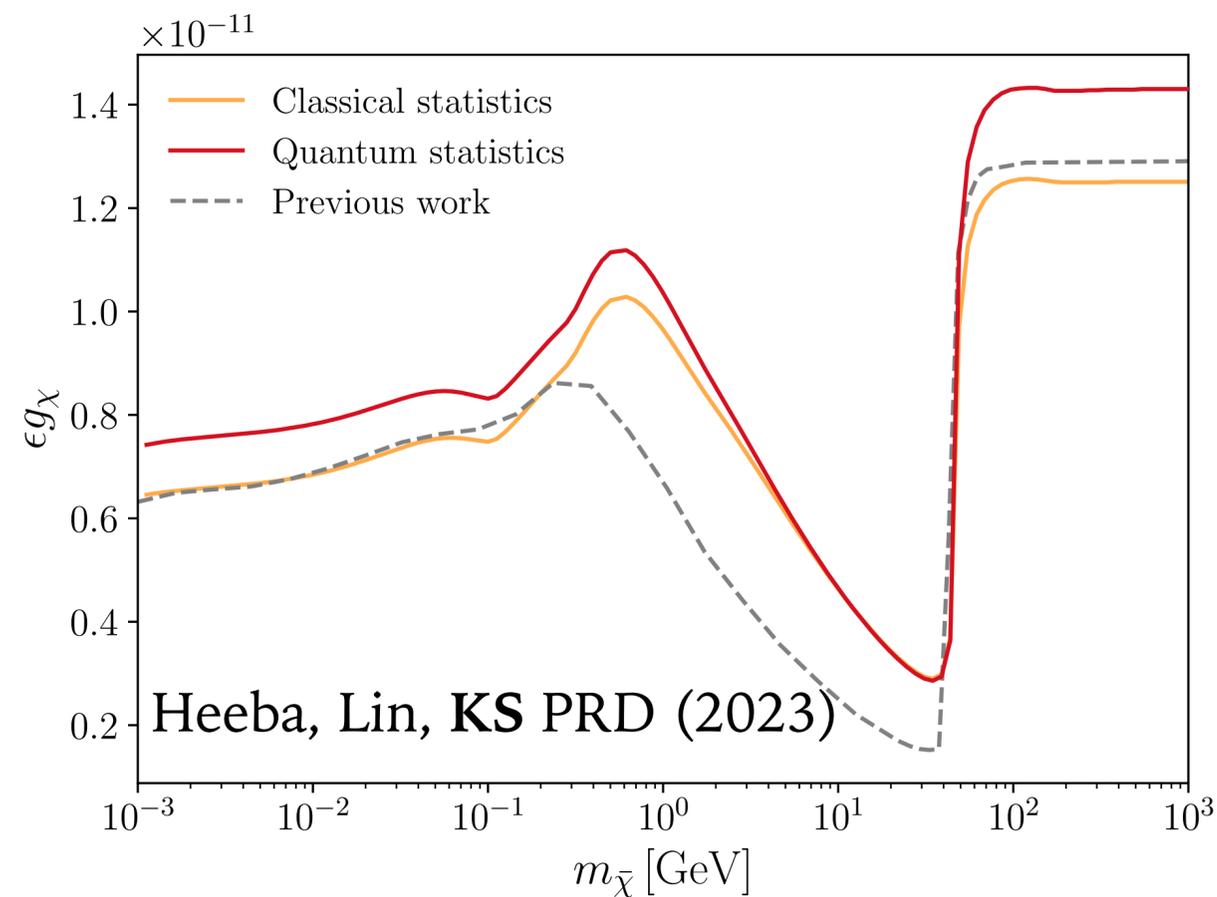


- DM is not in thermal equilibrium with SM, couplings *extremely* tiny
- Independent of initial conditions if IR-dominated process
- DM abundance produced by SM annihilation to DM
- Smallest meaningful DM contact with SM plasma, key benchmark for low-mass direct detection and fixed target

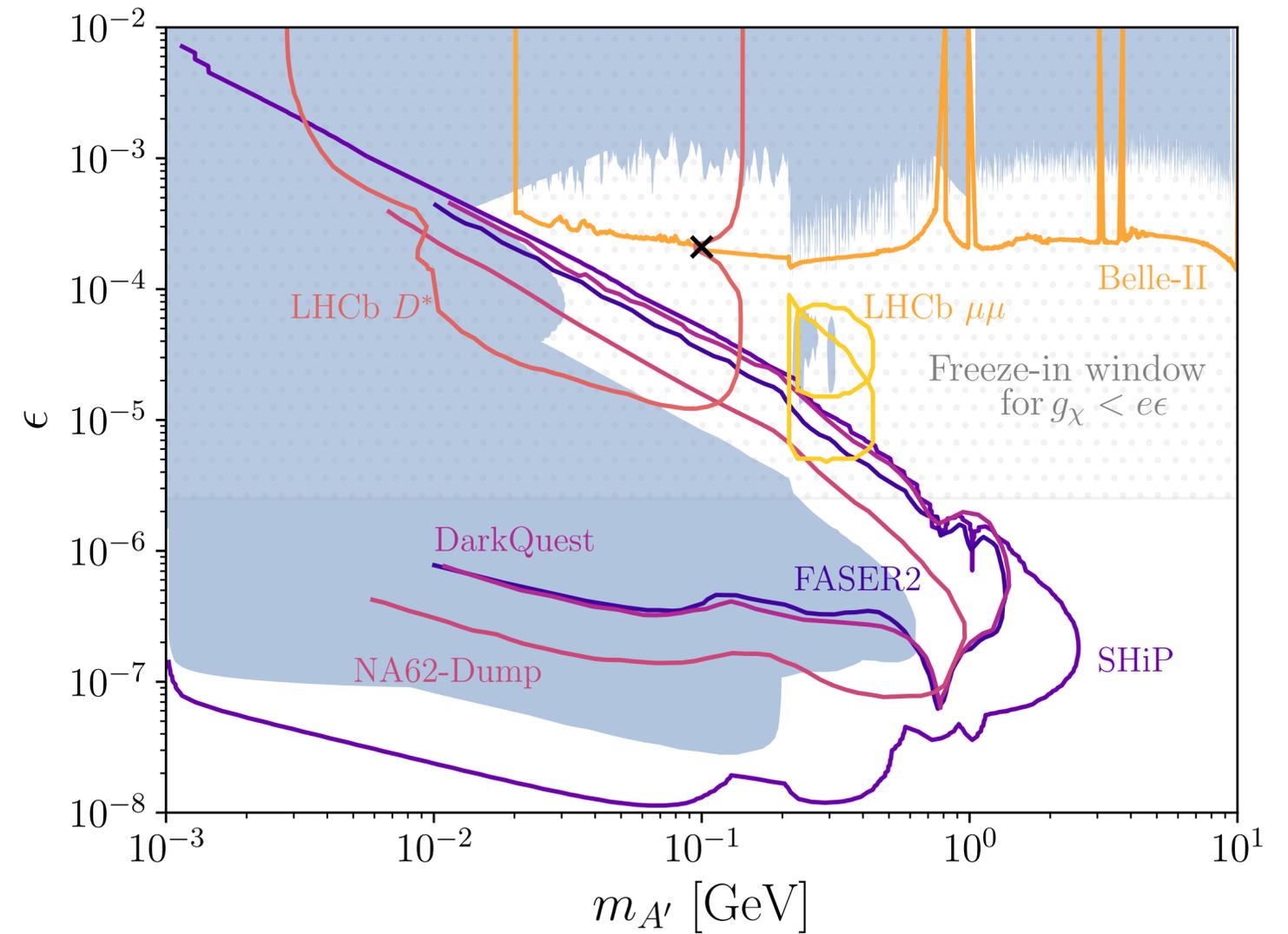
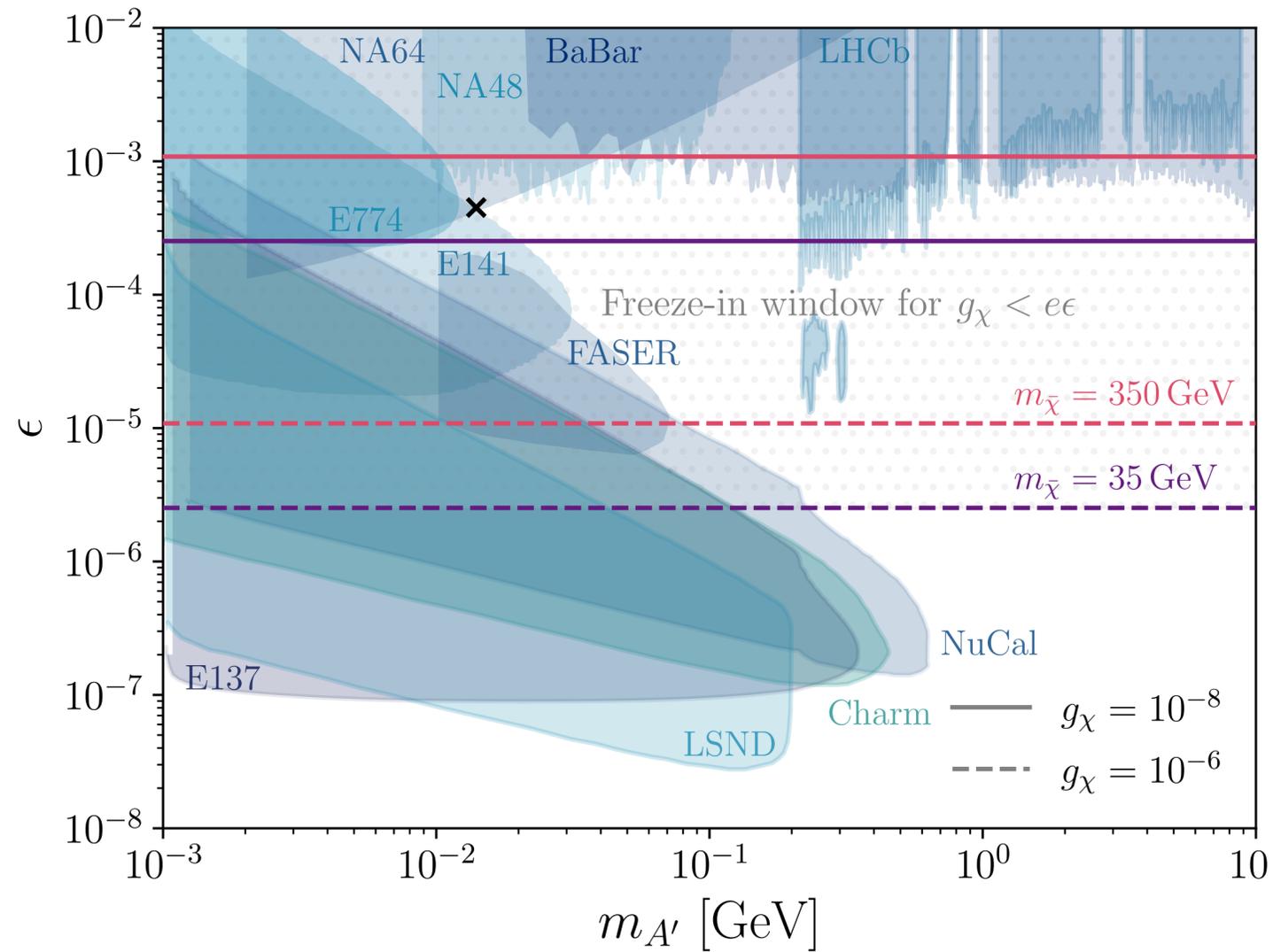
# FREEZE-IN OF PSEUDO-DIRAC DARK MATTER



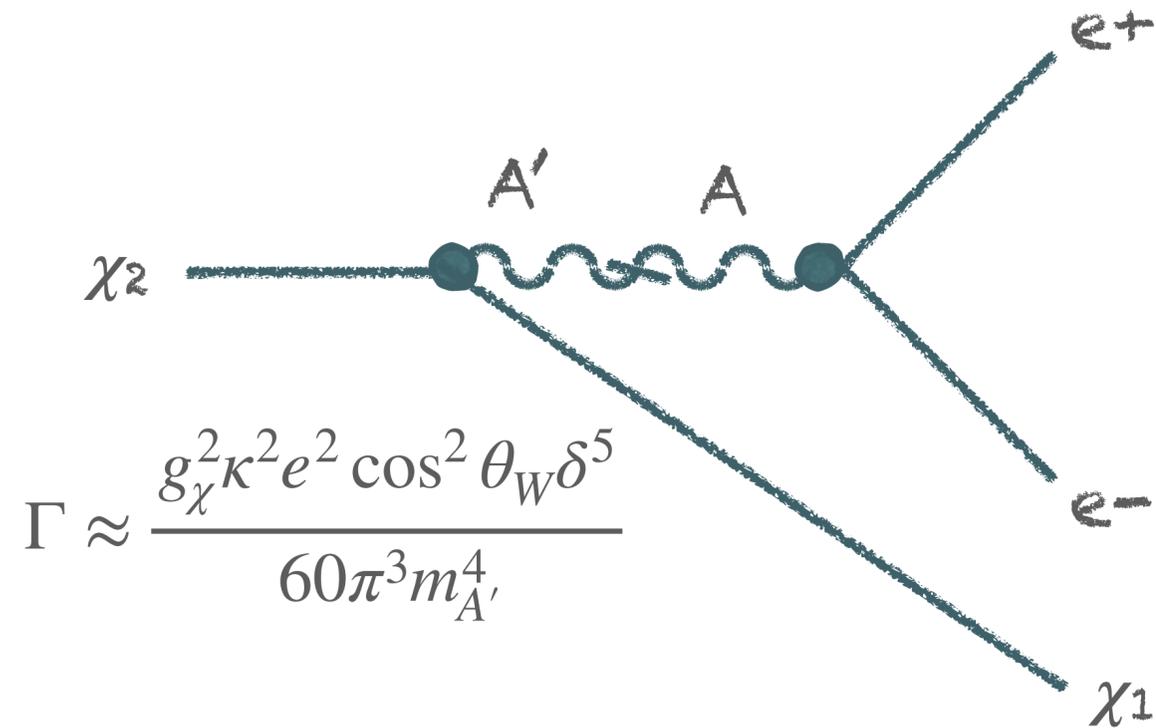
- ▶ Ground and excited state are produced symmetrically by fermion-antifermion annihilation with extremely small branching fraction
- ▶ Mass splitting is too small to matter kinematically so we (mostly) reproduce light mediator Dirac result



# HIGH DEGREE OF COMPLEMENTARITY WITH TERRESTRIAL EXPERIMENT



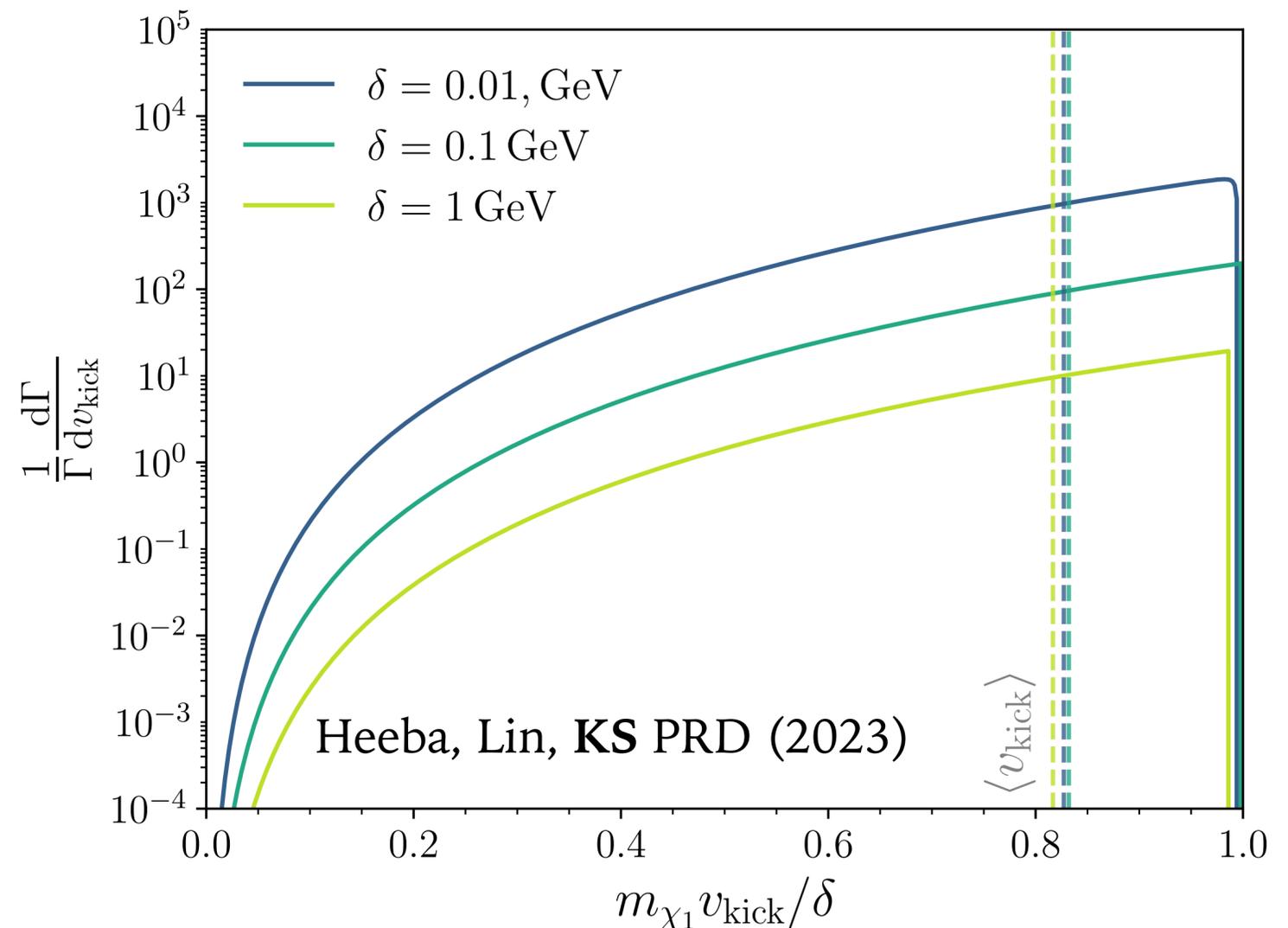
# COSMOLOGY OF THE META-STABLE EXCITED STATE



$$\Gamma \approx \frac{g_\chi^2 \kappa^2 e^2 \cos^2 \theta_W \delta^5}{60\pi^3 m_{A'}^4}$$

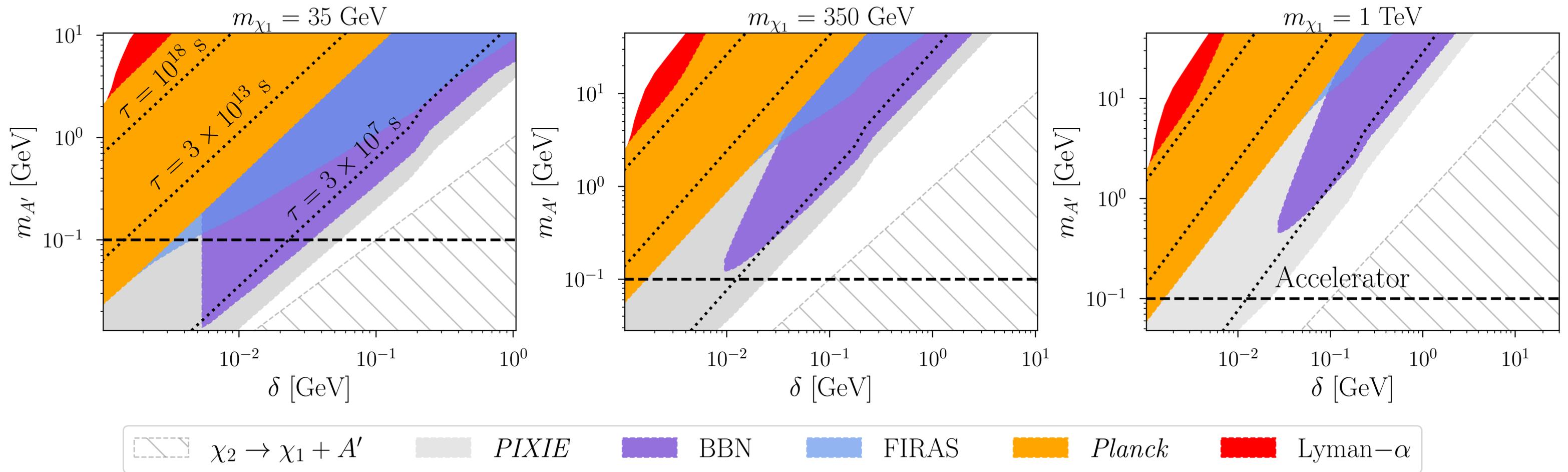
- ▶ All other processes are extremely suppressed/rare due to small freeze-in couplings and low DM density
- ▶ Most of mass splitting energy goes into recoiling electrons, ground state gets a velocity kick,  
 $v_{\text{kick}} \sim \delta/m_\chi$
- ▶ Decaying dark matter excited states have been of interest due to Hubble tension but lacking self-consistent thermal history!

$$\tau \sim 10^7 \text{ seconds} \times \left( \frac{m_{A'}}{1 \text{ GeV}} \right)^4 \left( \frac{100 \text{ MeV}}{\delta} \right)^5$$

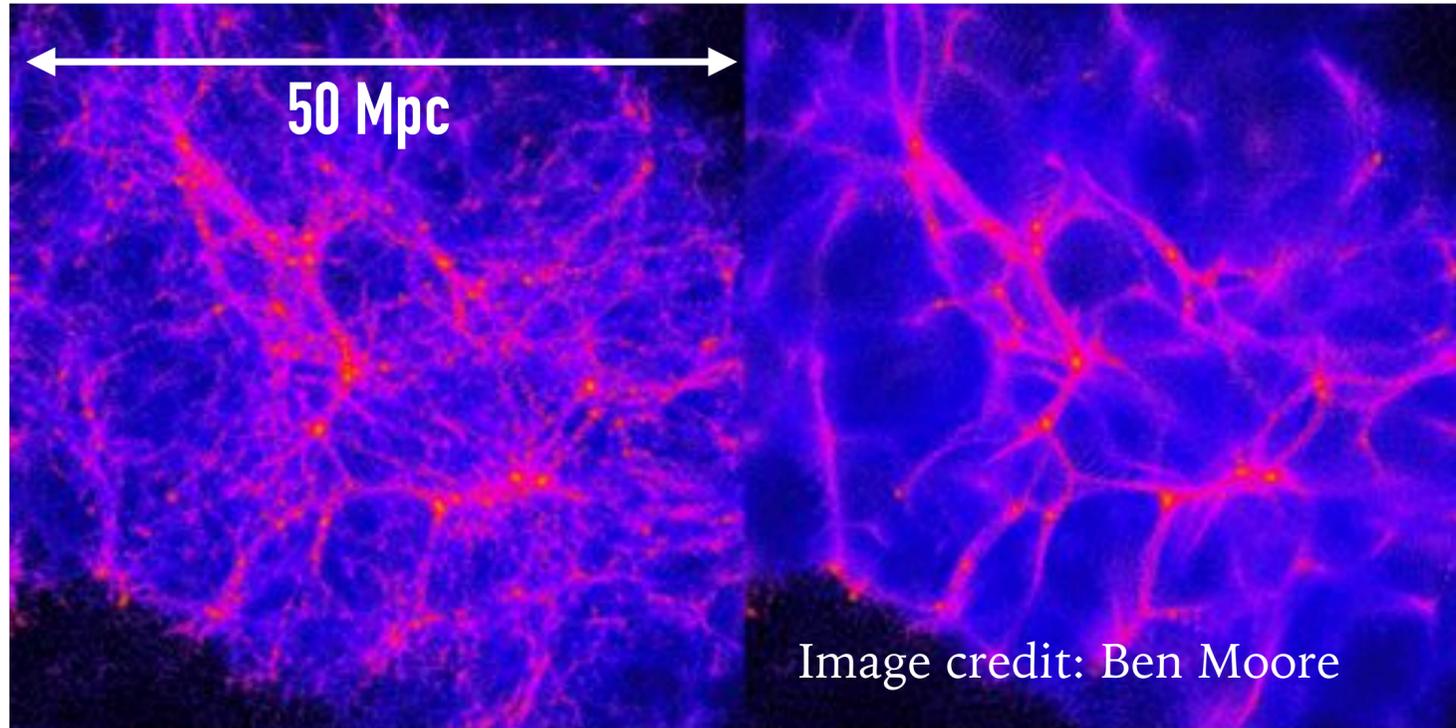


# UNIVERSE AS A CALORIMETER FOR INELASTIC FREEZE-IN

- Electron-positron pairs from three-body decay can inject energy into our cosmic calorimeter! Lots of the parameter space is available and will be tested by future probes (accelerator, PIXIE)



# DARK MATTER KICK COULD IMPACT THE FORMATION OF STRUCTURE

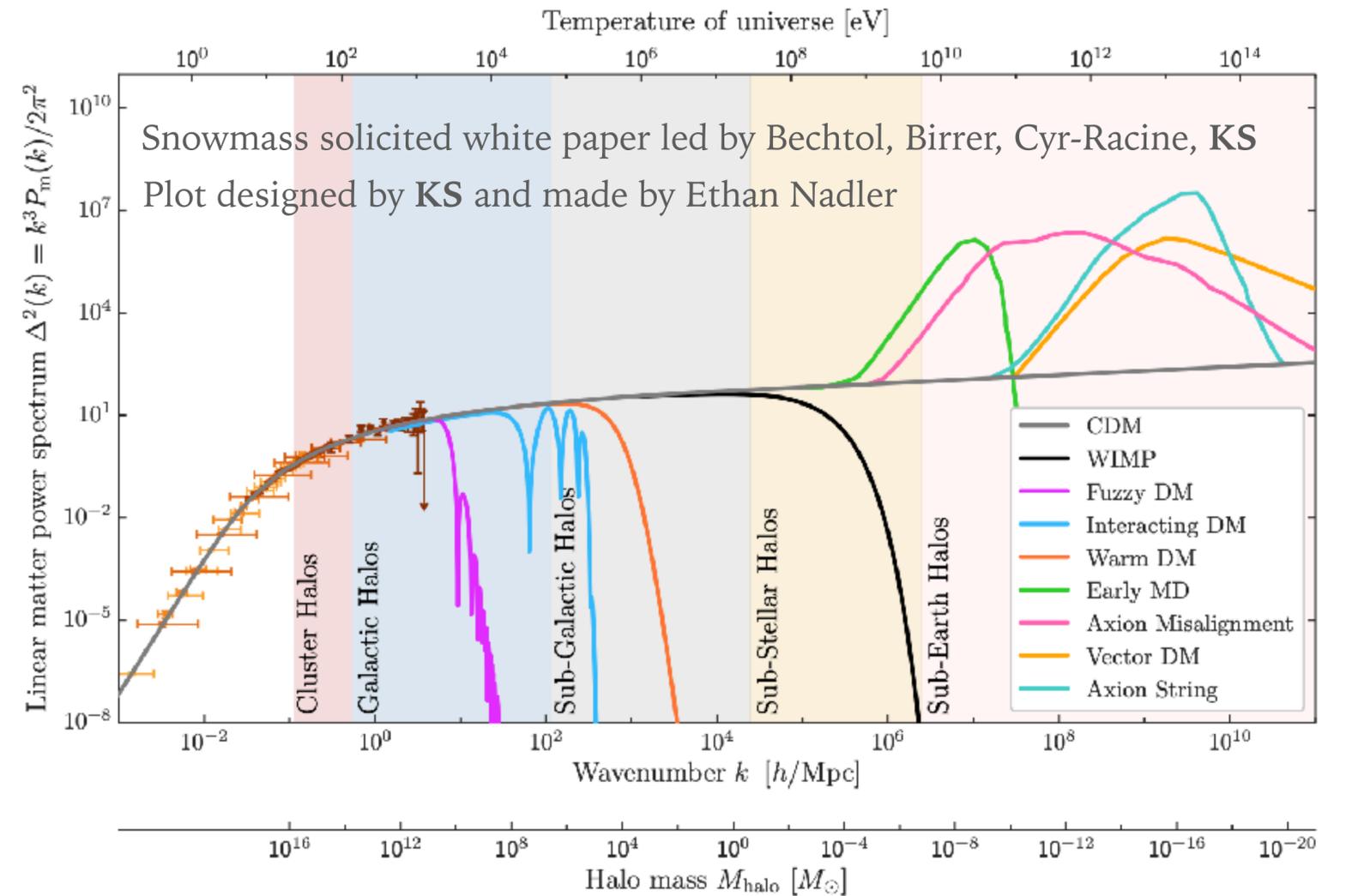


← Cooler/Slower

Hotter/Faster →

Three-body kick to the ground state particle could affect structure formation!

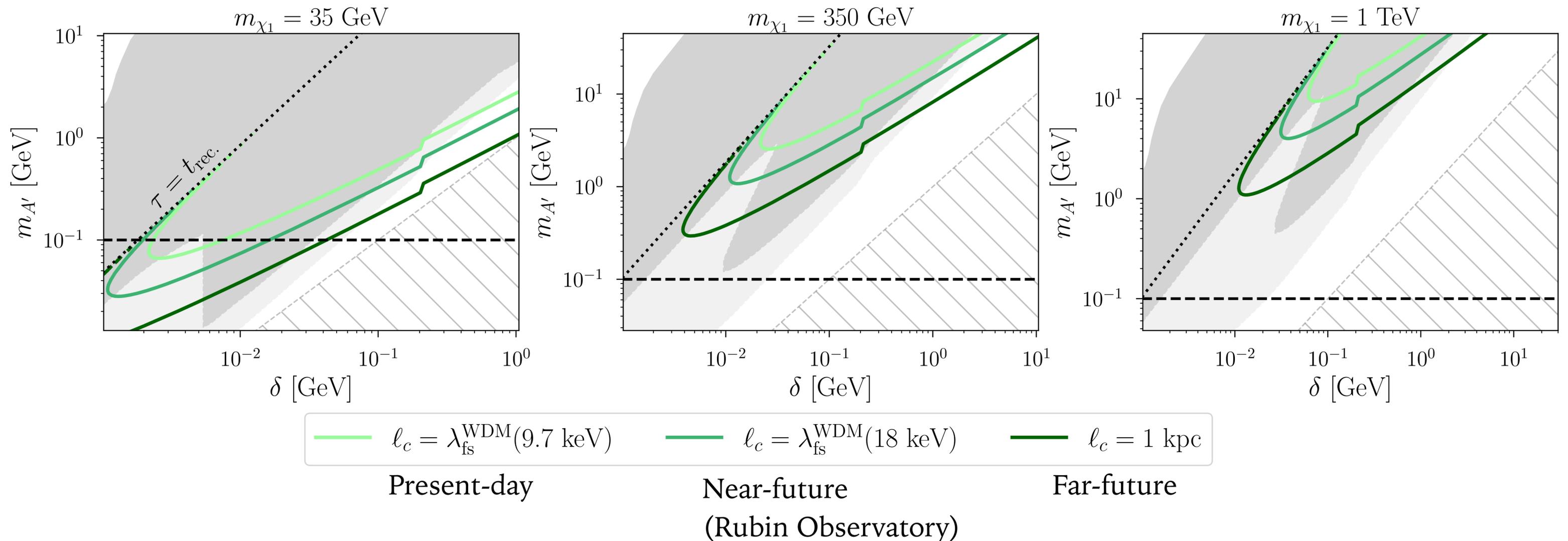
- Probes of cosmic structure formation on smaller scales provide another observational handle on dark sector



# IMPACT OF THE INELASTIC THREE-BODY VELOCITY KICK

Heeba, Lin, **KS PRD** (2023)

- Dark matter velocity kick from three-body decay can hinder the growth of structure on characteristic length scales... complementary to electron calorimeter signatures!



# SUMMARY

- Dark sectors are *incredibly* rich, even very simple, well-explored models have not been completely characterized in terms of thermal history and observables in very testable portions of parameter space
- Self-consistency of model requires complementarity between different types of probes (terrestrial, astrophysical, cosmological) and a holistic view rather than considering observables in isolation will allow us to explore parameter space faster
- It's a big universe, lots of room for creativity!

