Quark propagator 00000 Mesons 0000 Baryons 000 Summary O

Symmetries of hadrons after unbreaking the chiral symmetry

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- [L.Ya. Glozman, C.B. Lang, M.S., Phys. Rev. D 86 (2012); arXiv:1205.4887]
- [M.S., Phys. Lett. B 711 (2012); arXiv:1112.5107]
- [C.B. Lang, M.S., Phys. Rev. D 84 (2011); arXiv:1107.5195]





Motivation and introduction	Quark propagator	Mesons
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Baryons 000 Summary O

Motivation and introduction

Quark propagator

Mesons

Outline

Baryons

Summary



Motivation	and	introduction	
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Quark propagator

Mesons 0000 Baryons 000 Summary O

Key questions to QCD

- How is the hadron mass generated in the light quark sector?
- How important is chiral symmetry breaking for the hadron mass?
- Are confinement and chiral symmetry breaking directly interrelated?
- Is there parity doubling and does chiral symmetry get effectively restored in high-lying hadrons?
- Is there some other symmetry?



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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The Banks–Cas	her relation			

The lowest eigenmodes of the Dirac operator are related to the quark condensate of the vacuum:

$$\left<\overline{\psi}\psi
ight>=-\pi
ho$$
(0)

- ρ(0): density of the lowest quasi-zero eigenmodes of the Dirac
 operator
- here the sequence of limits is important: $V o \infty$ then $m_q o 0$



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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"Unbreaking" chiral symmetry

- Our goal is to construct hadron correlators out of *reduced* quark propagators which exclude a variable number of the lowest Dirac eigenmodes (see also, e.g., [DeGrand, PRD 69 (2004)]).
- we use the Hermitian Dirac operator $D_5 \equiv \gamma_5 D$ (real eigenvalues)
- split the quark propagator $S \equiv D^{-1}$ into a low mode (Im) part and a *reduced* (red) part

$$\begin{split} S &= \sum_{i \le k} \mu_i^{-1} \ket{v_i} \bra{v_i} \gamma_5 + \sum_{i > k} \mu_i^{-1} \ket{v_i} \bra{v_i} \gamma_5 \\ &= S_{\mathrm{lm}(k)} + S_{\mathrm{red}(k)} \end{split}$$



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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• in this work we investigate the *reduced* (red) part of the propagator

$$S_{\mathrm{red}(k)} = S - S_{\mathrm{lm}(k)}$$



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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The chirally improved (CI) Dirac operator

[Gattringer, PRD 63 (2001) 114501], [Gattringer et al., Nucl. Phys. 597 (2001) B451]

- approximate solution to the Ginsparg-Wilson (GW) equation
- constructed by expanding the most general Dirac operator in a basis of simple operators,

$$D_{\rm CI}(x,y) = \sum_{i=1}^{16} c_{xy}^{(i)}(U) \Gamma_i + m_0 \mathbb{1},$$

sum runs over all elements Γ_i of the Clifford algebra. The coefficients $c_{xy}^{(i)}(U)$ consist of path ordered products of the link variables U (here we use paths up to length four).

- Inserting this expansion into the GW equation then turns into a system of coupled quadratic equations for the expansion coefficients
- That expansion provides for a natural cutoff which turns the quadratic equations into a simple finite system.



Motivation	and	introduction	
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The setup

Quark propagator 00000 Mesons 0000 Baryons 000 Summary O

• 161 configurations [Gattringer et al., PRD 79 (2009)]

- size $16^3 \times 32$
- two degenerate flavors of light CI fermions, $m_{\pi}=322(5)\,{
 m MeV}$
- lattice spacing $a = 0.1440(12) \, \mathrm{fm}$
- three different kinds of quark sources: Jacobi smeared narrow (0.27 fm) and wide (0.55 fm) sources and a P wave like derivative source → serves a large operator basis for the variational method.



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Nonperturbative quark propagator

The tree-level quark propagator is

$$S_0(p) = rac{1}{i p + m}$$

¹Iattice gauge fixing on GPUs: [M.S., H. Vogt, LAT2012; arXiv:1209.4008]





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turning on the interactions with the gluon fields

$$S_0(p)
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the renormalized quark propagator

We calculate $S_{\text{bare}}(a; p)$ in minimal Landau gauge¹ on the lattice and therefrom extract

- the renormalization function $Z(\mu; p^2)$
- the renormalization point independent mass function $M(p^2)$

¹lattice gauge fixing on GPUs: [M.S., H. Vogt, LAT2012; arXiv:1209.4008]



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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The CI quark propagator at tree-level

• The lattice quark propagator at tree-level differs from the continuum case due to discretization artifacts

$$S_L^{(0)}(p) = \left(\textit{iak} + \textit{aM}_L^{(0)}(p)
ight)^{-1}$$
 .

• we extract the lattice momenta ak(p) and the tree-level mass function $aM_L^{(0)}(p)$ and compare it to its analytic expressions



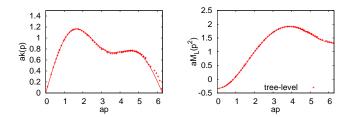
Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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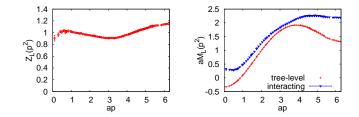
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Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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The interacting CI quark propagator



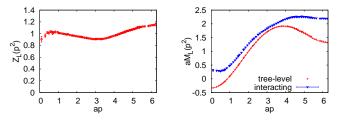
²[Skullerud et al., PRD 64 (2001) 074508]

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Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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The interacting CI quark propagator



Improvement:

- tree-level improvement to reduce $\mathcal{O}(a)$ errors of off-shell quantities
- tree-level correction to blank out tree-level discretization artifacts²:

$$Z_L(p) o rac{Z_L(p)}{Z_L^{(0)}(p)} , \quad aM_L(p) o rac{M_L(p)A_L^{(0)}(p)}{B_L^{(0)}(p) + m_{
m add}} am$$

 $\langle \alpha \rangle$

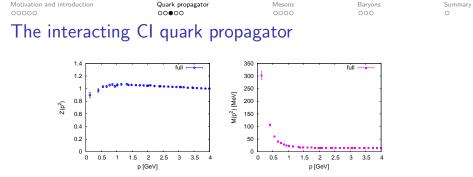
with $am_{\rm add}$ such that $B_L^{(0)}(0) = m$

 $\bullet\,$ a data cut at $4\,{\rm GeV}$

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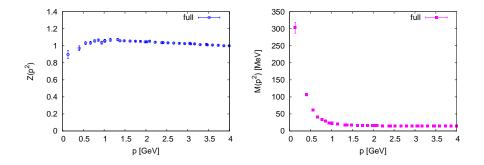
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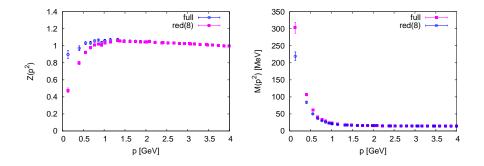


Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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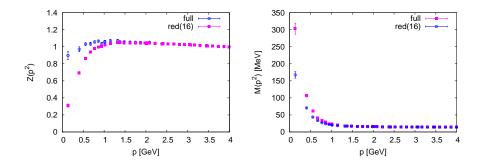
Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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- the dynamically generated mass decreases with the truncation level \rightarrow restoration of the chiral symmetry
- $Z(p^2)$ gets suppressed in the IR



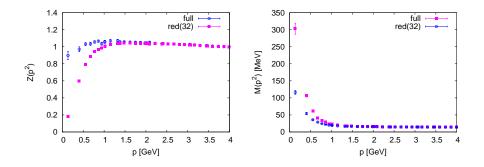
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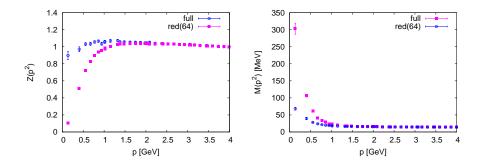
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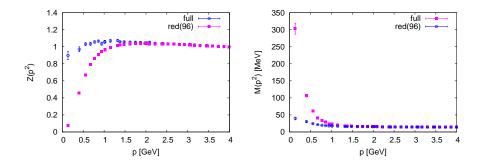
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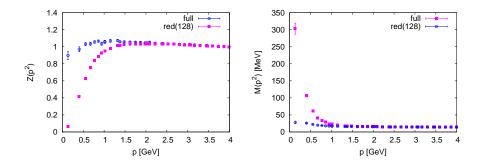
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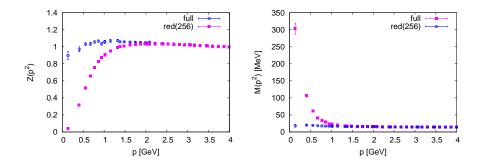
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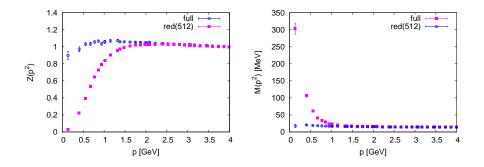
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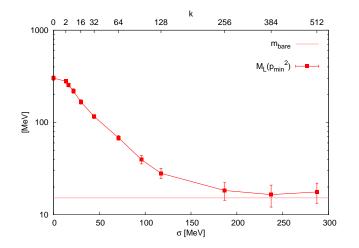


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Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Dynamical quark mass generation vs. truncation level





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Motivation and introduction	Quark propagator	Mesons	Baryons	Summary

Reminder: chiral symmetry and its breaking

When neglecting the two lightest quark masses, the QCD Lagrangian becomes invariant under the symmetry group

 $SU(2)_L imes SU(2)_R imes U(1)_A$

- axial vector part of the $SU(2)_L \times SU(2)_R$ symmetry is broken spontaneously in the vacuum
- vector part is (approximately) preserved
- $U(1)_A$ axial symmetry is not only broken spontaneously but also explicitly (axial anomaly)



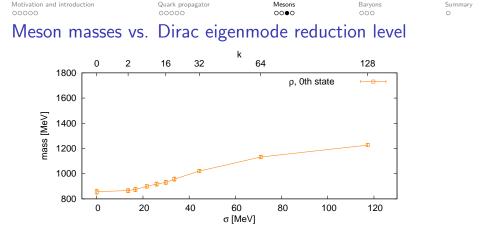
Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Mesons				

We explore the following isovector mesons which, in a chirally symmetric world, would be related via the following symmetries

$$\frac{SU(2)_L \times SU(2)_R \text{ (axial)}}{\rho \longleftrightarrow a_1} \quad \begin{array}{c} U(1)_A \\ \hline \rho \longleftrightarrow b_1 \end{array}$$

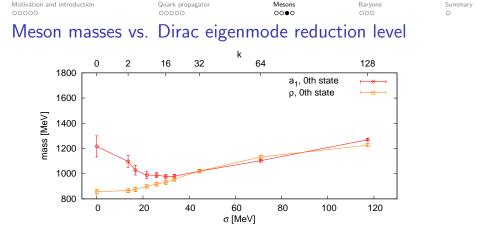
- can we restore the chiral symmetry and if, what happens to confinement?
- how does the mass of the light mesons change?
- what happens to the $U(1)_A$ axial symmetry?





• heavy ρ meson: mass not due to dynamical chiral symmetry breaking

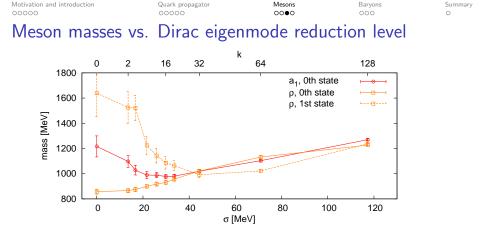




• heavy ρ meson: mass not due to dynamical chiral symmetry breaking • degeneracy of ρ and ρ ; restoration of the SU(2), $\times SU(2)$, chiral

degeneracy of ρ and a₁: restoration of the SU(2)_L × SU(2)_R chiral symmetry

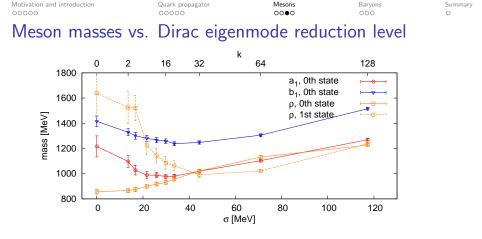




• heavy ρ meson: mass not due to dynamical chiral symmetry breaking

- degeneracy of ρ and a₁: restoration of the SU(2)_L × SU(2)_R chiral symmetry
- degeneracy of ρ and ρ' : hint to a higher symmetry which includes $SU(2)_L \times SU(2)_R$ as a subgroup

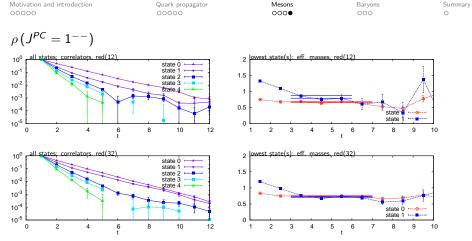




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- degeneracy of ρ and a₁: restoration of the SU(2)_L × SU(2)_R chiral symmetry
- degeneracy of ρ and ρ' : hint to a higher symmetry which includes $SU(2)_L \times SU(2)_R$ as a subgroup
- nondegeneracy of ρ and b_1 : $U(1)_A$ remains broken, still existence of confined states

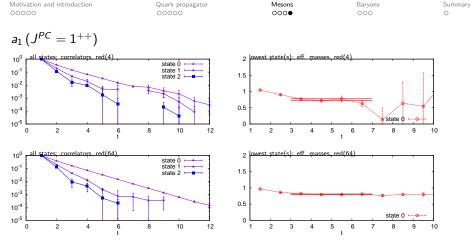




Do we really still observe exponentially decaying states?

- the noise in the correlators (l.h.s.) decreases under Dirac low-mode truncation
- as a consequence the effective mass plots (r.h.s.) become more stable than in full QCD!

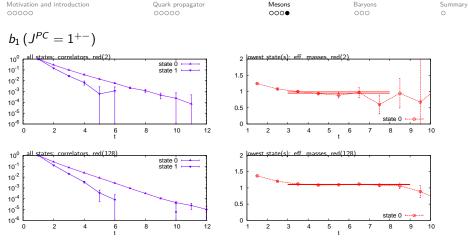




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Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Baryons				

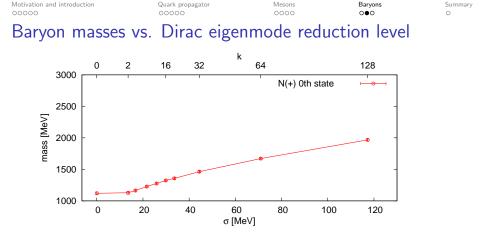
The $\Delta-N$ splitting is usually attributed to the hyperfine spin-spin interaction between valence quarks. The realistic candidates for this interaction are

- the spin-spin color-magnetic interaction
- the flavor-spin interaction related to the spontaneous chiral symmetry breaking

What happens to the $\Delta - N$ splitting after restoration of the chiral symmetry?

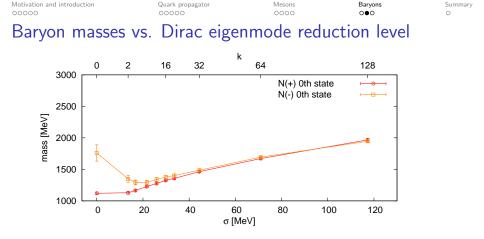
Do the masses of the nucleon and the N(1535) meet?





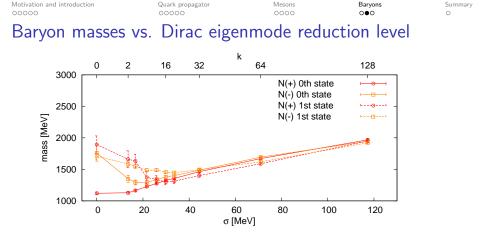
• heavy N(+): mass not due to dynamical chiral symmetry breaking





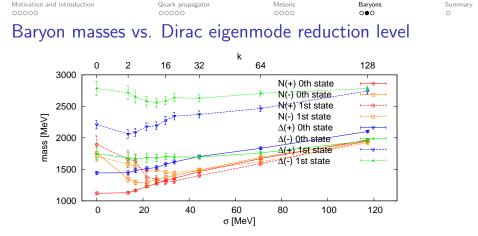
heavy N(+): mass not due to dynamical chiral symmetry breaking
parity doubling of N(+) and N(-)





- heavy N(+): mass not due to dynamical chiral symmetry breaking
- parity doubling of N(+) and N(-)
- degeneracy of two N(+) and N(-) states: hint to a higher symmetry which includes $SU(2)_L \times SU(2)_R$ as a subgroup



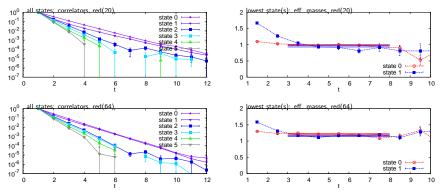


- heavy N(+): mass not due to dynamical chiral symmetry breaking
- parity doubling of N(+) and N(-)
- degeneracy of two N(+) and N(-) states: hint to a higher symmetry which includes $SU(2)_L \times SU(2)_R$ as a subgroup
- distinguished excited states of $\Delta(+)$ and $\Delta(-)$: confinement persists
- Δ -*N* splitting reduces to $\approx 50\%$



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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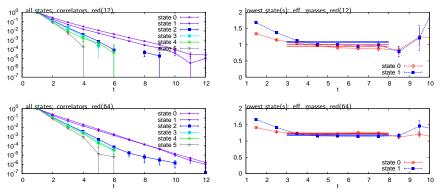






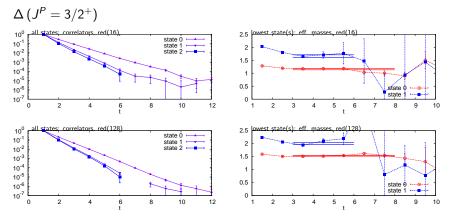
Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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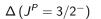


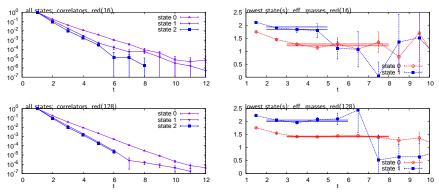
Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Summary				

- low lying eigenvalues of the Dirac operator are associated with chiral symmetry breaking
- we have computed hadron propagators while removing increasingly more of the low lying eigenmodes of the Dirac operator
- the confinement properties remain intact, i.e., we still observe clear bound states for all of the studied hadrons
- the mass values of the vector meson chiral partners a_1 and ρ approach each other: restoration of $SU(2)_L \times SU(2)_R$
- no degeneracy between ho and b_1 : $U(1)_A$ axial anomaly untouched
- the nucleon and the N(1535) become degenerate
- the spin-spin color-magnetic interaction and the flavor-spin interaction are of equal importance for the ΔN splitting

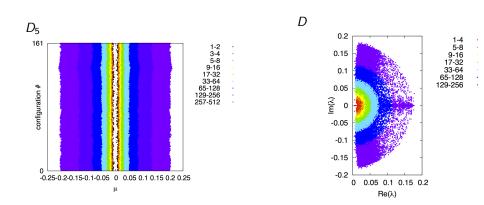


Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Extra slides.



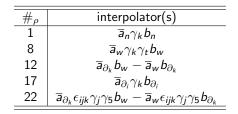
Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Eigenvalues				





Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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Interpolators for the ρ -meson, $J^{PC} = 1^{--}$. The first column shows the number, the second shows the explicit form of the interpolator. cf. [Engel et al., PRD 82 (2010), arXiv:1005.1748]



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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a_1 interpolators				

$\#_{a_1}$	interpolator(s)
1	$\overline{a}_n \gamma_k \gamma_5 b_n$
2	$\overline{a}_n \gamma_k \gamma_5 b_w + \overline{a}_w \gamma_k \gamma_5 b_n$
4	$\overline{a}_w \gamma_k \gamma_5 b_w$

 a_1 -meson, $J^{PC} = 1^{++}$, cf. [Engel et al., PRD 82 (2010), arXiv:1005.1748]



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
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b_1 interpolators				

:	$\#_{b_1}$	interpolator(s)
	6	$\overline{a}_{\partial_k}\gamma_5 b_n - \overline{a}_n\gamma_5 b_{\partial_k}$
	8	$\overline{a}_{\partial_k}\gamma_5 b_w - \overline{a}_w\gamma_5 b_{\partial_k}$

 b_1 -meson, $J^{PC} = 1^{+-}$, cf. [Engel et al., PRD 82 (2010), arXiv:1005.1748]



Motivation and introduction

Quark propagator

Mesons

Baryons

Summary

N interpolators

•	$\mathcal{N}^{(i)} = \epsilon_{abc} \Gamma_1^{(i)} u_a \left(u_b^T \Gamma_2^{(i)} d_c - d_b^T \Gamma_2^{(i)} u_c \right)$
۲	N(+): 1, 2, 4, 14, 15, 18
۲	N(-): 1, 7, 8, 9

$\chi^{(i)}$	г(<i>i</i>)	$\Gamma_2^{(i)}$	smearing	#N
			(nn)n	1
			(nn)w	2
			(nw)n	3
$\chi^{(1)}$	1	6	(nw)w	4
$\chi^{(1)}$	1	$C \gamma_5$	(ww)n	5
			(ww)w	6
			(<i>nn</i>) <i>n</i>	7
			(nn)w	8
			(nw)n	9
$\chi^{(2)}$		с	(nw)w	10
$\chi^{(-)}$	γ_5	C	(ww)n	11
			(ww)w	12
			(<i>nn</i>) <i>n</i>	13
			(nn)w	14
			(nw)n	15
χ ⁽³⁾ <i>i</i> 1 0	Carra	(nw)w	16	
	i 1 $C \gamma_t \gamma_5$	(ww)n	17	
			(ww)w	18

cf. [Engel et al., PRD 82 (2010), arXiv:1005.1748]



M. Schröck

Motivation	and	introduction	
00000			

Quark propagator 00000 Mesons

Baryons 000 Summary O

Δ interpolators

• $\epsilon_{abc} u_a \left(u_b^T C \gamma_k u_c \right)$

- Δ(+): 1, 2, 3
 Δ(-): 1, 2, 3
- Δ(−): 1, 2, 3

smearing $\#_{\Delta}$ $(nn)n$ 1 $(nn)w$ 2 $(nw)n$ 3 $(nw)w$ 4 $(ww)n$ 5 $(ww)w$ 6		
(nn)w 2 (nw)n 3 (nw)w 4 (ww)n 5	smearing	#∆
(nw)n 3 (nw)w 4 (ww)n 5	(<i>nn</i>) <i>n</i>	1
(nw)w 4 (ww)n 5	(nn)w	2
(ww)n 5	(nw)n	3
· · ·	(nw)w	4
(14/14/)14/ 6	(ww)n	5
	(ww)w	6

cf. [Engel et al., PRD 82 (2010), arXiv:1005.1748]



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
00000	00000	0000	000	0

Analytical expressions for the tree-level CI Dirac operator I

$$\begin{split} & \mathcal{M}_{L}^{(0)}(p) = s_{1} + 48s_{13} \\ & + (2s_{2} + 12s_{8})(\cos(p_{0}) + \cos(p_{1}) + \cos(p_{2}) + \cos(p_{3})) \\ & + (8s_{3} + 64s_{11})(\cos(p_{0})\cos(p_{1}) + \cos(p_{0})\cos(p_{2}) \\ & + \cos(p_{0})\cos(p_{3}) + \cos(p_{1})\cos(p_{2}) + \cos(p_{1})\cos(p_{3}) \\ & + \cos(p_{2})\cos(p_{3})) \\ & + 48s_{5}(\cos(p_{0})\cos(p_{1})\cos(p_{2}) + \cos(p_{0})\cos(p_{1})\cos(p_{3}) \\ & + \cos(p_{0})\cos(p_{2})\cos(p_{3}) + \cos(p_{1})\cos(p_{2})\cos(p_{3})) \\ & + 8s_{6}(\cos(p_{0})\cos(2p_{1}) + \cos(p_{0})\cos(2p_{2}) \\ & + \cos(p_{0})\cos(2p_{3}) + \cos(p_{1})\cos(2p_{2}) \\ & + \cos(p_{0})\cos(2p_{3}) + \cos(p_{2})\cos(2p_{3}) \\ & + \cos(2p_{0})\cos(p_{1}) + \cos(2p_{0})\cos(p_{2}) \\ & + \cos(2p_{0})\cos(p_{3}) + \cos(2p_{1})\cos(p_{2}) \\ & + \cos(2p_{1})\cos(p_{3}) + \cos(2p_{2})\cos(p_{3})) \\ & + 384s_{10}\cos(p_{0})\cos(p_{1})\cos(p_{2})\cos(p_{3}) \\ & + m_{0} \end{split}$$



Motivation and introduction	Quark propagator	Mesons	Baryons	Summary
00000	00000	0000	000	0

Analytical expressions for the tree-level CI Dirac operator II

$$\begin{split} k_0 &= 2v_1 \sin(p_0) + 8v_2 \sin(p_0)(\cos(p_1) + \cos(p_2) + \cos(p_3)) \\ &+ (32v_4 + 16v_5) \sin(p_0)(\cos(p_1) \cos(p_2) + \cos(p_1) \cos(p_3)) \\ &+ \cos(p_2) \cos(p_3)), \\ k_1 &= 2v_1 \sin(p_1) + 8v_2 \sin(p_1)(\cos(p_0) + \cos(p_2) + \cos(p_3))) \\ &+ (32v_4 + 16v_5) \sin(p_1)(\cos(p_0) \cos(p_2) + \cos(p_0) \cos(p_3)) \\ &+ \cos(p_2) \cos(p_3)), \\ k_2 &= 2v_1 \sin(p_2) + 8v_2 \sin(p_2)(\cos(p_0) + \cos(p_1) + \cos(p_3))) \\ &+ (32v_4 + 16v_5) \sin(p_2)(\cos(p_0) \cos(p_1) + \cos(p_0) \cos(p_3)) \\ &+ \cos(p_1) \cos(p_3)), \\ k_3 &= 2v_1 \sin(p_3) + 8v_2 \sin(p_3)(\cos(p_0) + \cos(p_1) + \cos(p_2)) \\ &+ (32v_4 + 16v_5) \sin(p_3)(\cos(p_0) + \cos(p_1) + \cos(p_2)) \\ &+ (32v_4 + 16v_5) \sin(p_3)(\cos(p_0) \cos(p_1) + \cos(p_0) \cos(p_2) \\ &+ \cos(p_1) \cos(p_2)) \end{split}$$



Motivation and introduction

Quark propagator

Mesons 0000 Baryons 000 Summary O

The relevant $D_{\rm CI}$ coefficients

$0.1481599252 imes 10^1$
$-0.5218251439 imes 10^{-1}$
$-0.1473643847 imes 10^{-1}$
$-0.2186103421 imes 10^{-2}$
$0.2133989696 imes 10^{-2}$
$-0.3997001821 imes 10^{-2}$
$-0.4951673735 imes 10^{-3}$
$-0.9836500799 imes 10^{-3}$
$0.7529838581 imes 10^{-2}$
$0.1972229309 imes 10^{0}$
$0.8252157565 imes 10^{-2}$
$0.5113056314 imes 10^{-2}$
$0.1736609425 imes 10^{-2}$
-0.077

