

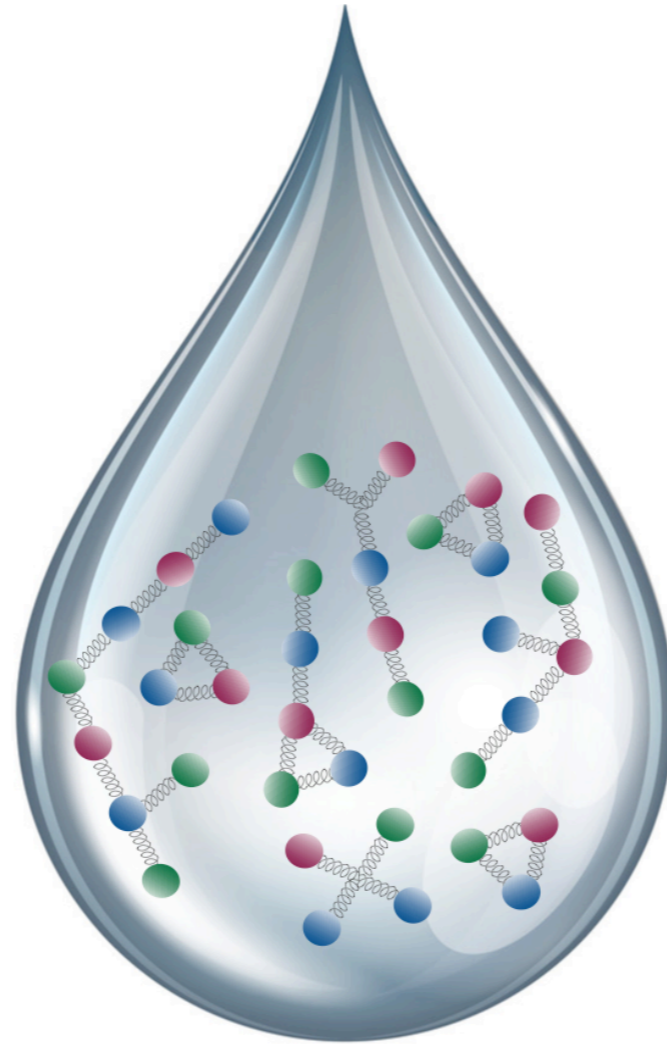
Magnetic catalysis, Chern-Simons diffusion and spin transport in QGP

Umut Gürsoy

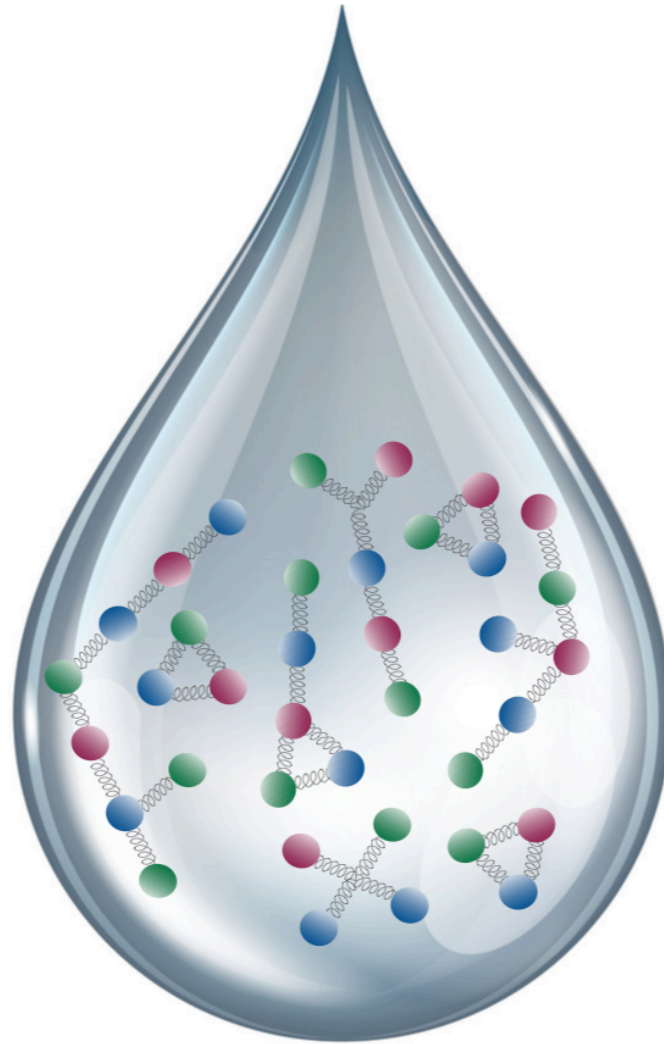
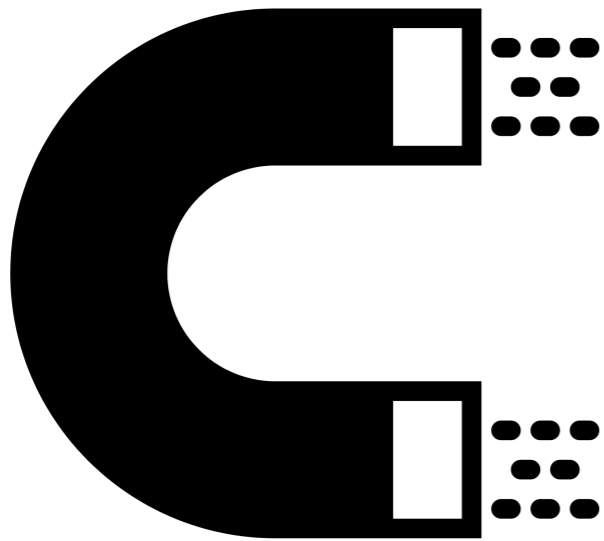
Utrecht University

AdS4CME workshop, 15/3/2022

QGP hydrodynamics



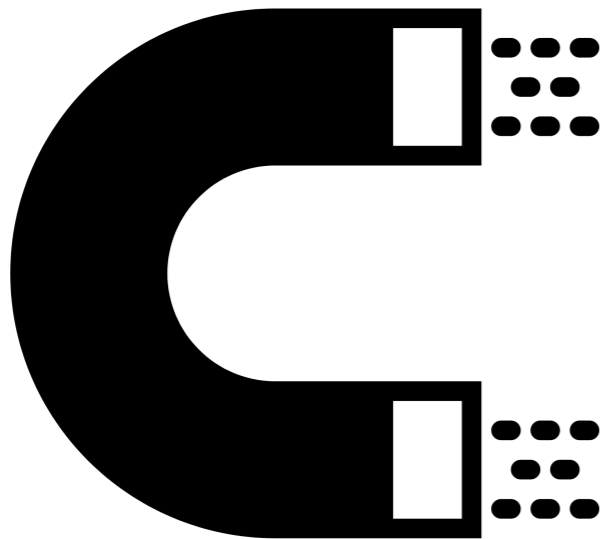
QGP hydrodynamics



Magnetic field

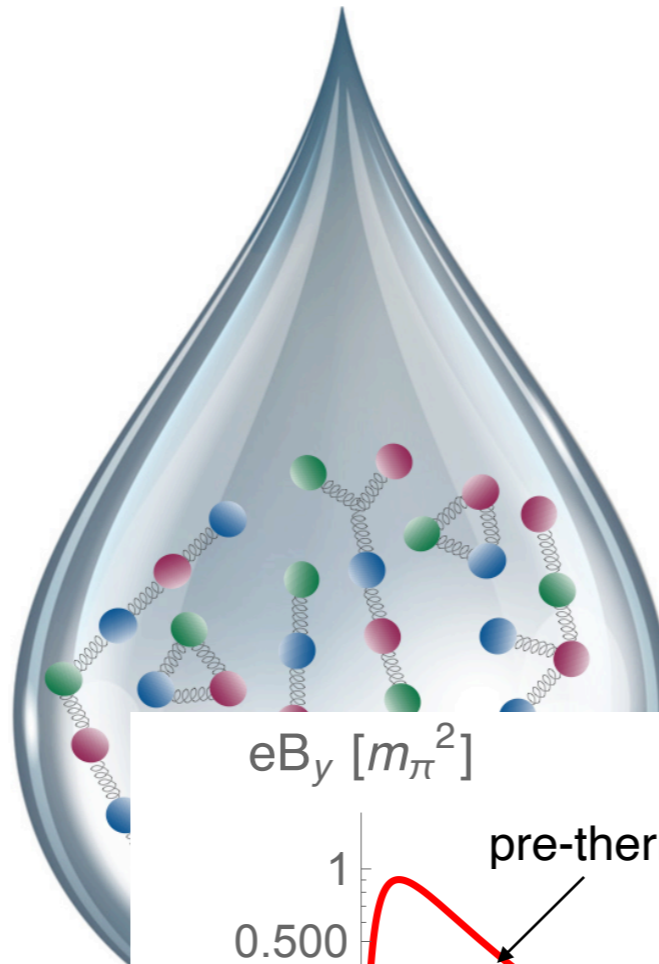
$$B \sim 10^{14} B_{\text{MRI}}$$

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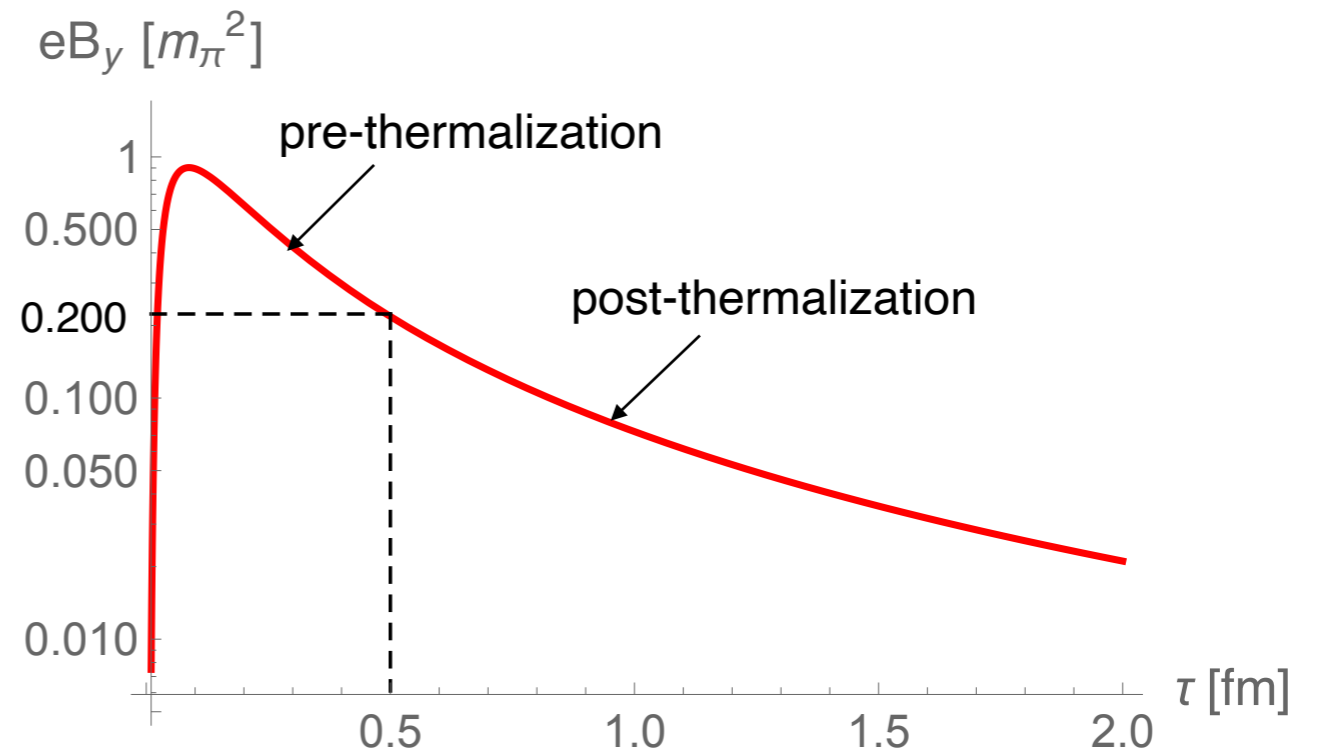


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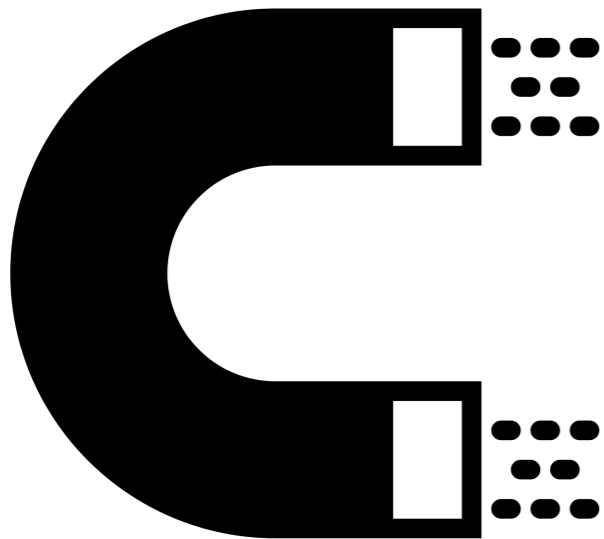
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Kharzeev, Rajagopal, UG '14



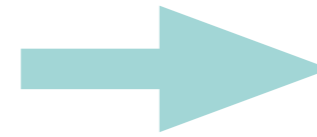
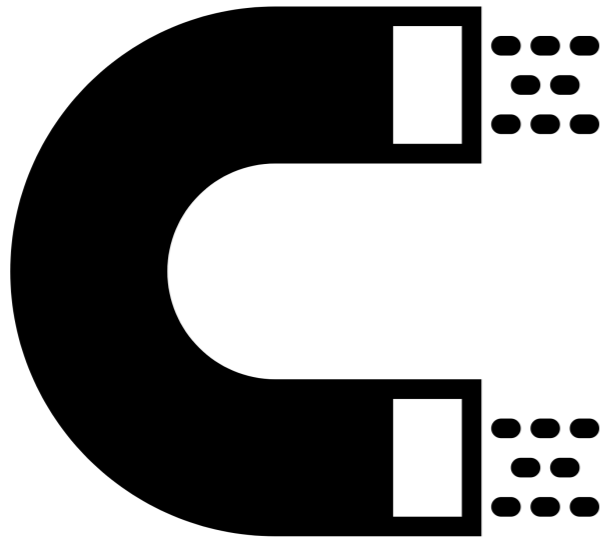
QGP hydrodynamics



Strong vortical structure

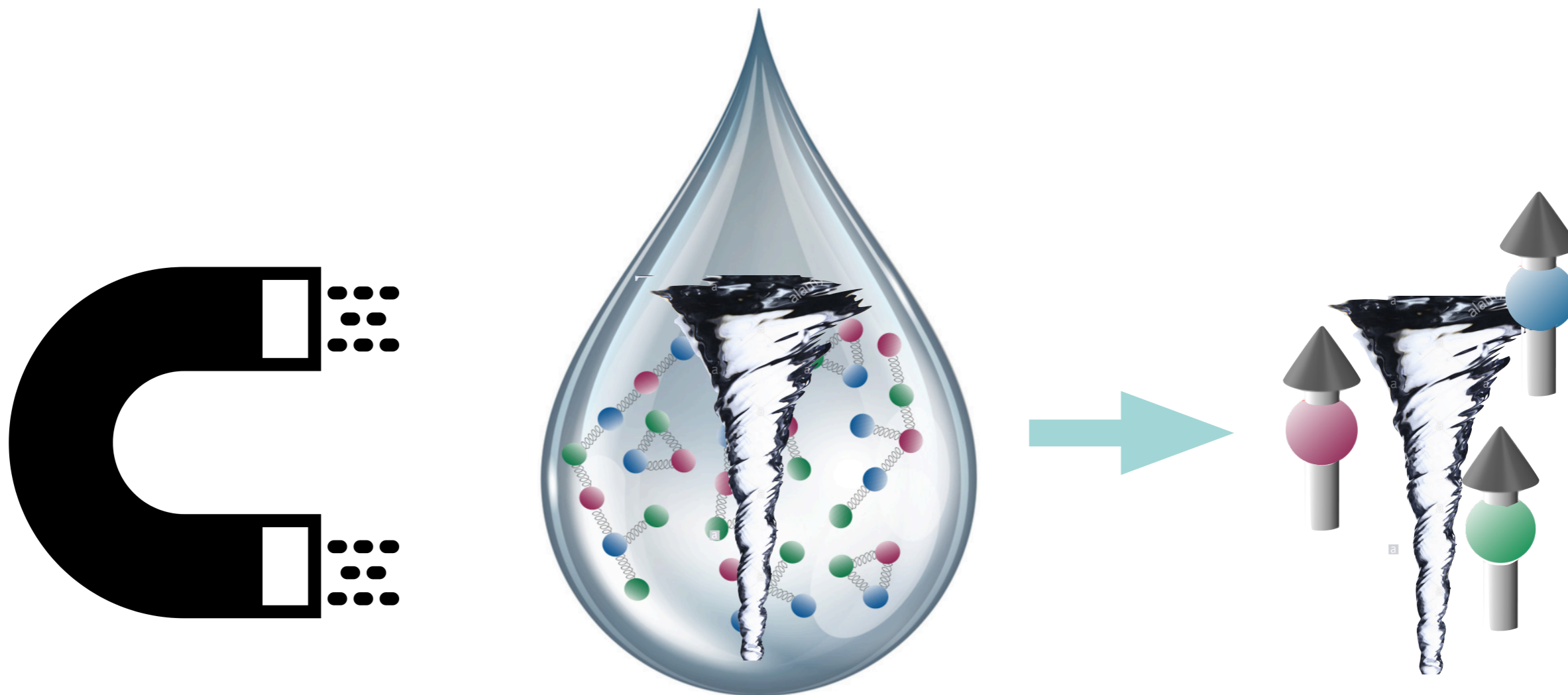
$$\omega \sim 1000\hbar$$

QGP hydrodynamics



Vorticity
 $\omega \sim 1000\hbar$

Charge and
spin flow



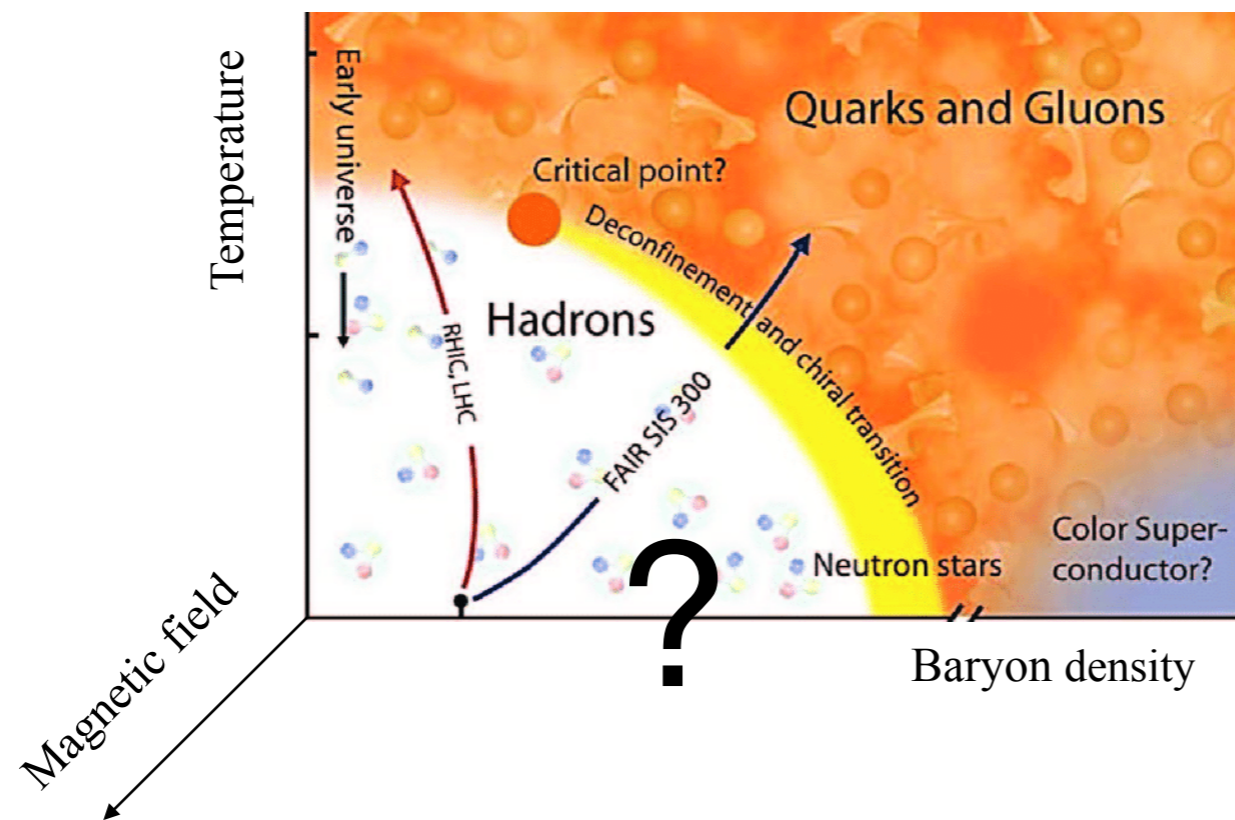
Chiral magnetic and vortical effect

→ Matter antimatter asymmetry

Part I: magnetic fields, anisotropic QCD

Open questions

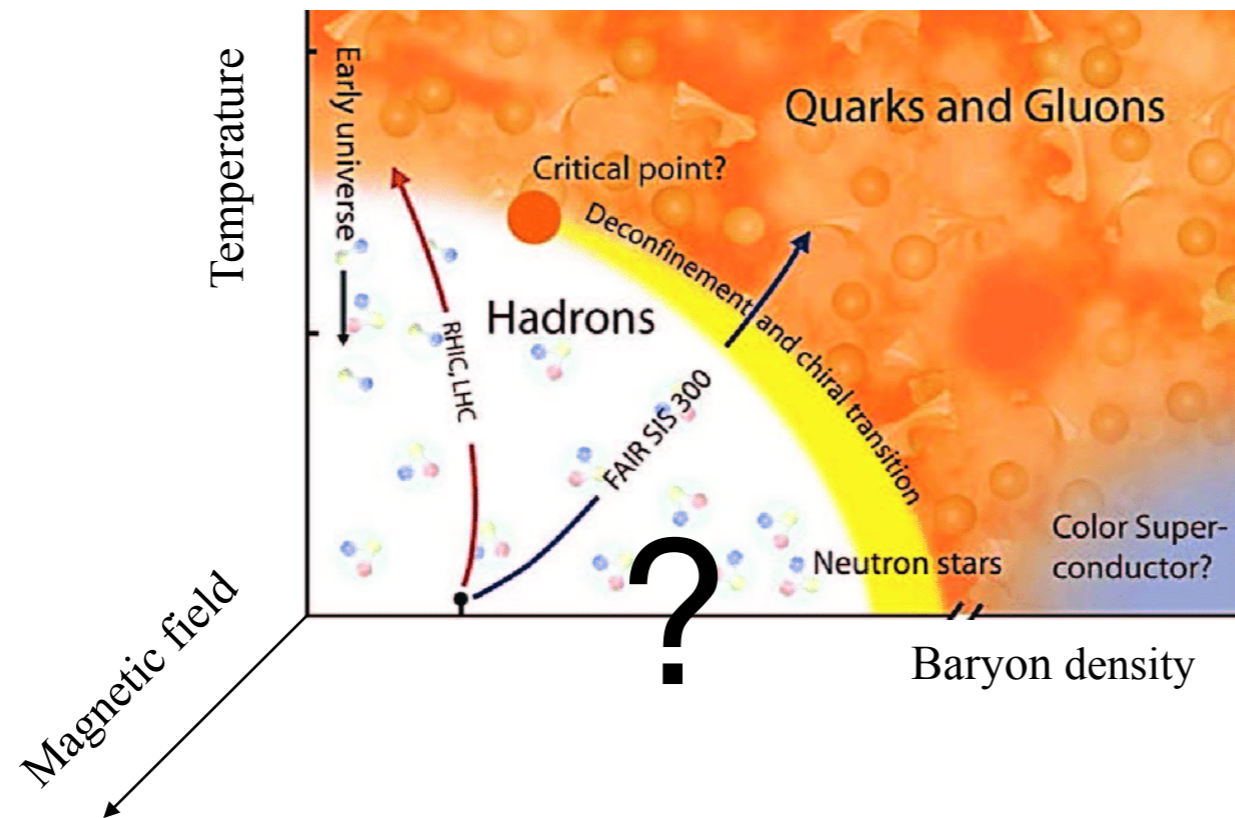
- * Ground state: dependence of $\langle \bar{q}q \rangle$ on B (inverse) magnetic catalysis
- * Thermodynamics: phase diagram of QCD at finite B



- * Hydrodynamics and transport: 2 conductivities, 2 shear, 3 bulk viscosities
B dependence of η , ζ [Hernandez, Kovtun '17](#)
[Grozdanov, Hofman, Iqbal '17](#)
- * Fully back-reacted magneto-hydrodynamics: HIC, neutron star mergers
- * Anomalous transport: chiral magnetic and vortical effects, Chern-Simons diffusion rate
- * Out of equilibrium: initial conditions for hydro, generation of chiral imbalance

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Improved holographic QCD in the Veneziano limit

Kiritsis, Nitti, UG '07; Kiritsis, Nitti, Mazzanti, UG '08 '09
Jarvinen, Kiritsis '11; Alho et al '12

- QCD has infinite operators unlike N=4 sYM
- General bulk \Leftrightarrow boundary should apply to QCD for $\lambda \gg 1$ Polyakov '98 '00
- Integrating out fast modes in the 5D non-critical string
 \Rightarrow effective 5D gravity + matter
- IR sum-rules in QCD: OPA semi-closed on relevant/marginal operators
Shifman, Vainshtein, Zakharov '79

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Write down a bulk 5D action for $T_{\mu\nu}, \text{tr } G^2, \text{tr } G \wedge G, \bar{q}q, J_\mu$

Color tube \Leftrightarrow fundamental string, flavor \Leftrightarrow D5 branes

Determine the potentials + integration const. from the basic features of QCD:
Confinement, asymptotic freedom, χ SB, gapped discrete spectrum, anomalies

Systematic errors largely reduced by fixing the large field limits of potentials

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$$\mathbf{A}_{LMN} = g_{MN} + w(\lambda, T) F_{MN}^{(L)} + \frac{\kappa(\lambda, T)}{2} \left[(D_M T)^\dagger (D_N T) + (D_N T)^\dagger (D_M T) \right]$$

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$U(1)_B \Leftrightarrow$ magnetic field

$U(1)_A$

$\bar{q}q$

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$\text{tr } G \wedge G$ CP-odd sector

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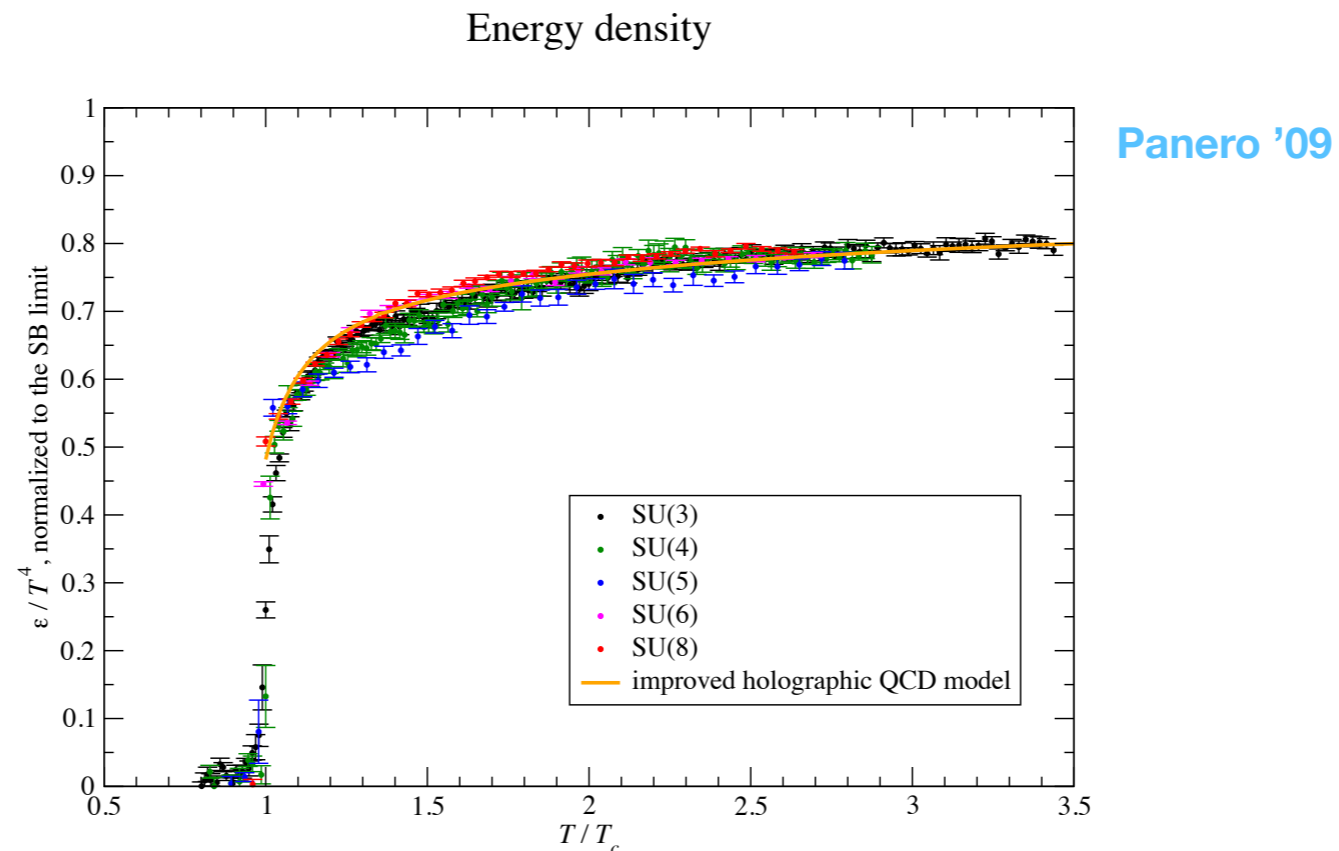
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Fixing the potentials

- Fix V_g by non-singular IR, linear confinement, linear mass spectrum, lowest glueball mass, $\Delta S(T_c)$



- Fix V_f , $\kappa(\lambda)$ by non-singular IR, qualitative features of the phase diagram in μ and x , condensate anomalous dimension, chiral anomaly, meson mass spectrum Jarvinen, Kiritsis '11; Alho et al '12 '13
- Choose $w(\lambda) = \kappa(c\lambda)$ by conductivity, diffusion const. of the plasma
Iatrakis, Zahed '12; Alho et al '13

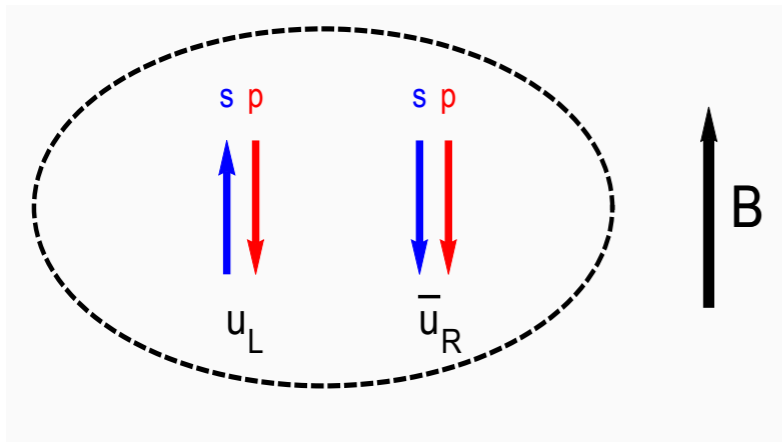
$$w(\lambda) = \kappa(c\lambda) = \frac{(1 + \log(1 + c\lambda))^{-\frac{1}{2}}}{\left(1 + \frac{3}{4} \left(\frac{115-16x}{27} - \frac{1}{2}\right) c\lambda\right)^{\frac{4}{3}}}$$

- Fix Z by topological susceptibility, axial glueball spectrum $Z(\lambda) = Z_0 (1 + c_4 \lambda^4)$

$$0 \lesssim c_1 \lesssim 5, \quad 0.06 \lesssim c_4 \lesssim 50.$$

Magnetic catalysis

Klevansky, Lemmer '89; Suganuma, Tatsumi '91; Gusynin, Miransky, Shovkovy '94



- B catalyses chiral symmetry breaking
- Generic: QED, NJL, free(!) ... 2+1, 3+1
- B aligns spins, effectively reduces 3+1 \Rightarrow 1+1
- Stronger correlation between opposite chiralities

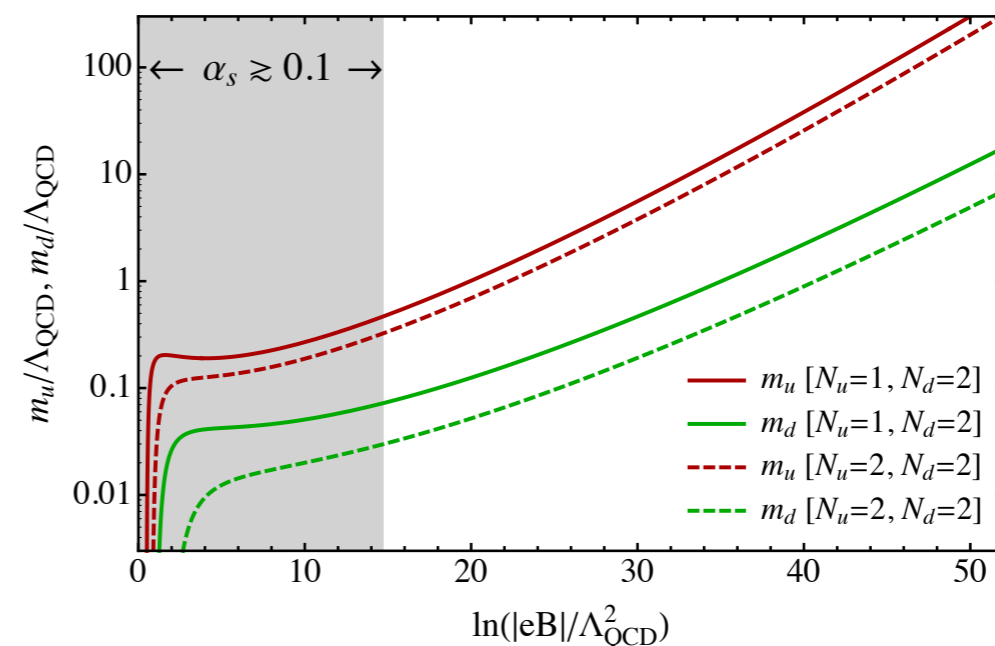
Free chiral fermions in 2+1:

$$\langle \bar{q}q \rangle = \frac{|eB|}{2\pi}$$

NJL in 3+1 (supercritical):

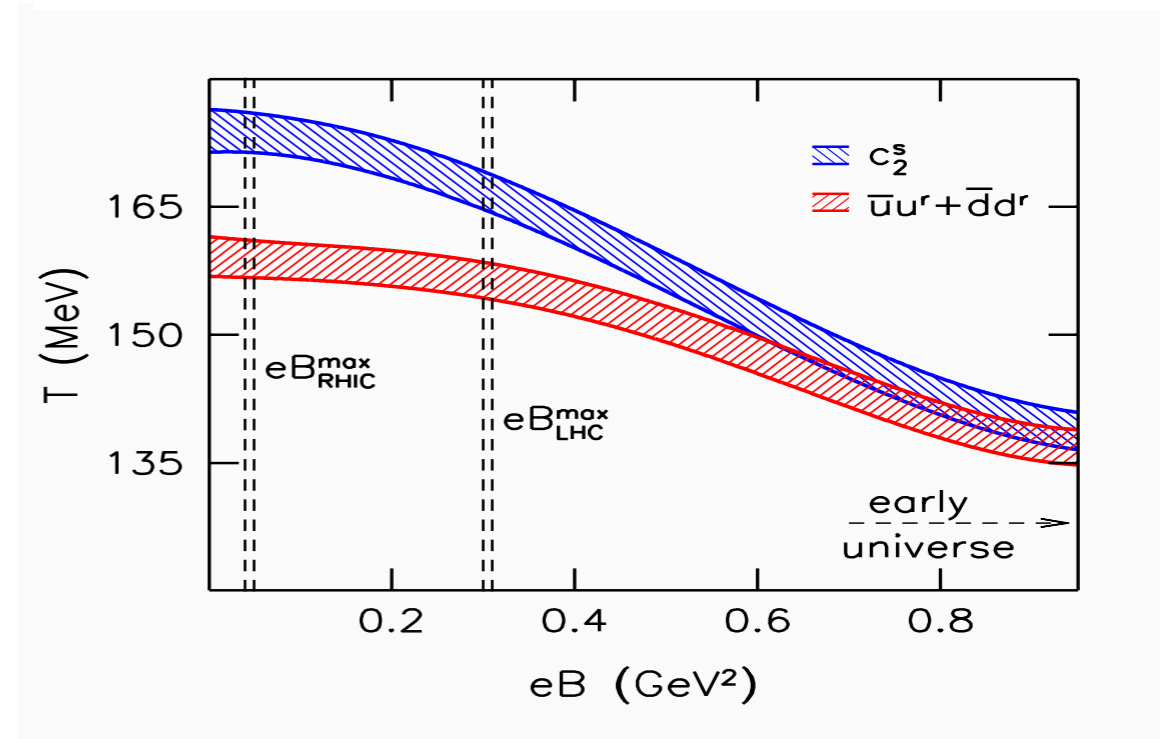
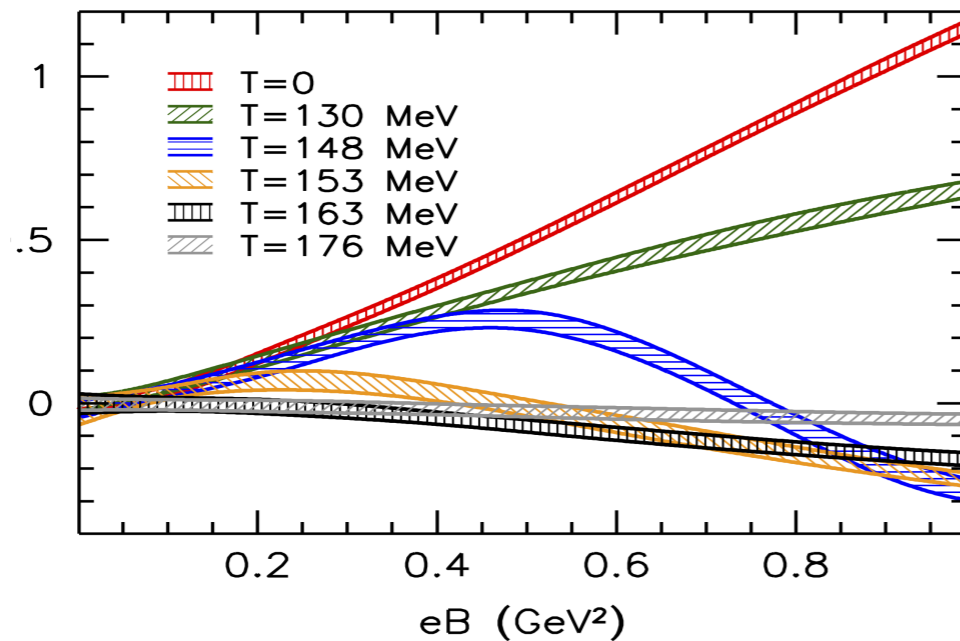
$$\langle \bar{q}q \rangle = \langle \bar{q}q \rangle_0 \left(1 + \frac{|eB|^2}{3G^4 (\langle \bar{q}q \rangle_0)^4 \log(\Lambda/G\langle \bar{q}q \rangle_0)^2} \right)^{\frac{1}{2}}$$

Gap equation in resummed pQCD



Magnetic catalysis on the lattice

Bali, Schafer et al '11 '12



- B acts destructively for $T \gtrsim T_c$
- Inverse effect missed in earlier studies with large m & coarse lattices

D'Elia et al '11

Magnetic catalysis generally

- **Banks-Casher relation** $\langle \bar{\psi}\psi \rangle = \pi\rho(0)$

Banks, Casher '80

Condensate \Leftrightarrow Dirac spectrum around zero

In LL_0 approx $\langle \bar{q}q \rangle \propto eB$

Likely to fail in presence of strong correlations

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Likely to fail in presence of strong correlations

- **Two competing contributions in general:** D'Elia, Negro '11; Bruckmann, Endrodi, Kovacs '13

$$\langle \bar{q}q \rangle = \int \mathcal{D}A e^{-S[A]} \det(D(A, B) + m) \text{tr}(D(A, B) + m)^{-1}$$

Banks-Casher applies to **valence** contribution \Rightarrow catalysis

Sea contribution acts destructively near $T_c \Rightarrow$ decatalysis:

Sea prefers A configurations that order the Polyakov loop near T_c

\Rightarrow punishes configurations with small Dirac eigenvalues

Bruckmann, Endrodi, Kovacs '13

Questions for holography

- **Valence** vs. **sea** separation fails at larger B , conjecture still holds?
- Lattice does not cover large B , what happens there?
- Are there other mechanisms at work?
- Magnetic catalysis at finite μ ?
- Are there new phases at finite T - B - μ ?

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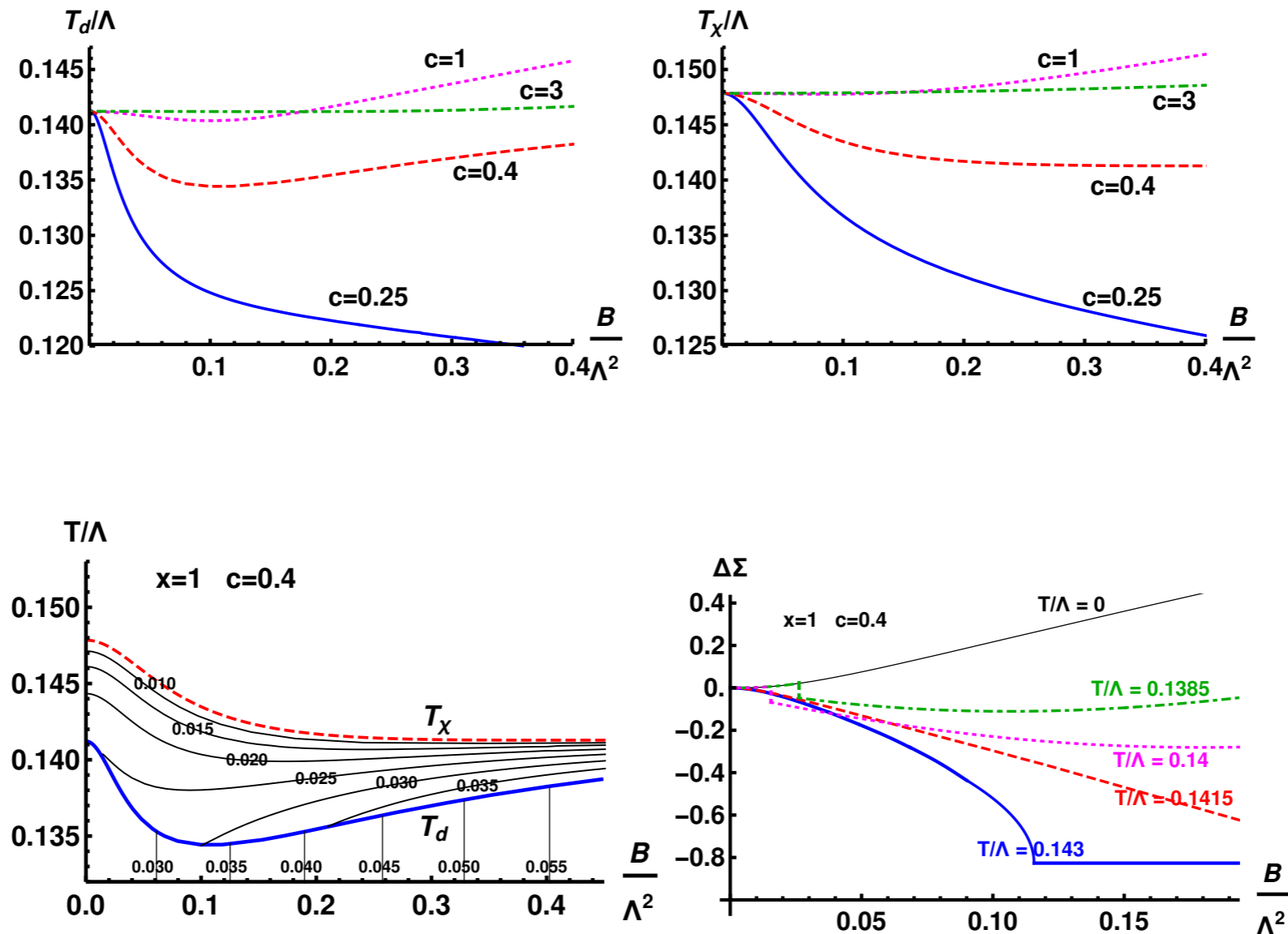
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Introduce μ and B in $V_\mu = (V_0(r), -x_2 B/2, x_1 B/2, 0, 0)$

Quark condensate in $\tau = m_q r (-\log \Lambda r)^{-\rho} + \langle \bar{q}q \rangle (-\log \Lambda r)^\rho + \dots$

Magneto-holographic QCD: inverse magnetic catalysis

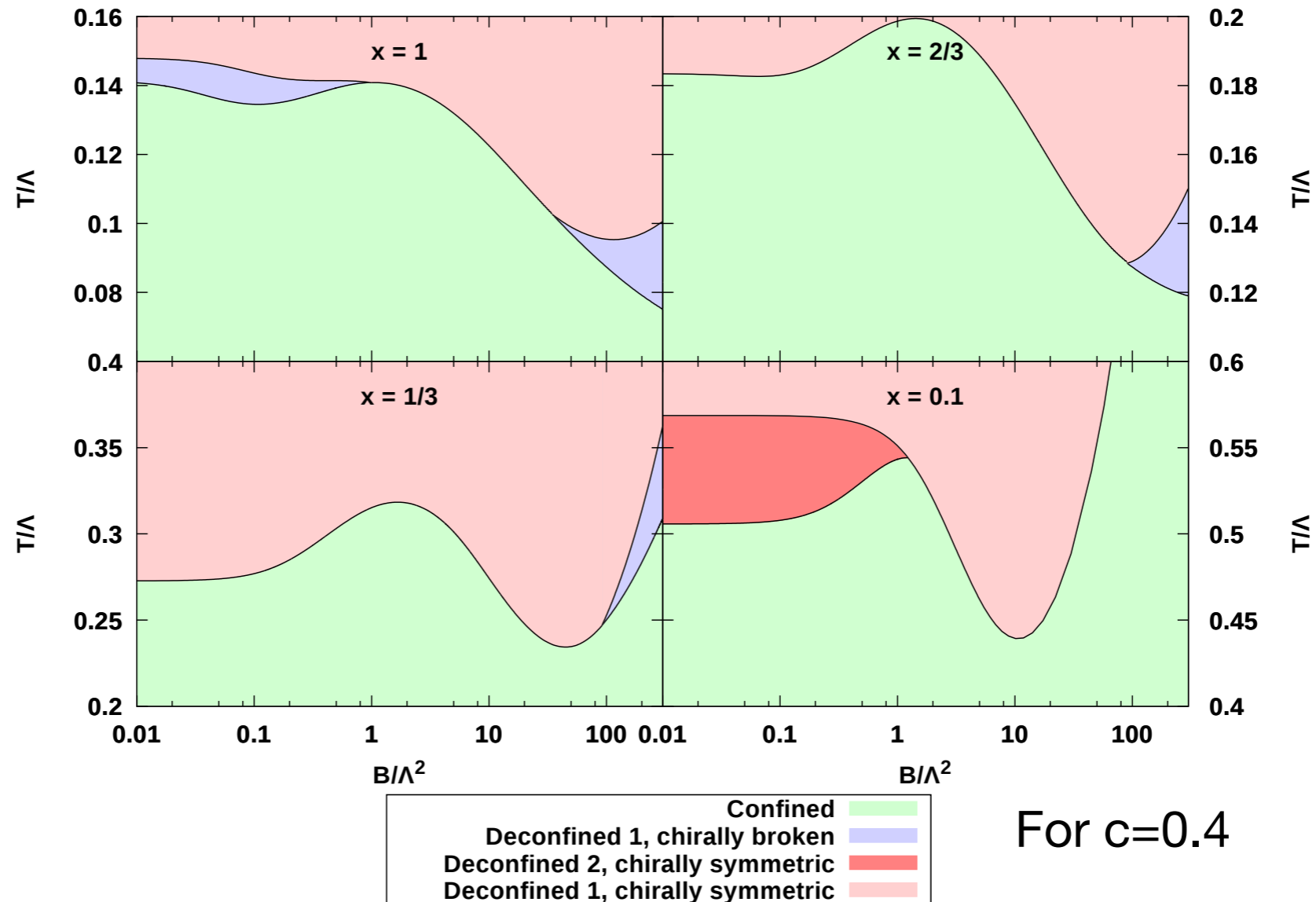
Preis, Rebhan, Schmitt '10; Mamo '15; Noronha et al '15; Evans et al '16;
Iatrakis, Jarvinen, Nijs, UG '16;



- Both T_χ and T_c generically decrease with B
- Clear sign of inverse magnetic catalysis around $T_\chi \sim T_c$ for small B
- Inverse catalysis more pronounced for small c
- Catalysis comes back at larger B
- T dependence suppressed in the confined phase as $1/N^2$

Magneto-holographic QCD: phase diagram

Iatrakis, Jarvinen, Nijs, UG '16



- Generically 3 separate phases with 1st and 2nd order boundaries
- Both T_x and T_c generically decrease with B
- New deconfined/chirally broken phase at very large B consistent with pQCD

Testing the valence vs. sea explanation

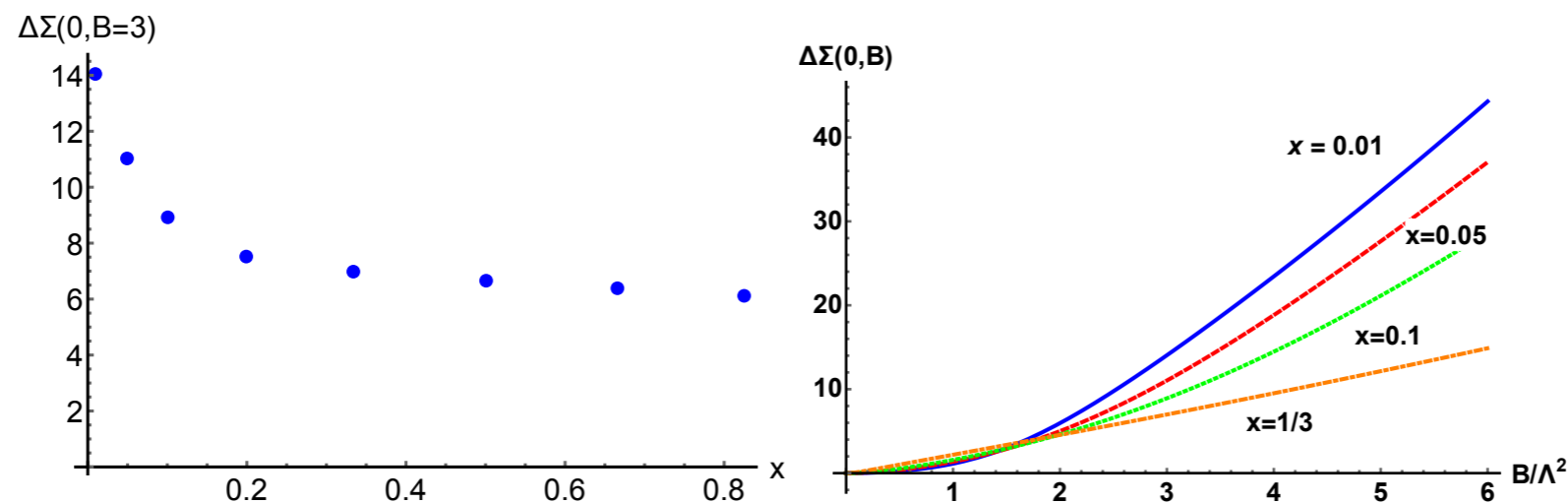
Iatrakis, Jarvinen, Nijs, UG '16

Two separate dependence on B: 1. Explicit dependence in the EOM for τ
2. Implicit dependence through the background fields

Tempting to identify 1 with the valence 2 with the sea

At large B explicit dependence vanishes \Rightarrow sea quarks

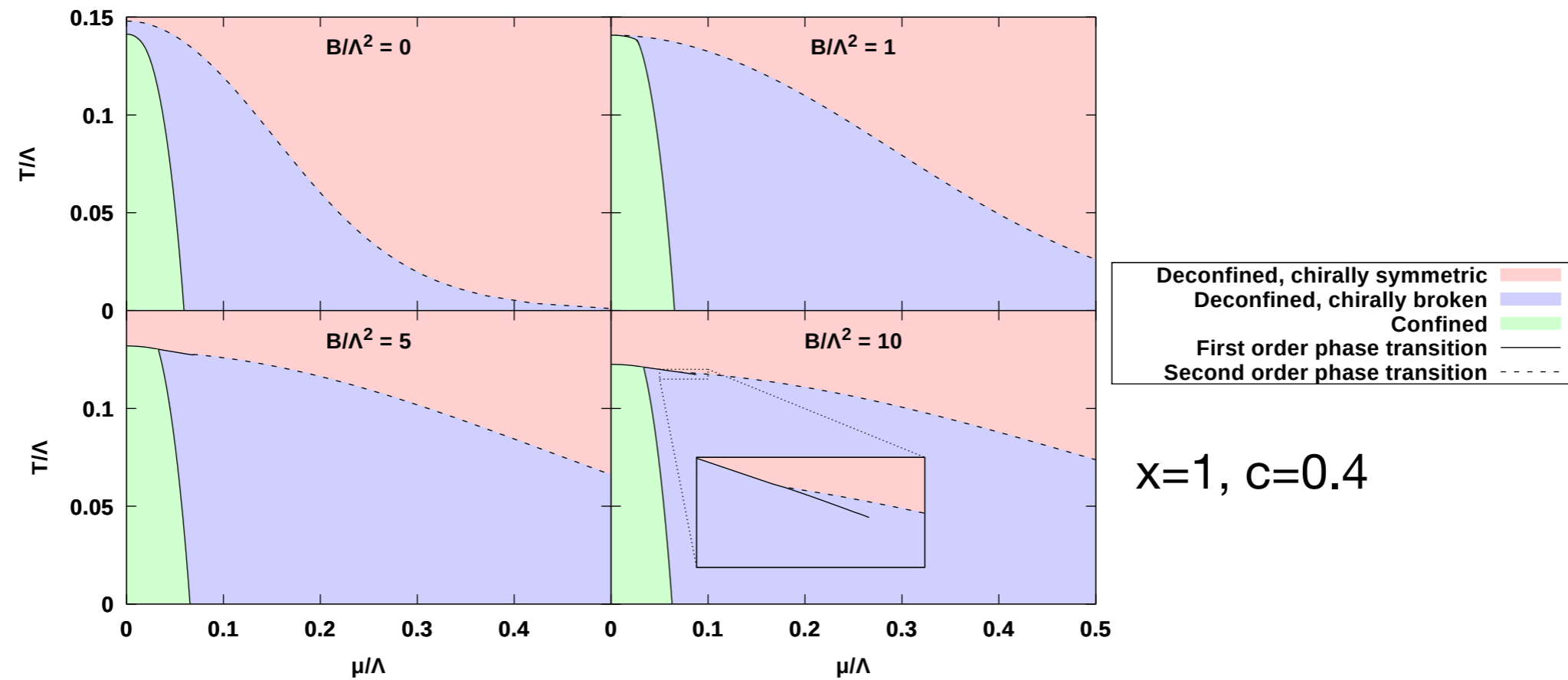
B influences background functions only through x \Rightarrow large x, more sea quarks



Holography supports the valence vs. sea explanation

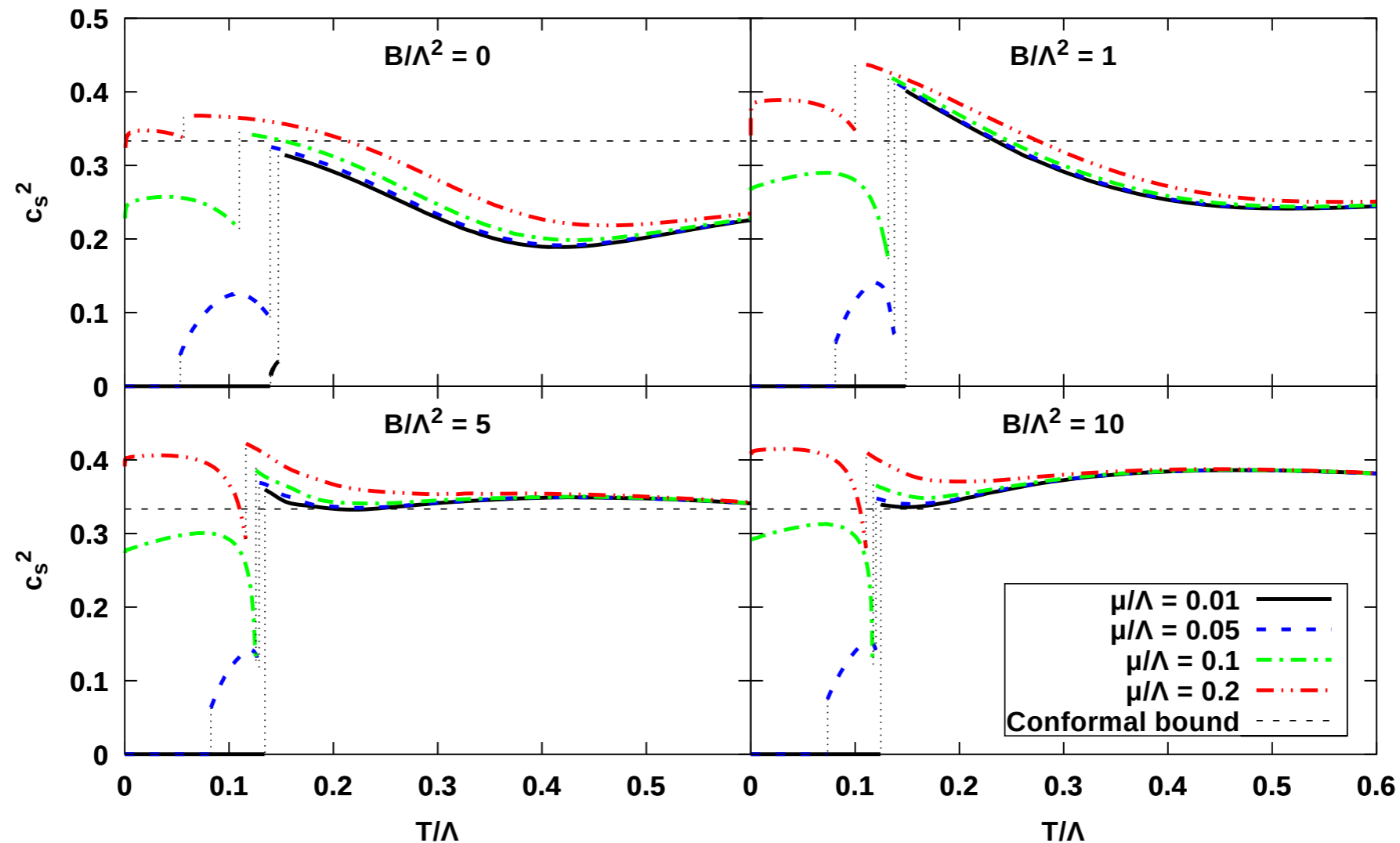
Finite μ

Jarvinen, Nijs, UG '17



- Deconfined/chiral asymmetric phase enlarged at finite μ
- Separation between confinement and χ SB scales shrink at larger B

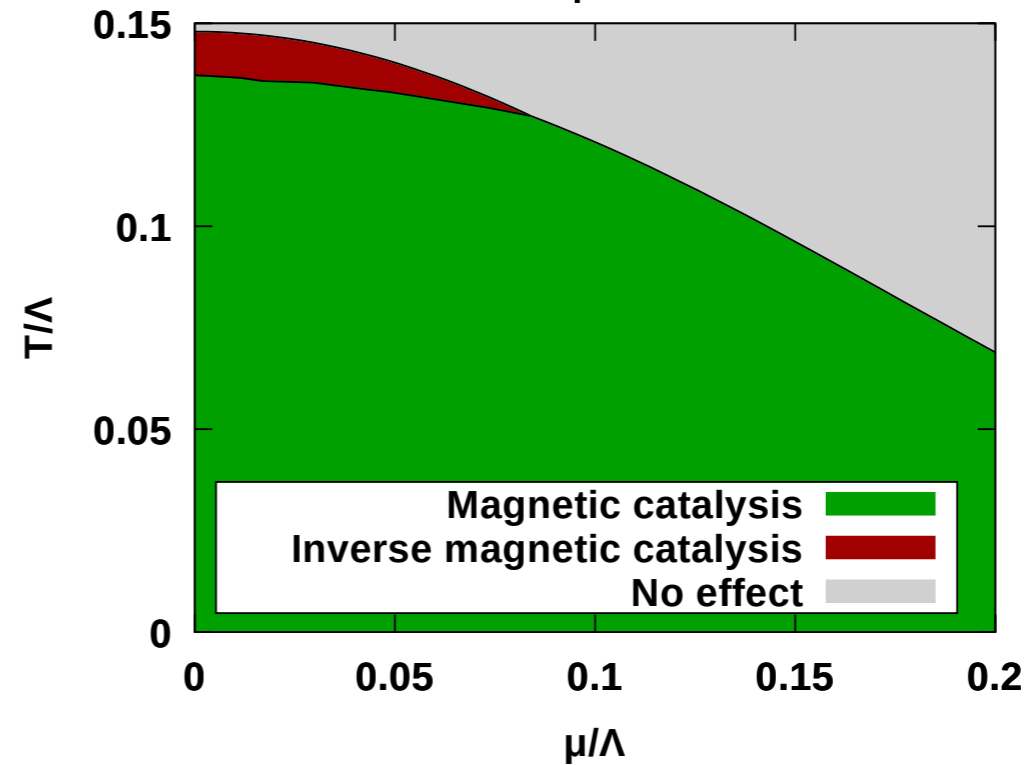
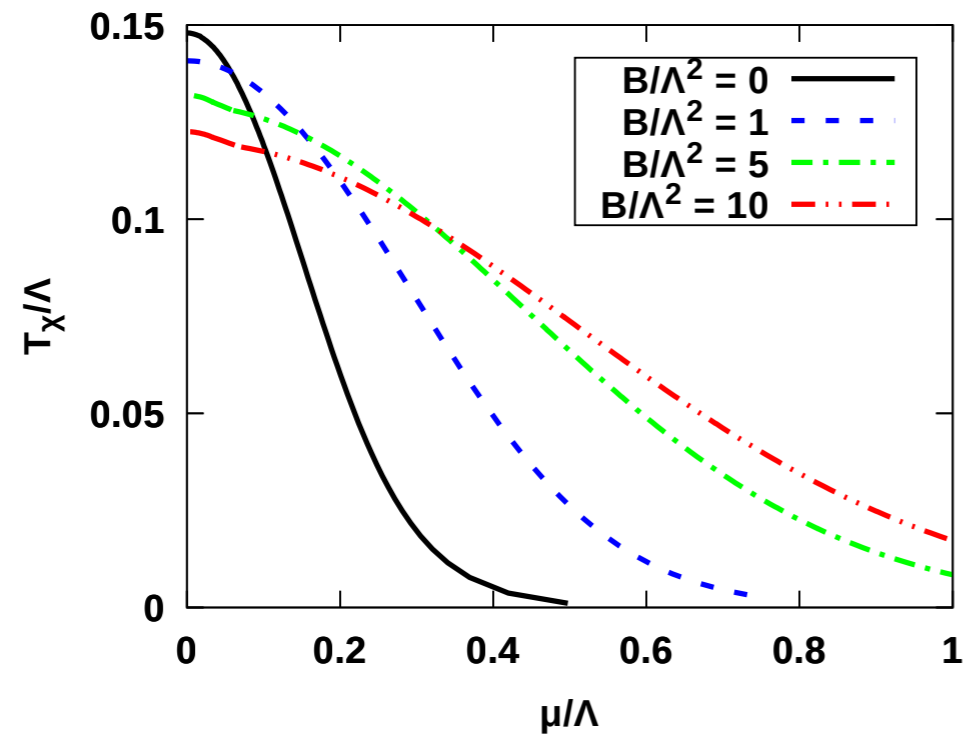
Speed of sound at finite μ and B



$$c_s^2 = \left. \frac{s dT + n d\mu}{T ds + \mu dn + B dM} \right|_{n/s, B}.$$

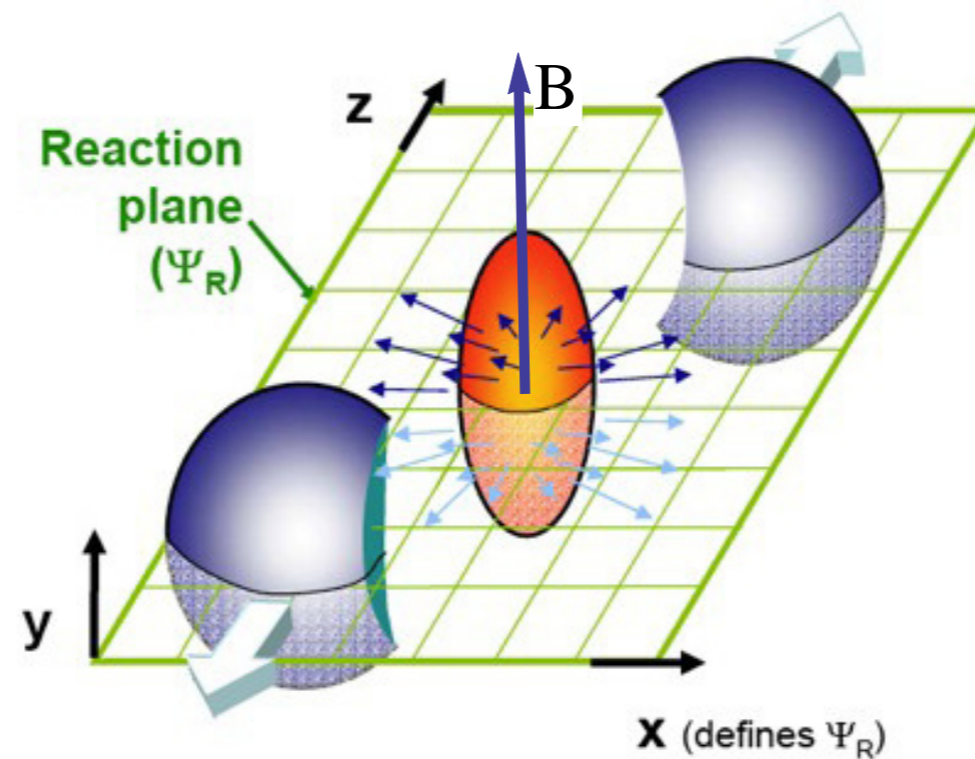
- Jumps at the phase boundaries
- Tends to increase both with μ and B
- Exceeds the conformal value $1/3$ generically
- Limits to $1/3$ from below at larger T , in agreement with earlier results

Chiral condensate at finite μ



- B facilitates the chiral transition for $\mu < 0.1 \Rightarrow$ inverse catalysis for small μ
- Magnetic catalysis instead at $\mu > 0.1$
- A small region of inverse magnetic catalysis in the phase diagram

Dynamics induced by anisotropy



- Anisotropic QGP produced in off-central collisions due to different pressure gradients
 - Does anisotropy act similar to B?
 - How to distinguish the effects of anisotropy from B?
- ⇒ consider an anisotropic but neutral plasma

A heuristic discussion

Jarvinen, Nijs, Pedraza, UG '18

Introduce anisotropy through space dependent θ -term: $\theta = a z$

$$Z[A_5, \theta] = \int \mathcal{D}q \mathcal{D}A^a e^{-\int L[A^a, q] + A_5 \cdot J^5 + \theta \text{Tr} \star F \wedge F}$$

invariant under $A_5 \rightarrow A_5 + d\lambda_5, \quad \theta \rightarrow \theta - c_a \lambda_5.$

because of the anomaly $d \star J_5 = c_a \text{Tr} F \wedge F.$

Rotate θ into the quark propagator:

$$\langle \bar{q}q \rangle_a = \frac{1}{\mathcal{Z}(a)} \int \mathcal{D}A_\mu^a e^{-S_g} \det(\not{D}(a)) \text{Tr} (\not{D}(a))^{-1},$$

$$\not{D}(a) = \gamma^\mu (\partial_\mu + A_\mu^a T^a) + \frac{a}{c_a} \gamma^3 \gamma^5.$$

Do valence and sea also have opposite effects?

Holographic, anisotropic, non-conformal, neutral plasma

Giataganas, Pedraza, UG '17

Nonconformality \Leftrightarrow a scalar ϕ , anisotropy \Leftrightarrow another scalar χ

$$S = \frac{1}{2\kappa^2} \int d^5x \sqrt{-g} [R + \mathcal{L}_M],$$
$$\mathcal{L}_M = -\frac{1}{2}(\partial\phi)^2 + V(\phi) - \frac{1}{2}Z(\phi)(\partial\chi)^2,$$

$$ds^2 = e^{2A(r)} \left[-f(r)dt^2 + d\vec{x}_\perp^2 + e^{2h(r)}dx_3^2 + \frac{dr^2}{f(r)} \right],$$
$$\phi = \phi(r), \quad \chi = a x_3. \quad \phi \rightarrow jr^{4-\Delta}$$

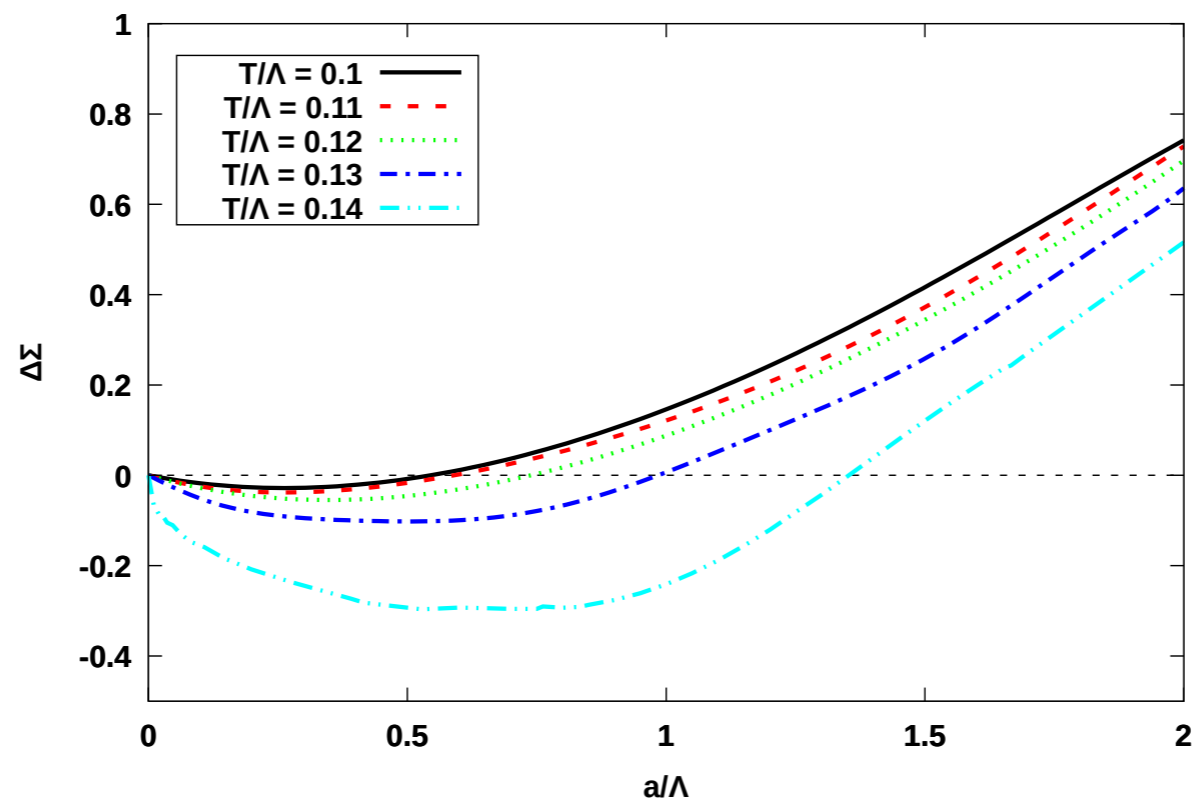
Holographic, anisotropic, non-conformal, neutral plasma

Giataganas, Pedraza, UG '17

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$$\phi = \phi(r), \quad \chi = ax_3. \quad \phi \rightarrow jr^{4-\Delta}$$



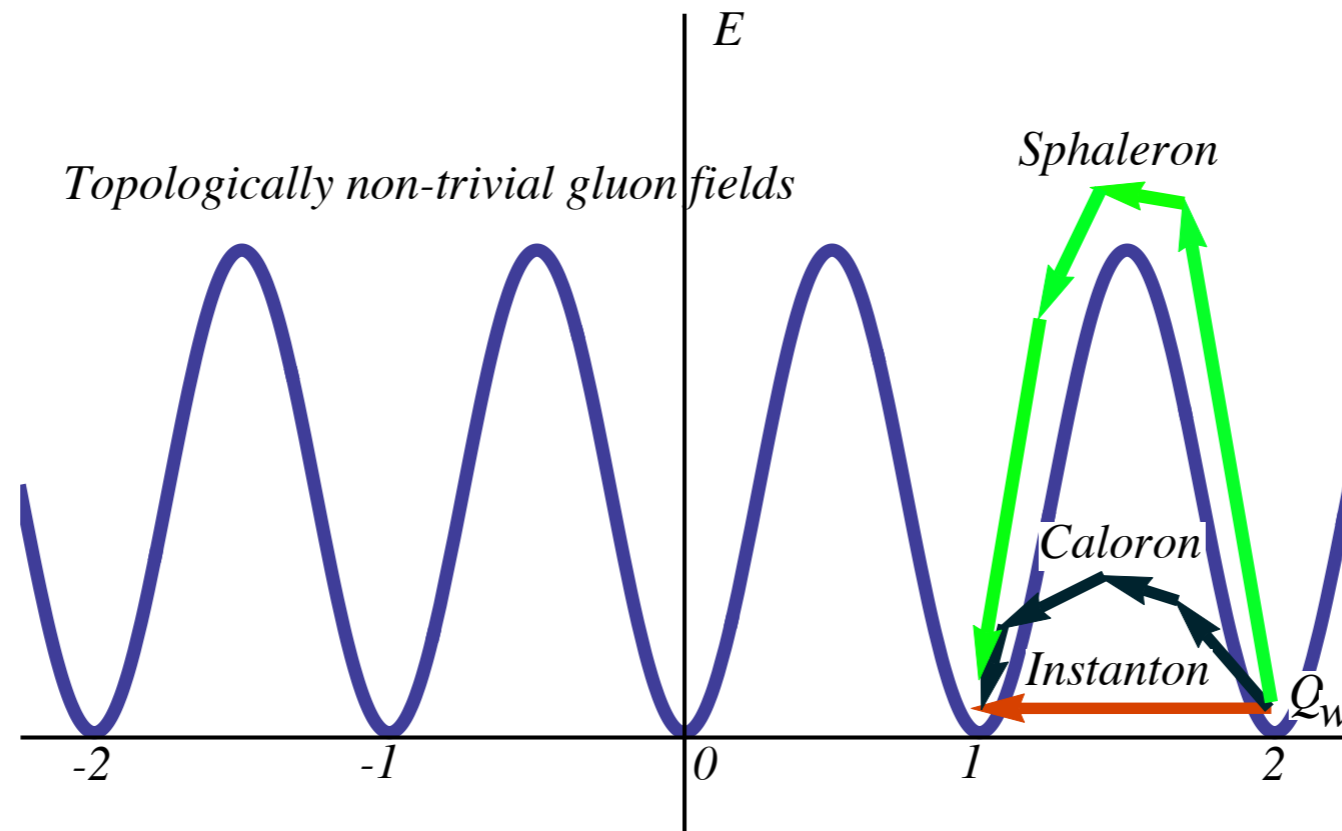
Inverse anisotropic catalysis

Conclusions I

- Holography reproduces **inverse magnetic catalysis** generically
- Supports **valence** vs. **sea** competition
Valence \Leftrightarrow explicit dependence in the tachyon equation
Sea \Leftrightarrow implicit dependence through background functions
- Inverse magnetic catalysis only for small μ
- **Inverse anisotropic catalysis:**
source of IMC anisotropy rather than charge dynamics caused by B ?
- New phases: confined-chiral symmetric, anisotropic confinement

Part II: Chern-Simons diffusion rate

Chern-Simons diffusion rate



$$\Delta N_{CS} = \frac{g^2}{32\pi^2} \int \text{tr} G \wedge G$$

Probability per unit time x volume of a CS number changing process:

$$\Gamma_{CS} = \frac{\langle \Delta N_{CS}^2 \rangle}{Vt} = \int d^4x \left\langle \frac{g^2}{32\pi^2} \text{tr} G \wedge G(x) \frac{g^2}{32\pi^2} \text{tr} G \wedge G(0) \right\rangle$$

Chern-Simons diffusion rate

Perturbative result: $\Gamma_{CS}/T^4 \approx 193\alpha_s^5$

Moore et al '99

N=4 sYM: $\Gamma_{CS}/T^4 = \frac{(g^2 N)^2}{256\pi^3} \approx 0.045$

Son, Starinets '02

Chern-Simons diffusion rate

Perturbative result: $\Gamma_{CS}/T^4 \approx 193\alpha_s^5$

Moore et al '99

N=4 sYM: $\Gamma_{CS}/T^4 = \frac{(g^2 N)^2}{256\pi^3} \approx 0.045$

Son, Starinets '02

Improved hQCD:

$$\Gamma_{CS} = \frac{1}{N^2} \frac{sT}{2\pi} Z(\lambda_h)$$

Iatrakis, Kiritsis, O'Bannon, UG '12

$$\frac{\Gamma_{CS}/(\kappa^2 Z_0/2\pi)}{(sT/N_c^2)}$$

2.0

$$1.64 \leq \Gamma_{CS}(T_c)/T_c^4 \leq 2.8.$$

1.5

1.0

0.5

1

2

3

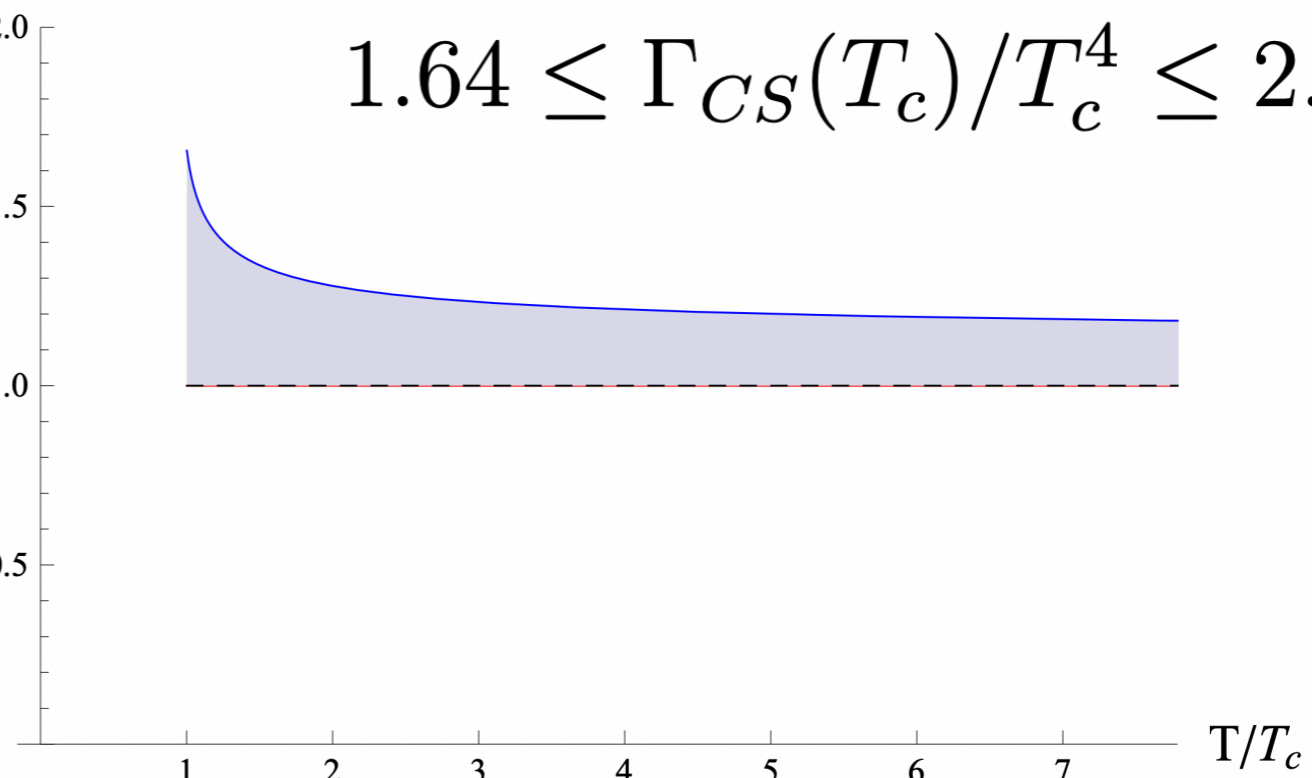
4

5

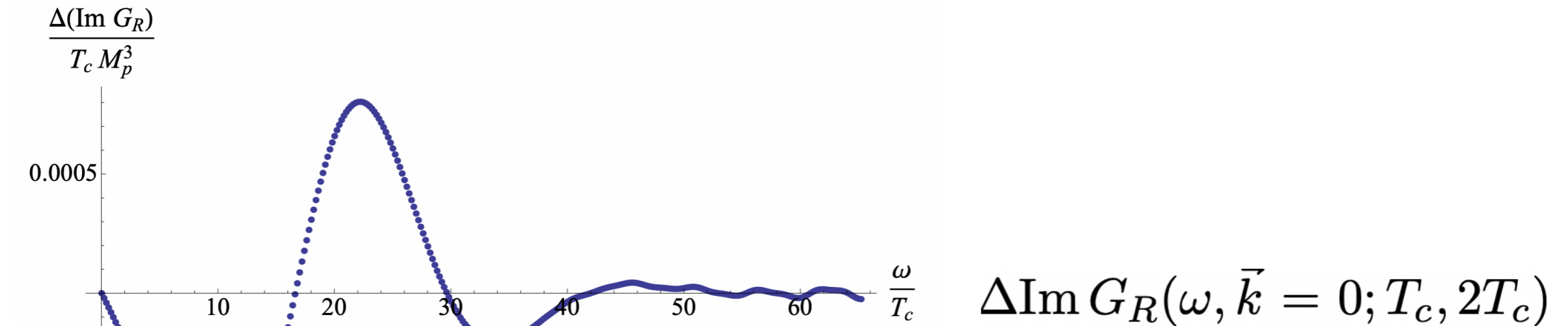
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7

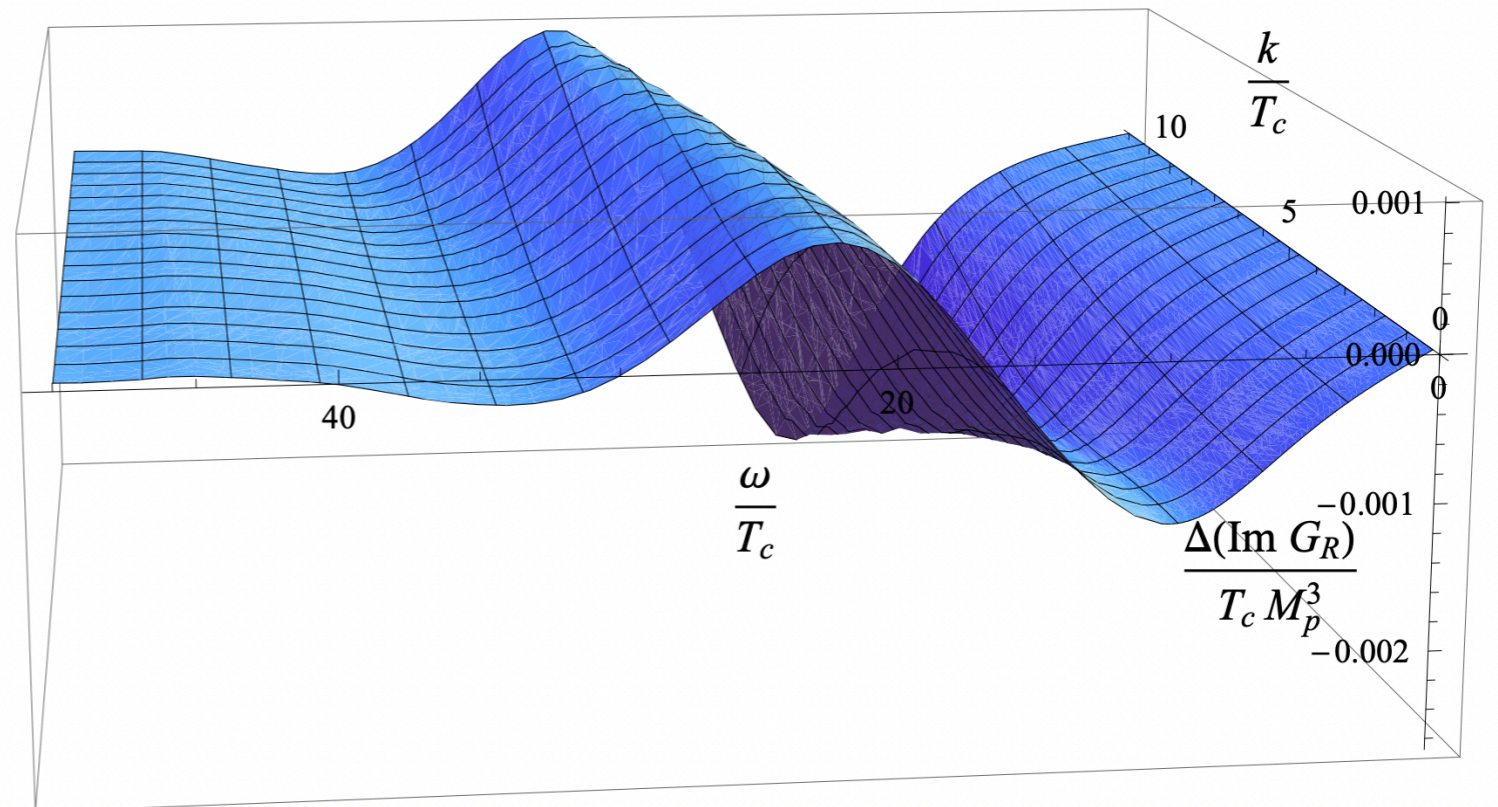
T/T_c



Frequency and momentum dependence



$$\Delta \text{Im } G_R(\omega, \vec{k}, T_c, 2T_c)$$



Conclusions II

- Improved holographic models predict larger Γ_{cs}
- Nontrivial ω and k dependence \Rightarrow spatial modulation of Γ_{cs}

Part III: Spin currents in QGP

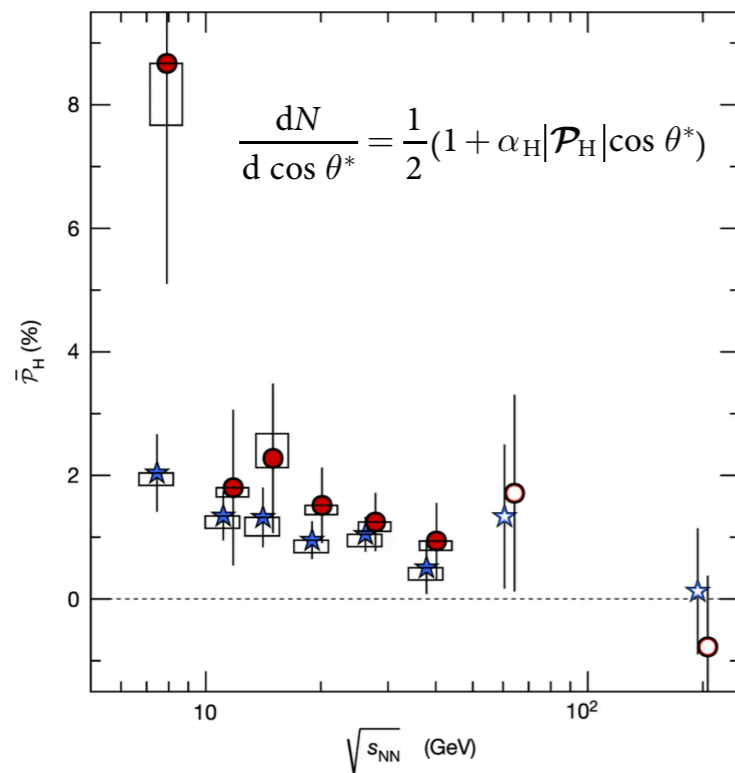
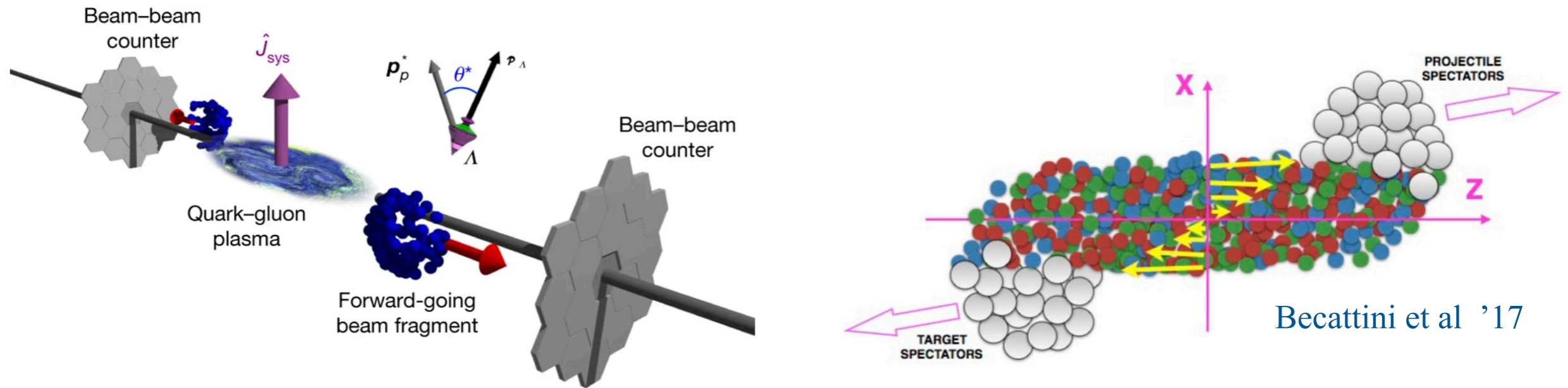
Spin-hydrodynamics



Strong vortical structure

$$\omega \sim 10^{22} \text{ s}^{-1}$$

Global spin polarization

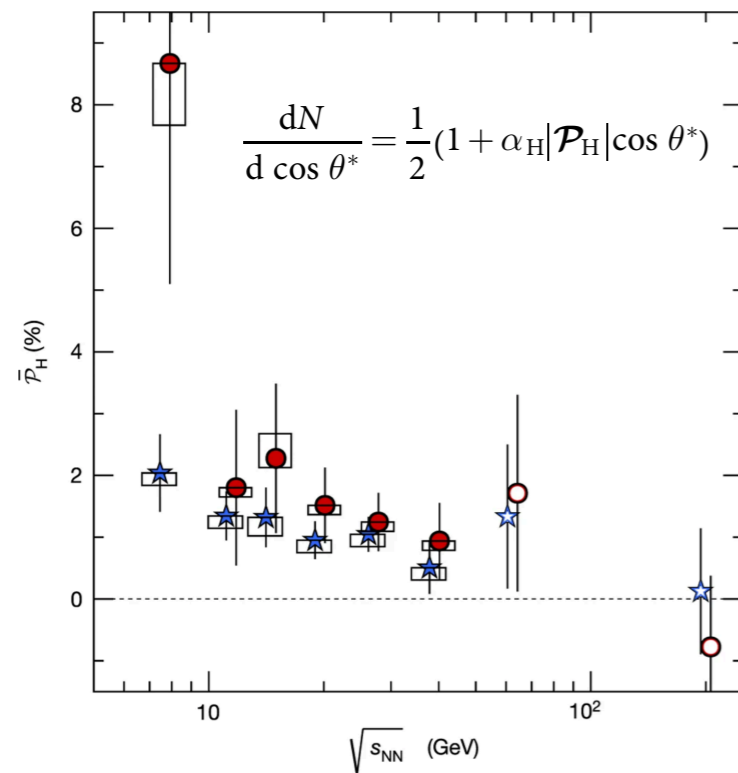
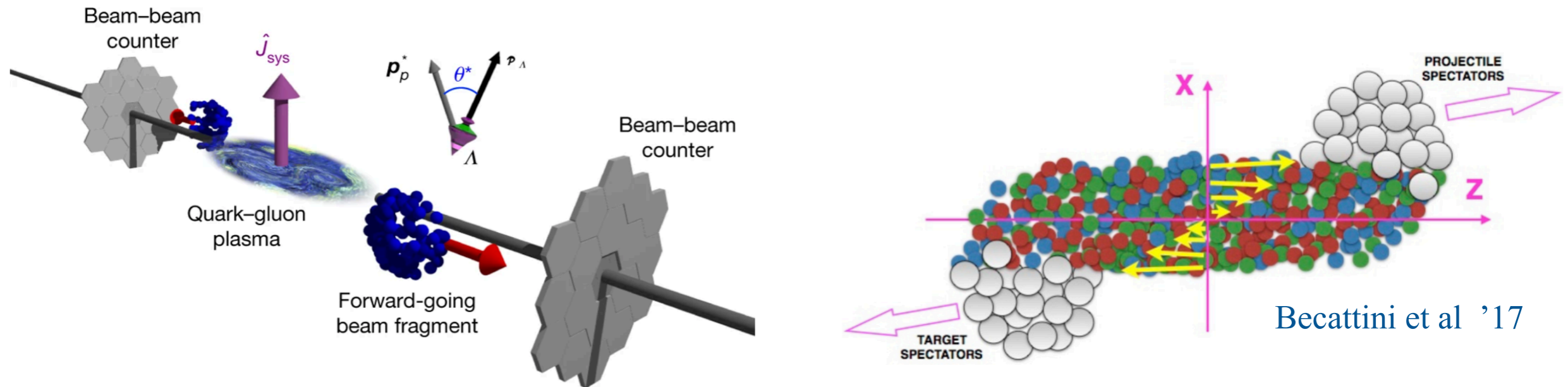


Global hyperon polarization at RHIC
by spin-orbit coupling $\vec{S} \cdot \vec{J}$

QGP: most vortical fluid: $\omega \sim 10^{22} \text{ s}^{-1}$

STAR collaboration, RHIC '19

Global spin polarization



Global hyperon polarization at RHIC
by spin-orbit coupling $\vec{S} \cdot \vec{J}$

QGP: most vortical fluid: $\omega \sim 10^{22} \text{ s}^{-1}$

STAR collaboration, RHIC '19

\Rightarrow hydrodynamic description?

Hydrodynamics with spin current

Gallegos, Yarom, UG '21

Slow variables: energy-momentum and spin current

$$T_{\mu\nu} \quad S_{\mu\nu}^{\lambda}$$

Earlier work: Becattini et al '08; Becattini, Piccinini '08
Karabali, Nair '14
Florkowski et al '18 '19; Hattori, X.-G. Huang et al '19
Gallegos, UG '19; Li, Stephanov, Yee '20

Hydrodynamics with torsion

- Metric couples to energy-momentum, contorsion sources spin :

$$\omega_{\mu}^{ab} = \dot{\omega}_{\mu}^{ab} + K_{\mu}^{ab}, \quad \dot{\omega} \sim \partial e$$

Hydrodynamics with torsion

- Metric couples to energy-momentum, contorsion sources spin :

$$\omega_{\mu}^{ab} = \dot{\omega}_{\mu}^{ab} + K_{\mu}^{ab}, \quad \dot{\omega} \sim \partial e$$

- Hydrodynamics on a manifold with non-trivial torsion:

$$T^{\mu\nu} = \frac{\delta W}{\delta e_{\mu}^a} e_a^{\nu}, \quad S_{ab}^{\lambda} = \frac{\delta W}{\delta \omega_{\lambda}^{ab}}$$

Hydrodynamic equations

$$\mathring{\nabla}_\mu T^{\mu\nu} = \frac{1}{2} R^{\rho\sigma\nu\lambda} S_{\rho\lambda\sigma} - T_{\rho\sigma} K^{\nu ab} e^\rho{}_a e^\sigma{}_b \quad 4 \text{ equations}$$

$$\mathring{\nabla}_\lambda S^\lambda{}_{\mu\nu} = 2T_{[\mu\nu]} - 2S^\lambda{}_{\rho[\mu} e_{\nu]}{}^a e_\rho{}^b K_{\lambda ab}, \quad 6 \text{ equations}$$

Hydrodynamic equations

$$\mathring{\nabla}_\mu T^{\mu\nu} = \frac{1}{2} R^{\rho\sigma\nu\lambda} S_{\rho\lambda\sigma} - T_{\rho\sigma} K^{\nu ab} e^\rho{}_a e^\sigma{}_b \quad 4 \text{ equations}$$

$$\mathring{\nabla}_\lambda S^\lambda{}_{\mu\nu} = 2T_{[\mu\nu]} - 2S^\lambda{}_{\rho[\mu} e_{\nu]}{}^a e_\rho{}^b K_{\lambda ab}, \quad 6 \text{ equations}$$

10 dynamical variables:

T

u^μ

$$\mu^{ab} = \omega_\mu^{ab} u^\mu$$

Spin “chemical”
potential

Analogous to electric potential

$$\mu_E = A_\mu u^\mu$$

Conformal spin hydro

Equations of motion + constitutive relations: determine T , u and $\mu^{\alpha\beta}$

$$\mu^{ab} = 2u^{[a} \underbrace{m^{b]}_{\text{“electric”}}} + \epsilon^{abcd} u_c \underbrace{\tilde{M}_d}_{\text{“magnetic”}}$$

$$u^\alpha \mathcal{D}_\alpha T = \hat{\eta} \sigma_{\alpha\beta} \sigma^{\alpha\beta},$$

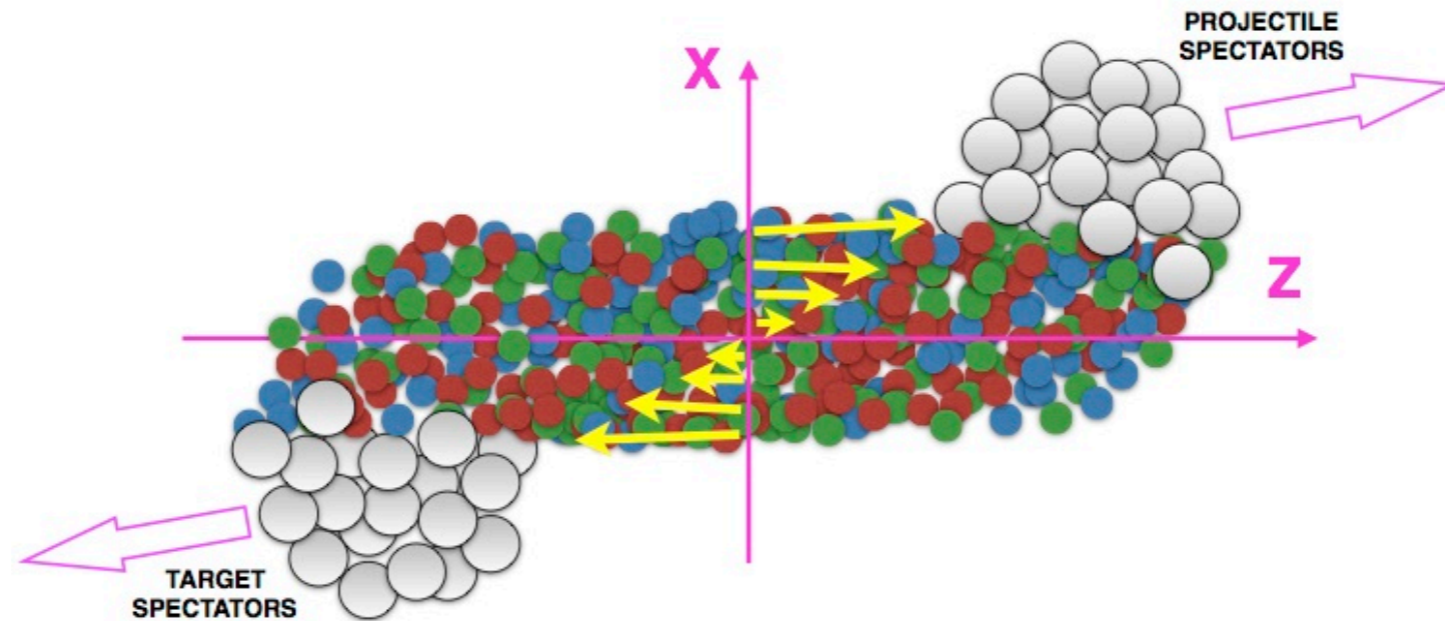
$$\Delta_\beta^\nu \mathcal{D}_\alpha \sigma^{\alpha\beta} = \left(\frac{\Delta^{\nu\beta}}{3\hat{\eta}} - \frac{3\sigma^{\nu\beta}}{T} \right) \mathcal{D}_\beta T,$$

$$\Delta_\beta^\lambda u^\alpha \mathcal{D}_\alpha m^\beta = c_1 \Delta_\beta^\lambda \mathcal{D}_\alpha \sigma^{\alpha\beta} + c_2 \Delta_\beta^\lambda \mathcal{D}_\alpha M^{\alpha\beta} + c_4 \sigma^{\lambda\alpha} m_\alpha + c_7 M^{\lambda\alpha} m_\alpha + c_8 \Omega^{\lambda\alpha} m_\alpha,$$

$$\Delta_\alpha^\rho \Delta_\beta^\sigma u^\lambda \mathcal{D}_\lambda M^{\alpha\beta} = -\hat{\sigma} \Delta_\alpha^\rho \Delta_\beta^\sigma u^\lambda \mathcal{D}_\lambda \Omega^{\alpha\beta} + c_3 \Delta^{\alpha[\rho} \Delta^{\sigma]\beta} \mathcal{D}_\alpha m_\beta + c_5 \sigma^{\alpha[\rho} M^{\sigma]}_\alpha + c_6 \sigma^{\alpha[\rho} \Omega^{\sigma]}_\alpha + c_9 M^{\alpha[\rho} \Omega^{\sigma]}_\alpha$$

Need: initial conditions + transport coefficients

Application to HIC

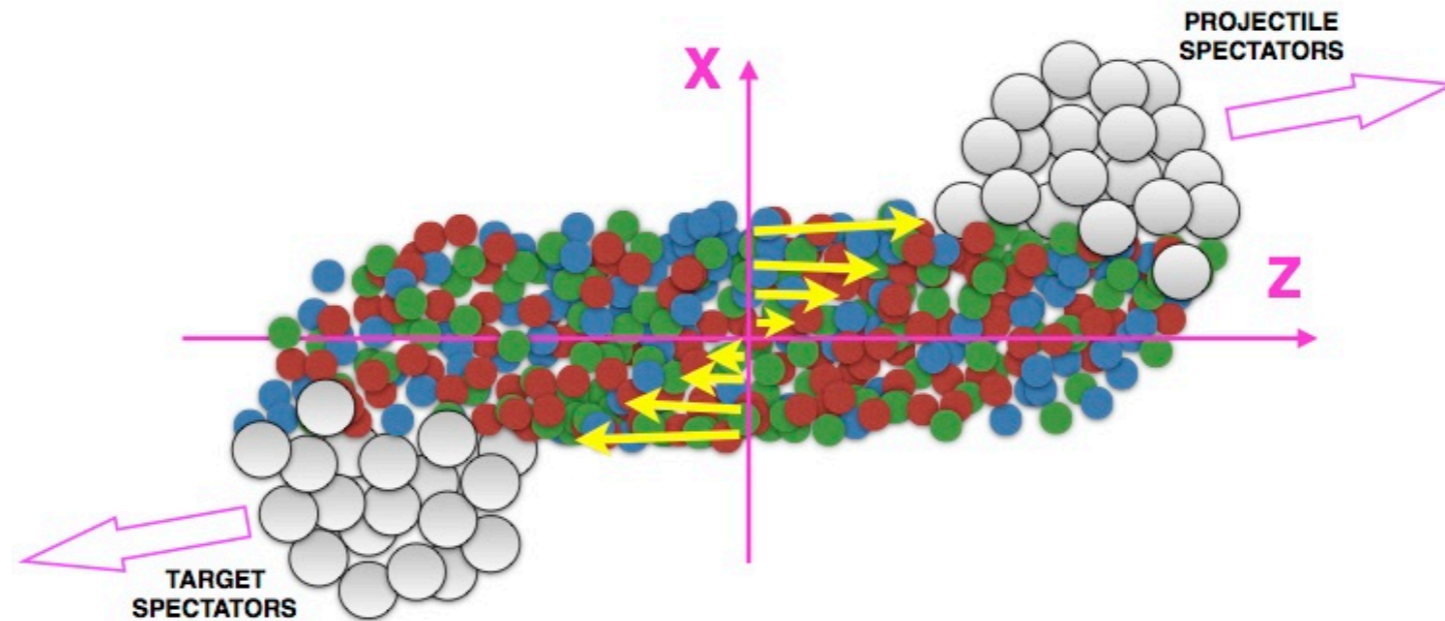


Polarization of hyperon:

$$\Pi_{\mu}(p) = -\frac{1}{4} \epsilon_{\mu\rho\sigma\beta} \frac{p^{\beta} \int d\Sigma_{\lambda} p^{\lambda} B(x, p) \mu^{\rho\sigma} \dots \dots \blacktriangleright \text{spin potential}}{m \dots \dots 2 \int d\Sigma_{\lambda} p^{\lambda} n_F \dots \dots \blacktriangle \text{ Boltzmann type distribution}}$$

freezout surface

Application to HIC



Polarization of hyperon:

$$\Pi_\mu(p) = -\frac{1}{4} \epsilon_{\mu\rho\sigma\beta} \frac{p^\beta \int d\Sigma_\lambda p^\lambda B(x, p) \mu^{\rho\sigma} \dots \blacktriangleright \text{spin potential}}{m \dots \blacktriangle \text{ Boltzmann type distribution} \quad 2 \int d\Sigma_\lambda p^\lambda n_F \dots}$$

▲ freezout surface
▲ Boltzmann type distribution

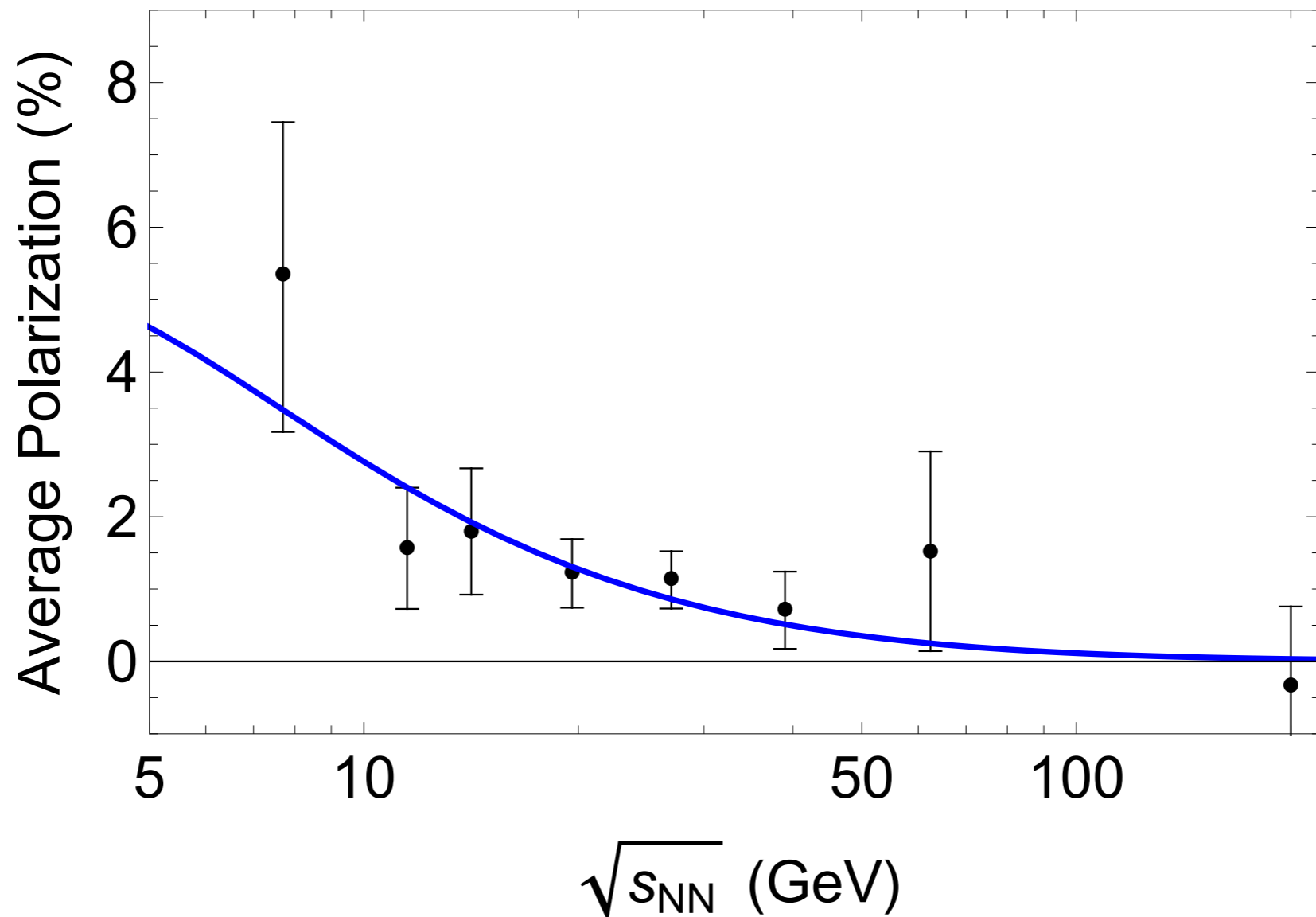
Spin hydrodynamics \Rightarrow spin potential

Comparison to data

Hydrodynamic solution, for small “kinematic viscosity”/time $\frac{3\eta_0}{4\epsilon_0} \frac{1}{T\tau} \ll 1$

Floerschinger, Wiedemann '11

$$\delta m^x(\tau) \propto \tau^{-\frac{8}{3}} e^{-\frac{9q^2\eta_0\tau_0}{16T_0\epsilon_0} \left(\frac{\tau}{\tau_0}\right)^{\frac{4}{3}}}, \quad \delta M^{x\eta}(\tau) \propto q^2 \tau^{-\frac{5}{3}} e^{-\frac{9q^2\eta_0\tau_0}{16T_0\epsilon_0} \left(\frac{\tau}{\tau_0}\right)^{\frac{4}{3}}}$$

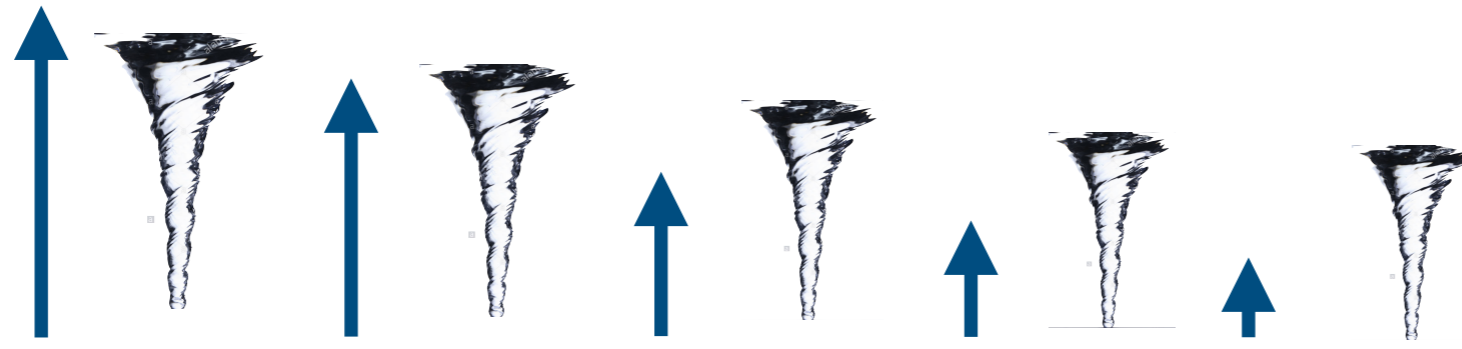


Conclusions III

- Spin-hydrodynamics: a novel theory of relativistic hydro
[Gallegos, Yarom, UG '22](#)
- Belinfante-Rosenfeld ambiguity fixed by torsion
- Reproduces observed global polarization of hyperons

Outlook

Magnetic field + vortices

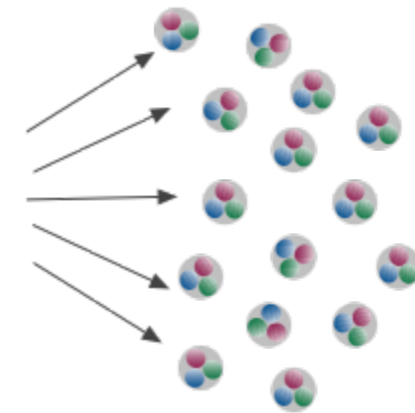


Time

Formation

Adiabatic evolution

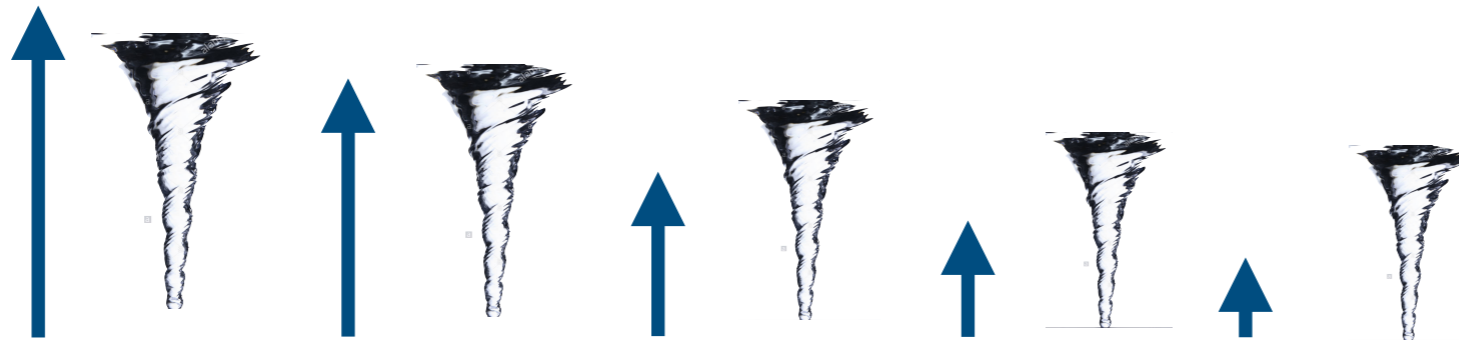
Decay



Hydrodynamics

Outlook

Magnetic field + vortices

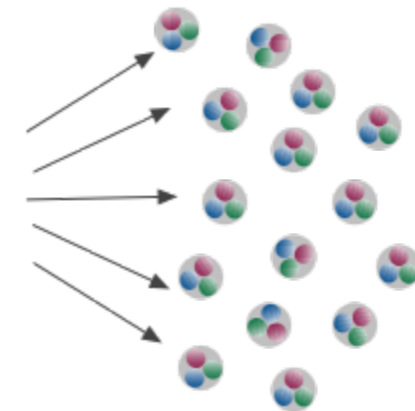


Time

Formation

Adiabatic evolution

Decay

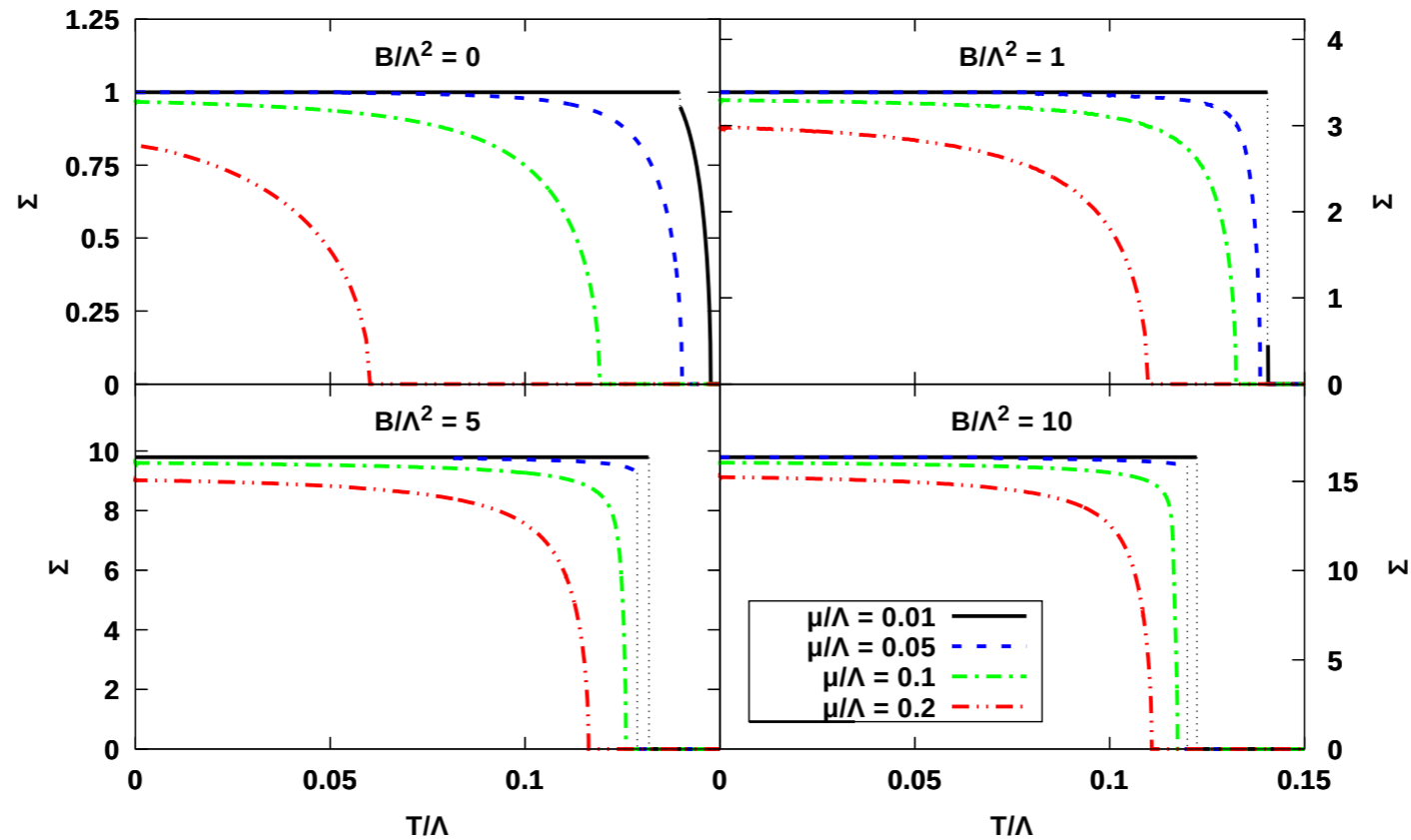


Holography

Hydrodynamics

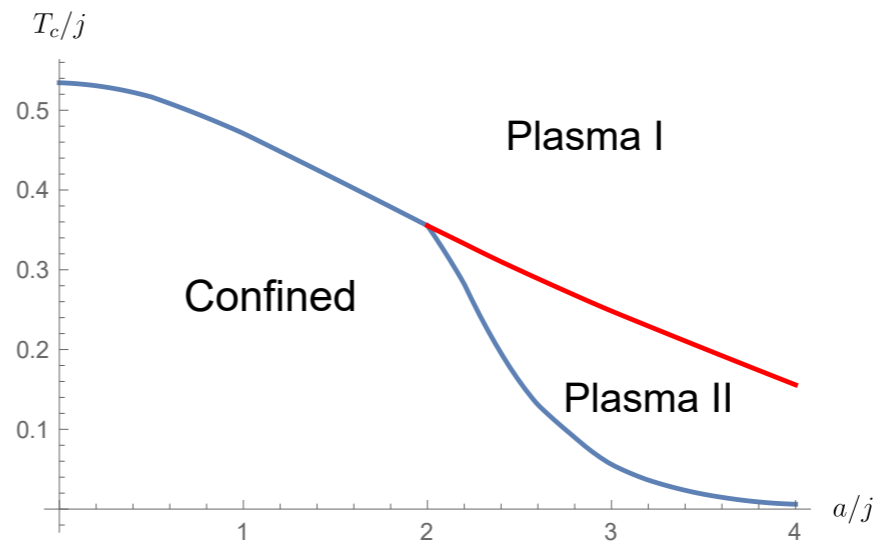
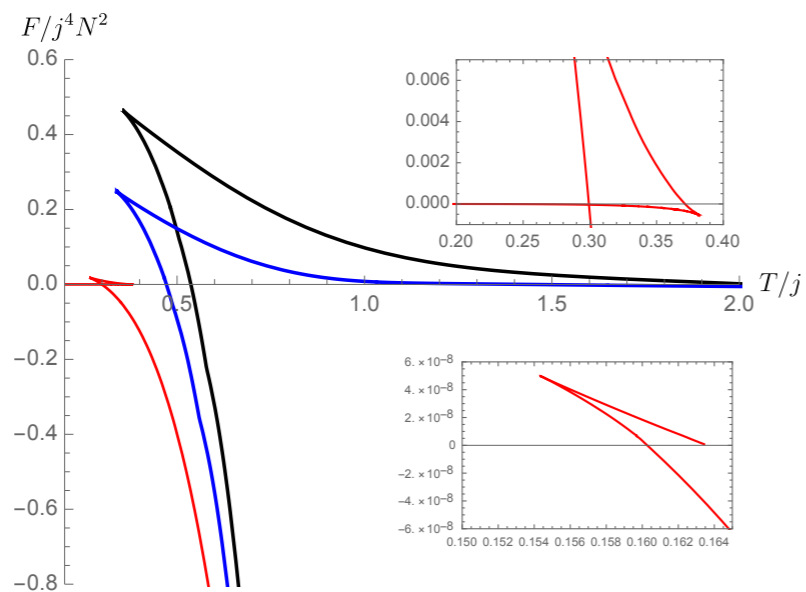
EoS, transport coefficients

Chiral condensate at finite μ



- μ decreases the condensate at fixed B
- B generically increases the condensate, except around T_c and for $\mu < 0.1$
- No T dependence in the confined phase, due to $1/N^2$ suppression

Thermodynamics of the anisotropic theory



- T_c decreases with anisotropy
- A new plasma phase and two phase boundaries

⇒ **inverse anisotropic catalysis?**

Holographic, anisotropic, non-conformal, neutral plasma

Giataganas, Pedraza, UG '17

Nonconformality \Leftrightarrow a scalar ϕ , anisotropy \Leftrightarrow another scalar χ

$$S = \frac{1}{2\kappa^2} \int d^5x \sqrt{-g} [R + \mathcal{L}_M],$$
$$\mathcal{L}_M = -\frac{1}{2}(\partial\phi)^2 + V(\phi) - \frac{1}{2}Z(\phi)(\partial\chi)^2,$$

$$V(\phi) = 12 \cosh(\sigma\phi) + b\phi^2, \quad Z(\phi) = e^{2\gamma\phi},$$

$$ds^2 = e^{2A(r)} \left[-f(r)dt^2 + d\vec{x}_\perp^2 + e^{2h(r)}dx_3^2 + \frac{dr^2}{f(r)} \right],$$
$$\phi = \phi(r), \quad \chi = a x_3. \quad \phi \rightarrow jr^{4-\Delta}$$

IR geometry is hyper scaling violating:

$$ds^2 = \tilde{L}^2(ar)^{2\theta/3z} \left[\frac{-dt^2 + d\vec{x}_\perp^2 + dr^2}{a^2r^2} + \frac{c_1 dx_3^2}{(ar)^{2/z}} \right],$$

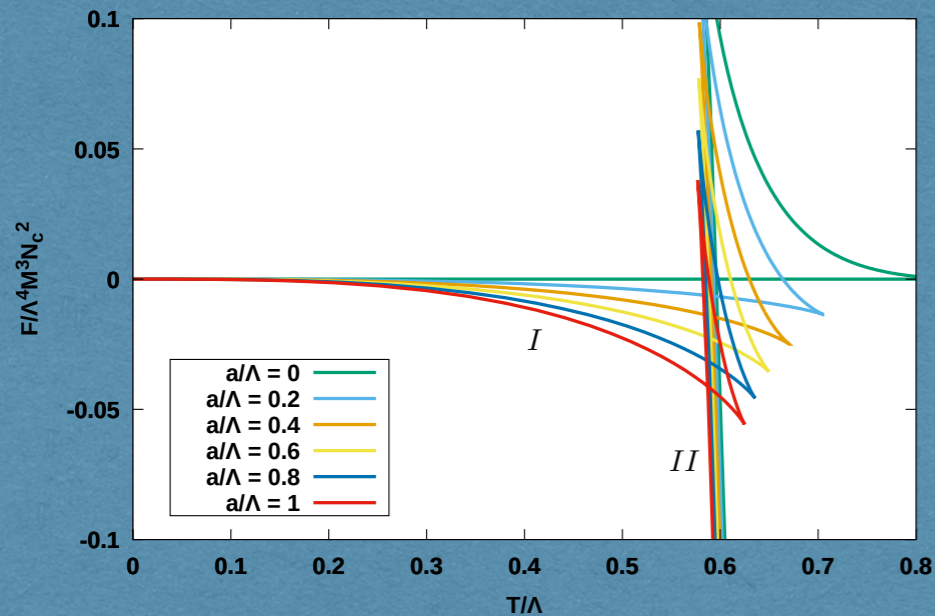
$$\phi = c_2 \log(ar) + \phi_0.$$

$$ds \rightarrow \lambda^{\theta/3z} ds.$$

$$t \rightarrow \lambda t, \quad \vec{x}_\perp \rightarrow \lambda \vec{x}_\perp, \quad r \rightarrow \lambda r, \quad x_3 \rightarrow \lambda^{\frac{1}{z}} x_3.$$

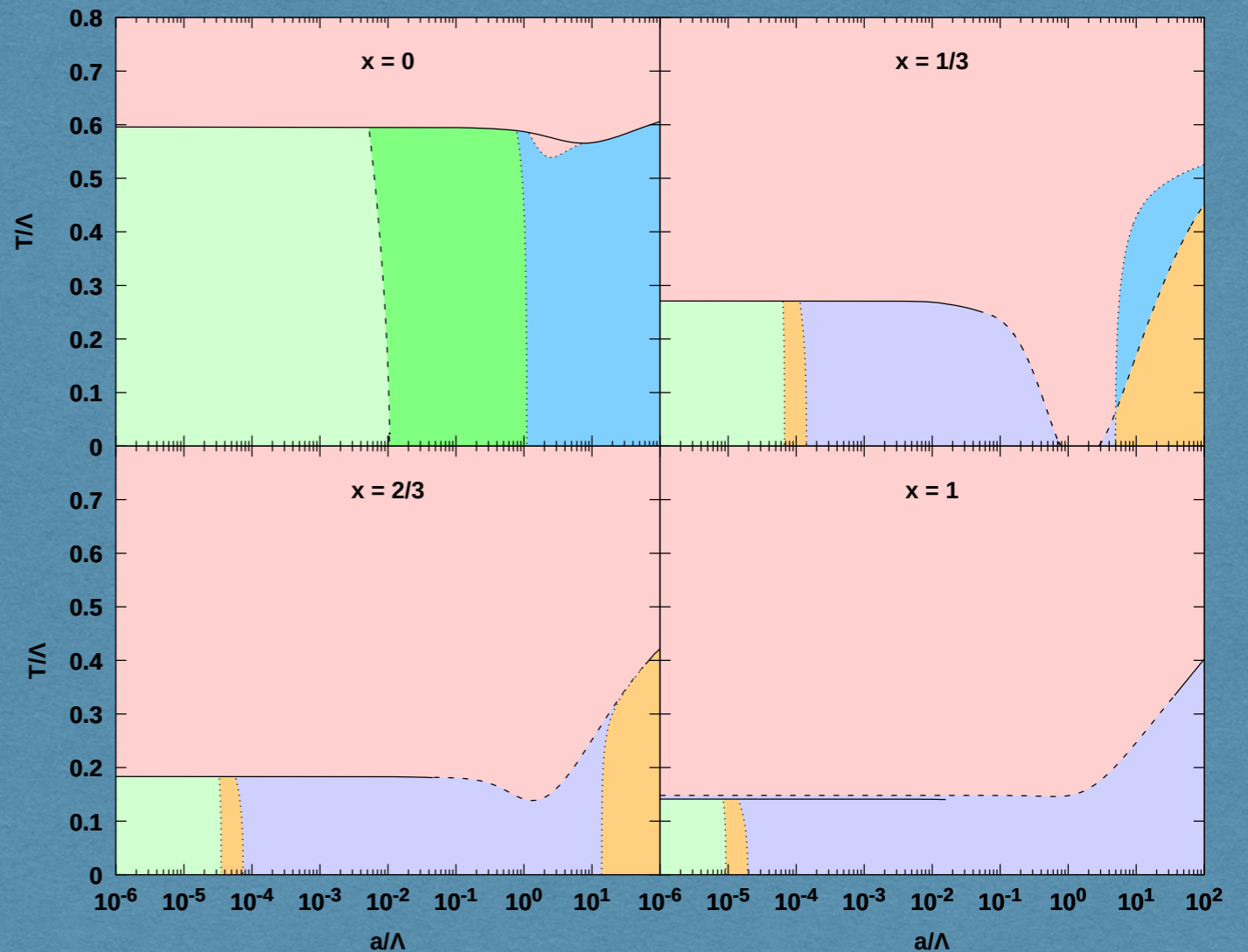
Thermodynamics

Jarvinen, Nijs, Pedraza, UG '18

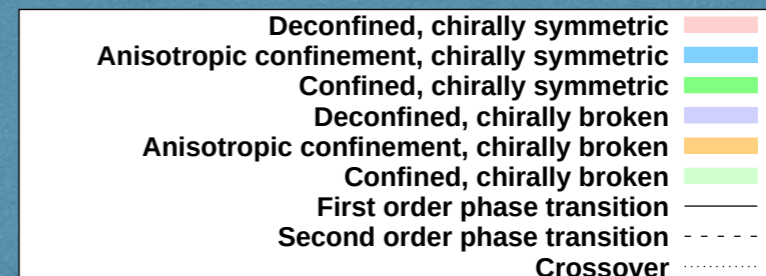


$x=0$

- $F \sim -T^4$ at large T ; $F \sim -T^3$ at small T
- Very different than $a=0$ case
- Black hole is “confining”



- T_x decreases with a generically
- Possibility of anisotropic confinement
- Quantum critical point for $x=1/3$
- Possibility of a confined chirally symmetric phase!?



Magnetic QCD

Anisotropy

B reduces original Lorentz : $SO(3, 1) \implies \underbrace{SO(1, 1)}_{\text{boost // B}} \times \underbrace{SO(2)}_{\text{rotation } \perp \text{ B}}$

propagators, transport coefficients decomposed using projectors

$$\Delta_{\mu\nu} = \eta_{\mu\nu} + u_\mu u_\nu - \frac{B_\mu B_\nu}{B^2} \quad \text{etc.}$$

Anisotropic confinement: $\sigma_\perp > \sigma_\parallel$ Bonati, D'Elia et al. '14

Chiral symmetry breaking

B reduces original chiral symmetry: u +2/3, d -1/3:

$$SU(N_u)_L \times SU(N_u)_R \times SU(N_d)_L \times SU(N_d)_R \times U(1)_{A-} \implies SU(N_u)_V \times SU(N_d)_V$$

IR effective theory: χ^{PT} of $N_u^2 + N_d^2 - 1$ NG bosons

Magnetic QCD

Fundamental scales at vanishing temperature and density

$1/\sqrt{eB}$	Magnetic screening length
$\Lambda_{QCD}(B)$	Confinement scale
$m_{dyn}(B)$	Dynamically generated quark mass

Separation of scales: $m_{dyn} \ll k \ll \sqrt{eB}$ χ SB
 $k \ll m_{dyn}$ confinement

Additional scales T, μ

$T \neq 0, \mu = 0$ pQCD + χ PT + lattice QCD

$T \neq 0, \mu \neq 0$ Holographic models

Various regimes

- I. $eB \gg \Lambda_{QCD}^2$ Perturbative QCD $\frac{1}{\alpha_s} \approx b \log \frac{|eB|}{\Lambda_{QCD}^2}$ Kabat, Lee, Weingerg '02
- II. $eB \approx \Lambda_{QCD}^2$ Lattice QCD, NJL effective theory, holography
- III. $eB \ll \Lambda_{QCD}^2$ Perturbative EM

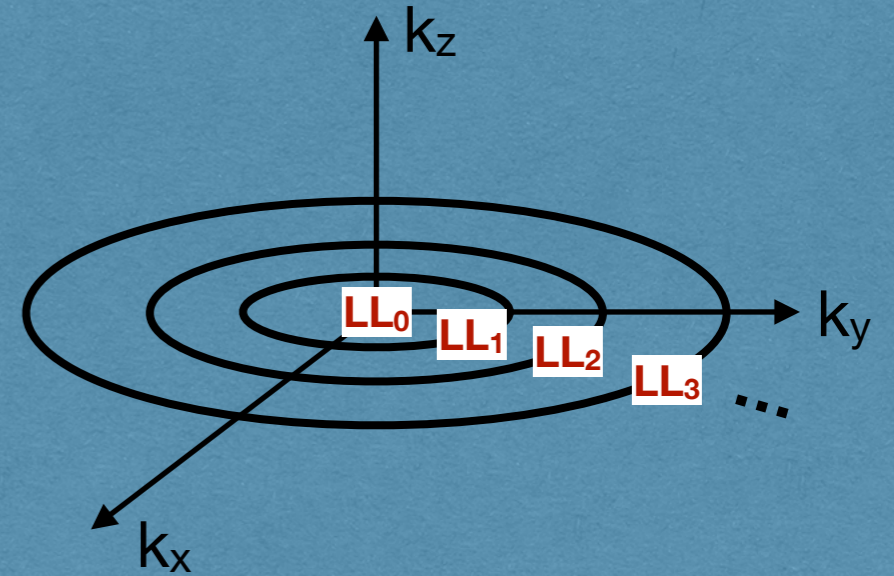
QCD in strong B (regime I)

Landau quantization

$$E_n(k_z) = \pm \sqrt{m^2 + 2|eB|n + k_z^2}$$

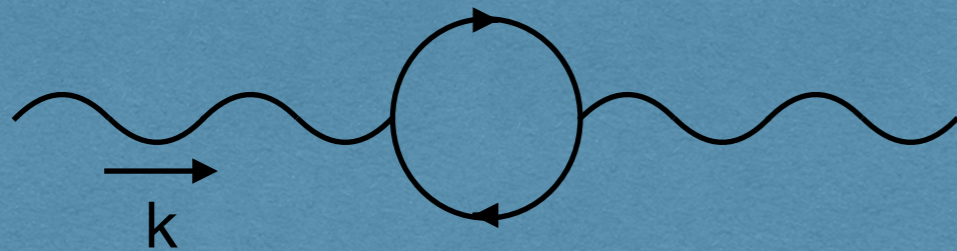
Dynamics effectively reduce 3+1 \rightarrow 1+1

Degeneracy of states $\sim |eB|$



Magnetic screening

Glueon polarisation at $|k|^2 \ll |eB|$ dominated by quarks at LL_0 over gluons and ghosts



$$M_g^2 \approx (2N_u + N_d) \frac{\alpha_s}{3\pi} |eB|$$

Color charge effectively screened in the regime

$$m_{dyn} \ll k \ll \sqrt{eB}$$

Magnetic catalysis in strong B

Three energy regimes

$$k \gg \sqrt{eB}$$

UV of QCD w/o B

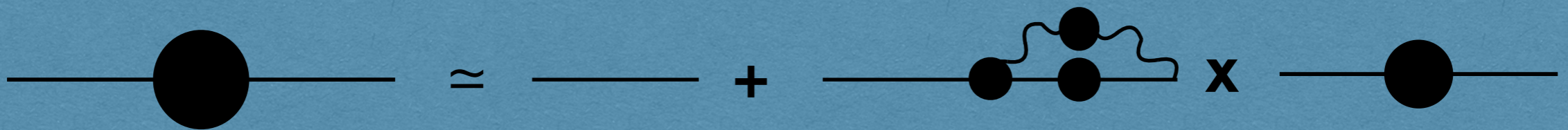
$$m_{dyn} \ll k \ll eB$$

Relevant for magnetic catalysis

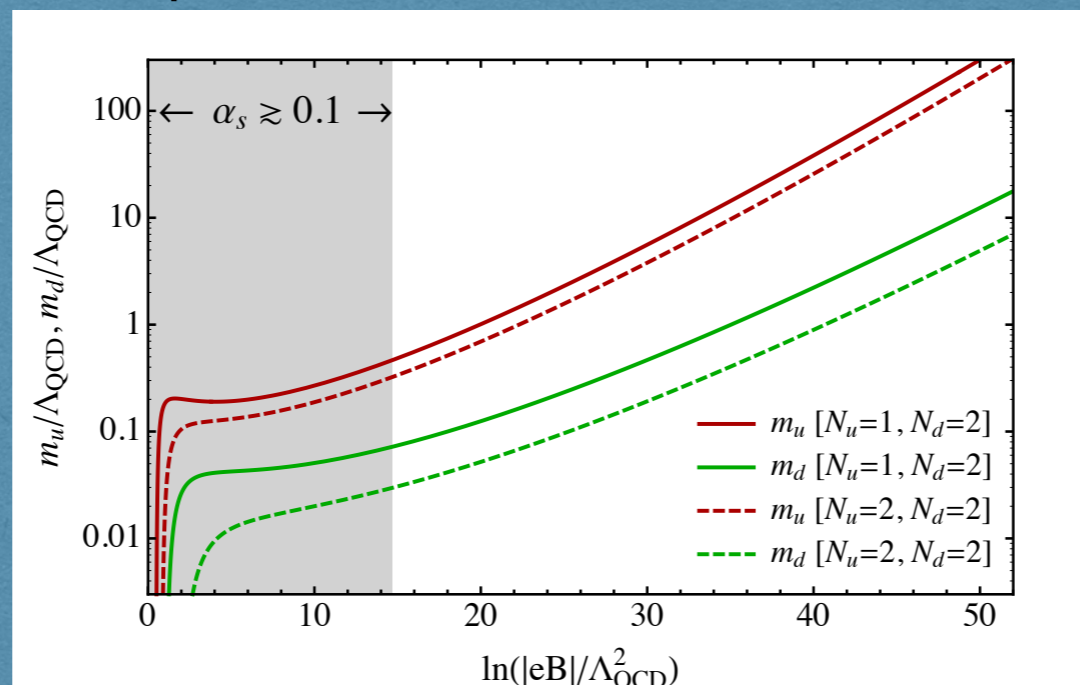
$$k \ll m_{dyn}$$

pure glue,
anisotropic confinement

- Regimes relevant for χ SB and confinement are separate at finite B!
- Solve the gap equation (improved rainbow approx) to obtain m_{dyn} at $eB \gg \Lambda_{QCD}^2$



Dynamically generated quark mass: [Miransky, Shovkovy '15](#)



Magnetic catalysis in strong B

Dynamically generated quark mass for $eB \gg \Lambda_{QCD}^2$

$$m_{dyn}^2 \approx 2|e_q B| (\bar{\alpha}_s)^{\frac{2}{3}} \exp \left[\frac{4N_c \pi}{\alpha_s (N_c^2 - 1) \log(\bar{\alpha}_s)} \right]$$

with $\bar{\alpha}_s = \alpha_s \frac{2N_u + N_d}{6\pi} \left| \frac{e}{e_q} \right|$ and $\frac{1}{\alpha_s} \approx \frac{11N_c - 2N_f}{12\pi} \log \frac{eB}{\Lambda_{QCD}^2}$

Remark I: Typically magnetic catalysis $m_{dyn} \propto eB$

But pQCD with resummation may exhibit inverse behaviour

Remark II: 't Hooft limit is trivial, need to take Veneziano limit:

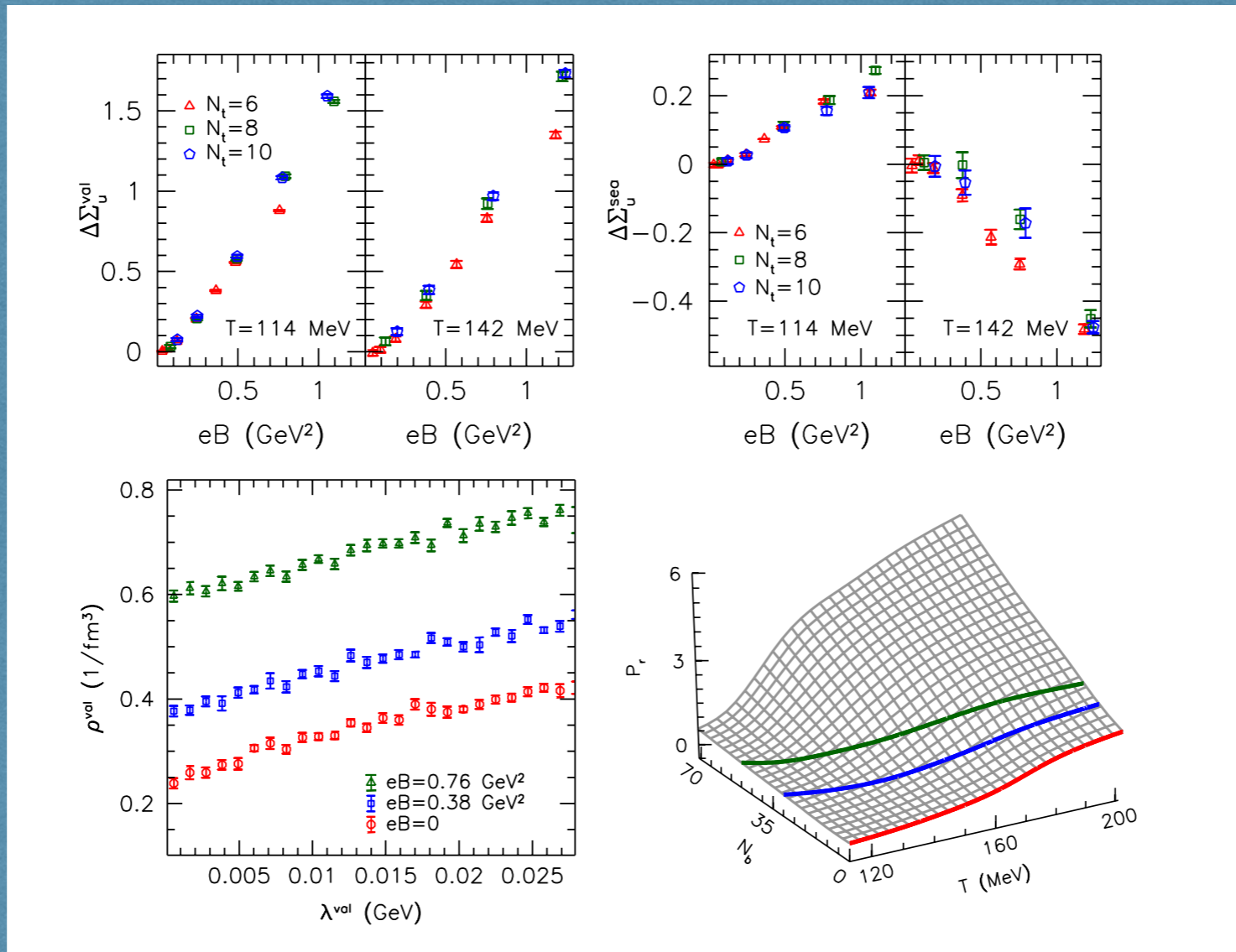
$$N_c, N_f \rightarrow \infty, \quad x = \frac{N_f}{N_c} = \text{const.}$$

Connection to Polyakov loop

- Testing the **valence** vs. **sea** idea: Bruckmann, Endrodi, Kovacs '13

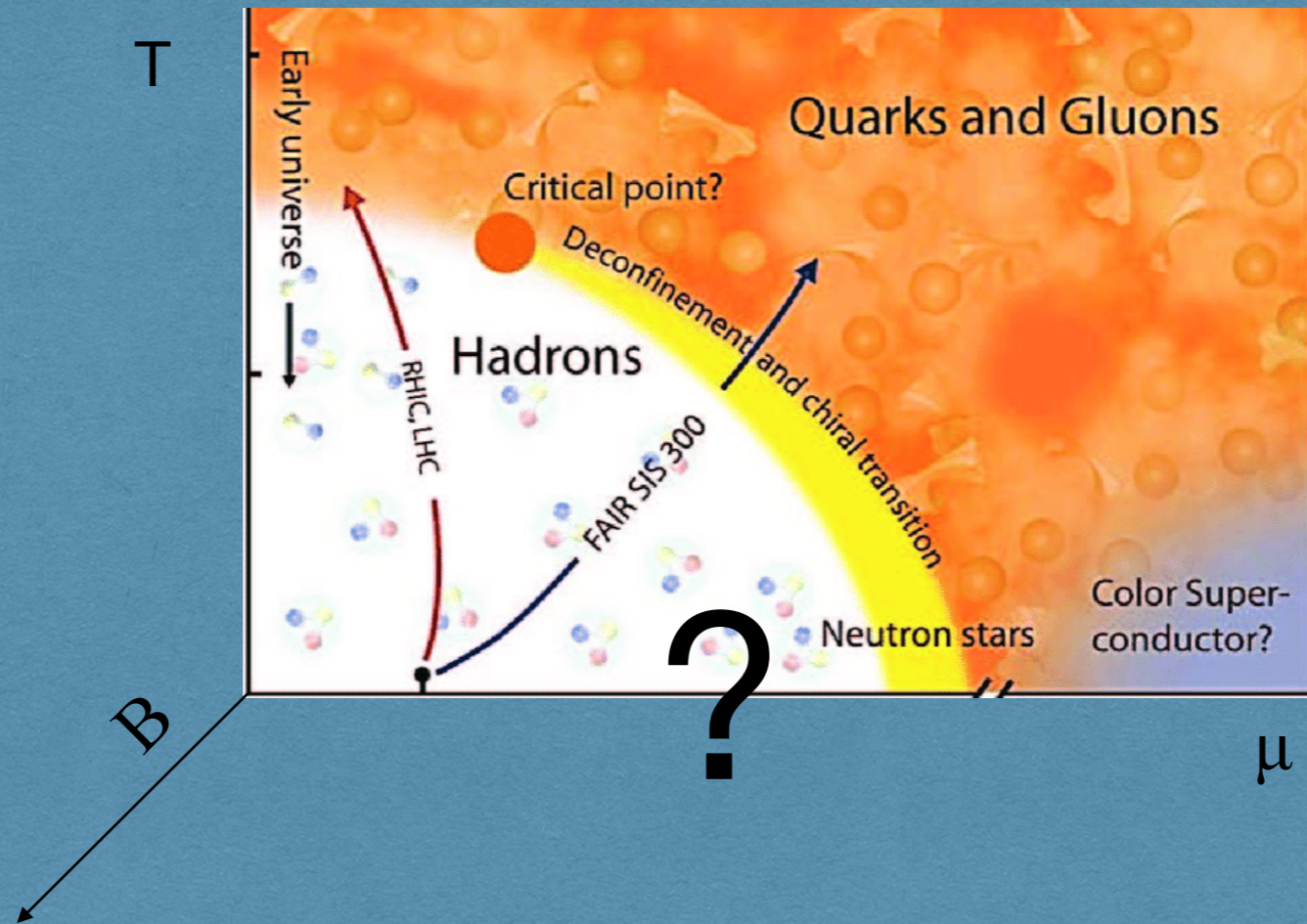
$$\bar{\psi}\psi^{\text{val}}(B) = \frac{1}{\mathcal{Z}(0)} \int \mathcal{D}U e^{-S_g} \det(\not{D}(0) + m) \text{Tr}(\not{D}(B) + m)^{-1},$$

$$\bar{\psi}\psi^{\text{sea}}(B) = \frac{1}{\mathcal{Z}(B)} \int \mathcal{D}U e^{-S_g} \det(\not{D}(B) + m) \text{Tr}(\not{D}(0) + m)^{-1}.$$



Finite density

Jarvinen, Nijs, UG '17



- New phases?
- **Magnetic catalysis at finite density?**
- **Urgent call:** upcoming RHIC isobar, FAIR, NICA experiments
- Lattice suffers from the **sign problem**

Inverse anisotropic catalysis

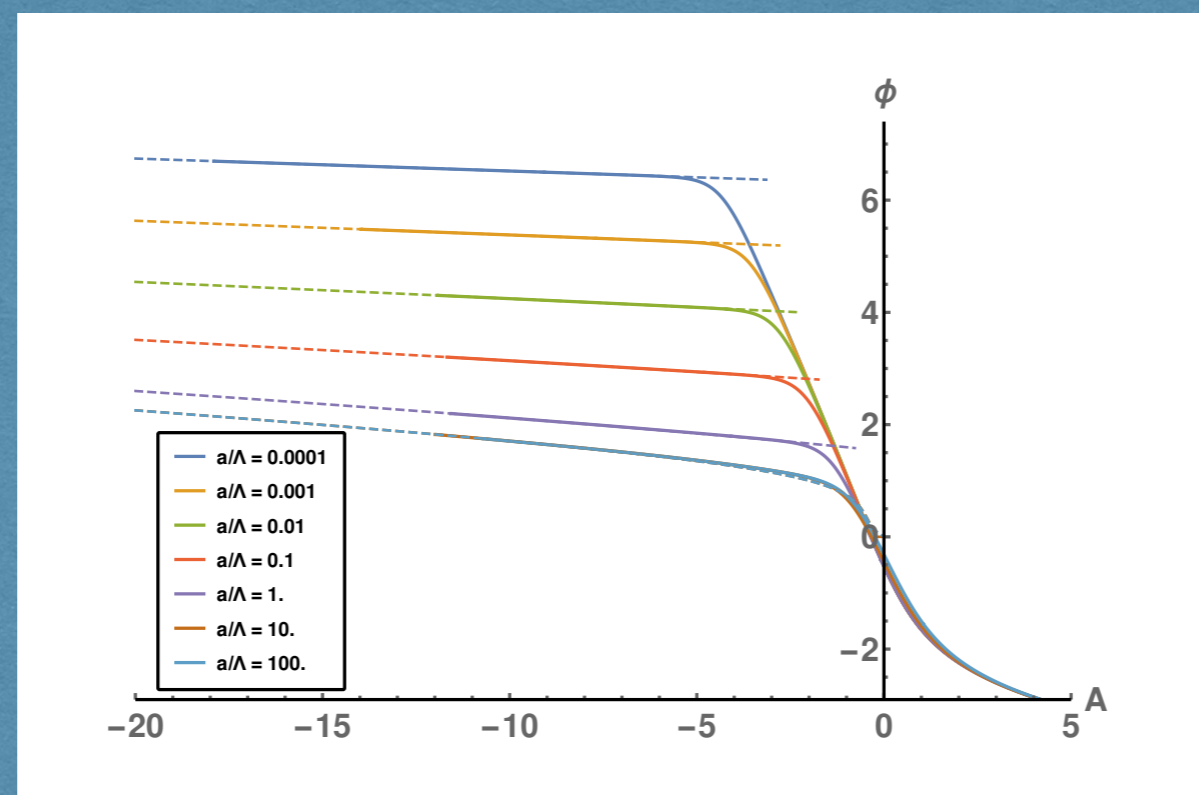
Jarvinen, Nijs, Pedraza, UG '18

Improved holographic QCD in the Veneziano limit with anisotropy

Same as before, with $\mu=0$, $B=0$ but $\theta=a z$ with

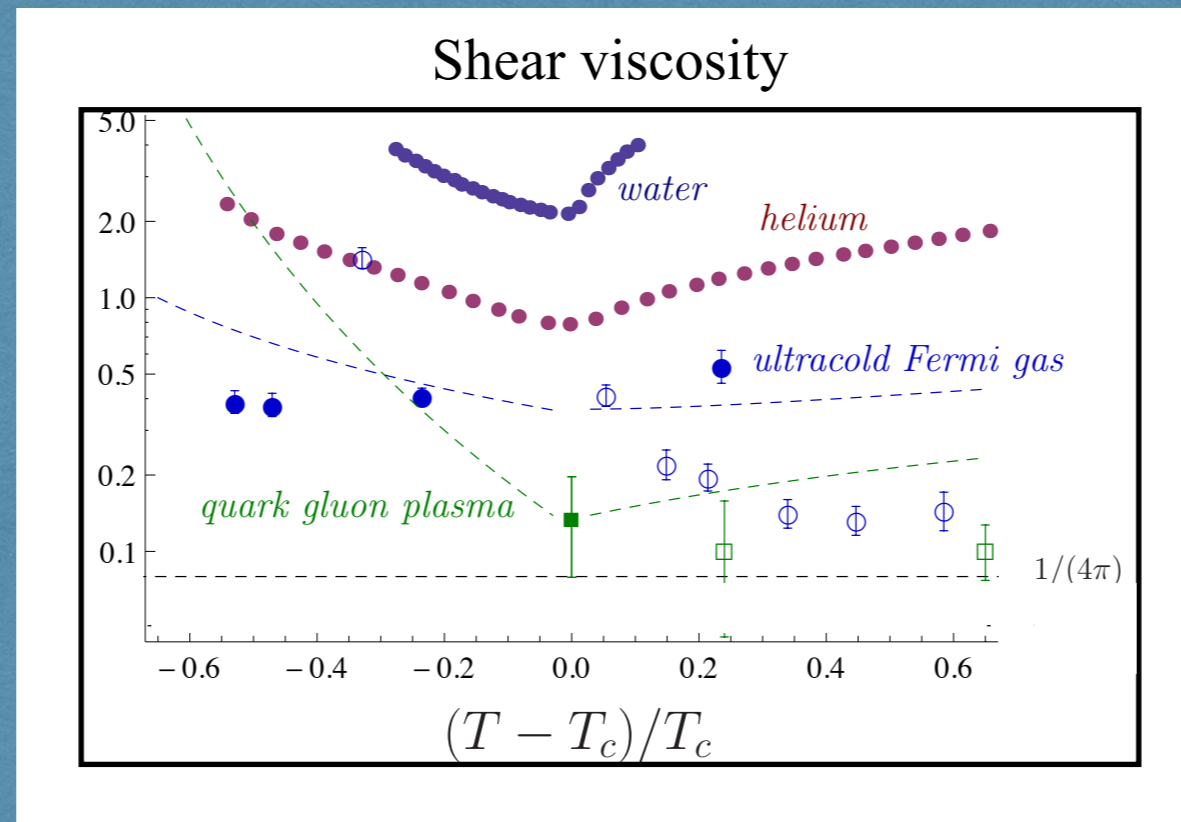
$$Z(\phi) = 1 + e^{4\phi}/10$$

IR geometry is “rolling” $\text{AdS}_4 \times \text{R}$: assuming broken chiral symmetry



Hydrodynamics in HEP??

One of the most universal theories in physics



Large (cosmic backgrounds, 10^9 ly) to small (quark gluon plasma $\sim 10^{-14}$ m)

Cold (Fermi gas, 10^{-8} K) to hot (quark gluon plasma $\sim 10^{12}$ K)

QGP is an almost ideal, highly magnetised fluid

Theory of slow variables

- Decompose $\varphi = \varphi_{UV} + \varphi_{IR}$, integrate out $\varphi_{UV} \Rightarrow$ Effective theory for φ_{IR}
- Local field theory $W[\varphi_{IR}]$ for $l_{mfp} \times \partial\varphi_{IR} = l_{mfp} \times L \ll 1$
- At thermal equilibrium, generic φ_{IR} decoheres in τ_{relax}

except **conserved quantities: charge, energy, momentum...**

